

# Lecture 6: Complexity

CS 62 - Spring 2016  
Michael J. Bannister

## Lab This Week

- Timing ArrayList operations
  - Encourage working in pairs
  - Stopwatch class: start(), stop(), getTime(), reset()
- Java has Just-In-Time compiler
  - Must “warm-up” before you get accurate timing
  - What can mess up timing?
- Uses Vector from Java libraries because can change way it increases in size.

## Programming Assignment This Week

- Weak AI/Natural Language Processing:
  - Generate text by building frequency lists based on pairs of words. ArrayList of Associations of String (words) and Integer (count of that word).

## Complexity

- Count the number of elementary operations used to perform a task (i.e., a method).
- Elementary Operations:
  - Read/Write
  - Arithmetic

## Adding to ArrayList

- Suppose  $n$  elements in ArrayList and we add 1 element.
- If space:
  - Add to end is a constant number of ops
  - Add to beginning is  $\sim n$  copy ops
- If not space,
  - What is cost of ensureCapacity?
  - $\sim n$  copy ops because  $n$  elements in array

## Multiple Adds

- What if only increase in size by 1 each time?
  - Adding  $n$  elements one at a time to end
    - Total cost is  $1+2+3+\dots+(n-1) = n(n-1)/2$  copy ops
- What if double in size each time?
  - Suppose add  $n$  new elements to end
    - Total cost is  $1+2+4+\dots+n/2 = n-1$  copy operations

## O-Notation

- Definition: We say that  $g(n)$  is  $O(f(n))$  if there exist two constants  $C$  and  $k$  such that  $|g(n)| \leq C |f(n)|$  for all  $n > k$ .
- Used to measure time and space complexity of algorithms on data structures of size  $n$ .
- Ignores constants and lower order terms

## ArrayList Ops

- Worst case
  - $O(1)$ : size, isEmpty, get, set
  - $O(n)$ : remove, add
- Amortized:  $O(1)$  for all operations