

1a)

$$I(\lambda) = \frac{2hc^2\lambda^{-5}}{e^{\frac{hc}{\lambda k_B T}} - 1}$$

$$x = \frac{hc}{\lambda k_B T}$$

Substitute for $\lambda^{-5} = \frac{x^5 k_B^5 T^5}{h^5 c^5}$

$$I(x) = \frac{2hc^2 x^5 k_B^5 T^5}{(e^x - 1) h^4 c^3} = \frac{2x^5 k_B^5 T^5}{(e^x - 1) h^4 c^3}$$

$$\begin{aligned} \frac{dI(x)}{dx} &= \frac{2k_B^5 T^5}{h^4 c^3} \frac{d}{dx} \left[\frac{x^5}{e^x - 1} \right] \\ &= \frac{2k_B^5 T^5}{h^4 c^3} \left[-x^4 \frac{(x-5)e^x + 5}{(e^x - 1)^2} \right] \stackrel{\text{set}}{=} 0 \end{aligned}$$

$$\Rightarrow x = -6 \times 10^{-16} \text{ or } x = 4.96511$$

$$\lambda_{\max} = \frac{hc}{x k_B T} = \frac{hc}{4.97 k_B T} \Rightarrow \lambda_{\max} = \frac{b}{T}$$

where $b = \frac{hc}{k_B \cdot (4.97)}$

$x = 4.97$ is also the answer to the solution:

$$5e^{-x} + x - 5 = 0$$

4a) Current through R_3 into V_2 :

$$I_{R3} = \frac{V_2 - V_+}{R_3}$$

Current through R_4 to $0V$:

$$I_{R4} = \frac{V_2 - 0}{R_4} = \frac{V_2}{R_4}$$

Current through diode from $V_1 \rightarrow V_2$

$$I_D = I_0 (e^{(V_2 - V_1)/V_T} - 1)$$

We have $I_{R3} + I_{R4} + I_D = 0$

$$\text{So } \frac{V_2 - V_+}{R_3} + \frac{V_2}{R_4} + I_0 (e^{(V_2 - V_1)/V_T} - 1)$$