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METHOD 1: SHOOTING METHOD
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Boundary conditions: y(0) = 1, y(1) = 2

Optimal initial slope: y'(0) = 0.024000

Achieved final value: y(1) = 2.000001

Error in boundary condition: 0.00000095
 Solution points:
Solution points:

x = 0.0, y = 1.000000, y' = 0.024000

x = 0.1, y = 1.016634, y' = 0.302355

x = 0.2, y = 1.059211, y' = 0.544550

x = 0.3, y = 1.124314, y' = 0.754099

x = 0.4, y = 1.209025, y' = 0.934403

x = 0.5, y = 1.310524, y' = 1.089549

x = 0.6, y = 1.426233, y' = 1.223938

x = 0.7, y = 1.554456, y' = 1.340453

x = 0.8, y = 1.693765, y' = 1.441832

x = 0.9, y = 1.842716, y' = 1.531383

x = 1.0, y = 2.000001, y' = 1.612523

METHOD 2: FINITE DIFFERENCE METHOD

Grid points: 11
 Grid points: 11
 Step size: h = 0.1
  Boundary conditions: y(0) = 1, y(1) = 2
 Solution points:
Solution points:

x = 0.0, y = 1.000000

x = 0.1, y = 0.992158

x = 0.2, y = 0.994922

x = 0.3, y = 1.010846

x = 0.4, y = 1.043396

x = 0.5, y = 1.097230

x = 0.6, y = 1.178600

x = 0.7, y = 1.295925

x = 0.8, y = 1.466607

x = 0.9, y = 1.688187

x = 1.0, y = 2.000000
 x = 1.0, y = 2.000000
METHOD 3: VARIATIONAL APPROACH (GALERKIN METHOD)
Number of basis functions: 5
 Coefficients for higher-order terms: [-0.97616757 \ 0.51691436 \ -0.1677539 \ 0.01369669]
Boundary conditions satisfied: y(0) = 1.000000, \ y(1) = 2.000000
 Solution points:
x = 0.0, y = 1.0000000

x = 0.1, y = 1.016647

x = 0.2, y = 1.059298

x = 0.3, y = 1.124478

x = 0.4, y = 1.209112

x = 0.5, y = 1.310516
      = 0.6, y = 1.426372
      = 0.7, y = 1.554716
= 0.8, y = 1.693922
      = 0.9, y = 1.842684
              1.0,
                              y = 2.000000
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