

Programming Practice: Rational Number Operator Overloading

We have designed and implemented rational numbers using C programming language. In this assignment, you will define and implement a rational number project using separate compilation of C++ programming language. Suppose a rational number p/q is represented by two relatively prime integers p and q , where q is a non-zero positive integer. In the case of $p/0$, set this number to rational number $0/1$. If rational number p/q that p and q are not relatively prime, simplify p/q by dividing both p and q by their greatest common division (GCD). If p/q is a negative rational number, simplify the rational number as $p < 0$ and $q > 0$. When printing a rational number, if the denominator is 1, print the numerator only. You will write a C++ project of a class named **Rational** with the following requirements:

1. Define a default constructor and a copy constructor. The default constructor may take 0, 1, or 2 arguments, say, (p, q) , with default value $0/1$, $p/1$, and p/q , respectively. The copy constructor takes a rational number as its argument and copy the value of the argument.
2. Use overloaded operator member functions and friend functions to define and implement arithmetic operations " $a+b$ " (addition), " $a-b$ " (subtraction), " $a*b$ " (multiplication), " a/b " (division), and " $|a|$ " (absolute value), and comparing relations " $a==b$ " (equal to), " $a!=b$ " (not equal to), " $a<b$ " (less than), " $a>b$ " (greater than), " $a<=b$ " (less than or equal to), and " $a>=b$ " (greater than or equal to), where each of a and b is either an integer or a rational number, but not both of them are integers. Note that the two operands **cannot** be integers at the same time.
3. Use overloaded operator member functions to define and implement assignment statement of rational numbers and its variations, including, " $<variable>=<expression>$ ", " $<variable>+=<expression>$ ", " $<variable>-=<expression>$ ", " $<variable>*=<expression>$ ", and " $<variable>/=<expression>$ ". The left-hand-side $<variable>$ is a rational reference and the right-hand-side $<expression>$ is either an integer object or a rational object.
4. Overload I/O stream operators " $<<$ " and " $>>$ " to enable output and input of rational numbers.

In the main function `int main()` declare three rational variables a , b , and c , and three integer variables d , e , and f . Input values of these variables from the console. Declare rational variable g without initial value. Perform the following operations:

1. Evaluate and print the results of expressions $-a$, $a+b$, $|a+b|$, $a+d$, $d+a$, $a-b$, $|a-b|$, $a-d$, $d-a$, $a*b$, $|a*b|$, $a*d$, $d*a$, a/b , $|a/b|$, a/d , and d/a ,
2. Evaluate and print the results of relations $a==b$, $a==e$, $f==c$, $a!=b$, $a!=e$, $f!=c$, $a<b$, $a<e$, $f<c$, $a<=b$, $a<=e$, $f<=c$, $a>b$, $a>e$, $f>c$, $a>=b$, $a>=e$, and $f>=c$.
3. Evaluate and print the results of expressions $a*c/d+e*b-d/b-a$, $a*c/(d+e*b)-d/(b-a)$, and $a*((c/(d+e)*b)-d/b)$
4. Execute statement **if** ($a>=b$) **then** $g=(d+e)*f$ **else** $g=(d-e)/f$; and print the value of g .
5. Execute statement **if** ($c*d==b*e$) **then** $g*=b/d+c/e$ **else** $g=b*d+c*e$; and print the value of g .
6. Evaluate and print the result of expression $\max(f-a/b, c+e*b)-\min(a+c/e, b*d)$.

Euclidean algorithm for computing the great common divisor of two integers m and n is given below for your reference:

```
// GCD: greatest common divisor
int gcd(int m, int n) {
    m = abs(m);
    n = abs(n);
```

```
        if (m % n == 0) return n;  
        else return gcd(n, m % n);  
    }
```

Using "cout <<" to print boolean value true/false, you need to include <iomanip>. Declare flag as a variable of type bool. Assign a boolean value to flag and then output the value with statement "cout << boolalpha << flag;" ([reference boolalpha](#)).

Execution Example: (next page)

```

D:\>rational_overloading
Enter rational number a (in the form of: p/q): 5/3
**** Value of a: 5/3
Enter rational number b (in the form of: p/q): 3/-5
**** Value of b: -3/5
Enter rational number c (in the form of: p/q): -7/4
**** Value of c: -7/4
Enter integer number d: -5
**** Value of d: -5
Enter integer number e: -4
**** Value of e: -4
Enter integer number f: 6
**** Value of f: 6
=====
**** Expression -a = -5/3
**** Expression a+b = 16/15
**** Expression |a+b| = 16/15
**** Expression a+d = -10/3
**** Expression d+a = -10/3
**** Expression a-b = 34/15
**** Expression |a-b| = 34/15
**** Expression a-d = 20/3
**** Expression d-a = -20/3
**** Expression a*b = -1
**** Expression |a*b| = 1
**** Expression a*d = -25/3
**** Expression d*a = -25/3
**** Expression a/b = -25/9
**** Expression |a/b| = 25/9
**** Expression a/d = -1/3
**** Expression d/a = -3
=====
**** Relation a==b is false.
**** Relation a==e is false.
**** Relation f==c is false.
**** Relation a!=b is true.
**** Relation a!=e is true.
**** Relation f!=c is true.
**** Relation a<b is false.
**** Relation a<e is false.
**** Relation f<c is false.
**** Relation a<=b is false.
**** Relation a<=e is false.
**** Relation f<=c is false.
**** Relation a>b is true.
**** Relation a>e is true.
**** Relation f>c is true.
**** Relation a>=b is true.
**** Relation a>=e is true.
**** Relation f>=c is true.
=====
**** Expression a*c/d+e*b-d/b-a = -421/60
**** Expression a*c/(d+e*b)-d/(b-a) = -2875/2652
**** Expression a*((c/(d+e)*b)-d/b)-a = -63/4
=====
Statement: if (a>=b) then g=(d+e)*f else g=(d-e)/f;
**** The new value of object g: -54
=====
Statement: if (c*d==b*e) then g*=b/d+c/e else g/=b*d+c*e;
**** The new value of object g: -27/5
=====
**** Expression max(f-a/b, c+e*b)-min(a+c/e, b*d) = 961/144
=====
D:\>_

```