

Problem 2

(a)

States: Determined by the location of the two friends and the total travel time elapsed (i,j,k) where i is city of first friend, j is city of second friend, and k is the sum of the maximum of each prior leg distance. For a map with x cities, there are x^2 combinations of i and j with infinite possibilities for k . E.g.

$\text{In}(\text{Fagaras}, \text{Rimnicu Vilcea}, 15)$

Initial state: $(i,j,0)$ where i and j are starting cities.

Actions: move friend one and two over one city each. Add the maximum of the two length costs to k . E.g. if $(\text{Fagaras}, \text{Rimnicu Vilcea}, 15)$ one possible action is $\text{Go}(\text{Sibiu}, \text{Pitesti})$

Transition model: the actions have their intended results. E.g.

$\text{Result}(\text{In}(\text{Arad}, \text{Oradea}, 0), \text{Go}(\text{Zerind}, \text{Zerind})) = (\text{Zerind}, \text{Zerind}, \max(75, 71))$

Goal: $\text{In}(x, x, k)$ where x is the same city for both friends. If we start out in same cities, $k=0$.

Path cost: maximum of travel length between two cities for two friends like above, i.e. $\max(75, 71) = 75$ for $(\text{Arad}, \text{Oradea}) \rightarrow (\text{Zerind}, \text{Zerind})$

(b)

(i) Yes. no path length is less than 1 so $h < h^*$ for all actions in all states.

(ii) No. transition could take $D(i,j)$ to complete so $2 \cdot D(i,j)$ overestimates.

(iii) Yes. The transition always takes the longer path time of the two movements, so half of $D(i,j)$ will always be less than the actual path time.

(c)

No, as every state is connected to every other state. There will always be a path from whatever state each friend is in to another state that is the same for both, by definition of the problem.

(d)

If the map contains a straight line and a cycle, this will cause all possible solutions to take that cycle, depending on initial state.