

## SPICE

SPICE is a general purpose simulation program that simulates different circuit and can perform various analysis of electrical and electronic circuits including Time domain response, frequency response, <sup>total power dissipation,</sup> determination of nodal voltage and branch current in a circuit, Transient analysis and determination of Transfer function etc.

The full form of SPICE is Simulation Program <sup>with</sup> Integrated Circuit Emphasis / Analysis.

PSPICE is one form of SPICE for personal computers available in different operating system such as DOS, Windows and UNIX.

The SPICE was first developed at University of California, Berkeley in mid 1970.

It is used as a tool for analysis, design and for testing of integrated, electrical and electronic circuits.

In SPICE we don't write the circuit equation, but describe the circuit using ASCII Text.

### Structure of circuit file

Title: One line for problem identification, e.g. Transient Analysis

Element Statement: These identify element types, element values and node to node connection.

Control Statement: This specifies types of analysis, e.g. DC, AC or Transient analysis, Frequency analysis.

End Statement: Indicates the end of data flow.

### The basic structure of Element Statement

Each element in the circuit have a specific element statement which contains the element name, the circuit nodes to which the elements are connected and values of the parameter.

#### Element name

R → Register

L → Inductor

C → Capacitor

D → Diode

V → Independent Voltage Source

I → Independent Current Source

Q → BJT

B → FET

There are 4 dependent sources —

G → Voltage Control Current Source

E → Voltage Control Voltage Source

F → Current Control Current Source

H → Current Control Voltage Source

K → Coupling factor

Nodes: It is a junction point of 2 circuit elements or source.

Any value → 1 - 999

0 → datum node (Reference Node)

The node must be non-negative.

## Values of an Element:



R1       $10 \rightarrow$  for  $10\Omega$   
 $10K \rightarrow$  for  $10K\Omega$   
 $10M \rightarrow$  for  $10M\Omega$

pico  $\rightarrow p 10^{-12}$

micro  $\rightarrow \mu 10^{-6}$

nano  $\rightarrow n$

milli  $\rightarrow m$

Kilo  $\rightarrow K$

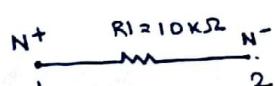
Giga  $\rightarrow G$

Tera  $\rightarrow T$

Mega  $\rightarrow M\Omega$

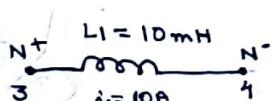
## Representation of Different Component in SPICE:

### Resistor:



Name	N <sup>+</sup>	N <sup>-</sup>	Value
R1	1	2	10K

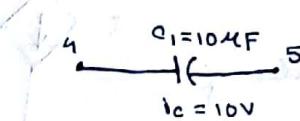
### Inductor:



Name	N <sup>+</sup>	N <sup>-</sup>	Value	IC
L1	3	4	10 m	10

Initial Condition  
 (Should be written if needed)  
 Don't write  $\rightarrow$  if not given

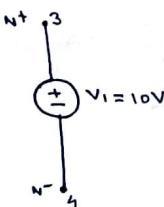
### Capacitor:



Name	N <sup>+</sup>	N <sup>-</sup>	Value	IC
C1	4	5	10μF	10

Energy Source:

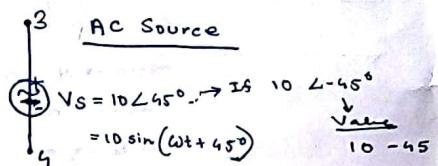
i) Independent Voltage Source:



Name N<sup>+</sup> N<sup>-</sup> Type Value

$V_1$

3 4 DC 10



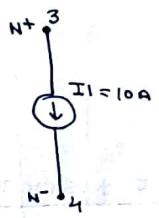
Name N<sup>+</sup> N<sup>-</sup> Type Value

$V_S$

3 4 AC 10 45

↓ magnitude Angle

ii) Independent Current Source:



Name N<sup>+</sup> N<sup>-</sup> Type Value

$I_1$

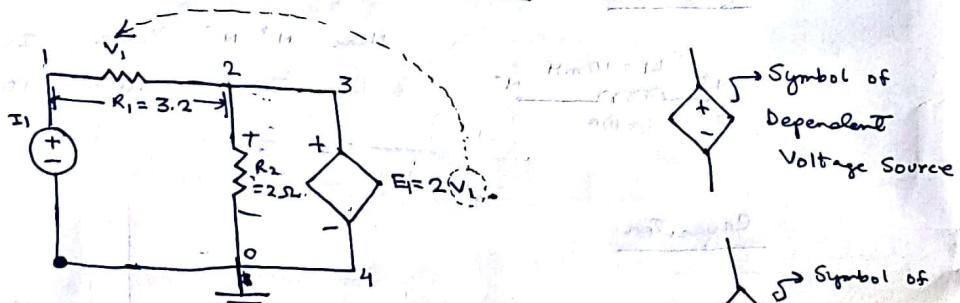
3 4 DC 10 } For DC Current Source

$I_S$

3 4 AC 10 45 } For AC Current Source

iii) Dependent Source:

a) Voltage control Voltage Source:



$E_1$  is changed by changing the value of another voltage source  $V_1$ .

Symbol of Dependent Voltage Source

Symbol of Dependent Current Source

Controlling Voltage +ve Node

Controlling Voltage -ve Node

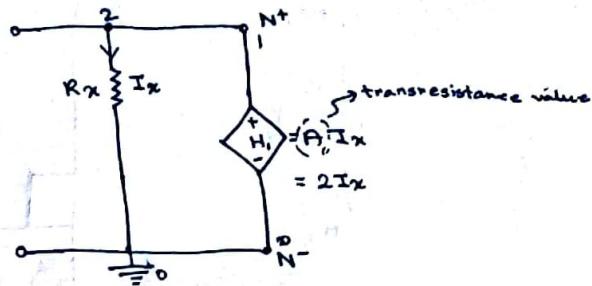
Gain Value

Name N<sup>+</sup> N<sup>-</sup> N<sub>c</sub><sup>+</sup> N<sub>c</sub><sup>-</sup> Gain Value

$E_1$

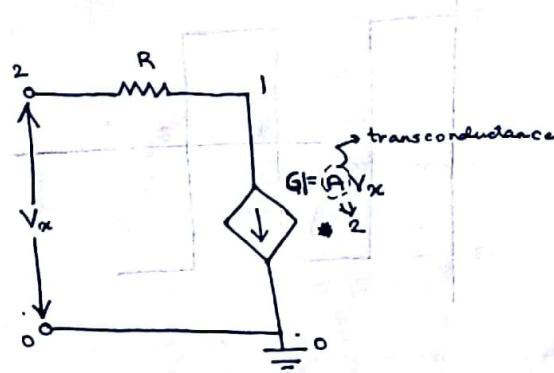
3 4 1 2 40 2

b) Current Control Current Source:



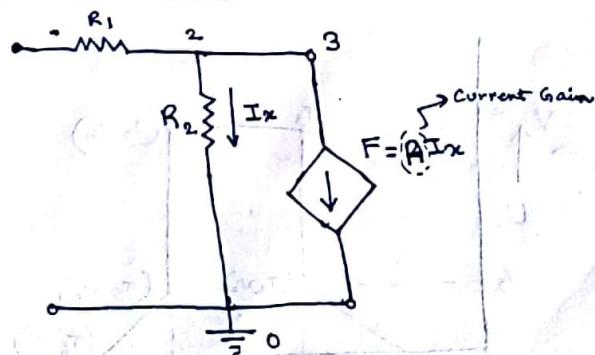
Name	N <sup>+</sup>	N <sup>-</sup>	N <sup>+</sup>	N <sup>-</sup>	A
H <sub>1</sub>	1	0	2	0	2

c) Voltage Control Current Source:



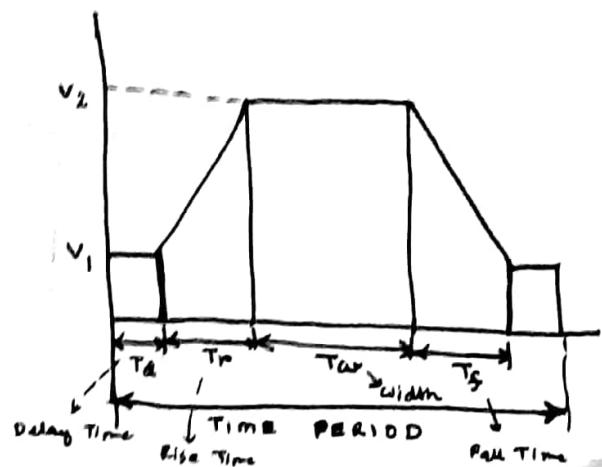
Name	N <sup>+</sup>	N <sup>-</sup>	N <sup>+</sup>	N <sup>-</sup>	A
G <sub>1</sub>	1	0	2	0	2

d) Current Control Current Source:



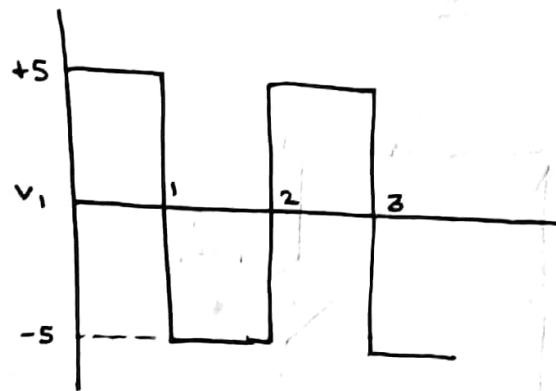
Name	N <sup>+</sup>	N <sup>-</sup>	N <sup>+</sup>	N <sup>-</sup>	Gain value
F <sub>1</sub>	3	0	2	0	A

## Pulse Source



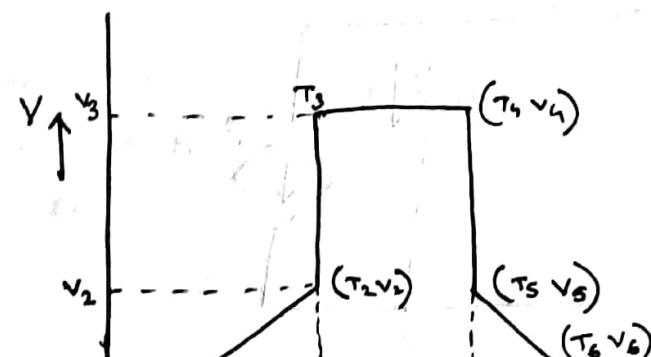
Voltage label  $\downarrow N_1^+ \quad N_2^- :$

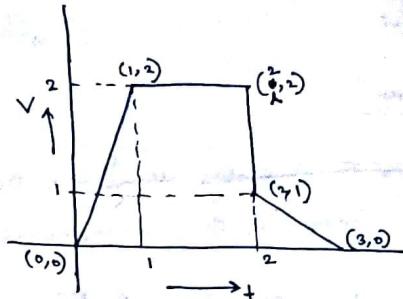
PULSE ( $v_1 \quad v_2 \quad T_d \quad T_r \quad T_f \quad T_w \quad \text{PERIOD}$ )



$v_1 \quad 1 \quad 2 \quad \text{PULSE} (-5 \quad +5 \quad 1\text{ns}, 1\text{ns} \quad 1\text{ns}, 1\text{s} \quad 2\text{s})$

## Piecewise Linear Independent Source (PWL)





$$V_1 \quad N^+ \quad N^- \quad PWL(00, 12, 22, 21, 30)$$

### SIN Source

$$v(t) = V_o + V_a e^{-(t-T_d)\alpha} \left[ \sin 2\pi f(t-T_d) - \theta \right]$$

DC

$V_o$  is the offset voltage

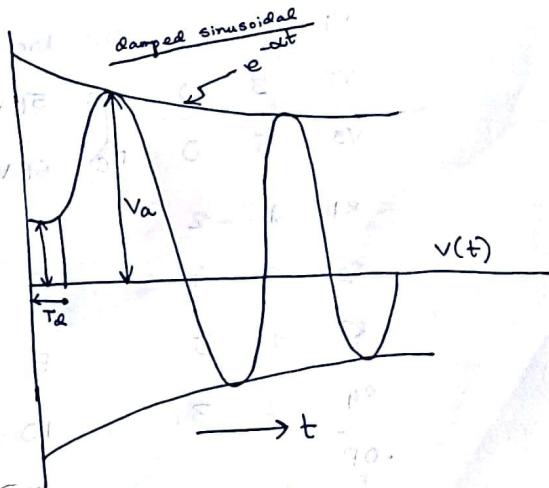
$V_a$  is the peak voltage

$f$  = frequency

$T_d$  = delay time

$\alpha$  = damping factor

$\theta$  = phase delay



$$v(\text{wave}) \quad N^+ \quad N^- \quad \sin(V_o, V_a, f, T_d, \alpha, \theta)$$

Transistor in this case is doped

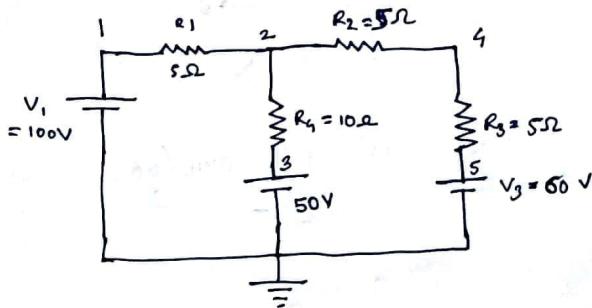
Conduction band  $\rightarrow$  Conduction band

Conduction band  $\rightarrow$  Valence band

Control Statement

1. DC Analysis:

i) .OP → ~~To find the DC operating points of all independent sources, measure the node voltages.~~ <sup>find</sup>

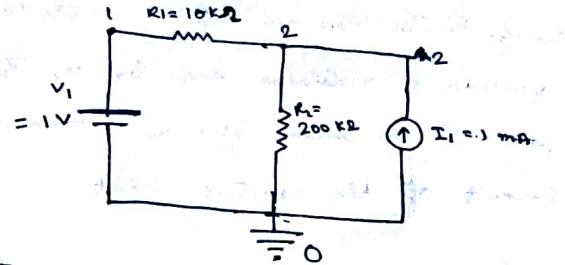


V1	1	0	DC	100V
V2	3	0	DC	50V
V3	5	0	DC	60V
R1	1	2		5
R2	2	4		5
R3	4	5		5
R4	2	3		10
.OP				
.End				

ii) .DC → ~~To vary the voltage source amplitude from starting value to final value with an increment.~~ <sup>current source</sup>

.DC <source name> <initial value> <final value> <increment>

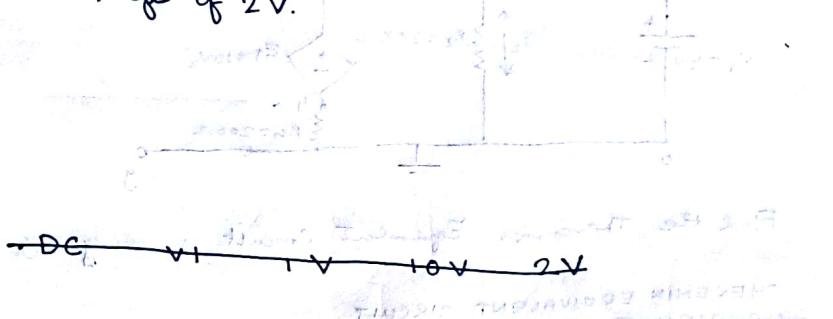
.DC	V1	1V	10V	1V
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Taking the

Unit

WAP and find the voltage between nodes 1 and 2, and the current through  $V_1$  where the voltage  $V_1$  varies from 1 to 10V, in steps of 2V.



### DC CIRCUIT

$V_1$  1 0 DC 1V

$R_1$  1 2 10k

$R_2$  2 0 200k

$I_1$  0 2 DC 1mA

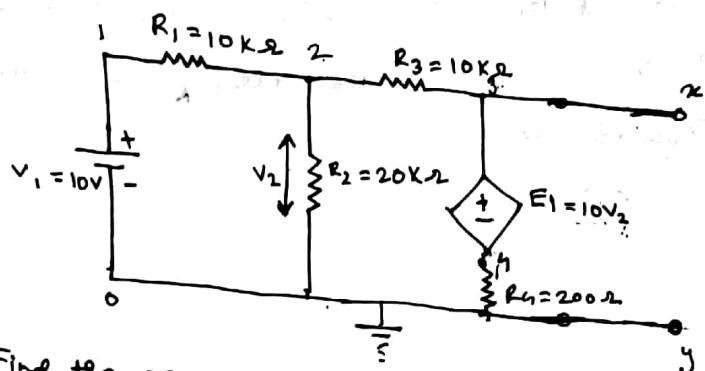
DC  $V_1$  1V 10V 2V

PRINT DC  $V(1,2)$ ,  $I(V_1)$

End

iii)  $\cdot \text{TF} \rightarrow$  gives Transfer function from an input variable to output variable and produces a resistance seen by the two voltage sources. It can also give a Thvenin's equivalent circuit of the resistive circuit.

$\cdot \text{TF}$        $\langle \text{output variable} \rangle$        $\langle \text{input source name} \rangle$



Find the Thvenin's Equivalent circuit across  $x$   $y$ .

~~THEVENIN EQUIVALENT CIRCUIT~~

~~V1      1      0      DC      10 V~~      THEVENIN CIRCUIT

~~E1      3      4      2      0      10 V~~      THEVENIN CIRCUIT

~~R1      1      2      10 k~~      THEVENIN CIRCUIT

~~R2      2      0      20 k~~      THEVENIN CIRCUIT

~~R3      2      3      10 k~~      THEVENIN CIRCUIT

~~R4      4      0      200~~      THEVENIN CIRCUIT

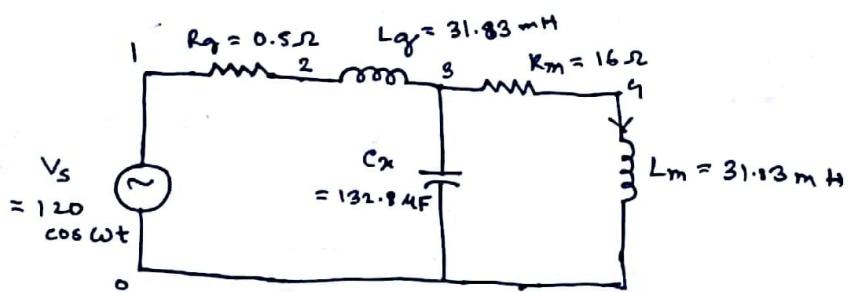
$\cdot \text{TF}$        $V(3,0)$        $V_1 \rightarrow$  Input Voltage

• End

## 2. AC Analysis:

i) AC → Obtain frequency analysis.

- .AC < sweep type > < no. of points > < starting frequency >
- LIN (linear)
- OCT (octave)
- DEC (decade)
- < stop frequency >



Find the voltage across  $\Rightarrow$  2 inductor and capacitor.

### AC CIRCUIT

$V_s$  1 0 AC 120 0

$R_g$  1 2 0.5

$L_g$  2 3 31.83 m  $I_C = 0$

$R_m$  3 4 16

$L_m$  4 0 31.13 m  $I_C = 0$

$C_x$  3 0 132.84 F  $I_C = 0$

.AC LIN 10 ~~50~~ 60 70

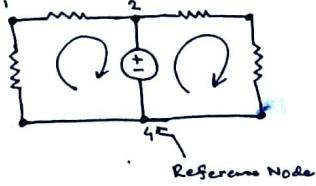
.PRINT AC ~~VM(2,3)~~, VP(2,3), IM(~~LM~~), IP(~~LM~~),

.End

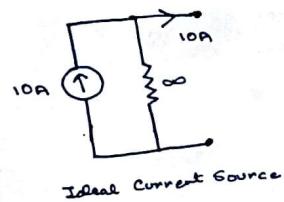
VM(~~CX~~), VP(~~CX~~)

## Circuit Theory

### Graph Theory



Ideal Voltage Sources  $\rightarrow$  Zero Internal Resistance



Undirected Graph

If directions are present  $\rightarrow$  Oriented/Directed Graph

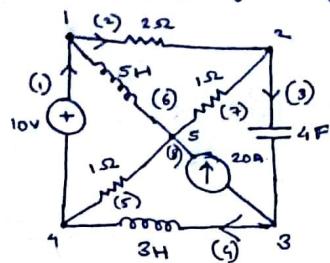
- If no direction is given and we want to draw a directed graph, then we can choose any direction as per our choice.

Rank of a graph:  $(n-1)$

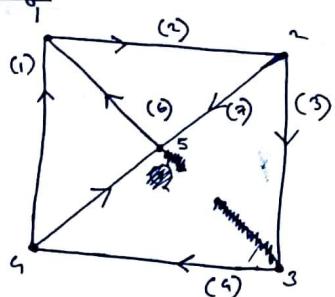
no. of nodes

Subgraph: Will have  $\frac{\text{subset}}{\text{Total}}$  of the Total nodes and edges.

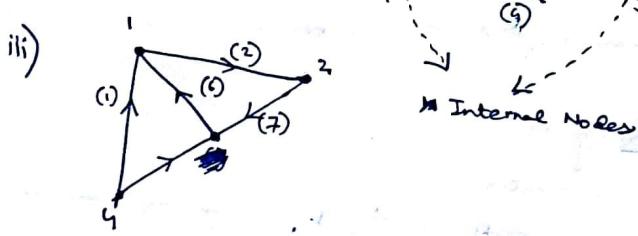
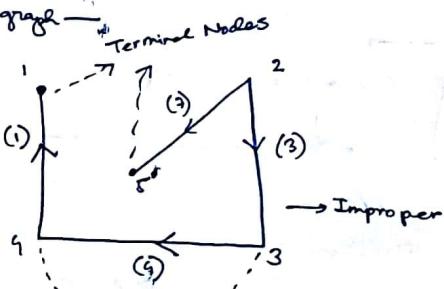
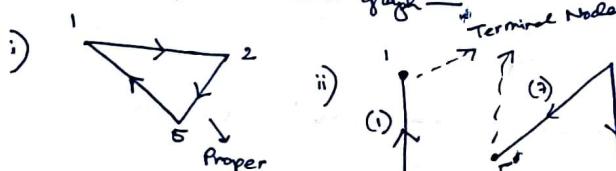
• draw the graph of the given circuit —



Graph —

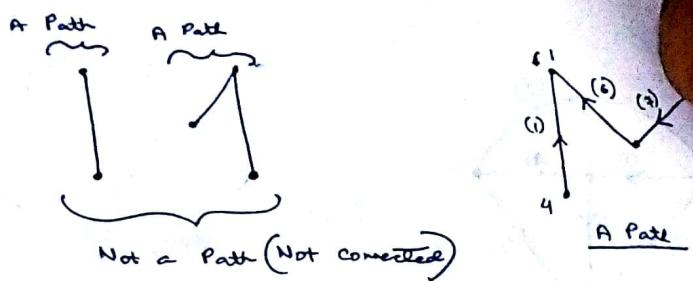


Subgraph of the above graph —

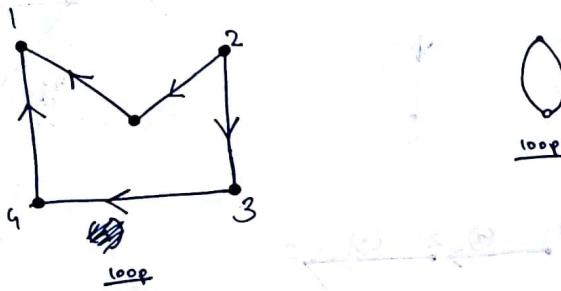


Proper Subgraph → No. of Nodes and Branches are strictly less than that of the main graph.

A Path is a subgraph consisting of an ordered sequence of branches having two terminal nodes at two ends and having all remaining nodes as internal nodes.



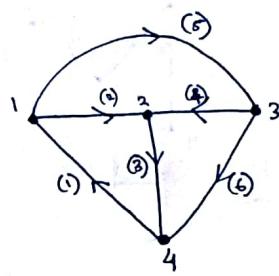
If two terminal nodes of a path coincide with each other, a closed path is formed which is called a loop.



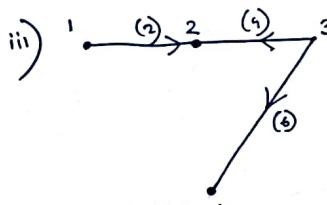
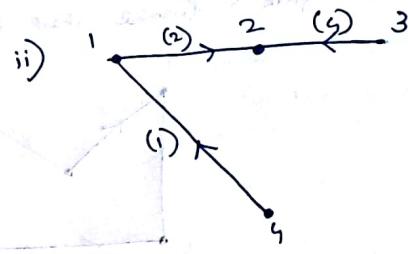
### Properties of Loop:

- i) Loop is a subgraph
- ii) All the nodes present in the loop are internal nodes.
- iii) No. of nodes and no. branches are equal in a loop
- iv) There exists two paths between any pair of nodes.
- v) Minimum two branches are required to form a loop.

Tree is a subgraph having all the nodes of the original graph, but no loop will be present.



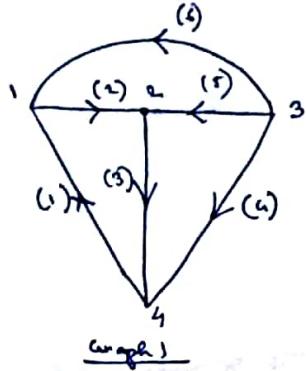
Draw some trees



## Properties of Tree:

- 1) Tree is a connected subgraph.
  - 2) All the nodes should be present, but no loops should be present
  - 3) No. of branches present in a tree is  $(n-1)$ , where  $n$  is the no. of nodes.
  - 4) There exists only 1 path between any pair of nodes.
  - 5) Rank of the tree is  $(n-1)$ .
  - 6) Every connected graph will have atleast one tree.

### Co-tree

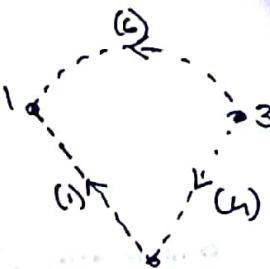
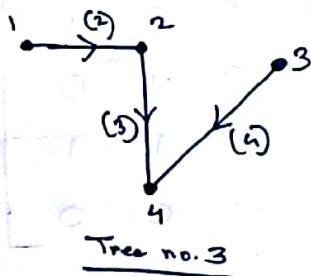
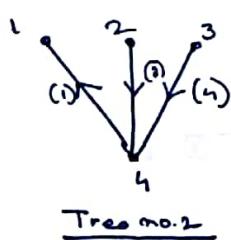
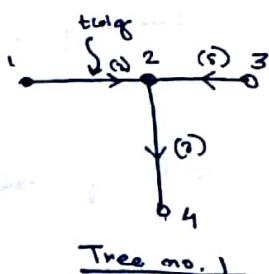
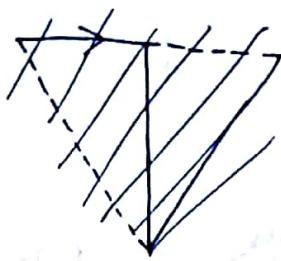


no. of nodes =  $n$

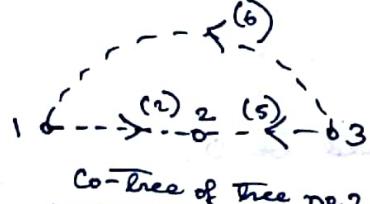
no. of branches =  $b$

no. of twigs =  $n - 1$

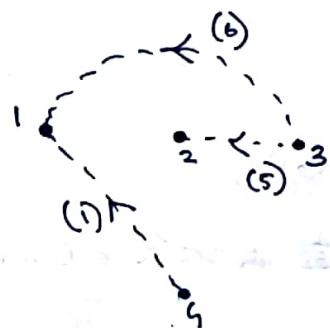
$$\begin{aligned} \text{no. of links} &= b - (n - 1) \\ &= b - (n + 1) \end{aligned}$$



Co-tree of tree no. 1



Co-tree of tree no. 2



Co-tree of tree no. 3

Co-tree is the remaining part of the graph that is left once the tree is removed from the original graph.

### Complete Incidence Matrix (CIM)

$$A_a = \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}_{n \times b}$$

Each element  $a_{hk} = +1$  if branch  $k$  is connected to node  $h$  and  
no. of node no. of branch directed away from node  $h$   
 $= -1$  if " " " " " " " " directed towards node  $h$   
 $= 0$  if branch  $k$  is not connected to node  $h$

Consider graph (i),

$$A_a = \begin{bmatrix} & (1) & (2) & (3) & (4) & (5) & (6) \\ 1 & -1 & 1 & 0 & 0 & 0 & -1 \\ 2 & 0 & -1 & 1 & 0 & -1 & 0 \\ 3 & 0 & 0 & 0 & 1 & 1 & 1 \\ 4 & 1 & 0 & -1 & -1 & 0 & 0 \end{bmatrix}$$

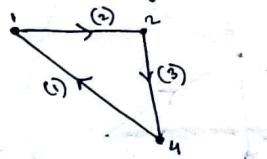


### Properties of CIM :

- 1) Rank of CIM is  $(n-1)$ .
- 2) Sum of the entries in each column should be 0.
- 3) Determinant of CIM of any closed loop is 0.



Take any closed loop -



$$\begin{matrix} & (1) & (2) & (3) \\ 1 & \begin{bmatrix} -1 & -1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & -1 \end{bmatrix} & \therefore \text{Determinant} \\ 2 & & = -1(-1-0) * -1(1-0) \\ 4 & & = 1-1 * +0 \\ & & = 0 \end{matrix}$$

### Reduced Incidence Matrix

$A \rightarrow$  Notation

$$A = \begin{bmatrix} \end{bmatrix}_{(n-1) \times b}$$

A row from CIM may be absent here.

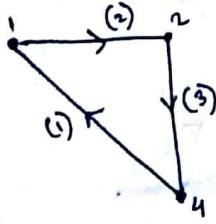
For nodal analysis, one node ~~is~~ is selected as reference node,  
and hence it ~~is~~ omitted. In this case we use RIM.

For RIM, sum of each column  $\neq 0$ .

$$RIM = \begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 & -1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & -1 & 1 & -1 \\ 0 & 0 & 0 & 1 & 0 & 0 & -1 & 0 \end{bmatrix} \rightarrow RIM$$

$$CIM = \begin{bmatrix} (1) & (2) & (3) & (4) & (5) & (6) & (7) & (8) \\ 1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 1 \\ 2 & 0 & 1 & 0 & 0 & -1 & 1 & 0 & 0 \\ 3 & 0 & 0 & 1 & 0 & 0 & -1 & 1 & -1 \\ 4 & 0 & 0 & 0 & 1 & 0 & 0 & -1 & 0 \\ 5 & -1 & -1 & -1 & -1 & 0 & 0 & 0 & 0 \end{bmatrix} \rightarrow CIM$$

Take any closed loop -



$$\begin{matrix} & (1) & (2) & (3) \\ \begin{matrix} 1 \\ 2 \\ 4 \end{matrix} & \left[ \begin{matrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{matrix} \right] & \therefore \text{Determinant} \\ & & = -1(-1-0) * -1(1-0) \\ & & = 1 - 1 * +0 \\ & & = 0 \end{matrix}$$

### Reduced Incidence Matrix

$A \rightarrow$  Notation

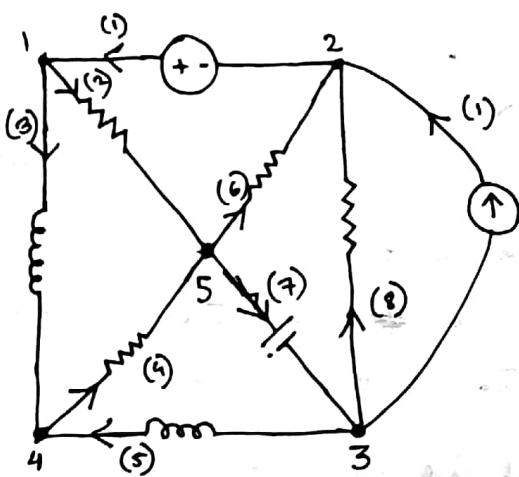
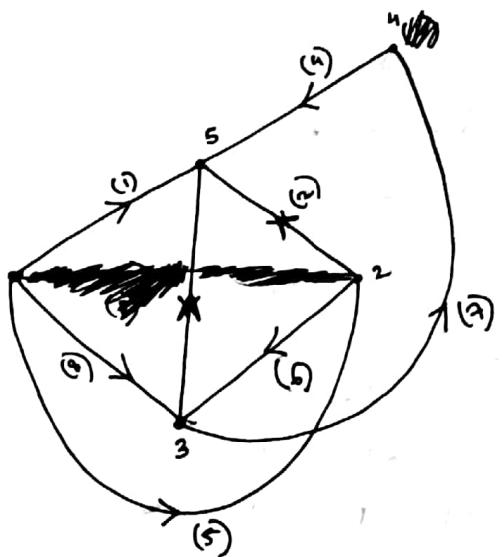
$$A = \left[ \begin{array}{c} \\ \end{array} \right]_{(n-1) \times 1}$$

A row from CIM may be absent here.  
For nodal analysis, one node ~~is~~ is selected as reference node,  
and hence it ~~is~~ omitted. In this case we use RIM.

For RIM, sum of each column  $\neq 0$ .

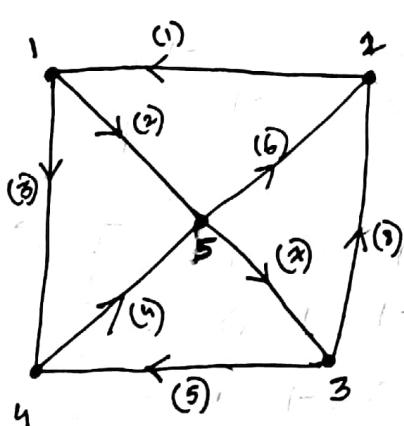
$$\begin{matrix} A &= & \left[ \begin{matrix} 1 & 0 & 0 & 0 & 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 & -1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & -1 & 1 & -1 \\ 0 & 0 & 0 & 1 & 0 & 0 & -1 & 0 \end{matrix} \right] \xrightarrow{\text{RIM}} \\ && \begin{matrix} (1) & (2) & (3) & (4) & (5) & (6) & (7) & (8) \end{matrix} \end{matrix}$$

$$A_a = \left[ \begin{matrix} 1 & 0 & 0 & 0 & 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 & -1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & -1 & 1 & -1 \\ 0 & 0 & 0 & 1 & 0 & 0 & -1 & 0 \\ -1 & -1 & -1 & -1 & 0 & 0 & 0 & 0 \end{matrix} \right] \xrightarrow{\text{CIM}}$$



draw the graph.

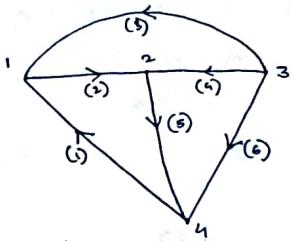
Then find cim.



$$A_a = \begin{bmatrix} (1) & (2) & (3) & (4) & (5) & (6) & (7) & (8) \\ 1 & -1 & 1 & 1 & 0 & 0 & 0 & 0 \\ 2 & 1 & 0 & 0 & 0 & 0 & -1 & 0 \\ 3 & 0 & 0 & 0 & 0 & 1 & 0 & -1 \\ 4 & 0 & 0 & -1 & 1 & -1 & 0 & 0 \\ 5 & 0 & -5 & 0 & -1 & 0 & 1 & 1 \\ 6 & & & & & & & 0 \end{bmatrix}$$

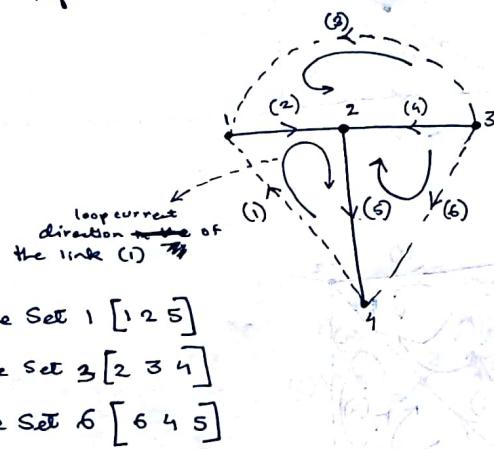


### Tie-Set Matrix or Fundamental Loop Matrix or f-loop Matrix



Step 1: Select a tree

Step 2: Connect one link at a time to form a loop.



$$\text{Tie Set Matrix } B = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 & 0 \end{bmatrix}^T = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 & 0 \end{bmatrix} = (b-n+1) \times b$$

(b-n+1) × b  
no. of links

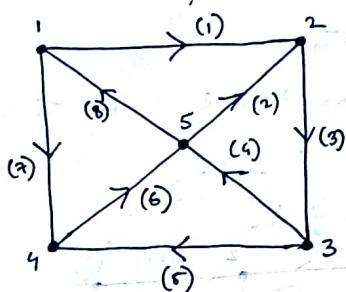
$b_{hk} = +1$  when branch  $k$  is present in tie set  $h$  ad direction of current is same as that of  $k$ .

$b_{hk} = -1$  when branch  $k$  is present in tie set  $h$  ad direction of current is same as the branch  $k$

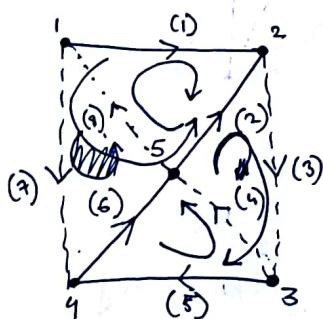
$= 0$  branch is not present

$$B = \begin{bmatrix} (1) & (2) & (3) & (4) & (5) & (6) \\ 1 & 1 & 0 & 0 & 1 & 0 \\ 0 & 1 & -1 & -1 & 0 & 0 \\ 0 & 0 & 0 & -1 & -1 & 1 \end{bmatrix}$$

2.



Trees:



Tie set 4 [4 5 6]

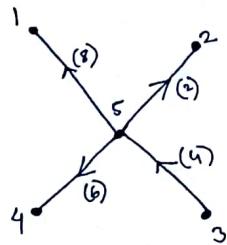
Tie set 8 [8 1 2]

Tie set 7 [7 2 6 1]

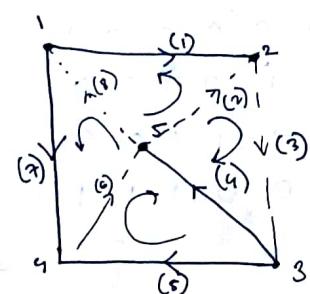
Tie set 3 [3 2 6 5]

$$B = \begin{bmatrix} (1) & (2) & (3) & (4) & (5) & (6) & (7) \\ 0 & 0 & 0 & 1 & -1 & -1 & 0 & 0 \\ 1 & -1 & 0 & 0 & 0 & 0 & 0 & 1 \\ -1 & 1 & 0 & 0 & 0 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 & 0 & 1 & 1 & 0 \end{bmatrix}$$

Tree 2:



Tree 3:



Tree 3:

Tie set 6  $[6 \ 4 \ 5]$

Tie set 8  $[8 \ 7 \ 5 \ 4]$

Tie set 2  $[2 \ 1 \ 7 \ 5 \ 4]$

Tie set 3  $[3 \ 5 \ 7 \ 1]$

$$B = \begin{bmatrix} (1) & (2) & (3) & (4) & (5) & (6) & (7) & (8) \\ TS6 & 0 & 0 & 0 & -1 & 1 & 1 & 0 & 0 \\ TS8 & 0 & 0 & 0 & 1 & -1 & 0 & 1 & 1 \\ TS2 & -1 & 1 & 0 & 1 & -1 & 0 & 1 & 0 \\ TS3 & 1 & 0 & 1 & 0 & 1 & 0 & -1 & 0 \end{bmatrix}$$

Tree 2:

Tri Set 1 [1 2 8]

Tri Set 3 [3 4 2] ~

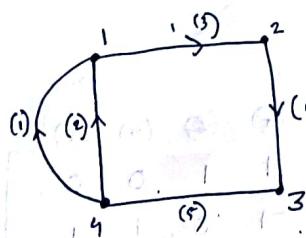
Tri Set 5 [5 6 4]

Tri Set 7 [6 7 8]

$$B = \begin{bmatrix} & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ \text{Tri Set 1} & 1 & -1 & 0 & 0 & 0 & 0 & 0 & 1 \\ \text{Tri Set 3} & 0 & 1 & 1 & 1 & 0 & 0 & 0 & 0 \\ \text{Tri Set 5} & 0 & 0 & 0 & -1 & 1 & 1 & 0 & 0 \\ \text{Tri Set 7} & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 \end{bmatrix}$$

Fundamental Cut Set Matrix or f-cut Set Matrix

? Minimal  
Minimum set of branches, removing which the rank of the graph is reduced by 1, and the graph is divided into 2 parts.



i. Rank =  $n-1 = 4-1 = 3$

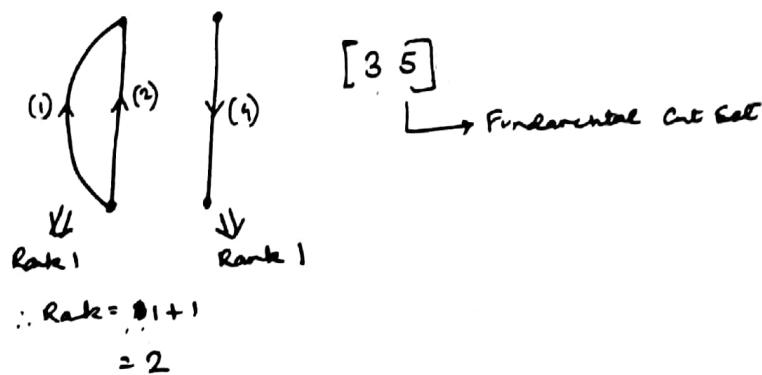
i) Suppose branch  $[1 \ 2 \ 4]$  is removed.

$$\therefore \begin{array}{c} 1 \xrightarrow{(5)} 2 \\ \text{---> Fundamental cut set} \\ \text{Rank} = 2-1=1 \end{array}$$

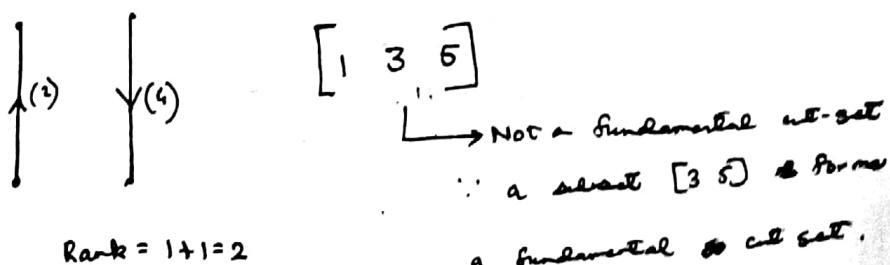
$$+ \xleftarrow{(5)} 3 \quad \text{---> Rank} = 2-1=1$$

$$\therefore \text{Rank} = 1+1=2 \quad \text{---> Decrease by 1}$$

ii)



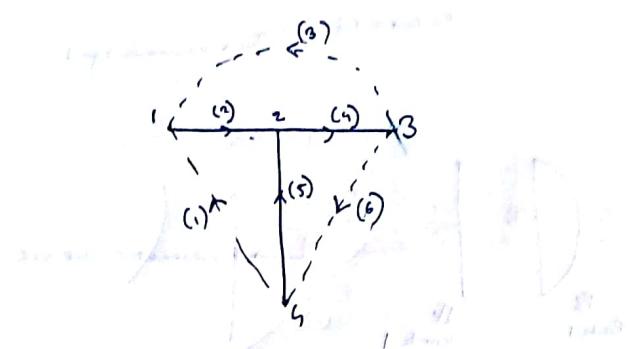
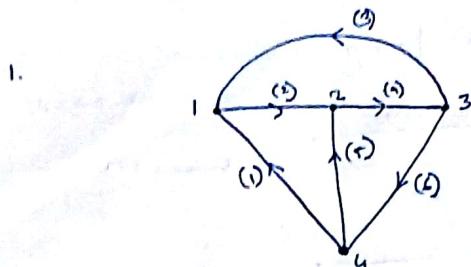
iii)



How to identify f-cut set?

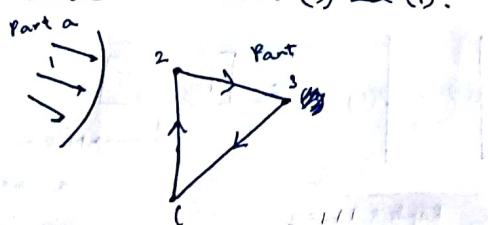
Step 1: Select a Tree

Step 2: Consider one Twig at a Time, remove that Twig along with other links



i) Consider twig (2).

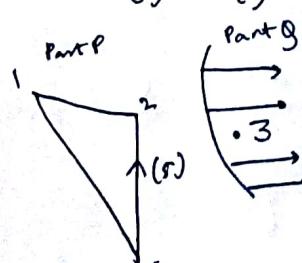
Remove it like links (3) and (1).



$f\text{-cut set } 2 [3 \ 2 \ 1]$

ii) Consider twig (4).

Remove links (3) and (6)



$f\text{-cut set } 4 [3 \ 4 \ 6]$

iii) Consider tube (5).  
Remove links (1) and (6).



$\delta$  cut set 5 [1 6 5]

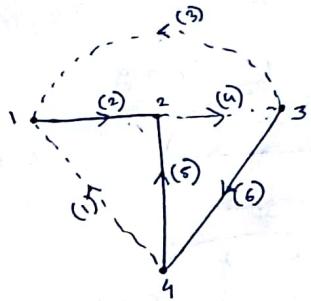


### Fundamental Cut Sets Method - Cut Set Matrix

$Q = q_{ik}$  = +1 present in cut set i, direction is same  
 at set no.      = -1    "    "    "    " i, absent. dir. is opposite  
 branch no.      = 0 absent in cut set i

$$Q = \begin{matrix} & (1) & (2) & (3) & (4) & (5) & (6) \\ \text{fc 2} & -1 & 1 & -1 & 0 & 0 & 0 \\ \text{fc 4} & 0 & 0 & -1 & 1 & 0 & -1 \\ \text{fc 5} & 1 & 0 & 0 & 0 & 1 & -1 \end{matrix}$$

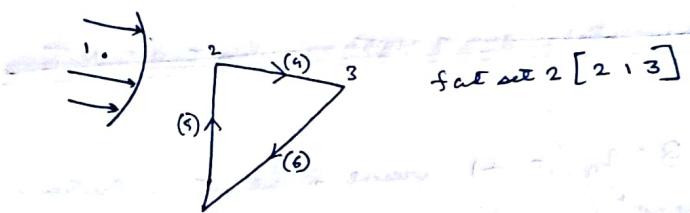
2.



3.

i) Consider twigs (2).

remove (3) and (1)



ii) Consider twig (5)

remove (1), (2), (3).

cut set 5 [5 4 1 3]

part x

Part Y

Part Z

Part W

iii) Consider twig (6).

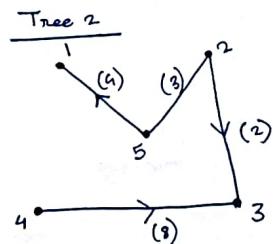
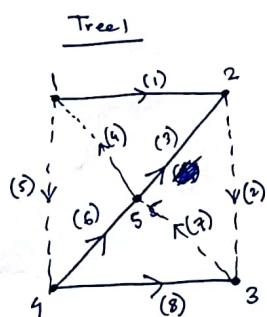
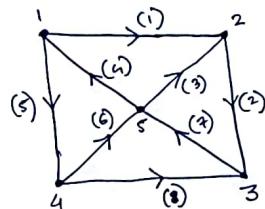
remove (3), (4).

cut set 6 [6 4 3]



$$Q = \begin{bmatrix} (1) & (2) & (3) & (4) & (5) & (6) \\ sc_2 & -1 & 1 & -1 & 0 & 0 & 0 \\ sc_5 & 1 & 0 & 1 & -1 & 1 & 0 \\ sc_6 & 0 & 0 & 1 & -1 & 0 & 1 \end{bmatrix}$$

3.

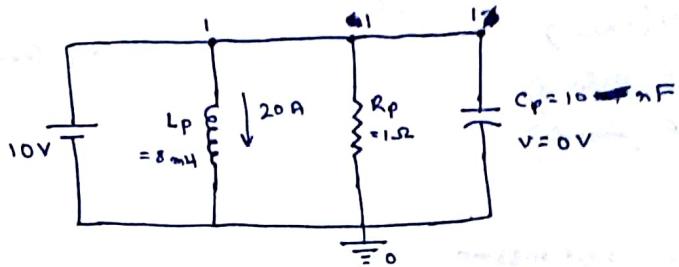


Tree 1  
Consider twig (7).

### 3. Transient Analysis:

increment  $\frac{0.1}{2}$   
 fine value  
 Using initial conditions  
 .TRAN T<sub>Step</sub> T<sub>Stop</sub> UIC

To perform transient analysis or transient response of the circuit.



Title: Transient Response

Rp 1 0 1

Lp 1 0 8m IC = 20 A

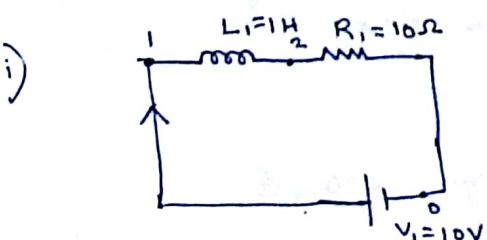
Cp 1 0 10n IC = 0 V

V 1 0 DC 10

.TRAN lower  $\frac{\zeta}{10}$  higher  $\zeta \times 10$  UIC

.PROBE

- End



$$\frac{L}{R} = \zeta_1$$

$$T_2 = RC$$

which ever of  $T_1$  and  $T_2$

is  $T_{stop}$ , i.e. the increment

Others one is the  $T_{start}$

Time =  $\frac{RC}{\zeta}$

$$\zeta = \frac{L}{R} = \frac{1}{10} = 0.1$$

Title: Transient Response of RL Circuit

V1 01 D DC 10

L1 1 2 1

R1 2 0 10

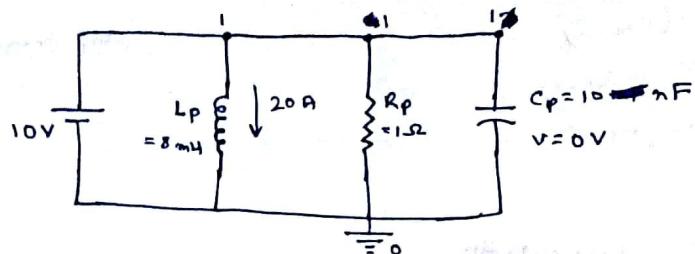
.TRAN 0.01 1 UIC

.PROBE

### 3. Transient Analysis:

.TRAN  $T_{Step}$   $T_{Stop}$  UIC  
 Increment  $\frac{1}{2} \Delta t$   
 And value  
 Using initial conditions

To perform transient analysis or transient response of the circuit.



Title: Transient Response

Rp 1 0

Lp 1 0 8m  $I_C = 20 \text{ mA}$

Cp 1 0 ~~10n~~  $I_C = 0 \text{ V}$

V 1 0 DC 10

$$\frac{L}{R} = T_1$$

$$T_2 = RC$$

Whichever of  $T_1$  and  $T_2$

$\Rightarrow T_{stop}$ , i.e. the increment

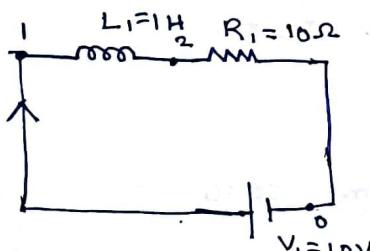
Others one is the  $T_{stop}$ .

.TRAN  $\frac{\text{lower } \tau}{10}$   $\frac{\text{higher } \tau \times 10}{10}$  UIC

.PROBE

.End

i)



$$\tau = \frac{L}{R} = \frac{1}{10} = 0.1$$

Title: Transient Response of RL Circuit

V1 0 1 D DC 10

L1 1 2 1

R1 2 0 10

.TRAN 0.01 1 UIC

.PROBE

.END

## Output Commands

### 1) .PRINT:

• PRINT DC  $I(R1)/VM(1,2)$  VP(1,2)  
• PRINT AC  $IM(R1) IP(R1)$

### 2) .PLOT:

Plot the ~~output~~ variables.

• PLOT DC  $I(R1)$   
• PLOT AC  $IM(R1) IP(R1)$   
• PLOT TRAN  $I(R1)$

### 3) .PROBE:

• Storing all variables in the file.

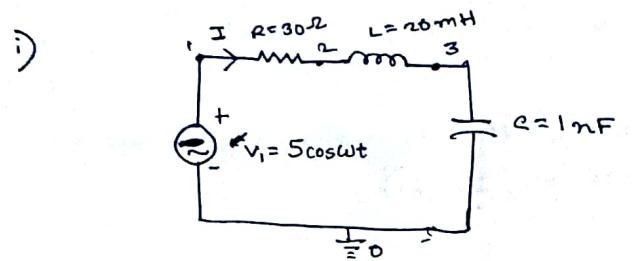
• PROBE <output variable>

• PROBE command generates a data file for viewing the analysis on the computer.

The .PROBE tells PSPICE to write the result of the DC, AC or Transient simulation.

If .PROBE is followed by the output variables, it only ~~said~~ save the output of those signals.

• .PROBE alone means saving all the signals to the data file.



In the RLC Series circuit, find the magnitude and phase of  $I$  when the source frequency is varied from 40-60 kHz in 100 steps.

Title: RLC Series Circuit

$$V_i \quad 1 \quad 0 \quad \text{AC} \quad 5 \quad \begin{matrix} \text{magnitude} \\ \text{phase} \end{matrix}$$

$$R \quad 1 \quad 2 \quad 30 \quad \Rightarrow Z_1 = \frac{L}{R} = \frac{20 \times 10^{-3}}{30} = 0.66 \times 10^{-3} \Omega = 0.66 \text{ m}$$

$$L \quad 2 \quad 3 \quad 20 \text{ mH} \quad \Rightarrow Z_2 = R \times C = 30 \times 1 \times 10^{-9} = 30 \text{ n}$$

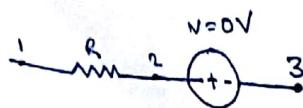
$$C \quad 3 \quad 0 \quad 1 \text{ nF}$$

AC LIN 100 40K 60K

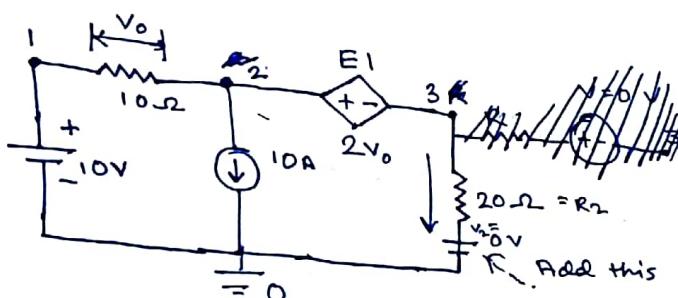
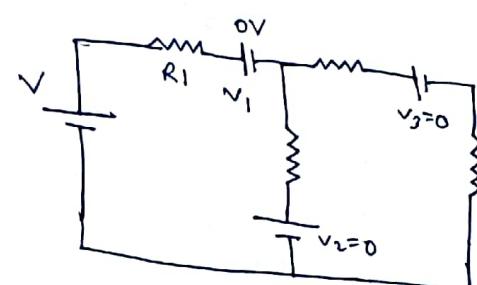
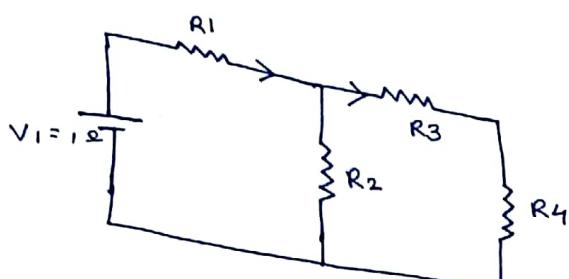
PROBE  $\text{IM}(v_i)$   $\text{IP}(v_i)$

END

Dummy Source



The objective of this dummy source along with .OP command is to get the value of current through the branch where dummy source is present.



Find the current through  $20\Omega$  resistance.

Title ~~→ Done~~

V1 1 0 DC 10

R1 1 2 10

I1 2 0 DC 10

E1 2 3 1 2 2

R2 3 0 20

V2 4 0 DC 0V

.OP

.END

## Module 1

### Network Analysis

#### Basis Elements

1. Resistance → from Ohm's Law  $V = IR$
2. Inductance → from Faraday's Law of EM Induction,

$$\text{not } \phi = LI$$

$$\frac{d\phi}{dt} = L \frac{di}{dt}$$

$$\Rightarrow e = L \frac{di}{dt}$$

↓  
emf induced

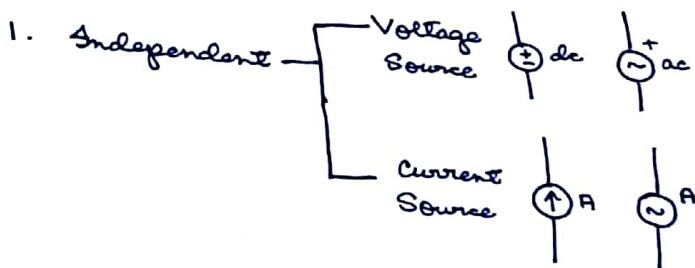
3. Capacitance →  $q = CV$

$$\Rightarrow q = CV$$

$$i = C \frac{dv}{dt}$$

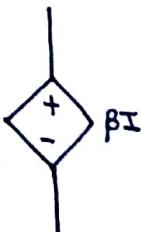
$$\Rightarrow \frac{dq}{dt} = C \frac{dv}{dt}$$

#### Types of Sources



#### 2. Dependent

- a) Voltage Controlled Voltage Source (V<sub>CVS</sub>)
- b) Voltage Controlled Current Source (V<sub>CCS</sub>)
- c) Current Controlled Voltage Source (C<sub>CVS</sub>)
- d) Current Controlled Current Source (C<sub>CCS</sub>)



### Basic Laws

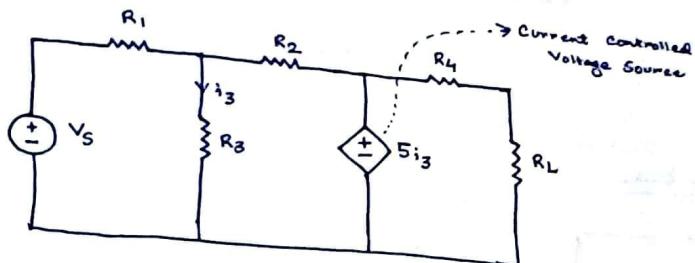
1. Ohm's Law
2. KVL  $\rightarrow$  Mesh or Loop Analysis
3. KCL  $\rightarrow$  Node Analysis

### Basic Properties

Circuit should be

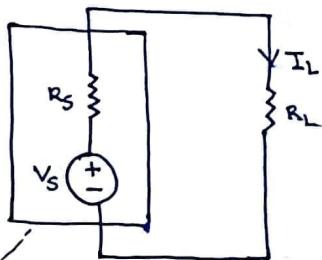
- i) Linear :  $V$  v/s  $I$  plot comes as linear; semiconductor elements like diode, Transistor make a circuit nonlinear.
- ii) Active: The circuit must contain some activation source.
- iii) Bilateral: Current can flow in either direction.

Ideal Voltage Source: External resistance is zero.



### Source Conversion

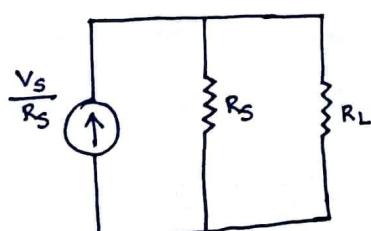
#### 1) Voltage to Current:



practical voltage source; internal resistance =  $R_s$

$$I_L = \frac{V_s}{R_s + R_L}$$

$$P_L = \left( \frac{V_s}{R_s} \right) \left( \frac{R_s}{R_s + R_L} \right)$$



### Basic Laws

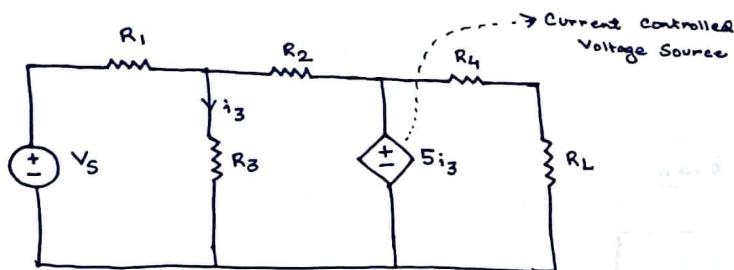
1. Ohm's Law
2. KVL  $\rightarrow$  Mesh or Loop Analysis
3. KCL  $\rightarrow$  Node Analysis

### Basic Properties

Circuit should be

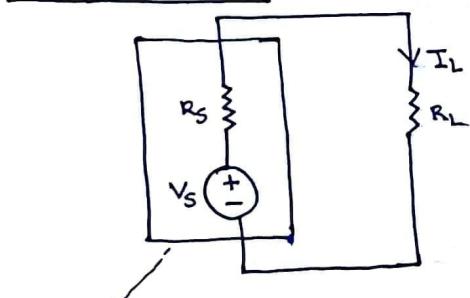
- i) Linear :  $V$  vs  $I$  plot comes as linear; semiconductor elements like diode, Transistor makes a circuit non-linear.
- ii) Active : The circuit must contain some activation source.
- iii) Bilateral : Current can flow in either direction.

Ideal Voltage Source: External resistance is zero.



### Source Conversion

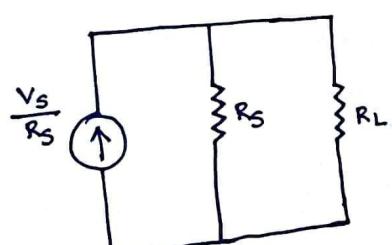
#### 1) Voltage to Current :



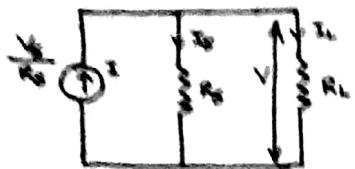
practical voltage source; internal resistance =  $R_s$

$$I_L = \frac{V_s}{R_s + R_L}$$

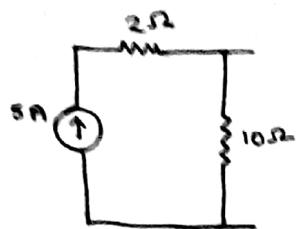
$$\Rightarrow I = \left( \frac{V_s}{R_s} \right) \left( \frac{R_s}{R_s + R_L} \right)$$



3) Current to Voltage

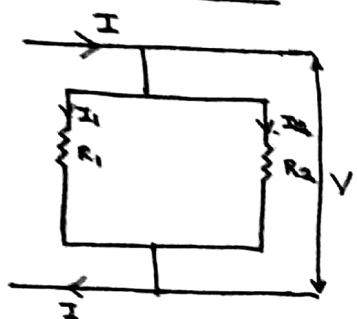


$$\begin{aligned} V &= I_L R_L \\ &= I \frac{R_B}{R_B + R_L} R_L \\ &= \underbrace{(I R_B)}_{V_0} \frac{R_L}{R_B + R_L} \end{aligned}$$



← Conversion To  
Voltage Source not possibl  
if the 2 ohm resistor is present

Current division Rule



$$V = I_1 R_1 = I_2 R_2$$

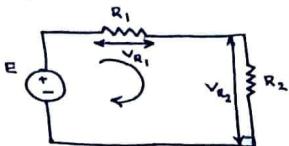
$$R_{eq} = \frac{R_1 R_2}{R_1 + R_2}$$

$$I = \frac{V}{R_{eq}} = \frac{I R_1 (R_1 + R_2)}{R_1 R_2}$$

$$\therefore I_1 = I \left( \frac{R_2}{R_1 + R_2} \right)$$

$$\therefore I_2 = I \left( \frac{R_1}{R_1 + R_2} \right)$$

### Voltage Division Rule



$$I = \frac{E}{R_1 + R_2}$$

$$V_{R_1} = IR_1 = \frac{ER_1}{R_1 + R_2}$$

$$V_{R_2} = IR_2 = \frac{ER_2}{R_1 + R_2}$$

### Node Analysis (Application of KCL)

1. The objective is to compute all branch currents.
2. Applicable to individual non-reference node of a given circuit.
3. To write current equation, it is assumed that the respective node potential is always higher than the other node potentials appearing in the equation.
4. The node pair equations to be solved to find the branch currents.

### Mesh Analysis

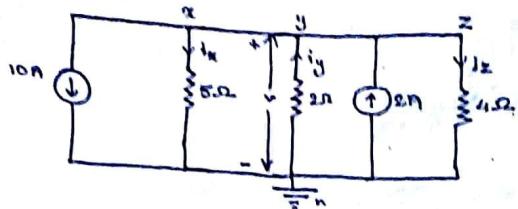
1. Objective is to find out the branch currents as well as the voltage across different elements.
2. Applicable to separate closed path of a circuit.
3. For each closed path one current is assumed to flow either in clockwise or in anti-clockwise direction.
4. The polarities of drops across each element has to be found out by the assumed direction of current.

5. Now we can apply KVL for each closed loop and the loop equations have to be solved to find the branch currents and voltages.

2

Problem:

1.



Find  $v$  and the magnitude and direction of unknown currents in branches  $xn$ ,  $yn$  and  $zn$ .

Using KCL,

$$10 + i_x + i_z = 2 + i_y$$

$\Rightarrow 10 + \frac{v}{5} + \frac{v}{4} = 2 - \frac{v}{2}$   $\rightarrow$  "current is flowing from - side to the + side, the sign must be reversed.

$$\Rightarrow \frac{v}{5} + \frac{v}{4} + \frac{v}{2} = -8$$

$$\Rightarrow \frac{4v + 5v + 10v}{20} = -8$$

$$\Rightarrow 19v = -160$$

$$\Rightarrow v = -\frac{160}{19} = -8.42 \text{ V (Ans)}$$

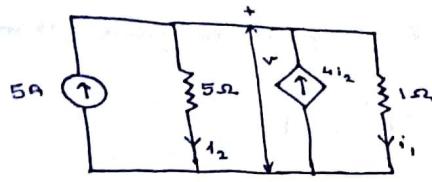
$$\therefore i_x = \frac{v}{5} = -\frac{8.42}{5} = -1.68 \text{ A (Ans)}$$

$$i_y = \frac{v}{2} = 4.21 \text{ A (Ans)}$$

$$i_z = -2.1 \text{ A (Ans)}$$

P

Q.



Find the value of  $v$  and the currents.

Ans:  $v = 12.5 \text{ V}$ ,  $i_2 = 2.5 \text{ A}$ ,  $4i_2 = 10 \text{ A}$

Using KCL,

$$5 + 4i_2 = i_2 + i_1$$

$$\Rightarrow 5 + 4 \cdot \frac{v}{5} = \frac{v}{6} + \frac{v}{1}$$

$$\Rightarrow 5 + \frac{3v}{5} - v = 0$$

$$\Rightarrow \frac{3v - 5v}{5} = -5$$

$$\Rightarrow -2v = -25$$

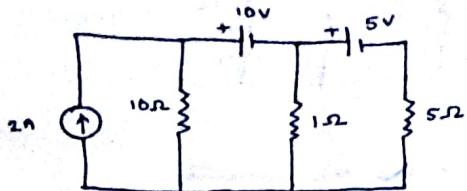
$$\Rightarrow v = 12.5 \text{ (Ans)}$$

$$\therefore i_2 = \frac{12.5}{5} = 2.5 \text{ A (Ans)}$$

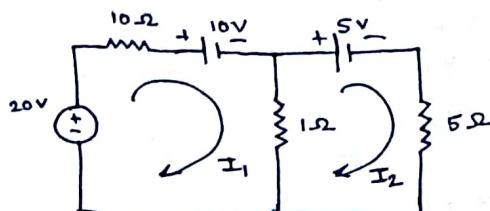
$$\therefore 4i_2 = 10 \text{ A (Ans)}$$

三

Did the current and power designated through 52 minutes



4.



$$\therefore 20 - 10I_1 - 10 - (I_1 - I_2) \cdot 1 = 0 \quad \dots \dots \quad (1)$$

$$-5 - 5I_2 - (I_2 - I_1) \cdot 1 = 0 \quad \text{--- (2)}$$

KVL in Loop 2

∴ From \*①,

$$20 - \cancel{10} I_1 - 10 - I_1 + I_2 = 0$$

$$\Rightarrow 11I_1 - I_2 = 10 \dots \textcircled{3}$$

From ②

$$-5 - 5x_2 - x_3 + x_4 = 0$$

$$\Rightarrow x_1 - 6x_2 = 5 \dots \text{④}$$

$$\begin{array}{r} \cancel{66I_1} - 6I_2 = 60 \\ - I_1 + \cancel{6I_2} = 5 \\ \hline 65I_1 = 55 \end{array}$$

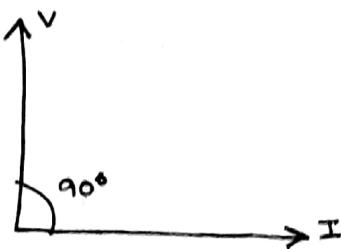
$$65 I_1 = 55$$

$$\Rightarrow I_1 = \frac{55}{65}$$

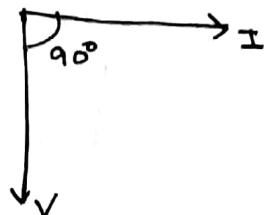
$$\therefore \pi \frac{55}{65} - 6I_2 = 5$$

$$\text{为负数} \Rightarrow 6I_2 = \frac{55}{65} - 5 \Rightarrow I_2 = -0.692 \text{ A}$$

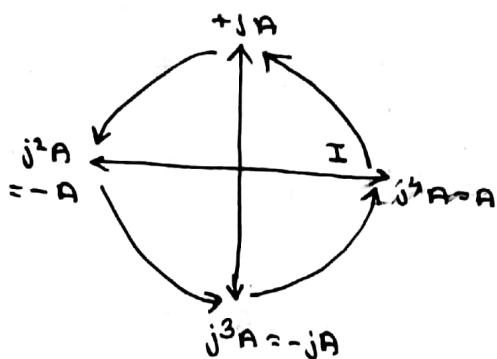
Inductor → Current lags voltage by  $90^\circ$  or voltage leads current by  $90^\circ$ .



Capacitor → Current leads voltage by  $90^\circ$  or voltage lags current by  $90^\circ$ .



### j-operator



$$L \Rightarrow \underline{\underline{X_L}} = 2\pi f L + j \text{ Inductor}$$

-j Capacitor

$$C \Rightarrow X_C = 2\pi f C$$

$\rightarrow +$  means inductor  
 $\rightarrow -$  means capacitor

$$\underline{\underline{(3+j4) \Omega}}$$

~~Rectangular Form~~

Polar Form  $M \angle \theta$

- Conversion from Polar to Rectangular
- Rectangular to Polar
- Form and vice versa

1. The multiplication and division, under form of phasors,  
2. The addition and subtraction, under form of complex numbers.

$$10 \angle 60^\circ \times 10 + 2i_1$$

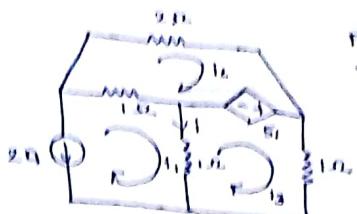
$$(10 \angle 60^\circ) / (10 + i_1)$$

$$10 \angle 120^\circ \angle -90^\circ$$

$$10 \angle 120^\circ$$

### Problem 1:

b)



Find the magnitude of  $\text{Max}$ ,  
the current dependent source,  
and the through the resistors.

#### Loop 1:

$$i_1 = 2A$$

#### Loop 2:

$$2i_2 + 5i_1 + (i_2 - i_1) \cdot 1 \approx 0$$

#### Loop 3:

$$i_3 \times 1 + (i_3 - i_1) \cdot 1 - 5i_1 \approx 0$$

$$\Rightarrow i_3 + i_3 - i_1 + 10 + 5i_3 \approx 0$$

$$i_3 - (-2 - i_3) \Rightarrow 7i_3 + 2 + 10 = 0$$

$$\Rightarrow 7i_3 = -12$$

$$\Rightarrow i_3 = \frac{-12}{7} (\text{A})$$

$$2i_2 + 5(-2 - i_3) + (i_2 + 2) \cdot 1 \approx 0$$

$$\Rightarrow 2i_2 + 5(-2 + \frac{12}{7}) + i_2 + 2 = 0 \quad \therefore i_2 = -2 + \frac{12}{7}$$

$$= \frac{-2}{7}$$

$$= -0.29 A (\text{A})$$

$$\Rightarrow i_2 = 0.19 A (\text{A})$$

$$\therefore 5i_1 = 5 \times (-0.29) \\ = 1.45 A (\text{A})$$

j)

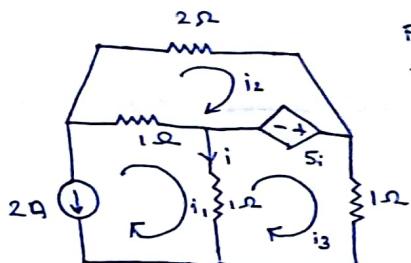
- For multiplication and division, polar form is better.
- For addition and subtraction, rectangular form is better.

$$10 \angle 60^\circ \times m_1 \angle \theta_1 \\ \downarrow \\ (10 \times m_1) \angle (60^\circ + \theta_1)$$

47.26  $\angle -57.13^\circ$   
~~-57.13~~

### Problems:

1.



Find the magnitude of the  
current dependent source,  
and the through  $2\Omega$  resistor.

loop 1:

$$i_1 = -2A$$

loop 2:

$$2i_2 + 5i + (i_2 - i_1) \cdot 1 = 0$$

loop 3:

$$i_3 \times 1 + (i_3 - i_1) \cdot 1 - 5i = 0$$

$$\Rightarrow i_3 + i_3 - i_1 + 10 + 5i =$$

However,  $i = i_1 - i_3$

$$i = (-2 - i_3)$$

$$\Rightarrow 7i_3 + 2 + 10 = 0$$

$$\Rightarrow 7i_3 = -12$$

$$\Rightarrow i_3 = -\frac{12}{7}$$

$$2i_2 + 5(-2 - i_3) + (i_2 + 2) \cdot 1 = 0$$

$$\Rightarrow 2i_2 + 5\left(-2 + \frac{12}{7}\right) + i_2 + 2 = 0$$

$$\Rightarrow 3i_2 = -0.57$$

$$\Rightarrow i_2 = 0.19A \text{ (Ans)}$$

$$\therefore i = -2 + \frac{12}{7}$$

$$= -\frac{2}{7}$$

$$= -0.29A$$

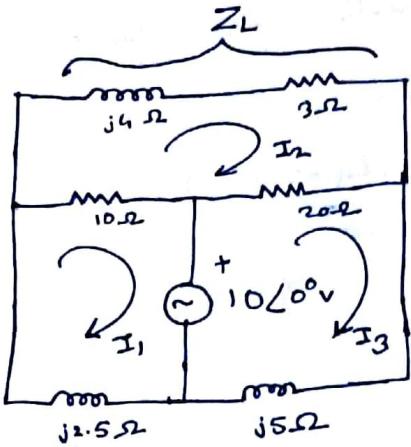
$$\therefore S_i = 5 \times (0.29) \\ = 1.45 A$$

ans

e

1

2.



Find the current flowing through  $Z_L$  using mesh analysis.

loop 1:

$$(10 + j2.5) \cdot I_1 - 10 I_2 - 0 \times I_3 = -10 \angle 0^\circ$$

loop 2:

$$-10 I_1 + (3 + j4) I_2 - 20 I_3 = 0$$

$$10(I_2 - I_1) + 20(I_2 - I_3) + (3 + j4) I_3 = 0$$

loop 3:

$$20(I_3 - I_2) + j5\Omega I_3 = 10 \angle 0^\circ$$

$$\Rightarrow 0 \times I_1 - 20 I_2 + (20 + j5) I_3 = 10 \angle 0^\circ$$

$$\begin{bmatrix} (10 + j2.5) & -10 & 0 \\ -10 & (20 + j4) & -20 \\ 0 & -20 & (20 + j5) \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = \begin{bmatrix} -10 \\ 0 \\ 10 \end{bmatrix}$$

$$I_2 = \frac{\Delta_2}{\Delta}$$

~~20~~ ~~-100~~

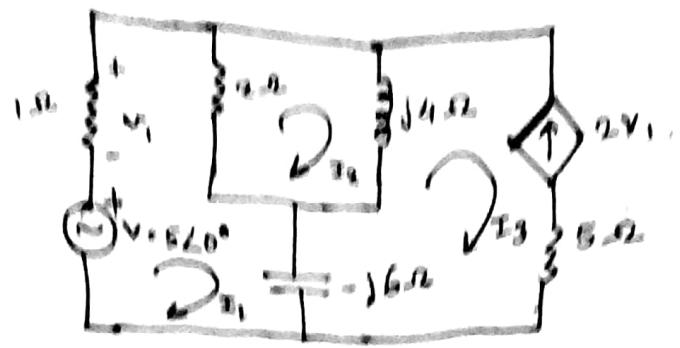
$$\frac{12.5}{\cancel{200}} \times \cancel{200}$$

$$\begin{bmatrix} (10 + j2.5) & -10 & 0 \\ -10 & 0 & -20 \\ 0 & 10 & (20 + j5) \end{bmatrix}$$

$$\begin{aligned} &= (10 + j2.5)(200) + (-10)(\cancel{-100} + 200 + j50) + 0 \\ &= 2000 + \cancel{-100} j500 - \cancel{2000} - j500 + 0 \end{aligned}$$

$$= 0$$

$$\therefore I_2 = \frac{0}{\Delta} = 0 \text{ A (Ans)}$$



Find the current through capacitor.

Loop 2

$$I_2 = -2V_1$$

Loop 1

$$V_1 = I_1 \times 1$$



Loop 3

$$I_3 = -2I_1$$

$$\Rightarrow I_3 + 2I_1 = 0$$

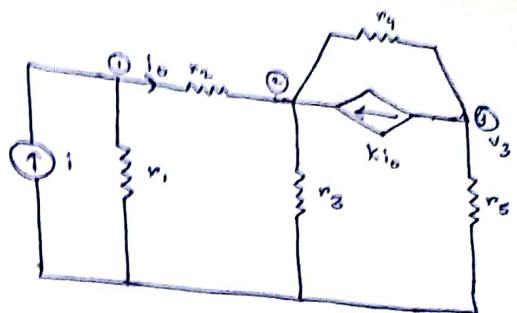
Loop 1

$$5\angle 0^\circ = (3 - j6)I_1 - 2I_2 - (-j6)I_3$$

Loop 2

$$-2I_1 + (2 + j4)I_2 - j4I_3 = 0$$

4.

At Node 1:

$$\frac{v_1}{r_1} + \frac{v_1 - v_2}{r_2} = i$$

At Node 2:

$$\frac{v_2 - v_1}{r_2} + \frac{v_2}{r_3} + \frac{v_2 - v_3}{r_4} = k_{1o}$$

At Node 3:

$$\frac{v_3}{r_5} + \frac{v_3 - v_2}{r_4} = -k_{1o}$$

$$\left[ \begin{array}{ccc} \left( \frac{1}{r_1} + \frac{1}{r_2} \right) & \left( \frac{1}{r_2} \right) & 0 \\ -\frac{1}{r_2} & \left( \frac{1}{r_2} + \frac{1}{r_3} + \frac{1}{r_4} \right) & \left( -\frac{1}{r_4} \right) \\ 0 & -\frac{1}{r_4} & \left( \frac{1}{r_5} + \frac{1}{r_4} \right) \end{array} \right]$$