

Jeffrey_hw8

Jack Jeffrey

HW8

setup

```
# Set consistent root directory for all chunks
knitr::opts_knit$set(root.dir = "/Users/jackjeffrey/Documents/Poli502_Jeffrey/Data")
# Set CRAN mirror to avoid errors during package installation
options(repos = c(CRAN = "https://cran.rstudio.com/"))

install.packages("effects") # Only if not already installed
```

The downloaded binary packages are in
/var/folders/5g/td22kj7s5q9frby6hwm2szv80000gn/T//RtmpEdoKX8/downloaded_packages

```
library(effects)
```

Loading required package: carData

lattice theme set by effectsTheme()
See ?effectsTheme for details.

```
getwd()
```

```
[1] "/Users/jackjeffrey/Documents/Poli502_Jeffrey/hw8"
```

```
setwd("/Users/jackjeffrey/Documents/Poli502_Jeffrey/Data")

world <- read.csv("world.csv")

world <- read.csv("/Users/jackjeffrey/Documents/Poli502_Jeffrey/Data/world.csv")
```

1. Estimate a constant-only model

```
# Fit a constant only model
model_constant <- lm(women09 ~ 1, data = world)
# View summary of model
summary(model_constant)
```

Call:

```
lm(formula = women09 ~ 1, data = world)
```

Residuals:

Min	1Q	Median	3Q	Max
-17.177	-7.477	-1.627	5.773	39.123

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	17.1772	0.8238	20.85	<2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 11.05 on 179 degrees of freedom
(11 observations deleted due to missingness)

```
# Estimate of intercept/mean equals 17.1772 which is 17% female representation
# across all countries on average, standard error of 0.8238, P-value below zero
# indicates the result is statistically significant meaning there is a clear
# average.
# 110 Observations not included due to NA's.
```

2. Estimate a model that uses per capita GDP (gdp_10_thou) as the main independent variable.

```
# Fitting a linear model with women09 variable as dependent and gdp_10_thou
# as independent variable
model_gdp <- lm(women09 ~ gdp_10_thou, data = world)
# view summary of model
summary(model_gdp)
```

Call:

```
lm(formula = women09 ~ gdp_10_thou, data = world)
```

Residuals:

Min	1Q	Median	3Q	Max
-24.74	-6.74	-1.62	5.78	41.38

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	14.8430	0.9542	15.56	< 2e-16 ***
gdp_10_thou	3.4574	0.8351	4.14	5.5e-05 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 10.38 on 167 degrees of freedom

(22 observations deleted due to missingness)

Multiple R-squared: 0.09308, Adjusted R-squared: 0.08765

F-statistic: 17.14 on 1 and 167 DF, p-value: 5.501e-05

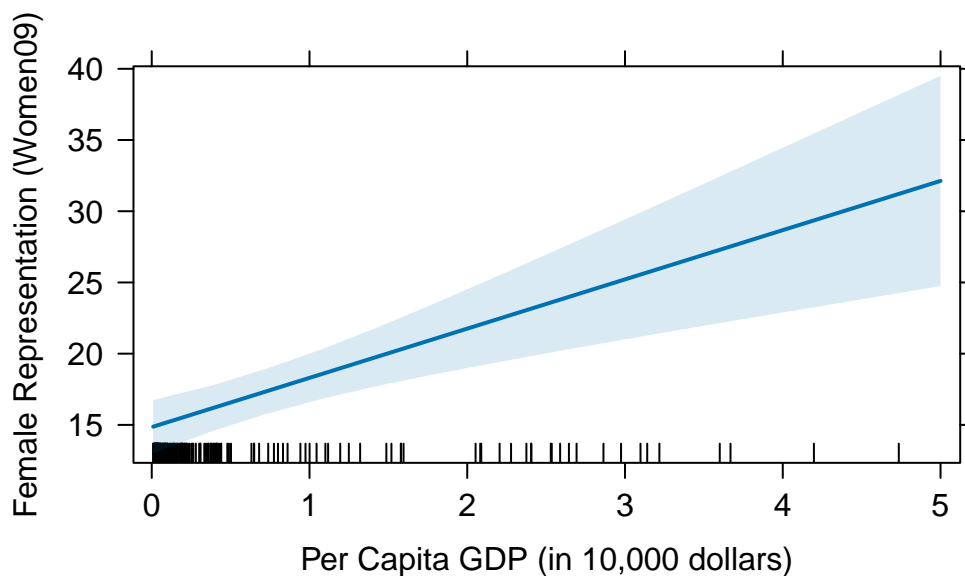
```
# The intercept is 14.8430. When GDP (gdp_10_thou) is 0, the baseline female
# representation would be approximately 14.84%. The coefficient for GDP is 3.4574, meaning
# for each increase of 1,000 dollars in per capita GDP, female representation is
# expected to increase by 3.46%. The p-value for gdp_10_thou is 5.5e-05, which is
# much smaller than 0.05. This means that the relationship between GDP and female
# representation is statistically significant.
# The R-squared value is low (9.3%), which suggests that while GDP
# is statistically significant, it explains only a small portion
# of the variation in female representation.
```

3. Create a graph that shows the estimated effect of per capita GDP on female representation

using the effect function.

```
# Create effect graph for GDP per capita's effect on female representation
effect_gdp <- effect("gdp_10_thou", model_gdp)
plot(effect_gdp, main = "Estimated Effect of Per Capita GDP on Female Representation",
      xlab = "Per Capita GDP (in 10,000 dollars)", ylab = "Female Representation (Women09)")
```

Estimated Effect of Per Capita GDP on Female Representation



4. Estimate a model that uses a dummy variable that measures electoral system (pr_sys) as the

main independent variable.

```
# Investigate PR system variable to see if it is binary
unique(world$pr_sys)
```

```
[1] "No"  "Yes"
```

```
# Estimate a model with PR system as the main independent variable
model_pr_sys <- lm(women09 ~ pr_sys, data = world)
# summarize result
summary(model_pr_sys)
```

Call:

```
lm(formula = women09 ~ pr_sys, data = world)
```

Residuals:

Min	1Q	Median	3Q	Max
-16.589	-7.835	-1.860	7.140	33.911

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	14.1596	0.9686	14.619	< 2e-16 ***
pr_sysYes	8.2297	1.5996	5.145	7.02e-07 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 10.34 on 178 degrees of freedom

(11 observations deleted due to missingness)

Multiple R-squared: 0.1295, Adjusted R-squared: 0.1246

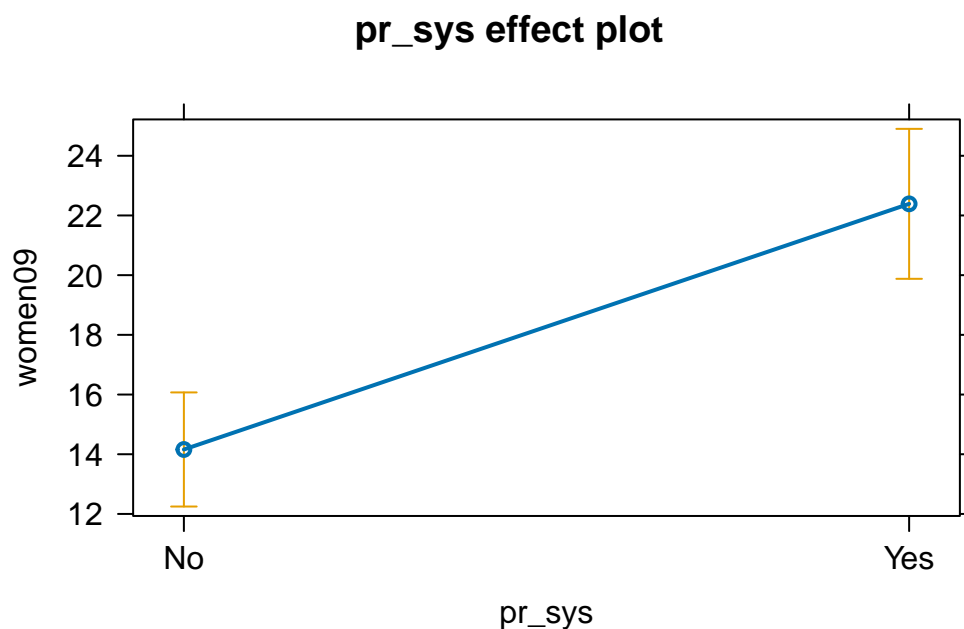
F-statistic: 26.47 on 1 and 178 DF, p-value: 7.019e-07

```
# Proportional representation has a positive effect on female representation,
# with a coefficient of 8.23. P-value is 7.02e-07 and highly significant,
# meaning the electoral system has a statistically significant impact
# on female representation. The R-squared value is quite low, suggesting
# that the electoral system alone explains only about 12.95% of the
# variation in female representation. For countries with a non-proportional
# representation electoral system, the average
# female representation is about 14.16.
```

5. Create a graph that shows the estimated effect of electoral system on female representation

using the effect function.

```
# Create an effect graph for the effect of electoral systems
# on female representation
effect_pr_sys <- effect("pr_sys", model_pr_sys)
# Plot the effect
plot(effect_pr_sys)
```



```
# Based on the plot, proportional representation systems result in
# much higher female representation
```

6. Estimate a model that includes per capita GDP AND electoral system dummy at the same time.

```
# Create a multiple regression model
model_gdp_prsys <- lm(women09 ~ gdp_10_thou + pr_sys, data = world)
# View results
summary(model_gdp_prsys)
```

Call:

```
lm(formula = women09 ~ gdp_10_thou + pr_sys, data = world)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-20.371	-7.872	-1.266	6.399	36.148

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	12.3922	1.0248	12.092	< 2e-16 ***
gdp_10_thou	2.7864	0.7948	3.506	0.000585 ***
pr_sysYes	7.7007	1.5713	4.901	2.25e-06 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 9.73 on 166 degrees of freedom

(22 observations deleted due to missingness)

Multiple R-squared: 0.2077, Adjusted R-squared: 0.1982

F-statistic: 21.76 on 2 and 166 DF, p-value: 4.049e-09

```
# Interpretation - The residual standard error of 9.73 is the average difference
# between the actual values of female representation and the values
# predicted by the model. 20.77% of the variation in female representation
# is explained by the per capita GDP and electoral system combined based on the R-squared value.
# With a p-value of 4.049e-09, this model is highly significant.
```

7. Comparing the four models you have estimated so far, which one fits the data best?

```
# Model 4 fits the data best of the four models as it has
# the lowest Residual Standard Error and highest Adjusted R-squared
# meaning it accounts for more of the variation in female representation after penalizing for
```

8. Create a graph that shows the effect of per capita GDP on Y for countries that adopt a

proportional representation system.

```
# filter out missing data in pr_sys (ensure pr_sys is a factor with 1/0 values or "Yes"/"No")
world$pr_sys <- as.factor(world$pr_sys) # make sure it's a factor
levels(world$pr_sys) # check factor levels to ensure correct filtering
```

```
[1] "No" "Yes"
```

```
# Filter data for countries with proportional representation system
pr_data <- subset(world, pr_sys == "Yes") # Adjust to match your factor level

# Define the model
pr_model <- lm(women09 ~ gdp_10_thou, data = pr_data)

# Generate predictions
gdp_seq <- seq(min(pr_data$gdp_10_thou, na.rm = TRUE),
               max(pr_data$gdp_10_thou, na.rm = TRUE),
               length.out = 100)

# Create data frame from predictions
prediction_data <- data.frame(gdp_10_thou = gdp_seq)

# Predict Y for GDP values
prediction_data$women09_pred <- predict(pr_model, newdata = prediction_data)

# Load tidyverse
library(tidyverse)
```

```
-- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
v dplyr      1.1.4      v readr      2.1.5
v forcats    1.0.0      v stringr    1.5.1
v ggplot2    3.5.1      v tibble     3.2.1
v lubridate  1.9.3      v tidyr      1.3.1
v purrr      1.0.2

-- Conflicts ----- tidyverse_conflicts() --
x dplyr::filter() masks stats::filter()
```

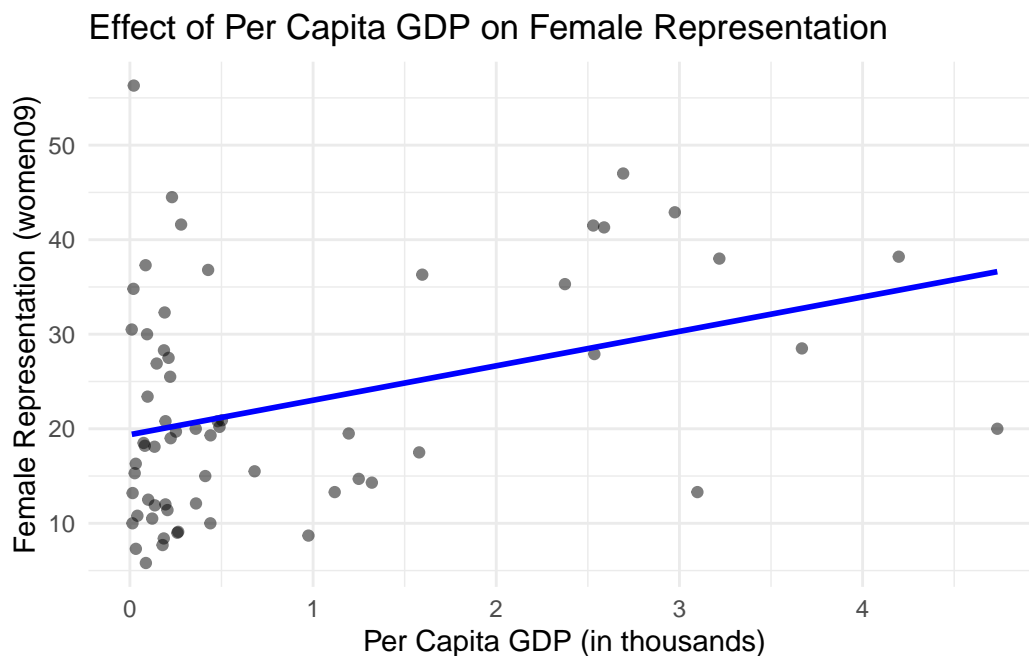


```
x dplyr::lag()      masks stats::lag()
i Use the conflicted package (<http://conflicted.r-lib.org/>) to force all conflicts to become
```

```
# Graph plot
ggplot(pr_data, aes(x = gdp_10_thou, y = women09)) +
  geom_point(alpha = 0.5) + # Scatterplot of actual data
  geom_line(data = prediction_data, aes(x = gdp_10_thou, y = women09_pred),
           color = "blue", size = 1) + # Predicted effect line
  labs(
    title = "Effect of Per Capita GDP on Female Representation",
    x = "Per Capita GDP (in thousands)",
    y = "Female Representation (women09)"
  ) +
  theme_minimal()
```

Warning: Using `size` aesthetic for lines was deprecated in ggplot2 3.4.0.
i Please use `linewidth` instead.

Warning: Removed 4 rows containing missing values or values outside the scale range
(`geom_point()`).

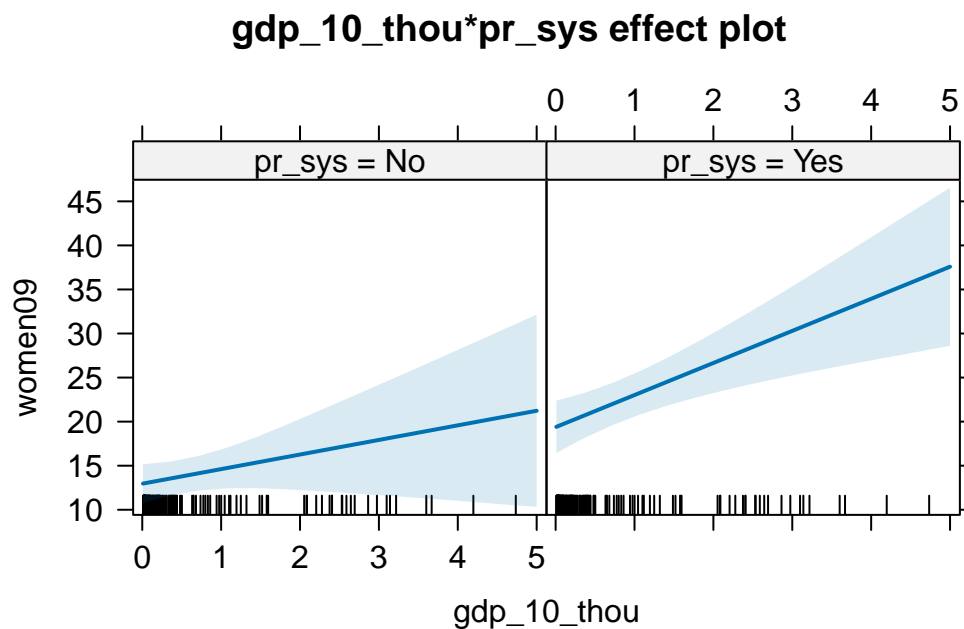


9. Try creating the same graph by providing “gdp_10_thou:pr_sys” as the term.

```
# Model with interaction term
model_interaction <- lm(women09 ~ gdp_10_thou * pr_sys, data = world)

# Plot effect for interaction term
effect_gdp_pr_interaction <- Effect(
  focal.predictors = c("gdp_10_thou", "pr_sys"),
  mod = model_interaction,
  given.values = list(pr_sysYes = 1)
)

# Plot graph
plot(effect_gdp_pr_interaction)
```



10. Estimate a regression model of female representation that uses region as the main

independent variable.

```
# Ensure region is a factor variable
world$region <- as.factor(world$region)
# Estimate regression model
model_region <- lm(women09 ~ region, data = world)
# View model summary
summary(model_region)
```

Call:

```
lm(formula = women09 ~ region, data = world)
```

Residuals:

Min	1Q	Median	3Q	Max
-17.984	-7.135	-1.746	4.914	38.740

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	17.5600	1.4445	12.157	< 2e-16 ***
regionAsia-Pacific	-5.0569	2.2407	-2.257	0.0253 *
regionC&E Europe	-0.7680	2.4171	-0.318	0.7511
regionMiddle East	-8.0705	2.6511	-3.044	0.0027 **
regionN. America	4.8067	5.7780	0.832	0.4066
regionS. America	0.4244	2.2407	0.189	0.8500
regionScandinavia	23.9600	4.5679	5.245	4.54e-07 ***
regionW. Europe	6.1926	2.6511	2.336	0.0207 *

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 9.69 on 172 degrees of freedom

(11 observations deleted due to missingness)

Multiple R-squared: 0.2615, Adjusted R-squared: 0.2314

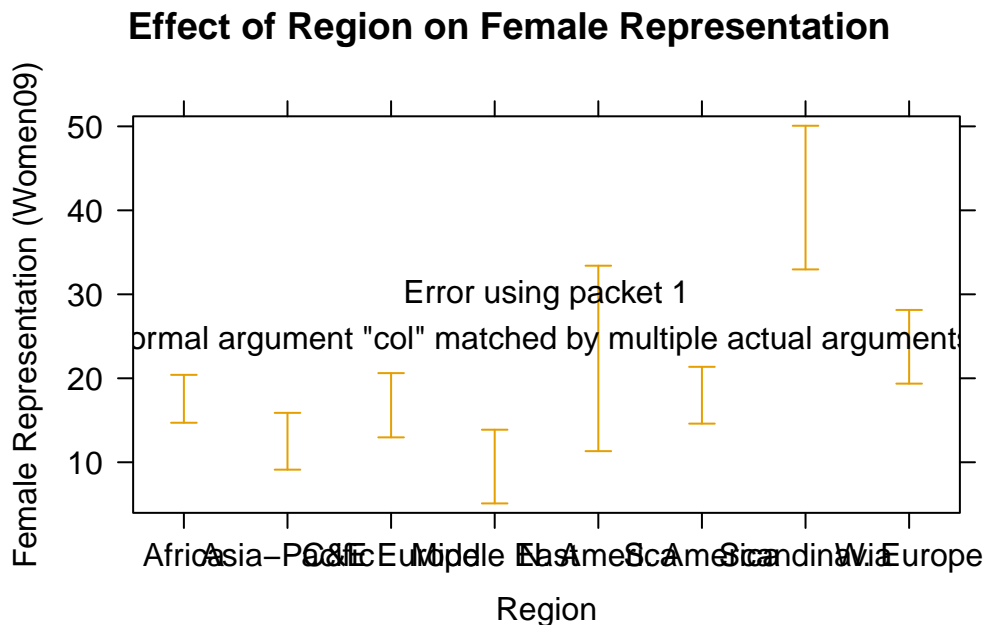
F-statistic: 8.7 on 7 and 172 DF, p-value: 3.929e-09

```
# The regions with statistically significant results are - Asia-Pacific, Middle
# East, Scandinavia, and Western Europe.
# The Scandinavia region has the highest positive impact
# on female representation, while the Middle East has the
# largest negative impact. The Multiple R-squared of 0.2615
# indicates that approximately 26.15% of the variability
# in female representation is explained by the region variable.
```

11. Create an effect plot that shows the relationship between region and female

representation.

```
# Generate effect of region on female representation
effect_region <- Effect(focal.predictors = "region", mod = model_region)
# Plot the effect
plot(effect_region, main = "Effect of Region on Female Representation",
      xlab = "Region", ylab = "Female Representation (Women09)",
      col = "blue", cex.lab = 1.2, cex.axis = 1.2)
```



12. Estimate a regression model of female representation on per capita GDP that controls for

region.

```
# Fit the model with per capita GDP and region as independent variables
model_gdp_region <- lm(women09 ~ gdp_10_thou + region, data = world)
# View model summary
summary(model_gdp_region)
```

Call:

```
lm(formula = women09 ~ gdp_10_thou + region, data = world)
```

Residuals:

Min	1Q	Median	3Q	Max
-17.123	-6.959	-1.845	4.348	38.563

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	17.7141	1.4194	12.480	< 2e-16 ***
gdp_10_thou	1.0914	1.2707	0.859	0.391693
regionAsia-Pacific	-4.9372	2.2856	-2.160	0.032254 *
regionC&E Europe	-1.2315	2.3610	-0.522	0.602678
regionMiddle East	-11.0675	2.8079	-3.942	0.000121 ***
regionN. America	2.2842	6.1856	0.369	0.712410
regionS. America	-0.9546	2.2279	-0.428	0.668890
regionScandinavia	20.3981	5.8626	3.479	0.000648 ***
regionW. Europe	3.1906	3.9828	0.801	0.424264

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 9.38 on 160 degrees of freedom

(22 observations deleted due to missingness)

Multiple R-squared: 0.2903, Adjusted R-squared: 0.2549

F-statistic: 8.183 on 8 and 160 DF, p-value: 2.991e-09

```
# The model shows the effect of GDP after controlling for region.
# The Adjusted R-squared of 0.2643 is slightly higher than previous models.
```

13. Estimate a regression model of female representation on frac_eth3, a

three-category ordinal variable that measures levels of ethnic fractionalization.

```
# Create a model using ethnic fractionalization as a categorical nominal variable
model_frac_eth3 <- lm(women09 ~ factor(frac_eth3), data = world)
# view summary of model
summary(model_frac_eth3)
```

Call:

```
lm(formula = women09 ~ factor(frac_eth3), data = world)
```

Residuals:

Min	1Q	Median	3Q	Max
-17.457	-7.502	-1.610	5.493	39.416

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	11.967	6.422	1.864	0.0641 .
factor(frac_eth3)High	5.469	6.583	0.831	0.4072
factor(frac_eth3)Low	5.491	6.578	0.835	0.4050
factor(frac_eth3)Medium	4.918	6.588	0.746	0.4564

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 11.12 on 176 degrees of freedom

(11 observations deleted due to missingness)

Multiple R-squared: 0.004347, Adjusted R-squared: -0.01262

F-statistic: 0.2562 on 3 and 176 DF, p-value: 0.8569

14. Based on the results, do you think ethnic fractionalization levels have a positive/negative impact on female representation?

```
# Based on the regression results,  
# we cannot conclude that ethnic fractionalization  
# levels have a statistically significant positive  
# or negative impact on female  
# representation in this dataset.  
# The p-values for all categories of ethnic fractionalization  
# are high, and the model as a whole is not significant.
```