

Feng Chia University 110-1 Class Purdue I Calculus HW ONE (due by 9/29)

Name : _____ SID : _____

1. Find the domain of the function

$$f(x) = \frac{\sqrt{16 - x^2}}{x^2 - 2x - 3}$$

2. Find the domain of

$$f(x) = \frac{x^2 + 1}{x^2 - 2x - 15}$$

3. Find the value of $\lim_{x \rightarrow 0} \frac{\tan 5x}{\sin 3x}$.

4. Find the value of $\lim_{x \rightarrow 0} \frac{\sin 7x}{\sin 3x}$.

5. Find the limit $\lim_{x \rightarrow 2} \frac{x^2 + x - 6}{|x - 2|}$

6. Find the limit $\lim_{x \rightarrow \infty} x \sin\left(\frac{1}{x}\right)$

7. Evaluate $\lim_{x \rightarrow 1} \frac{x^2 - 1}{x^2 + 4x - 5}$

8. Evaluate $\lim_{x \rightarrow 0} \frac{x}{\sqrt{x+4} - 2}$

9. Find the limits $\lim_{x \rightarrow 2^+} f(x)$, $\lim_{x \rightarrow 2^-} f(x)$

and $\lim_{x \rightarrow 2} f(x)$ if

$$f(x) = \begin{cases} \frac{x^2 - 2x - 8}{x + 2}, & , x \leq 2 \\ 3x - 2 & , x > 2 \end{cases}$$

10. Evaluate the limit $\lim_{x \rightarrow \infty} \frac{2x^2 + 7x - 6}{5 - 4x + 3x^2}$

11. Find the vertical asymptote(s) of the function $f(x) = \frac{x^2 + 2x - 1}{x^2 - 25}$.

12. Show that $\lim_{x \rightarrow 0} |x| \sin(x) = 0$