

Data Structure Midterm Examination
3:30pm-5:20pm (110 minutes), April. 17, 2017

#: _____ Student ID: _____ Name: _____

- ✧ 看清題目再作答。
- ✧ 中英文、鉛筆原子筆作答都可以。
- ✧ Please answer **questions 1 - 5 on the question sheet**. For other questions, please answer on the answer sheet in any order you want.
- ✧ There are 9 questions. You can obtain up to 114 points.

1. **(12pt)** Please analyze the **time complexity** of the following algorithms

```
for (int i=0; i<N; i++)
  for (int j=0; j<i*i; j++)
    for (int k=1; k<j; k=k*2)
      print("Hello");
```

$\Omega(\quad)$

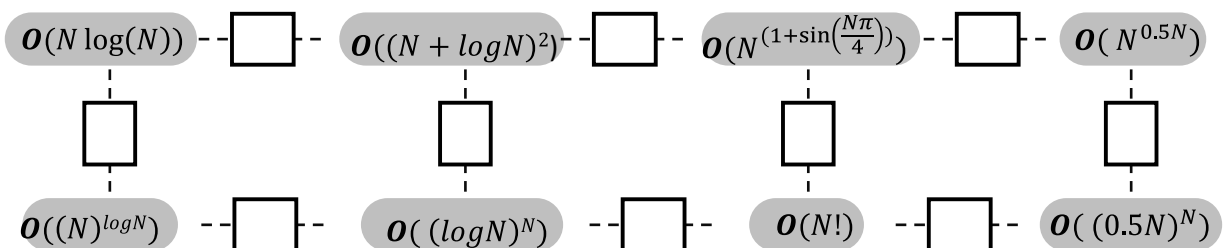
$O(\quad)$

```
x = 2; y = 2;
while (x<N) {
  j = random 0 or 1;
  if (j == 0 && y<x) {
    y=y+1;
  }else{
    x=x*x;
  }
}
```

$\Omega(\quad)$

$O(\quad)$

2. **(15pt)** Please fill out the boxes with "=", "<", or ">" to show the asymptotic complexity hierarchy. For example, $O(n^2) < O(n^3) = O(n^3/10)$.

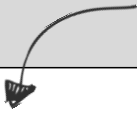


3. **(12pt)** Please complete the following **recursive function** that **recursively divides an array into two halves** (i.e., 遞迴二分法) to find the maximum value in the array.

Please also show the **time complexity** using 1) a recursive definition and 2) a closed-form θ notation.

```
int RMAX(int array[], int size)
{
    int m;
    
    return m;
}
```

your code goes here



(1) $T(\text{size}) =$

(2)

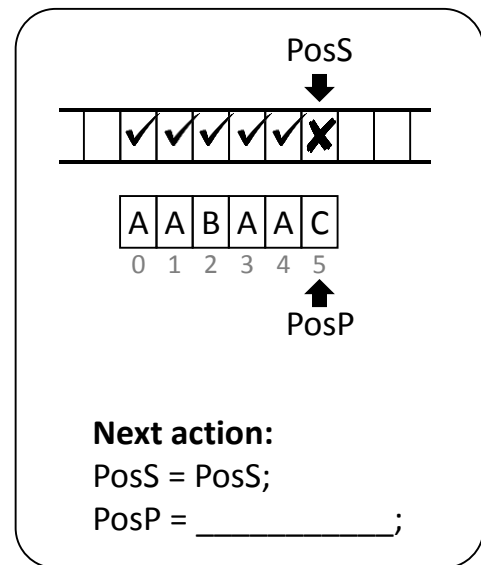
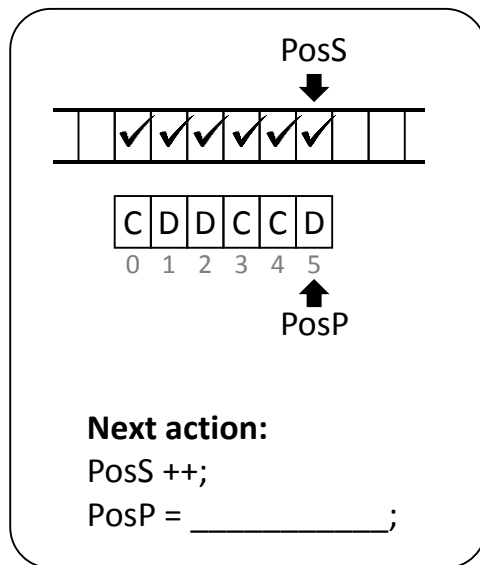
→ $T(\text{size}) = \theta(\text{_____})$

4. KMP algorithm

- (1) **(7pt)** Please show the 0-based failure function of the following patterns.

S	D	T	D	S	S	D	T	D	S	S	x
0											_____ if $x == \text{'D'}$ _____ if $x == \text{'S'}$ _____ if $x == \text{'T'}$ _____ otherwise

- (2) **(8pt)** What is the next PosP index (0~5)? A check mark (✓) stands for a match, and a cross mark stands for a mismatch.



5. **(12pt)** Please convert $A || (A + B * C \% 9) < D == T \&\& B$ into a postfix expression.

Only the four boxes with thick borders will be graded (只有粗黑框格子计分).

bottom				
Token	Stack	Output So Far	Priority	Operator
A (A + B * C % 9) < D == T && B			High	In-coming (
				*, /, %
				+, -
				<, <=, >=, >
				==, !=
				&&
			Low	
				In-stack (

----- 以下請於答案卷作答 Answer the following questions on the answer sheet -----

6. (12pt) Asymptotic notations

$$(F(N) + G(N)) = O(N!) \Rightarrow (F(N) \times G(N)) = O((2N)!)$$

- (1) (4pt) Is the above statement **true or false**?
- (2) (8pt) Please prove your answer **according to the definition of Big-O**.

Hint: $\frac{x+y}{2} \geq \sqrt{xy}$

7.

- (1) (4pt) What are the three basic structures of **structured programming**?
- (2) (4pt) To solve a problem, a structured program can always achieve **the same or better speed** than a non-structured program can. Is this statement **true or false**? Please briefly explain.
- (3) (4pt) Can the access levels of object members affect the function of a program? Why don't we always use *public*?

8. (12pt) We want to design a data structure to store an lower-triangular matrix (LTM). The following figure shows a 3x3 LTM example.

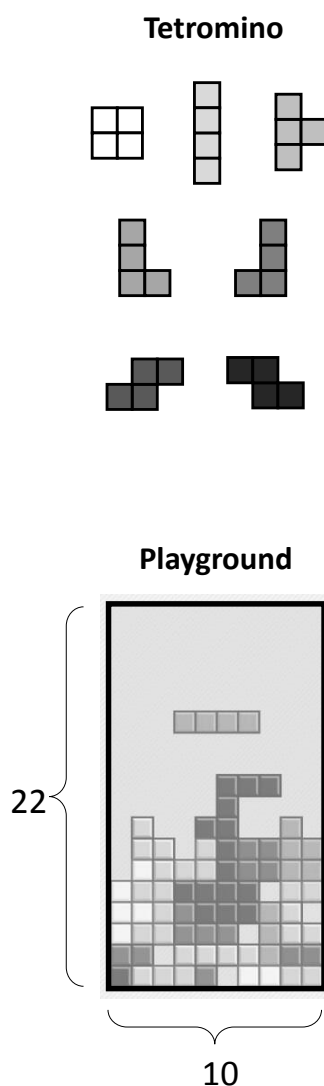
$$\begin{bmatrix} T_{00} & 0 & 0 \\ T_{10} & T_{11} & 0 \\ T_{20} & T_{21} & T_{22} \end{bmatrix}$$

T_{00}	T_{10}	T_{11}	T_{20}	T_{21}	T_{22}
0	1	2	3	4	5

- (1) (4pt) How many integers are exactly needed for an NxN LTM if only the triangular part is stored in a 1-D array, row by row, as shown above?
- (2) (4pt) Following the above question, let $f(i, j)$ be the array index of term T_{ij} . Please show $f(i, j)$.
- (3) (4pt) Let R be the probability that $T_{ij} = 0$. If a data structure treats a LTM as a **sparse matrix** and stores only non-zero terms, how many integers are exactly needed for an NxN LTM?

9. **(12pt)** Please design a simple Tetris (俄羅斯方塊) game. The skeleton code is shown below. **Make reasonable assumptions and simplification** yourself if appropriate. Please write C/C++ style pseudo code and focus on the following two functions.

- (1) **(6pt) Tetromino::tryMove()** which tries to move the incoming tetromino piece, updates the tetromino's (x, y) coordinates, and returns whether the movement is successful.
- (2) **(6pt) Playground::tryClearLines()** which calculates how many horizontal lines on the playground are full, clears full lines, and moves other lines downward.



```
class Playground;

class Tetromino{
friend class Playground;
    Tetromino();
    void reset(); // reset x, and y. randomize type.
    int tryMove(int direction, const Playground & pg);
                // 0: cannot move, 1: successfully move
private:
    int type;    // 1~7 for the seven types
    int x, y;    // Tetromino's position in the playground
    int score;
};

class Playgrond{
friend class Tetromino;
    Playground();
    void fix(const Tetromino & t); // fix the tetromino
    int tryClearLines();
    void draw(const Tetromino & curr_tetromino);
    void addScore(int s);
private:
    int grid[10][22]; // 0 for empty. 1~7 for tetrominos
};

int main()
{
    Tetromino t;
    Playground pg;
    While(1){
        int k = GetKey(); // LEFT, RIGHT, DOWN, or NONE
        if(k == NONE) { k = DOWN; }
        if(k == DOWN && t.tryMove(k, pg) == 0) {
            pg.fix(t);
            pg.addScore(pg.tryClearLines());
            t.reset();
        }else{
            pg.draw(t);
        }
        sleep(0.5); // sleep 0.5 second
    }
}
```