

Graves 2013, “Generating Sequences with Recurrent Neural Networks”

Johannes Bausch and Jack Kamm

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Outline

- 1 RNN and LSTM
- 2 Learning and Generating Sequences
- 3 Generating handwriting

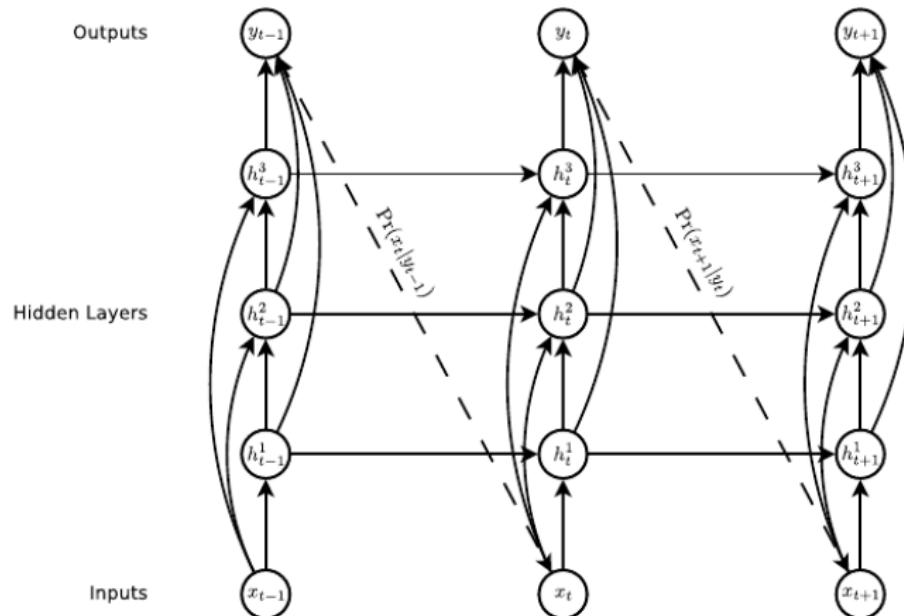
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2 Learning and Generating Sequences

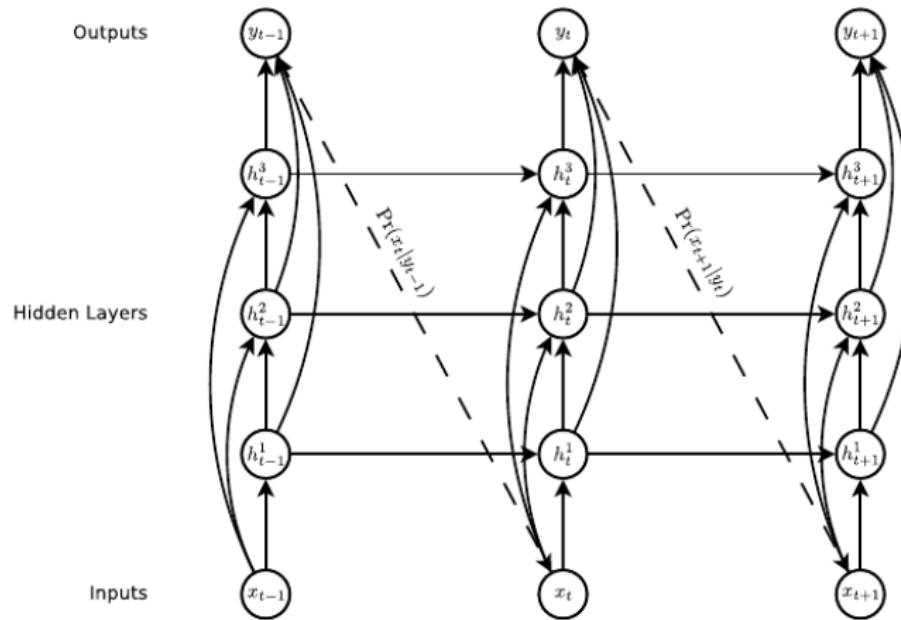
3 Generating handwriting

Recurrent Neural Networks



Input x_t , hidden layers h_t^n , output y_t , generative model $\mathbb{P}(x_{t+1} | y_t)$

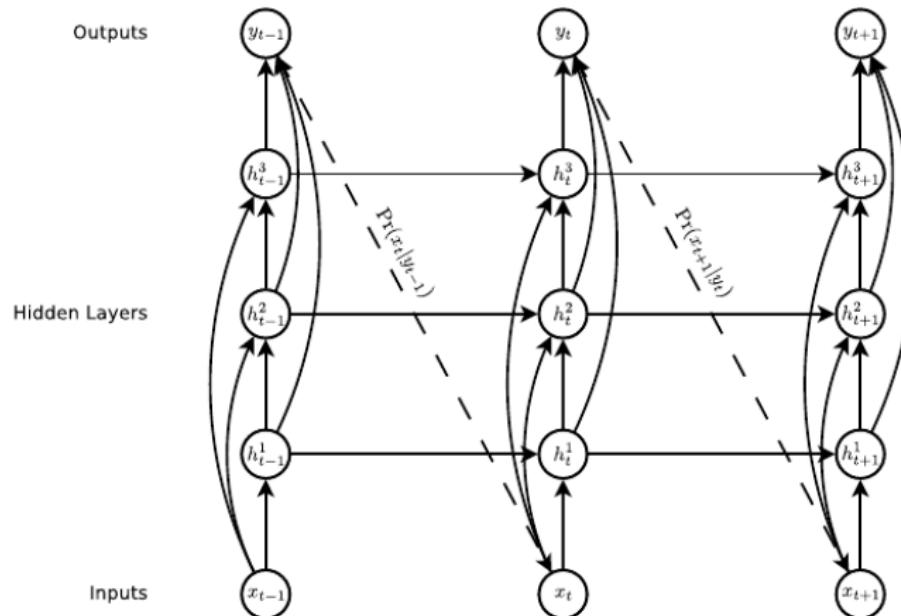
Recurrent Neural Networks



$h_t^n = \text{nonlinear link} \circ \text{affine combo of } x_t, h_{t-1}^n, h_t^{n-1}$

$$h_t^n = \mathcal{H}(W_{ih^n}x_t + W_{h^{n-1}h^n}h_t^{n-1} + W_{h^nh^n}h_{t-1}^n + b_h^n)$$

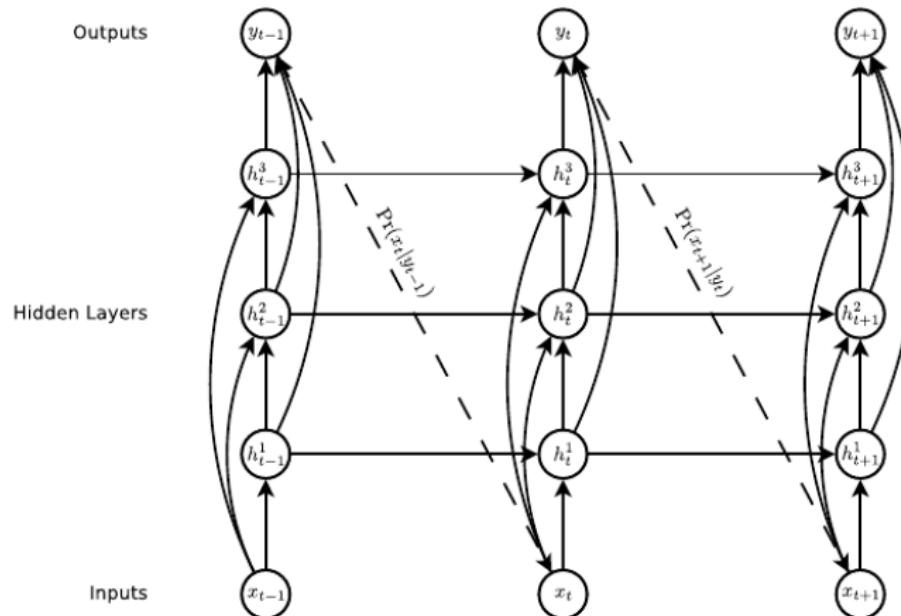
Recurrent Neural Networks



$$y_t = \text{nonlinear link} \circ \text{affine combo of } h_t^n$$

$$y_t = \mathcal{Y}(b_y + \sum_{n=1}^N W_{h^n y} h_t^n)$$

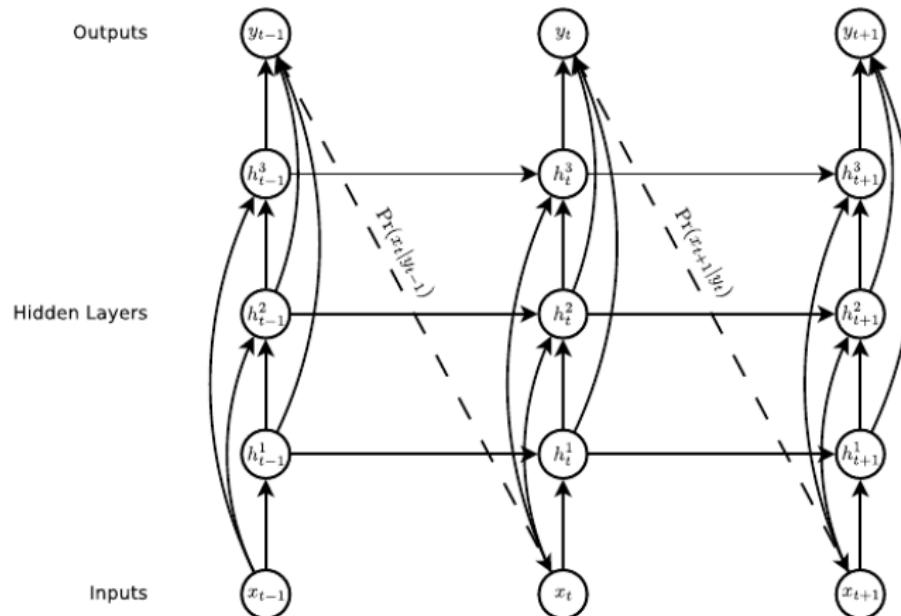
Recurrent Neural Networks



Train by maximizing likelihood of generative model:

$$\mathbb{P}(\mathbf{x}) = \prod_{t=1}^T \mathbb{P}(x_t | y_{t-1})$$

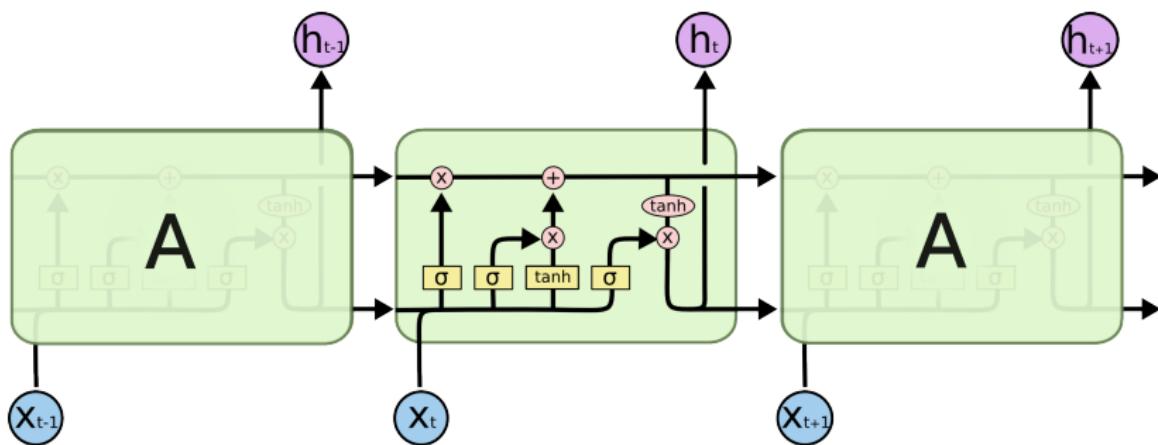
Recurrent Neural Networks



Compute $\nabla_\Theta \log \mathbb{P}_\Theta(\mathbf{x})$ by "truncated backpropagation through time"

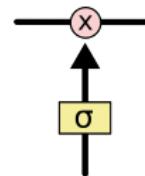
- i.e., reverse chain-rule + "clip" exploding derivatives

Long short term memory¹

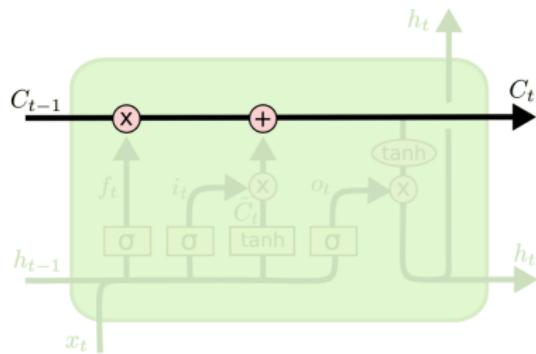


Information passes through a series of “gates”

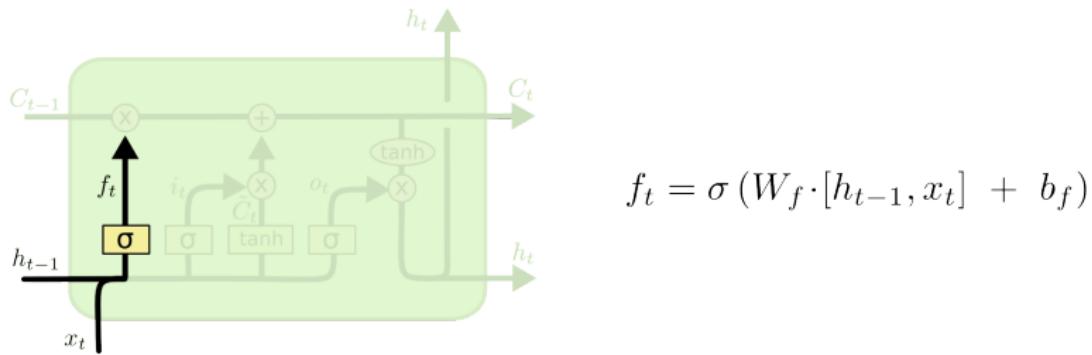
- “Gate” = multiplication with sigmoid
 - $\sigma = 0 \Rightarrow$ “let nothing thru”
 - $\sigma = 1 \Rightarrow$ “let all thru”



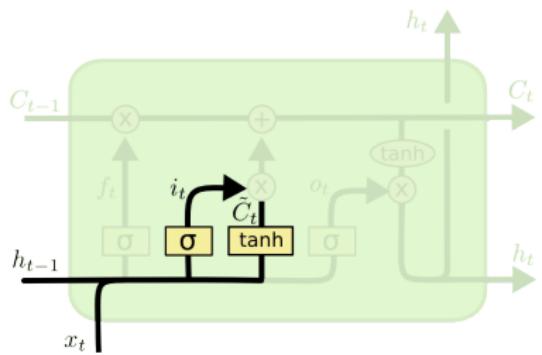
¹graphics have slight differences with Graves 2013; they are taken from:
<https://colah.github.io/posts/2015-08-Understanding-LSTMs>



C_t = “cell state” = flows horizontally across LSTM units



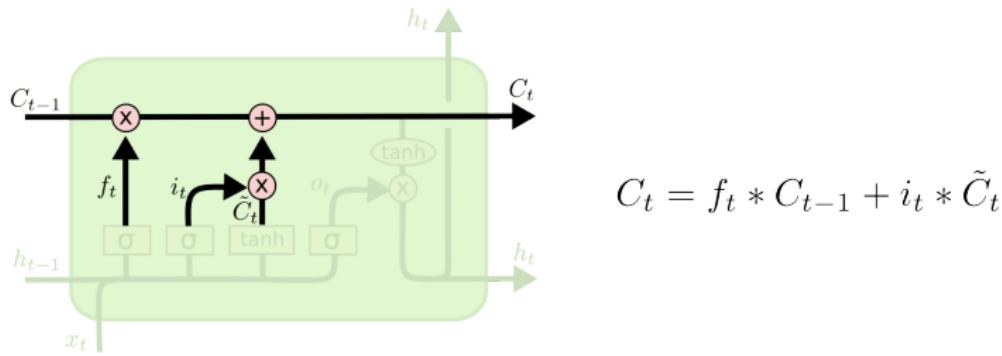
f_t = “forget gate” = gate to forget information from C_{t-1}



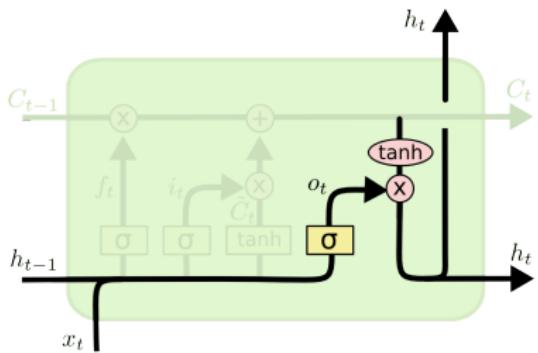
$$i_t = \sigma(W_i \cdot [h_{t-1}, x_t] + b_i)$$

$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

i_t = “input gate” = gate to add information from h_{t-1} and x_t to C_t



Update C_t using f_t and i_t

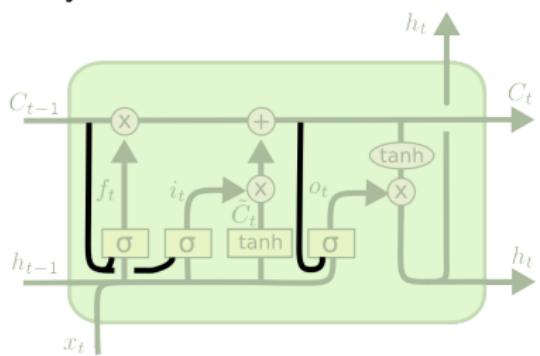


$$o_t = \sigma (W_o [h_{t-1}, x_t] + b_o)$$

$$h_t = o_t * \tanh (C_t)$$

o_t = “output gate” = gate to output information to cell above/right

Many variations on LSTM exist. Here is the one used in Graves 2013:



$$f_t = \sigma(W_f \cdot [C_{t-1}, h_{t-1}, x_t] + b_f)$$

$$i_t = \sigma(W_i \cdot [C_{t-1}, h_{t-1}, x_t] + b_i)$$

$$o_t = \sigma(W_o \cdot [C_t, h_{t-1}, x_t] + b_o)$$

Notice the extra “peephole” connections from C to f, i, o

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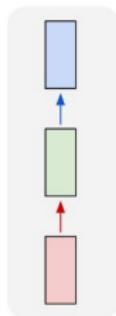
2 Learning and Generating Sequences

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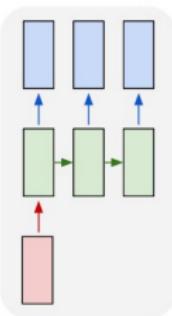
Text Prediction

How do we model a NN that takes a variable input length?
(<http://karpathy.github.io/2015/05/21/rnn-effectiveness/>).

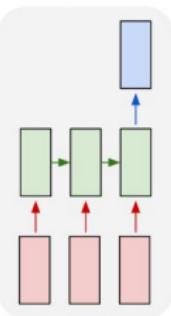
one to one



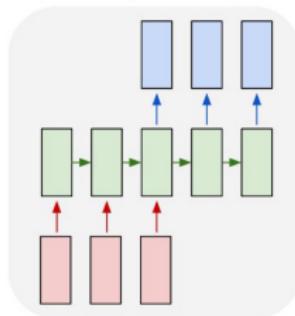
one to many



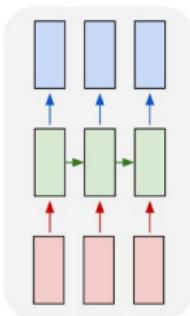
many to one

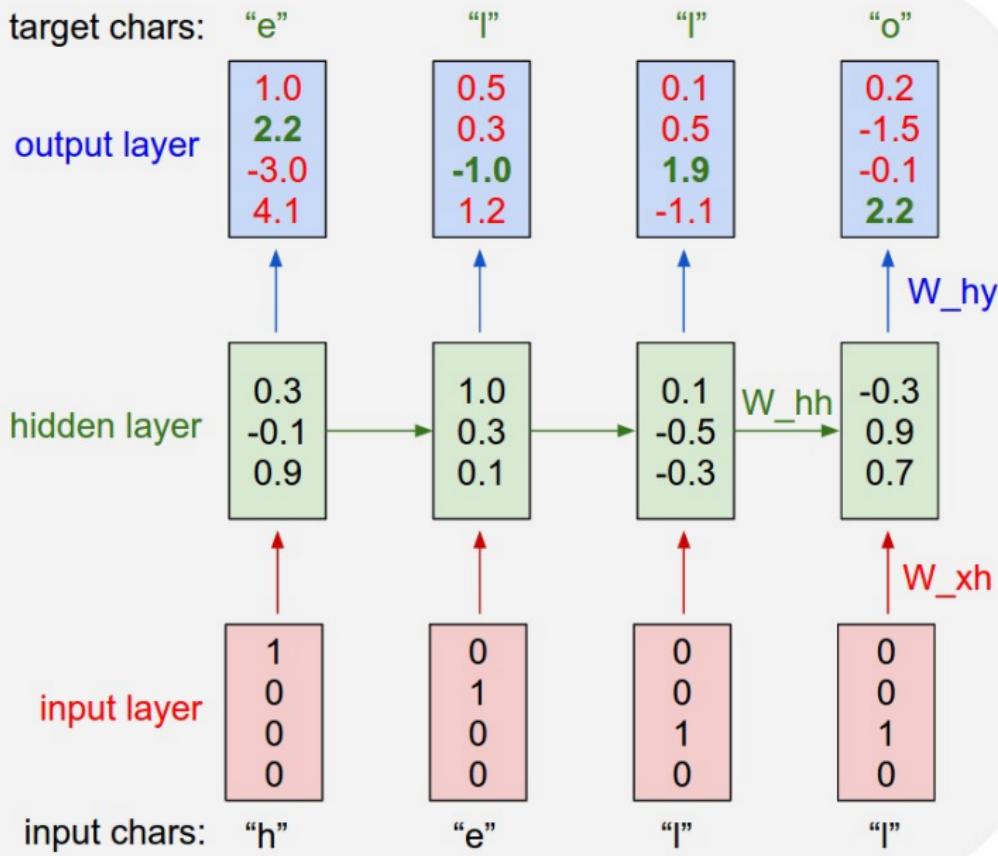


many to many



many to many





RNN and LSTM Shakespeare

We compare an RNN with an LSTM to predict Shakespeare.

LSTM Shakespeare

KING LEAR:

O, if you were a feeble sight, the courtesy of your law,
Your sight and several breath, will wear the gods
With his heads, and my hands are wonder'd at the deeds,
So drop upon your lordship's head, and your opinion
Shall be against your honour.

LSTM Wikipedia

Naturalism and decision for the majority of Arab countries' capitalide was grounded by the Irish language by [[John Clair]], [[An Imperial Japanese Revolt]], associated with Guangzham's sovereignty. His generals were the powerful ruler of the Portugal in the [[Protestant Immineners]], which could be said to be directly in Cantonese Communication, which followed a ceremony and set inspired prison, training. The emperor travelled back to [[Antioch, Perth, October 25|21]] to note, the Kingdom of Costa Rica, unsuccessful fashioned the [[Thrales]], [[Cynth's Dajoard]], known in western [[Scotland]], near Italy to the conquest of India with the conflict.

LSTM Wiki Markdown

```
{ { cite journal | id=Cerling Nonforest Department|format=
    Newlymeslated|none } }
''www.e-complete''.

'''See also'''': [[List of ethical consent processing]]

== See also ==
* [[Iender dome of the ED]]
* [[Anti-autism]]

====[[Religion|Religion]]====
* [[French Writings]]
* [[Maria]]
* [[Revelation]]
* [[Mount Agamul]]
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LSTM XML

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    <text xml:space="preserve">#REDIRECT [[Christianity]]</text>
  </revision>
</page>
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LSTM XML

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    <comment>Automated conversion</comment>
    <text xml:space="preserve">#REDIRECT [[Christianity]]</text>
  </revision>
</page>
```

LSTM LAT \backslash EX

For $\bigoplus_{m=1,\dots,m} \mathcal{L}_{m\bullet} = 0$, hence we can find a closed subset H in \mathcal{H} and any sets \mathcal{F} on X , U is a closed immersion of S , then $U \rightarrow T$ is a separated algebraic space.

Proof. Proof of (1). It also start we get

$$S = \text{Spec}(R) = U \times_X U \times_X U$$

and the comparicoly in the fibre product covering we have to prove the lemma generated by $\coprod Z \times_U U \rightarrow V$. Consider the maps M along the set of points Sch_{fppf} and $U \rightarrow U$ is the fibre category of S in U in Section ?? and the fact that any U affine, see Morphisms, Lemma ???. Hence we obtain a scheme S and any open subset $W \subset U$ in $\text{Sh}(G)$ such that $\text{Spec}(R') \rightarrow S$ is smooth or an

$$U = \bigcup U_i \times_{S_i} U_i$$

which has a nonzero morphism we may assume that f_i is of finite presentation over S . We claim that $\mathcal{O}_{X,x}$ is a scheme where $x, x', s'' \in S'$ such that $\mathcal{O}_{X,x'} \rightarrow \mathcal{O}'_{X',x'}$ is separated. By Algebra, Lemma ?? we can define a map of complexes $\text{GL}_{S'}(x'/S'')$ and we win. \square

To prove study we see that $\mathcal{F}|_U$ is a covering of X' , and \mathcal{T}_i is an object of $\mathcal{F}_{X/S}$ for $i > 0$ and \mathcal{F}_p exists and let \mathcal{F}_i be a presheaf of \mathcal{O}_X -modules on \mathcal{C} as a \mathcal{F} -module. In particular $\mathcal{F} = U/\mathcal{F}$ we have to show that

$$\widetilde{M}^\bullet = \mathcal{I}^\bullet \otimes_{\text{Spec}(k)} \mathcal{O}_{S,s} - i_X^{-1} \mathcal{F}$$

is a unique morphism of algebraic stacks. Note that

$$\text{Arrows} = (\text{Sch}/S)^{\text{opp}}_{fppf}, (\text{Sch}/S)_{fppf}$$

and

$$V = \Gamma(S, \mathcal{O}) \longrightarrow (U, \text{Spec}(A))$$

is an open subset of X . Thus U is affine. This is a continuous map of X is the inverse, the groupoid scheme S .

Proof. See discussion of sheaves of sets. \square

The result for prove any open covering follows from the less of Example ???. It may replace S by $X_{\text{spaces},\text{etale}}$ which gives an open subspace of X and T equal to S_{Zar} , see Descent, Lemma ???. Namely, by Lemma ?? we see that R is geometrically regular over S .

Lemma 0.1. Assume (3) and (3) by the construction in the description.

Suppose $X = \lim |X|$ (by the formal open covering X and a single map $\text{Proj}_X(\mathcal{A}) = \text{Spec}(B)$ over U compatible with the complex

$$\text{Set}(\mathcal{A}) = \Gamma(X, \mathcal{O}_{X,\mathcal{O}_X}).$$

When in this case of to show that $\mathcal{Q} \rightarrow \mathcal{C}_{Z/X}$ is stable under the following result in the second conditions of (1), and (3). This finishes the proof. By Definition ?? (without element is when the closed subschemes are catenary. If T is surjective we may assume that T is connected with residue fields of S . Moreover there exists a closed subspace $Z \subset X$ where U in X' is proper (some defining as a closed subset of the uniqueness it suffices to check the fact that the following theorem

(1) f is locally of finite type. Since $S = \text{Spec}(R)$ and $Y = \text{Spec}(R)$.

Proof. This is form all sheaves of sheaves on X . But given a scheme U and a surjective étale morphism $U \rightarrow X$. Let $U \cap U = \coprod_{i=1,\dots,n} U_i$ be the scheme X over S at the schemes $X_i \rightarrow X$ and $U = \lim_i X_i$. \square

The following lemma surjective restrecomposes of this implies that $\mathcal{F}_{x_0} = \mathcal{F}_{x_0} = \mathcal{F}_{X,\dots,0}$.

Lemma 0.2. Let X be a locally Noetherian scheme over S , $E = \mathcal{F}_{X/S}$. Set $\mathcal{I} = \mathcal{J}_1 \subset \mathcal{I}'_n$. Since $\mathcal{I}^n \subset \mathcal{I}^n$ are nonzero over $i_0 \leq p$ is a subset of $\mathcal{J}_{n,0} \circ \tilde{A}_2$ works.

Lemma 0.3. In Situation ???. Hence we may assume $q' = 0$.

Proof. We will use the property we see that p is the next functor (??). On the other hand, by Lemma ?? we see that

$$D(\mathcal{O}_{X'}) = \mathcal{O}_X(D)$$

where K is an F -algebra where δ_{n+1} is a scheme over S . \square

LSTM C++

```
/*
 * If this error is set, we will need anything right after
 * that BSD.
 */
static void action_new_function(struct s_stat_info *wb)
{
    unsigned long flags;
    int lel_idx_bit = e->edd, *sys & ~((unsigned long) *
        FIRST_COMPAT);
    buf[0] = 0xFFFFFFFF & (bit << 4);
    min(inc, slist->bytes);
    printk(KERN_WARNING "Memory allocated %02x/%02x, "
        "original MLL instead\n"),
    min(min(multi_run - s->len, max) * num_data_in),
        frame_pos, sz + first_seg);
    div_u64_w(val, inb_p);
    spin_unlock(&disk->queue_lock);
    mutex_unlock(&s->sock->mutex);
    mutex_unlock(&func->mutex);
    return disassemble(info->pending_bh);
}
```

LSTM C++

```
static void num_serial_settings(struct tty_struct *tty)
{
    if (tty == tty)
        disable_single_st_p(dev);
    pci_disable_spool(port);
    return 0;
}

static void do_command(struct seq_file *m, void *v)
{
    int column = 32 << (cmd[2] & 0x80);
    if (state)
        cmd = (int)(int_state ^ (in_8(&ch->ch_flags) & Cmd) ? 2 : 1);
    else
        seq = 1;
    for (i = 0; i < 16; i++) {
        if (k & (1 << i))
            pipe = (in_use & UMXTHREAD_UNCCA) +
                ((count & 0xfffffffffffff8) & 0x0000000f) << 8;
        if (count == 0)
            sub(pid, ppc_md.kexec_handle, 0x20000000);
        pipe_set_bytes(i, 0);
    }
    /* Free our user pages pointer to place camera if all dash */
    subsystem_info = &of_changes[PAGE_SIZE];
    rek_controls(offset, idx, &soffset);
    /* Now we want to deliberately put it to device */
    control_check_polarity(&context, val, 0);
    for (i = 0; i < COUNTER; i++)
        seq_puts(s, "policy ");
}
```

Visualizing Predictions: What Do Neurons Do?

<code>http://www.ynetnews.com/</code>	English-language website of Israel's largest news website
<code>http://www.bacahets.com/</code>	- English language site of Israel's largest news website
<code>mw-2@philipssis.ern.c</code>	(deeen) pesaaki ieel edh,irthraonse, cose
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Visualizing Predictions: What Do Neurons Do?

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Visualizing Predictions: What Do Neurons Do?

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a dpeamArbdeorpitee]dts-| T{[[BaAvTpoSwaoo...oacstp,tcoa2drulwoclens

Visualizing Predictions: What Do Neurons Do?

The figure shows a heatmap where each row represents a character and each column represents a time step. The colors indicate the activation level of different neurons for each character at each time step. The sequence being generated is "The Guardian Israel Insider http://www.israeliins".

'	'	[[The	Guar	dian]]	'	.	*	*	[[Israe	l	Insider]]	'	[ht	t	p	:	/	/	www.	israeli	ins		
l	'	[[The	Soi	rd	an]]	'	.	*	*	[[Tn	iae	I	hde]]	'	([tp	:	/	/	www.	bmsacl	ng.	
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Visualizing Predictions: What Do Neurons Do?

Cell sensitive to position in line:

The sole importance of the crossing of the Berezina lies in the fact that it plainly and indubitably proved the fallacy of all the plans for cutting off the enemy's retreat and the soundness of the only possible line of action--the one Kutuzov and the general mass of the army demanded--namely, simply to follow the enemy up. The French crowd fled at a continually increasing speed and all its energy was directed to reaching its goal. It fled like a wounded animal and it was impossible to block its path. This was shown not so much by the arrangements it made for crossing as by what took place at the bridges. When the bridges broke down, unarmed soldiers, people from Moscow and women with children who were with the French transport, all--carried on by vis inertiae--pressed forward into boats and into the ice-covered water and did not, surrender.

Cell that turns on inside quotes:

"You mean to imply that I have nothing to eat out of... On the contrary, I can supply you with everything even if you want to give dinner parties," warmly replied Chichagov, who tried by every word he spoke to prove his own rectitude and therefore imagined Kutuzov to be animated by the same desire.

Kutuzov, shrugging his shoulders, replied with his subtle penetrating smile: "I meant merely to say what I said."

Visualizing Predictions: What Do Neurons Do?

Cell that robustly activates inside if statements:

```
static int __dequeue_signal(struct sigpending *pending, sigset_t *mask,
    siginfo_t *info)
{
    int sig = next_signal(pending, mask);
    if (sig) {
        if (current->notifier) {
            if (sigismember(current->notifier_mask, sig)) {
                if (!!(current->notifier)(current->notifier_data)) {
                    clear_thread_flag(TIF_SIGPENDING);
                    return 0;
                }
            }
        }
        collect_signal(sig, pending, info);
    }
    return sig;
}
```

A large portion of cells are not easily interpretable. Here is a typical example:

```
/* Unpack a filter field's string representation from user-space
 * buffer. */
char *audit_unpack_string(void **bufp, size_t *remain, size_t len)
{
    char *str;
    if (!*bufp || (len == 0) || (len > *remain))
        return ERR_PTR(-EINVAL);
    /* Of the currently implemented string fields, PATH_MAX
     * defines the longest valid length.
    */
```

Visualizing Predictions: What Do Neurons Do?

Cell that turns on inside comments and quotes:

```
/* Duplicate LSM field information.  The lsm_rule is opaque, so
 * re-initialized. */
static inline int audit_dupe_lsm_field(struct audit_field *df,
    struct audit_field *sf)
{
    int ret = 0;
    char *lsm_str;
    /* our own copy of lsm_str */
    lsm_str = kstrdup(sf->lsm_str, GFP_KERNEL);
    if (unlikely(!lsm_str))
        return -ENOMEM;
    df->lsm_str = lsm_str;
    /* our own (refreshed) copy of lsm_rule */
    ret = security_audit_rule_init(df->type, df->op, df->lsm_str,
        (void *)df->lsm_rule);
    /* Keep currently invalid fields around in case they
     * become valid after a policy reload. */
    if (ret == -EINVAL) {
        pr_warn("audit rule for LSM '\\%s\\' is invalid\n",
            df->lsm_str);
        ret = 0;
    }
    return ret;
}
```

Visualizing Predictions: What Do Neurons Do?

Cell that is sensitive to the depth of an expression:

```
#ifdef CONFIG_AUDITSYSCALL
static inline int audit_match_class_bits(int class, u32 *mask)
{
    int i;
    if (classes[class]) {
        for (i = 0; i < AUDIT_BITMASK_SIZE; i++)
            if (mask[i] & classes[class][i])
                return 0;
    }
    return 1;
}
```

Cell that might be helpful in predicting a new line. Note that it only turns on for some " ") :

```
char *audit_unpack_string(void **bufp, size_t *remain, si
{
    char *str;
    if (!*bufp || (len == 0) || (len > *remain))
        return ERR_PTR(-EINVAL);
    /* of the currently implemented string fields, PATH_MAX
     * defines the longest valid length.
     */
    if (len > PATH_MAX)
        return ERR_PTR(-ENAMETOOLONG);
    str = kmalloc(len + 1, GFP_KERNEL);
    if (unlikely(!str))
        return ERR_PTR(-ENOMEM);
    memcpy(str, *bufp, len);
    str[len] = 0;
    *bufp += len;
    *remain -= len;
    return str;
}
```

Table of Contents

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2 Learning and Generating Sequences

3 Generating handwriting

would find the bus safe and sound
As for Clark, unless it were a
cancer at the ages of fifty-five
Editorial. Dilemma of
the the tides in the affairs of men;

Figure: Training samples from IAM handwriting database

$$\text{Input } x_t = (\text{pos}_t - \text{pos}_{t-1}) \times (\text{is-end-of-stroke}) \in \mathbb{R}^2 \times \{0, 1\}$$

Mixture density network

$$x_t \in \mathbb{R} \times \mathbb{R} \times \{0, 1\}$$

$$y_t = (e_t, \{\pi_t^j, \mu_t^j, \sigma_t^j, \rho_t^j\}_{j=1}^M)$$

$$\mathbb{P}(x_{t+1} | y_t) = \sum_{j=1}^M \pi_t^j \mathcal{N}(x_{t+1} | \mu_t^j, \sigma_t^j, \rho_t^j) \begin{cases} e_t & \text{if } (x_{t+1})_3 = 1 \\ 1 - e_t & \text{else} \end{cases}$$

- $e_t = \text{end-of-stroke prob} = \frac{1}{1 + \exp(\hat{e}_t)}$
- $\pi_t^j = \text{mixture prob} = \frac{\exp(\hat{\pi}_t^j)}{\sum_{j'} \exp(\hat{\pi}_t^{j'})}$
- $\mu_t^j = \text{component mean} = \hat{\mu}_t^j$
- $\sigma_t^j = \text{component variance} = \exp(\hat{\sigma}_t^j)$
- $\rho_t^j = \text{component x/y correlation} = \tanh(\hat{\rho}_t^j)$

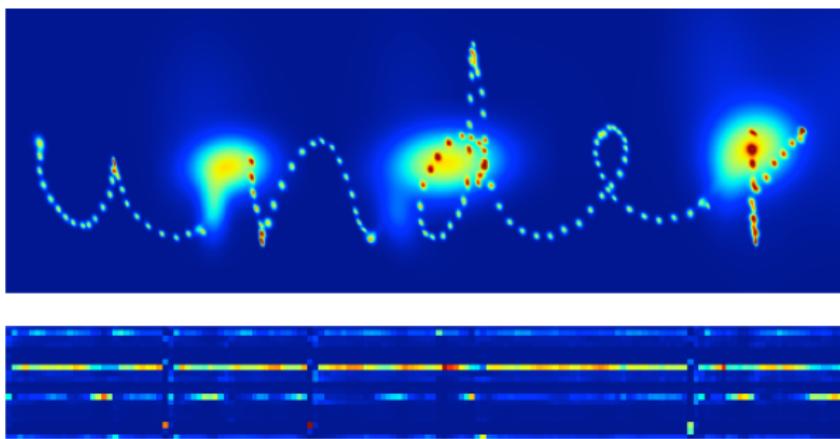


Figure: Mixture density outputs as word “under” is written

- Blobs = Predictions at end of strokes for first point in next stroke
- Lower panel = component weights

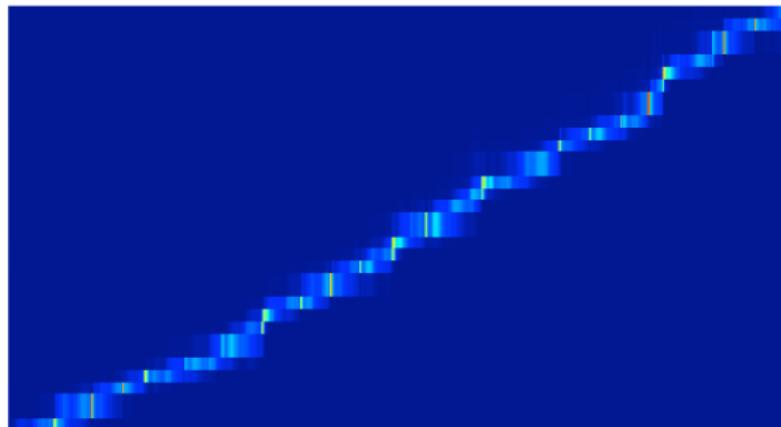
After my return from Gourkaje I have written
you my notes on the 1st before leaving the
country and another 1st before leaving the
Marine Cenotaph of King Marattra
on Board a. The account will be
purely historical as I have not been
engaged & cold wine & wine case
held. Yesterdays the garrison
style salutes during the singing of a
military march.

Figure: Samples generated by prediction network (700-timesteps each). Network has learned strokes, some characters, and even short words (e.g. "of").

- 3 hidden layers, each with 400 LSTM cells
 - 3.4×10^6 parameters total
 - Trained with rmsprop and adaptive weight noise
 - Output derivatives $\frac{\partial \log \mathbb{P}(x)}{\partial \hat{y}_t}$ clipped to be in $[-100, 100]$; LSTM derivatives clipped within $[-10, 10]$
 - Clipping vital for numerical stability

Handwriting synthesis

Thought that the muster from



thought that the muster from

- Generate handwriting for a given text
- Need to align handwriting with discrete text
- Bottom layer → distribution of current position (“soft window”)

Synthesis Network

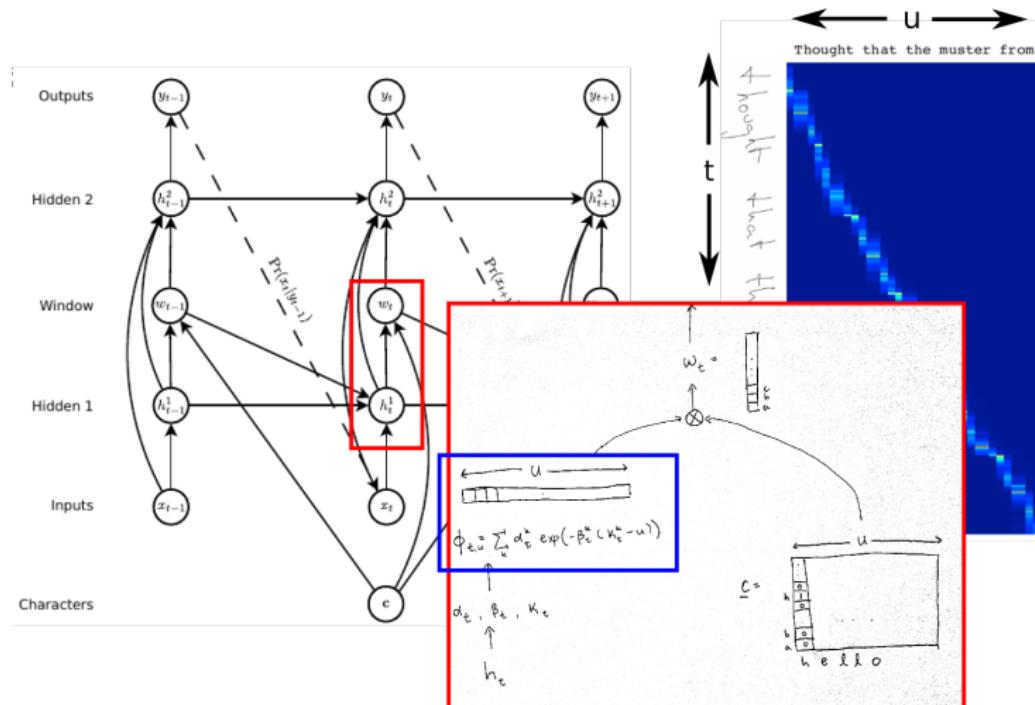


Figure: $\phi_t(h_t^1) = \text{distrn over positions}$; $w_t = c\phi_t = \text{distrn over characters}$

Unbiased sampling

from his travels it might have been
from his travels it might have been

more of national temperament
more of national temperament

- Sample from $\mathbb{P}(\mathbf{x} | \mathbf{c})$ by iteratively sampling from $\mathbb{P}(x_{t+1} | y_t)$
- Stop when $\phi(t, U + 1) > \max_{u \leq U} \phi(t, u)$
- First line of each block is real; subsequent lines generated by network

Biased sampling

- 0 when the samples are biased
- 0.1 towards more probable sequences
- 0.5 they get easier to read
- 2 but less diverse
- 5 until they all look
- 10 exactly the same
- 10 exactly the same
- 10 exactly the same

- ↓ variance ⇒ neater writing
 - Component variance:

$$\sigma_t^j = \exp(\hat{\sigma}_t^j - b)$$

- Mixture probabilities:

$$\pi_t^j = \frac{\exp(\hat{\pi}_t^j(1 + b))}{\sum_{j'} \exp(\hat{\pi}_t^{j'}(1 + b))}$$

Primed sampling

Take the smooth away when they are
when the network is primed
with a real sequence
the samples mimic
the writer's style

She looked closely as she
when the network is primed
with a real sequence
the samples mimic
the writer's style

He dismissed the idea
when the network is primed
with a real sequence
the samples mimic
the writer's style

postman welfare Officer complement
when the network is primed
with a real sequence
the samples mimic
the writer's style

- Mimic specific person without retraining whole network
- For real \mathbf{x}, \mathbf{c} and new \mathbf{s} , set $\mathbf{c}' = \mathbf{c} + \mathbf{s}$, and clamp first T inputs to \mathbf{x}

Combining biasing + priming

Take the smooth away when they are

when the network is primed
and biased, it writes
in a cleaned up version
of the original style

She looked closely as she

when the network is primed
and biased, it writes
in a cleaned up version
of the original style

He dismissed the idea

when the network is primed
and biased, it writes
in a cleaned up version
of the original style

prison welfare Officer complement

when the network is primed
and biased, it writes
in a cleaned up version
of the original style

Application: artificial enhancement of poor handwriting?