Math 325. Quiz #5

(1) State the definition of a **strictly increasing** sequence.

(2) True or false, and justify with a short proof or example: If $\{a_n^2 - 3\}_{n=1}^{\infty}$ converges to 1 then $\{a_n\}_{n=1}^{\infty}$ converges to $2 (= \sqrt{1+3})$.

(3) True or false, and justify with a short proof or example: If $\{a_n\}_{n=1}^{\infty}$ is a divergent sequence, then $\left\{\frac{2}{5}a_n\right\}_{n=1}^{\infty}$ is also divergent.