$a_n = \max(\min(\text{num_digits}(a_{n-2}), (a_{n-1} + a_{n-1}), (a_{n-2} + 1)), (a_{n-1} + 1), a_{n-1})$