

6

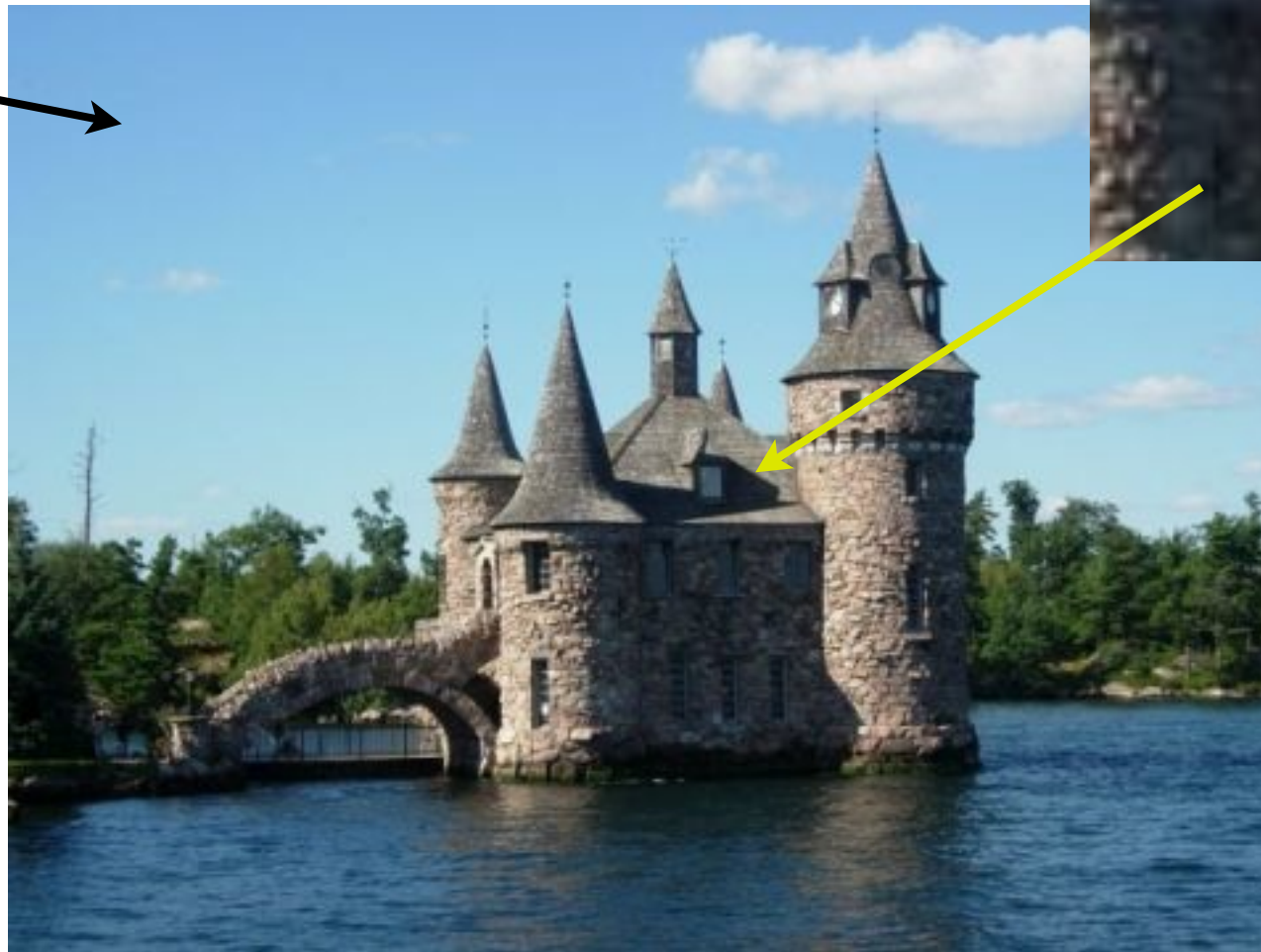
Filtering the Images

- ▶ Filtering images using low-pass filters
- ▶ Filtering images using a median filter
- ▶ Applying directional filters to detect edges
- ▶ Computing the Laplacian of an image

Frequency domain representation of the image



small variation
=
low frequency



large variation
=
high frequency

Frequency domain representation of the image

Low pass filter

= Low frequency pass filter

= image spacial smoothing



Image Smoothing = Low pass filtering

$$I'(x) = \frac{1}{3}I(x-1) + \frac{1}{3}I(x) + \frac{1}{3}I(x+1)$$

$$I' = \begin{bmatrix} \frac{1}{3} & \frac{1}{3} & \frac{1}{3} \end{bmatrix} * I$$

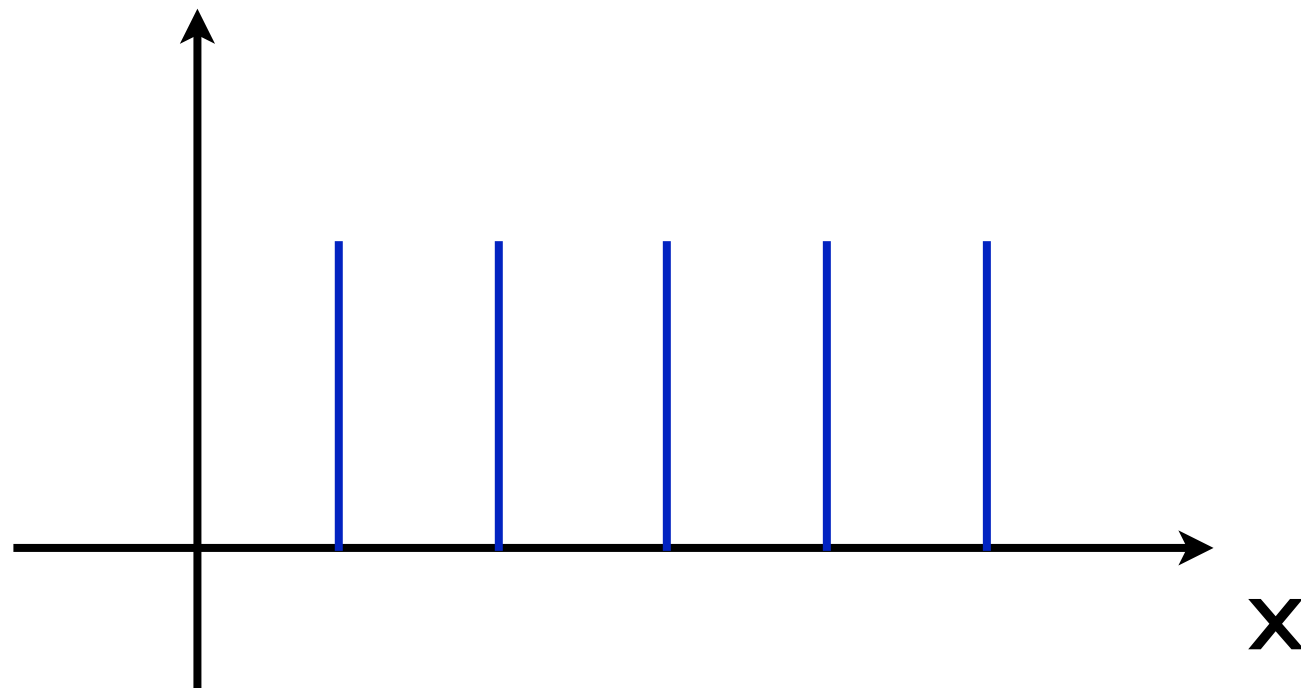
- Smoothing in the x-direction
- No change in the constant intensity area
- Big change on the edge (intensity discontinuity)
- Some simple examples

How to program in C/C++ with OpenCV

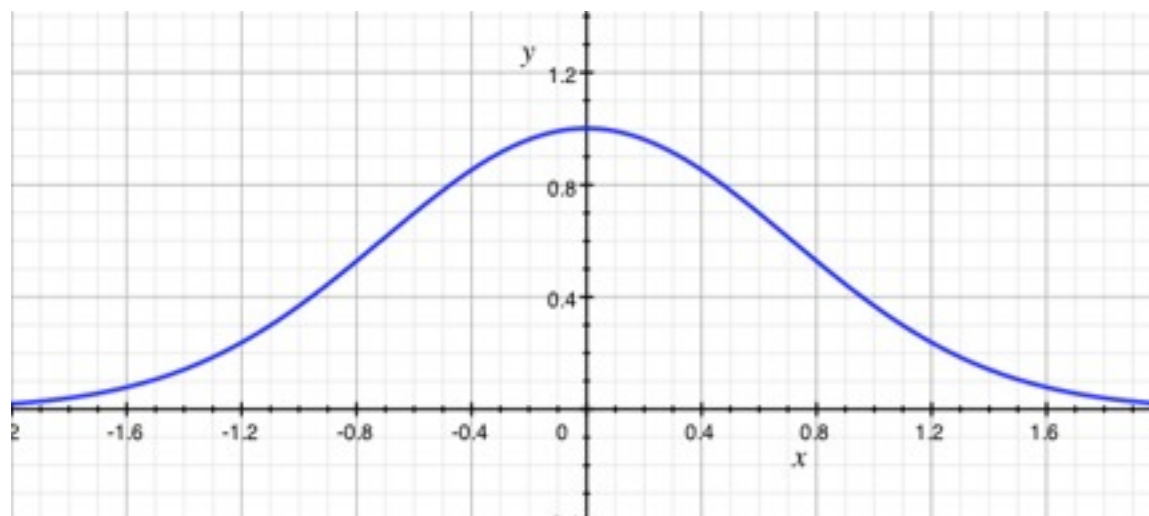
```
for (int r=0; r<I.rows; r++)  
{  
    uchar *ptr = I.ptr<uchar>(r);  
    for (int c=1; c<I.cols-1; c++)  
        J.at<uchar>(r,c) = (uchar)(ptr[c-1]/3.0+ptr[c]/3.0+ptr[c+1]/3.0);  
}
```

- The kernel size may be increased.
 - The sum of the kernel is 1. Why?
- The smoothing direction may be changed.

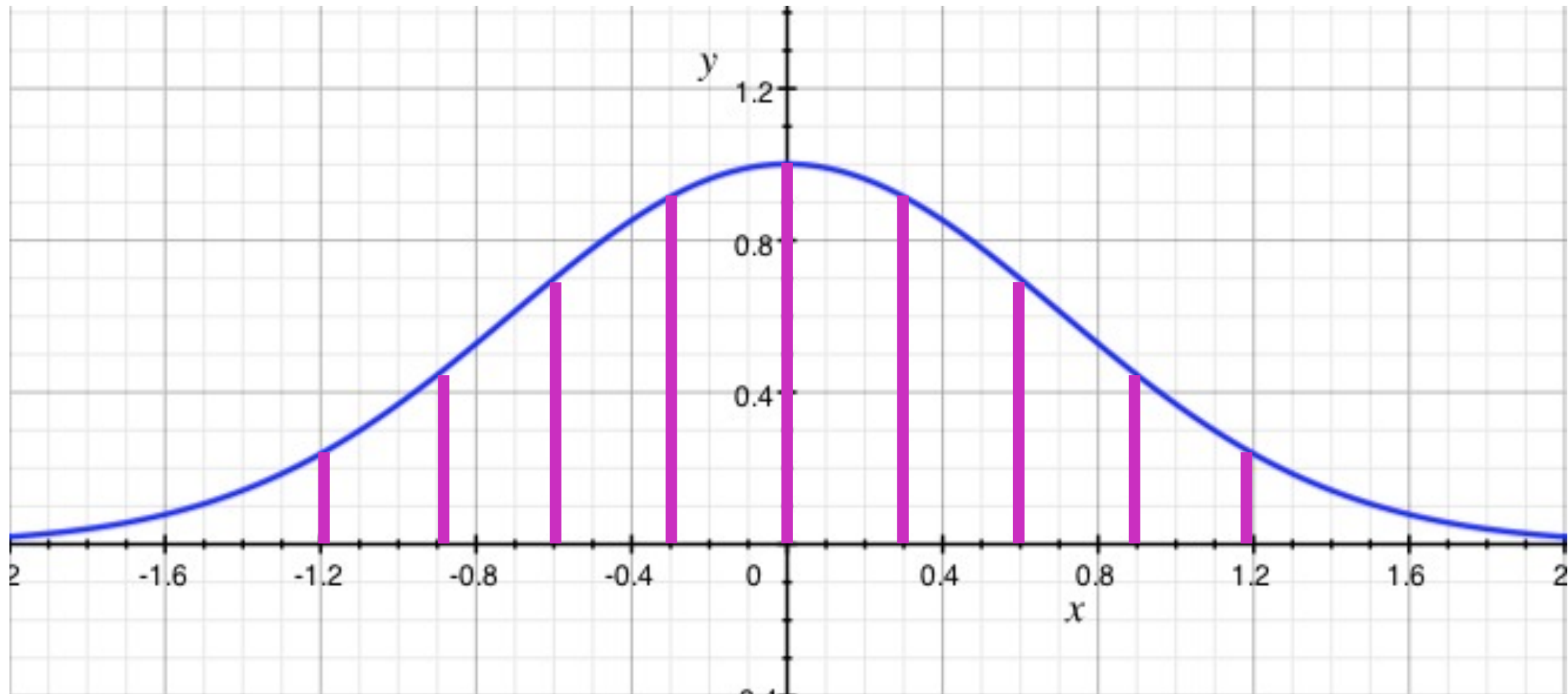
The shape of the filter kernel looks like a box.



- This filter is called a box filter (average/mean filter)
- Triangle filter.
- Gaussian filter

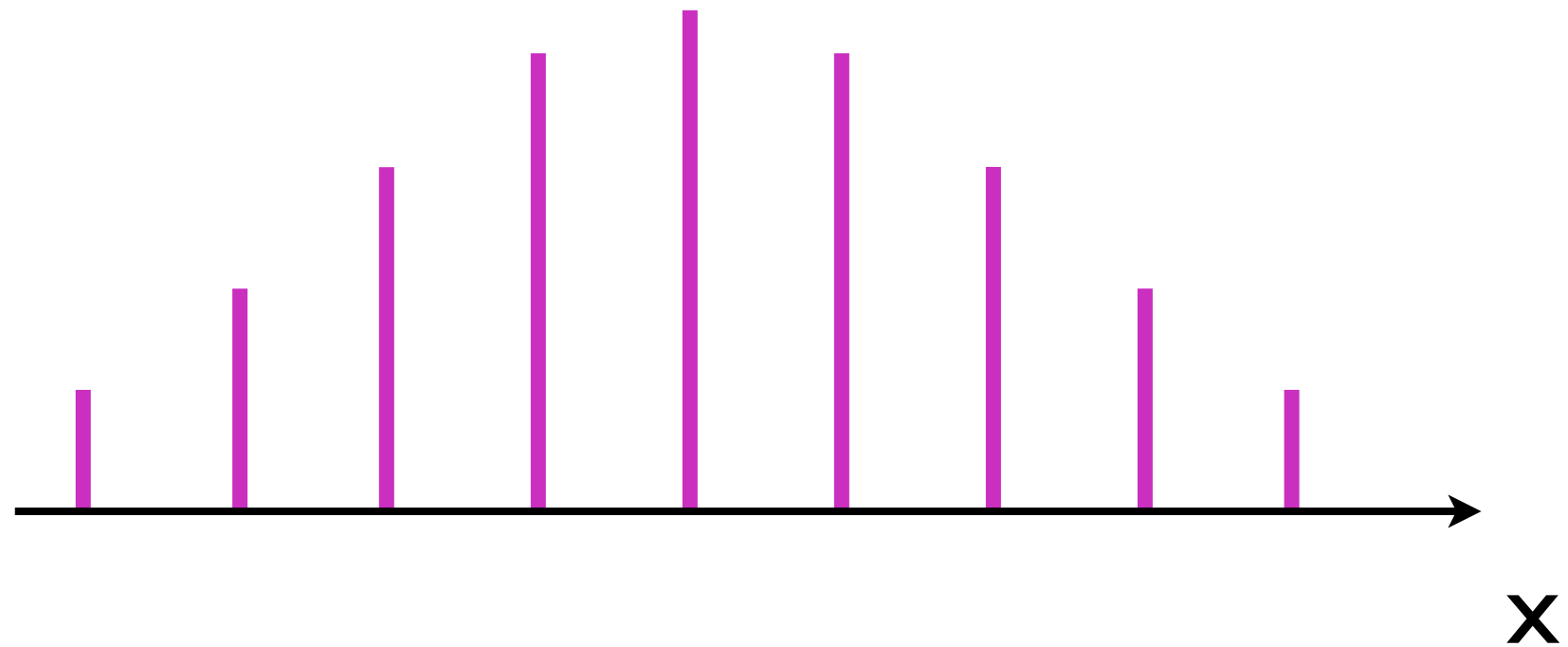


Gaussian Filter



$$G(x, \sigma) = A \exp \left\{ -\frac{1}{2} \left(\frac{x}{\sigma} \right)^2 \right\}$$

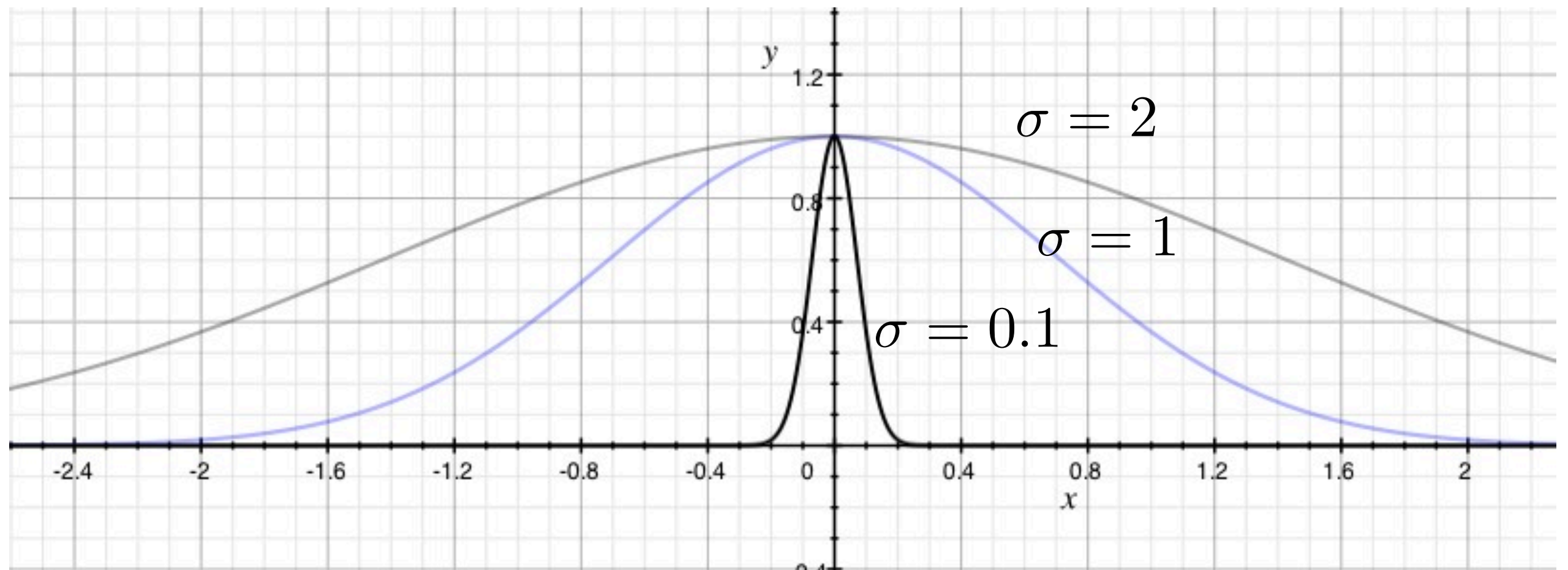
Gaussian Filter



$$G(x, \sigma) = A \exp \left\{ -\frac{1}{2} \left(\frac{x}{\sigma} \right)^2 \right\}$$

Gaussian Filter and Sigma

$$\exp \left\{ - \left(\frac{x}{\sigma} \right)^2 \right\}$$



For example, if we compute the coefficients of the 1D Gaussian filter for the interval $[-4, \dots, 0, \dots, 4]$ with $\sigma=0.5$, we obtain:

```
[0.0 0.0 0.00026 0.10645 0.78657 0.10645 0.00026 0.0 0.0]
```

While for $\sigma=1.5$ these coefficients are:

```
[0.00761 0.036075 0.10959 0.21345 0.26666  
0.21345 0.10959 0.03608 0.00761 ]
```

Note that these values were obtained by calling the `cv::getGaussianKernel` function with the appropriate σ value:

```
cv::Mat gauss= cv::getGaussianKernel(9,sigma,CV_32F);
```

getGaussianKernel

Returns Gaussian filter coefficients.

C++: Mat **getGaussianKernel**(int **ksize**, double **sigma**, int **ktype**=CV_64F)

Parameters:

- 1 **ksize** – Aperture size. It should be odd () and positive.
- 2 **sigma** – Gaussian standard deviation. If it is non-positive, it is computed from **ksize** as $\text{sigma} = 0.3 * ((\text{ksize} - 1) * 0.5 - 1) + 0.8$.
- 3 **ktype** – Type of filter coefficients. It can be CV_32f or CV_64F .

The function computes and returns the matrix of Gaussian filter coefficients:

$$G_i = \alpha * e^{-(i-(\text{ksize}-1)/2)^2 / (2*\text{sigma})^2},$$
$$i = 0..\text{ksize} - 1$$

Two of such generated kernels can be passed to [sepFilter2D\(\)](#) or to [createSeparableLinearFilter\(\)](#). Those functions automatically recognize smoothing kernels (a symmetrical kernel with sum of weights equal to 1) and handle them accordingly. You may also use the higher-level [GaussianBlur\(\)](#).

See also [sepFilter2D\(\)](#), [createSeparableLinearFilter\(\)](#), [getDerivKernels\(\)](#), [getStructuringElement\(\)](#), [GaussianBlur\(\)](#)

Blurring & Gaussian Smoothing

```
cv::Mat image= cv::imread("../images/boldt.jpg",0);
if (!image.data) return 0;

// Display the image
cv::namedWindow("Original Image");
cv::imshow("Original Image",image);

// Blur the image
cv::Mat result;
cv::GaussianBlur(image,result,cv::Size(5,5),1.5);

// Display the blurred image
cv::namedWindow("Gaussian filtered Image");
cv::imshow("Gaussian filtered Image",result);

// Get the gaussian kernel (1.5)
cv::Mat gauss= cv::getGaussianKernel(9,1.5,CV_32F);

// Display kernel values
std::cout << "GaussianKernel(9,15)=[";
for (int i=0; i<gauss.rows; i++) {
    std::cout << gauss.at<float>(i) << " ";
}
std::cout << "]" << std::endl;
```

Filter: Separable or Non-Separable

Separable: 2D filtering = two 1D filtering

Non-Separable: 2D filtering = 2D filtering, no other option!

Median filtering

In [probability theory](#) and [statistics](#), a **median** is described as the numerical value separating the higher half of a sample, a [population](#), or a [probability distribution](#), from the lower half.

To demonstrate, using a window size of three with one entry immediately preceding and following each entry, a median filter will be applied to the following simple 1D signal:

$x = [2 \ 80 \ 6 \ 3]$

So, the median filtered output signal y will be:

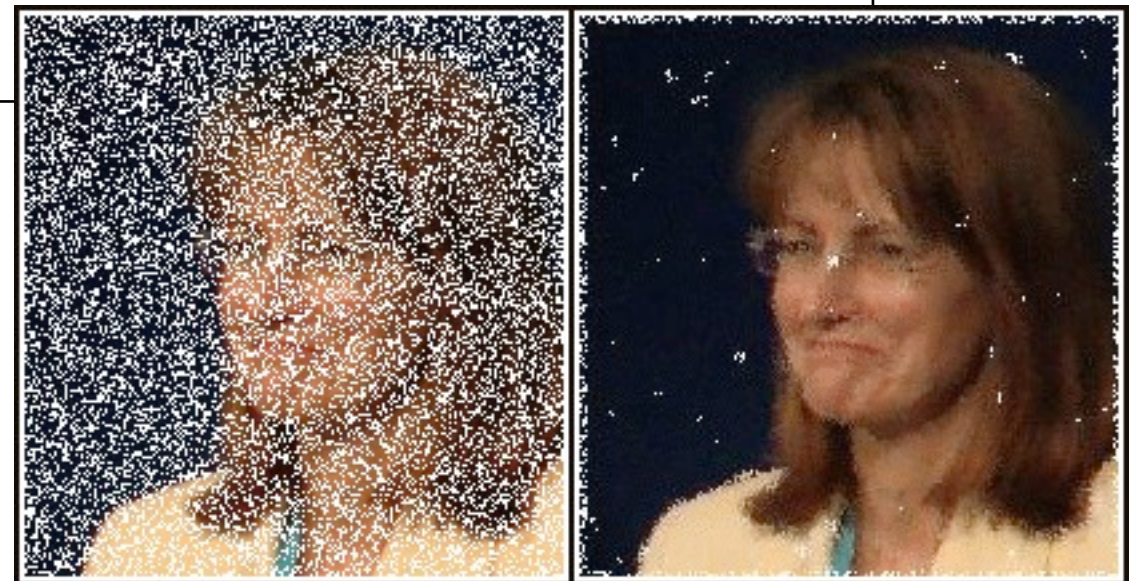
$y[1] = \text{Median}[2 \ 2 \ 80] = 2$

$y[2] = \text{Median}[2 \ 80 \ 6] = \text{Median}[2 \ 6 \ 80] = 6$

$y[3] = \text{Median}[80 \ 6 \ 3] = \text{Median}[3 \ 6 \ 80] = 6$

$y[4] = \text{Median}[6 \ 3 \ 3] = \text{Median}[3 \ 3 \ 6] = 3$

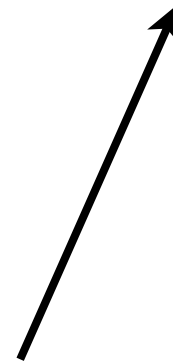
i.e. $y = [2 \ 6 \ 6 \ 3]$.



How to do it...

The call to the median filtering function is done in a way similar to the other filters:

```
cv::medianBlur(image, result, 5);
```



What is this value?

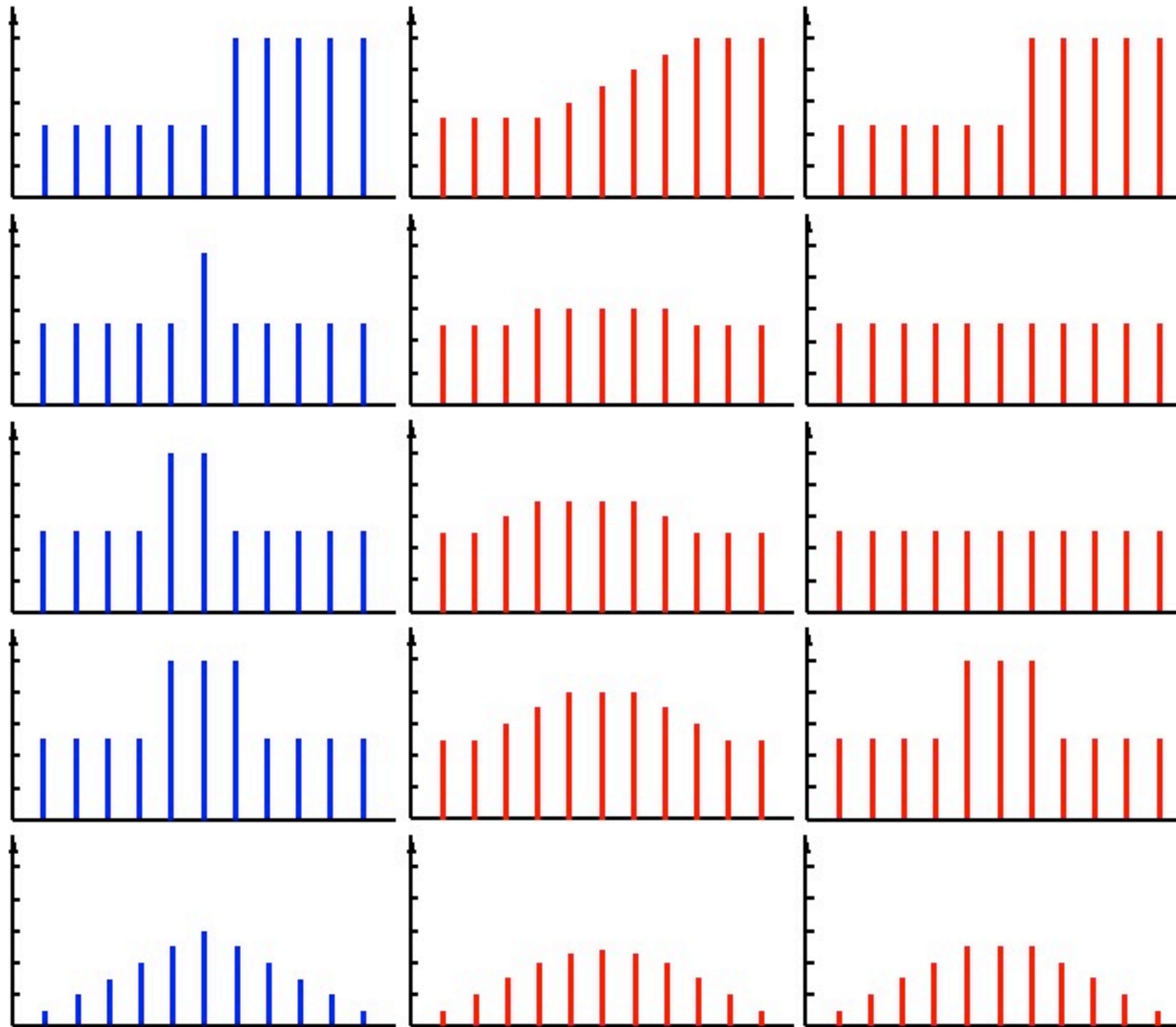
Pseudo-code for median filtering

```
For each pixel (x,y) in Image
{
    W := collect_values_in_the_window(s);
    W := sort (W);
    median := W(s/2);
    J(x,y) = median;
}
```


src

mean(5)

median(5)



http://fourier.eng.hmc.edu/e161/lectures/smooth_sharpen/node3.html

High pass filtering = edge finding = image enhancement

Computing a gradient: $G(x) = \frac{1}{2}(I(x+1) - I(x-1))$

$$G_x(x, y) = \frac{1}{2}(I(x+1, y) - I(x-1, y))$$

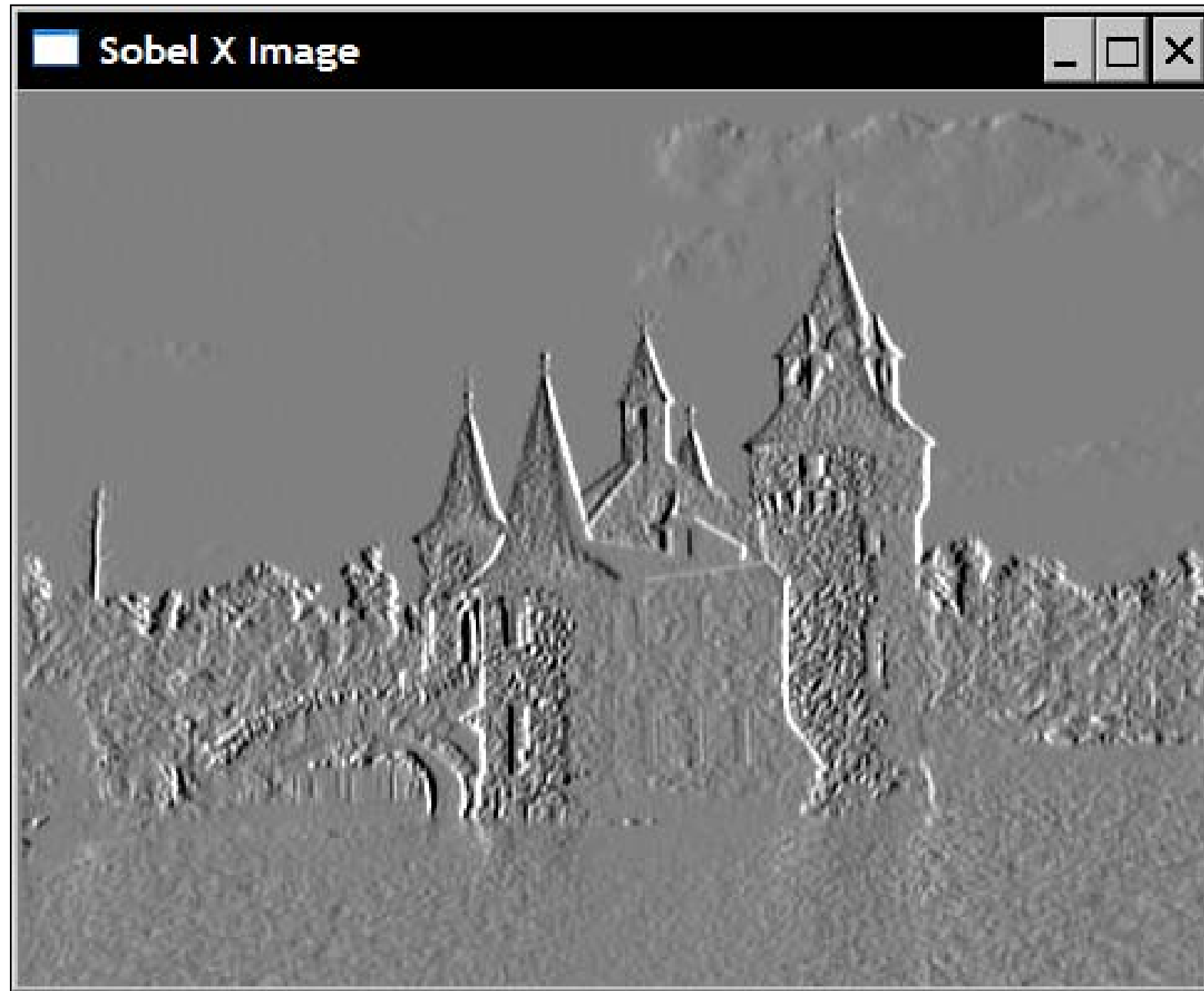
$$G_y(x, y) = \frac{1}{2}(I(x, y+1) - I(x, y-1))$$



conversion to magnitude/angle

$$\begin{aligned} M(x, y) &= ||[G_x, G_y]|| \\ D(x, y) &= \angle[G_x, G_y] \end{aligned}$$

The result of the horizontal Sobel operator is as follows:



```
cv::Sobel(image, sobelX, CV_8U, 1, 0, 3, 0.4, 128);
```

Sobel operators: a digital approximation of the gradient.

-1	0	1
-2	0	2
-1	0	1

$$\textit{grad} (I) = \left[\frac{\partial I}{\partial x}, \frac{\partial I}{\partial y} \right]^T$$

-1	-2	-1
0	0	0
1	2	1

```
cv::Sobel(image, // input
          sobel, // output
          image_depth, // image type
          xorder,yorder, // kernel specification
          kernel_size, // size of the square kernel
          alpha, beta); // scale and offset
```

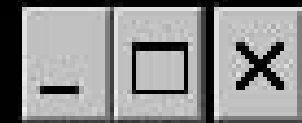
C++: void **Sobel** (InputArray src, OutputArray dst, int ddepth, int xorder, int yorder, int ksize=3, double scale=1, double delta=0, int borderType=BORDER_DEFAULT)

```
// Compute norm of Sobel
cv::Sobel(image,sobelX,CV_16S,1,0);
cv::Sobel(image,sobelY,CV_16S,0,1);
cv::Mat sobel;
//compute the L1 norm
sobel= abs(sobelX)+abs(sobelY);
```

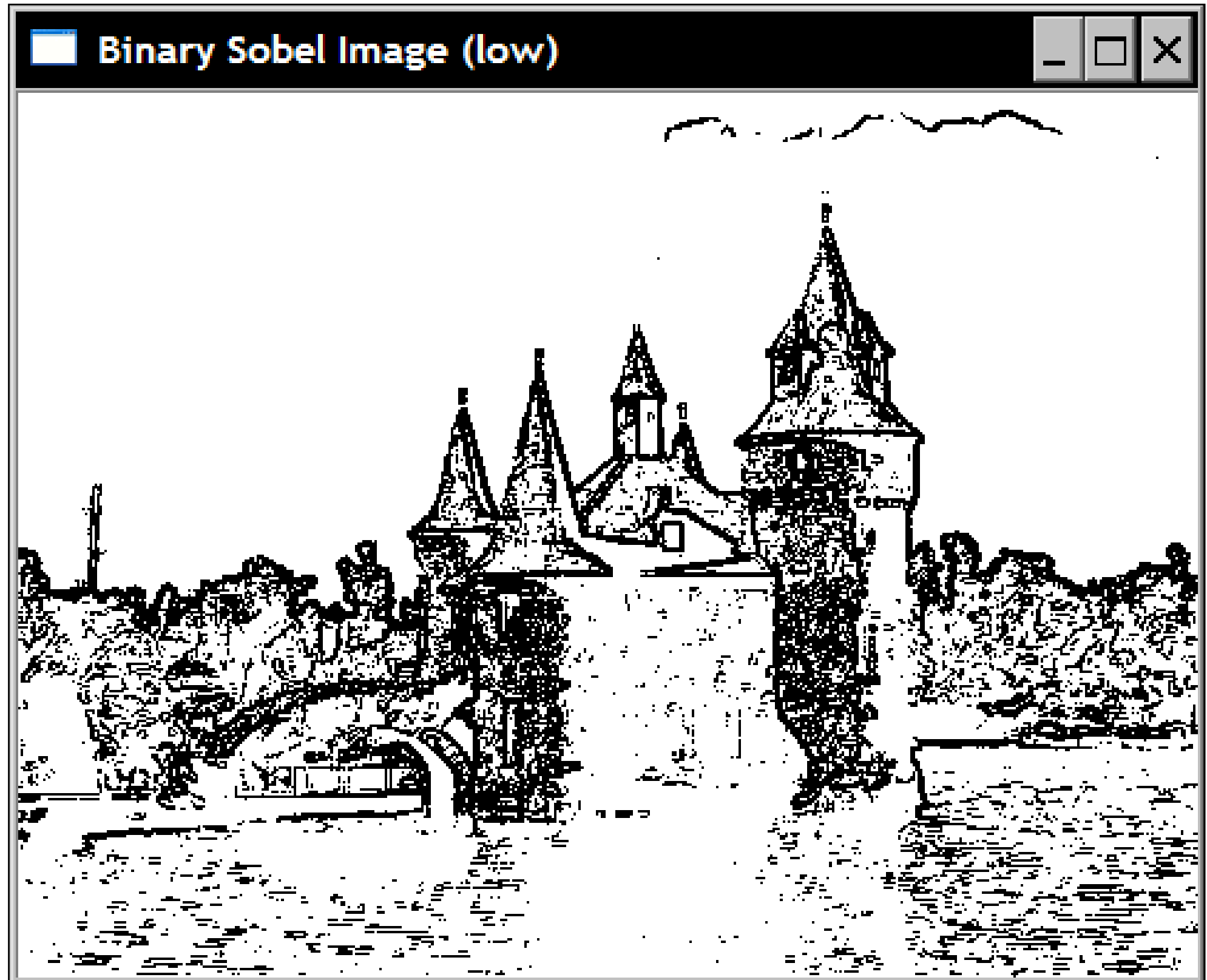
```
// Find Sobel max value
double sobmin, sobmax;
cv::minMaxLoc(sobel,&sobmin,&sobmax);
// Conversion to 8-bit image
// sobelImage = -alpha*sobel + 255
cv::Mat sobelImage;
sobel.convertTo(sobelImage,CV_8U,-255./sobmax,255);
```



Sobel Image



```
cv::threshold(sobelImage, sobelThresholded,  
              threshold, 255, cv::THRESH_BINARY);
```



```
// Apply threshold to Sobel norm (low threshold value)
cv::Mat sobelThresholded, otsuThresholded;
cv::threshold(sobelImage, sobelThresholded, 225, 255, cv::THRESH_BINARY);

float otsuTh = cv::threshold(sobelImage, otsuThresholded, 225, 255, cv::THRESH_OTSU);
std::cerr << "Otsu_TH = " << otsuTh << std::endl;

// Display the image
cv::namedWindow("Binary Sobel Image (low)");
cv::imshow("Binary Sobel Image (low)", sobelThresholded);

cv::namedWindow("Otsu Output");
cv::imshow("Otsu Output", otsuThresholded);
```

Otsu_TH = 211

