

## Programming Assignment 3: Binary Adder-Subtractor

Write a C program to simulate the combinational logic design of a 32-bit binary adder-subtractor. A 32-bit binary adder-subtractor is a logic circuit of 32 one-bit full adders. When adding/subtracting two 32-bit integers,  $S=X+Y$  or  $S=X-Y$ , an additional bit  $M$  is used to indicate addition or subtraction operation. If the operator is "+",  $M$  is set to 0; if the operator is "-",  $M$  is set to 1. The initial carry-in bit  $c_{in}$  is set to  $M$ . A full adder takes  $x_i$ ,  $y_i$ , and  $c_{in}$  as input and produces  $s_i$  and  $c_{out}$ , where  $x_i$  and  $s_i$  are the  $i$ -th bit of  $X$  and  $S$ , respectively,  $y_i$  is  $y_i \oplus M$ . The carry-out bit  $c_{out}$  of the  $i$ -th full adder becomes  $c_{in}$  of the  $(i+1)$ -st full adder. The logic formula of a full adder is defined as below:

$$s_i = (x_i \oplus y_i) \oplus c_{in}$$
$$c_{out} = (x_i \wedge y_i) \vee (c_{in} \wedge (x_i \oplus y_i))$$

Refer to Digital System Design Lecture 12, Combinational Logic Design Binary Adder-Subtractor (binary\_adder\_subtractor.pdf) for more details of the logic design of binary adder-subtractor. The program will repeatedly input two 32-bit integers  $X$  and  $Y$ , and use a binary adder-subtractor to compute  $S=X+Y$  or  $S=X-Y$ , until both  $X$  and  $Y$  are 0's. **Do not** use addition/subtraction operation in C programming language. The output will print  $X$ ,  $Y$ , and  $S$  in both decimal and binary format. Also, print a message to confirm that the binary adder-subtractor has the same result as the addition/subtraction operation of C programming language. If the addition/subtraction results in the overflow situation, print an overflow message. Repeat the program until both  $X$  and  $Y$  are 0. (Hint: Use "scanf("%d %c %d", &X, &op, &Y);" to enter expression " $X + Y$ " or " $X - Y$ ".)

Write comments in your program solution. Also, write a report to explain how you develop your assignment solution, in particular, how to produce pretty printing of the quadratic equation and solution. Homework assignment 3 is due by **23:59 pm, Sunday, October 29**. Use **assgn3\_DXXXXXXX.c** for your source code file and **assgn3\_DXXXXXXX.pdf** for your report. where DXXXXXXX is your student ID. Submit the source code and the report to **iLearn**.

Example of program execution (next page):

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D:\>binary_adder_subtractor
Enter "X + Y" or "X - Y" (X, Y: -2,147,483,648 to 2,147,483,647): 28 + 45
X = 28      Binary value: 0000 0000 0000 0000 0000 0000 0001 1100
Y = 45      Binary value: 0000 0000 0000 0000 0000 0000 0010 1101
S = 73      Binary value: 0000 0000 0000 0000 0000 0000 0100 1001
Correct! Adder-subtractor operation test: 28 + 45 = 73
-----
Enter "X + Y" or "X - Y" (X, Y: -2,147,483,648 to 2,147,483,647): 28 - 45
X = 28      Binary value: 0000 0000 0000 0000 0000 0000 0001 1100
Y = 45      Binary value: 0000 0000 0000 0000 0000 0000 0010 1101
S = -17     Binary value: 1111 1111 1111 1111 1111 1111 1110 1111
Correct! Adder-subtractor operation test: 28 - 45 = -17
-----
Enter "X + Y" or "X - Y" (X, Y: -2,147,483,648 to 2,147,483,647): 28 + -45
X = 28      Binary value: 0000 0000 0000 0000 0000 0000 0001 1100
Y = -45     Binary value: 1111 1111 1111 1111 1111 1111 1101 0011
S = -17     Binary value: 1111 1111 1111 1111 1111 1111 1110 1111
Correct! Adder-subtractor operation test: 28 + -45 = -17
-----
Enter "X + Y" or "X - Y" (X, Y: -2,147,483,648 to 2,147,483,647): -28 + 45
X = -28     Binary value: 1111 1111 1111 1111 1111 1111 1110 0100
Y = 45      Binary value: 0000 0000 0000 0000 0000 0000 0010 1101
S = 17      Binary value: 0000 0000 0000 0000 0000 0000 0000 0001
Correct! Adder-subtractor operation test: -28 + 45 = 17
-----
Enter "X + Y" or "X - Y" (X, Y: -2,147,483,648 to 2,147,483,647): -28 - 45
X = -28     Binary value: 1111 1111 1111 1111 1111 1111 1110 0100
Y = 45      Binary value: 0000 0000 0000 0000 0000 0000 0010 1101
S = -73     Binary value: 1111 1111 1111 1111 1111 1111 1011 0111
Correct! Adder-subtractor operation test: -28 - 45 = -73
-----
Enter "X + Y" or "X - Y" (X, Y: -2,147,483,648 to 2,147,483,647): -28 - -45
X = -28     Binary value: 1111 1111 1111 1111 1111 1111 1110 0100
Y = -45     Binary value: 1111 1111 1111 1111 1111 1111 1101 0011
S = 17      Binary value: 0000 0000 0000 0000 0000 0000 0001 0001
Correct! Adder-subtractor operation test: -28 - -45 = 17
-----
Enter "X + Y" or "X - Y" (X, Y: -2,147,483,648 to 2,147,483,647): 45 - 28
X = 45      Binary value: 0000 0000 0000 0000 0000 0000 0010 1101
Y = 28      Binary value: 0000 0000 0000 0000 0000 0000 0001 1100
S = 17      Binary value: 0000 0000 0000 0000 0000 0000 0000 0001
Correct! Adder-subtractor operation test: 45 - 28 = 17
-----
Enter "X + Y" or "X - Y" (X, Y: -2,147,483,648 to 2,147,483,647): 45 - -28
X = 45      Binary value: 0000 0000 0000 0000 0000 0000 0010 1101
Y = -28     Binary value: 1111 1111 1111 1111 1111 1111 1110 0100
S = 73      Binary value: 0000 0000 0000 0000 0000 0000 0100 1001
Correct! Adder-subtractor operation test: 45 - -28 = 73
-----
Enter "X + Y" or "X - Y" (X, Y: -2,147,483,648 to 2,147,483,647): 1000000000 + 1000000000
X = 1000000000 Binary value: 0011 1011 1001 1010 1100 1010 0000 0000
Y = 1000000000 Binary value: 0011 1011 1001 1010 1100 1010 0000 0000
S = 2000000000 Binary value: 0111 0111 0011 0101 1001 0100 0000 0000
Correct! Adder-subtractor operation test: 1000000000 + 1000000000 = 2000000000
-----
Enter "X + Y" or "X - Y" (X, Y: -2,147,483,648 to 2,147,483,647): 1000000000 - 2000000000
X = 1000000000 Binary value: 0011 1011 1001 1010 1100 1010 0000 0000
Y = 2000000000 Binary value: 0111 0111 0011 0101 1001 0100 0000 0000
S = -1000000000 Binary value: 1100 0100 0110 0101 0011 0110 0000 0000
Correct! Adder-subtractor operation test: 1000000000 - 2000000000 = -1000000000
-----
Enter "X + Y" or "X - Y" (X, Y: -2,147,483,648 to 2,147,483,647): 1000000000 + 2000000000
X = 1000000000 Binary value: 0011 1011 1001 1010 1100 1010 0000 0000
Y = 2000000000 Binary value: 0111 0111 0011 0101 1001 0100 0000 0000
S = -1294967296 Binary value: 1011 0010 1101 0000 0101 1110 0000 0000
Correct! Adder-subtractor operation test: 1000000000 + 2000000000 = -1294967296
**** The addition-subtraction operation is overflow.
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Enter "X + Y" or "X - Y" (X, Y: -2,147,483,648 to 2,147,483,647): -1000000000 - 2000000000
X = -1000000000 Binary value: 1100 0100 0110 0101 0011 0110 0000 0000
Y = 2000000000 Binary value: 0111 0111 0011 0101 1001 0100 0000 0000
S = 1294967296 Binary value: 0100 1101 0010 1111 1010 0010 0000 0000
Correct! Adder-subtractor operation test: -1000000000 - 2000000000 = 1294967296
**** The addition-subtraction operation is overflow.
-----
Enter "X + Y" or "X - Y" (X, Y: -2,147,483,648 to 2,147,483,647): 0 + 0
微軟注音 半 ;
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