

(3) Prove or disprove: If $\{a_n\}_{n=1}^{\infty}$ diverges to $-\infty$ then $\{-a_n\}_{n=1}^{\infty}$ diverges to $+\infty$.

Assume that $\{a_n\}_{n=1}^{\infty}$ diverges to $-\infty$.
To show that $\{-a_n\}_{n=1}^{\infty}$ diverges to $+\infty$,
let $M \in \mathbb{R}$. By def. of diverges to $-\infty$,
there is some $N \in \mathbb{R}$ s.t. for all $n > N$
in \mathbb{N} , we have $-a_n < -M$. For such n ,
we have $a_n > M$. Thus, for the same
 N , we have $a_n > M$ for all $n > N$.
This means that $\{a_n\}_{n=1}^{\infty}$ diverges to $+\infty$.