

# Digital System Design Lab

## Lab 6

### Realization of a Boolean Function

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## **1. Objectives**

- To learn how to generate waveform in Quartus II

## **2. Theorem**

The Boolean algebra is a fundamental concept in digital logic and computer science, used for the manipulation and analysis of binary variables. In Boolean algebra, Boolean expressions can be represented using two standard forms: minterms and maxterms.

### **(1) Minterm**

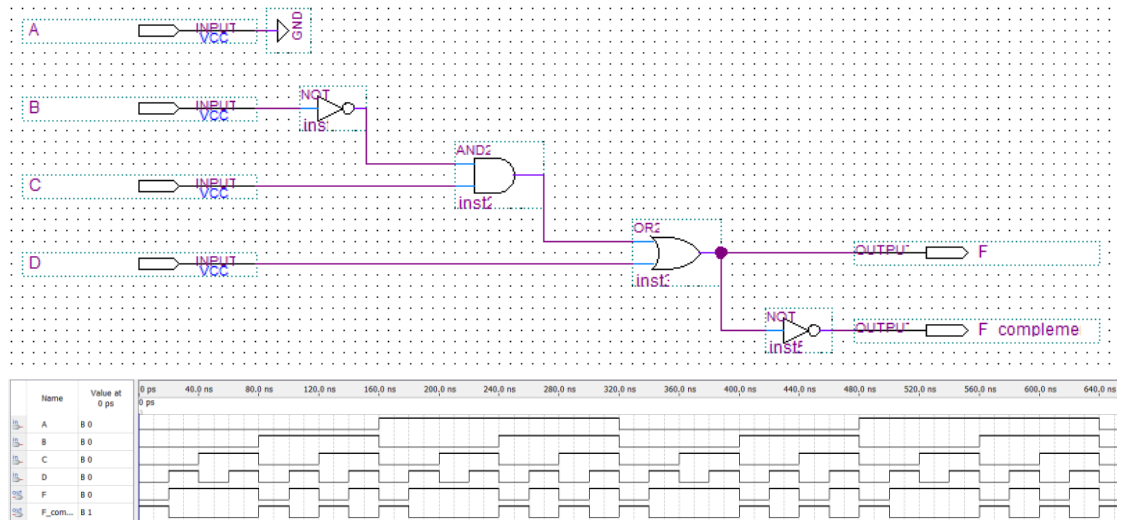
Minterms are the logical product (AND operation) of the input variables, where each term represents a specific combination of the variables that make the Boolean expression true. They are also known as the product terms and are characterized by their full disjunctive normal form.

### **(2) Maxterm**

Maxterms are the logical sum (OR operation) of the input variables, where each term represents a specific combination of the variables that make the Boolean expression false. Maxterms are the dual of minterms and are characterized by their full conjunctive normal form.

### 3. Experimental Results

#### (1) Step 1



A	B	C	D	F(A, B, C, D)
0	0	0	0	0
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	0
1	1	1	1	1

a. *Minterm:*

$$\begin{aligned} F &= A'B'C'D + A'B'CD' + A'B'CD + A'BC'D + A'BCD + AB'C'D + \\ &\quad AB'CD' + AB'CD + ABC'D + ABCD \\ &= B'C'D + B'CD' + B'CD + BC'D + BCD \\ &= B'C + D(B'C' + B'C + BC + BC') \\ &= B'C + D \end{aligned}$$

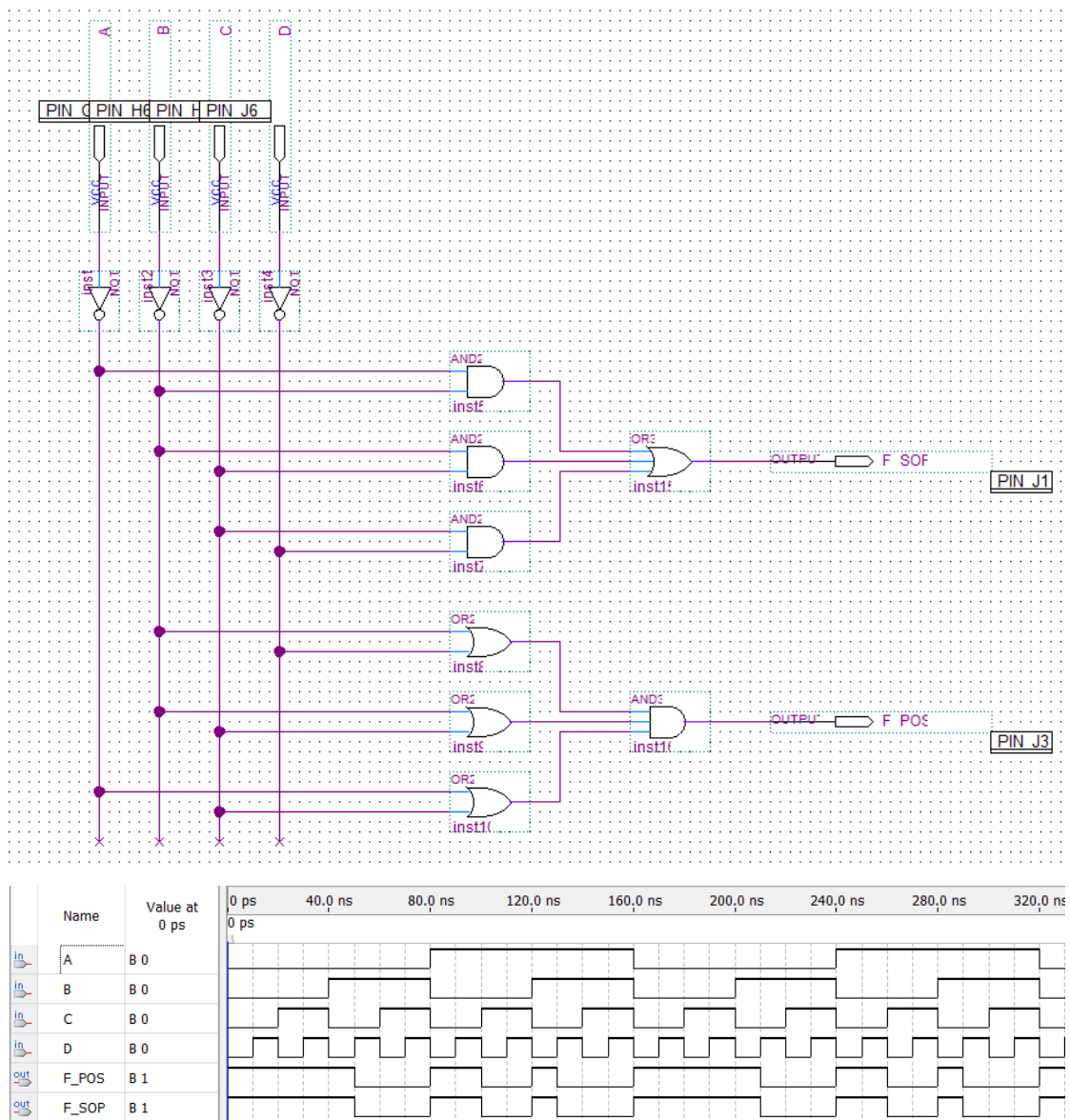
b. *Maxterm:*

$$\begin{aligned} F &= (A+B+C+D) \cdot (A+B'+C+D) \cdot (A+B'+C'+D) \cdot (A'+B+C+D) \cdot \\ &\quad (A'+B'+C+D) \cdot (A'+B'+C'+D) \\ &= (B+C+D+BC+BD+CD) \cdot (B'+C+D+B'C+B'D+CD) \cdot \\ &\quad (B'+C'+D+B'C'+B'D+C'D) \\ &= (C+D)(B'+C'+D) \\ &= B'C + B'D + CC' + C'D + CD + DD \\ &= B'C + D \end{aligned}$$

c. *Simplify*

$$\begin{aligned} F &= A'D + BD + B'C + AB'D \\ &= D(AB' + A') + BD + B'C \\ &= D(A' + B') + BD + B'C \\ &= B'D + A'D + BD + B'C \\ &= D(B + B') + A'D + B'C \\ &= D(1 + A') + B'C \\ &= D + B'C \end{aligned}$$

## (2) Step 2



## 4. Comments

None

## 5. Problems & Solutions

When I tried to use input, I made a mistake—bind each input to a gnd. Because of it, it made my program ruined and can't be compiled. At the end, I removed the gnds and reconnected wires, and it works!

## 6. Feedback

None