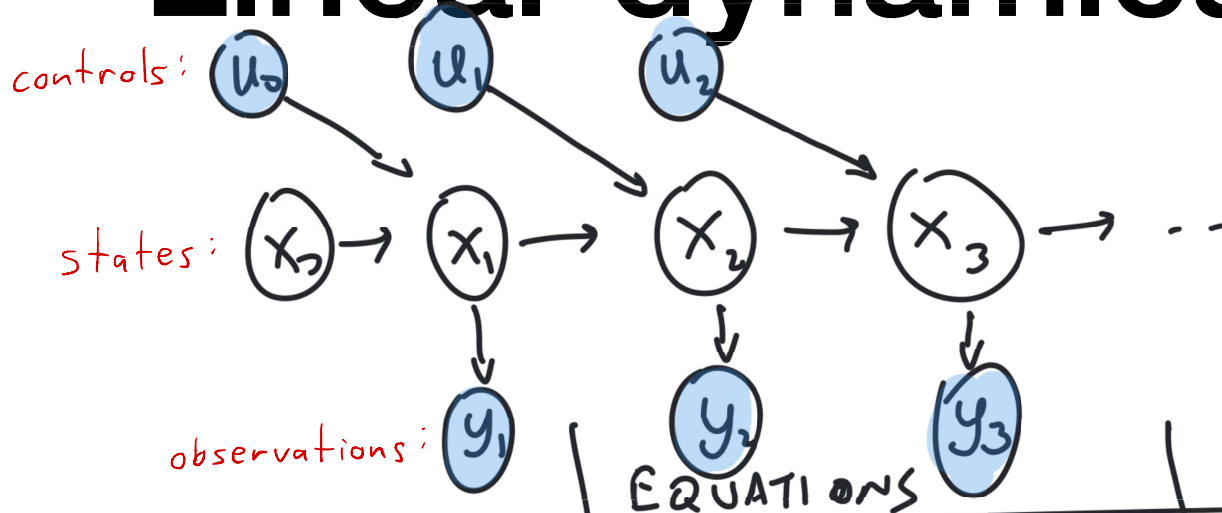


# Linear dynamical systems



Dimensions:

$x \in \mathbb{R}^d, u \in \mathbb{R}^m, y \in \mathbb{R}^q$

$\mu_0 \in \mathbb{R}^d, z_0 \in \mathbb{R}^d, \Sigma_0 \in \mathbb{R}^{d \times d} \text{ p.d.}$

$A \in \mathbb{R}^{d \times d}, B \in \mathbb{R}^{d \times m}, Q \in \mathbb{R}^{d \times d} \text{ p.d.}$

$C \in \mathbb{R}^{q \times d}, w_n \in \mathbb{R}^q, R \in \mathbb{R}^{q \times q} \text{ p.d.}$

PROBABILISTIC

Initial Prob.

$$x_0 = \mu_0 + z_0$$

$$z_0 \sim N(0, \Sigma_0)$$

$$p(x_0) = N(x_0 | \mu_0, \Sigma_0)$$

Transition Prob.

$$x_{n+1} = A x_n + B u_n + z_n$$

$$z_n \sim N(0, Q)$$

$$p(x_{n+1} | x_n, u_n) = N(x_{n+1} | A x_n + B u_n, Q)$$

Emission Prob.

$$y_n = C x_n + w_n$$

$$w_n \sim N(0, R)$$

$$p(y_n | x_n) = N(y_n | C x_n, R)$$