

PRODUCTOS NOTABLES

⑧ Si:

$$a = \sqrt[3]{7+4\sqrt{3}} + \sqrt[3]{7-4\sqrt{3}}$$

$$b = \sqrt[3]{7+4\sqrt{3}} - \sqrt[3]{7-4\sqrt{3}}$$

$$a+b = 2\sqrt[3]{7+4\sqrt{3}}$$

$$a-b = 2\sqrt[3]{7-4\sqrt{3}}$$

$$a^3 - b^3 = 4\sqrt[3]{(7+4\sqrt{3})(7-4\sqrt{3})} \quad \text{o} \quad 4(1) = 4$$

$$\begin{array}{l} \text{Ojo } (a+b)^3 \\ (a-b)^3 \end{array}$$

$$\begin{array}{l} a^3 + 3a^2b + 3ab^2 + b^3 \\ a^3 - 3a^2b + 3ab^2 - b^3 \\ \hline a^3 + 3a^2b + 3ab^2 + b^3 \end{array}$$

$$E = \frac{a^4(a^2-3b^2) + b^4(3a^2-b^2) + 3(a^2-b^2)}{4(a^2-b^2)}$$

$$\frac{(a^2)^3 - 3a^4b^2 + 3a^2b^4 - (b^2)^3 + 3(a^2-b^2)}{4(a^2-b^2)}$$

$$\frac{(a^2-b^2)^3 + 3(a^2-b^2)}{4(a^2-b^2)}$$

$$\frac{(a^2-b^2)^2 + 3(a^2-b^2)}{4}$$

$$\begin{array}{r} 4^2 \\ 4 \overline{) 4} + 3(4) \\ 4 + 12 \\ \hline 16 \end{array}$$

⑤

$$+3(a^2-b^2)$$

$$(a^2-b^2)$$

$$+3(4)$$

$$4+12$$

$$16$$

⑤ Si:

$$x^2 - 3x + 1 = 0$$

$$x - 3 + \frac{1}{x} = 0$$

$$x + \frac{1}{x} = 3$$

$$x^2 + \frac{1}{x^2} = 3^2 - 2$$

$$x^3 + \frac{1}{x^3} = 3^3 - 3(3) = 27 - 9 = 18$$

Alors:

$$\left[x + \left(\frac{1}{x} \right) \right] \left[x + \left(\frac{1}{x} \right) \right]$$

$$x^{x+\frac{1}{x}} + x^{\frac{1}{x}} + \frac{1}{x^x} + \frac{1}{x^{\frac{1}{x}}} + \left(\frac{1}{x} \right)^x$$

$$x^3 + \frac{1}{x^3} + 2$$

$$18 + 2 = 20$$

⑩ Si:

$$ax + by = 8 \rightarrow 8^2$$

$$ay - bx = 6 \rightarrow 6^2 + \frac{100}{5} = 20$$

$$a^2 + b^2 = 5$$

Calcule: $x^2 + y^2$

$$(a^2 + b^2)(x^2 + y^2) = (ax + by)^2 + (ay - bx)^2$$

$$5(x^2 + y^2) = (8)^2 + (6)^2$$

$$x^2 + y^2 = \frac{100}{5} = 20$$

$$\textcircled{3} \quad \sqrt[8]{1 + (2^3+1)(2^4+1)(2^5+1) \cdot \textcircled{3}} \\ \sqrt[8]{2^{16}} \Rightarrow 2^2 \Rightarrow 4$$

④ Efectuar:

$$\begin{aligned} & (\underbrace{1+\sqrt{6}}_{11} + \underbrace{\sqrt{5}+\sqrt{2}}_{4}) (\underbrace{1+\sqrt{6}}_{11} - \underbrace{\sqrt{5}+\sqrt{2}}_{4}) \\ & \left. \begin{array}{l} (\sqrt{3}+\sqrt{6}) \cdot (\sqrt{5}+\sqrt{2}) \\ 11 - 4 \end{array} \right\} \left. \begin{array}{l} (\sqrt{1+\sqrt{6}})^2 - (\sqrt{5}+\sqrt{2})^2 \\ 4 \end{array} \right\} 4 \end{aligned}$$

$$\begin{aligned} \textcircled{6} \quad d) \quad & x^4 + x^2 y^2 + y^4 \\ & (x^2 + xy + y^2)(x^2 - xy + y^2) \\ & x^8 + x^4 + 1 \\ & (x^4 + x^2 + 1)(x^4 - x^2 + 1) \\ & (x^2 + x + 1)(x^2 - x + 1)(x^4 - x^2 + 1) \end{aligned}$$

$$\begin{aligned} \textcircled{7} \quad & \frac{1}{x} + \frac{1}{y} = \frac{4}{x+y} \\ & \frac{y+x}{xy} = \frac{4}{x+y} \rightarrow x=y \\ & (x+y)^2 = 4xy \\ & \rightarrow x=y \\ & x^2 + 2xy + y^2 = 4xy \\ & x^2 - 2xy + y^2 = 0 \\ & (x-y)^2 = 0 \\ & \boxed{x=y} \checkmark \end{aligned}$$

$$\textcircled{9} \quad S_i \\ E = \sqrt{\quad}$$

$$\begin{aligned} & (X+1) \\ & (X^2 + \end{aligned}$$

22 Factorizar en \mathbb{R}

$$P(x) = x^3 - x^2 - 5x + 5$$

$$x^2(x-1) - 5(x-1)$$

$$(x-1)(x^2-5)$$

$$(x-1)(x+\sqrt{5})(x-\sqrt{5})$$

$$-1 + \sqrt{5} - \sqrt{5}$$

$$-1$$

26 No F.P. Cuadráticos

$$a^4 + b^4 - 7a^2b^2$$

$$a^4 + 2a^2b^2 + b^4 - 7a^2b^2 - 2a^2b^2$$

$$(a^2 + b^2)^2 - 9a^2b^2$$

$$(a^2 + b^2)^2 - (3ab)^2$$

$$(a^2 + b^2 + 3ab)(a^2 + b^2 - 3ab)$$

$$(a^2 + 3ab + b^2)(a^2 - 3ab + b^2)$$

$$9$$

27 Suma de coef de un F.P

$$(x+3)^4 + 5x(x+6) + 39$$

$$((x+3)^2)^2 + 5(x^2+6x) + 39$$

$$(x^2+6x+9)^2 + 5(x^2+6x) + 39$$

$$(a+9)^2 + 5a + 39$$

$$a^2 + 18a + 81 + 5a + 39$$

$$a^2 + 23a + 120$$

$$a \begin{matrix} \nearrow 15 \\ \searrow 8 \end{matrix}$$

$$a \begin{matrix} \nearrow 15 \\ \searrow 8 \end{matrix}$$

$$(a+15)(a+8)$$

$$(x^2+6x+5)(x^2+6x)$$

$$x$$

$$x$$

$$(x^2+6x+5)(x+4)(x+2)$$

$$1+6+5$$

$$22$$

$$1+4$$

$$5$$

$$1+2$$

$$3$$

$$+8$$

$$4$$

$$2$$

$$(y)^2 = 4xy$$

$$(y)^4 = 8xy(x^2 + y^2)$$

$$(se_2)^{k-1}$$

$$(y)^4$$

$$48$$

$$(11) \quad \frac{4n+12}{n-8} = \frac{4n-3}{n-9}$$

$$n=12$$

$$\frac{60}{4} = \frac{45}{3} \Rightarrow (5)$$

$$(13) \quad \frac{x^{21} + y^{35}}{x^3 + y^5}$$

$$NoT=7$$

$$T_3 = (x^3)^{7-3} (y^5)^{3-1}$$

$$x^{12} \cdot y^{10}$$

$$G.A = 22$$

$$(15) \quad \frac{x^{15} + x^{10} + x^5 + 1}{x^{20} - 1}$$

$$(16) \quad \frac{x^{18} - x^{15} + x^{12} - x^9 + x^6 - x^3 + 1}{x^{21} + 1}$$

FACTORIZACION

$$(25) \quad \text{Suma Prima } \downarrow \text{ Grado}$$

$$(x+3)^4 - x^2(x+6)^2 - 81$$

$$[(x+3)^2]^2 - (x^2+6x)^2 - 81$$

$$(x^2+6x+9)^2 - (x^2+6x)^2 - 81$$

$$(a+9)^2 - a^2 - 81$$

$$a^2 + 18a + 81 - a^2 - 81$$

$$\begin{array}{r} 18a \\ 18(x^2+6x) \end{array} \bigg| \begin{array}{r} 18(x+6) \\ x; x+6 \\ 2x+6 \end{array}$$

$$C_5 = \{8, -1\} \cup \{8, 1\}$$

18) Simplification:

$$G = \frac{X^{4n-1} + X^{4n-2} + X^{4n-3} + \dots + X^2 + X + 1}{X^{2n-1} + X^{2n-2} + X^{2n-3} + \dots + X^2 + X + 1}$$

$$\begin{array}{r} \textcircled{4n} \\ X - 1 \\ \hline \textcircled{1} \\ X - 1 \\ \hline \textcircled{2n} \\ X - 1 \\ \hline \textcircled{1} \\ X - 1 \\ \hline X^{2n} + 1 \end{array} \Rightarrow \frac{\textcircled{4n} X - 1}{X^{2n} - 1} = \frac{X^{4n} - 1}{(X^{2n} + 1)(X^{2n} - 1)}$$

20) T.N. det T_C ($X=3$)

$$Y = 2\sqrt{2}$$

$$(X+Y)^{100} - (X-Y)^{100}$$

$$8XY(X^2+Y^2)$$

$$(X+Y)^{100} - (X-Y)^{100}$$

$$(X+Y)^4 - (X-Y)^4$$

Note 25

$$T_C = T_{\frac{25+1}{2}} = T_{13}$$

$$(X+Y)^2 - (X-Y)^2 = 4XY$$

$$(X+Y)^4 - (X-Y)^4 = 8XY(X^2+Y^2)$$

$$T_K = \left(\text{base}_1 \right)^{\text{NOT-K}} \left(\text{base}_2 \right)^{K-1}$$

$$T_{13} = (X+Y)^4 (X-Y)^4$$

$$(X+Y)^{48} (X-Y)^{48}$$

$$(X^2 - Y^2)^{48} = (X^2 - Y^2)^{48}$$

9 Simplificar:

$$E = \sqrt{(x+1)(x-1)(x+2)(x+0) + 1}$$

1
-1
2
0

+1

$$(x+1)x \cdot (x-1)(x+2) + 1$$

$$(x^2+x)(x^2+x-2) + 1$$

$$a(a-2) + 1$$

$$a^2 - 2a + 1$$

$$a - 1$$

$$a - 1$$

$$\sqrt{(a-1)^2}$$

$$a-1$$

$$x^2 + x - 1$$

$$0j0$$

$$(x+3)(x-5)(x-4)(x+4)$$

1ⁿ
2^o
3^a
4^{to}

COCIENTES NOTABLES

14 Suma de todos los Expo.

$$x^{100} - y^{100}$$

$$x^4 - y^4$$

$$NOT = \frac{100}{4} = 25$$

$$96 \times 25$$

$$2400$$

$$x^96 + x^92 + x^88 + \dots$$

17

$$x^{91} \cdot y^{54} + x^{63} \cdot y^{14}$$

$$145$$

$$145$$

$$145$$

F (de un F.p)

$$)+39$$

$$x)+39$$

$$^2+6x)+39$$

$$39$$

$$39$$

$$+15)(a+8)$$

$$6x+5)(x^2+6x$$

$$x$$

$$x$$

$$+8) \\ 4 \\ 2$$

$$(x^2+6x+15)(x+4)(x+2)$$

1+6+15 = 22
1+2 = 3

(28)

$$\cancel{6x^2} + 12xy + \cancel{6y^2} + 24x + \cancel{24y} + 28$$

3x, 2x, 3y, 2y, 4, 7

$$(3x+3y+4)(2x+2y+7)$$

$$5x+5y+11$$

(30) Mayor Grado de un F.p. $\rightarrow 6n$

$$x^{8n} + x^{4n} + x^{3n} + 2$$

$$(x^{8n} + x^{4n} + 1) + (x^{3n} + 1)$$

$$(x^{4n} + x^{2n} + 1)(x^{4n} - x^{2n} + 1) + (x^n + 1)(x^{2n} - x^n + 1)$$

$$(x^{2n} + x^n + 1)(x^{2n} - x^n + 1)(x^{4n} - x^{2n} + 1) + (x^n + 1)(x^{2n} - x^n + 1)$$

$$(x^{2n} - x^n + 1) \left[(x^{2n} + x^n + 1)(x^{4n} - x^{2n} + 1) + x^n + 1 \right]$$

$$(x^{2n} - x^n + 1) \cdot (x^{6n} + \dots + x^n + 1)$$

$$5k + k = 5 \\ \frac{5}{2} + \frac{5}{2} \\ \text{No KAYAK} \\ \frac{11}{2}$$

$$CS = \{-8, -1\} \cup \{8, 1\}$$