

BLOQUE II:

16) \overline{abab} tiene 6 DIV. = $2 \cdot 3$
 $= (1+1)(2+1)$

$$\overline{ab00} + \overline{ab}$$

$$100 \cdot \overline{ab} + \overline{ab}$$

$$\overline{101} \cdot \overline{ab} = \overset{1}{X} \cdot \overset{2}{Y}$$

PRIMOS

$$\therefore X = 101$$

$$\therefore \overline{ab} = Y^2$$

$$25 = 5^2$$

$$49 = 7^2$$

17) $N = 128 \cdot a \cdot b$
 $= 2^7 \cdot a^1 \cdot b^1 \rightarrow D.C$

PRIMOS

$$\therefore \frac{2^{7+1}-1}{2-1} \times \frac{a^{1+1}-1}{a-1} \times \frac{b^{1+1}-1}{b-1} = \frac{85}{28} \cdot 2^7 \cdot a \cdot b$$

$$\cancel{255} \cdot \frac{a^2-1}{a-1} \cdot \frac{b^2-1}{b-1} = \cancel{85} \cdot \cancel{128} \cdot a \cdot b$$

7

$$(a+1)(b+1) = \frac{32}{21} \cdot a \cdot b$$

$$\frac{(a+1)(b+1)}{a \cdot b} = \frac{32}{21}$$

7 · 3

CANG

DMs

$$18) N = 30^a; SD = 2 \cdot SD\left(\frac{N}{2}\right)$$

PARES
2

$$\therefore N = 2^2 \cdot 3^2 \cdot 5^2$$

$$\frac{N}{2} = \frac{2^a \cdot 3^a \cdot 5^a}{2}$$

$$= 2^{a-1} \cdot 3^a \cdot 5^a$$

$$2418 = 2 \cdot \frac{2^a - 1}{1} \cdot \frac{3^{a+1} - 1}{2} \cdot \frac{5^{a+1} - 1}{4}$$

$$2 \cdot 3 \cdot 31 \cdot 13 \cdot 4 = (2^{a-1} - 1)(3^{a+1} - 1)(5^{a+1} - 1)$$

$$3 \cdot 26 \cdot 124$$

$$\therefore a = 2$$

$$\begin{array}{r|l} 2418 & 2 \\ 1209 & 3 \\ 403 & 31 \\ 13 & \end{array}$$

$$CD_N = 1 + \underbrace{CD_{\text{PRIM}}}_{CD_{\text{SIMPLES}}} + CD_{\text{COMP}}$$

$$\frac{3 \cdot 3 \cdot 3}{27} = 1 + 3 + CD_{\text{COMP}}$$

$$23 = CD_{\text{COMP}}$$

TOSCAN

$$= \underline{2} \cdot \underline{5} \cdot \underline{2} \cdot 3^{x+2} \cdot \underline{5}^{x+2} \text{ IMPARES.}$$

$$= \cancel{2^{3x+2}} \cdot 3^{x+2} \cdot 5^{2x+2}$$

$$\therefore 3 \cdot 5 \xrightarrow{5} CD = (x+3)(2x+2)$$

$$48 \quad \quad \quad 2(x+1)$$

$$24 = (x+3)(x+1)$$

$$6 \cdot 4$$

$N \rightarrow \underline{24}_{\text{DIV.}} = 6 \cdot 4 \rightarrow N = X^5 \cdot Y^3$
 $ \phantom{\underline{24}_{\text{DIV.}}} = 8 \cdot 3 \rightarrow N = X^7 \cdot Y^2$
 $ \phantom{\underline{24}_{\text{DIV.}}} = 12 \cdot 2 \rightarrow N = X^{11} \cdot Y^1$
 $(3N) \rightarrow 30_{\text{DIV.}} 2 \cdot 3 \cdot 4 \rightarrow N = X^1 \cdot Y^2 \cdot Z^3$

$$\therefore \underbrace{3 \cdot X^5 \cdot y^3}_3 = X^5 \cdot 3^4$$

$$CD = 6 \cdot 5 = 30 \checkmark$$

$$3 \cdot x^1 \cdot y^2 \cdot z^3 = x^1 \cdot y^2 \cdot z^4$$

$$CD = 2 \cdot 3 \cdot 5 = 30 \checkmark$$

$$\therefore 3(x^5 \cdot y^3)^2 = 3 \cdot x^{10} \cdot y^6 = x^{10} \cdot y^7$$

$$3(x \cdot y^2 \cdot z^3)^2 = 3 \cdot x^2 \cdot y^4 \cdot z^6 = x^2 \cdot y^4 \cdot z^6$$

CANG

DMs

$$21) A - B = 44 ; MCM - MCD = 500$$

$$K\alpha - K\beta$$

$$K(\alpha - \beta) = 44 ; K\alpha\beta - K$$

$$4 \cdot 11$$

$$K(\alpha\beta - 1) = 500$$

$$\therefore \frac{K(\alpha\beta - 1)}{K(\alpha - \beta)} = \frac{500}{44} \quad \begin{matrix} 125 \\ 11 \end{matrix}$$

$$\frac{\alpha\beta - 1}{\alpha - \beta} = \frac{125}{11}$$

$$\alpha\beta = 126 ; \alpha - \beta = 11$$

$$18 \cdot 7 \quad 18 - 7$$

$$; MCD(A, B) = K$$

$$\therefore A = K \cdot \alpha$$

$$B = K \cdot \beta$$

P.E.SI

$$MCM(A, B) = K \cdot \alpha \cdot \beta$$

$$\begin{array}{r|l} 126 & 2 \\ 63 & 3 \\ 21 & 3 \\ 7 & 7 \\ 1 & 1 \end{array} \left. \vphantom{\begin{array}{r|l} 126 \\ 63 \\ 21 \\ 7 \\ 1 \end{array}} \right\} 18$$

$$A = 4(18) = 72$$

$$\therefore B = 4(7) = 28 \checkmark$$

BLOQUE II:

22) $MCM^2 = MCD^3$; $A+B=180$

~~$K \cdot \alpha^2 \cdot \beta^2 = K$~~

$3 \cdot 2^2 = \alpha^2 \cdot \beta^2 = K$

36.

$$\begin{array}{r|l} 180 & 2 \\ 90 & 2 \\ 45 & 3 \\ 15 & 3 \\ 5 & 5 \\ 1 & \end{array}$$

$K\alpha + K\beta = 180$

$K(\alpha + \beta) = 180$

$\alpha^2 \cdot \beta^2 (\alpha + \beta) = 180$

$3 \cdot 2^2 \cdot 5$

$\alpha = 3$

$\beta = 2$

23) MCD.

$$\begin{array}{r|l} 5068 - 3388 - 4032 & 2 \\ 2534 - 1694 - 2016 & 2 \\ 1267 - 847 - 1008 & 7 \\ 181 - 121 - 144 & 28 \end{array}$$

Precio : $\underbrace{\text{div } 28}_{\text{entrada}}$

$$\begin{array}{c} 1 \\ 2 \\ 4 \\ 7 \\ 14 \\ 28 \end{array}$$

$10 < 14 < 20$

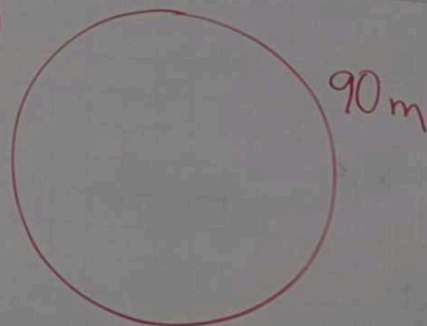
28.

$N^{\circ} \text{PER: } \frac{5068 + 3388 + 4032}{14} : 892$

E L
TOS CANG

DNIS

24)



$$V_A: 9 \text{ m/s} \rightarrow t_A: 10 \text{ s}$$

$$V_B: 5 \text{ m/s} \rightarrow t_B: 18 \text{ s}$$

$$V_C: 3 \text{ m/s} \rightarrow t_C: 30 \text{ s}$$

$$\text{MCM}(10, 18, 30) = 90 \text{ s}$$

BLOQUE III

$$25) N = 2^\alpha \cdot 5^\beta \cdot 3 \text{ tiene } 16 \text{ DIV } 15$$

$$\frac{N}{15} = \frac{2^\alpha \cdot 5^\beta \cdot 3}{5 \cdot 3} = 2^\alpha \cdot 5^{\beta-1}$$

$$CD = (\alpha+1) \cdot \beta = 16$$

$$\frac{N}{20} = \frac{2^\alpha \cdot 5^\beta \cdot 3}{2^2 \cdot 5} = 2^{\alpha-2} \cdot 5^{\beta-1} \cdot 3$$

$$CD = (\alpha-1) \cdot \beta \cdot 2 = 16$$

$$(\alpha-1) \beta = 8$$

$$\therefore N = 2^3 \cdot 5^4 \cdot 3$$

$$= (2^3 \cdot 5^3) \cdot 5 \cdot 3$$

$$CD = 2 \cdot 2 = 4$$

27) $31!$ tiene n DIV.
 \hat{c} $32!$

$$31 \begin{array}{l} \div 2 \\ \hline 15 \end{array} \begin{array}{l} \div 2 \\ \hline 7 \end{array} \begin{array}{l} \div 2 \\ \hline 3 \end{array} \begin{array}{l} \div 2 \\ \hline 1 \end{array} +$$

$$\rightarrow 31! = \dots \cdot 2^{\textcircled{26}} \cdot \dots$$

$$CD = \frac{(26+1)(b+1)(c+1)\dots}{27} = n$$

$$32! = \dots \cdot 2^{26} \cdot \dots \cdot \textcircled{32} \cdot \dots$$

$2^{31} \qquad \qquad \qquad 2^5$

$$CD = \frac{32}{(31+1)} \left(\frac{n}{27} \right) =$$

23
 506
 253
 126
 181
 Prec
 entro

OS LANG

DWG

$$12 = 2^2 \cdot 3^1$$

$$\begin{aligned} SD_N &= \frac{2^{2+1} - 1}{2 - 1} \times \frac{3^{1+1} - 1}{3 - 1} \\ &= \frac{7}{1} \times \frac{8}{2} = 7 \times 4 = 28. \end{aligned}$$

$$12 = 2^{\textcircled{2}} \cdot 3^{\textcircled{1}} \rightarrow D.C$$

PRIMOS.

$$\therefore C.D = (2+1)(1+1)$$
$$3 \cdot 2 = 6$$