

MAD 3105 Assignment 02
Closure of Relations

NAME: _____
DUE: Thursday, January 26th (11:59pm EST)

Directions: See Canvas.

Complete all work individually without outside help. **50 points total.**

(1) (5 points each)

If possible, give an example of a *nonempty relation* R on the set $A = \{0,1\}$ that satisfies the following. Give the *Matrix representation*.

(a) R is reflexive and symmetric. Explain why you chose this matrix.

(b) R is irreflexive, but R^2 (i.e. $R \circ R$) is reflexive. Explain why you chose this matrix.

(c) R is asymmetric and irreflexive. Explain why you chose this matrix.

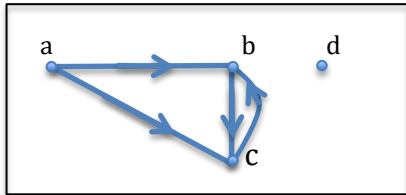
(2) (5 points)

Find the transitive closure of the given relation, R , on $\{a, b, c, d, e\}$, using either algorithm presented in Section 9.4 of the Rosen textbook (i.e., using a series of matrices). Please state what method you are using and label your matrices. Do not use a digraph.

$$R = \{(e, d), (d, b), (c, a), (b, d), (a, c)\}$$

(3) (5 points each)

Given the directed graph in the box below, draw the directed graph of



(a) The reflexive closure of the relation.

(b) The symmetric closure of the relation.

(c) The transitive closure.

(4) (5 point each)

Let R be represented by the matrix $\mathbf{M}_R = \begin{bmatrix} 0 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$

(a) Give the *matrix* that represents the *reflexive closure* of R , $r(R)$:

(b) Give the *matrix* that represents the *symmetric closure* of R , $s(R)$:

(5)(5 points)

Prove directly that if the relation R is symmetric, then its transitive closure, $t(R) = R^*$, is also symmetric.