

3. Show that $\text{cov}(a+bx, a+bx) = b^2 \text{cov}(x, x)$
and in particular $\text{cov}(x, x) = s^2$

• ~~$\text{cov}(a+bx, a+bx) = b^2 \text{cov}(x, x)$~~

• It's the same thing as the last question, except instead of one b we get two b 's, so look at Q^2 for proofs

so we get $b^2 \text{cov}(x, x)$

and $\text{cov}(x, x) = (x_i - M(x))(x_i - M(x))$ which
is $(x_i - M(x))^2$ which equals s^2 which
is $\frac{1}{N} \sum_{i=1}^N (x_i - M(x))^2$

4. Yes, the median of the transformed variable equals non-decreasing transformation of the median. This is because ~~$x > x'$~~
 $x > x'$ and $g(x) \geq g(x')$ retains the same properties.

• Range is not preserved because x' and x are different

• IQR is preserved because it is the difference of the transformed, not the total length

5. No, because $g(x)$ and $m(x)$ can mean fundamentally different things