

Lab 1: Airplane Lab

IB Physics II Period 6, Petach

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1 Design

1.1 Research

The aim of the experiment is to investigate the relationship between period and height for the circular motion of an airplane moving in a circle at equilibrium. This will be done by changing the length of the string that the airplane is attached to and then measuring the period and the height of the airplane's flight with a stopwatch and a laser, and a meter stick, respectively.

Prior to the experiment, I derived a relationship between the period and the height of the circular motion of an airplane's flight by using the force analysis of the airplane, the definition of a period, and the radius of the flight path. Section 2.2.3 will more specifically detail the derivation. The derived relationship predicted that period and height will follow a square root relationship. The experiment itself was to test if Newtonian physics upheld this square root relationship with tangible experimentation.

1.2 Variables

The independent variable is the length of the string that the airplane is attached to. The dependent variables are the period and height of the circular motion that the airplane makes. The controlled variables include the mass of the airplane, material of the string, the timer, the laser, and the properties of the surrounding environment.

1.3 Apparatus

- Hook
- Model airplane
- String
- Stopwatch (on a phone)
- Meter stick
- Laser
- Ring stand with clamp

1.4 Procedure

1. Attach the model airplane to a 100cm string and connect it to a hook attached to the ceiling.
2. Turn the airplane on, and wait for the motion to reach equilibrium.
3. Clamp a laser onto a ring stand and make the laser parallel to the surface that the ring stand is on.
4. Raise or lower the laser (without changing its angle) so its light hits the moving airplane anywhere in its circular orbit.
5. Measure the height of the airplane with respect to the ceiling by measuring the placement of the laser with respect to the ceiling with a meter stick.
6. Use the timer to measure the amount of seconds it takes the airplane to complete three revolutions.
7. Repeat steps 5-6 five times for five different trials.
8. Repeat the experiment (for one trial) for strings of lengths: 90cm, 80cm, 70cm, and 60cm.

1.5 Diagram

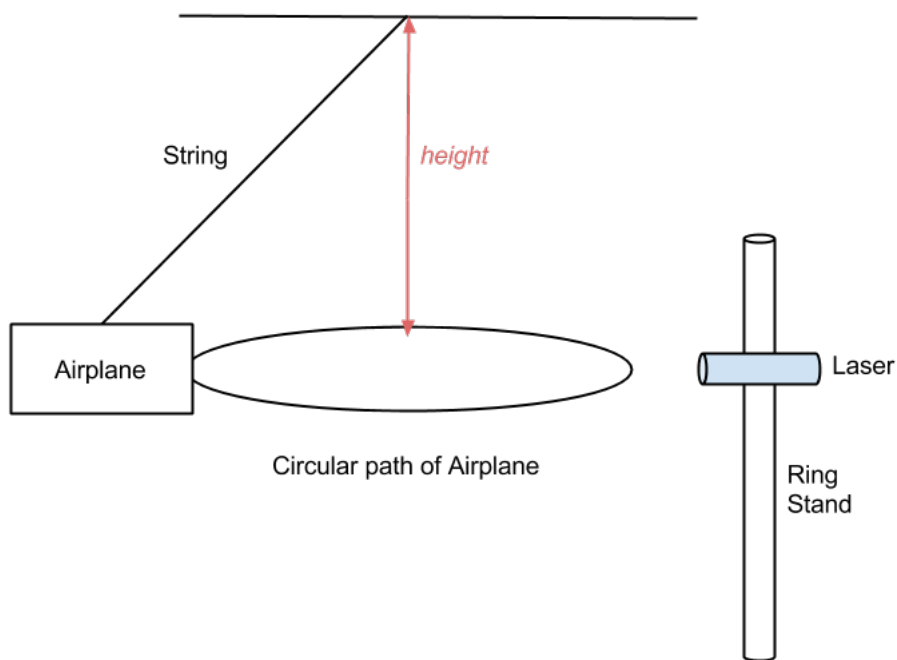


Figure 1: Diagram of apparatus setup

2 Data

2.1 Data Collection

String length (cm)	Trial	Height (cm)	Time per 3 revs(s)
100 ± 2	1	71.30	4.89
100 ± 2	2	70.11	4.90
100 ± 2	3	69.45	5.03
100 ± 2	4	67.50	5.03
100 ± 2	5	66.98	5.01

Table 1: Data for a string length of 100 ± 2 cm. The purpose of five trials was to determine uncertainty.

String length (cm)	Height (cm)	Time per 3 revs(s)
90 ± 2	57.95	4.58
80 ± 2	46.85	4.51
70 ± 2	37.92	3.95
60 ± 2	42.24	3.85

Table 2: Data for four different string lengths

2.2 Data Processing

2.2.1 Averaging the five trials for a string length of 100 ± 2 cm

The average heights over the five trials for a string length of 100 ± 2 cm is:

$$\frac{71.30 + 70.11 + 69.45 + 67.50 + 66.98}{5} = 69 \pm 2cm$$

The uncertainty is calculated by dividing the range by 2. The average time per 3 revolutions over the five trials for a string length of 100 ± 2 cm is calculated in the same way:

$$\frac{4.89 + 4.90 + 5.03 + 5.03 + 5.01}{5} = 4.97 \pm 0.07s$$

The uncertainties that were just calculated will be applied to the rest of the data, as the purpose of performing five trials was to determine the uncertainty for height and time per 3 revolutions.

2.2.2 Calculating Period

The period of the plane's circular flight, is the seconds per 1 revolution. Since the time per 3 revolutions is a measured quantity, the period can be calculated by dividing that value by 3. For example, the period for string length 100 ± 2 cm is:

$$\frac{4.97 \pm 0.07}{3} = 1.66 \pm 0.07s$$

After processing the data in sections 2.2.1 and 2.2.2, Tables 1 and 2 can be consolidated into one table, append uncertainty for height and time per 3 revolutions columns, as well as include a new column for period. This will be presented in Table 3.

String length (cm)	Height (cm)	Time per 3 revs(s)	Period (s)
100 ± 2	69 ± 2	4.97 ± 0.07	1.66 ± 0.07
90 ± 2	58 ± 2	4.58 ± 0.07	1.53 ± 0.07
80 ± 2	47 ± 2	4.51 ± 0.07	1.50 ± 0.07
70 ± 2	38 ± 2	3.95 ± 0.07	1.32 ± 0.07
60 ± 2	42 ± 2	3.85 ± 0.07	1.28 ± 0.07

Table 3: Consolidated table with 5 string lengths, period, and uncertainty

2.2.3 Deriving a relationship between period and height

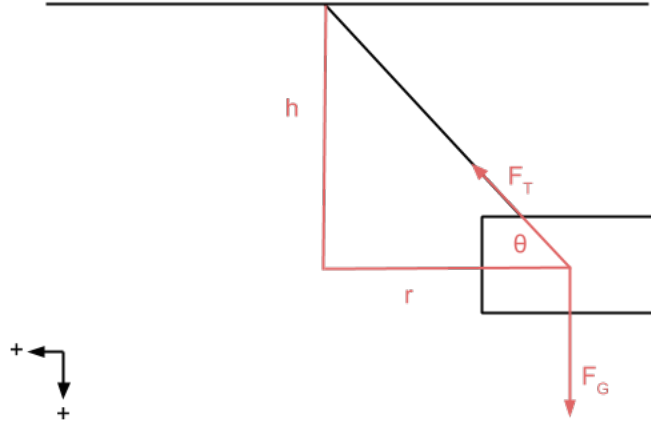


Figure 2: Free Body Diagram of Airplane

As mentioned in Section 1.1, the purpose of the investigation was to test if experimental data supported a derived relationship between period and height. This derivation is as follows:

$$\begin{aligned}\Sigma F_y = 0 &= F_G - F_{Ty} = mg - F_T \sin \theta \\ F_T &= \frac{mg}{\sin \theta}\end{aligned}\tag{1}$$

$$\Sigma F_x = ma = F_{Tx} = F_T \cos \theta = F_c = \frac{mv^2}{r}$$

By the definition of period, $T = \frac{2\pi r}{v}$. Therefore $v = \frac{2\pi r}{T}$, which can be substituted in:

$$F_T \cos \theta = \frac{m}{r} * \left(\frac{2\pi r}{T} \right)^2$$

From Figure 2, we can see $r = \frac{h}{\tan \theta}$. Substituting r, and F_T from Equation 1:

$$\begin{aligned}mg \frac{\cos \theta}{\sin \theta} &= \frac{m}{\frac{h}{\tan \theta}} * \left(\frac{2\pi h}{T \tan \theta} \right)^2 \\ mg \cot \theta &= \frac{m \tan \theta}{h} * \frac{4\pi^2 h^2}{T^2 \tan^2 \theta} \\ g \cot \theta &= \frac{4\pi^2 h}{T^2 \tan \theta}\end{aligned}$$

$$T^2 = \frac{4\pi^2 h}{g}$$

$$T = 2\pi \sqrt{\frac{h}{g}} \quad (2)$$

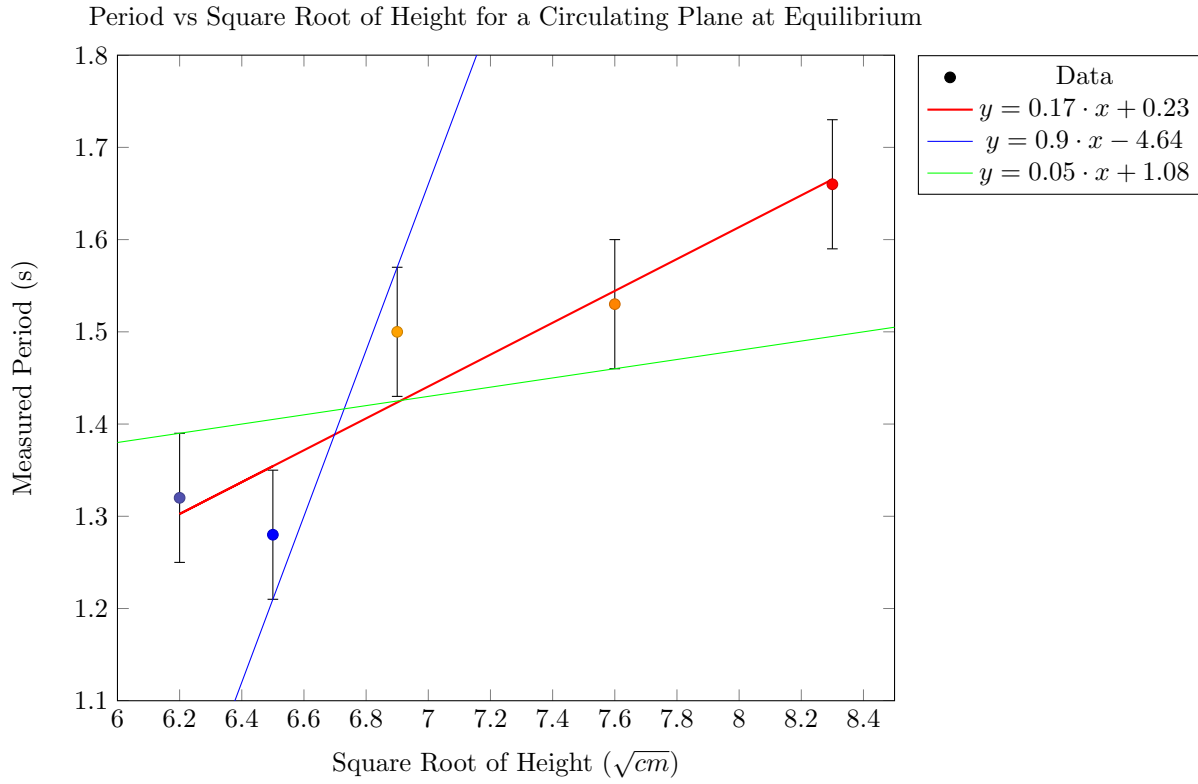


Figure 3: Graph of T vs \sqrt{h} with line of best fit, maximum slope, and minimum sloped lines.

3 Conclusion