Two One

October 18, 2024

Contents

1	Obj	1
2	Definition	1
3	Definition Minors and Cofactors 3.1 Minors	2 2
4	Definition of Determinant 4.1 Compute	2 2
5	Triangle Determinant	2
6	Trick	3
1	Ohi	

Obj

Use cofactor expansion on any row or col to compute the determinant of a square matrix Use diagonals to copute the determinants of 2x2 and 3x3matricies

2 Definition

ad-bc

- 1. 0
- 2. 50

3 Definition Minors and Cofactors

If A is a square matrix, then the minor M_{ij} of the entry a_{ij} is the determinant of the matrix obtained by deleting the ith row and the jth column of ja. The cofactor C_{ij} of the entry a_{ij} is $C_{ij} = (-1)^{i+j} M_{ij}$.

Find the minors and the cofactors for $|A| = \begin{bmatrix} 1 & 2 & 4 \\ 3 & 1 & 5 \\ 4 & 6 & 10 \end{bmatrix}$

3.1 Minors

$$\begin{split} &M_{11} = \begin{bmatrix} 1 & 5 \\ 6 & 10 \end{bmatrix} = -20, \, C \to (-1)^{1+1} (-20) = -20 \,\, M_{12} = \begin{bmatrix} 3 & 5 \\ 4 & 10 \end{bmatrix} = 10, \, C \to \\ &(-1)^{1+2} (10) = -10 \,\, M_{13} = \begin{bmatrix} 3 & 1 \\ 4 & 6 \end{bmatrix} = 14, \, C \to (-1)^{1+3} (14) = 14 \,\, M_{21} = \begin{bmatrix} 2 & 4 \\ 6 & 10 \end{bmatrix} \\ &= -4, \, C \to () \,\, (-2)^{2+1} (-4) = 4 \,\, M_{22} = \begin{bmatrix} 1 & 4 \\ 4 & 10 \end{bmatrix} = -6, \, -6 \,\, M_{23} = \begin{bmatrix} 1 & 2 \\ 4 & 6 \end{bmatrix} = -2, \, 2 \\ &M_{31} = \begin{bmatrix} 2 & 4 \\ 1 & 5 \end{bmatrix} = 6, \, 6 \,\, M_{32} = \begin{bmatrix} 1 & 4 \\ 3 & 5 \end{bmatrix} = -7, \, 7 \,\, M_{33} = \begin{bmatrix} 1 & 2 \\ 3 & 1 \end{bmatrix} = -5, \, -5 \end{split}$$

4 Definition of Determinant

For A a square matrix of order $n \geq 2$, the determinant of A is the sum of the entries in the first row of A (or any row or column of A), multiplied by their respective cofactors.

$$Det(A) = |A| = \sum_{j=1}^{n} a_{ij} C_{ij} = a_{11} C_{11} + a_{12} C_{12} + \dots + a_{1n} C_{1n}.$$

4.1 Compute

$$|A| = \begin{bmatrix} 1 & 2 & 4 \\ 3 & 1 & 5 \\ 4 & 6 & 10 \end{bmatrix}$$

Find the column or row with the most zero entries

Pick the second row $\Rightarrow |A| = a_{21}C_{21} + a_{22}C_{22} + a_{23}C_{23} \ 3*4 + 1*-6 + 5*2 = 16$

5 Triangle Determinant

Product of main diagonal entries

6 Trick