

$$a_n = (\max(\text{num_digits}(n), (a_{n-1} + n), (a_{n-2} - a_{n-3}))) + a_{n-3}$$