# My "realistic" graph

Once built the graph, you should **compute the metrics** we discussed in class and **draw** some conclusions on the type of the underlying network.

Examples of questions you can answer are the following:

- 1. Does the graph have the same characteristics of a random or a power-law network?
- 2. Which are the most important nodes, with respect to a given centrality measure?
- 3. Are the <u>paths short</u> with respect to the size of the network?
- 4. Is the network **dense**?
- 5. And so on

Some measures provide indicators to know.

The importance of a node or an area in the network.

The distance among nodes or areas in the network Cohesion degree of an area in the network.

A geodesic path (shortest path) is a path between two vertices such that no shorter paths exist.

The diameter of a network is the length of the longest shortes-path between any pairs of vertices.

The <u>simplest centrality measure</u> is <u>node degree</u> and it can be applied to directed and undirected graphs:

- 1. **indegree**: number of links entering node i;
- 2. **outdegree**: number of links leaving node i;
- 3. **degree**: number of links of node i. Provides an indication of the ability of a node engaging in a direct relationship with the other nodes;

node degree=The total number of links of the node;

The maximun number of possible edges in a simple undirected network is  $\frac{1}{2}$  (N)(N-1)

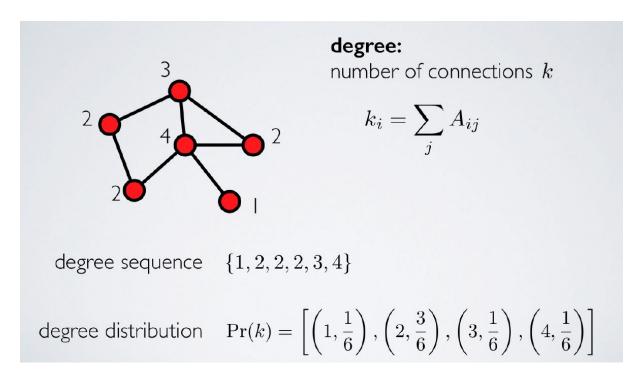
The density  $\rho$  of a network is the fraction of these edges really present in the network. So, it's simply: #edges/#max\_number of possible edges.  $0 \le \rho \le 1$  always.

If  $(\rho \to \text{costant when N} \to \infty)$  dense network;

else If  $(\rho \to 0 \text{ when } N \to \infty)$  sparse network.

## Degree distribution pk: Provides the probability that a randomly selected node

in the network has degree k. Nodes'link/maxLink.



## Betweenness\_centrality of a node v

is the sum of the fraction of all-pairs shortest paths that pass through v. So, the node's size it's related with the node's betweenness\_centrality. In practice: how many pairs of individuals would have to go through you in order to reach one another in the

minimum number of hops? Their removal may disrupt communication.

• Nodes with high betweenness have more important.

#### **Closeness** measures the mean distance of a vertex to other vertices:

 Nodes with high closeness have better access to information or more direct influence on other vertices.

<u>Closeness centrality</u> of a node u is the reciprocal of the sum of the shortest path distances from u to all n-1 other nodes. Since the sum of distances depends on the number of nodes in the graph, closeness is normalized by the sum of minimum possible distances n-1.

From: Stanford Large Network Dataset Collection (http://snap.stanford.edu/data/ego-Facebook.html)

Social networks: online social networks, edges represent interactions between people

# My real Network Analysis

Name: Facebook Type: Graph

Number of nodes: 4039 (named from 0 to 4038) Number of edges: 88234

Average degree: 43.6910

**Density:** 0.010820, so we can see that our graph is not dense: it's **sparse** because  $\rho \to 0$ .

is directed: False is complete: False

Diameter (it is the maximum eccentricity): 8

## top 7 nodes with highest-betweenness\_centrality (runn. time : ~3min.):

- 1. **107**: 0.48077531149557645
- 2. **1684**: 0.33812535393929544,
- 3. **3437**: 0.23649361170042005,
- 4. **1912**: 0.22967697101070242,
- 5. **1085**: 0.14943647607698152,
- 6. **0**: 0.14672864694039878,
- 7. **698**: 0.1157685138598761, ... other 4031 nodes.

### top 7 nodes with highest-closeness\_centrality (runn. time : ~3min.):

- 1. **107**: 0.45969945355191255
- 2. **58**: 0.3974018305284913,
- 3. **428**: 0.3948371956585509,
- 4. **563**: 0.3939127889961955,
- 5. **1684**: 0.39360561458231796,
- 6. **171**: 0.37049270575282134,
- 7. **348**: 0.36991572004397216, ... other 4031 nodes.

## top 7 nodes with highest-degree (runn. time : ~15sec.):

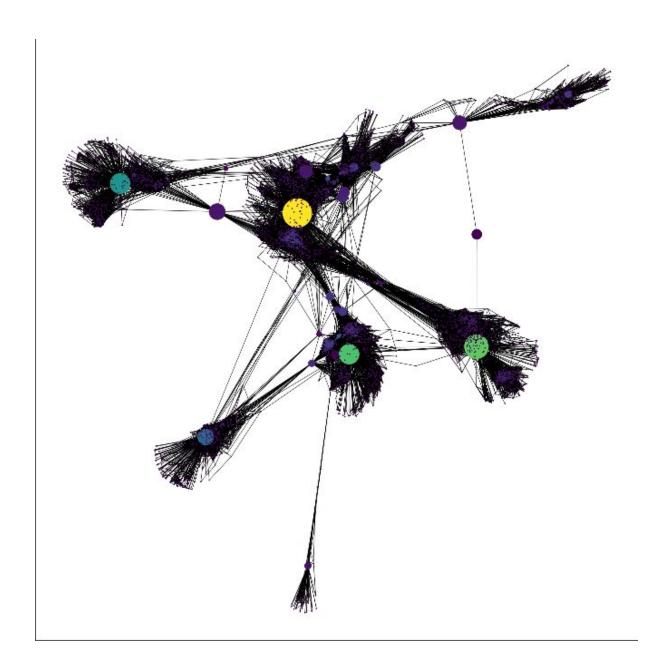
- 1. node: **107** degree:1045
- 2. node: **1684** degree:792
- 3. node: **1912** degree: 755

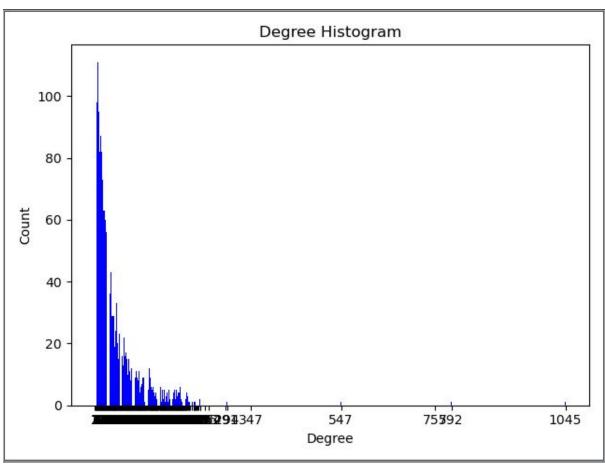
node: 3437 degree:547
node: 0 degree:347
node: 2543 degree:294
node: 2347 degree:291

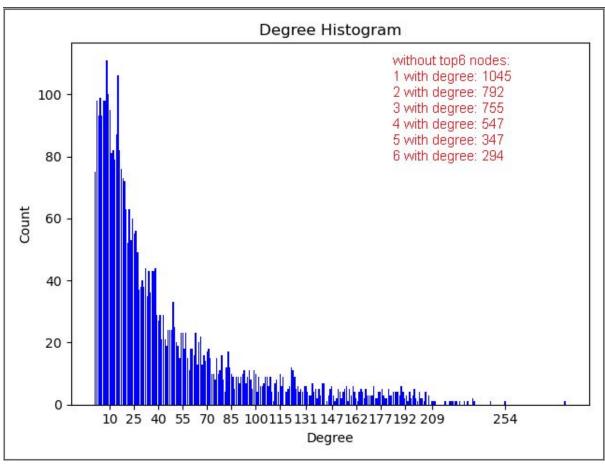
**node with max-degree** is 107 with degree=1045 and clustering=0.049038 that is under the average\_clustering!

My graph have the same characteristics of a **scale-free** network, in particular we can see that it follows a **power-law** distribution. The most notable characteristic in a scale-free network is the relative commonness of vertices with a degree that greatly exceeds the average.

In addition, I found some **hubs**: people with degree >> Average degree (=43.6910).







In graph theory, a **clustering coefficient** is a measure of the degree to which nodes in a graph tend to cluster together. Evidence suggests that in most real-world networks, and in particular <u>social networks</u>, **nodes tend to create tightly knit groups characterised by a relatively high density of ties**; this likelihood tends to be greater than the average probability of a tie randomly established between two nodes (Holland and Leinhardt, 1971;<sup>[1]</sup> Watts and Strogatz, 1998<sup>[2]</sup>).

Two versions of this measure exist: the global and the local. We calculated the **local** that gives an indication of the embeddedness of single nodes.

average\_clustering: 0.605547

### top 5 nodes with Low-clustering coefficient:

- 1. **3437**: 0.032230414314509376,
- 2. **0**: 0.04196165314587463,
- 3. **1684**: 0.044774546986936364,
- 4. **107**: 0.049038479165520905,
- 5. **3980**: 0.0853302162478083.

### top 5 nodes with High-clustering coefficient:

- 1. **595**: 0.9883040935672515,
- 2. **3919**: 0.9848484848484849,
- 3. **3639**: 0.98484848484849,
- 4. **3668**: 0.9818181818181818,
- 5. **576**: 0.978021978021978.

In conclusion, we can say that the **node** 107 is the most important node followed by node 1684.

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