Internal Assessment: The Impact of the Sphere's Radius on the Sphere's Angular Velocity

IB Physics II Period 6, Dr. Petach

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1 Exploration

1.1 Research

The aim of the experiment is to investigate the relationship between radius and angular velocity for the linear motion of a sphere unraveling from a string at a fixed height. This will be done by changing the radius of the sphere that is being dropped through the use of various sizes balls that are unraveled from the string and then measuring the linear velocity of the falling ball using a photogate. The purpose of the string is to cause the ball to rotate while falling, due to the nature of its unraveling motion.

Prior to the experiment, I derived a relationship between the radius and the angular velocity of the rotational motion of the falling ball by using the law of conservation of energy. Section 2.1 will more specifically detail the derivation. The derived relationship predicted that radius and angular velocity will follow an inverse relationship. The experiment itself was to test whether Newtonian physics upheld this inverse relationship with tangible experimentation.

1.2 Personal Engagement

I have always been a fan of yo-yo's. One day while playing with a yo-yo, I noticed how quickly the yo-yo was spinning, which was made especially conspicuous by the bright design on the side of the yo-yo. I became curious, did the size of the yo-yo affect how quickly it spun? I took a smaller yo-yo and noticed that it seemed to spin more quickly. However, this was just a casual observation, not performed under standard experimentation conditions. Interested in seeing if this was truly the case, I came up with my research question: does the radius of a sphere affect its angular velocity?

1.3 Variables

The independent variable is the radius of the sphere. The dependent variable is the angular velocity of the ball as it passes through the photogate. The controlled variables include the height of the initial position of the ball that is attached to the clamp, material of the string, the photogate, and the properties of the surrounding environment.

1.4 Apparatus

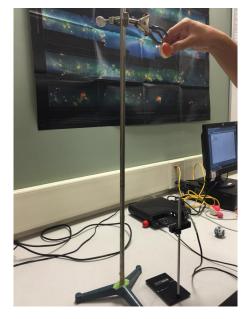
- Photogate
- Four different sizes balls that are relatively uniform spheres
- \bullet String
- DataWorks software that reads data from the photogate

- Ring stand with clamp
- Meter stick

1.5 Procedure

- 1. Attach a clamp to a ringstand
- 2. Place a photogate toward the bottom of the ringstand so that the ball will drop through it.
- 3. Connect the photogate to the DataWorks software, such that it reads the linear velocity of the falling ball
- 4. Measure the height difference between the placement of the clamp and the photogate along the ring stand using a meter stick
- 5. Pick a ball, measure it radius using a meter stick
- 6. Tie one end of the string to a clamp attached to a ring stand, and the other end around the ball
- 7. Carefully wrap the string around the ball until the ball is level with the clamp
- 8. Drop the ball so that it falls through the photogate
- 9. Record the linear velocity that is measured by the photogate
- 10. Repeat steps 6 to 9 for six trials
- 11. Repeat steps 5 through 10 for the four different balls

1.6 Experiment Setup



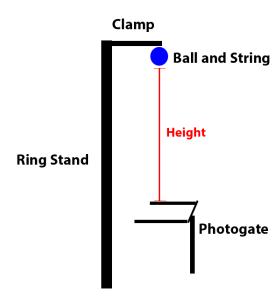


Figure 1: Picture of the experiment setup

Figure 2: Diagram of the experiment setup

1.7 Data Collection

Trial	Radius (cm)	Linear Velocity (m/s)
1	2.34 ± 0.05	1.86
2	2.34 ± 0.05	1.81
3	2.34 ± 0.05	3.10
4	2.34 ± 0.05	2.50
5	2.34 ± 0.05	2.87
6	2.34 ± 0.05	2.20

Table 1: Data for six trials with ball radius of 2.34 cm and height of 50.00 ± 0.05 cm.

Trial	Radius (cm)	Linear Velocity (m/s)
1	1.90 ± 0.05	2.12
2	1.90 ± 0.05	2.38
3	1.90 ± 0.05	2.98
4	1.90 ± 0.05	2.23
5	1.90 ± 0.05	2.35
6	1.90 ± 0.05	2.23

Table 2: Data for six trials with ball radius of 1.90 cm and height of 50.00 ± 0.05 cm.

Trial	Radius (cm)	Linear Velocity (m/s)
1	1.69 ± 0.05	3.32
2	1.69 ± 0.05	3.18
3	1.69 ± 0.05	2.22
4	1.69 ± 0.05	3.91
5	1.69 ± 0.05	2.85
6	1.69 ± 0.05	3.63

Table 3: Data for six trials with ball radius of 1.69 cm and height of 50.00 ± 0.05 cm.

Trial	Radius (cm)	Linear Velocity (m/s)
1	1.40 ± 0.05	2.91
2	1.40 ± 0.05	3.62
3	1.40 ± 0.05	3.62
4	1.40 ± 0.05	2.31
5	1.40 ± 0.05	3.67
6	1.40 ± 0.05	3.41

Table 4: Data for six trials with ball radius of 1.40 cm and height of 50.00 ± 0.05 cm.

2 Analysis

2.1 Deriving the relationship between radius and angular velocity

A relationship can be found between radius and angular velocity by using the law of conservation of energy. Effects of thermal energy (friction) from the string are negligible.

$$GPE = KE_T + KE_R$$

$$mgh = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2$$

$$mgh = \frac{1}{2}m(R\omega)^2 + \frac{1}{2}\left(\frac{2}{5}mR^2\right)\omega^2$$

$$mgh = \frac{1}{2}mR^2\omega^2 + \frac{1}{5}mR^2\omega^2$$

The masses can be eliminated:

$$gh = \frac{7}{10}R^2\omega^2$$

$$\omega^2 = \frac{10gh}{7R^2}$$

$$\omega = \sqrt{\frac{10gh}{7R^2}}$$

$$\omega = \boxed{\frac{1}{R} \cdot \sqrt{\frac{10gh}{7}}}$$

2.2 Calculating angular velocity

Using Equation 1, derived above, the angular velocity can be calculated for each ball size. For radius 2.34 cm:

$$\omega = \frac{1}{0.234}$$

2.3 Averaging the six trials for each ball size and finding uncertainty

A sample calculation will be done for the set of data around the ball with radius 2.34 cm.

Uncertainty for linear velocity can be calculated by dividing the linear velocity range by 2:

$$\frac{3.10 - 1.81}{2} = 0.65$$

Now to find the average:

$$\frac{1.86 + 1.81 + 3.10 + 2.50 + 2.87 + 2.20}{6} = 2.39 \frac{m}{s}$$

Radius (cm)	Linear Velocity (m/s)
2.34 ± 0.05	2.39 ± 0.65

Table 5: Data for six trials with ball radius of 1.40 cm and height of 50.00 ± 0.05 cm.

2.4 Analyzing experiment evidence for radius vs angular velocity

3 Evaluation