

WHAT TO KNOW FOR QUIZZES AND EXAMS

DEFINITIONS

- (1) Rational number
- (2) Contrapositive
- (3) Converse
- (4) Irrational number
- (5) Upper bound / lower bound
- (6) Bounded above / bounded below
- (7) Supremum / infimum
- (8) Absolute value
- (9) (sequence) converges to L
- (10) (sequence) is convergent
- (11) (sequence) is divergent
- (12) increasing / decreasing sequence
- (13) strictly increasing / decreasing sequence
- (14) monotone sequence
- (15) diverges to ∞ or $-\infty$
- (16) Subsequence

AXIOMS/THEOREMS

- (1) Well-ordering axiom
- (2) Completeness axiom
- (3) Theorem 7.1 (large natural numbers)
- (4) Archimedean principle
- (5) Density of rational numbers/ irrational numbers
- (6) Triangle inequality
- (7) Theorem 12.2 (limits and algebra)
- (8) Squeeze Theorem
- (9) Monotone convergence theorem
- (10) Principle of induction
- (11) Theorem 18.6 (convergence and subsequences)
- (12) Theorem 19.2 (sequence with subsequences converging to every real number)
- (13) Cantor's Theorem
- (14) Bolzano-Weierstrass

KEY SKILLS

- (1) Proving “if-then” statements, “for every” statements, “there exists” statements, “is unique” statements
- (2) Proofs by contradiction
- (3) Finding the negation of a statement
- (4) Finding the contrapositive of a statement
- (5) Using examples to prove/disprove statements
- (6) Proving that a number is the supremum of a set
- (7) Proving that a sequence converges to some value using the definition

- (8) Algebra with limits of sequences: using these to determine if a sequence converges, and to what
- (9) Using squeeze theorem to show sequences converge
- (10) Relationship between boundedness, convergence, and monotonicity
- (11) Proofs by induction