1. a) 
$$P(I_{i}) \pi_{i} \pi$$

So, 
$$P(\lambda | \beta, \overline{\tau}^{2}, y, x) \propto P(\beta | \overline{\sigma}^{2}, \lambda) P(\overline{\sigma}^{2} | \lambda) P(\lambda)$$

Now  $\beta | \sigma^{1}, \lambda \sim N(0, \lambda^{2} | \overline{\Gamma})$ 
 $\sigma^{2} | \lambda \sim Inv - \chi^{2}$ 
 $\rho(\lambda | \beta, \overline{\sigma}^{2}, y, x) \propto \frac{1}{1+1} \frac{1}{1+1} \exp\left(-\frac{1}{2} \cdot \frac{1}{4} \beta^{2}\right) \cdot \exp\left(-\frac{R_{0} \lambda_{0}}{2\lambda}\right) \frac{1}{\lambda^{1+1} n^{2} 2}$ 
 $\propto \gamma^{2} \exp\left(-\frac{1}{2} \cdot \frac{2}{1+1} \beta^{2}\right) \exp\left(-\frac{N_{0} \lambda_{0}}{2\lambda}\right) \frac{1}{\lambda^{1+1} n^{2} 2}$ 
 $= \chi^{2} \frac{1}{2} \frac{1}{1+1} \exp\left(-\frac{1}{2} \cdot \frac{2}{1+1} \beta^{2}\right) \exp\left(-\frac{N_{0} \lambda_{0}}{2\lambda}\right) \frac{1}{\lambda^{1+1} n^{2} 2}$ 
 $= \chi^{2} \frac{1}{2} \frac{1}{1+1} \exp\left(-\frac{1}{2} \cdot \frac{2}{1+1} \beta^{2}\right) \exp\left(-\frac{N_{0} \lambda_{0}}{2\lambda}\right)$ 

Not so good. Better if pron wes of the form

 $\lambda^{\alpha} \exp\left(-\lambda b\right)$ .

This the Gamma distribution.

The way to go.

 $\frac{1}{\lambda} \sim \ln u \chi^{2} \left(\eta_{0}, \lambda_{0}\right)$ 
 $\frac{1}{\lambda} \sim \ln u \chi^{2} \left(\eta_{0}, \lambda_{0}\right)$ 

$$\frac{1}{\lambda} \sim |n_{V} - \chi^{2}(n_{0}, \lambda)| \Rightarrow \frac{1}{\lambda} \sim |n_{V} - G_{amna}| \left(\frac{n_{0}}{2}, \frac{n_{0}\lambda_{0}}{2}\right)$$

$$\Rightarrow \lambda \sim G_{amna}| \left(\frac{n_{0}\lambda_{0}}{2}, \frac{n_{0}\lambda_{$$

$$Var(X) = \frac{o^2}{n} \qquad o^2 = Var(X;) \quad X_1 \sim U(\theta^{-1}2, \theta^{-1}2)$$

$$\times \sim U(0,1) \qquad Var(X) = \frac{1}{12}$$

$$So \quad Var(X) = \frac{1}{12n}$$

2b) 
$$P(\theta|X_{1,-},X_{-}) \propto P(X_{1,-},X_{-}|\theta) P(\theta)$$

$$= \prod_{i=1}^{n} P(X_{i}|\theta) P(\theta)$$

$$= \prod_{i=1}^{n} \left(\theta_{2} \leq X_{i} \leq \theta + \frac{1}{2}\right) \cdot 1$$

$$= \theta + \frac{1}{2} \geq X_{max} \Rightarrow \theta \in \left[X_{max} - \frac{1}{2}, X_{min} + \frac{1}{2}\right] \quad \theta + \frac{1}{2} = X_{min}$$

$$= \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} + \frac{1}{2}\right) \cdot \frac{1}{2} \quad \theta + \frac{1}{2} = X_{min}$$

2c) Frequentity: 
$$\hat{Q} = \hat{X} = 1.53$$

$$Va-(\hat{\sigma}) = \frac{1}{12h} = \frac{1}{12.3} = 0.027777$$

$$SO(\hat{Q}) = 0.1666$$

$$Dayerin = \Theta[X,XXX, -U(1.59,1.6)]$$

$$\frac{3a}{9} \frac{9|x_{1...} \times x_{1}}{8} \sim \frac{8ete(x+s, \beta+f)}{1-e}$$

$$\frac{9|t| \times x_{2}}{9} \sim \frac{8ete(x+s, \beta+f)}{1-e} \sim \frac{1}{1-e} \frac{1}{1-e} \frac{1}{1-e} \sim \frac{1}{1-e}$$

$$P(A|T_1,T_2) \propto P(T_1,T_2|A)P(A)$$
  
=  $P(T_1|A)\cdot P(T_2|A)P(A)$ 

$$E(\theta_1|h_A, h_{B,N_c}) = \frac{6}{23} \approx 0.26$$

$$E(\theta_2|\cdot) = \frac{6}{23} = 0.26$$

$$E(\theta_3|\cdot) = \frac{11}{23} \approx 0.48$$

$$P(T, 1A) \qquad N(M_{1A}, 1)$$

$$M_{1A} | X_{1} = 1.2 \quad -N(1.2, \frac{1}{5})$$

$$M_{1D} | X_{1} = 1.4 \quad -N(1.4, \frac{1}{5})$$

$$M_{1C} | X_{1} = 0.7 \quad -N(0.7, \frac{1}{10})$$

$$M_{2A} | X_{2} = 21 \quad -N(2.7, \frac{1}{5})$$

$$M_{2C} | X_{2} = 21 \quad -N(2.7, \frac{1}{5})$$

$$M_{2C} | X_{2} = 21 \quad -N(2.7, \frac{1}{5})$$

$$M_{2C} | X_{2} = 21 \quad -N(2.7, \frac{1}{5})$$

 $P(A | T_{1}=1.3, T_{2}=4.2) \propto P(T_{1}=1.3) A) \cdot P(T_{2}=4.2| A) \cdot P(A)$   $= \phi(1.3, M=1.2, \sigma^{2}=\frac{1}{5}) \cdot \phi(4.2, M=2.5, \sigma^{2}=\frac{1}{5}) \cdot \frac{6}{23}$   $P(B|T_{1}=1.3, T_{2}=4.2) \propto \phi(1.3) \cdot 1.4, \frac{1}{5}) \phi(4.2, 3.5, \frac{1}{5}) \cdot \frac{6}{23}$   $P(C|T_{1}=1.5, T_{2}=4.2) \propto \phi(1.5) \cdot 0.7, \frac{1}{60} \cdot \phi(4.2) \cdot 4.2 \cdot \frac{1}{60} \cdot \frac{11}{23}$