

CS312 Notes

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1 Theory Of Computation Introduction

The 3 componenets of problem solving

1. Unknowns
2. Data
3. Conditions

To solve a problem we need to find a way of determining the unknowns from given data such that conditions of the problem are satisfied.

The traditional areas of the theory of computation (TOC)

- Automata
 - Provide problem solving devices
- Computability
 - Provide framework that can characterize devices by their computing power

- Complexity
 - Provide framework to classify problems according to time/space complexity of the tool used to solve them

1.1 Automata (Automaton)

- Abstraction of computing devices
- How much memory can be used?
- What operations can be performed?

1.2 Computability

- Study different computing models and identify the most powerful ones
- Range of problems
- Problems can be undecidable or uncomputable
 - The halting problem

1.3 Complexity

- Computing problems range from easy to hard; sorting is easier than scheduling
- Question
 - What makes some problems computationally hard or others easy?

1.4 Problem Abstraction

Data

- Abstracted as a word in a given alphabet

Conditions

- Abstracted as a set of words called a language

Unknowns

- A boolean variable: true if a word is in the language or false otherwise

1.4.1 Abstraction of Data

- Σ : alphabet, a finite, nonempty set of symbols
- Σ^* : all words of a finite length built up using Σ
- Rules: (1) the empty word (ϵ) is in Σ^* ; (2) if $w \in \Sigma^*$ and $a \in \Sigma$, then $aw \in \Sigma^*$, and (3) nothing else is in Σ^*

Example: If $\Sigma = \{0,1\}$, then $\Sigma^* = \{\epsilon, 0, 1, 00, 01, 10, 11, 000, 001, 010, 011, \dots\}$.

1. Valid C

```
int my_func() { return 1; };

int main() {
    int var = my_func(1,2,3,4,5,6,7);
    for (;;) {}
    // You cannot just simply change the syntax of a for loop
    for(;) {}
}
```

2. Invalid C++

```
int my_func() { return 1; };

int main() {
    int var = my_func(1,2,3,4,5,6,7);
    for (;;) {}
    // You cannot just simply change the syntax of a for loop
    for(;) {}
}
```

1.4.2 $\neg \wedge \vee$