

Understanding Einstein's General Relativity Equation

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Objective

Focus on gaining a better understanding of Einstein's
General Relativity equation

- Describe what a matrix is
- Describe every variable in the matrix
- Describe what each variable does

This will help us gain a better intuition of this extremely
valuable tool, and how we can use it

$$G_{\mu\nu} = \begin{matrix} & \begin{matrix} t & r & \theta & \phi \end{matrix} \\ \begin{matrix} t \\ r \\ \theta \\ \phi \end{matrix} & \begin{bmatrix} G_{tt} & G_{tr} & G_{t\theta} & G_{t\phi} \\ G_{rt} & G_{rr} & G_{r\theta} & G_{r\phi} \\ G_{\theta t} & G_{\theta r} & G_{\theta\theta} & G_{\theta\phi} \\ G_{\phi t} & G_{\phi r} & G_{\phi\theta} & G_{\phi\phi} \end{bmatrix} \end{matrix}$$

What is a Matrix: The Flat Sheet Analogy

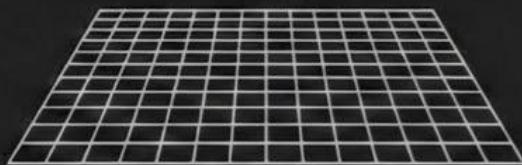
The Matrix ($G_{\mu\nu}$)

$$\begin{pmatrix} G_{tt} & G_{tr} & G_{t\theta} & G_{t\phi} \\ G_{rt} & G_{rr} & G_{r\theta} & G_{r\phi} \\ G_{\theta t} & G_{\theta r} & G_{\theta\theta} & G_{\theta\phi} \\ G_{\phi t} & G_{\phi r} & G_{\phi\theta} & G_{\phi\phi} \end{pmatrix}$$

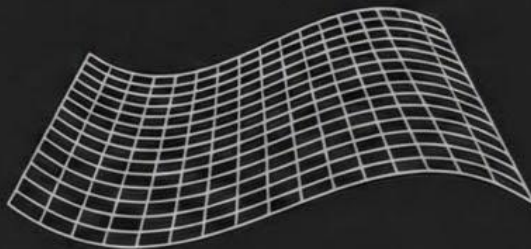
Represents the geometry of spacetime.
The 'numbers' (like G_{tt} , G_{rr}) define its shape.



Flat Sheet of Paper (Flat Spacetime)



Bent Sheet of Paper (Curved Spacetime)



Changing the matrix numbers causes
the 'paper' to bend and curve.

Matrix Columns: Dimensions of Spacetime

$G_{\mu\nu}$ =

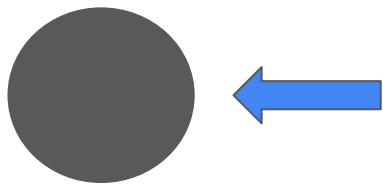
G_{tt}	G_{tr}	$G_{t\theta}$	$G_{t\phi}$
G_{rt}	G_{rr}	$G_{r\theta}$	$G_{r\phi}$
$G_{\theta t}$	$G_{\theta r}$	$G_{\theta\theta}$	$G_{\theta\phi}$
$G_{\phi t}$	$G_{\phi r}$	$G_{\phi\theta}$	$G_{\phi\phi}$

It's a tensor. A single point in space time.

4D (Time) 1D (Space) 2D (Space) 3D (Space)

The diagram shows the metric tensor $G_{\mu\nu}$ as a 4x4 matrix. The columns are color-coded and labeled with their corresponding dimensions: the first column (red) is 4D (Time), the second (green) is 1D (Space), the third (orange) is 2D (Space), and the fourth (purple) is 3D (Space). Arrows point from these labels to their respective columns. A red circle highlights the $G_{\mu\nu}$ symbol, with an arrow pointing to the text 'It's a tensor. A single point in space time.'

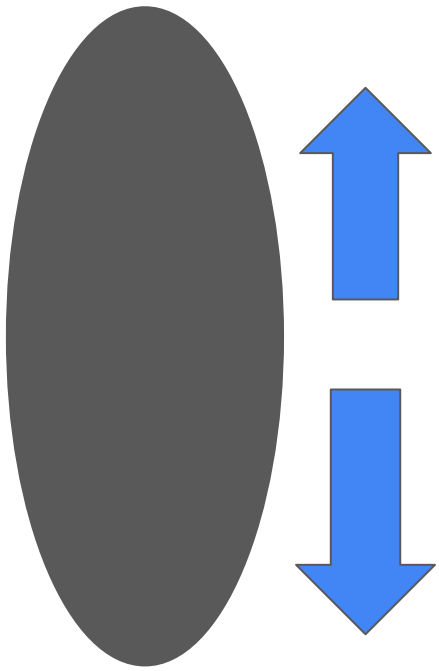
Each column of the metric tensor corresponds to a specific dimension of spacetime, with time treated as the fourth dimension.



Tensor
(Single point in space time)

This is an example of what a tensor can look like. As the numbers in the matrix change, the tensor will warp and reshape. This gives us what space time looks like at that one point

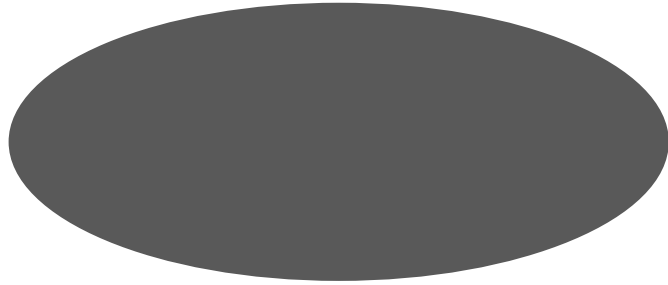
	t	r	θ	ϕ
t	G_{tt}	G_{tr}	$G_{t\theta}$	$G_{t\phi}$
r	G_{rt}	G_{rr}	$G_{r\theta}$	$G_{r\phi}$
θ	$G_{\theta t}$	$G_{\theta r}$	$G_{\theta\theta}$	$G_{\theta\phi}$
ϕ	$G_{\phi t}$	$G_{\phi r}$	$G_{\phi\theta}$	$G_{\phi\phi}$



Tensor
(Single point in space time)

When the radial number
(G_{rr}) changes the tensor
grows radially, up and
down.

	t	r	θ	ϕ
t	G_{tt}	G_{tr}	$G_{t\theta}$	$G_{t\phi}$
r	G_{rt}	G_{rr}	$G_{r\theta}$	$G_{r\phi}$
θ	$G_{\theta t}$	$G_{\theta r}$	$G_{\theta\theta}$	$G_{\theta\phi}$
ϕ	$G_{\phi t}$	$G_{\phi r}$	$G_{\phi\theta}$	$G_{\phi\phi}$

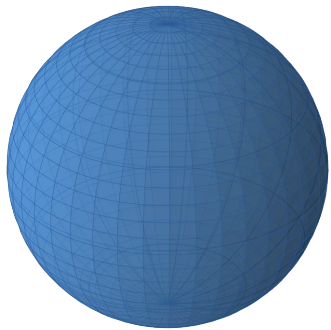


Tensor
(Single point in space time)

When the 2d number, θ
(theta), changes the
tensor grows
horizontally left to right

	t	r	θ	ϕ
t	G_{tt}	G_{tr}	$G_{t\theta}$	$G_{t\phi}$
r	G_{rt}	G_{rr}	$G_{r\theta}$	$G_{r\phi}$
θ	$G_{\theta t}$	$G_{\theta r}$	$G_{\theta\theta}$	$G_{\theta\phi}$
ϕ	$G_{\phi t}$	$G_{\phi r}$	$G_{\phi\theta}$	$G_{\phi\phi}$

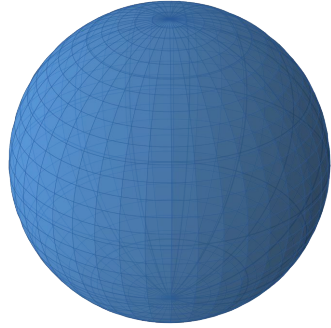
3d Sphere



Tensor
(Single point in space time)

When, $G_{\phi\phi}$ — the azimuthal component, changes the tensor grows in 3d space as a sphere.

	t	r	θ	ϕ
t	G_{tt}	G_{tr}	$G_{t\theta}$	$G_{t\phi}$
r	G_{rt}	G_{rr}	$G_{r\theta}$	$G_{r\phi}$
θ	$G_{\theta t}$	$G_{\theta r}$	$G_{\theta\theta}$	$G_{\theta\phi}$
ϕ	$G_{\phi t}$	$G_{\phi r}$	$G_{\phi\theta}$	$G_{\phi\phi}$



Tensor
(Single point in space time)

Time is an equation. It says the bigger the mass and the closer you are to it, time slows down. And the result of that equation goes here.

	t	r	θ	ϕ
t	G_{tt}	G_{tr}	$G_{t\theta}$	$G_{t\phi}$
r	G_{rt}	G_{rr}	$G_{r\theta}$	$G_{r\phi}$
θ	$G_{\theta t}$	$G_{\theta r}$	$G_{\theta\theta}$	$G_{\theta\phi}$
ϕ	$G_{\phi t}$	$G_{\phi r}$	$G_{\phi\theta}$	$G_{\phi\phi}$

Summary

We have focused on gaining a better understanding of Einstein's General Relativity equation

- We described what a matrix is
- We described every variable in the matrix
- We focused on understanding what each variable does

This will help us gain a better intuition of this extremely valuable tool, and how we can use it