



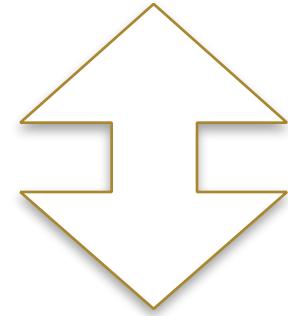
Traffic Control Systems Security: Coordinated Ramp Metering Attacks

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Work with Professor Alexandre Bayen
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Mathias Payer

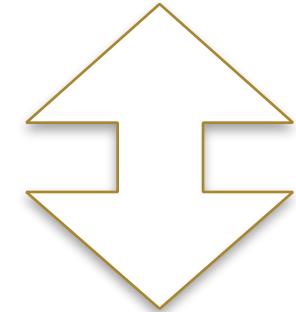
Overview of Talk

- * Traffic Control Infrastructure
 - * Actual Attack Examples
- * SmartRoads: Traffic/Cybersecurity Testbed
- * Coordinated Ramp Metering Attacks
 - * Optimal Control
 - * Multi-objective Optimization
- * Attack Examples
 - * Aiding a fleeing vehicle
 - * Creating precise congestion patterns

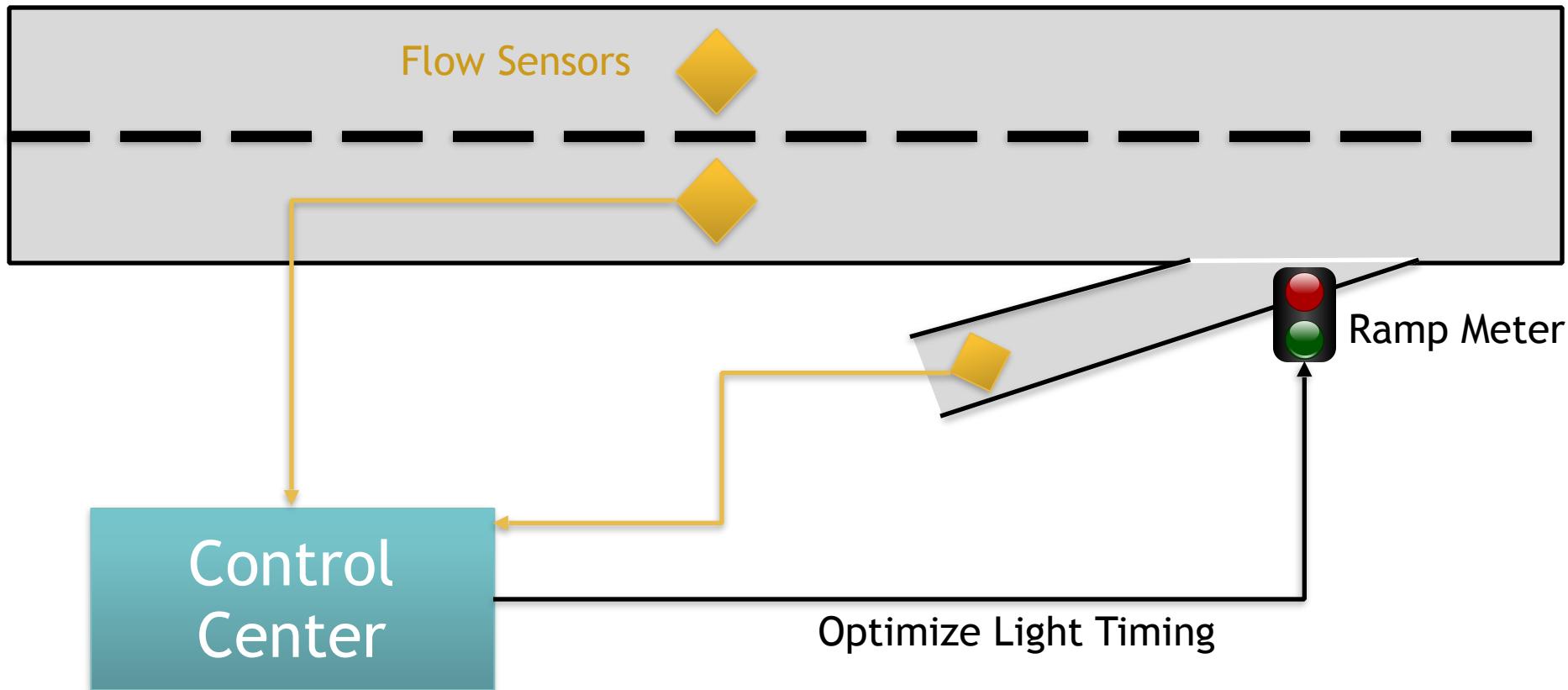


SmartRoads: Cyber-physical Security on Traffic Networks

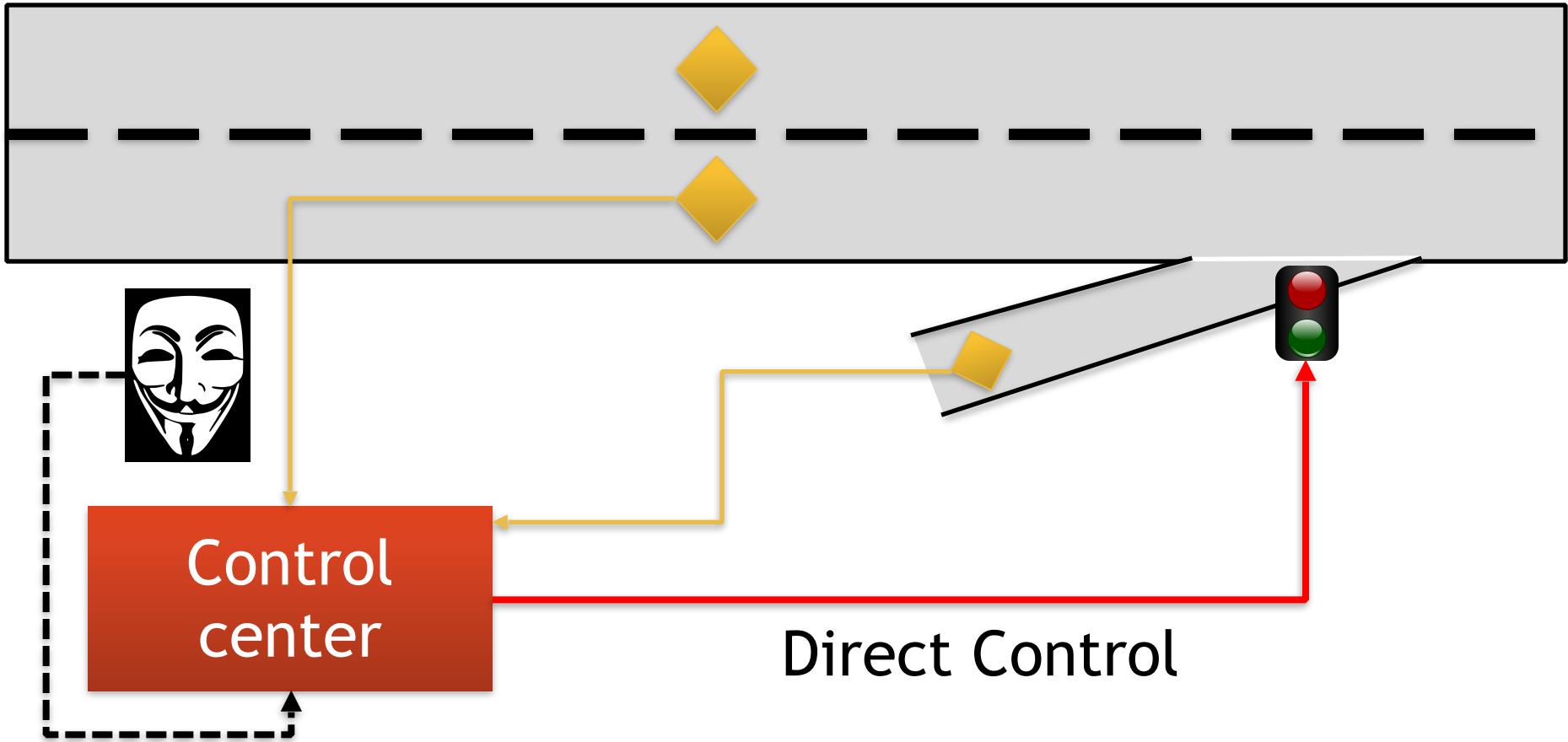
- * Traffic management has two components:
 - * Physical sensors and traffic lights
 - * Virtual control and estimation algorithms
- * Compromise of cyber traffic systems has been demonstrated* in the wild.
- * Potential attack vectors numerous:
 - * Broadcasting fake accident reports
 - * Compromise of metering light network.
- * Resiliency to attack through fault detection and modeling/sensing discrepancies.



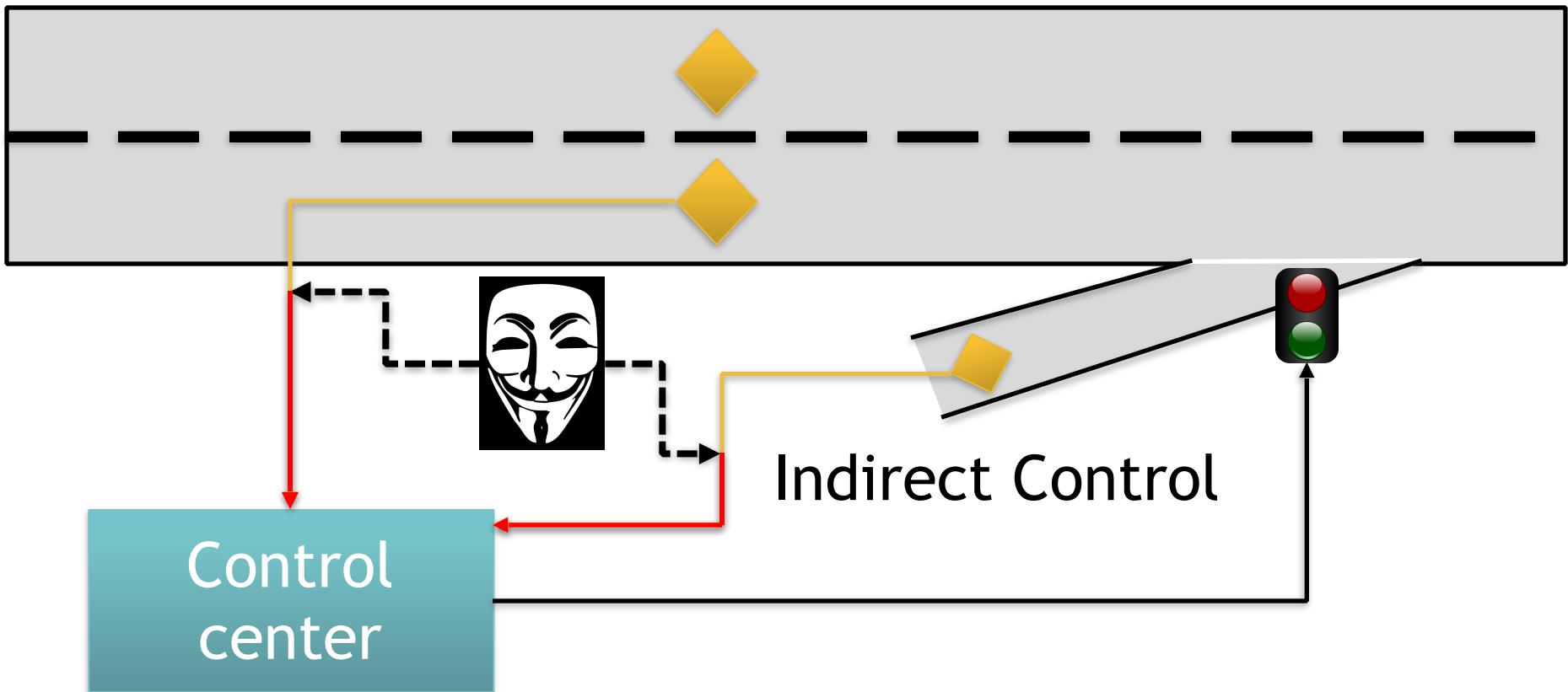
Freeway Traffic systems



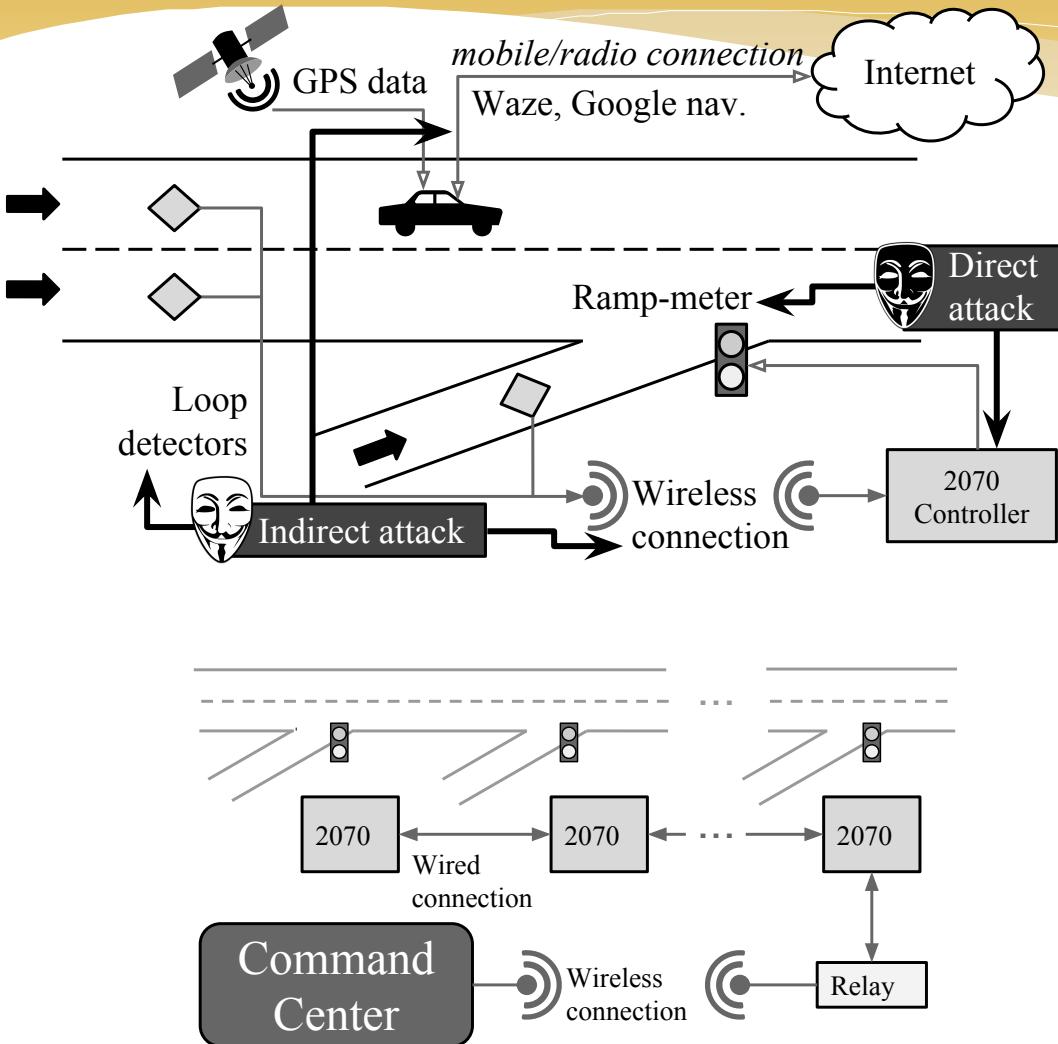
Compromise : complete takeover



Compromise : spoofing the sensors



Vulnerability Points

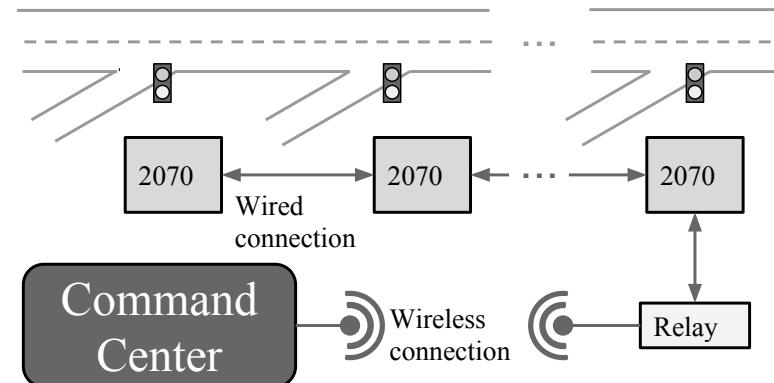
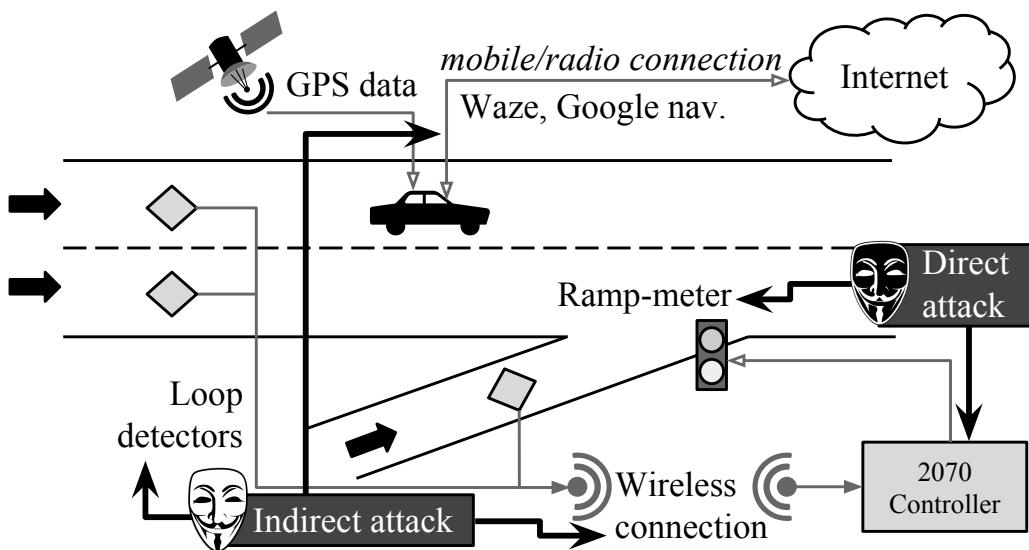


Local Architecture

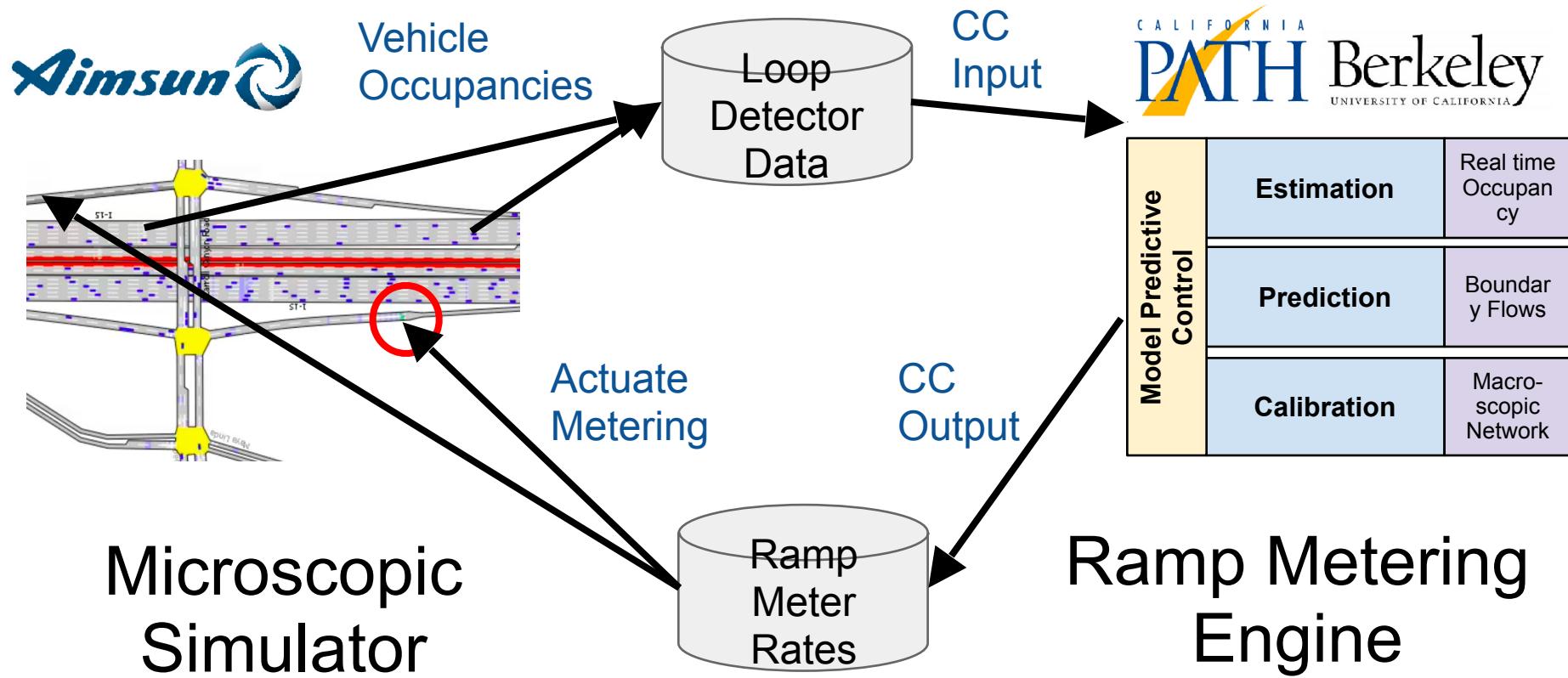
Networked Meters

Vulnerability Points Taxonomy

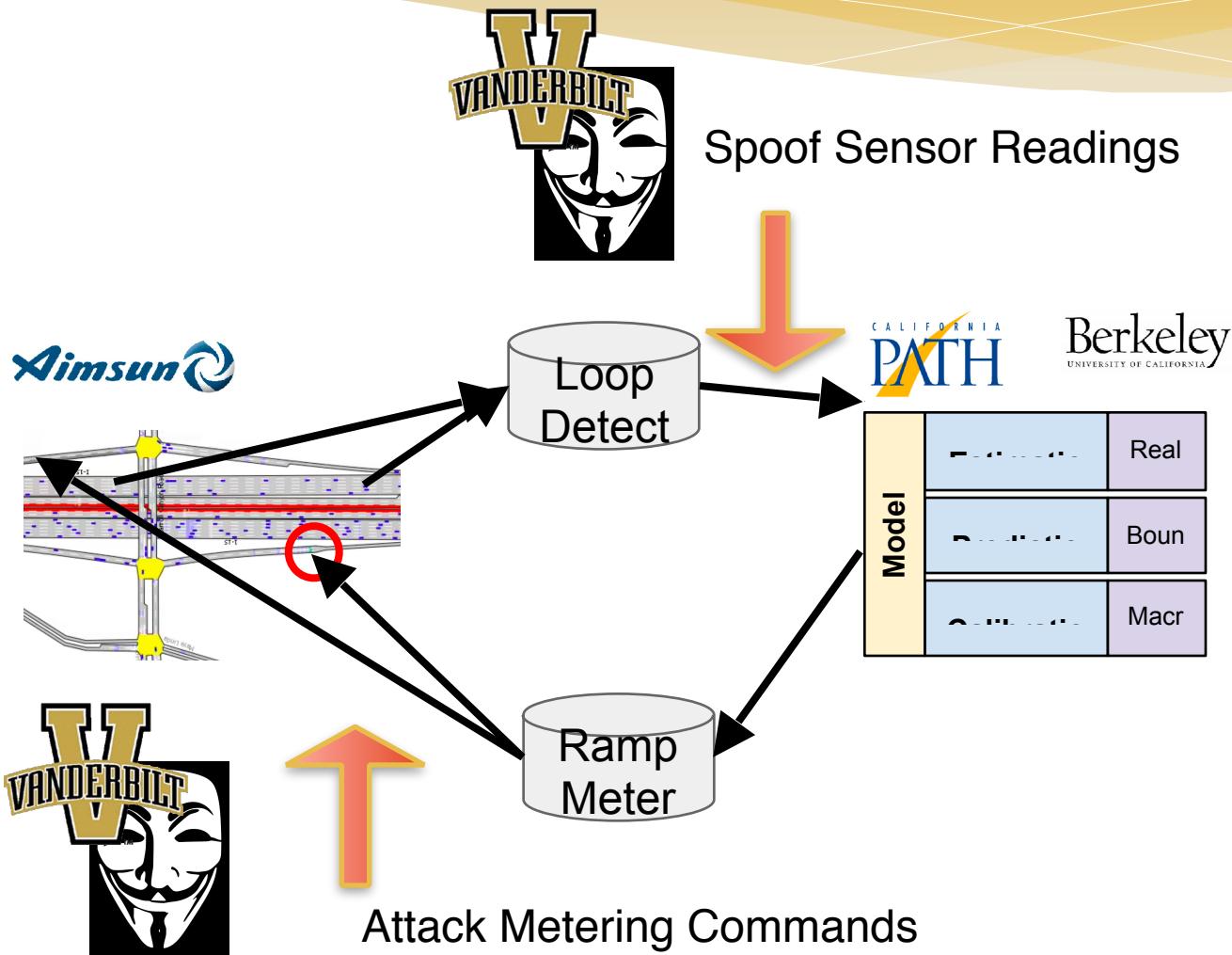
Attack Description	Access	Control	Complexity	Cost
copper theft/clipping wires	physical	low	low	low
replacing a single sensor/actuator	physical	low	low	low
attacking a single sensor/actuator	locality	low	medium	low
replacing a single control box	physical	medium	medium	medium
replacing a set of sensors/actuator	physical	medium	medium	medium
attacking a set of sensors/actuator	locality	low	medium	low
replacing a corridor of control boxes	physical	high	medium	medium
attacking a corridor of control boxes	network	high	high	medium
attacking the control center	network	high	high	high
spoofing GPS data	network	medium	high	medium
attacking navigation software	network	medium	medium	medium



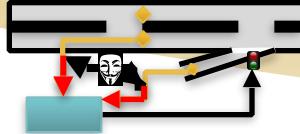
SmartRoads Architecture



SmartRoads Architecture

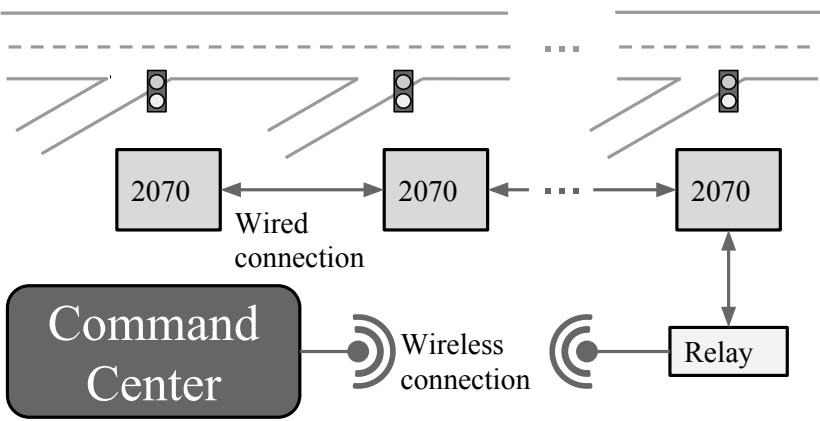


SmartAmerica Scenario



Coordinated Ramp Metering Attacks

MAXIMIZE Attack Objective



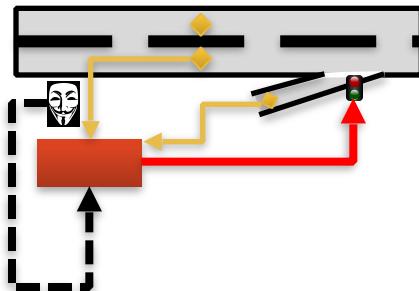
Create Jam between Exits 4-6

+

Achieve Free-flow Otherwise
(Stealthy Attack, avoid detection)

+

Limit Onramp Queue Sizes



SUBJECT TO Traffic Dynamics

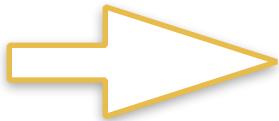
$$\frac{\partial \rho}{\partial t} + \frac{\partial f(\rho)}{\partial x} = 0$$

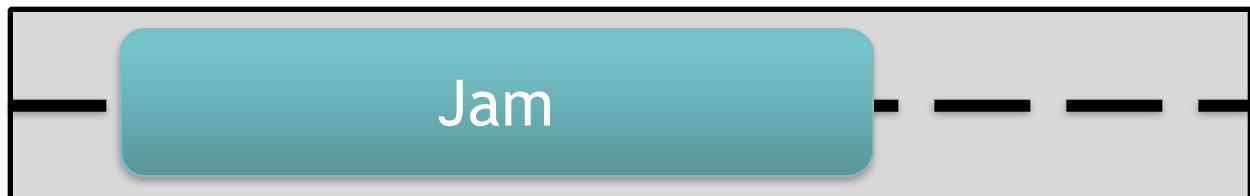
Finite Horizon Optimal Control Formulation

- * Discretize continuous PDE dynamics (Godunov's method)

$$H_{i,t} = \rho_{i,t} - \rho_{i,t-1} + \frac{\Delta t}{\Delta x} (f^{\text{in}}_{i,t-1} - f^{\text{out}}_{i,t-1}) = 0$$

- * Objective: State tracking $\min_{u \in U} J = \sum_i \sum_t \| \rho_{i,t} - \bar{\rho}_{i,t} \|$

$\bar{\rho}$ 



$$\min_{\mathbf{u} \in U} J(\mathbf{u}, \rho)$$

Finite-horizon Optimal Control Problem

$$\min_{\mathbf{u} \in U} \underbrace{\sum_{t=1}^{T-1} \sum_{i=1}^N f(u_{i,t}, \rho_{i,t})}_{\text{Running Cost}} + \underbrace{\sum_{i=1}^N f_T(u_{i,T}, \rho_{i,T})}_{\text{Terminal Cost}}$$

subject to system dynamics:

$$\begin{aligned}\rho_{i,0} &= \rho_i^0 \\ \rho_{i,t+1} &= \rho_{i,t} + \frac{\Delta t}{\Delta x} (G(\rho_{i-1,t}, \rho_{i-1,t}, u_{i,t}) - \\ &\quad G(\rho_{i,t}, \rho_{i+1,t}, u_{i,t})) \\ \forall i &\in [1, N], \forall t \in [1, T]\end{aligned}$$

$$\min_{\mathbf{u} \in U} J(\mathbf{u}, \rho)$$

$$\text{s.t. } H(\mathbf{u}, \rho) = 0$$

- *Non-linear
- *Non-smooth
- *Non-convex

- * Performing gradient descent w/ finite-differences infeasible for large networks!

Adjoint Formulation

$$\min_{\mathbf{u} \in U} J(\mathbf{u}, \rho)$$

$$\text{s.t. } H(\mathbf{u}, \rho) = 0$$

Compute gradient: $\nabla_{\mathbf{u}} J = \frac{\partial J}{\partial \mathbf{u}} + \frac{\partial J}{\partial \rho} \frac{d\rho}{d\mathbf{u}}$

EasyHard

Eliminate $\frac{d\rho}{d\mathbf{u}}$ using system dynamics: $\nabla_{\mathbf{u}} H = \frac{\partial H}{\partial \mathbf{u}} + \frac{\partial H}{\partial \rho} \frac{d\rho}{d\mathbf{u}} = 0$

$$\begin{aligned}\nabla_{\mathbf{u}} J &= \\ J_u + J_\rho \rho_u + \lambda^T [H_\rho + H_u] &= \\ (J_\rho + \lambda^T H_\rho) \rho_u + (J_u + \lambda^T H_u) &\end{aligned}$$


$$\begin{aligned}\nabla_{\mathbf{u}} J &= \\ J_u + \lambda^T H_u &\\ \text{s.t. } H_\rho^T \lambda &= -H_u^T\end{aligned}$$

Coordinated Freeway Control using Adjoint Methods

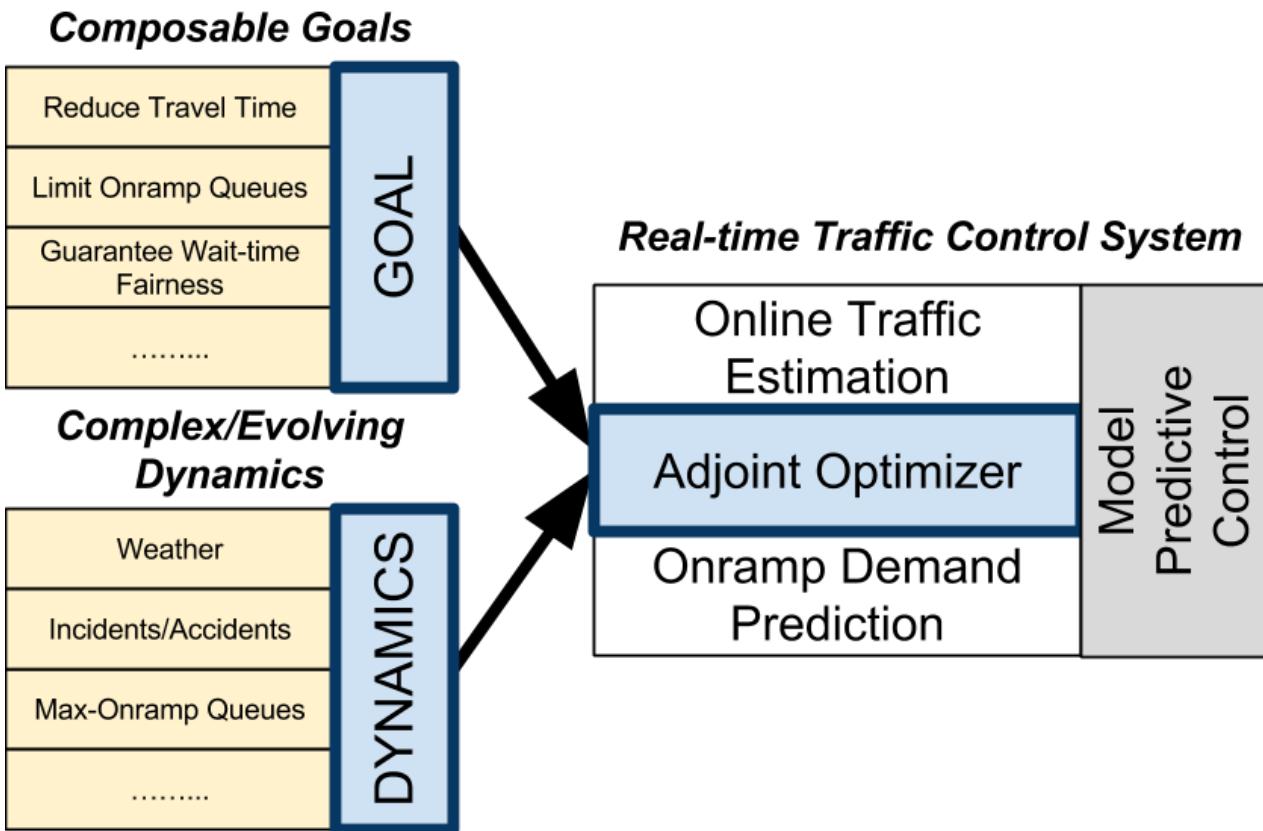
Composable Goals

Reduce Travel Time	GOAL
Limit Onramp Queues	
Guarantee Wait-time Fairness	
.....	

Complex/Evolving Dynamics

Weather	DYNAMICS
Incidents/Accidents	
Max-Onramp Queues	
.....	

Coordinated Freeway Control using Adjoint Methods



Coordinated Freeway Control using Adjoint Methods

Composable Goals

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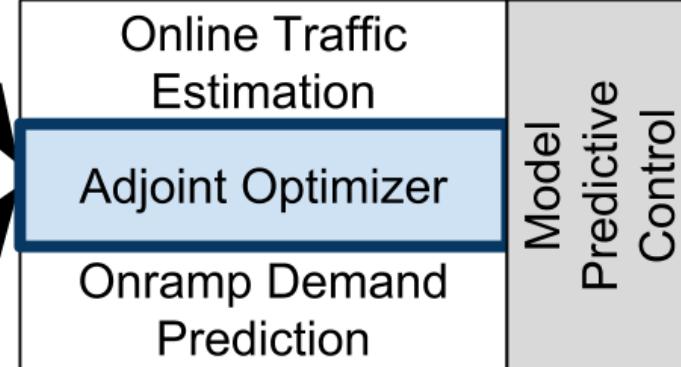
GOAL

Complex/Evolving Dynamics

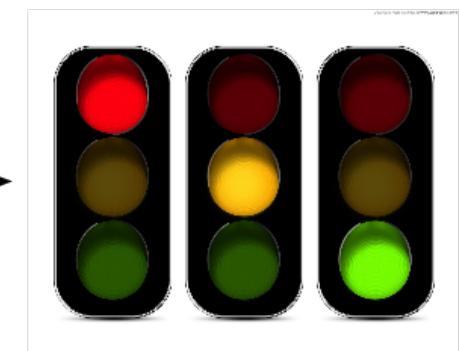
Weather
Incidents/Accidents
Max-Onramp Queues
.....

DYNAMICS

Real-time Traffic Control System



Coordinated and Predictive Congestion Management



Adjoint Method scales linearly with:
Size of network
Time horizon

Gradient Descent

- * Compute gradient of constrained problem via adjoint

$$\min_{\mathbf{u} \in U} J(\mathbf{u}, \rho)$$

$$\text{s.t. } H(\mathbf{u}, \rho) = 0$$

$$\nabla_{\mathbf{u}} J =$$

$$J_u + \lambda^T H_u$$

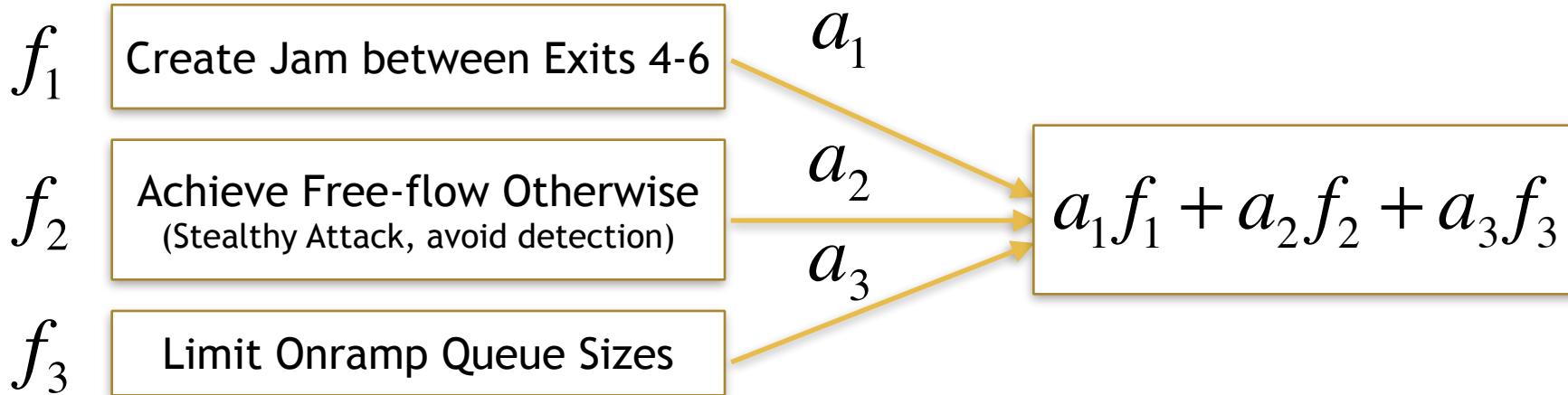
$$\text{s.t. } H_{\rho}^T \lambda = -H_u^T$$

- * Embed within gradient descent loop:

- * 1) Compute new state $\rho^k : H(\rho^k, u^k) = 0$ [forward sim]
- * 2) Compute gradient $\nabla_{\rho} J(\rho^k, u^k)$
- * 3) Update $u^{k+1} = f(u^1, \dots, u^k, \nabla_{\rho} J^k)$ [e.g. L-BFGS]
- * 4) Loop $k \leftarrow k + 1$

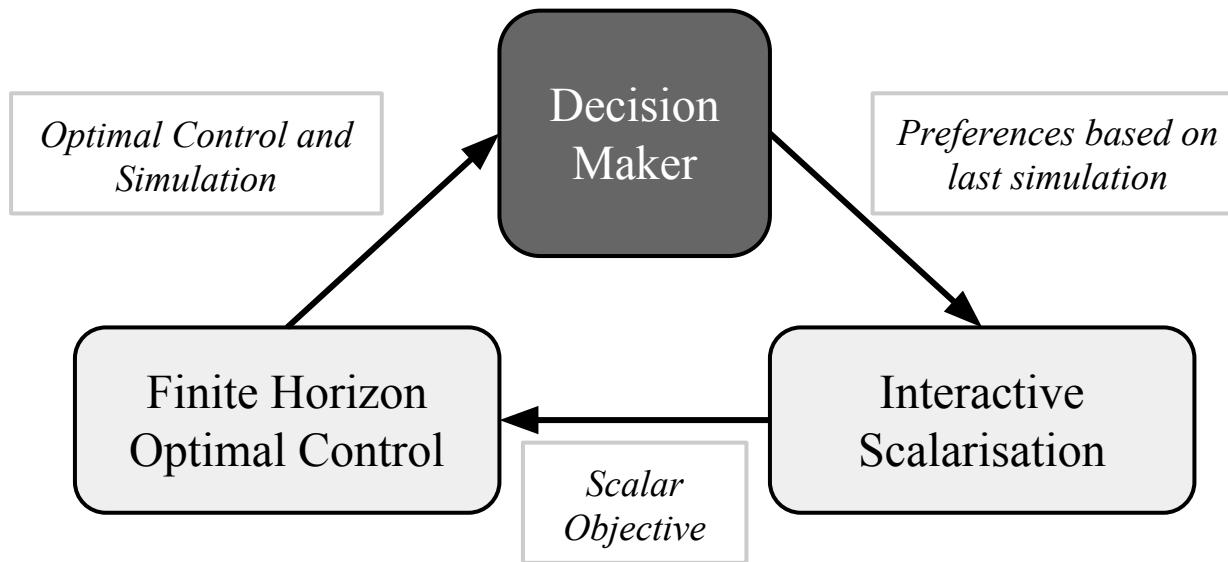
Multi-objective Optimization for Attacks

- * **Goal:** Achieve success on many conflicting goals simultaneously
- * **Solution:** Scalarization
 - * Objective -> linear combination of sub-objectives.



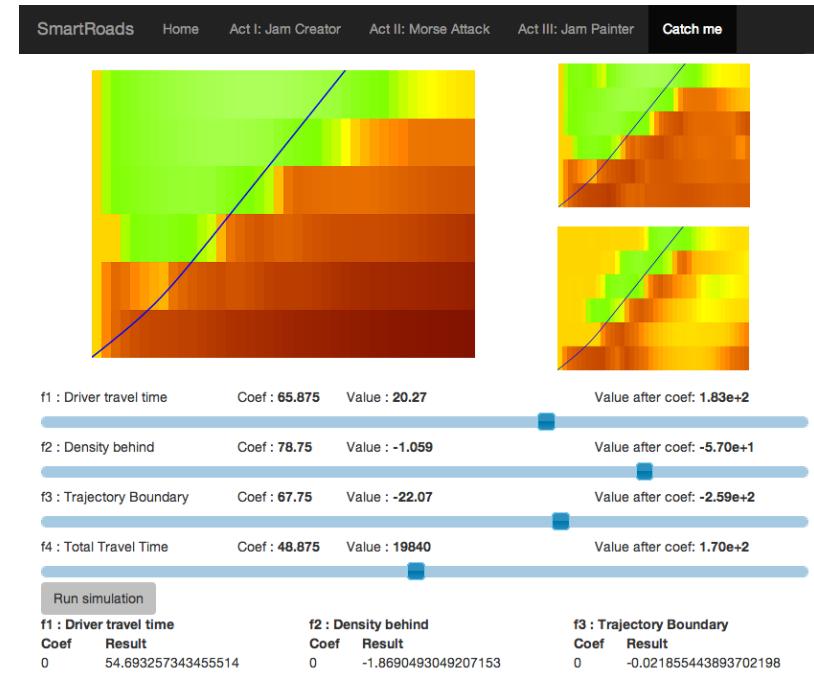
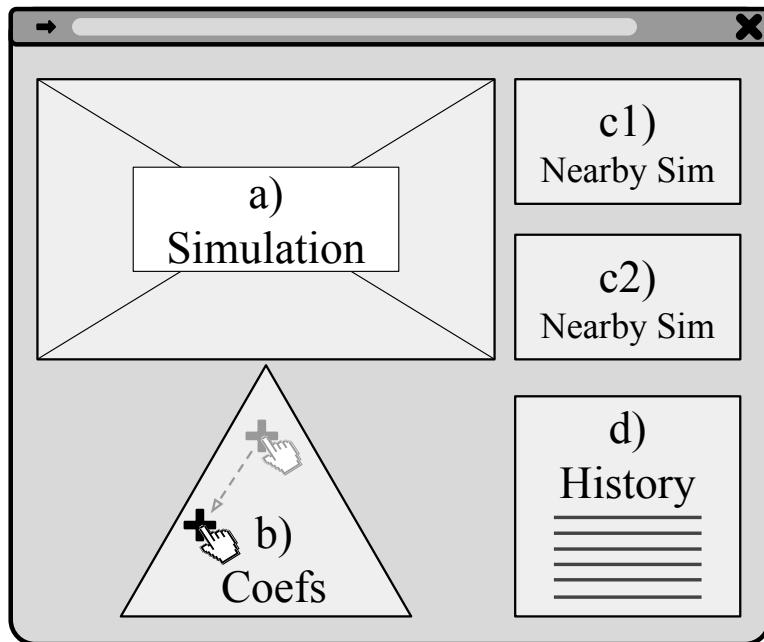
Interactive Optimization

- * Use human expertise to find proper a_i coefficients during exploration



Interactive Optimization

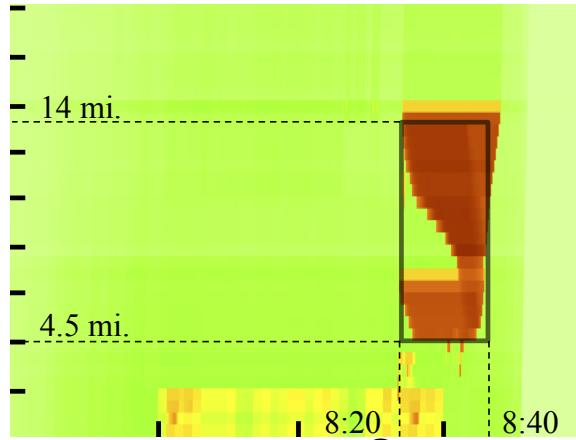
- * Use human expertise to find proper a_i coefficients



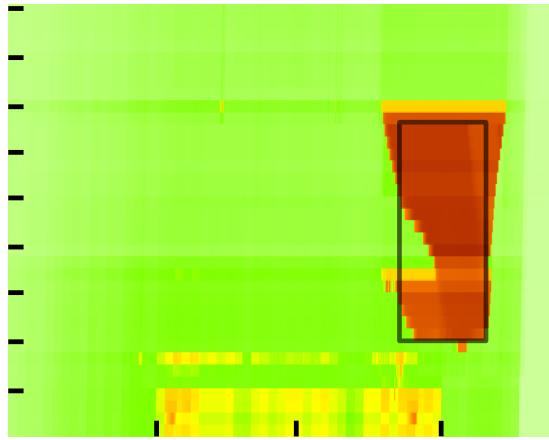
Box Attack Sim: I15 Freeway in San Diego

- * Create isolated, precise jam over predetermined time.
- * Balance between maximizing jam in “box” and minimizing free-flow outside box.

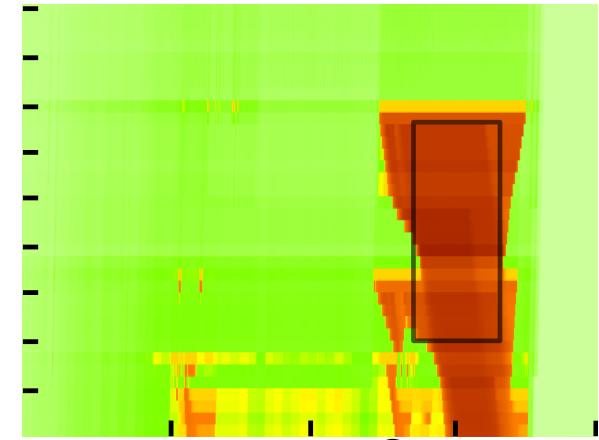
$$f = \alpha f_{\text{jam box}} + (1 - \alpha) f_{\text{clear outside box}}$$



$\alpha = .3$

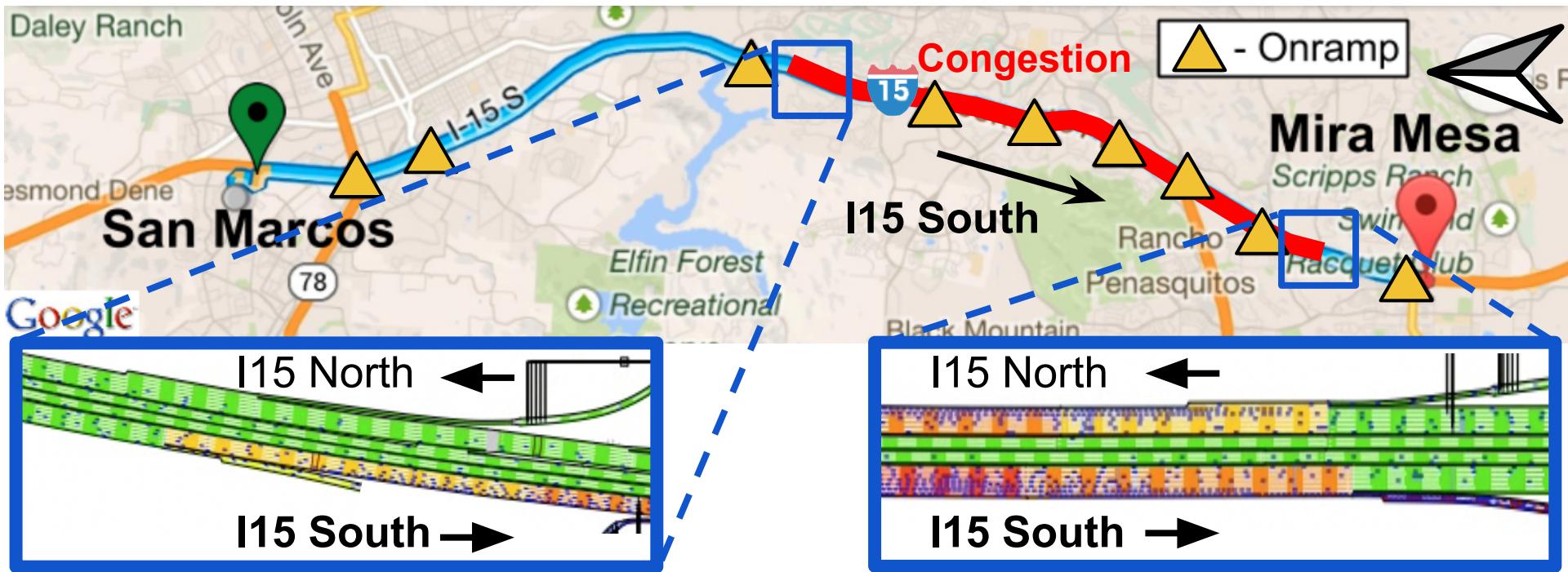


$\alpha = .5$



$\alpha = .9$

Box Attack Sim: I15 Freeway in San Diego

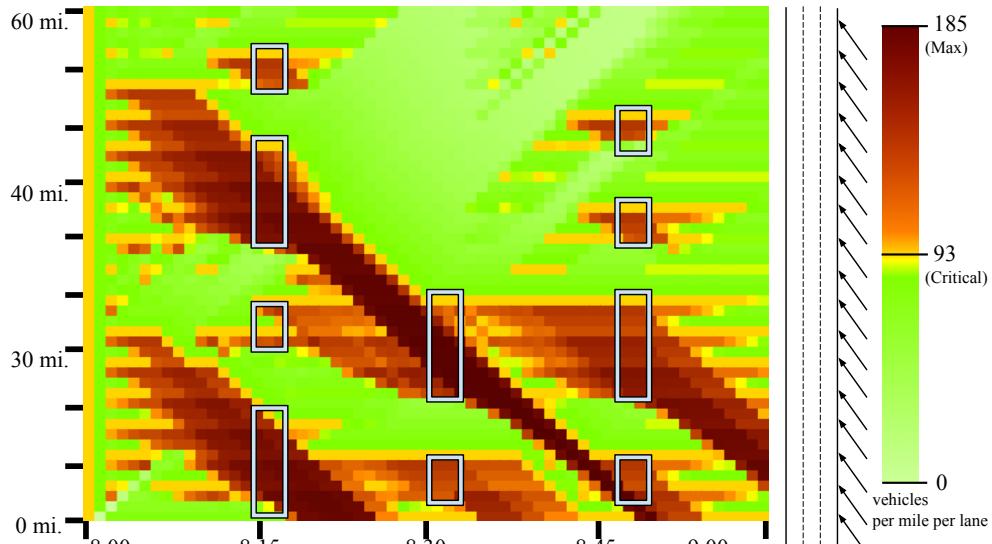


Box Attack Sim: I15 Freeway in San Diego

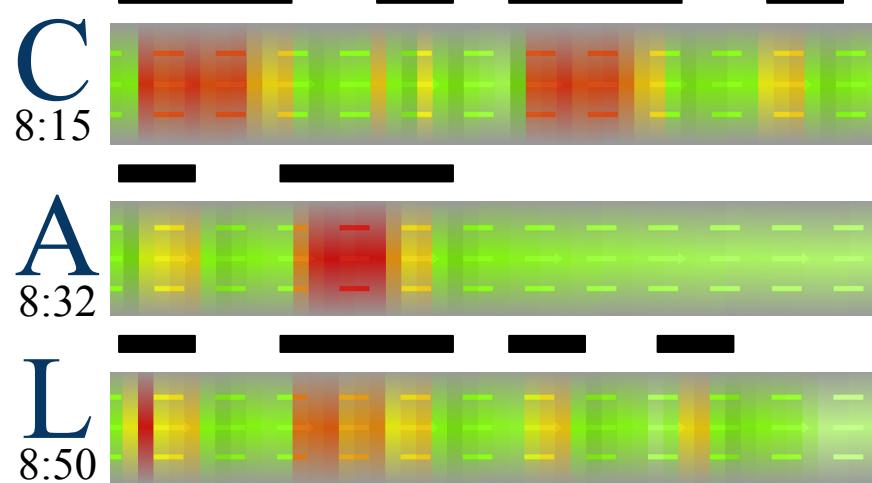


Morse Code Attack on the Freeway

- * Use Box Objective is “building block” for more sophisticated attacks
- * Example: Write Morse code on freeway with traffic jams



Space-time Diagram



Time Slices along Freeway

Morse Code Attack on the Freeway

SmartRoads: Hacking Freeway Congestion

Home

Freeway Speed Viewer

Act I: Jam Creator

Act II: Morse Attack

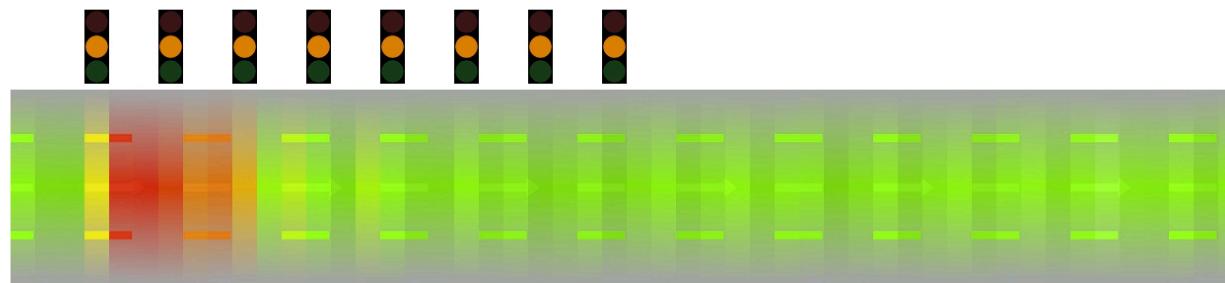
Act III: Jam Painter

Type your initials and watch a "personalized" jam take place along the freeway.

[Continue to Act III](#)



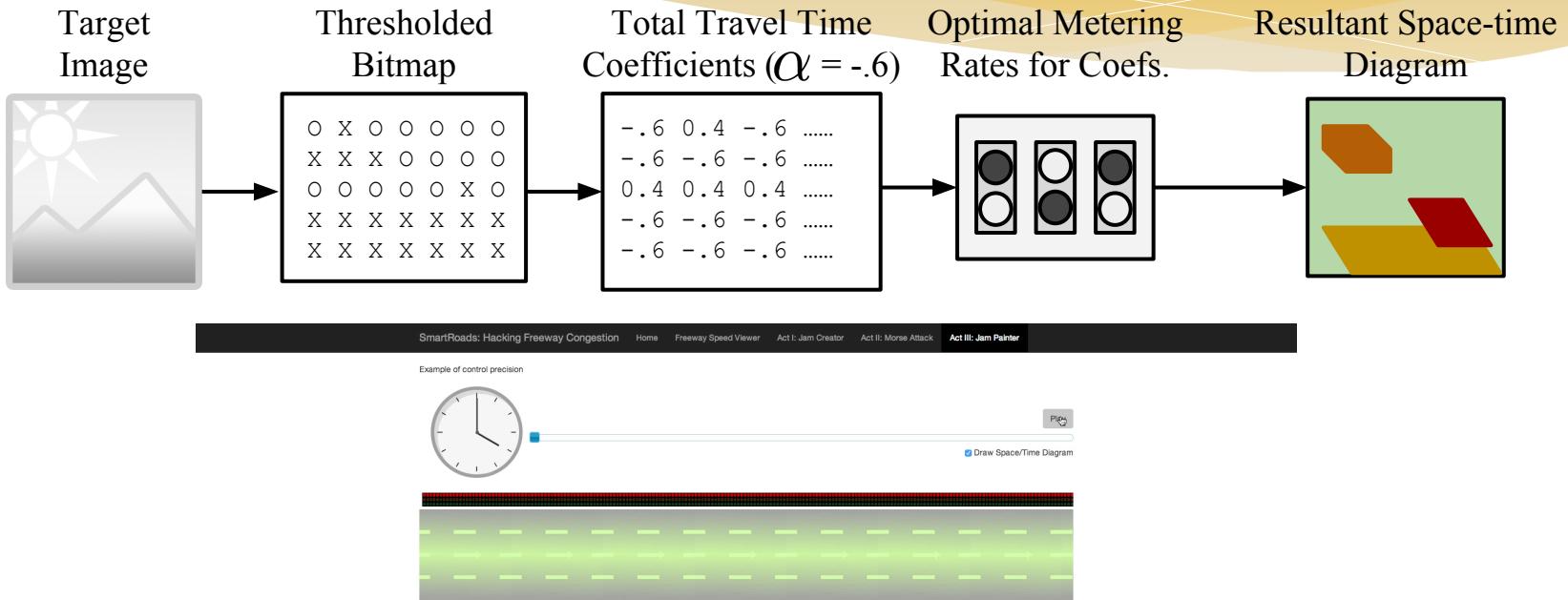
Play



[Console Log]

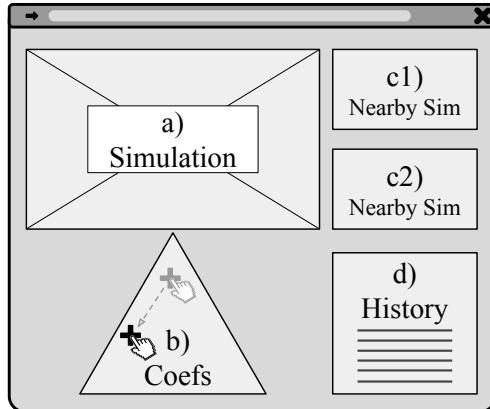
```
pirate@hackysack.hack>> Your jam is ready to be simulated, take a close look
pirate@hackysack.hack>> Taking control of the freeway...
pirate@hackysack.hack>> Converting to morse...
pirate@hackysack.hack>> Analyzing your initials...
pirate@hackysack.hack>> Simulation loaded
pirate@hackysack.hack>> *** Demo 2 : write your initials ***
```

Drawing *Cal* On the Freeway

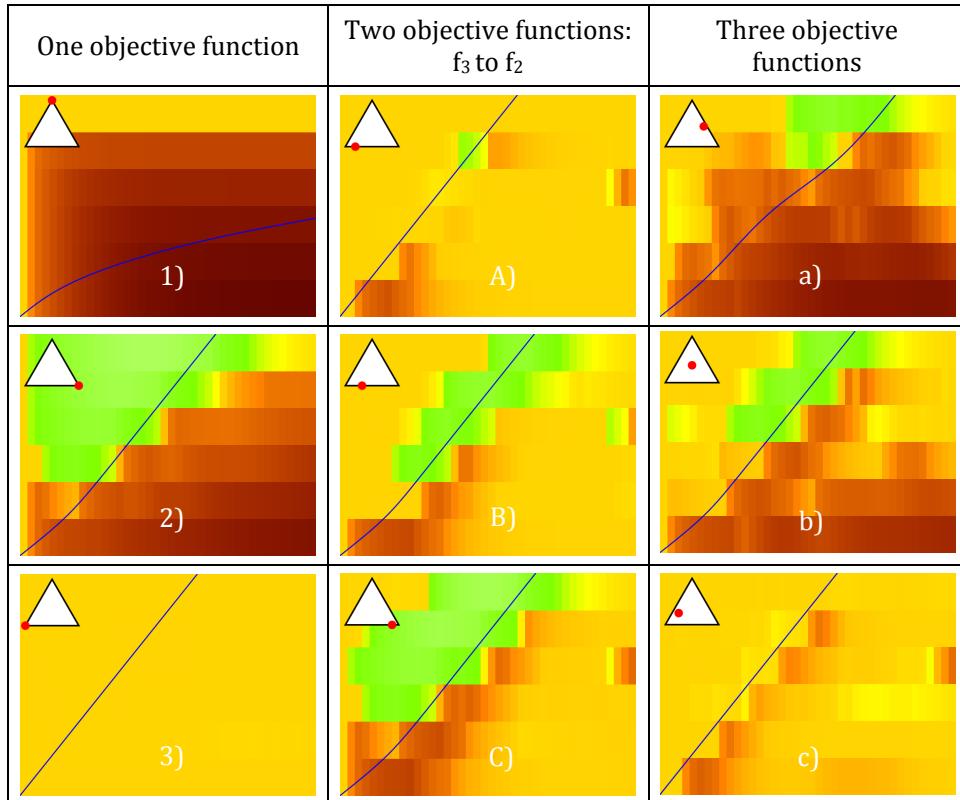
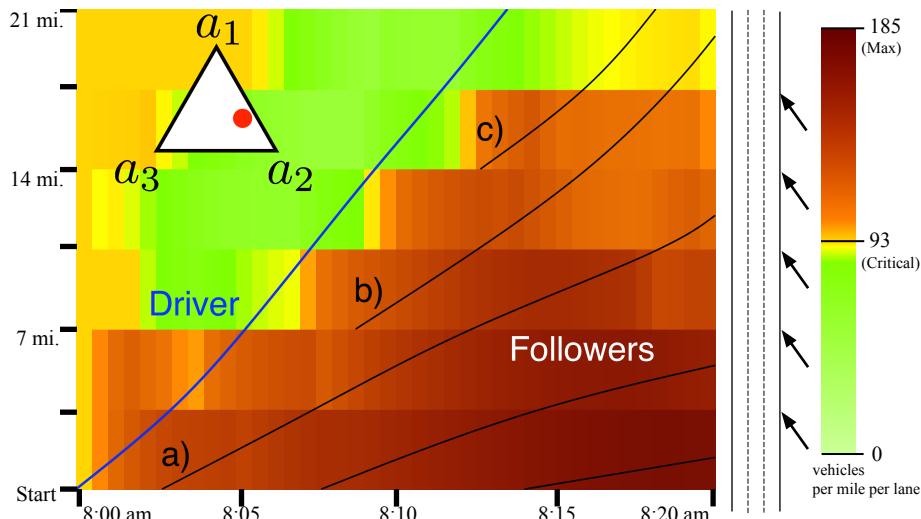


Attack Example: *CATCH ME IF YOU CAN*

- * Attacker wishes to escape vehicles chasing him.
- * Three objectives:
 - * f_1 Maximize congestion behind driver
 - * f_2 Maximize speed change **directly** behind driver trajectory
 - * f_3 Minimize travel time otherwise (avoid suspicion)

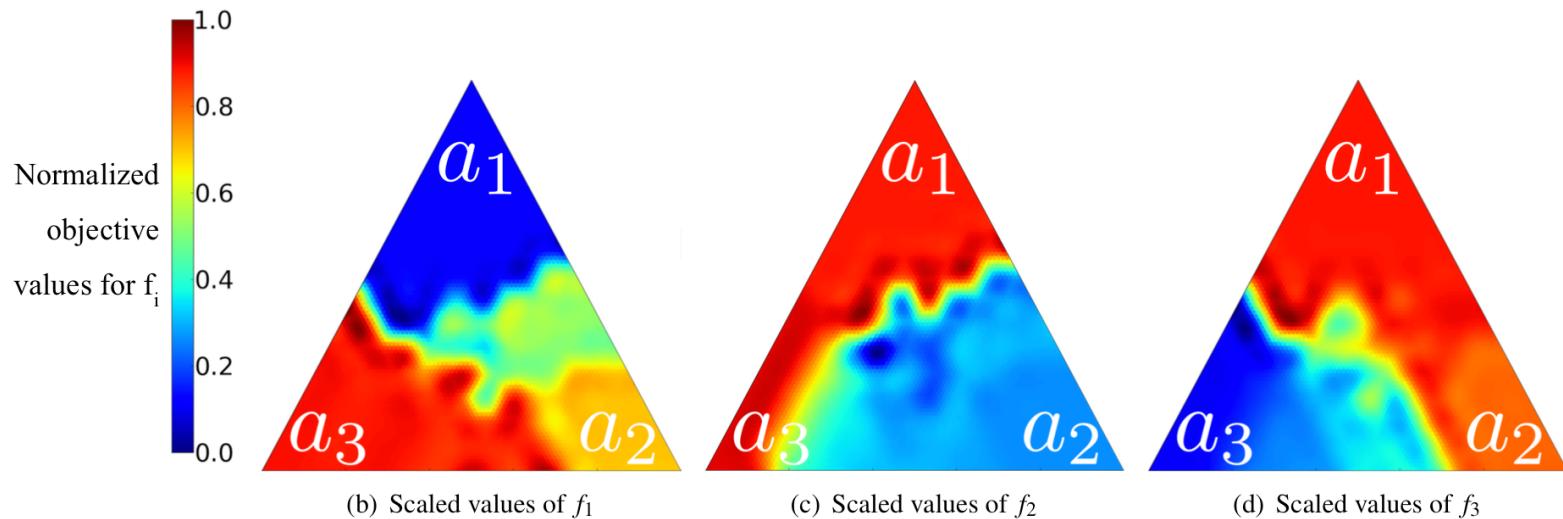


Attack Example: *CATCH ME IF YOU CAN*



A posteriori Optimization

- * Explore a_i space, creating a “representative” subset of Pareto solutions



Open Questions

- * Risk To Reward Ratio
 - * How costly to society are the attacks?
 - * How costly is the implementation of the attacks?
- * Connected Vehicles/Infrastructure Security
 - * What vulnerabilities exist when vehicles are in the loop?
- * Prevention
 - * How can we leverage knowledge traffic dynamics to prevent attacks?

Publications

- * Reilly, J., Martin, S., Payer, M., & Bayen, A. M. (2014). On Cybersecurity of Freeway Control Systems: Analysis of Coordinated Ramp Metering Attacks. *Transportation Research Part B Methodological*, (In Review)
- * Reilly, J., Krichene, W., Delle Monache, M. L., Samaranayake, S., Goatin, P., & Bayen, A. M. (2014). Adjoint-based optimization on a network of discretized scalar conservation law PDEs with applications to coordinated ramp metering. *Journal of Optimization Theory and Applications* (under Review).
- * Reilly, J., & Bayen, A. M. (2014). Distributed Optimization for Shared State Systems: Applications to Decentralized Freeway Control via Subnetwork Splitting. *Journal of Computational Physics* (In Preparation).
- * Delle Monache, M. L., Reilly, J., Samaranayake, S., Krichene, W., Goatin, P., & Bayen, A. M. (2014). A PDE-ODE model for a junction with ramp buffer. *SIAM Journal on Applied Mathematics*, 74(1), 22-39.

Thank you for listening!

Questions?