

p8131\_hw6\_xy2395

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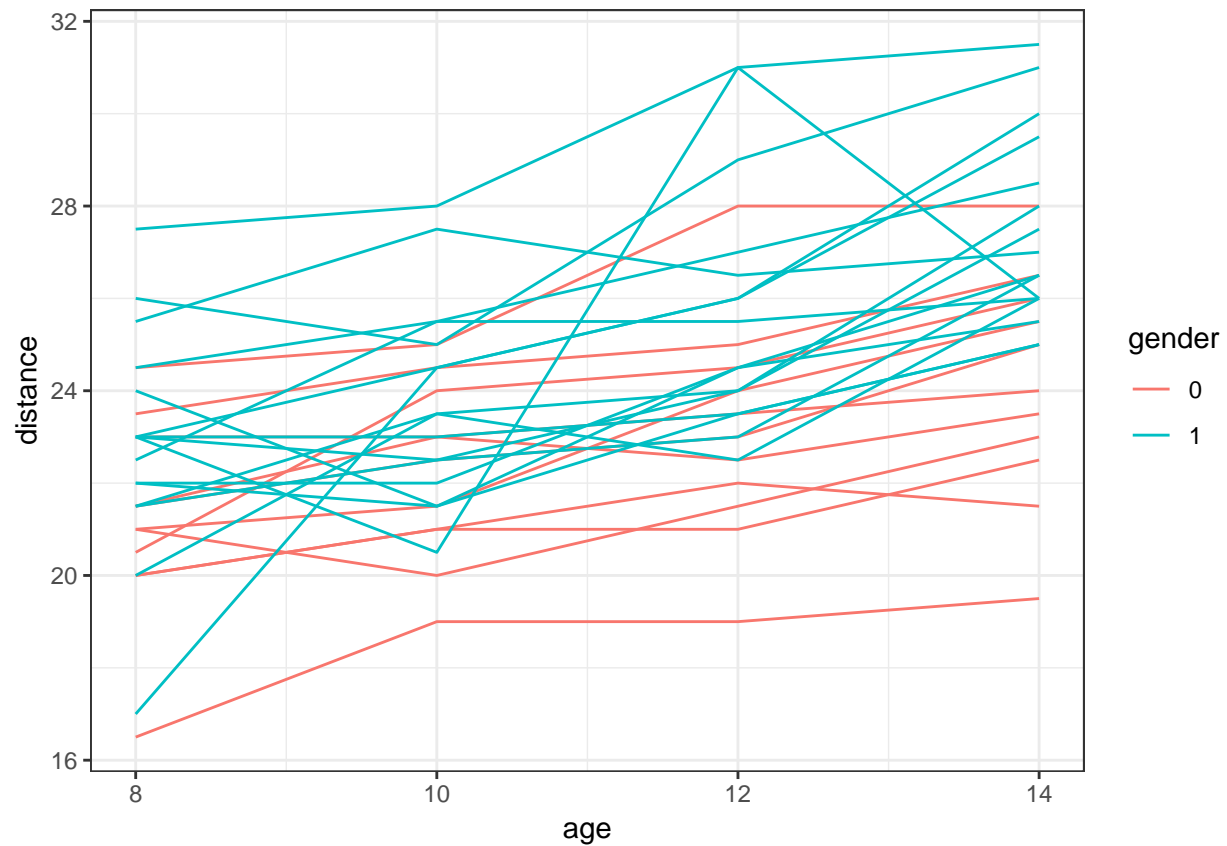
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## Problem 2

### 2.1 Spaghetti Plot

```
# Import data
dental <-
  read.table('HW6-dental.txt', header = TRUE) %>%
  as.tibble() %>% janitor::clean_names() %>%
  mutate(gender = as.factor(gender))

# Spaghetti plot
dental %>%
  ggplot(aes(x = age, y = distance, group = child, color = gender)) +
  geom_line() +
  theme_bw()
```



## 2.2 Marginal Form

$$\begin{aligned} E(Y_{ij}) &= E(\beta_0 + a_i + b_0 * I_{(sex_i=0)} + b_1 * I_{(sex_i=1)} + \beta_1 * age_{ij} + e_{ij}) \\ &= \beta_0 + \beta_1 * age_{ij} \\ Var(Y_i) &= Var(a_i + e_{ij} + b_k) \\ &= Var(a_i) + Var(e_{ij}) + Var(b_k) \\ &= \sigma_a^2 + \sigma_e^2 + \sigma_b^2 \end{aligned}$$

## 2.3 Comparing models with different covariance patterns

Assume equal variance across measurements.

```
# Compound Symmetry covariance
compsym = gls(distance ~ gender + age,
  data = dental,
  correlation = corCompSymm(form = ~1 | child),
  method="REML")

# Exponential covariance
expo = gls(distance ~ gender + age,
  data = dental,
  correlation = corExp(form = ~1 | child),
  method = 'REML')

# Autoregressive covariance
auto1 = gls(distance ~ gender + age,
  data = dental,
  correlation = corAR1(form = ~1 | child),
  method = 'REML')

# Compare coefficient parameter estimates
bind_rows(
  compsym$coefficients,
  expo$coefficients,
  auto1$coefficients,
) %>%
mutate(CovType = c('CompSym', 'Exp', 'Auto')) %>%
select(CovType, everything()) %>%
knitr::kable()
```

CovType	(Intercept)	gender1	age
CompSym	15.38569	2.321023	0.6601852
Exp	15.45999	2.418714	0.6529597
Auto	15.45999	2.418714	0.6529597

The coefficient parameter estimates are similar across the 3 covariance patterns.

```
# Compare covariance estimates
tibble(
  Covtype = c('CompSym', 'Exp', 'Auto'),
  variance = c(compsym$sigma, expo$sigma, auto1$sigma)^2
) %>%
knitr::kable()
```

Covtype	variance
CompSym	5.316240
Exp	5.296881
Auto	5.296881

The covariance estimates are similar across the 3 covariance patterns.