

% 7.1 EXAMPLE: NEWTON'S METHOD AGAIN

% Use the Editor to create and save (in the current MATLAB directory) the function
% file f.m as follows:

```
function y = f(x)
y = x^3 + x - 3;
```

%-----

% Then create and save another function file df.m:

```
function y = df(x)
y = 3*x^2 + 1;
```

%-----

% Now write a separate script file, newtgen.m (in the same directory), which will
% stop either when the relative error in x is less than 10^{-8} , or after 20 steps, say:

% Newton's method in general
% excludes zero roots!

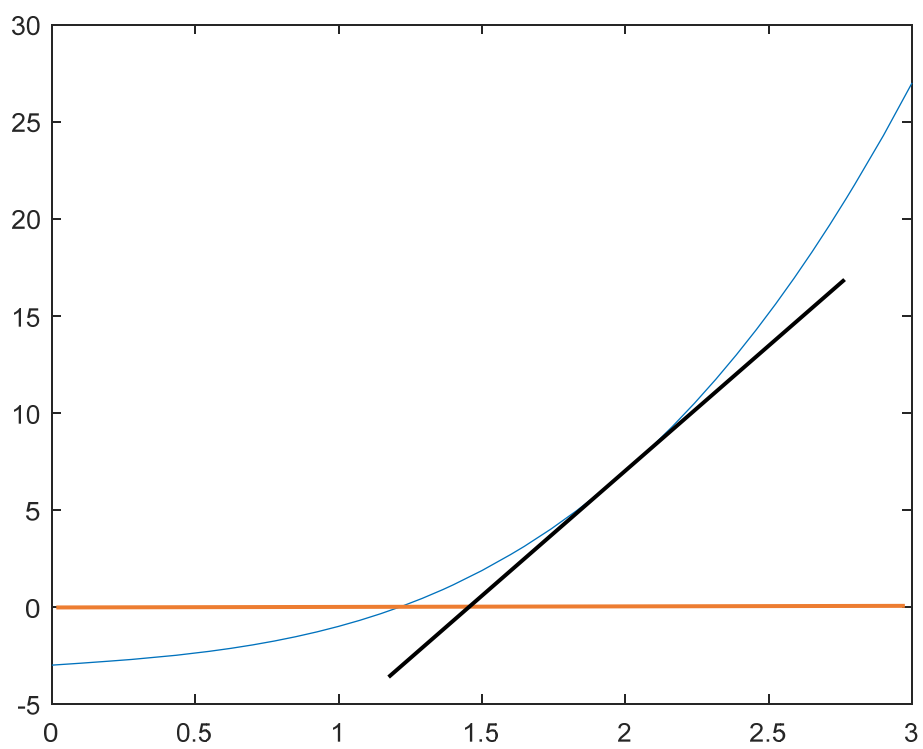
```
steps = 0; % iteration counter
x = input( 'Initial guess: '); % estimate of root
re = 1e-8; % required relative error
myrel = 1;
while myrel > re & (steps < 20)
    xold = x;
    x = x - f(x)/df(x);
    steps = steps + 1;
    disp( [x f(x)] )
    myrel = abs((x-xold)/x);
end
if myrel <= re
    disp( 'Zero found at' )
    disp( x )
else
    disp( 'Zero NOT found')
end
%=====
=====
```

%% To rewrite newton's method in book 7.1 by using (for & if break)

Ans:

```
% excludes zero roots!
```

```
steps = 0; % iteration counter
x = input( 'Initial guess: '); % estimate of root
re = 1e-8; % required relative error
myrel = 1;
for steps=1:19
    xold = x;
    x = x - f(x)/df(x);
    steps = steps + 1;
    disp( [x f(x)] )
    myrel = abs((x-xold)/x);
    if myrel <= re
        break;
    end
end
if myrel <= re
    disp( 'Zero found at' )
    disp( x )
else
    disp( 'Zero NOT found')
end
```



% 7.2 BASIC RULES : p. 165

% Write a function file stats.m:

```
function [avg, stdev] = stats( x )
% function definition line
% STATS Mean and standard deviation % H1 line
% Returns mean (avg) and standard % Help text
% deviation (stdev) of the data in the
% vector x, using Matlab functions
```

```
avg = mean(x); % function body
stdev = std(x);
```

```
%-----
```

% Now test it in the Command Window with some random numbers, e.g.,

```
r = rand(100,1);
```

```
[a, s] = stats(r);
```

```
%-----
```

- (1) Start with the **function** keyword.
- (2) Input & output arguments.
- (3) Multiple output arguments.
- (4) Function naming. (same as variable)
- (5) Help text (start with '%')
Using help function_name display Help text.
- (6) Local variable : exist inside the function
Here, avg, & stdev are the local variable, they are available only inside the stats subfunction.
- (7) Global variable.

Two rules of using global variables:

- Before define every workspace, to declare global variable.
- Using 'capital letters' for Global variable. Make different from the local variable.

'whos global' : to check the global variable in the workspace.

'clear global X' : clear global variable X to all workspace.

- (8) Function that do not return values
function stars(n)
asteriks = char(abs('*')*ones(1,n));
disp(asteriks);
- (9) Vector arguments

```
% Vector arguments
function d = dice( n )
d = floor( 6 * rand(1, n) + 1 );    % d is a vector
```

(10) Input arguments is “Call by Value” to pass the values to the sunfunction.

(11) Checking the number of function arguments

Add a common line ‘disp(nargin)’, you can find the number of the input.

(12) Call a function with any number of input & output arguments

- Exec: Exec 7.5 in p.179 (a) write as a .m function (b) keep the input (x value)-output in the mean function and call this function as the subfunction.

```
% Debugging a script Newton's method in general
clear all;clc;
value=1; % initial value
x=3;
re = 1e-6; % required relative error
step=1;
myerr = 1;
while (myerr > re)
    value_old=value;
    value =value+(x.^(step))./(fact(step));
    disp( [step value] )
    step=step+1;
    myerr = value-value_old;
end

disp( [x value] )
```

% % Sec 7.2.3 : p-code

- In general, M – function is the script file. Source code can be seen.
- Let someone can run your function, however the source code cannot be seen. Translate it to p-code (Pseudo-Code).
- For example
 - pcode stats
 - can generate a ‘stats.p’ p-code.
- P-code can save computation time.

%% Sec. 7.3 FUNCTION HANDLES

% FUNHANDLE = @FUNCTION_NAME returns a handle to the named function,
% FUNCTION_NAME. A function handle is a MATLAB value that provides a
% means of calling a function indirectly. You can pass function
% handles in calls to other functions (which are often called function
% functions).

% Try the following on the command line:

```
fhandle = @sqrt;  
feval(fhandle, 9)  
feval(fhandle, 25)
```

% To defined function handle

Fhandle=@ (arglist) expression

For example:

Two kinds of functions: **anonymous function, and parameterized function.**

(1) anonymous function, the parameters value is anonymous (hided in expression)

```
Fh1= @ (x) 4*x.^2-50*x+2;  
Fh2= @ (x,y) sqrt(x.^2+y.^2)  
Fh3=@(x) (x-1.5).^2;
```

(2) parameterized function: you can change parameter every time you call it

```
fh2 = @(x,c) (x-c).^2;% the value of the parameter is not defined  
yet  
c = 1.5;  
fh3 = @ (x) fh2(x,c); % Now the value is defined  
d=fh3(3)
```

% Two build-in function to pass the funtion name as the argument

% feval & fminbnd

% feval(F,x1,...,xn) evaluates the function specified by a function

% handle or function name, F, at the given arguments, x1,...,xn.

```
fhandle = @sqrt;  
feval(fhandle, 9)  
feval(fhandle, 25)
```

```
f = @(x,y,c) (x-c).^2+y.^2; % The parameterized function.  
c = 1.5; % The parameter.  
% IN BUILD-IN FUNCTION feval call the function that you define  
b = feval(@(x,y) f(x,y,c),0.6,0.5)
```

```

% fminbnd Single-variable bounded nonlinear function minimization.
%     X = fminbnd(FUN,x1,x2) attempts to find a local minimizer X of the function
%     FUN in the interval  $x_1 < X < x_2$ . FUN is a function handle. FUN accepts
%     scalar input X and returns a scalar function value F evaluated at X.
Two function forms for the definition of the function handle:
    X = fminbnd(@(x) sin(x)+3,2,8)
    y=2:0.1:8;
    plot(y,sin(y)+3)
%-----
clear all;clc;
    f = @(x,c) (x-c).^2; % The parameterized function.
    c = 1.5; % The parameter.
    X = fminbnd(@(x) f(x,c),0,2)
% use help to find the fplot
fplot(@(x) f(x,c),[0,2])

% fplot Plot 2-D function
%     fplot(FUN) plots the function FUN between the limits of the current
%     axes, with a default of [-5 5].
%
%     fplot(FUN,LIMS) plots the function FUN between the x-axis limits
%     specified by LIMS = [XMIN XMAX].

% Example: fplot(@(x) x.^2.*sin(1./x),[-1,1])

% As an example, we would like to
% rewrite our newtgen script as a function newtfun, to be called as follows:

function y = f(x)
y = x^3 + x - 3;

%-----
% Then create and save another function file df.m:

function y = df(x)
y = 3*x^2 + 1;

% [x f conv] = newtfun( fh, dfh, x0 )

```

% The complete M-file newtfun.m is as follows:

```
function [x, f1, conv] = newtfun(fh, dfh, x0)
% NEWTON Uses Newton's method to solve  $f(x) = 0$ .
% fh is handle to  $f(x)$ , dfh is handle to  $f'(x)$ .
% Initial guess is x0.
% Returns final value of x, f(x), and
% conv (1 = convergence, 0 = divergence)
```

```
steps = 0; % iteration counter
x = x0;
re = 1e-8; % required relative error
myrel = 1;
while myrel > re & (steps < 20)
    xold = x;
    x = x - feval(fh, x)/feval(dfh, x);
    steps = steps + 1;
    disp( [x feval(fh, x)] )
    myrel = abs((x-xold)/x);
end;
if myrel <= re
    conv = 1;
else
    conv = 0;
end;
f1 = feval(fh, x); % return the function value at x
```

%----After previous 3 function defined we can use the following command to run newtfun

% -----

% Method 1: define two function handle

```
clear all;clc;
fhand = @f;
dfhand = @df;
[x,f1,con] = newtfun(fhand, dfhand, 2)
```

% Method 2

```
clear all;clc;
fhand = @(x) x^3 + x - 3; % The parameterized function.
dfhand= @(x) 3*x^2 + 1;
```



```
[x,f1,con] = newtfun(fhnd, dfhnd, 2)
```

● Exer

- (a) Find the minimum value for the function $y = 1 + e^{-0.2x} \sin(x + 2)$, for the interval of $0 < x < 10$. (Ans: (x,y)=(2.515, 9.0). (Use fminbnd)
- (b) Use fplot to plot this function for the interval of $0 < x < 10$.
- (c) Write this function as the parametric form, that is $y = 1 + e^{-0.2x} \sin(x + c)$, where c is the parameter.
Do the same thing as (a) & (b), by given c=2.5.

%% Sec 7.5: function name resolution

% if you having the same name in a variable and a function then the

% priority of the MATLAB (check p. 174):

% variable ---> subfunction ---> private function ---> dictionary

%% Sec. 7.6 Debugging a script: please open the subfunction 'newtgen1.m' and run it in a debugging mode

% Newton's method in general

- (1) In command Window '>>k' means that you are in the Debug mode.
- (2) Green arrow means the run ending at this point.

```
1      %% Debugging a script Newton's method in general
2 -    clear all;clc;
3      % excludes zero roots!
4  ➡    steps = 0; % iteration counter
5 -    x = input( 'Initial guess: '); % estimate of root
6 -    re = 1e-8; % required relative error
7 -    myrel = 1;
8 -    while myrel > re & (steps < 20)
9 -        xold = x;
```

Command Window

New to MATLAB? See resources for [Getting Started](#).

fx K>>

%% Check the procedure in p. 175 for the debugging

% Debugging a script Newton's method in general

% (1) set breakpoint at Line 4; and Line 11

% (2) run & continuous to run the program

```
clear all;clc;
```

% excludes zero roots!

● steps = 0; % iteration counter

x = input('Initial guess: '); % estimate of root

re = 1e-8; % required relative error

myrel = 1;

while myrel > re & (steps < 20)

 xold = x;

● x = x - f(x)/df(x);

 steps = steps + 1;

 disp([x f(x)])

 myrel = abs((x-xold)/x);

end

if myrel <= re

 disp('Zero found at')

 disp(x)

else

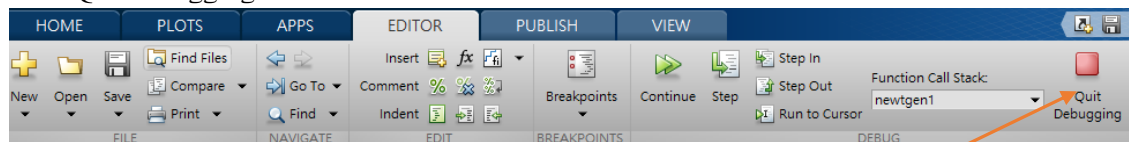
 disp('Zero NOT found')

end

%=====

=====

➤ Quit debugging



Click this button

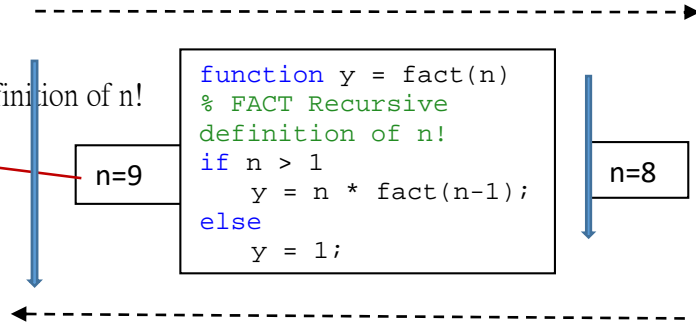
% Sec 7.7 RECURSION Call by one function itself

% The factorial function may be written recursively in

% an M-file fact.m like this:

n=10
call fact(n)

```
function y = fact(n)
% FACT Recursive definition of n!
if n > 1
    y = n * fact(n-1);
else
    y = 1;
end;
```



%=====

- Exec 7.8 in p.180 fibonacci number

```
function y = fib(n)
fib(1)=1;
for i=2:n
    if (i<3)
        fib(i)=1+fib(i-1);
    else
        fib(i)=fib(i-2)+fib(i-1);
    end
    disp(fib(i));
end
```

1. To rewrite newton's method in book 7.1 by using (for & if break)

Ans:

```
% excludes zero roots!

steps = 0; % iteration counter
x = input( 'Initial guess: '); % estimate of root
re = 1e-8; % required relative error
myrel = 1;
for steps=1:19
    xold = x;
    x = x - f(x)/df(x);
    steps = steps + 1;
    disp( [x f(x)] )
    myrel = abs((x-xold)/x);
    if myrel <= re
        break;
    end
end
if myrel <= re
    disp( 'Zero found at' )
    disp( x )
else
    disp( 'Zero NOT found' )
end
```

2. Function handle: (a) Find the minimum value for the function $y = 1 + e^{-0.2x} \sin(x + 2)$, for the interval of $0 < x < 10$. (Ans: (x,y)=(2.515, 9.0). (Use fminbnd)
(b) Use fplot to plot this function for the interval of $0 < x < 10$.
(c) Write this function as the parametric form, that is
 $y = 1 + e^{-0.2x} \sin(x + c)$, where c is the parameter.
Do the same thing as (a) & (b), by given c=2.5.
3. Exer in textbook 7.2,7.4,7.5,7.6, 7.8,7.9.