

Truncation error  $\rightarrow 7^{\text{th}}$  order Taylor expansion term:

$$\frac{(mh)^7}{7!} f^7(x)$$

$$\frac{h^7 f^7(x)}{7!} \left[ (-3)^7 \left( \frac{1}{80h} \right) + (-2)^7 \left( \frac{3}{20h} \right) + (-1)^7 \left( \frac{-3}{4h} \right) + \frac{3}{4h} + 2^7 \left( \frac{-3}{20h} \right) + 3^7 \left( \frac{1}{60h} \right) \right]$$

$$= \frac{h^7 f^7(x)}{h 7!} \left[ \frac{3^7}{60} - 2^7 \left( \frac{3}{20} \right) + \frac{3}{4} + \frac{3}{4} - 2^7 \left( \frac{3}{20} \right) + \frac{3^7}{60} \right]$$

$$= \frac{h^6 f^7(x)}{7!} \left[ \frac{6}{4} - 2^8 \left( \frac{3}{2^2 \cdot 5} \right) + \frac{2 \cdot 3^7}{60} \right]$$

$$= \frac{h^6 f^7(x)}{7!} \left[ \frac{6}{4} - \frac{(64)(3)}{5} + \frac{3^6}{10} \right]$$

$$= \frac{h^6 f^7(x)}{7!} [36]$$

$$= h^6 f^7(x) \left( \frac{36}{7!} \right)$$

$$= \boxed{h^6 f^7(x) \left( \frac{1}{140} \right)} \rightarrow f^7(x) = \frac{d^7 \sin(x)}{dx^7}$$

$\max_{0 \leq x \leq 1} |f^7(x)| = 2181.29$   
 Wolfram Alpha

$$\text{MAX Truncation Error} = \frac{2181.29}{140} h^6$$