M 362K Pre-Class Work for 2/12

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3-10

$$E[W] = 0 * Pr(W = 0) + 1 * Pr(W = 1) + 2 * Pr(W = 2) = \frac{{}_{6}C_{1}*{}_{5}C_{1}}{{}_{11}C_{2}} + 2 * \frac{{}_{6}C_{2}}{{}_{11}C_{2}} = \frac{12}{11} \approx 1.09$$

$$E[W^{2}] = 0 * Pr(W = 0) + 1 * Pr(W = 1) + 2^{2} * Pr(W = 2) = \frac{{}_{6}C_{1}*{}_{5}C_{1}}{{}_{11}C_{2}} + 4 * \frac{{}_{6}C_{2}}{{}_{11}C_{2}} = \frac{18}{11} \approx 1.64$$

3-12

From the distribution given in the table, we get Pr(X=39)=1-0.16-0.42-0.1-0.28=0.04

Let E[X] denote the mean age

$$\therefore E[X] = 32 * 0.16 + 39 * 0.04 + 45 * 0.42 + 57 * 0.1 + 62 * 0.28 = 48.64$$

3-17

(a)

$$percentage = 100 * \frac{3}{4+1} = 60$$

(b)

let i be the i^{th} number

$$i = \frac{50}{100} * 5 = 2.5$$

let x_i be the value of the i^{th} number

$$x_{2.5} = 43412 + (45500 - 43412) * 0.5 = 44456$$

(c)

let i be the i^{th} number

$$\therefore \frac{2}{3} = \frac{i}{5}$$

$$i = \frac{10}{3}$$

let x_i be the value of the i^{th} number

$$x_{\frac{10}{3}} = 45500 + (53750 - 45500) * (\frac{10}{3} - 3) = 48250$$

(d)

let i be the rank of \$49,000

Then
$$45500 + (i - 3) * (53750 - 45500) = 49000$$

$$i = \frac{113}{33}$$

$$\therefore percentage = 100 * \frac{\frac{113}{33}}{5} \approx 68.48$$