

Evaluate Logarithms and Graph Logarithmic Functions

KEY CONCEPT

For Your Notebook

Definition of Logarithm with Base b

Let b and y be positive numbers with $b \neq 1$. The logarithm of y with base b is denoted by $\log_b y$ and is defined as follows:

$$\log_b y = x \quad \text{if and only if} \quad b^x = y$$

The expression $\log_b y$ is read as "log base b of y ."

Ex 1: Rewrite each logarithm in exponential form.

Logarithmic Form	Exponential Form
A. $\log_5 625 = 4$	
B. $\log_2 \frac{1}{16} = -4$	
C. $\log_{64} 4 = \frac{1}{3}$	

Ex 2: Solve for the unknown in the logarithmic equation.

A. $\log_9 x = 2$

B. $\log_5 125 = y$

Ex 3: Use a calculator to evaluate each logarithm. Round to the nearest thousandth.

A. $\log 15.125$

B. $\ln 2.371$

C. $\ln e^2$

Ex 4: Evaluate each logarithmic expression without a calculator.

A. $\log_7 49$

B. $\log_3 27$

C. $\log_6 \sqrt{6}$

D. $\log_3 \frac{1}{9}$

E. $\log_{81} 9$

F. $\log_{11} 11$

G. $\log_6 1$

H. $\log_4 4^6$

I. $\log_8 32$

Properties of Logarithms

★ $\log_b 1 =$

★ $\log_b b =$

★ $\log_b b^x =$

★ $b^{\log_b x} =$

Ex 5: Simplify the expression.

A. $\log_6 36^x$

B. $7^{\log_7 x}$

C. $10^{\log 4}$