

Problem Set 3

Applied Stats/Quant Methods 1

Due: November 12, 2021

Instructions

- Please show your work! You may lose points by simply writing in the answer. If the problem requires you to execute commands in R, please include the code you used to get your answers. Please also include the .R file that contains your code. If you are not sure if work needs to be shown for a particular problem, please ask.
- Your homework should be submitted electronically on GitHub in .pdf form.
- This problem set is due before class on Friday November 12, 2021. No late assignments will be accepted.
- Total available points for this homework is 80.

In this problem set, you will run several regressions and create an add variable plot (see the lecture slides) in R using the `incumbents_subset.csv` dataset. Include all of your code.

Question 1

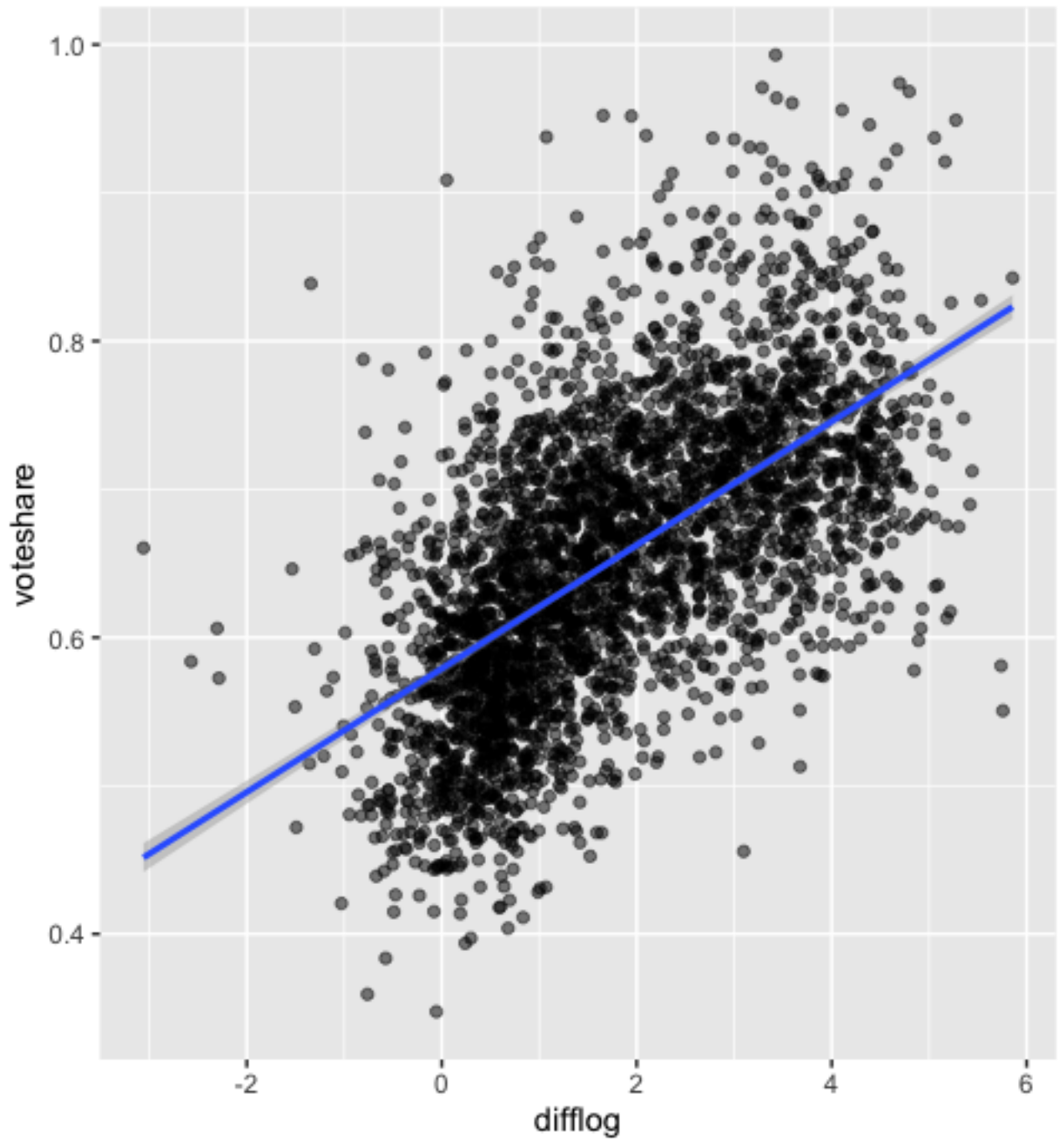
We are interested in knowing how the difference in campaign spending between incumbent and challenger affects the incumbent's vote share.

1. Run a regression where the outcome variable is `voteshare` and the explanatory variable is `difflog`.

```
1 #Load the data set incumbents
2 incumbents <- read_csv("https://raw.githubusercontent.com/jackoneillWHU/
  StatsI_Fall2021/main/datasets/incumbents_subset.csv")
3
4 #run regression with voteshare as outcome variable and difflog as
  explanatory variable
5 summary(lm( data = incumbents, voteshare ~ difflog))
6 lm1 <- lm( data = incumbents, voteshare ~ difflog)
```

2. Make a scatterplot of the two variables and add the regression line.

```
1 #create a scatterplot with regression line
2 ggplot(data = incumbents, aes(x = difflog, y = voteshare)) +
3   geom_point(alpha = 0.5) + #add a scatterplot
4   geom_smooth(method = "lm") #add a linear regression line
```



3. Save the residuals of the model in a separate object.

```
1 #save residuals as new object
2 residuals(lm1)
3 incumbents$residuals <- residuals(lm1)
```

4. Write the prediction equation.

The mathematical formula of the linear regression can be written as $y = a + b \cdot x$ or $y = b_0 + b_1 \cdot x$, where: b_0 and b_1 are known as the regression beta coefficients or parameters: b_0 is the intercept of the regression line; that is the predicted value when $x = 0$. b_1 is the slope of the regression line. For our regression the prediction equation is: $y = 0.579031 + 0.041666 \cdot x$

Question 2

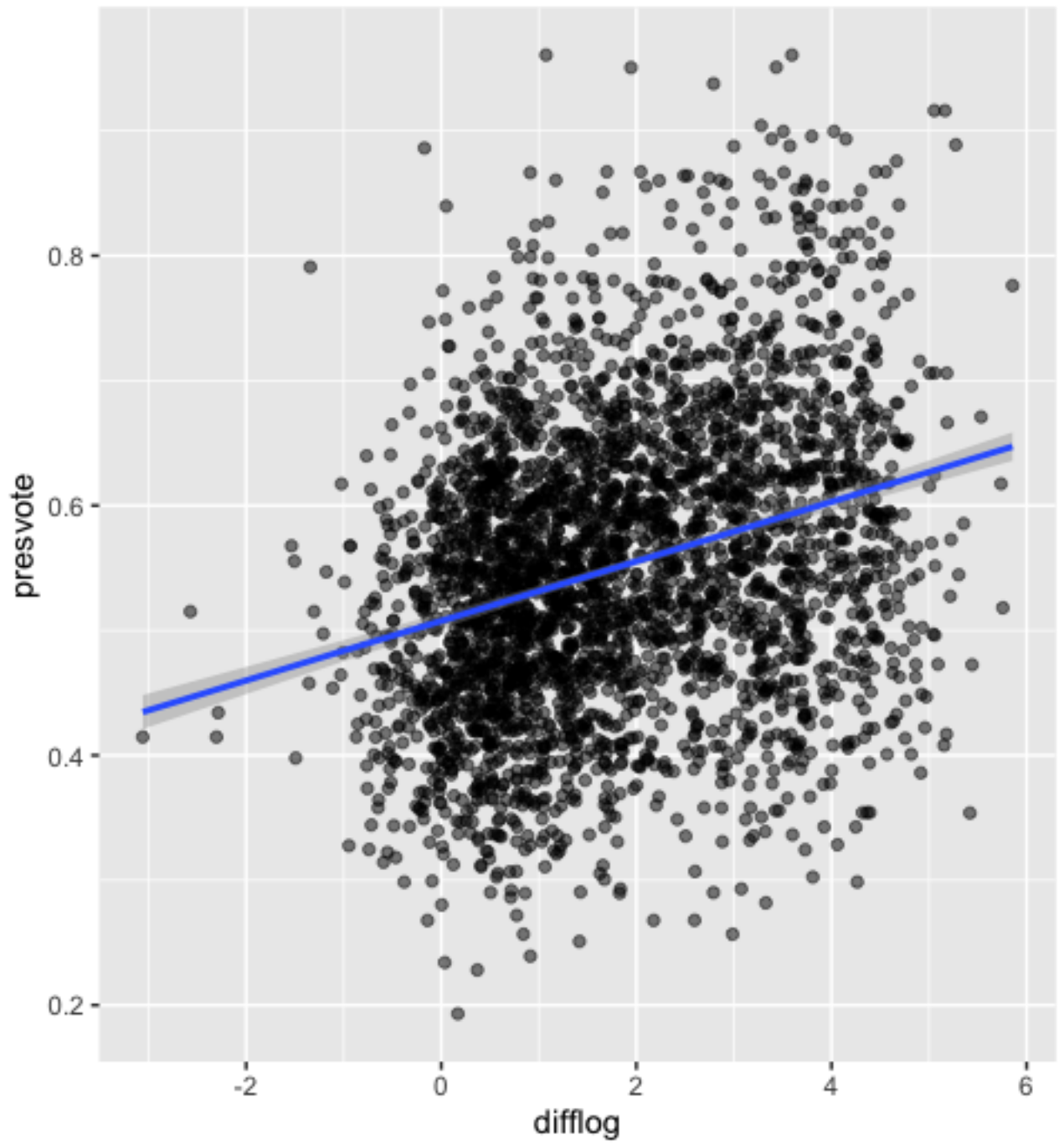
We are interested in knowing how the difference between incumbent and challenger's spending and the vote share of the presidential candidate of the incumbent's party are related.

1. Run a regression where the outcome variable is `presvote` and the explanatory variable is `difflog`.

```
1 #run regression with presvote as outcome variable and difflog as
  explanatory variable
2 summary(lm( data = incumbents, presvote ~ difflog))
3 lm2 <- lm( data = incumbents, presvote ~ difflog)
```

2. Make a scatterplot of the two variables and add the regression line.

```
1 #run regression with presvote as outcome variable and difflog as
  explanatory variable
2 summary(lm( data = incumbents, presvote ~ difflog))
3 lm2 <- lm( data = incumbents, presvote ~ difflog)
```



3. Save the residuals of the model in a separate object.

```
1 #save residuals as new object
2 residuals(lm2)
3 incumbents$residuals2 <- residuals(lm2)
```

4. Write the prediction equation.

For this regression the prediction equation is: $y = 0.507583 + 0.023837x$

Question 3

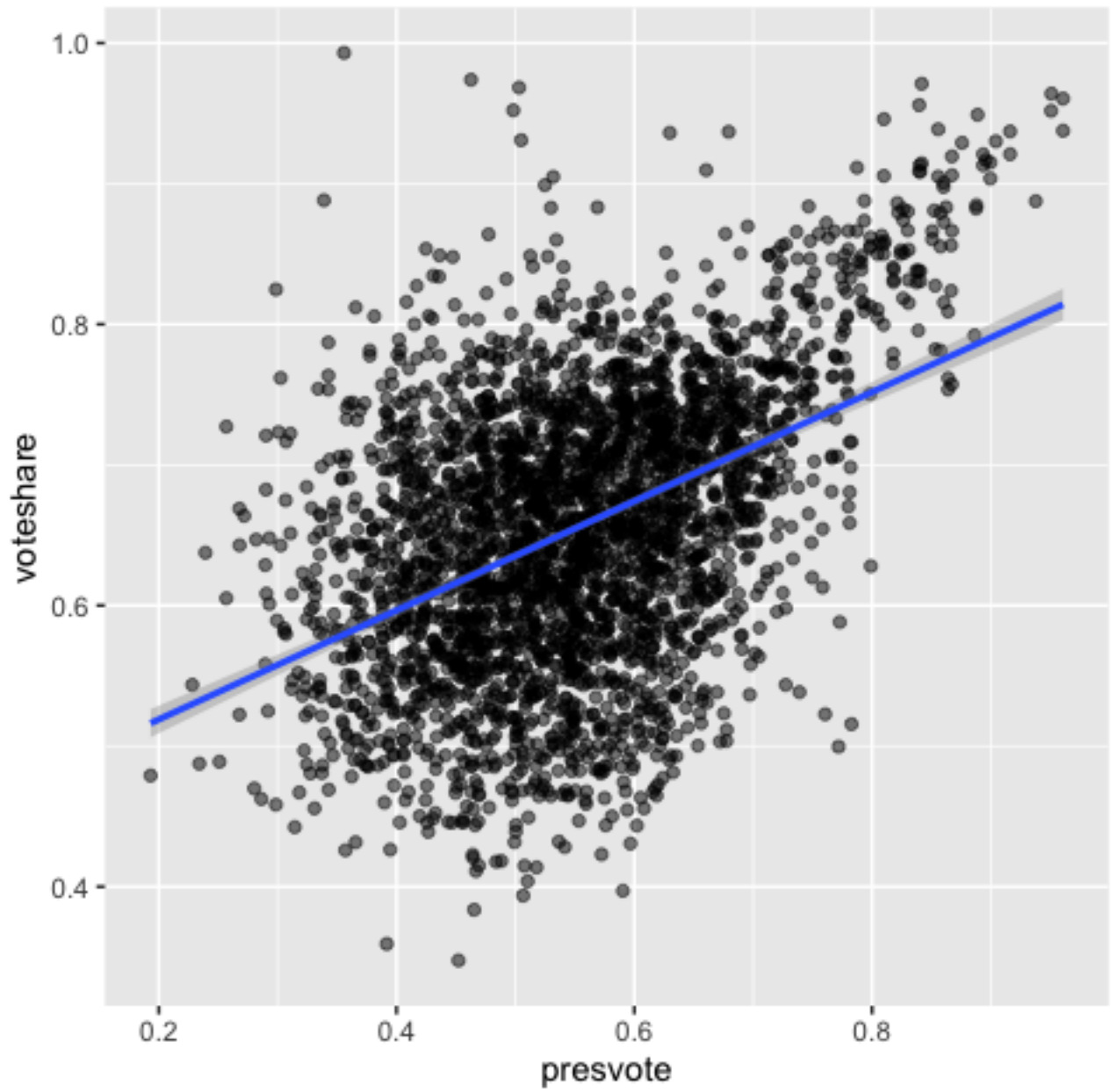
We are interested in knowing how the vote share of the presidential candidate of the incumbent's party is associated with the incumbent's electoral success.

1. Run a regression where the outcome variable is **voteshare** and the explanatory variable is **presvote**.

```
1 #run regression with voteshare as outcome variable and presvote as  
  explanatory variable  
2 summary(lm( data = incumbents, voteshare ~ presvote))  
3 lm3 <- lm( data = incumbents, voteshare ~ presvote)
```

2. Make a scatterplot of the two variables and add the regression line.

```
1 #create a scatterplot with regression line  
2 ggplot(data = incumbents, aes(x = presvote, y = voteshare)) +  
3   geom_point(alpha = 0.5) + #add a scatterplot  
4   geom_smooth(method = "lm") #add a linear regression line
```



3. Write the prediction equation.

For this regression the prediction equation is: $y = 0.441330 + 0.388018 \cdot x$

Question 4

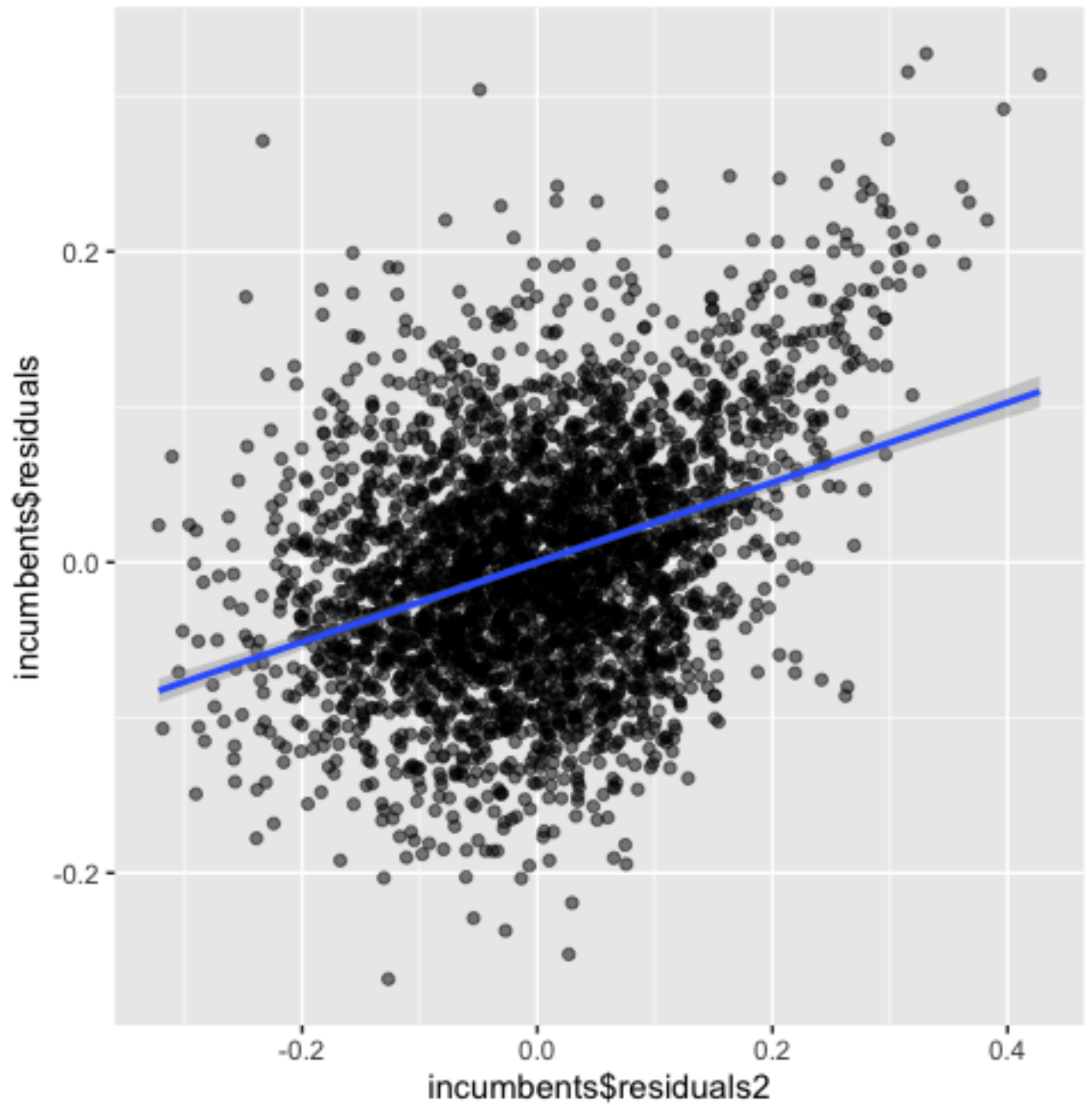
The residuals from part (a) tell us how much of the variation in **voteshare** is *not* explained by the difference in spending between incumbent and challenger. The residuals in part (b) tell us how much of the variation in **presvote** is *not* explained by the difference in spending between incumbent and challenger in the district.

1. Run a regression where the outcome variable is the residuals from Question 1 and the explanatory variable is the residuals from Question 2.

```
1 #run regression with incumbents$residuals as outcome variable and  
  incumbents$residuals2 as the explanatory variable  
2 summary(lm(data=incumbents, incumbents$residuals ~incumbents$residuals2))
```

2. Make a scatterplot of the two residuals and add the regression line.

```
1 #create a scatterplot with regression line  
2 ggplot(data = incumbents, aes(x = incumbents$residuals2, y = incumbents$  
  residuals)) +  
3   geom_point(alpha = 0.5) + #add a scatterplot  
4   geom_smooth(method = "lm") #add a linear regression line
```



3. Write the prediction equation.

For this regression the prediction equation is: $y = -0.00000000000000005207 + 0.256877012700097828724 \cdot x$

Question 5

What if the incumbent's vote share is affected by both the president's popularity and the difference in spending between incumbent and challenger?

1. Run a regression where the outcome variable is the incumbent's `voteshare` and the explanatory variables are `difflog` and `presvote`.

```
1 #run regression with voteshare as outcome variable and difflog and  
  presvote as the explanatory variables  
2 summary(lm(data = incumbents, voteshare ~ difflog + presvote))
```

2. Write the prediction equation.

For this regression the prediction equation is: $y = -0.4486442 + 0.0355431 \cdot \text{difflog} + 0.2568770 \cdot \text{presvote}$

3. What is it in this output that is identical to the output in Question 4? Why do you think this is the case?