Lab Lesson 01

Giacomo Bergami

October 24, 2017

Exercises

- 1. Write two programs, for both bytes and integers, that are affected by a overflow representation.
- 2. Write a program that prints the seconds into a human readable format. This means that each second must show the number of years, days, hours, minutes and seconds it corresponds. The following output format must be used:

Oy 2d 3h 1m 20s

- 3. A year with 366 days is said to be a leap. Following the adoption of the Gregorian calendar (1582), in order to determine if a year is a leap, you can follow these steps:
 - a) If the year can be divided by four, see b) and e) otherwise
 - b) If the year can be divided by one hundred, see c) and d) otherwise
 - c) If the year can be divided by four hundred, see d) and e) otherwise
 - d) return **true**
 - e) return **false**

Solve this exercise without using any if-then-else statement.

4. Create a program that takes a string with the following format as an input:

1024356 h S

and converts 1024356 hours (h) into seconds (S). In particular, the source time unit is in lowercase, and the upper time unit is the target time unit towards which apply the conversion. The strings that can be used to express such time units are the following ones:

• y/Y = Year

- d/D = Day
- h/H = Hour
- m/M = Minute
- s/S = Seconds

Create a program that parses the string and provides the desired time conversion.

5. Write a program that associates to a pair of integers (i, j) an unique integer c, such that $(i, j) \to c$ is a bijection.

In order to do that, we can use the dovetailing function:

$$c = \frac{(i+j)(i+j+1)}{2} + j$$

Then, we want to make sure that the resulting number is uniquely associated to (i, j). Then, we can ask ourselves if there is an inverse function. Such inverse function is:

$$j = c - \frac{1}{2} \left(\left\lfloor \frac{\sqrt{8c+1} - 1}{2} \right\rfloor + 1 \right) \cdot \left(\left\lfloor \frac{\sqrt{8c+1} - 1}{2} \right\rfloor \right)$$
$$i = \left(\left\lfloor \frac{\sqrt{8c+1} - 1}{2} \right\rfloor \right) - j$$

- 6. Repeat exercises 2 and 3 using the if..then..else construct.
- 7. Write a program that, reading two doubles from terminal separated by space, print to which quadrant the two numbers belong. Recall briefly that:
 - If both its coordinates are positive, it stays in the first quadrant.
 - If only the first coordinate (x) is negative, it stays in the second quadrant.
 - If both coordinates are negative, it stays in the third quadrant.
 - If only the second coordinate (y) is negative, it stays in the fourth quadrant.
- 8. Create a program that reads four pairs of doubles from terminal. Each of these pairs will represent a (x, y) coordinate in the plan representing a quadrilateral. Remember the following rules:
 - The distance between two points A and B is $\overline{AB} = \sqrt{(y_B y_A)^2 + (x_B x_A)^2}$.
 - \bullet The slope between two points A and B is $m_{AB}=\frac{y_B-y_A}{x_B-x_A}$
 - The size of the angle $\stackrel{\triangle}{ABC}$ where B is fixed is $\arccos\left(\frac{\overline{AB}^2 + \overline{BC}^2 \overline{CA}^2}{2 \cdot \overline{AB} \cdot \overline{BC}}\right)$. **Please Node:** the result of Math.acos is expressed in rad. If you want to use the degrees you must use Math.toDegrees.

Also remember that:

- A quadrilateral with only two parallel opposite sides is a trapezoid.
- A quadrilateral with parallel opposite sides, perpendicular two by two and of same length is a square.
- A quadrilateral with parallel opposite sides, perpendicular two by two and having parallel sides of equal length is a rectangle.
- A quadrilateral with parallel opposite sides and all the sides with the same length and does not fit in the previous cases is a rhombus, otherwise if it has the opposite parallel sides of the same length, it is a parallelogram.
- Otherwise is a parallelogram.