**Neural Networks and Learning Systems** TBMI 26, 2017

# Lecture 4 **Ensemble learning & Boosting**

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### History

(roughly)

- 1960's (and before): Linear methods, perceptron, LDA
- 1980's: Nonlinear breakthroughs, neural networks
- 1990's-now:
  - Kernel methods, SVM
  - Ensemble learning, boosting, bagging
- · Recent years
  - Deep neural networks

**Applications** Face detection Pedestrian detection Organ detection Pose estimation

## Combining simple rules

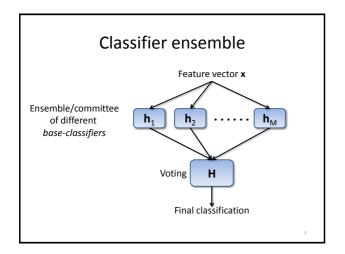
Example taken from "A Short Introduction to Boosting" by Y. Freund and R. Schapire

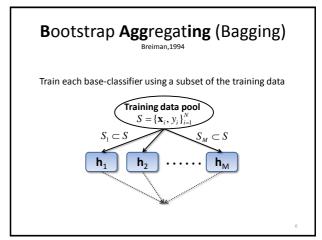
- "A horse-racing gambler, hoping to maximize his winnings, decides to create a computer program that will accurately predict the winner of a horse race based on the usual information (number of races recently won by each horse, betting odds for each horse, etc.)."

  "To create such a program, he asks a highly successful expert gambler to explain his betting strategy. Not surprisingly, the expert is <u>unable</u> to <u>articulate a grand set of rules</u> for selecting a horse. On the other hand, when presented with the data for a specific set of races, the expert has no trouble coming up with a "<u>rule of thumb"</u> for that set of races (such as, "Bet on the horse that has recently won the most races" or "Bet on the horse with the most favored odds"). Although such a rule of thumb, by itself, is obviously very rough and inaccurate, it is not unreasonable to expect it to provide predictions that are at least <u>a little bit better than random guessing."</u>

  "Furthermore, by repeatedly asking the expert's opinion on different collections of races, the gambler is able to extract many rules of thumb."

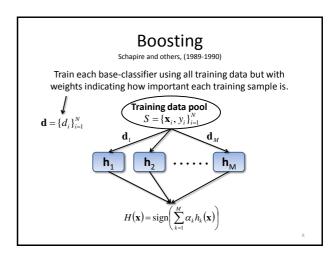
"Boosting refers to a general and provably effective method of <u>producing a very accurate prediction</u> <u>rule by combining rough and moderately inaccurate rules of thumb in a manner similar to that suggested above."</u>





# Bagging

- · Reduces overfitting
- Is best used with base-classifiers that can be become very different after training
  - Neural networks different initializations lead to different local minima
  - Decision trees small input difference can generate a very different classifier



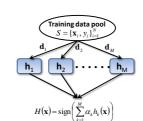
## **Boosting**

- We have seen before that all training samples are not equally important, e.g., SVM.
- Both SVM and Bagging can also be considered to use weights for each sample d<sub>i</sub> ={0,1}.
- While the base-classifiers in principle can be any classifier (SVM, neural network, etc.), the driving question has been:

Can we combine a number of <u>simple classifiers</u> to create a single strong classifier?

General boosting algorithm

Train weak classifiers sequentially!



- Set weights d<sub>1</sub>=1/N
   Train weak classifier h<sub>1</sub>(x) using weights d<sub>1</sub>
- Increase and decrease weight for wrongly and correctly classified training examples respectively -> d<sub>2</sub>
- Train weak classifier h<sub>2</sub>(x) using weights d<sub>2</sub>
- Repeat until h<sub>M</sub>(x)

10

# Simple/Weak classifiers

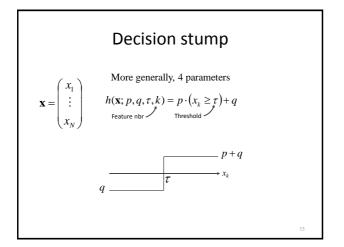
cf. "a rule of thumb"

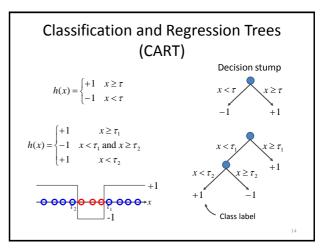
Example: Threshold one feature

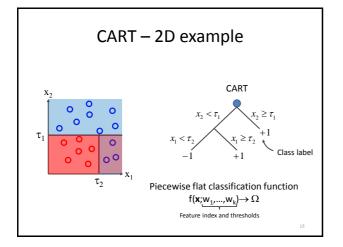
$$\mathbf{x} = \begin{bmatrix} \vdots \\ x_N \end{bmatrix} \qquad h(x_2) = \begin{cases} +1 & x_2 \ge \\ -1 & x_2 < \end{cases}$$

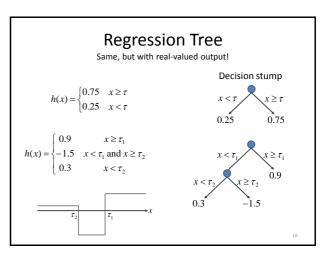
Weak classifiers – Threshold polarity  $h(x) = \begin{cases} +1 & p \ge p\tau \\ -1 & p \le p\tau \end{cases} \quad \text{Polarity } p = \{-1,1\}$   $p = 1 \qquad p = -1$   $h(x) = \begin{cases} +1 & x \le \tau \\ -1 & x < \tau \end{cases} \quad h(x) = \begin{cases} +1 & x \le \tau \\ -1 & x > \tau \end{cases}$ 

3









## Training a decision stump

Find best split threshold  $\tau!$ 

Class label 
$$\{\cdot 1, +1\}$$
 Training input:  $\{x_i, y_i, d_i\}_{i=1}^M$  Normalized weights:  $\sum_{i=1}^M d_i = 1$  Consider only one feature

Threshold function: 
$$h(x; \tau, p) = \begin{cases} +1 & p \ x \ge p \ \tau \\ -1 & p \ x$$

0-1 cost function: 
$$\min_{\tau,p} \varepsilon(\tau,p) = \sum_{i=1}^{M} d_i I(y_i \neq h(x_i;\tau,p))$$
1 for false classifications

## Training a decision stump, cont.

$$\min_{\tau,p} \varepsilon(\tau,p) = \sum_{i=1}^{M} d_i I(y_i \neq h(x_i;\tau,p)) \text{ is always } \le 0.5!$$

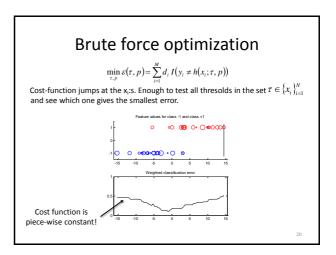
Why? If we classify all training samples wrong we get:

$$\varepsilon(\tau, p) = \sum_{i=1}^{M} d_{i} = 1$$

But we can then just change polarity/sign and get all samples correct, i.e.,  $\varepsilon$  = 0!

In general, if we obtain an error  $\epsilon$  between 0.5 and 1.0, we can switch polarity and get the error  $1.0-\epsilon$ , which is smaller than 0.5.

# 



## Brute force optimization

Training samples 
$$\mathbf{x}_i = \begin{pmatrix} x_{1,i} \\ x_{N,j} \end{pmatrix}$$
,  $i=1\dots M$  # training samples

Pseudo code:

$$\begin{array}{l} \varepsilon_{\min} = \inf; \\ \text{for all feature components } \mathbf{k} = 1:\mathbf{N} \\ \text{for all thresholds } \tau \in \{x_{1,i}\}_{i=1}^{M} \\ \varepsilon(\tau,p=1) = \sum_{i=1}^{M} d_i \ I(y_i \neq h(x_i;\tau,p=1)) \\ \text{if } \varepsilon > 0.5 \\ p = -1; \\ \varepsilon = 1 - \varepsilon; \\ \text{end} \\ \text{if } \varepsilon < \varepsilon_{\min} = \text{nd} \\ \text{end} \\ \text{end} \\ \text{end} \end{array}$$

## Discrete AdaBoost

Freund & Schapire, 1995

Training data 
$$\{\mathbf{x}_i, y_i\}_{i=1}^M$$
,  $y_i \in \{-1,+1\}$ 
Initialization:  $d_1(i) = \frac{1}{M}$ ,  $T = \#$  base classifiers for  $t = 1$  to  $T$ 
Find weak classifier  $h_t(\mathbf{x}) = \{-1,+1\}$  that minimizes the weighted classification error: 
$$\varepsilon_i = \sum_{i=1}^M d_i(i)I(y_i \neq h_i(\mathbf{x}_i))$$
 Update weights: 
$$d_{t+1}(i) = d_t(i)e^{-a_iy_ih_i(\mathbf{x}_i)}, \text{ where } \alpha_i = \frac{1}{2}\ln\frac{1-\varepsilon_i}{\varepsilon_i}$$
 and renormalize so that  $\sum_{i=1}^M d_{t+1}(i) = 1$ 

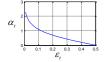
Final strong classifier:  $H(\mathbf{x}) = \text{sign}\left(\sum_{t=1}^{T} \alpha_t \mathbf{h}_t(\mathbf{x})\right)$ 

## Discrete AdaBoost

- <u>Discrete</u> output from the weak classifier h<sub>t</sub>(x) = {-1,+1}
- Weight update

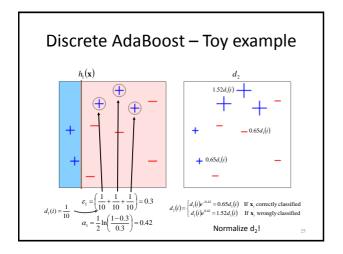
$$d_{\iota+1}(i) = d_{\iota}(i)e^{-a_{\iota}y_{\iota}b_{\iota}(\mathbf{x}_{\iota})} = \begin{cases} d_{\iota}(i)e^{-a_{\iota}} & \text{if } \mathbf{x}_{\iota} \text{ correctly classified} \\ d_{\iota}(i)e^{a_{\iota}} & \text{if } \mathbf{x}_{\iota} \text{ wrongly classified} \end{cases}$$

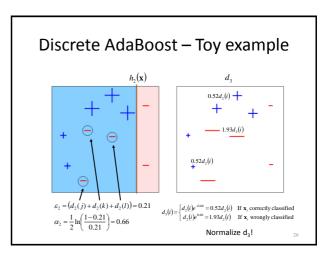
• Performance of weak classifier:  $\alpha_t = \frac{1}{2} \ln \frac{1 - \varepsilon_t}{\varepsilon_t}$ 

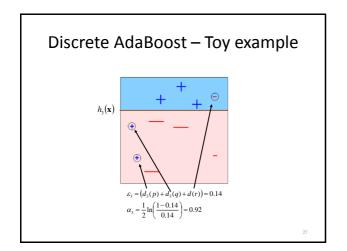


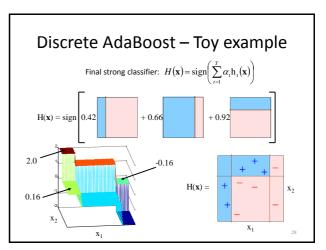
Final strong classifier:  $H(\mathbf{x}) = \operatorname{sign}\left(\sum_{t=1}^{T} \alpha_{t} \mathbf{h}_{t}(\mathbf{x})\right)$ 

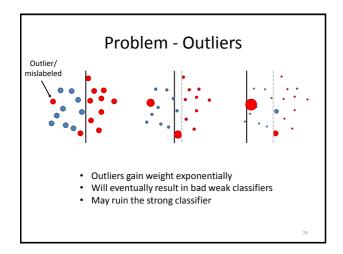
Discrete AdaBoost — Toy example  $\begin{array}{c} \text{Initial weights } d_i(i) = \frac{1}{10}, \text{T} = 3 \\ \hline + & + & - \\ + & - & - \\ \hline + & - & - \\ \end{array}$  In training samples  $\mathbf{x}_i, i = 1...10$  Images borrowed from R. Schapire, "A Boosting Tutorial"







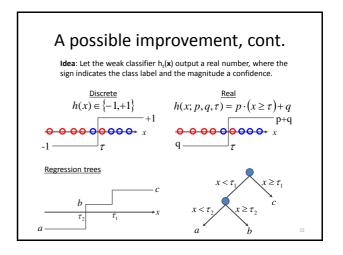




## **Outlier strategies**

- Keep an eye on the weights (plot them!)
- Weight trimming
  - Don't allow weights larger than a certain threshold
  - Disregard training samples with too large weights
- Use alternative weight update schemes with less agressive increases for misclassified training data
  - LogitBoost
  - GentleBoost

Discrete AdaBoost Find weak classifier  $h_i(\mathbf{x}) = \{-1, +1\}$  that minimizes the weighted classification error:  $\varepsilon_i = \sum_{i=1}^M d_i(i) I(y_i \neq h_i(\mathbf{x}_i))$  Will receive the same weight update • In discrete AdaBoost, the weight update for each sample ignores how correct/wrong that sample is. Instead, all correct/wrong samples are updated using an average over all samples! • The discrete weak classifier  $h_i(\mathbf{x}) = \{-1, +1\}$  throws away important information!



### AdaBoost modifications

- Use real-valued outputs from weak classifiers  $h_t(\mathbf{x})$ 
  - Real AdaBoost (as opposed to Discrete AdaBoost)
- More robustness against outliers/noise:
  - LogitBoost
  - GentleBoost

33

## **Summary AdaBoost**

- Nonlinear classifier that is easy to implement
- Easy to use just one parameter (T)
- Can obtain performance similar to SVM
- Inherent feature selection
- Slow to train fast to classify (real-time)
- · Look out for outlier problems
- Try applet:
  - <a href="http://cseweb.ucsd.edu/~yfreund/adaboost/">http://cseweb.ucsd.edu/~yfreund/adaboost/</a>

3.4

# Real-time object detection P. Viola and M. Jones "Rapid Object Detection using a Boosted Cascade of Simple Features", 2001 Sweep a sub-window over the image. for each position, determine if the sub-window contains a face or not.

