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ECE 637
Exam #2

4.1) The columns of A are samples that could either be image data or some other data. The matrix \hat{R} is an estimate of the covariance of the columns of A , averaged with $1/n$ because A has n columns. The columns of A may be obtained from some sampling or imaging process

4.2) $A = U\Sigma V^+$

$$\begin{aligned}\hat{R} &= \frac{1}{n} AA^+ = \frac{1}{n} (U\Sigma V^+)(U\Sigma V^+)^+ = E\Lambda E^+ \\ &= \frac{1}{n} U\Sigma V^+ V\Sigma U^+ \quad ; \quad \Sigma^+ = \Sigma \\ &= \frac{1}{n} U\Sigma^2 U^+\end{aligned}$$

$$\begin{aligned}E &= U \\ \Lambda &= \frac{1}{n} \Sigma^2\end{aligned}$$

4.3) $A = U\Sigma V^+$

$$\begin{aligned}B &= \frac{1}{n} A^+ A = \frac{1}{n} (U\Sigma V^+)^+ (U\Sigma V^+) = TDT^+ \\ &= \frac{1}{n} V\Sigma U^+ U\Sigma V^+ \quad ; \quad \Sigma^+ = \Sigma \\ &= \frac{1}{n} V\Sigma^2 V^+\end{aligned}$$

$$\begin{aligned}T &= V \\ D &= \frac{1}{n} \Sigma^2\end{aligned}$$