

University of Toronto

Duration: 2 hours 30 minutes  
Examiner: Kuei (Jack) Sun

Please fill your student number, last and first name below and then read the instructions carefully.

Student Number: \_\_\_\_\_

Last Name: \_\_\_\_\_

First Name: \_\_\_\_\_

### Instructions

**Examination Aids: Ruler and examiner approved aid sheet are allowed.**

### MARKING GUIDE

Do not turn this page until you have received the signal to start.

Q1: \_\_\_\_\_ (10)

You may remove the aid sheet from the back of this test book. Do not remove any other sheets from this test book. Answer all questions in the space provided. No additional sheets are permitted. Use the blank space in last page as scratch space. Its content will not be marked.

Q2: \_\_\_\_\_ (10)

Q3: \_\_\_\_\_ (7)

This exam consists of 8 question on 15 pages (including this page). The value of each part of each question is indicated. The total value of all questions is 75 marks.

Q4: \_\_\_\_\_ (8)

Q5: \_\_\_\_\_ (9)

For the written answers, explain your reasoning clearly. Be as brief and specific as possible. Clear, concise answers will be given higher marks than vague, wordy answers. Marks will be deducted for incorrect statements in an answer. Please write legibly!

Q6: \_\_\_\_\_ (9)

Q7: \_\_\_\_\_ (12)

Work independently.

Q8: \_\_\_\_\_ (10)

*Total:* \_\_\_\_\_ (75)

**Question 1. What's the Point?** [10 marks]

Given the following programming language terms:

- |                             |                  |
|-----------------------------|------------------|
| 1. Abstraction              | 4. Memory Safety |
| 2. Code Reuse               | 5. Type Safety   |
| 3. Performance Optimization | 6. Thread Safety |

For each one of the programming language paradigms or features, first state its primary purpose (choose from 1 to 6), then explain your choice. Note: you may only choose 1 option out of the 6.

a) Functions (example answer)

2 (code reuse) – a function can be called in multiple parts of the source code to perform same or similar tasks, allowing the functionality to be reused without duplicating code.

b) Concurrent Programming

3 – the purpose of having multiple threads is to speed up the program by using more CPUs.

c) Macro Programming

2 – macro constants and functions allow reusing code fragments.

d) Atomic Variables

6 – an atomic variable allows a thread to update its value without interference from other threads.

e) Tagged Union

5 – tagged union guarantees type-safety for variant types.

f) Constexpr functions

3 – constexpr functions are run at compile-time, which is a form of performance optimization by moving the computation from runtime to compile-time.

**Question 2. Pure or Not?** [10 marks]

For the following C++ functions, state whether they are pure functions. If no, explain why not.

```
int x = 5; // global variables
constexpr int y = 2;
```

<pre>int f(int a) {     int x = a + 3;     return x; }</pre>	<p>Yes. <math>x</math> is a local variable that shadows the global variable of the same name.</p>
<pre>int g(int &amp; a, int &amp; b) {     a += 2;     return a + b; }</pre>	<p>No. <math>a</math> is passed by reference and modified, which changes state outside of the function.</p>
<pre>template&lt;int N&gt; int h(const int (&amp;a)[N]) {     int total = 0;     for (int i = 0; i &lt; N; i++)         total += a[i];     return total; }</pre>	<p>Yes. It is not possible access memory out-of-bound in this situation.</p>
<pre>int k(int a) {     int b = a++;     return b * a; }</pre>	<p>Yes. Both <math>a</math> and <math>b</math> are local variables.</p>
<pre>int p(const int * a, int i) {     int n = a[0];     return a[i] + n; }</pre>	<p>No. Depending on the value of <math>i</math>, it is possible to access out-of-bound memory.</p>
<pre>int q(int a) {     // returns random number     int b = rand();     return b % a; }</pre>	<p>No. The <code>rand()</code> function is impure because it uses and modifies a global variable.</p>
<pre>int t() {     return y; }</pre>	<p>Yes. <math>y</math> is a compile-time constant value that cannot change.</p>

**Question 3. Palindrome** [7 marks]

In C++11, write a constexpr function named `palindrome` to check whether a string is a palindrome. A palindrome is a word or a phrase that reads the same forward and backward, e.g., “madam”, “top spot”. Your solution must be able to ignore space characters, and your code must compile using the `--std=c++11` flag. You may assume all letters in the string are lower case, and you do not need to deal with punctuations. Hint: you may need a helper function.

```
constexpr bool palindrome(const char * s, int front, int back) {
    // 1 mark
    return (front >= back) ? true :

    // 1 mark
    ( (s[front] == ' ') ? palindrome(s, front+1, back) :

        // 1 mark
        ( (s[back] == ' ') ? palindrome(s, front, back-1) :

            // 1 mark          // 1 mark
            s[front] == s[back] && palindrome(s, front+1, back-1)
        )
    );
}

// 1 mark
template<int N>
constexpr bool palindrome(const char (&s)[N]) {
    // 1 mark
    return palindrome(s, 0, N-2);
}
```

**Question 4. Python 2.2** [8 marks]

Given the following class definitions:

```
class A:
    def __init__(self, a, **kwargs):
        self.x = a
        super().__init__(**kwargs)
        self.z = a

class B:
    def __init__(self, b, **kwargs):
        self.y = b
        super().__init__(**kwargs)

class D(B):
    def __init__(self, d, **kwargs):
        self.x = d
        super().__init__(**kwargs)
        self.y = d

class M(A, B):
    def __init__(self, m, **kwargs):
        self.x = m
        super().__init__(**kwargs)
        self.z = m

class N(D, A):
    def __init__(self, n, **kwargs):
        super().__init__(**kwargs)
        self.z = n

class Q(M, N):
    def __init__(self):
        self.y = 1
        super().__init__(a=2, b=3, d=4, m=5, n=6)

foo = Q()
```

Assume this code is run under Python 2.2, where the method resolution order is calculated using depth-first search, left to right, *with refinement* (i.e., remove earlier duplicates).

- a) What is the linearization of the class Q? For class A, B, D, M, N, you may show results only. For class Q, you must show work to receive full marks. [5 marks]

```
L[A] = (A, o)
L[B] = (B, o)
L[D] = (D, B, o)
L[M] = (M, A, B, o)

L[N] = (N, L[D], L[A])
L[N] = (N, D, B, o, L[A])
L[N] = (N, D, B, o, A, o)
# removed earlier duplicate, o
L[N] = (N, D, B, A, o)

L[Q] = (Q, L[M], L[N])
L[Q] = (Q, M, A, B, o, N, D, B, A, o)
# remove earlier duplicate, A, B, o
L[Q] = (Q, M, N, D, B, A, o)
```

- b) What are the values of the following attributes? [3 marks]

foo.x	2	foo.y	4	foo.z	5
-------	---	-------	---	-------	---

**Question 5. Rust Tournament** [10 marks]

You are simulating a knockout tournament in a Rust program. Given the following struct definition for a Team:

```
struct Team {  
    name: String,  
    power: i32,  
}
```

- a) Write a constructor for Team in the form of a static method named new that takes two parameters: name, which is a *string literal* (not a String object), and power, which is an i32 integer. [2 marks]

```
impl Team {  
    fn new(name: &str, power: i32) -> Team {  
        Team { name : name.to_string(), power : power }  
    }  
}
```

- b) Complete the function, match\_up, which takes two teams, home and away, by reference, and returns the team with higher power. On a tie, return the home team. [2 marks]

```
fn match_up<'a>(home: &'a Team, away: &'a Team) -> &'a Team {  
    if home.power >= away.power { home } else { away }  
}
```

- c) Complete the function, round, which takes two vectors of teams by references (i.e. vectors of references), do an element-wise match-up of the two set of teams using the match\_up function, and return a vector of the winning teams *by reference*. You must complete this function in one line of Rust code, without using a semicolon within the function body. [5 marks]

```
fn round<'a>(home: Vec<&'a Team>, away: Vec<&'a Team>)  
    -> Vec<&'a Team> {  
    home.iter().zip(away.iter())  
        .map(|(&x, &y)| match_up(x, y)).collect()  
}
```

**Question 6. Problem with Homonyms** [9 marks]

Given the following two classes in C++.

```
class Prisoner {
    Person * person;
public:
    /* ... other functions ...*/
    void execute() {
        person->kill();
        delete person;
        person = nullptr;
    }
};
```

```
class Method {
    int i = 0;
public:
    /* ... other functions ...*/
    void execute() {
        i++;
        std::cout << "i = " << i
                  << std::endl;
    }
};
```

And a template function which will repeatedly call the execute member function.

```
template<typename T>
void repeat(T & repeatable, int n) {
    for (int i = 0; i < n; i++)
        repeatable.execute();
}
```

Below is the output when running the repeat function on an object of the above two classes:

```
[main.cpp for Prisoner]
Person * person = new Person();
Prisoner prisoner(person);
repeat(prisoner, 3);
```

Program Output:

```
He's Dead, Jim
Segmentation fault (core dumped)
```

```
[main.cpp for Method]
Method method;
repeat(method, 3);
```

Program Output:

```
i = 1
i = 2
i = 3
```



- a) Convert the C++ code to Rust while maintaining the same program structure. If there is a language feature that can avoid the problem shown above, use it to fix the problem. If not, show that the same problem will manifest. Briefly explain your answer. [5 marks]

```
struct Prisoner {
    person : Option<Person>
}

impl Prisoner {
    fn execute(&mut self) {
        if let Some(person) = &self.person {
            person.kill();
        } else {
            panic!("Person is already dead!");
        }
        self.person = None;
    }
}

struct Method {
    i : i32
}

pub trait Repeatable {
    fn execute(&mut self);
}

impl Repeatable for Method {
    fn execute(&mut self) {
        self.i += 1;
        println!("i = {}", self.i);
    }
}

//
// Rust is able to avoid the problem that Prisoner::execute is not
// repeatable by applying a trait bound to the repeat function.
//
pub fn repeat<T: Repeatable>(repeatable: &mut T, n: i32) {
    for _ in 0..n {
        repeatable.execute();
    }
}
```

- b) Convert the C++ code to Python while maintaining the same program structure. If there is a language feature that can avoid the problem shown above, use it to fix the problem. If not, show that the same problem will manifest. Briefly explain your answer. [4 marks]

```
class Prisoner:
    def __init__(self, person):
        self.person = person

    def execute(self):
        self.person.kill()
        self.person = None

class Method:
    def __init__(self):
        self.i = 0

    def execute(self):
        self.i += 1
        print("i = %d"%self.i)

#
# The problem will persist because Python does not type-check the
# object before accepting it.
#
def repeat(repeatable, n):
    for i in range(n):
        repeatable.execute()
```

-----

Note that full marks will also be awarded if the student adds runtime type-checking as a solution, e.g.:

```
class Method(Repeatable):
    ...

def repeat(repeatable, n):
    assert(isinstance(repeatable, Repeatable))
    for i in range(n):
        repeatable.execute()
```

**Question 7. Roman Numerals** [12 marks]

The following macro constant contains a list of macro invocations that maps roman numeral symbols to their values.

```
/* N(SYMBOL, VALUE, SUFFIX) */
#define ROMAN_NUMERALS \
    N(I,      1, S(V) S(X)) \
    N(V,      5) \
    N(X,     10, S(L) S(C)) \
    N(L,     50) \
    N(C,    100, S(D) S(M)) \
    N(D,    500) \
    N(M, 1000)
```

For example, the symbol X maps to the value 10, and the symbol M maps to 1000. The roman numeral “III” is the integer value 3, and “MLXXI” equals to  $1000 + 50 + 10 + 10 + 1 = 1071$ .

Roman numerals use a subtractive notation where the value of two consecutive symbols is the difference between their values. For example, IV is  $5 - 1 = 4$  (i.e., V – I), and XC is  $100 - 10 = 90$  (i.e., C – X). When subtractive notation is allowed for a particular symbol, the N macro function takes an optional third parameter which contains an inner list of macro invocations for each suffix symbol. For example, when C is followed by D or M, subtractive notation is applied, but not for L.

Complete the function, `roman_to_integer`, which will convert roman numerals, encoded as null-terminated strings, to integers. You must use the X-macro technique to receive full marks. Note: while processing the string, if it contains any non-roman numeral characters, the function should return 0 immediately. You may otherwise assume that all input will be roman numerals in standard form.

```
/* Hint: create a mapping between the symbols and the values here */

enum Roman {                                     // 2 marks
#define N(SYM, ...) SYM,
    ROMAN_NUMERALS
#undef N
};

unsigned roman_value[] = {                       // 2 marks
#define N(SYM, VAL, ...) VAL,
    ROMAN_NUMERALS
#undef N
};
```

```
Unsigned roman_to_integer(const char * str)
{
    unsigned idx = 0;
    unsigned len = strlen(str);
    unsigned val = 0;

    while (idx < len)
    {

// 4 marks
#define N(SYM, VAL, ...) \
    if (str[idx] == #SYM[0]) { \
        unsigned cur = VAL; /* needed by S */ \
        __VA_ARGS__ \
        { val += VAL; idx += 1; } \
    } else

// 3 marks (1 per line)
#define S(SYM) if (str[idx+1] == #SYM[0]) { \
    val += roman_value[SYM] - cur; \
    idx += 2; \
    } else

        ROMAN_NUMERALS
#undef S
#undef N

        // 1 mark
        { return 0; }
    }

    return val;
}
```

**Question 8. Database Row** [10 marks]

You are writing a template class to represent a database row object. Each row has many columns, and each column has a type. Columns inside a row may have different types.

```
template <typename ... ColumnTypes> struct Row;
```

- a) Write the recursive template definition for struct Row. Remember to define a constructor. [4 marks]

```
// 1 mark
template<typename ... ColumnTypes> struct Row {};

template<typename T, typename ... ColumnTypes>
// 1 mark
struct Row<T, ColumnTypes...> : public Row<ColumnTypes...> {
    // 2 marks (for part b)
    using ParentType = Row<ColumnTypes...>;
    using ValueType = T;

    T value; // 1 mark

    // 1 mark
    Row(T v, ColumnTypes ... cols)
        : ParentType(cols...), value(v) {}
};
```

- b) The struct ColumnOf can be used to get the column type given a row type. For example: ColumnOf<Row<int, float>, 1>::Type would be the type float. Read the following code and add two statements to struct Row definition above to make it work with ColumnOf. Note: inside a template definition, when referring to a type defined inside another template, you must prefix the type (known as dependent name) with the keyword typename. [2 marks]

```
template <typename T, int N>
struct ColumnOf {
    using Type = typename ColumnOf<typename T::ParentType,
                                   N - 1>::Type;
};

template <typename T>
struct ColumnOf<T, 0> {
    using Type = typename T::ValueType;
};
```

- c) Write a template class named `Column` with a *static template member function* named `Get` that will allow the programmer to retrieve a particular column from a row object. For example:

```
using BankRow = Row<const char *, const char *, int, double>;
auto row = BankRow("Mike", "Qin", 31, 1000.25);
int age = Column<2>::Get(row); // returns 31
```

Hint: `ColumnOf` will be very helpful when extracting values from the row object. [4 marks]

```
template<int N> struct Column
{
    template<typename T>
    // 1 mark
    static typename ColumnOf<T, N>::Type Get(T & row) {
        // 1 mark
        return Column<N-1>::Get((typename T::ParentType &)row);
    }
};

// 1 mark
template<>
struct Column<0>
{
    template<typename T>
    static typename ColumnOf<T, 0>::Type Get(T & row) {
        // 1 mark
        return row.value;
    }
};
```

*[Use the space below for rough work]*

END OF EXAMINATION