

# WHAT TO KNOW FOR QUIZZES AND EXAMS

## DEFINITIONS

- (1) Rational number
- (2) Contrapositive
- (3) Converse
- (4) Irrational number
- (5) minimum / maximum
- (6) Upper bound / lower bound
- (7) Bounded above / bounded below
- (8) Supremum / infimum
- (9) Absolute value
- (10) (sequence) converges to  $L$
- (11) (sequence) is convergent
- (12) (sequence) is divergent
- (13) increasing / decreasing sequence
- (14) strictly increasing / decreasing sequence
- (15) monotone sequence
- (16) diverges to  $+\infty$  or  $-\infty$

## AXIOMS/THEOREMS

- (1) Well-ordering axiom
- (2) Completeness axiom
- (3) Theorem 5.3 (large natural numbers)
- (4) Archimedean principle
- (5) Density of rational numbers / irrational numbers
- (6) Triangle inequality
- (7) Theorem 10.2 (limits and algebra)
- (8) Squeeze Theorem
- (9) Monotone convergence theorem
- (10) Principle of induction

## KEY SKILLS

- (1) Proving “if-then” statements, “for every” statements, “there exists” statements, “is unique” statements
- (2) Proofs by contradiction
- (3) Finding the negation of a statement
- (4) Finding the contrapositive of a statement
- (5) Using examples to prove / disprove statements
- (6) Proving that a number is the supremum of a set
- (7) Proving that a sequence converges to some value using the definition
- (8) Algebra with limits of sequences: using these to determine if a sequence converges, and to what
- (9) Using squeeze theorem to show sequences converge
- (10) Relationship between boundedness, convergence, and monotonicity

## (11) Proofs by induction