

# Absolute scale velocity determination combining visual and inertial measurements for micro aerial vehicles

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## Micro aerial vehicles



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**Localization in various environments**

# Micro aerial vehicles



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A basic state vector:

$$X = \begin{bmatrix} \textit{position} \\ \textit{velocity} \\ \textit{orientation} \end{bmatrix}$$

**Localization in various environments**

# Micro aerial vehicles



A basic state vector:

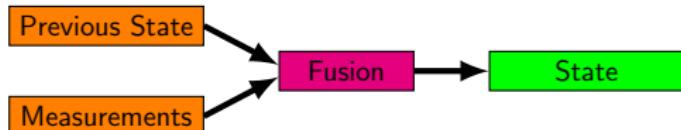
$$X = \begin{bmatrix} \textit{position} \\ \textit{velocity} \\ \textit{orientation} \end{bmatrix}$$

## Localization in various environments

The goal of sensor fusion for state estimation is to **recover  $X$**

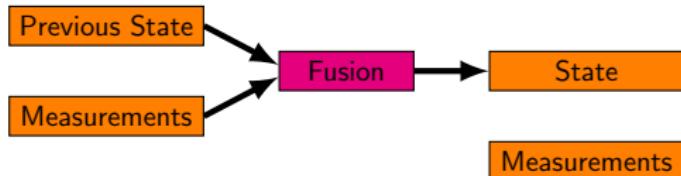
# Visual-inertial sensor fusion

## Filter based method



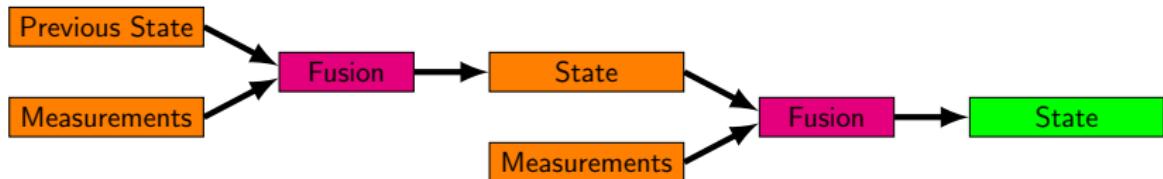
# Visual-inertial sensor fusion

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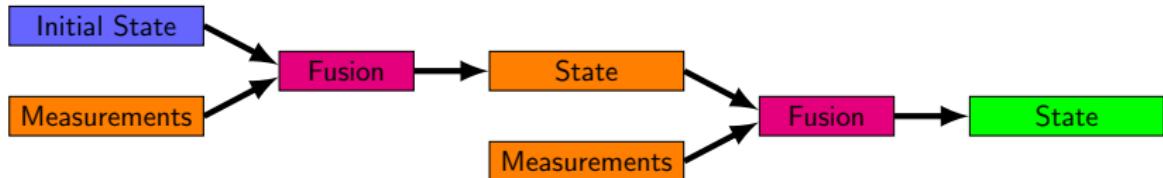
# Visual-inertial sensor fusion

## Filter based method



# Visual-inertial sensor fusion

## Filter based method



How to recover the **initial state**?

# Visual-inertial sensor fusion

## Filter based method

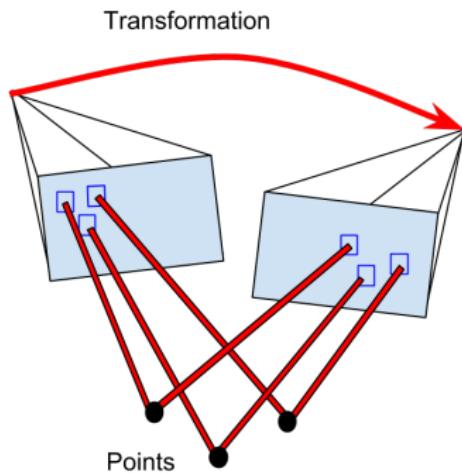


How to recover the **initial state**?

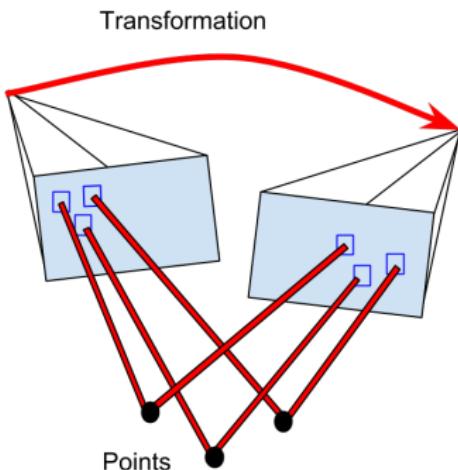
We need a **deterministic solution**



# Deterministic solutions in Computer Vision



# Deterministic solutions in Computer Vision



But the relative **translation** and **distance to features** are recovered only  
**up to scale**

# Absolute scale from visual measurements

How big is this building?



## Absolute scale from visual measurements



## Methods to recover the absolute scale



## Methods to recover the absolute scale



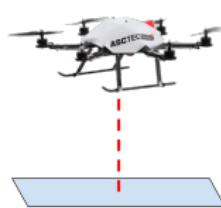
## Methods to recover the absolute scale



# Methods to recover the absolute scale



Not suited to  
unknown  
environments



Not precise, works  
only in hover



Does not work in GPS  
denied environments

## Inertial Measurement Unit (IMU)

The IMU consists of two sensors providing **physical quantities**:

- ▶ Accelerometer: linear acceleration (and gravity) ( $m/s^2$ );
- ▶ Gyroscope: angular velocity ( $rad/s$ ).

[Back to the title](#)

Absolute scale velocity determination combining visual and inertial measurements for micro aerial vehicles

[Back to the title](#)

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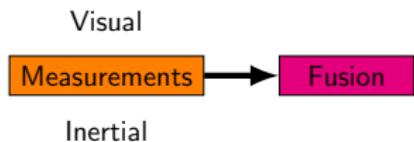
Visual

Measurements

Inertial

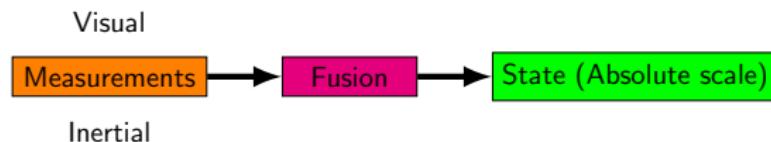
## Back to the title

Absolute scale velocity **determination** combining **visual** and **inertial measurements** for micro aerial vehicles



[Back to the title](#)

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# Table of Contents

## Sensor fusion

- Filter based fusion

- Deterministic solution

- Absolute scale

## The closed-form solution

- Expression

- Identifying performance bottlenecks

- Estimating the gyroscope bias

- Validation

## Conclusion

## The closed-form solution

Transactions on Robotics (T-RO) 2012

International Journal of Computer Vision (IJCV) 2014

# The Closed-Form Solution

Requires:

- ▶ Calibrated camera;
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Output:

- ▶ Initial velocity;
- ▶ Distance to point-features;
- ▶ Roll, pitch.

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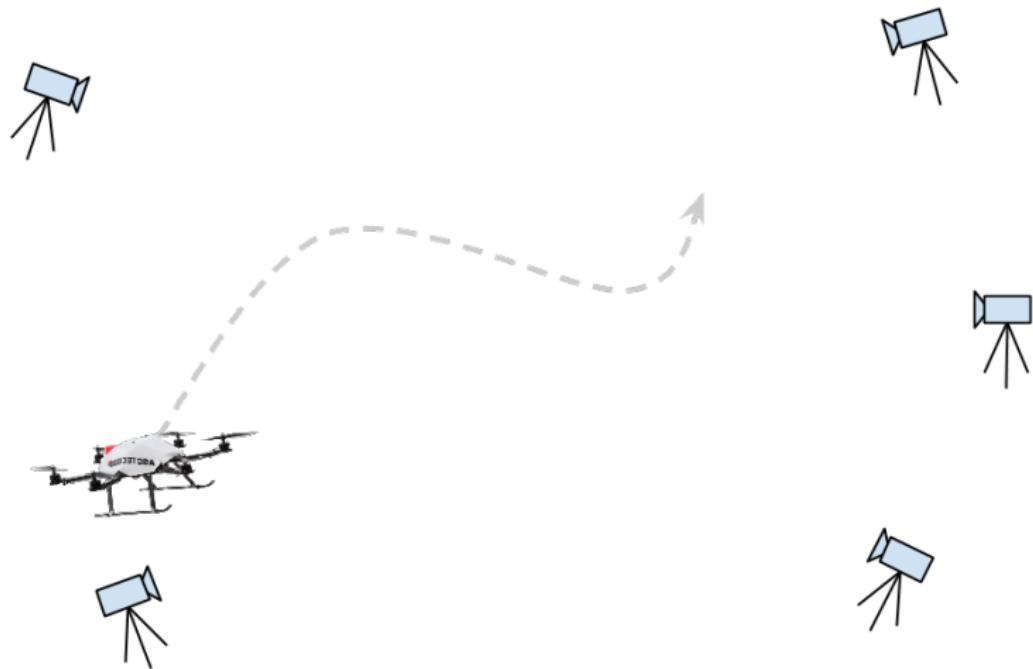
## Test setup



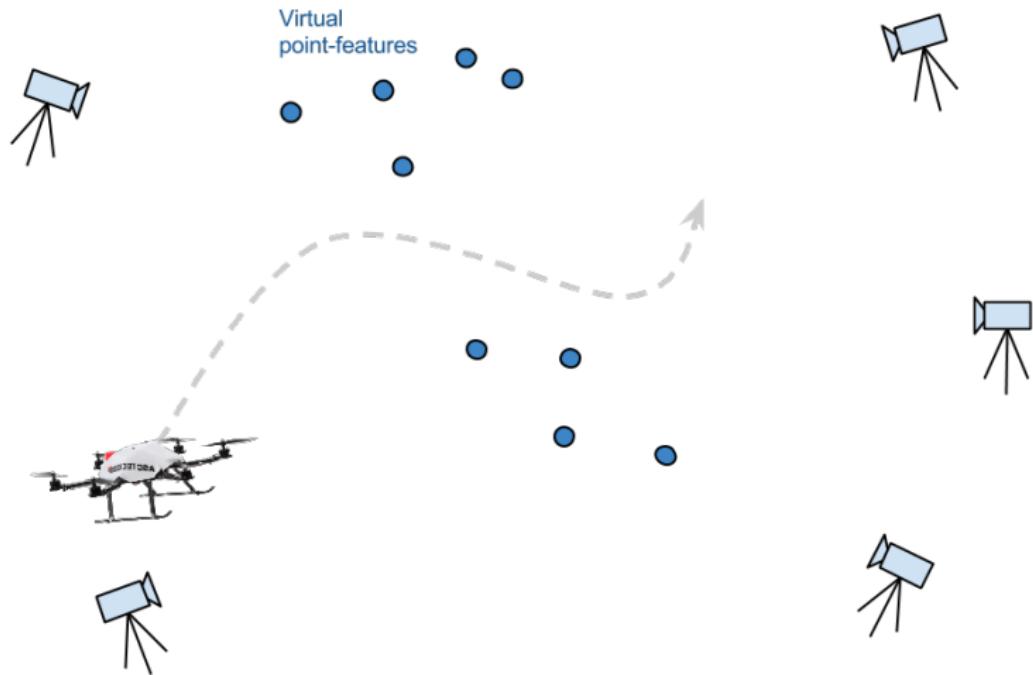
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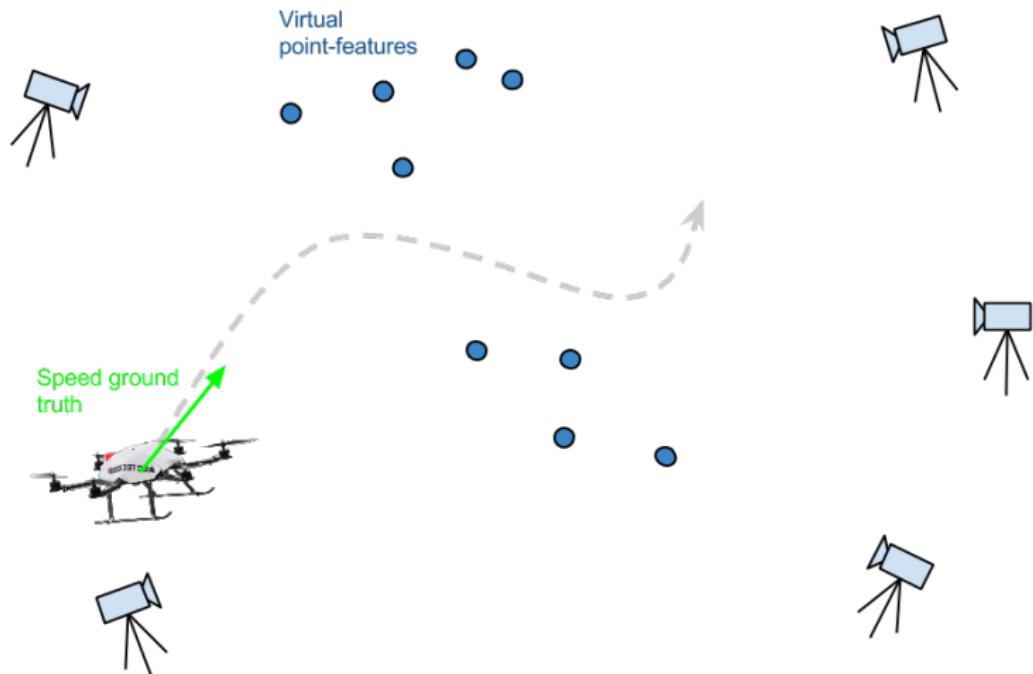
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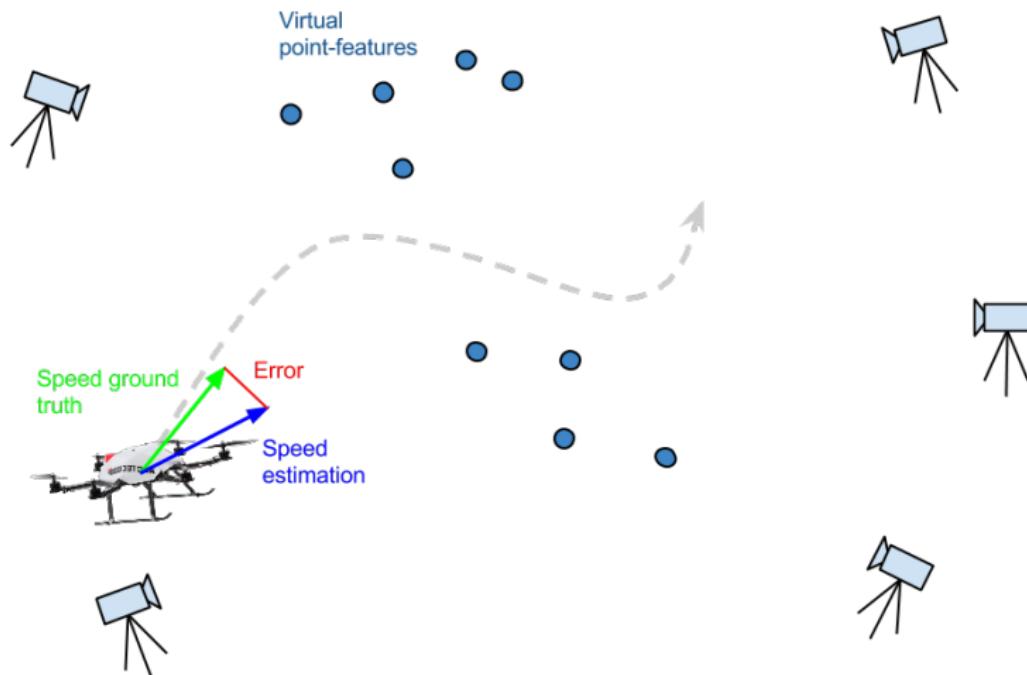
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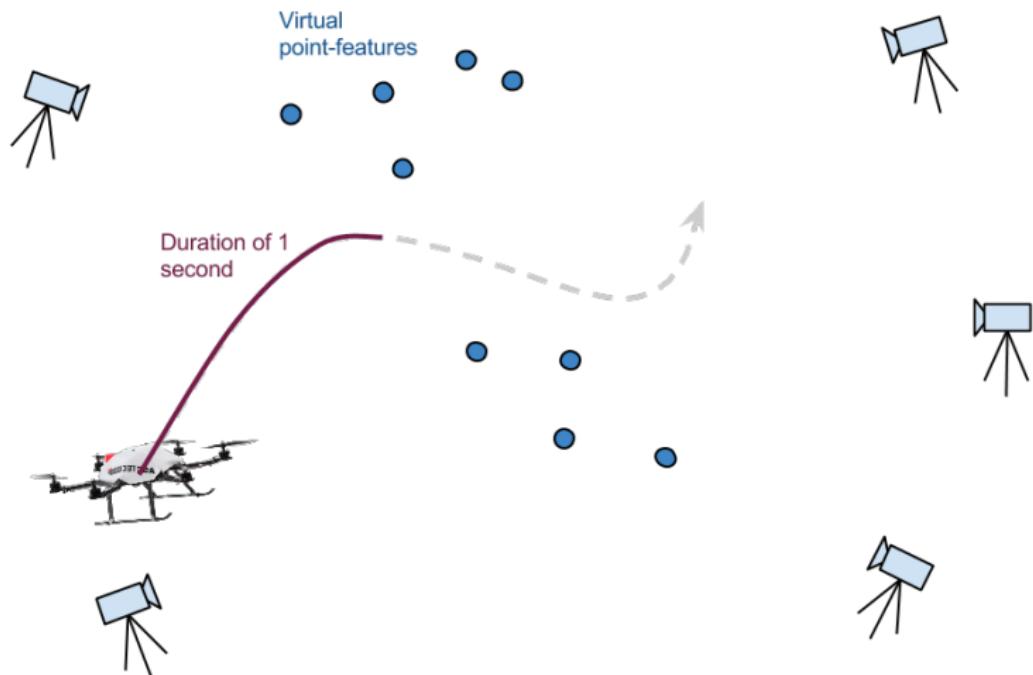
## Test setup



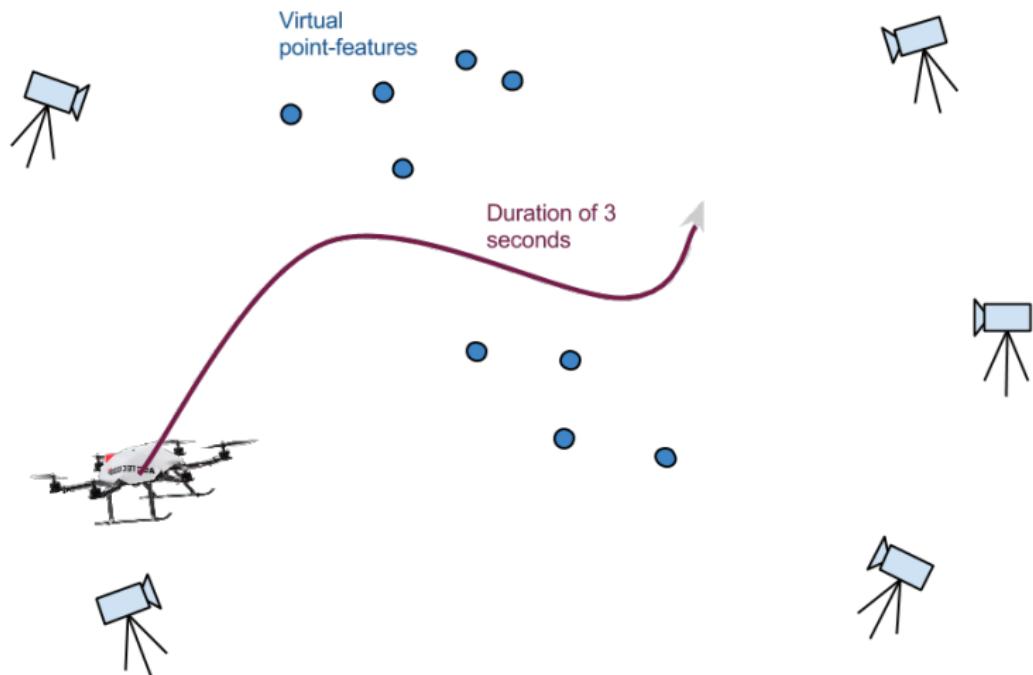
# Test setup



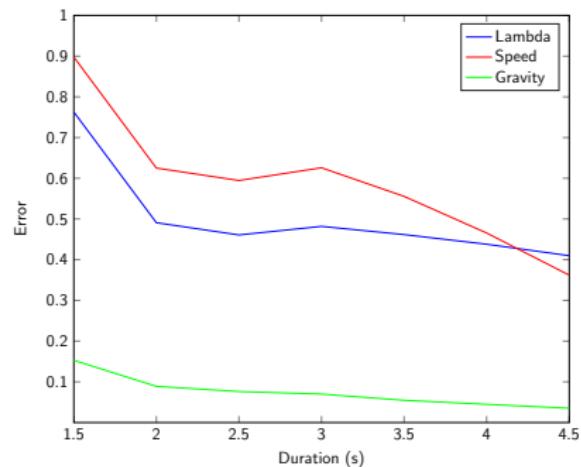
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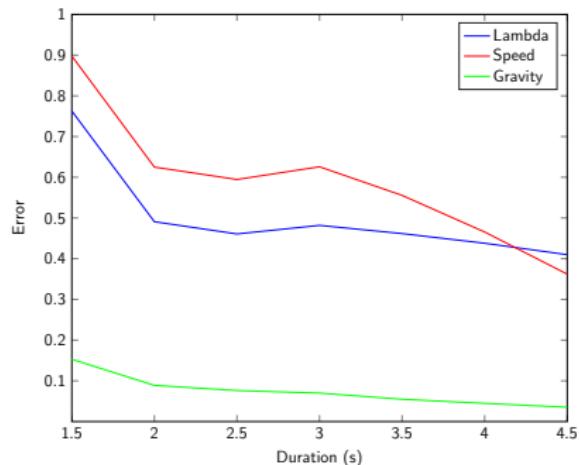
## Test setup



## Problem: not robust in practice

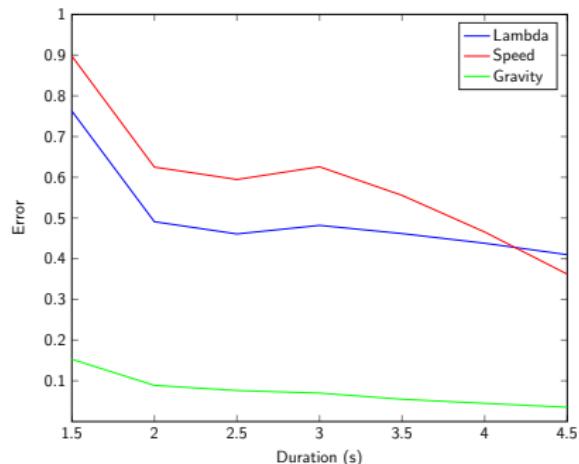


## Problem: not robust in practice



50% relative error on speed and distance estimation

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50% relative error on speed and distance estimation

**"A closed-form solution for state estimation with a visual-inertial system that does not require initialization was presented. However, this approach is not suitable for systems that rely on noisy sensor data"**

— Matthias Faessler, ICRA 2015

# Improving the performance

What makes the estimations so bad?

Possible bottlenecks

- ▶ Motion;

# Improving the performance

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## Possible bottlenecks

- ▶ Motion;
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## Possible bottlenecks

- ▶ Motion;
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Sensors provide measurements affected by a Gaussian noise:

$$N(\mu + B, \sigma^2)$$

# Improving the performance

What makes the estimations so bad?

## Possible bottlenecks

- ▶ Motion;
- ▶ Observed features;
- ▶ Noisy sensors.

Sensors provide measurements affected by a Gaussian noise:

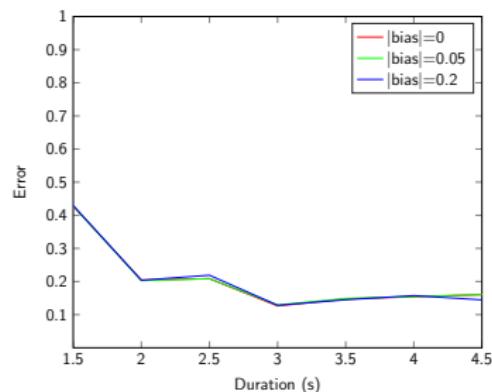
$$N(\mu + B, \sigma^2)$$

We considered:

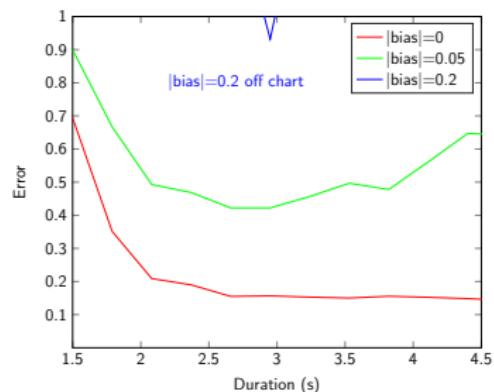
- ▶ Biased accelerometer;
- ▶ Biased gyroscope.

# Biased inertial measurements

## Speed estimation error



Varying accelerometer bias



Varying gyroscope bias

## Estimating the gyroscope bias

Reminder:  $\Xi X = S$



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- ▶ Insert the gyro bias  $B$  in  $X$ ;

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- ▶ Insert the gyro bias  $B$  in  $X$ ;
- ▶ Alternative: non-linear minimization of the residual

$$cost(B) = \underset{X}{\operatorname{argmin}} ||\Xi X - S||^2$$

With:

$B$  the gyroscope bias,

$\Xi$  and  $S$  computed with respect to  $B$

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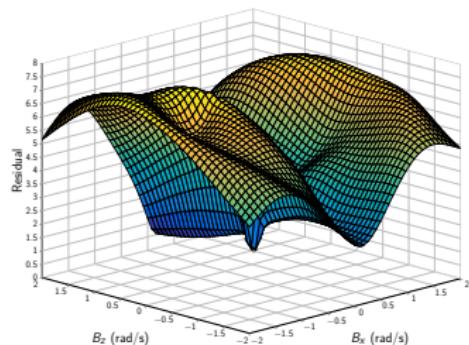
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Cost function: residual with respect to gyroscope bias

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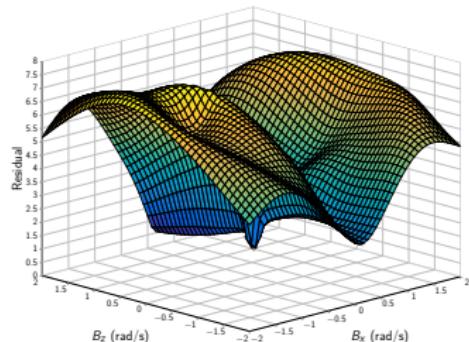
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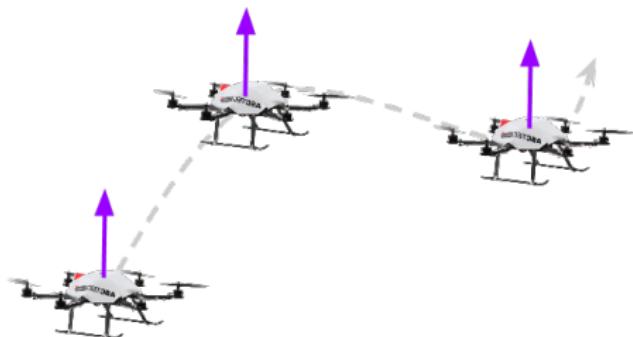
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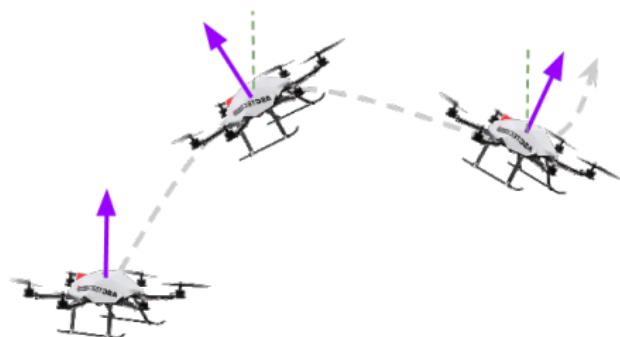
Cost function: residual with respect to gyroscope bias

Symmetry induced by the strong weight of the gravity

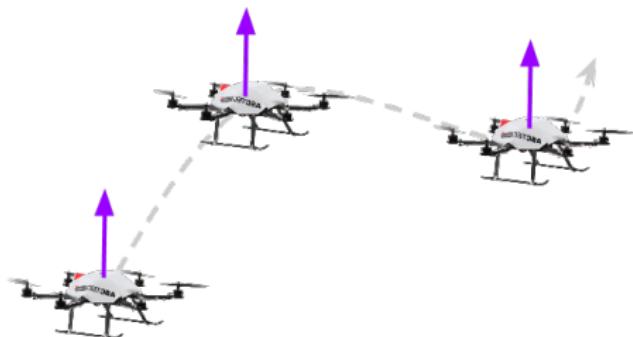
## Dealing with the symmetry



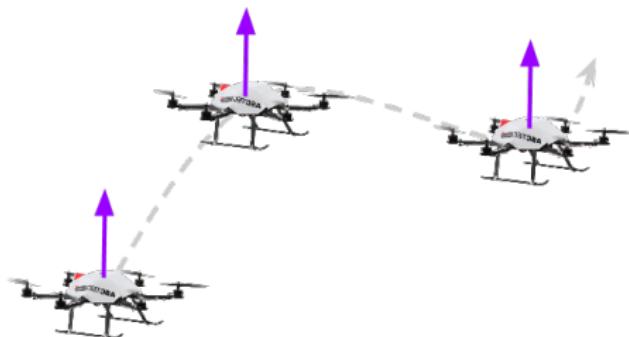
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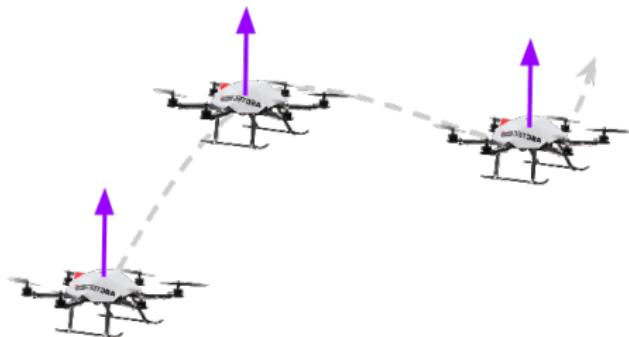
## Dealing with the symmetry



We tweak the cost function:

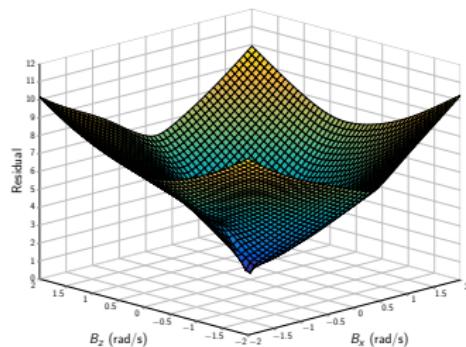
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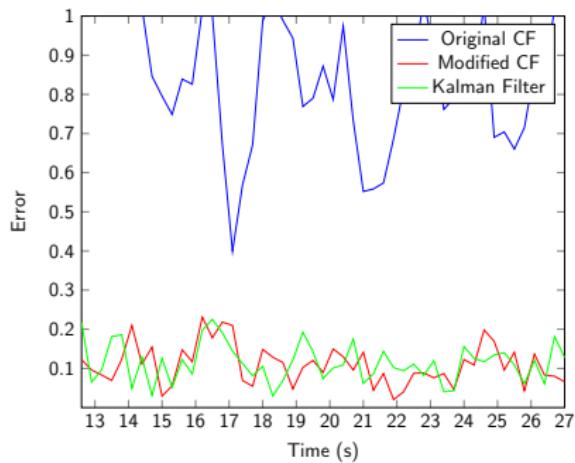
$$\text{cost}(B) = \underset{X}{\operatorname{argmin}} ||\Xi X - S||^2 + \lambda \times |B|$$



Regularized cost function with  $\lambda = 3$

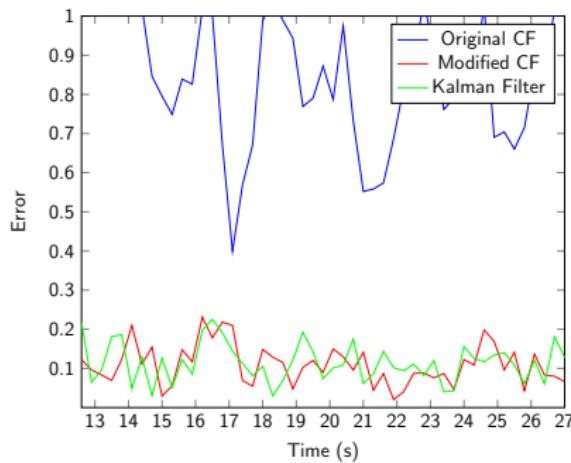
# Results

## Speed estimation error



## Results

### Speed estimation error



Moreover, our technique:

- ▶ Does not require initialization;
- ▶ Provides the gyroscope bias.

## Conclusion

# Conclusion

## Theory:

Visual



Inertial

# Conclusion

## Theory:

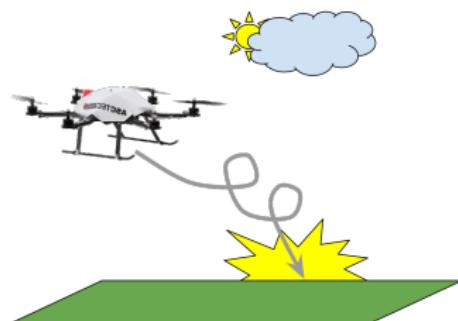
Visual



Inertial

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## Practice:



# Conclusion

## Theory:

Visual

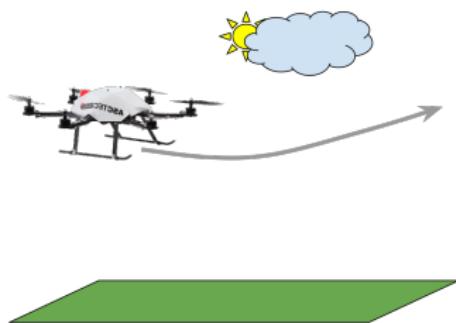


Inertial

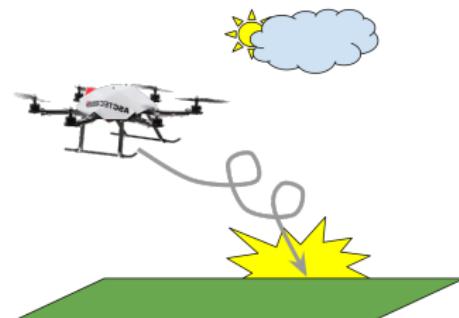
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## Practice:

Accelerometer bias?



Gyroscope bias?



# Conclusion

## Theory:

Visual



Inertial

---

## Practice:

**Optimization** to recover the gyroscope bias



## Future work

Implementation on a real platform



Thank you for your attention,  
Any question?

# The Closed-Form Solution

Requires:

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$$S_j = \lambda_1^i \mu_1^i - V t_j - G \frac{t_j^2}{2} - \lambda_j^i \mu_j^i$$

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## The Overconstrained Linear System

$$S_j = \lambda_1^i \mu_1^i - V t_j - G \frac{t_j^2}{2} - \lambda_j^i \mu_j^i$$

Valid for every point-feature  $i$  at any time  $t_j$ :

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$$\begin{cases} S_2 = \lambda_1^1 \mu_1^1 - V t_2 - G \frac{t_2^2}{2} - \lambda_2^1 \mu_2^1 \\ S_2 = \lambda_1^2 \mu_1^2 - V t_2 - G \frac{t_2^2}{2} - \lambda_2^2 \mu_2^2 \\ \vdots \\ S_3 = \lambda_1^1 \mu_1^1 - V t_3 - G \frac{t_3^2}{2} - \lambda_3^1 \mu_3^1 \\ \vdots \\ S_N = \lambda_1^{n_i} \mu_1^{n_i} - V t_N - G \frac{t_N^2}{2} - \lambda_N^{n_i} \mu_N^{n_i} \end{cases}$$

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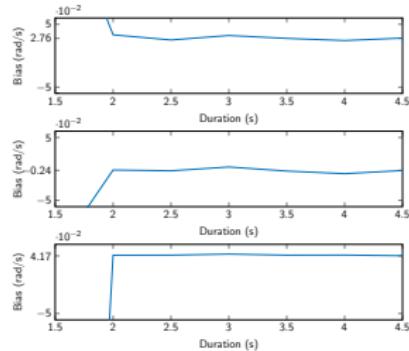
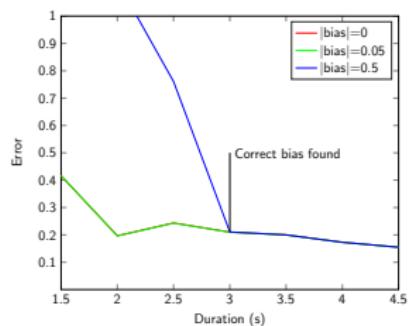
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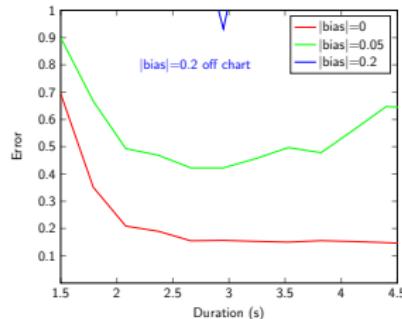
$$\Xi X = S$$

# Gyroscope bias estimation

## Optimized Closed-form solution



## Original Closed-form solution



## Numerical stability

$$\left[ \begin{array}{lcl} S_j & = & \lambda_1^1 \mu_1^1 - Vt_j - G \frac{t_j^2}{2} - \lambda_j^1 \mu_j^1 \\ 0_3 & = & \lambda_1^1 \mu_1^1 - \lambda_j^1 \mu_j^1 - \lambda_1^i \mu_1^i + \lambda_j^i \mu_j^i \end{array} \right] \quad \left| \quad S_j = \lambda_1^i \mu_1^i - Vt_j - G \frac{t_j^2}{2} - \lambda_j^i \mu_j^i \right.$$

