Algorithm EE398000 hw01

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1. **Introduction:**

The analysis and comparisons of the four sorting algorithms: selection sort, insertion sort, bubble sort and shaker sort.

The goal of the algorithms is to sort a list of vocabulary into alphabetical order.

The input of the algorithms is a list of vocabulary, which is in a form of 2d array. The output of the algorithms is a list of sorted, alphabetically ordered vocabulary.

1. **Approach:**
2. Analysis:

Analysis of **Selection Sort**:

1. Intro: Find minimum value, put it in the front of array.
2. Space complexity:

Fixed part: int: (i, j, k, n), \*char: (tmp)

Variable part: \*char (A) x n

Total: n (\*char) + 4

1. Time complexity:

|  |  |  |  |
| --- | --- | --- | --- |
| Statement | s/e | Freq. | Total |
| 1. **Algorithm** SelectionSort(**A, n**) 2. { 3. **for** i := 1 **to** n **do** { 4. j := i; 5. **for** k := i+1 **to** n **do** { 6. **if** (A[k] < A[j]) then j = k 7. } 8. tmp = list[i];  list[i] = list[j];   list[j] = tmp; 9. } 10. } | 0  0  n+1  1  n+1  2 or 1  0  3  0  0 | 0  0  1  n  n  n(n+1)  0  n  0  0 | 0  0  n+1  n  n(n+1)  n(n)\*2or1  0  3n  0  0 |
| Total |  |  | 3n2 +4n+0 |

\*since aveg of i is n/2, I calculate T(P) with i = n/2.

Best case: 2n2 +4n+2 (O(n^2)).

Worst Case: 3n2 +4n+2 (O(n^2)).

Average Case: O(n^2).

**Therefore, the time complexity of Selection sort is O(n^2).**

Analysis of **Insertion Sort**:

1. Intro: Compare with the minimum value, if true, swap, put it in the front of array.
2. Space complexity:

Fixed part: int: (i, j, n), \*char: (tmp)

Variable part: \*char (A) x n

Total: n (\*char) + 3

1. Time complexity:

|  |  |  |  |
| --- | --- | --- | --- |
| Statement | s/e | Freq. | Total |
| 1. **Algorithm** InsertionSort(**A, n**) 2. { 3. **for** j := 2 **to** n **do** { 4. tmp := A[j]; 5. i := j - 1; 6. **while** ((i >= 1) **and** (tmp < A[i])) **do** { 7. A[i + 1] := A[i]; I := i-1; 8. } 9. A[i + 1] = tmp; 10. } 11. } | 0  0  n-1  1  1  n (\*)  2  0  1  0  0 | 0  0  1  n-2  n-2  n-2  (n-2)(c)n  (n-2)(c)n  n-2  0  0 | 0  0  n-2  n-2  n-2  n^2-2n  (2n-4)cn  0  n-2  0  0 |
| Total |  |  | (1+2c)n^2 |

\*Assume >=, <, and are all performed. (I recall that if i<1, computer won’t bother do the rest computation.)

Best case: if c = 0 or 1, it is mostly sorted, it won’t do anything. (O(1))

Worst case: if c ~= n, it is almost decreasing, it is ~ (1+2c)n^2.(O(n^2))

Average case: O(n^2) since most of the case require sorting.

**Therefore, the time complexity of Selection sort is O(n^2).**

Analysis of **Bubble Sort**:

1. Intro: Swap whenever it’s in the wrong order.
2. Space complexity:

Fixed part: int: (i, j, n), \*char: (tmp)

Variable part: \*char (A) x n

Total: n (\*char) + 3

1. Time complexity:

|  |  |  |  |
| --- | --- | --- | --- |
| Statement | s/e | Freq. | Total |
| 1. **Algorithm** BubbleSort(**A, n)** 2. { 3. **for** i := 1 **to** n - 1 **do** { 4. **for** j := n **to** i + 1 **step** -1 **do** { 5. **if** (A[j] < A[j – 1]) { 6. tmp = list[i];  list[i] = list[j];   list[j] = tmp; 7. } 8. } 9. } 10. } | 0  0  n  n  1  3  0  0  0  0 | 0  0  1  n-1  n-1  c(n-1)  0  0  0  0 | 0  0  n  n^2-n  n-1  3c(n-1)  0  0  0  0 |
| Total |  |  | n^2+… |

Best case: if c = 0 or 1, the 2nd iteration does nothing, then it is (O(n)).

Worst case: if c ~= n, it is almost decreasing, it is ~ n^2+…(O(n^2))

Average case: O(n^2) since most of the case require sorting.

**Therefore, the time complexity of Bubble sort is O(n^2).**

Analysis of **Shaker Sort**:

1. Intro: Swap whenever it’s in the wrong order but goes from both ends repeatedly.
2. Space complexity:

Fixed part: int: (i, j, l, r, n), \*char: (tmp)

Variable part: \*char (A) x n

Total: n (\*char) + 5

1. Time complexity:

|  |  |  |  |
| --- | --- | --- | --- |
| Statement | s/e | Freq. | Total |
| 1. **Algorithm** ShakerSort(**A, n)** 2. { 3. l := 1; r := n; 4. **while** l <= r **do** { 5. **for** j := r **to** l + 1 **step** -1 **do** { 6. **if** (A[j] < A[j – 1]) { 7. tmp = list[i];  list[i] = list[j];   list[j] = tmp; 8. } 9. } 10. l = l + 1; 11. **for** j := l **to** r - 1 **do** { 12. **if** (A[j] > A[j + 1]) { 13. tmp = list[i];  list[i] = list[j];   list[j] = tmp; 14. } 15. } 16. r := r – 1; 17. } 18. } | 0  0  2  n+1  n  c  3  0  0  1  n  c  3  0  0  1  0  0 | 0  0  1  1  n  n  n  n  n  n  n  n  n  n  n  n  0  0 | 0  0  2  n+1  n^2  cn  3n  0  0  1n  n^2  cn  3n  0  0  1n  0  0 |
| Total |  |  | 2n^2… |

Best case: if c = 0 or 1, 2nd iterations do nothing, then it is (O(n)).

Worst case: if c ~= 1/2n, it is almost decreasing, it is(O(n^2)).

Average case: O(n^2) since most of the case require sorting, but it goes 2 times slower than bubble sort.

**Therefore, the time complexity of Shaker sort is O(n^2).**

**Comparing Table:**

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  | Selection | Insertion | Bubble | Shaker |
| Space | n (\*char) + 4 | n (\*char) + 3 | n (\*char) + 3 | n (\*char) + 5 |
| Time | **O(n^2)** | **O(n^2)** | **O(n^2)** | **O(n^2)** |

Prediction: Shaker > Bubble ? Insertion > Selection

The reason of Insertion > Selection is because the comparing step is lesser in Insertion sort. Shaker sort reduce the swapping steps by comparing from 2 ends.

The speed of the algorithms depends on whether writing data(swapping) or going through more steps is faster. Based on my learning in Computer Architecture, writing data is way slower.

Therefore, **my prediction is: Insertion > Selection > Shaker > Bubble**.

1. Implementation: (hw01.c on NTHUEE workstation, gcc 4.1.2)
2. Result:
3. Result Table:

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| N | Selection | Insertion | Bubble | Shaker |
| 10 | 9.90E-07 | 7.30E-07 | 1.11E-06 | 1.12E-06 |
| 20 | 6.79E-06 | 5.09E-06 | 1.00E-05 | 9.99E-06 |
| 40 | 2.33E-05 | 1.44E-05 | 3.96E-05 | 4.04E-05 |
| 80 | 8.60E-05 | 5.27E-05 | 1.64E-04 | 1.64E-04 |
| 160 | 1.33E-04 | 7.21E-05 | 2.77E-04 | 2.65E-04 |
| 320 | 1.14E-03 | 3.03E-04 | 1.13E-03 | 1.07E-03 |
| 640 | 2.76E-03 | 1.24E-03 | 4.81E-03 | 4.39E-03 |
| 1280 | 9.75E-03 | 5.32E-03 | 2.06E-02 | 1.87E-02 |
| 2560 | 3.58E-02 | 2.31E-02 | 8.74E-02 | 8.21E-02 |

1. Observation:

* N vs CPU time chart:

**Speed: Insertion > Selection > Shaker > Bubble**.

It seems that the result meets by prediction. Furthermore, the time complexities of the four algorithms are O(n^2), same as those that I’ve calculated.

* Log(N) vs log(CPU time) chart:

When y-axis is logged, the graph looks linear. It indicates that they are O(n^2).

Logged x-axis is just for good spacing between different Ns.

\*The N=10 & N=40 case’s bubble sort is faster than shaker sort. They might just be the special case when N is small.

1. Conclusion:
2. Experimented Speed: **Insertion > Selection > Shaker > Bubble**.
3. Time Complexity: **Insertion = Selection = Shaker = Bubble = O(n^2)**.
4. Best Case: **Insertion > Shaker = Bubble > Selection.**
5. Space Complexity: **Insertion = Selection = Shaker = Bubble = theta(1)**
6. **Swapping (data writing) is much slower than comparing.**