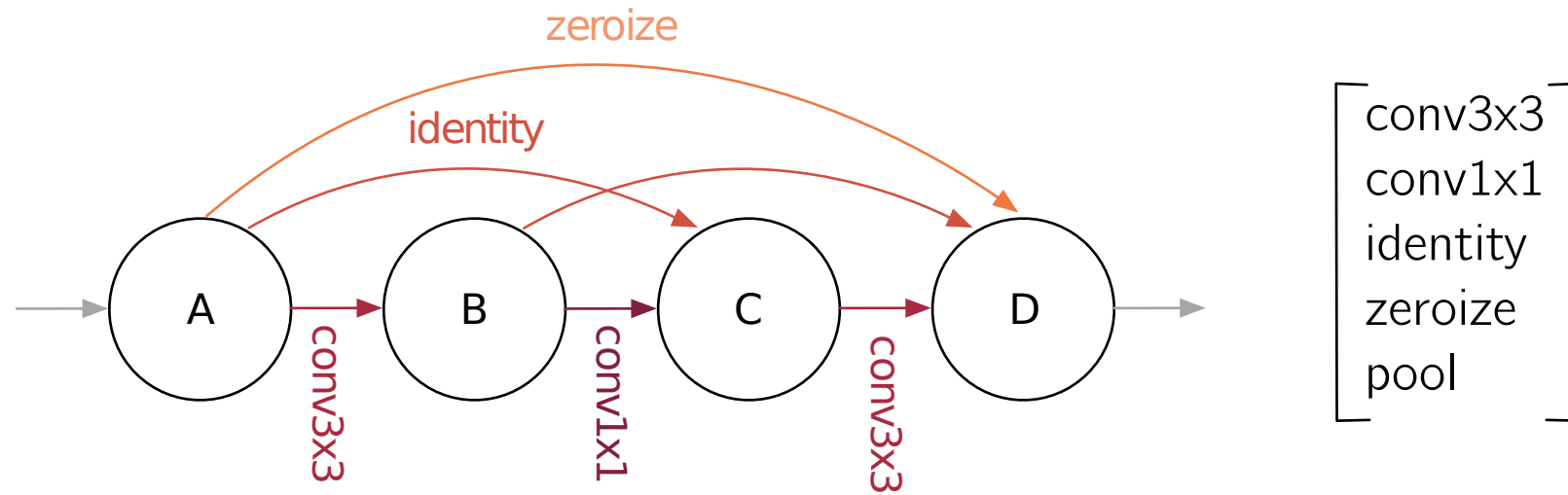
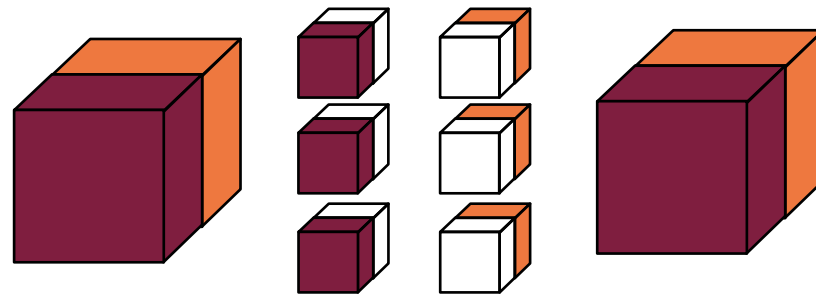


NAS is too coarse-grained



Grouped convolutions



Input

Weights

Output

[conv3x3
gconv(2)
gconv(4)
gconv(N)]

Convolution

```
for co in range(CO):           # out_channels
    for ci in range(CI):       # in_channels
        for oh in range(OH):   # out_height
            for ow in range(OW): # out_width
                for kh in range(KH): # kernel_height
                    for kw in range(KW): # kernel width
                        O[co][oh][ow] +=
                            I[ci][oh+kh][ow+kw] *
                            W[co][ci][kh][kw]
```

Convolution

```
for co in range(CO):
    for ci in range(CI):
        for oh in range(OH):
            for ow in range(OW):
                for kh in range(KH):
                    for kw in range(KW):
                        O[co][oh][ow] +=
                            I[ci][oh+kh][ow+kw] *
                            W[co][ci][kh][kw]
```

Group convolution

```
for g in range(G):
    for co in range(CO//G*g, CO//G*(g+1)):
        for ci in range(CI//G*g, CI//G*(g+1)):
            for oh in range(OH):
                for ow in range(OW):
                    for kh in range(KH):
                        for kw in range(KW):
                            O[co][oh][ow] +=
                                I[ci][oh+kh][ow+kw] *
                                W[co][ci][kh][kw]
```

Generalisation

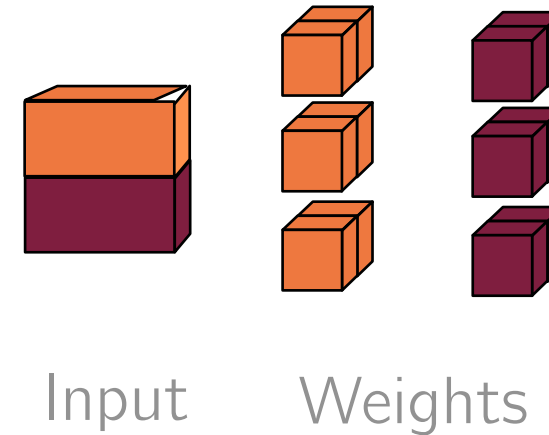
```
for i in range(I):  
    for j in range(J):  
        # do thing
```

$\xrightarrow{\text{group}(G)}$

```
for g in range(G):  
    for i in range(I//G*g, I//G*g+1):  
        for j in range(J//G*g, J//G*g+1):  
            # do thing
```

Example 1

```
for co in range(CO):      # out_channels
  for oh in range(OH):    # out_height
    for ci in range(CI):  # in_channels
      for ow in range(OW): # out_width
        for kh in range(KH): # kernel_height
          for kw in range(KW):
            O[co][oh][ow] +=
              I[ci][oh+kh][ow+kw] *
              W[co][ci][kh][kw]
```



Example 2

```
O[0][0][0] += I[0][0+0][0+0] *  
              W[0][0][0][0]
```

```
...
```

```
O[U][OH][OW] += I[CI][OH+KH][OW+KW] *  
                W[CO][CI][KH][KW]
```

```
for co in range(U, CO):  
    for ci in range(CI):  
        for oh in range(OH):  
            for ow in range(OW):  
                for kh in range(KH):  
                    for kw in range(KW):  
                        O[co][oh][ow] +=  
                            I[ci][oh+kh][ow+kw] *  
                            W[co][ci][kh][kw]
```

Example 2

```
O[0][0][0] += I[0][0+0][0+0] *  
              W[0][0][0][0]  
  
...  
O[U][OH][OW] += I[CI][OH+KH][OW+KW] *  
                W[CO][CI][KH][KW]  
  
for co in range(U, CO):  
    for ci in range(CI):  
        for oh in range(OH):  
            for ow in range(OW):  
                for kh in range(KH):  
                    for kw in range(KW):  
                        O[co][oh][ow] +=  
                            I[ci][oh+kh][ow+kw] *  
                            W[co][ci][kh][kw]
```

```
O[0][0][0] += I[0][0+0][0+0] *  
              W[0][0][0][0]  
  
...  
O[U][OH][OW] += I[CI][OH+KH][OW+KW] *  
                W[CO][CI][KH][KW]  
  
for g in range(G):  
    for co in range(U+CO//G*g, U+CO//G*(g+1)):  
        for ci in range(CI//G*g, CI//G*(g+1)):  
            for oh in range(OH):  
                for ow in range(OW):  
                    for kh in range(KH):  
                        for kw in range(KW):  
                            O[co][oh][ow] +=  
                                I[ci][oh+kh][ow+kw] *  
                                W[co][ci][kh][kw]
```