

5. Find the limit if it exists, $\lim_{(x,y) \rightarrow (0,0)} \frac{x^2 y}{x^4 + y^2}$

6. Is the function $f(x,y)$ continuous at $(0,0)$, if $f(x,y) =$
$$\begin{cases} 0. & \text{for } (x,y) = (0,0) \\ \sqrt{x^2 + y^2} \ln(\sqrt{x^2 + y^2}). & \text{for } (x,y) \neq (0,0) \end{cases}$$

Prove your answer.

7. Given $f(x,y) = \cos(x^2 + xy)$, find the

$$\lim_{h \rightarrow 0} \frac{f\left(\frac{\sqrt{\pi}}{2}, h\right) - f\left(\frac{\sqrt{\pi}}{2}, 0\right)}{h}.$$

8. Let $f(x,y) = \ln(x^2 + y^2)$

- (a) Find differential df and
- (b) Find the linearly approximation to $f(x,y)$ at the point $(1,1)$.
- (c) Use (b), to approximate $f(1.01, 0.98)$
(Hint: $\ln 2 = 0.693$)

9. Find $\frac{dy}{dx}$ if $x^3 - 4xy + 2y^2 = 3$.

10. Find $\frac{\partial w}{\partial r}$ and $\frac{\partial w}{\partial s}$ if $w = e^{(x^2y+xy^2)}$
and $x = sr$ and $y = 2s+3r$ if $r = 1$,
 $s = -1$.