hw1

September 22, 2023

1 Applied Problems

Jack Krebsbach Stats 313 9/16/23

1.0.1 #8

(a) Use the pd.read_csv() function to read the data into Python. Call the loaded data college. Make sure that you have the directory set to the correct location for the data.

```
[]: import numpy as np
import pandas as pd
college = pd.read_csv("./data/College.csv")
```

```
[]: # The first column is not named.
college
```

		Unn	amed: 0	Priva	te	Apps	Accept	Enrol	1 T	op10per	: \
0	Abilene	Christian Uni	versity	Y	es	1660	1232	72	1	23	3
1		Adelphi Uni	versity	Y	es	2186	1924	51:	2	16	3
2		Adrian	College	Y	es	1428	1097	33	6	22	2
3		Agnes Scott	College	Y	es	417	349	13	7	60)
4	Alask	a Pacific Uni	versity	Y	es	193	146	5	5	16	3
				•••	•••	•••	•••				
772	Wor	cester State	College	1	No	2197	1515	54	3	4	ŀ
773		Xavier Uni	versity	Y	es	1959	1805	69	5	24	ŀ
774	Xavier Uni	versity of Lo	uisiana	Y	es	2097	1915	69	5	34	ŀ
775		Yale Uni	versity	Y	es	10705	2453	131	7	95	5
776	York Col	lege of Penns	ylvania	Y	es	2989	1855	69	1	28	3
	Top25perc	F.Undergrad	P.Undei	rgrad	Out	state	Room.Bo	ard B	ooks	\	
0	52	2885		537						•	
1	29	2683		1227		12280	6	450	750		
2	50	1036		99		11250	3	750	400		
3	89	510		63		12960	5	450	450		
4	44	249		869		7560	4	120	800		
	•••	•••			•••						
772	26	3089		2029		6797	3	900	500		
773	47	2849		1107		11520	4	960	600		
	1 2 3 4 772 773 774 775 776	1 2 3 4 Alask 772 Wor 773 774 Xavier Uni 775 776 York Col Top25perc 0 52 1 29 2 50 3 89 4 44 772 26	O Abilene Christian Uni 1 Adelphi Uni 2 Adrian 3 Agnes Scott 4 Alaska Pacific Uni 772 Worcester State 773 Xavier Uni 774 Xavier University of Lo 775 Yale Uni 776 York College of Penns Top25perc F.Undergrad 0 52 2885 1 29 2683 2 50 1036 3 89 510 4 44 249 772 26 3089	Abilene Christian University Adelphi University Adrian College Agnes Scott College Alaska Pacific University Worcester State College Xavier University Adrian College Agnes Scott College Alaska Pacific University T72 Worcester State College Y73 Xavier University Y64 Vavier University of Louisiana Y65 Yale University Y76 York College of Pennsylvania Top25perc F.Undergrad P.Under 0 52 2885 1 29 2683 2 50 1036 3 89 510 4 44 249 T772 26 3089	0 Abilene Christian University Y 1 Adelphi University Y 2 Adrian College Y 3 Agnes Scott College Y 4 Alaska Pacific University Y 772 Worcester State College 773 Xavier University Y 774 Xavier University of Louisiana Y 775 Yale University Y 776 York College of Pennsylvania Y Top25perc F.Undergrad P.Undergrad 0 52 2885 537 1 29 2683 1227 2 50 1036 99 3 89 510 63 4 44 249 869 772 26 3089 2029	1 Adelphi University Yes 2 Adrian College Yes 3 Agnes Scott College Yes 4 Alaska Pacific University Yes 772 Worcester State College No 773 Xavier University Yes 774 Xavier University of Louisiana Yes 775 Yale University Yes 776 York College of Pennsylvania Yes Top25perc F.Undergrad P.Undergrad Out 0 52 2885 537 1 29 2683 1227 2 50 1036 99 3 89 510 63 4 44 249 869 772 26 3089 2029	0 Abilene Christian University Yes 1660 1 Adelphi University Yes 2186 2 Adrian College Yes 1428 3 Agnes Scott College Yes 417 4 Alaska Pacific University Yes 193 772 Worcester State College No 2197 773 Xavier University Yes 1959 774 Xavier University of Louisiana Yes 2097 775 Yale University Yes 10705 776 York College of Pennsylvania Yes 2989 Top25perc F.Undergrad P.Undergrad Outstate 0 52 2885 537 7440 1 29 2683 1227 12280 2 50 1036 99 11250 3 89 510 63 12960 4 44 249 869 7560	0 Abilene Christian University Yes 1660 1232 1 Adelphi University Yes 2186 1924 2 Adrian College Yes 1428 1097 3 Agnes Scott College Yes 417 349 4 Alaska Pacific University Yes 193 146 772 Worcester State College No 2197 1515 773 Xavier University Yes 1959 1805 774 Xavier University of Louisiana Yes 2097 1915 775 Yale University Yes 10705 2453 776 York College of Pennsylvania Yes 2989 1855 Top25perc F.Undergrad P.Undergrad Outstate Room.Bo 0 52 2885 537 7440 3 1 29 2683 1227 12280 6 <t< td=""><td>0 Abilene Christian University Yes 1660 1232 72 1 Adelphi University Yes 2186 1924 51 2 Adrian College Yes 1428 1097 33 3 Agnes Scott College Yes 417 349 13 4 Alaska Pacific University Yes 193 146 5 </td><td>0 Abilene Christian University Yes 1660 1232 721 1 Adelphi University Yes 2186 1924 512 2 Adrian College Yes 1428 1097 336 3 Agnes Scott College Yes 417 349 137 4 Alaska Pacific University Yes 193 146 55 772 Worcester State College No 2197 1515 543 773 Xavier University Yes 1959 1805 695 774 Xavier University of Louisiana Yes 2097 1915 695 775 Yale University Yes 10705 2453 1317 776 York College of Pennsylvania Yes 2989 1855 691 Top25perc F.Undergrad P.Undergrad Outstate Room.Board Books</td><td>0 Abilene Christian University Yes 1660 1232 721 23 1 Adelphi University Yes 2186 1924 512 16 2 Adrian College Yes 1428 1097 336 22 3 Agnes Scott College Yes 417 349 137 60 4 Alaska Pacific University Yes 193 146 55 16 772 Worcester State College No 2197 1515 543 4 773 Xavier University Yes 1959 1805 695 24 774 Xavier University of Louisiana Yes 2097 1915 695 34 775 Yale University Yes 10705 2453 1317 95 776 York College of Pennsylvania Yes 2989 1855 691 28 0 52 2885 537 7440 3300 450 1</td></t<>	0 Abilene Christian University Yes 1660 1232 72 1 Adelphi University Yes 2186 1924 51 2 Adrian College Yes 1428 1097 33 3 Agnes Scott College Yes 417 349 13 4 Alaska Pacific University Yes 193 146 5	0 Abilene Christian University Yes 1660 1232 721 1 Adelphi University Yes 2186 1924 512 2 Adrian College Yes 1428 1097 336 3 Agnes Scott College Yes 417 349 137 4 Alaska Pacific University Yes 193 146 55 772 Worcester State College No 2197 1515 543 773 Xavier University Yes 1959 1805 695 774 Xavier University of Louisiana Yes 2097 1915 695 775 Yale University Yes 10705 2453 1317 776 York College of Pennsylvania Yes 2989 1855 691 Top25perc F.Undergrad P.Undergrad Outstate Room.Board Books	0 Abilene Christian University Yes 1660 1232 721 23 1 Adelphi University Yes 2186 1924 512 16 2 Adrian College Yes 1428 1097 336 22 3 Agnes Scott College Yes 417 349 137 60 4 Alaska Pacific University Yes 193 146 55 16 772 Worcester State College No 2197 1515 543 4 773 Xavier University Yes 1959 1805 695 24 774 Xavier University of Louisiana Yes 2097 1915 695 34 775 Yale University Yes 10705 2453 1317 95 776 York College of Pennsylvania Yes 2989 1855 691 28 0 52 2885 537 7440 3300 450 1

774	61		2793	166	6900	420	0 617
775	99		5217	83	19840	651	0 630
776	63		2988	1726	4990	356	0 500
	Personal	PhD	Terminal	S.F.Ratio	perc.alumni	Expend	Grad.Rate
0	2200	70	78	18.1	12	7041	60
1	1500	29	30	12.2	16	10527	56
2	1165	53	66	12.9	30	8735	54
3	875	92	97	7.7	37	19016	59
4	1500	76	72	11.9	2	10922	15
				•••		•••	
772	1200	60	60	21.0	14	4469	40
773	1250	73	75	13.3	31	9189	83
774	781	67	75	14.4	20	8323	49
775	2115	96	96	5.8	49	40386	99
776	1250	75	75	18.1	28	4509	99

[777 rows x 19 columns]

(b) We don't need the name of the college to be treated as data, but we want to have that for later, so we take it as the index.

```
[]: college2 = pd.read_csv('./data/College.csv', index_col=0)
college3 = college.rename(columns = {'Unnamed: 0': 'College'})
college3
```

[]:				College	Priva	te	Apps	Accept	Enr	oll	Top10	perc	\
	0	Abilene	Christian Uni	versity	Y	es	1660	1232		721	-	23	
	1		Adelphi Uni	versity	Y	es	2186	1924		512		16	
	2		Adrian	College	Y	es	1428	1097	;	336		22	
	3		Agnes Scott	College	Y	es	417	349		137		60	
	4	Alask	a Pacific Uni	versity	Y	es	193	146		55		16	
				•••	•••		•••	•••		•••			
	772	Wor	cester State	College		No	2197	1515		543		4	
	773		Xavier Uni	versity	Y	es	1959	1805		695		24	
	774	Xavier Uni	versity of Lo	uisiana	Y	es	2097	1915		695		34	
	775		Yale Uni	versity	Y	es	10705	2453	1	317		95	
	776	York Col	lege of Penns	ylvania	Y	es	2989	1855	(691		28	
		Top25perc	F.Undergrad	P.Under	rgrad	Out	tstate	Room.Bo	ard	Book	s \		
	0	52	2885		537		7440	3	300	45	0		
	1	29	2683		1227		12280	6	450	75	0		
	2	50	1036		99		11250	3	750	40	0		
	3	89	510		63		12960	5	450	45	0		
	4	44	249		869		7560	4	120	80	0		
						•••							
	772	26	3089		2029		6797	3	900	50	0		

773 774 775 776	47 61 99 63		2849 2793 5217 2988	1107 166 83 1726	11520 6900 19840 4990	496 420 651 356	0 617 0 630
	Personal	PhD	Terminal	S.F.Ratio	perc.alumni	Expend	Grad.Rate
0	2200	70	78	18.1	12	7041	60
1	1500	29	30	12.2	16	10527	56
2	1165	53	66	12.9	30	8735	54
3	875	92	97	7.7	37	19016	59
4	1500	76	72	11.9	2	10922	15
	•••		•••	•••		•••	
772	1200	60	60	21.0	14	4469	40
773	1250	73	75	13.3	31	9189	83
774	781	67	75	14.4	20	8323	49
775	2115	96	96	5.8	49	40386	99
776	1250	75	75	18.1	28	4509	99

[777 rows x 19 columns]

[]: # We keep the original data college = college3 college

[]:				College	Priva	te	Apps	Accept	Enro	11 '	Top10pe	rc	\
	0	Abilene	Christian Uni	versity	Y	es	1660	1232	7	21	2	23	
	1		Adelphi Uni	versity	Y	es	2186	1924	5	12	:	16	
	2		Adrian	College	Y	es	1428	1097	3	36	2	22	
	3		Agnes Scott	College	Y	es	417	349	1	37	(60	
	4	Alask	a Pacific Uni	versity	Y	es	193	146		55	:	16	
					•••	•••	•••	•••		•••			
	772	Wor	cester State	College		No	2197	1515	5	43		4	
	773		Xavier Uni	versity	Y	es	1959	1805	6	95	2	24	
	774	Xavier Uni	versity of Lo	uisiana	Y	es	2097	1915	6	95	3	34	
	775		Yale Uni	versity	Y	es	10705	2453	13	17	9	95	
	776	York Col	lege of Penns	ylvania	Y	es	2989	1855	6	91	4	28	
		Top25perc	${\tt F.Undergrad}$	P.Under	rgrad	Out	tstate	Room.Bo	ard :	Book	s \		
	0	52	2885		537		7440	3	300	45	0		
	1	29	2683		1227		12280	6	450	75	0		
	2	50	1036		99		11250	3	750	40	0		
	3	89	510		63		12960	5	450	45	0		
	4	44	249		869		7560	4	120	80	0		
		•••	•••										
	772	26	3089		2029		6797	3	900	50	0		
	773	47	2849		1107		11520	4	960	60	0		
	774	61	2793		166		6900	4	200	61	7		

775	99		5217	83	19840	651	0 630
776	63		2988	1726	4990	356	0 500
	Personal	PhD	Terminal	S.F.Ratio	perc.alumni	Expend	Grad.Rate
0	2200	70	78	18.1	12	7041	60
1	1500	29	30	12.2	16	10527	56
2	1165	53	66	12.9	30	8735	54
3	875	92	97	7.7	37	19016	59
4	1500	76	72	11.9	2	10922	15
			•••	•••	•••	•••	
772	1200	60	60	21.0	14	4469	40
773	1250	73	75	13.3	31	9189	83
774	781	67	75	14.4	20	8323	49
775	2115	96	96	5.8	49	40386	99
776	1250	75	75	18.1	28	4509	99

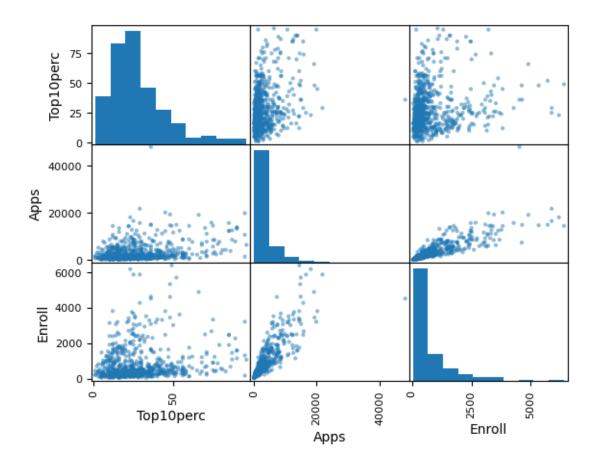
[777 rows x 19 columns]

(c) We can look at the data by using describe.

[]: college.describe()

[]:		Apps	Accept	Enroll	Top10perc	Top25perc \	
	count	777.000000	777.000000	777.00000	777.000000	777.000000	
	mean	3001.638353	2018.804376	779.972973	27.558559	55.796654	
	std	3870.201484	2451.113971	929.176190	17.640364	19.804778	
	min	81.000000	72.000000	35.000000	1.000000	9.000000	
	25%	776.000000	604.000000	242.000000	15.000000	41.000000	
	50%	1558.000000	1110.000000	434.000000	23.000000	54.000000	
	75%	3624.000000	2424.000000	902.000000	35.000000	69.000000	
	max	48094.000000	26330.000000	6392.000000	96.000000	100.000000	
		F.Undergrad	P.Undergrad	l Outstat	e Room.Boar	d Books	\
	count	777.000000	777.000000	777.00000	0 777.00000	777.000000	
	mean	3699.907336	855.298584	10440.66924	1 4357.52638	34 549.380952	
	std	4850.420531	1522.431887	4023.01648	4 1096.69641	165.105360	
	min	139.000000	1.000000	2340.00000	0 1780.00000	96.000000	
	25%	992.000000	95.000000	7320.00000	0 3597.00000	00 470.000000	
	50%	1707.000000	353.000000	9990.00000	0 4200.00000	500.000000	
	75%	4005.000000	967.000000	12925.00000	0 5050.00000	00 600.000000	
	max	31643.000000	21836.000000	21700.00000	0 8124.00000	00 2340.000000	
		Personal	PhD	Terminal S	.F.Ratio per	c.alumni \	
	count	777.000000	777.000000 7	77.000000 77	7.000000 77	7.000000	
	mean	1340.642214	72.660232	79.702703 1	4.089704 2	22.743887	
	std	677.071454	16.328155	14.722359	3.958349 1	2.391801	
	min	250.000000	8.000000	24.000000	2.500000	0.000000	

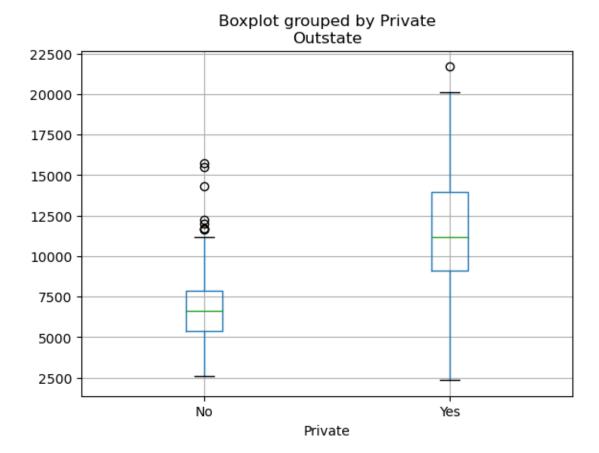
```
25%
             850.000000
                          62.000000
                                      71.000000
                                                  11.500000
                                                               13.000000
     50%
            1200.000000
                          75.000000
                                      82.000000
                                                  13.600000
                                                               21.000000
     75%
            1700.000000
                          85.000000
                                      92.000000
                                                  16.500000
                                                               31.000000
            6800.000000 103.000000 100.000000
                                                  39.800000
                                                               64.000000
    max
                  Expend Grad.Rate
              777.000000
                          777.00000
     count
    mean
             9660.171171
                           65.46332
             5221.768440
                           17.17771
     std
    min
             3186.000000
                           10.00000
    25%
             6751.000000
                           53.00000
     50%
             8377.000000
                           65.00000
     75%
            10830.000000
                           78.00000
    max
            56233.000000 118.00000
[]: #Compare the data to each other using scatter matrix
     pd.plotting.scatter_matrix(college[['Top10perc', 'Apps', 'Enroll']])
[]: array([[<Axes: xlabel='Top10perc', ylabel='Top10perc'>,
             <Axes: xlabel='Apps', ylabel='Top10perc'>,
             <Axes: xlabel='Enroll', ylabel='Top10perc'>],
            [<Axes: xlabel='Top10perc', ylabel='Apps'>,
             <Axes: xlabel='Apps', ylabel='Apps'>,
             <Axes: xlabel='Enroll', ylabel='Apps'>],
            [<Axes: xlabel='Top10perc', ylabel='Enroll'>,
             <Axes: xlabel='Apps', ylabel='Enroll'>,
             <Axes: xlabel='Enroll', ylabel='Enroll'>]], dtype=object)
```



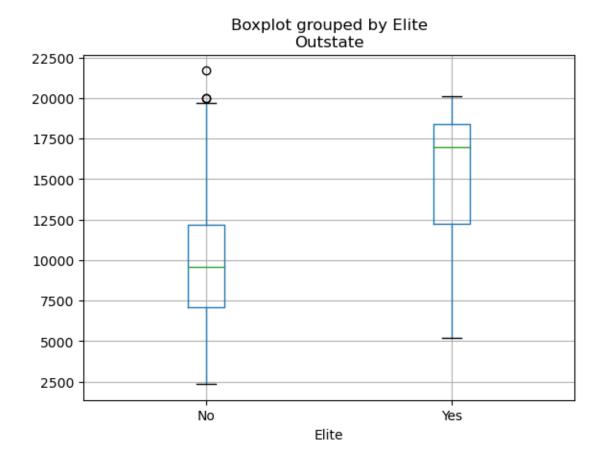
1.0.2 (e)

Private colleges appear to have a higher median number of out-of-state students. They also have a higher spread of number of students out of state compared to non-private schools

```
[]: # Create a boxplot of Outstate vs Private.
college.boxplot('Outstate', by='Private');
```



(f) There are 78 elite universities



1.0.3 (g)

Exploring the histograms of different features of the data. If we are plotting histograms we want numerical data so we can bin each feature and look at the frequency counts.

```
[]: from matplotlib.pyplot import subplots

# Let's make histograms of all the numerical columns
column_names = college.select_dtypes(include='number').columns

# Number of histograms we want
number_of_histograms = column_names.size

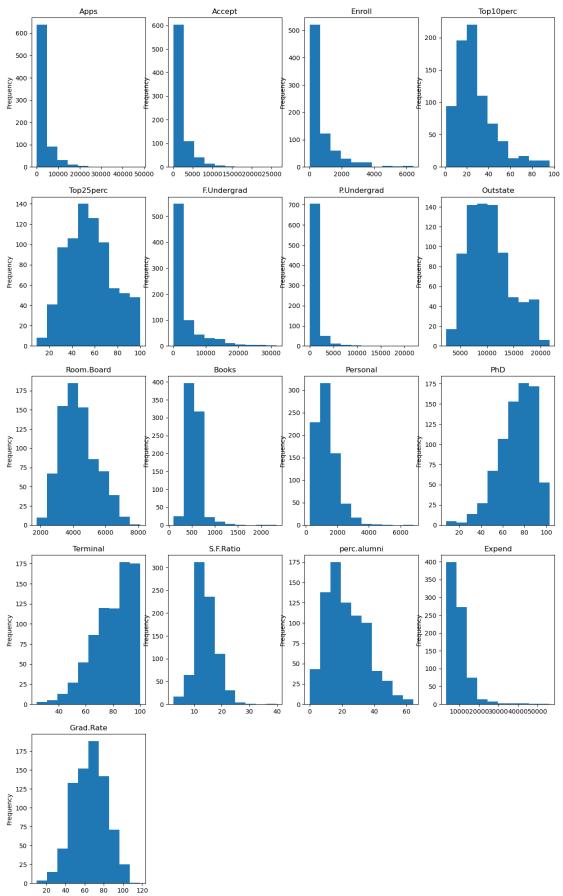
# Number of rows
num_rows = number_of_histograms // 4 + (number_of_histograms % 4 > 0) # Roundu
aup to the nearest integer

# Make the subplots
fig, axes = subplots(nrows=num_rows, ncols=4, figsize=(15, 5 * num_rows))

# Append the histograms to subplots
for i, column_name in enumerate(column_names):
ax = axes[i // 4, i % 4] # Select the subplot
```

```
college[column_name].plot(kind='hist', ax=ax)
   ax.set_title(column_name)

# Remove any unused subplots
for i in range(number_of_histograms, num_rows * 4):
   fig.delaxes(axes[i // 4, i % 4])
```



1.0.4 (h)

Continue to explore the data. We see that the graduation rate is normally distributed across colleges. Peculiarly it seems that some colleges have above 100% graduation rate which does not make sense.

Most faculty members at these colleges have a Phd, we see the Phd histogram is skewed to the left. The percentage of students who graduated in the top 25% percent of their class also normally distributed. The histograms for the number of applicants received, rejected, and enrolled are consistent and skewed to the right.

1.0.5 #10

```
[]: from ISLP import load_data

Boston = load_data('Boston')

Boston
```

	Bost	on										
]:		crim	zn	indus	chas	nox	rm	age	dis	rad	tax	\
	0	0.00632	18.0	2.31	0	0.538	6.575	65.2	4.0900	1	296	
	1	0.02731	0.0	7.07	0	0.469	6.421	78.9	4.9671	2	242	
	2	0.02729	0.0	7.07	0	0.469	7.185	61.1	4.9671	2	242	
	3	0.03237	0.0	2.18	0	0.458	6.998	45.8	6.0622	3	222	
	4	0.06905	0.0	2.18	0	0.458	7.147	54.2	6.0622	3	222	
		•••		•••	•••			•••				
	501	0.06263	0.0	11.93	0	0.573	6.593	69.1	2.4786	1	273	
	502	0.04527	0.0	11.93	0	0.573	6.120	76.7	2.2875	1	273	
	503	0.06076	0.0	11.93	0	0.573	6.976	91.0	2.1675	1	273	
	504	0.10959	0.0	11.93	0	0.573	6.794	89.3	2.3889	1	273	
	505	0.04741	0.0	11.93	0	0.573	6.030	80.8	2.5050	1	273	
		ptratio	lstat	\mathtt{medv}								
	0	15.3	4.98	24.0								
	1	17.8	9.14	21.6								
	2	17.8	4.03	34.7								
	3	18.7	2.94	33.4								
	4	18.7	5.33	36.2								
		•••										
	501	21.0	9.67	22.4								
	502	21.0	9.08	20.6								
	503	21.0	5.64	23.9								
	504	21.0	6.48	22.0								
	505	21.0	7.88	11.9								

[506 rows x 13 columns]

1.0.6 (b)

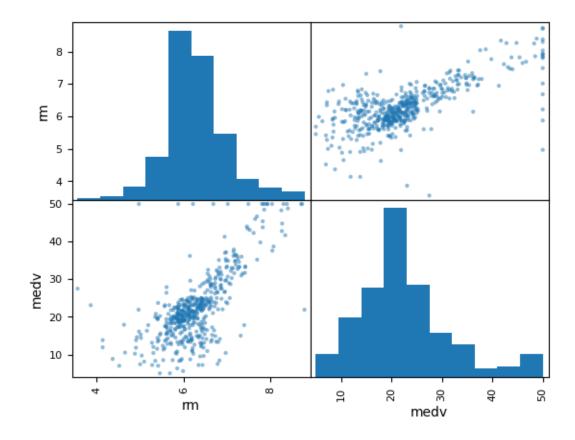
There are 506 rows and 13 columns. The rows represent housing values of suburbs in boston, and the columns represent various characteristics about the suburb. For example, we have the average number of rooms per dwelling, the zone within the city, and crime rate per capita.

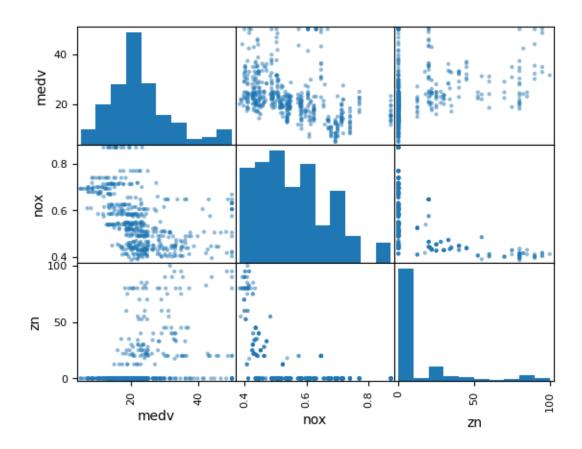
1.0.7 (c)

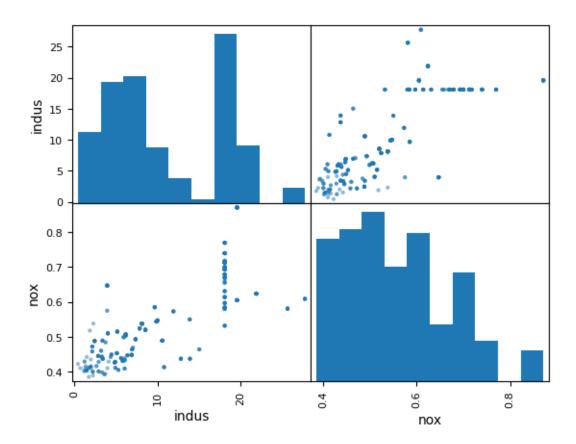
We see that there is a strong correlation between Zone and median value of home in \$1000s. This makes sense as the more rooms you have the higher the home is likely to be in value. However, it is peculiar that the nitrgoen oxygen concentrate is corellated with median value of home.

We can explain this by the indus variable. Suburbs that have a high proportion of non-retail business acres have a high conventration of nitrogen dioxide.

```
[]: names = Boston.columns
  pd.plotting.scatter_matrix(Boston[['rm', 'medv']])
  pd.plotting.scatter_matrix(Boston[['medv', 'nox', 'zn']])
  pd.plotting.scatter_matrix(Boston[['indus', 'nox']])
```





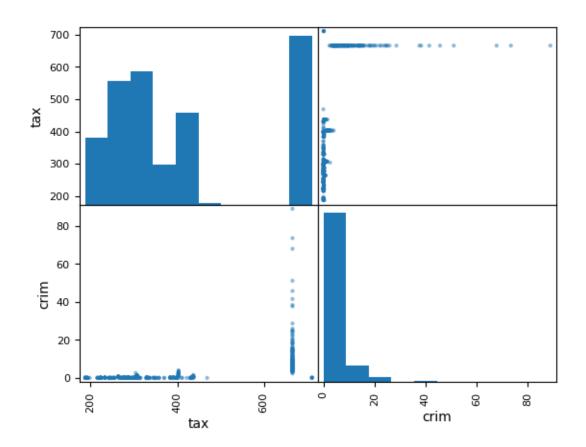


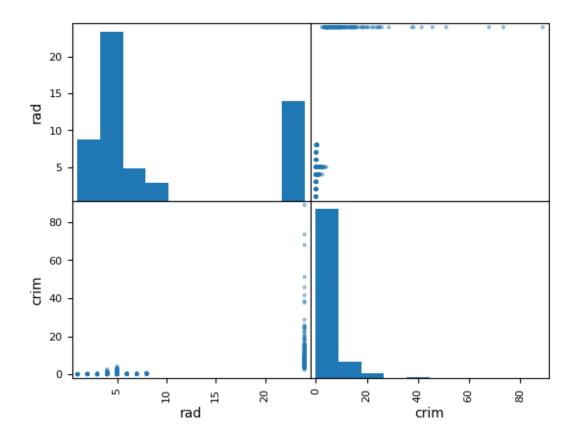
```
[]:
             crim
                     zn
                         indus
                               chas
                                       nox
                                              rm
                                                   age
                                                         dis
                                                               rad
                                                                     tax
                                                                         ptratio \
    crim
             1.00 -0.20
                          0.41 -0.06 0.42 -0.22
                                                  0.35 - 0.38
                                                              0.63
                                                                             0.29
                                                                    0.58
    zn
            -0.20 1.00
                         -0.53 -0.04 -0.52 0.31 -0.57 0.66 -0.31 -0.31
                                                                            -0.39
    indus
             0.41 - 0.53
                          1.00 0.06 0.76 -0.39 0.64 -0.71
                                                             0.60 0.72
                                                                             0.38
            -0.06 -0.04
                          0.06 1.00 0.09 0.09 0.09 -0.10 -0.01 -0.04
                                                                            -0.12
    chas
             0.42 - 0.52
                          0.76 0.09 1.00 -0.30
                                                  0.73 - 0.77
                                                             0.61
                                                                             0.19
    nox
            -0.22 0.31
                         -0.39 0.09 -0.30 1.00 -0.24
                                                       0.21 -0.21 -0.29
                                                                            -0.36
    rm
                          0.64 0.09 0.73 -0.24 1.00 -0.75
    age
             0.35 - 0.57
                                                             0.46
                                                                             0.26
    dis
            -0.38 0.66
                         -0.71 -0.10 -0.77 0.21 -0.75
                                                       1.00 -0.49 -0.53
                                                                            -0.23
             0.63 - 0.31
                          0.60 -0.01 0.61 -0.21 0.46 -0.49
                                                              1.00
                                                                             0.46
    rad
                                                                   0.91
    tax
             0.58 - 0.31
                          0.72 -0.04 0.67 -0.29 0.51 -0.53 0.91
                                                                    1.00
                                                                             0.46
```

```
0.29 - 0.39
                       0.38 -0.12  0.19 -0.36  0.26 -0.23
                                                            0.46
                                                                   0.46
                                                                            1.00
ptratio
                                                                            0.37
lstat
         0.46 - 0.41
                       0.60 -0.05 0.59 -0.61
                                               0.60 - 0.50
                                                            0.49
                                                                   0.54
medv
        -0.39 0.36
                      -0.48 0.18 -0.43 0.70 -0.38 0.25 -0.38 -0.47
                                                                           -0.51
         1stat medv
          0.46 - 0.39
crim
         -0.41 0.36
zn
indus
          0.60 - 0.48
         -0.05 0.18
chas
          0.59 - 0.43
nox
         -0.61 0.70
rm
          0.60 -0.38
age
dis
         -0.50 0.25
rad
          0.49 - 0.38
          0.54 - 0.47
tax
ptratio
          0.37 - 0.51
lstat
          1.00 - 0.74
medv
         -0.74 1.00
```

1.0.8 (d)

Factors per capita crime rate are the index of accessibility to radial highways and property tax rate per \$10,0000. However, these are not very strong relationships, the correlation coefficient between tax and crime is 0.58 and the correlation coefficient betwee rad and crime is 0.63. They both have a positive relationship, but neither are very strong.





(e) Do any of the suburbs of Boston appear to have particularly high crime rates? Tax rates? Pupil-teacher ratios? Comment on the range of each predictor.

Crime: There are 14 suburbs with a crime rate per capita between 80 and 89. Overall suburbs had a minimum of 0.006 crime rate and a maximum of 88.97.

Tax Rates: There are 85 suburbs in the top percentile with a tax property rate between 705.76 and 711.0 per \$10,000 dollars. The full range of tax rates of the suburbs are 187 and 711.

Pupil-teacher ratio: There are 34 suburbs with in the lowest 1 percent of pupil teach ratio ranging from 21.9 to 22. The full range of pupil teacher ratio across suburbs is 12 to 22.

```
[]: cut = pd.cut(Boston.crim, bins = 10)
Boston['crime_bins'] = cut

print('Min:', np.min(Boston.crim))
print('Max:', np.max(Boston.crim))

top_10th_percentile_interval = cut.cat.categories[-1]
print("Top 10 percent of crime:", top_10th_percentile_interval)
Boston['crime_bins'] = cut
high_crime = Boston[Boston.crime_bins == top_10th_percentile_interval]
```

```
print('Number in top 10 percentile:', high_crime.size)
     Boston.crim.describe()
    Min: 0.00632
    Max: 88.9762
    Top 10 percent of crime: (80.079, 88.976]
    Number in top 10 percentile: 14
[]: count
              506.000000
    mean
                3.613524
    std
                8.601545
    min
                0.006320
    25%
                0.082045
    50%
                0.256510
    75%
                3.677083
               88.976200
    max
    Name: crim, dtype: float64
[]: cut = pd.cut(Boston.tax, bins = 100)
     Boston['tax_bins'] = cut
     print('Min:', np.min(Boston.tax))
     print('Max:', np.max(Boston.tax)
                                         )
     top 1 percentile interval = cut.cat.categories[-1]
     print("Top 1 percent of tax:", top_1_percentile_interval)
     Boston['tax bins'] = cut
     high_tax = Boston[Boston.tax_bins == top_1_percentile_interval]
     print('Number in top percentile:', high_tax.size)
     Boston.tax.describe()
    Min: 187
    Max: 711
    Top 1 percent of tax: (705.76, 711.0]
    Number in top percentile: 75
[]: count
              506.000000
    mean
              408.237154
    std
              168.537116
    min
              187.000000
    25%
              279.000000
    50%
              330.000000
    75%
              666.000000
              711.000000
    max
    Name: tax, dtype: float64
```

```
[]: cut = pd.cut(Boston.ptratio, bins=100)
     Boston['ptratio_bins'] = cut
     print('Min:', np.min(Boston.ptratio))
     print('Max:', np.max(Boston.ptratio))
     top_1_percentile_interval = cut.cat.categories[-1]
     print("Top 1 percent of parent teach ratio:", top_1_percentile_interval)
     Boston['ptratio cut'] = cut
     high_ptratio = Boston[Boston.ptratio_bins == top_1_percentile_interval]
     print('Number in top percentile:', high ptratio.size)
     Boston.ptratio.describe()
    Min: 12.6
    Max: 22.0
    Top 1 percent of parent teach ratio: (21.906, 22.0]
    Number in top percentile: 34
[]: count
              506.000000
    mean
               18.455534
     std
                2.164946
    min
               12.600000
     25%
               17.400000
    50%
               19.050000
     75%
               20.200000
    max
               22.000000
    Name: ptratio, dtype: float64
    (f) How many of the suburbs in this data set bound the Charles river?
    35 suburbs
[]: bound_charles_river = Boston[Boston.chas == 1]
     bound charles river.shape[0]
[]: 35
    (g) What is the median pupil-teacher ratio among the towns in this data set?
[]: ptratio = Boston['ptratio']
     medium_ptratio = np.median(ptratio)
     medium_ptratio
```

[]: 19.05

The median pupil-teacher ratio is: 19.05

(h) Which suburb of Boston has lowest median value of owner- occupied homes? What are the values of the other predictors for that suburb, and how do those values compare to the overall ranges for those predictors? Comment on your findings.

Suburbs 398 and 405 have the lowest median value of owner occupied homes. They have a much greater incident of crime with crime indices in the greater 75th percentile with indexes if 38.3 and 67.92 respectively.

```
[]: min_value_home = min(Boston.medv)
suburbs = Boston[Boston.medv == min_value_home]

print(Boston.crim.describe())
print(suburbs)
```

```
count
         506.000000
            3.613524
mean
            8.601545
std
min
            0.006320
25%
            0.082045
50%
            0.256510
75%
            3.677083
          88.976200
Name: crim, dtype: float64
        crim
                zn
                     indus
                            chas
                                                             dis
                                                                   rad
                                                                        tax
                                     nox
                                              rm
                                                    age
                                                                    24
398
     38.3518
               0.0
                      18.1
                                   0.693
                                          5.453
                                                  100.0
                                                          1.4896
                                                                        666
405
     67.9208
               0.0
                      18.1
                                   0.693
                                          5.683
                                                  100.0
                                                          1.4254
                                                                    24
                                                                        666
     ptratio
               lstat
                       medv
                                    crime_bins
                                                          tax_bins
                              (35.594, 44.491]
398
        20.2
               30.59
                        5.0
                                                 (663.84, 669.08]
405
        20.2
               22.98
                        5.0
                              (62.285, 71.182]
                                                 (663.84, 669.08]
        ptratio_bins
                            ptratio_cut
398
     (20.12, 20.214]
                        (20.12, 20.214]
405
     (20.12, 20.214]
                        (20.12, 20.214]
```

(i) In this data set, how many of the suburbs average more than seven rooms per dwelling? More than eight rooms per dwelling? Comment on the suburbs that average more than eight rooms per dwelling.

More than seven rooms per dwelling: 64 More than eight rooms per dwelling: 13

The suburbs with that average 8 rooms per dwelling have a low mean crime index. The 75th percentile of Boston overall has an average index of 3.67 while the suburbs averaging 8 rooms or more has an index of 0.71. Some other extreme values (>75% or <25% percentiles) are accessibility to radial highways and lower status of the population. The targeted suburbs have a mean of 4.31% of the population having lower status.

```
[ ]: stats = Boston.describe()
eight = Boston[Boston.rm > 8].describe()
```

```
seventy_fifth = stats.loc['75%']
     twenty_fifth = stats.loc['25%']
     extreme_columns = eight.columns[(eight.iloc[1] > seventy_fifth) | (eight.
      →iloc[0] < twenty_fifth)].tolist()</pre>
     filtered eight = eight[extreme columns]
     filtered_eight.iloc[1]
[]: zn
                 13.615385
    chas
                  0.153846
     rm
                  8.348538
                 71.538462
     age
     tax
                325.076923
                 16.361538
    ptratio
     medv
                 44.200000
     Name: mean, dtype: float64
[]: # For reference
     Boston.describe()[extreme_columns].iloc[1:]
[]:
                   zn
                           chas
                                                               tax
                                                                      ptratio \
                                       rm
                                                   age
            11.363636
                       0.069170
                                 6.284634
                                                        408.237154
                                                                   18.455534
    mean
                                             68.574901
                       0.253994
     std
            23.322453
                                 0.702617
                                            28.148861
                                                        168.537116
                                                                     2.164946
    min
             0.000000
                       0.000000
                                 3.561000
                                             2.900000
                                                        187.000000
                                                                   12.600000
     25%
             0.000000
                       0.000000
                                 5.885500
                                            45.025000
                                                        279.000000
                                                                    17.400000
     50%
             0.000000
                       0.000000
                                 6.208500
                                            77.500000
                                                        330.000000 19.050000
     75%
            12.500000
                       0.000000
                                 6.623500
                                            94.075000
                                                        666.000000
                                                                    20.200000
    max
           100.000000
                       1.000000 8.780000
                                           100.000000
                                                        711.000000 22.000000
                medv
    mean
          22.532806
     std
            9.197104
    min
            5.000000
     25%
           17.025000
     50%
           21.200000
     75%
           25.000000
           50.000000
    max
[]: eight = Boston[Boston.rm > 8]
     print('Number of suburbs with greater than eight:', eight.shape[0])
     eight.describe()
    Number of suburbs with greater than eight: 13
[]:
                 crim
                              zn
                                      indus
                                                   chas
                                                               nox
                                                                           rm
           13.000000
                       13.000000
                                 13.000000
                                             13.000000
                                                         13.000000
                                                                   13.000000
     count
                                   7.078462
                                               0.153846
             0.718795
                       13.615385
                                                          0.539238
                                                                     8.348538
     mean
```

```
std
        0.901640
                   26.298094
                                5.392767
                                           0.375534
                                                       0.092352
                                                                   0.251261
min
        0.020090
                    0.000000
                                2.680000
                                           0.000000
                                                                   8.034000
                                                       0.416100
25%
        0.331470
                    0.000000
                                3.970000
                                           0.000000
                                                       0.504000
                                                                   8.247000
50%
        0.520140
                    0.000000
                                6.200000
                                           0.000000
                                                       0.507000
                                                                   8.297000
75%
        0.578340
                   20.000000
                                6.200000
                                           0.000000
                                                       0.605000
                                                                   8.398000
        3.474280
                   95.000000
                               19.580000
                                           1.000000
                                                       0.718000
                                                                   8.780000
max
                                                         ptratio
                                                                              /
             age
                         dis
                                     rad
                                                  tax
                                                                       lstat
                                                       13.000000
       13.000000
                   13.000000
                               13.000000
                                           13.000000
                                                                   13.000000
count
                                          325.076923
                                                       16.361538
mean
       71.538462
                    3.430192
                                7.461538
                                                                    4.310000
std
       24.608723
                    1.883955
                                5.332532
                                          110.971063
                                                        2.410580
                                                                    1.373566
        8.400000
                    1.801000
                                2.000000
                                          224.000000
                                                       13.000000
                                                                    2.470000
min
25%
       70.400000
                    2.288500
                                5.000000
                                          264.000000
                                                       14.700000
                                                                    3.320000
50%
       78.300000
                    2.894400
                                7.000000
                                          307.000000
                                                       17.400000
                                                                    4.140000
75%
                                8.000000
                                          307.000000
       86.500000
                    3.651900
                                                       17.400000
                                                                    5.120000
max
       93.900000
                    8.906700
                               24.000000
                                          666.000000
                                                       20.200000
                                                                    7.440000
            medv
       13.000000
count
       44.200000
mean
std
        8.092383
       21.900000
min
25%
       41.700000
50%
       48.300000
75%
       50.000000
max
       50.000000
```