a)

$$\frac{d\langle x\rangle}{dt} = \int x \frac{\partial}{\partial t} |\psi|^2 dx = \frac{ih}{2m} \int x \frac{\partial}{\partial t} (\psi * \frac{\partial \psi}{\partial x} - \frac{\partial \psi *}{\partial x} \psi) dx \quad 1.29$$

The middle expression here is $\int x \frac{\partial}{\partial t} |\psi|^2 dx$

This is not of the form $\int v \cdot du$ because there is a partial derivative with respect to time which is integrated with respect to distance. If the partial derivative was with respect to distance, it's fair game for integration-by-parts.