

Double Angle Formulae

$$1. \sin(2A) = 2 \sin(A) \cos(A)$$

$$= \frac{2 \tan(A)}{1 + \tan^2(A)}$$

$$2. \cos(2A) = \cos^2(A) - \sin^2(A)$$

$$= 2 \cos^2(A) - 1$$

$$= 1 - 2 \sin^2(A)$$

$$3. \tan(2A) = \frac{2 \tan(A)}{1 - \tan^2(A)}$$

$$4. \cot(2A) = \frac{\cot^2(A) - 1}{2 \cot(A)}$$

Half Angle Formulae

$$5. \sin(A) = 2 \sin\left(\frac{A}{2}\right) \cos\left(\frac{A}{2}\right)$$

$$= \frac{2 \tan\left(\frac{A}{2}\right)}{1 + \tan^2\left(\frac{A}{2}\right)}$$

$$6. \cos(A) = \cos^2\left(\frac{A}{2}\right) - \sin^2\left(\frac{A}{2}\right)$$

$$= 1 - 2 \sin^2\left(\frac{A}{2}\right)$$

$$= 2 \cos^2\left(\frac{A}{2}\right) - 1$$

$$= \frac{1 - \tan^2\left(\frac{A}{2}\right)}{1 + \tan^2\left(\frac{A}{2}\right)}$$

$$7. \tan(A) = \frac{2 \tan\left(\frac{A}{2}\right)}{1 - \tan^2\left(\frac{A}{2}\right)}$$

$$8. \sin\left(\frac{A}{2}\right) = \sqrt{\frac{1 - \cos(A)}{2}}$$

$$9. \cos\left(\frac{A}{2}\right) = \sqrt{\frac{1 + \cos(A)}{2}}$$

$$10. \quad \tan\left(\frac{A}{2}\right) = \sqrt{\frac{1-\cos(A)}{1+\cos(A)}}$$

Triple Angle Formula

$$11. \quad \sin(3A) = 3 \sin(A) - 4 \sin^3(A)$$

$$12. \quad \cos(3A) = 4 \cos^3(A) - 3 \cos(A)$$

$$13. \quad \tan(3A) = \frac{3 \tan(A) - \tan^3(A)}{1 - 3 \tan^2(A)}$$