Feng Chia University 110-1 Class Purdue I Calculus HW TWO (due by 10/19)

Name:_____ SID:

1. What value of k makes the function

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$$f(x) = \begin{cases} \frac{x^2 + x - 6}{x^2 - 9}, & , x \neq -3 \\ k, & , x = -3 \end{cases}$$
continuous at $x = -3$.

2. Evaluate the limit $\lim_{x \to -\infty} \frac{2|x^3| + 5}{5 - 3x^3}$

3. Evaluate $\lim_{h \to 0} \frac{\sqrt[3]{27 + h} - 3}{h}$

4. Evaluate $\lim_{x \to 1} \frac{x^{2023} - 1}{x - 1}$

- 5. Find the derivative of $f(x) = 5x^3 - 3x^2 + 2x - 7$
- 6. Find the equation of tangent line to the graph of $f(x) = x^3 - 2x + 1$ at a=0.

7.	Find the horizontal asymptote(s)	to
	$f(x) = \frac{2 x -3}{x+5}.$	

8. Find the horizontal asymptote(s) to
$$f(x) = \frac{2x+3}{\sqrt{5x^2+7}}.$$

9. Find
$$f'(x)$$
, $f''(x)$, and $f'''(x)$ of $f(x)$

$$f(x) = 5x^4 - 4x^3 + 3x^2 - 2x + 7$$

10. Prove that $f(x) = x^4 + x - 3$ has a root on the interval (1, 2)