24 Jul words that are duplicates should be ignored (words may appear just once in any owl)
31 Jul if there is more than one maximum owl, the list of owls must also be in alphabetic order

## **Assignment 2: Ordered Word Ladders**

An ordered word ladder ('owl') is an alphabetically-ordered sequence of words where each word in the sequence differs from its predecessor by one action:

- 1. changing one letter, e.g. barn→born
- 2. adding or removing one letter, e.g. band→brand and bran→ran

The following are examples of word ladders of different length:

- ban→bar→boar→boat→goat, length 5
- $an \rightarrow can \rightarrow cane \rightarrow dane \rightarrow date \rightarrow mate \rightarrow mite \rightarrow site \rightarrow size$ , length 9

## Phase 1

At the heart of the assignment is a function that compares 2 arbitrary null-terminated strings and returns true if the strings satisfy one of the 2 conditions above, and false otherwise. This function has signature:

```
切換行號
1 bool differByOne(char *, char *)
```

Write such a function and of course test it.

## Phase 2

Generate a graph that represents all the words in the input that differ by one. Each word is represented by a vertex in the graph, and vertices are adjacent if the corresponding words differ by one. For example, if a dictionary consists of the 7 words an ban bean ben hen mean men then the graph that represents all ordered word ladders would be drawn as:

```
0
| 1
| 1
| / \
2 --- 3
| / \
5---6---4
```

where the vertices 0..6 represent the 7 words in the given order. There are lots of ordered word ladders in this graph: for example,  $0 \rightarrow 1 \rightarrow 2 \rightarrow 5$  representing  $an \rightarrow ban \rightarrow bean \rightarrow mean$ . Any path between any two vertices in the graph is an owl, but notice that, although the edges are undirected, you can select vertices only in ascending order (the ladders must be in dictionary order).

In this phase of the assignment you are asked to create a graph for a dictionary, and simply print the graph.

• Input The words in the dictionary should be read from stdin. There will be whitespace between the words (i.e. spaces, tabs, newlines). You may assume that the words are in lower-case letters (so there are no capital letters, punctuation, hyphens ...) You may assume also the words are sorted in dictionary order. For example, an input file could consist of:

```
an ban bean ben hen mean men
```

You should use the *Graph ADT* from lectures to build your graph (I will be using the *Adjacency Matrix* version), and you are welcome to use any part of the *readGraph.c* program from lectures as well. You do not have to check the input for correctness (that is not what this assignment is about), so your program does not be have to handle 'bad' input (except for handling *whitespace*).

• Output Print the dictionary and the resulting graph (using showGraph() from the ADT). For the example above, the output of your program should look like:

```
Dictionary
0: an
1: ban
2: bean
3: ben
4: hen
5: mean
6: men
Ordered Word Ladder Graph
V=7, E=9
<0 1>
<1 0> <1 2> <1 3>
<2 1> <2 3> <2 5>
<3 1> <3 2> <3 4> <3 6>
<4 3> <4 6>
<5 2> <5 6>
<6 3> <6 4> <6 5>
```

You may also assume in the assignment that the length of dictionary words is less than or equal to 20, and that there will not be more than 1000 nodes in the graph.

## Phase 3

In this phase you need to find the length of the longest owl in the graph, which corresponds to finding the maximal path in the graph.

• You should first concentrate on dictionaries that have a single longest path, as in the dictionary above, which has one ladder of length 6, namely  $0 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 6$ , and no other paths are longer. When you have determined the longest owl, print its length and the corresponding path as follows:

```
Maximum ladder length: 6 Maximal ladders:
1: an -> ban -> bean -> ben -> hen -> men
```

This output appears directly after the output above of course. Note that in general the maximal path may start at any vertex in the graph.

Now address the problem of finding all the paths that have the longest length. All these paths should be output.

For example, the input file an at in it on generates the following output:

```
Dictionary
0: an
1: at
2: in
3: it
4: on
Ordered Word Ladder Graph
V=5, E=6

<0 1> <0 2> <0 4>

<1 0> <1 3>

<2 0> <2 3> <2 4>

<3 1> <3 2>

<4 0> <4 2>
Longest ladder length: 3
Longest ladders:
1: an -> at -> it
2: an -> in -> it
3: an -> in -> on
```

You see there are 3 owls here that have maximal length.

To test your program, you should create your own small dictionaries. If you want to see more of my examples see the links below.

- 1. 'case' example, 4 longest ladders
- 2. 'bear' example, 1 longest ladder
- 3. 'aaaa' example, 24 longest ladders