#### PSTAT 5LS Lab 7

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Week of November 18, 2024

#### Section 1

#### Announcements

## **Upcoming Deadlines**

- HW 7 due by 11:59pm on **Tuesday**, November 26
- HW 8 due by 11:59pm on Friday, December 6
- Exam 2 on Thursday, November 21
  - Coverage:
    - CI/HT for one proportion *p* (theory)
    - ullet CI/HT for one mean  $\mu$
    - ullet "Name That Scenario" (determine if the parameter is  ${\it p},\,\mu,\,\mu_{\it d},\,\mu_{\it 1}-\mu_{\it 2})$
    - Don't forget the earlier ideas from Slide Sets 1 and 2 (e.g., observational study or experiment, explanatory and response variables, describing a distribution using a histogram)
  - Professor Miller has posted the formula sheet, Exam 2 Review, and Exam 2 Section Review on Canvas. We will talk about the Exam 2 Section Review next time

#### Section 2

Learning Objectives

## R Learning Objectives

- Generate R output providing confidence intervals and hypothesis tests for inference on the difference in two population means.
- ② Create histograms of just one group in order to check the normality conditions.

## Statistical Learning Objectives

- Ontinue discussing quantitative data in regards to a difference in two means scenario.
- Understand whether data is considered paired or from two independent samples.
- Understand confidence intervals and hypothesis test for a difference in two means.

#### Functions Covered in this Lab

- pt()
- 4 qt()
- 1 t.test()

#### Section 3

Lab Tutorial

#### Collecting Two Sets of Numeric Data

Today, we're talking about inference when data from 2 **sets** of a *numeric* variable is collected. Let's first revisit the conditions.

## Condition 1: Independence Within the Sample(s)

We are **always** hoping that the observations within the sample (or within the samples) are independent of one another. When we have taken a random sample (or samples), we can generalize to the appropriate population (or populations).

#### Condition 2: Independence Between the Samples

The question we have to ask ourselves, when dealing with 2 sets of observations of a numeric variable:

Are the two sets of observations independent of **one another**, such that observations in one sample tell us nothing about the observations in the other sample (and vice versa)?

If the answer is **yes**, then the appropriate method of inference is to keep the data separate and discuss a **difference in two population means**, with parameter  $\mu_1 - \mu_2$ .

If the answer is  $\mathbf{no}$ , then the appropriate method of inference is to pair the data and discuss the mean of the population of differences, with parameter  $\mu_{\mathbf{d}}$ .

#### Paired or Independent?

Consider the following scenarios and determine if the data are paired or if the data come from independent samples.

 A company wants to compare job satisfaction levels between their full-time and part-time employees. They survey 100 full-time and 100 part-time employees.

A psychologist is studying the effects of caffeine on reaction times. They test each participant's reaction time once after drinking regular coffee and once after drinking decaf coffee, with tests done on separate days.

#### Paired or Independent?

• An educational researcher wants to investigate if there's a difference in math performance between students who attend public schools and those who attend private schools. They randomly select 200 8th grade students from public schools and 200 from private schools, then administer the same standardized math test to both groups.

A language learning app developer wants to assess the improvement in users' vocabulary after using the app for two months. They test the vocabulary of 100 users when they first download the app and then test the users again after two months of app usage.

#### Difference in Two Means

When we have two independent samples, we need to work with the difference in two means. In this scenario, our parameter is

$$\mu_1 - \mu_2$$

where  $\mu_1$  represents the population mean for "group 1" and  $\mu_2$  represents the population mean for "group 2".

The point estimate is

$$\bar{x}_1 - \bar{x}_2$$

#### Difference in Two Means

#### The conditions are

Independence within each sample: The observations within each sample are independent.

This condition is typically satisfied by taking two random samples (one from each population) or by taking one random sample and splitting it into two independent groups (e.g., in-state students and out-of-state students).

- Independence between the samples: The two samples are independent of one another such that observations in one sample tell us nothing about the observations in the other sample (and vice versa).
- Normality (must check for both groups): Each sample of observations should come from a nearly-normal population.

We will check by making a histogram of the sample observations from each of the groups. We can relax the condition more and more for larger and larger sample sizes.

#### Back to the Penguins!

Let's compare the mean flipper lengths of Adelie and Chinstrap penguins.

Run the tryIt1 code chunk, to read in the penguins data.

```
penguins <- read.csv("penguins.csv", stringsAsFactors = TRUE)</pre>
```

#### Subsetting the Data to Only Include Two Groups

First, we'll subset the data to just involve Adelie and Chinstrap penguins. This is only because we're not interested in Gentoo penguins for this question, so we'll take them out.

Since we are interested in penguins that are either Adelie or Chinstrap, R has an easy way to achieve this by using the %in% operator. Don't forget the double quotes around Adelie and Chinstrap!

Run the code in the tryit2 code chunk in your notes document.

```
penguinsSubset <- subset(penguins,</pre>
                           species %in% c("Adelie", "Chinstrap"))
```

## Normality Condition x 2

To check the normality conditions, we will need to make **two** histograms: one for the Adelie penguins, and another for the Chinstrap penguins.

Since we only need these one group subsets for the histograms, we will not bother to give it a name. Instead, we will embed the subset code inside the histogram code.

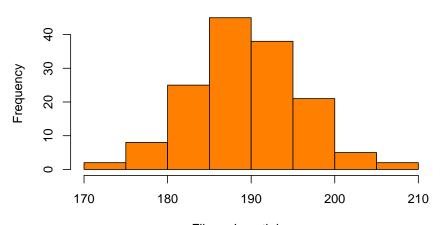
## Histogram of Just Adelie Penguins Flipper Length

Let's first create a histogram of the flipper lengths for the Adelie penguins. Run the tryit3 code chunk in your notes document to generate this histogram.

```
hist(penguinsSubset$flipper_length_mm[penguinsSubset$species == "Adelie"],
    main = "Histogram of Flipper Lengths of Adelie Penguins",
    xlab = "Flipper Length in mm",
    col = "darkorange1")
```

## Histogram of Just Adelie Penguins Flipper Length

#### **Histogram of Flipper Lengths of Adelie Penguins**



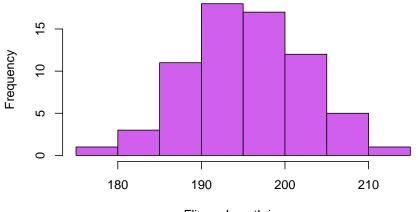
## Histogram of Just Chinstrap Penguins Flipper Length

Next up, let's create a histogram of the flipper lengths for the Chinstrap penguins. Change the code in the tryit4 code chunk in your notes document so that you get the histogram we need.

```
hist(penguinsSubset$flipper_length_mm[penguinsSubset$species == "Chinstrap"],
    main = "Histogram of Flipper Lengths of Chinstrap Penguins",
    xlab = "Flipper Length in mm",
    col = "mediumorchid2")
```

#### Histogram of Just Chinstrap Penguins Flipper Length

#### **Histogram of Flipper Lengths of Chinstrap Penguins**



## Normality Condition

Does the normality condition appear to be satisfied?

## Hypothesis Test for the Difference in Two Means

We would like to test the claim that there **is** a difference in the mean flipper length for the two groups, Adelie penguins and Chinstrap penguins.

$$H_0: \mu_1 - \mu_2 = 0$$
  $H_A: \mu_1 - \mu_2 \neq 0$ 

The parameter here is  $\mu_1 - \mu_2$ , where  $\mu_1$  is the mean flipper length in mm for Adelie penguins on Palmer Archipelago, and  $\mu_2$  is the mean flipper length in mm for Chinstrap penguins on Palmer Archipelago.

## Performing the t-test for the Difference in Two Population Means

The code to conduct the two-sample test is in the tryit5 code chunk in your notes document. Make sure to specify the alternative in the alternative argument ("two.sided", "less", "greater") before running the chunk.

```
t.test(flipper_length_mm ~ species,
       data = penguinsSubset,
       alternative = "two.sided")
```

## Performing the *t*-test for the Difference in Two Population Means

```
##
## Welch Two Sample t-test
##
## data: flipper_length_mm by species
## t = -5.6115, df = 120.88, p-value = 1.297e-07
## alternative hypothesis: true difference in means between group Ar
## 95 percent confidence interval:
## -7.739129 -3.702450
## sample estimates:
## mean in group Adelie mean in group Chinstrap
```

##

190,1027

195.8235

#### **Decision and Conclusion**

From the R output, we see that the test statistic is t=-5.6115 and the p-value is tiny (much less than any of the standard significance levels.) We reject the null hypothesis.

Our analysis suggests that there is a difference between the mean flipper length in mm for Adelie penguins on Palmer Archipelago and the mean flipper length in mm for Chinstrap penguins on Palmer Archipelago.

#### Difference in Two Means Confidence Interval

When we have statistically significant results that suggest there is a difference between the two populations means, it is helpful to construct a confidence interval to find a range of reasonable values for that difference. (Confidence intervals are also helpful when we are simply interested in estimating the parameter.)

As a reminder, the parameter here is  $\mu_1-\mu_2$ , where  $\mu_1$  is the mean flipper length in mm for Adelie penguins on Palmer Archipelago, and  $\mu_2$  is the mean flipper length in mm for Chinstrap penguins on Palmer Archipelago.

# Computing the 98% Confidence Interval for the Difference in Two Population Means

Try this code in the tryit6 code chunk in your notes document. Be sure to specify the confidence level before running the chunk.

## Computing the 98% Confidence Interval for the Difference in Two Population Means

```
##
##
   Welch Two Sample t-test
##
## data: flipper_length_mm by species
## t = -5.6115, df = 120.88, p-value = 1.297e-07
## alternative hypothesis: true difference in means between gr
## 98 percent confidence interval:
## -8.124296 -3.317284
## sample estimates:
##
      mean in group Adelie mean in group Chinstrap
                  190, 1027
```

##

195.8235

#### Interpreting the Confidence Interval

The 98% confidence interval is (-8.124, -3.317).

A fairly standard way to interpret this confidence interval is to talk about reasonable values of the difference between the two means:

"We estimate, with 98% confidence, that the difference between the mean flipper length in mm for Adelie penguins on Palmer Archipelago and the mean flipper length in mm for Chinstrap penguins on Palmer Archipelago is between -8.124 mm and -3.317."

This confidence interval is awkward. A better way to understand what the confidence interval tells us is to say

"We estimate, with 98% confidence, that the mean flipper length in mm for Adelie penguins on Palmer Archipelago is between 3.317 mm and 8.124 mm less than the mean flipper length in mm for Chinstrap penguins on Palmer Archipelago."

## Tie between Hypothesis Tests and Confidence Intervals

Remember that confidence intervals use what we have from our sample(s) to give us a range of values we think are reasonable for the parameter.

If we had not already conducted a hypothesis test for the difference in the two means, the 98% confidence interval we created could be used to test the hypotheses

$$H_0: \mu_1 - \mu_2 = 0$$

$$H_A: \mu_1 - \mu_2 \neq 0$$

at the  $\alpha = 0.02$  significance level.

## Tie between Hypothesis Tests and Confidence Intervals

The 98% confidence interval for the difference between the mean flipper length in mm for Adelie penguins and the mean flipper length in mm for Chinstrap penguins is -8.124 mm to -3.317. Do we reject or fail to reject  $H_0: \mu_1 - \mu_2 = 0$  at the  $\alpha = 0.02$  significance level?

#### Section 4

Questions

#### What Questions Do You Have?

