Math 325. Group Quiz #10c

(1) State the Extreme Value Theorem.

(2) TRUE OR FALSE, and *justify* with a short proof: The function

$$f(x) = \begin{cases} x^2 - x & \text{if } x \ge 0\\ -x & \text{if } x < 0 \end{cases}$$

is differentiable at x = 0.

(3) True or false, and *justify* with a short proof or example: There is a continuous function $f:[1,3]\to\mathbb{R}$ with range $[1,3]\cup[5,7]$.