

WHAT TO KNOW FOR QUIZZES AND EXAMS

DEFINITIONS

- (1) Rational number
- (2) Contrapositive
- (3) Converse
- (4) Irrational number
- (5) minimum / maximum
- (6) Upper bound / lower bound
- (7) Bounded above / bounded below
- (8) Supremum
- (9) Absolute value
- (10) (sequence) converges to L
- (11) (sequence) is convergent
- (12) (sequence) is divergent
- (13) increasing / decreasing sequence
- (14) strictly increasing / decreasing sequence
- (15) monotone sequence
- (16) diverges to $+\infty$ or $-\infty$
- (17) Subsequence
- (18) Limit of a function
- (19) Continuous at a point

AXIOMS/THEOREMS

- (1) Well-ordering axiom
- (2) Completeness axiom
- (3) Archimedean principle
- (4) Density of rational numbers / irrational numbers
- (5) Triangle inequality
- (6) Theorem on limits and algebra for sequences
- (7) Squeeze Theorem
- (8) Monotone convergence theorem
- (9) Principle of induction
- (10) Theorem on convergence and subsequences
- (11) Cantor's Theorem
- (12) Bolzano-Weierstrass
- (13) Main corollary of Bolzano-Weierstrass
- (14) Theorem on limits and sequences
- (15) Theorem on limits of functions and algebra
- (16) Squeeze Theorem for functions
- (17) Theorem on continuity and limits
- (18) Theorem on continuity and algebra
- (19) Theorem on continuity and compositions

KEY SKILLS

- (1) Proving “if-then” statements, “for every” statements, “there exists” statements, “is unique” statements
- (2) Proofs by contradiction
- (3) Finding the negation of a statement
- (4) Finding the contrapositive of a statement
- (5) Using examples to prove / disprove statements
- (6) Proving that a number is the supremum of a set
- (7) Proving that a sequence converges to some value using the definition
- (8) Algebra with limits of sequences: using these to determine if a sequence converges, and to what
- (9) Using squeeze theorem to show sequences converge
- (10) Relationship between boundedness, convergence, and monotonicity
- (11) Proofs by induction
- (12) Relationship between convergence/boundedness of sequences and convergence of sub-sequences
- (13) Using the $\varepsilon - \delta$ definition to compute limits
- (14) Using algebra/squeeze theorem to compute limits
- (15) Using the $\varepsilon - \delta$ definition to show continuity
- (16) Using algebra/compositions to show continuity
- (17) Applying the $\varepsilon - \delta$ definitions of limits and continuity