

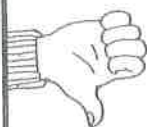
Name _____

Multiplying & Dividing Rational Expressions

$$\frac{x^2 - 7x + 12}{x^2 - 3x} \div 3x - 12 =$$

~~-7x~~

Wrong!



Right!

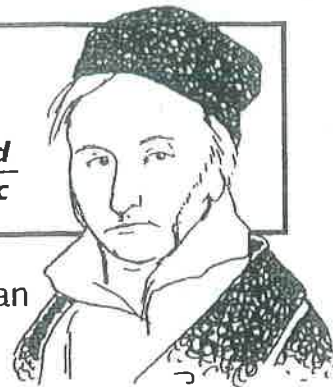
$$\begin{aligned} \frac{x^2 - 7x + 12}{x^2 - 3x} \div 3x - 12 &= \\ \frac{x^2 - 7x + 12}{x^2 - 3x} \cdot \frac{1}{3x - 12} &= \\ \frac{(x-3)(x-4)}{x(x-3)} \cdot \frac{1}{3(x-4)} &= \\ \frac{\cancel{(x-3)}\cancel{(x-4)}}{x\cancel{(x-3)}3\cancel{(x-4)}} = \frac{1}{3x} \end{aligned}$$

Quick Review

- To multiply, factor all polynomials. Then cancel out factors that are alike.
- To divide, invert the divisor and multiply.

$$\frac{a}{b} \cdot \frac{c}{d} = \frac{ac}{bd}$$

$$\frac{a}{b} \div \frac{c}{d} = \frac{a}{b} \cdot \frac{d}{c} = \frac{ad}{bc}$$



Simplify each expression. Use the code to learn the name of the German mathematician who developed the fundamental theorem of algebra.

L 1. $\frac{x}{x-4} \div \frac{x+6}{x-4} =$

$$\frac{x}{\cancel{x-4}} \cdot \frac{\cancel{x-4}}{x+6} =$$

$$\frac{x}{x+6}$$

H 7. $\frac{x^2 - 3x}{x^2 - 8x + 15} \cdot \frac{(x-5)^2}{2x} =$

$$\frac{\cancel{x(x-3)}}{(\cancel{x-5})(x-3)} \cdot \frac{(x-5)^2}{2\cancel{x}} =$$

$$\frac{x-5}{2}$$

I 2. $\frac{2x-2}{x^2-1} \cdot x+1 =$

$$\frac{2\cancel{(x-1)}}{(\cancel{x+1})(x-1)} \cdot \cancel{x+1} =$$

$$2$$

G 8. $\frac{9x^2}{4} \cdot \frac{8x+8}{18x} =$

$$\frac{9\cancel{x^2}}{\cancel{4}} \cdot \frac{8\cancel{(x+1)}}{18\cancel{x}} =$$

$$x(x+1)$$

D 3. $\frac{2x}{x+5} \div \frac{x-9}{x+5} =$

$\frac{2x}{\cancel{x+5}} \cdot \frac{\cancel{x+5}}{x-9} = \frac{2x}{x-9}$

R 9. $\frac{x^2-5x+6}{x+2} \div \frac{x-3}{x^2-4} =$

$\frac{(x-2)(x-3)}{(x+2)} \cdot \frac{(x+2)(x-2)}{(x-3)} = \frac{(x-2)^2}{1}$

4. $\frac{2x-5}{-3} \cdot \frac{24}{4x-10} =$

S $\frac{2x-5}{-3} \cdot \frac{24}{2(2x-5)} = \frac{24}{-6} = -4$

10. $\frac{4x}{x^2-25} \cdot \frac{x-5}{8x^2+20x} =$

U $\frac{4x}{(x+5)(x-5)} \cdot \frac{\cancel{x-5}}{4x(2x+5)} = \frac{1}{(x+5)(2x+5)}$

5. $\frac{x^2-16}{3x^2} \div x-4 =$

F $\frac{(x+4)(x-4)}{3x^2} \cdot \frac{1}{\cancel{x-4}} = \frac{x+4}{3x^2}$

11. $\frac{x^2-9}{5} \div \frac{x+3}{10} =$

C $\frac{(x+3)(x-3)}{5} \cdot \frac{10}{x+3} = 2(x-3)$

6. $\frac{x+2}{x} \cdot \frac{x^2}{x^2-4} =$

A $\frac{\cancel{x+2}}{x} \cdot \frac{x^2}{(\cancel{x+2})(x-2)} = \frac{x}{x-2}$

12. $\frac{-6x+12}{5x} \div \frac{x+2}{10x} =$

E $\frac{6(\cancel{x+2})}{5x} \cdot \frac{10x}{x+2} = 12$

A	C	D	E	F	G	H	I	L	R	S	U
$\frac{x}{x-2}$	$2x-6$	$\frac{2x}{x-9}$	12	$\frac{x+4}{3x^2}$	x^2+x	$\frac{x-5}{2}$	2	$\frac{x}{x+6}$	x^2-4x+4	-4	$\frac{1}{2x^2+15x+25}$

C A R L F R I E D R I C H G A U S S

11 6 9 1 5 9 2 12 3 9 2 11 7 8 6 10 4 4