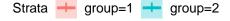
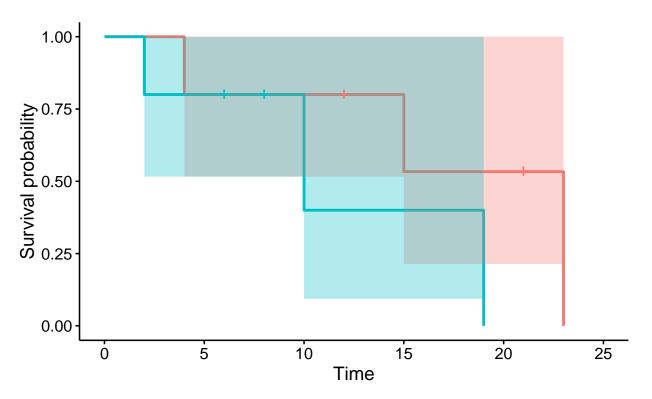


```
library(tidyverse)
library(survival)
library(survminer)
library(KMsurv)
```

Problem 1

```
data1 =
   tibble(
    time = c(4, 12, 15, 21, 23, 2, 6, 8, 10, 19),
    delta = c(1, 0, 1, 0, 1, 1, 0, 0, 1, 1),
    group = c(1, 1, 1, 1, 1, 2, 2, 2, 2, 2)
)
Surv(data1$time, data1$delta, type = 'right')
## [1] 4 12+ 15 21+ 23 2 6+ 8+ 10 19
# Plot
ggsurvplot(survfit(Surv(time, delta) ~ group, data = data1), conf.int=TRUE)
```





```
# Log-rank test
survdiff(Surv(time, delta)~group, data = data1)
## Call:
## survdiff(formula = Surv(time, delta) ~ group, data = data1)
##
##
           N Observed Expected (0-E)^2/E (0-E)^2/V
## group=1 5
                    3
                          4.14
                                   0.313
                                              1.15
## group=2 5
                    3
                          1.86
                                   0.697
                                              1.15
##
## Chisq= 1.1 on 1 degrees of freedom, p= 0.3
```

The chi-squared statistic is 1.1 and p-value is 0.3 > 0.05, so we fail to reject the null and conclude that the survival curves of the 2 groups are not different.

Problem 2

```
data(kidtran)
head(kidtran)
     obs time delta gender race age
##
## 1
                  0
                                 46
       1
            1
                         1
                               1
## 2
       2
            5
                  0
                          1
                               1
                                  51
## 3
       3
            7
                  1
                                 55
                         1
                               1
## 4
       4
            9
                  0
                          1
                               1
                                 57
## 5
       5
           13
                  0
                               1 45
                          1
## 6
       6
           13
                  0
                          1
                               1 43
# plot
ggsurvplot(survfit(Surv(time, delta) ~ gender + race, data = kidtran), conf.int=F)
```

```
Strata + gender=1, race=1 + gender=1, race=2 + gender=2, race=1 + gender=2, race
   1.00
Survival probability
0.50
0.25
   0.00
                                   1000
            0
                                                            2000
                                                                                     3000
                                               Time
# Log-rank test
# male
survdiff(Surv(time, delta)~ gender + race, data = kidtran, subset = (gender == 1))
## Call:
   survdiff(formula = Surv(time, delta) ~ gender + race, data = kidtran,
##
##
       subset = (gender == 1))
##
##
                       N Observed Expected (O-E)^2/E (O-E)^2/V
   gender=1, race=1 432
                               73
                                      71.9
                                               0.0168
                                                          0.097
   gender=1, race=2 92
                               14
                                      15.1
                                               0.0801
                                                          0.097
##
##
   Chisq= 0.1 on 1 degrees of freedom, p= 0.8
survdiff(Surv(time, delta)~ gender + race, data = kidtran, subset = (gender == 2))
## Call:
   survdiff(formula = Surv(time, delta) ~ gender + race, data = kidtran,
##
       subset = (gender == 2))
##
##
                       N Observed Expected (O-E)^2/E (O-E)^2/V
## gender=2, race=1 280
                               39
                                      44.79
                                                0.748
                                                            4.85
   gender=2, race=2 59
                               14
                                      8.21
                                                4.076
                                                            4.85
##
##
    Chisq= 4.8 on 1 degrees of freedom, p= 0.03
```

For males, the chi-squared statistic is 0.1 and p-value is 0.8 > 0.05, so we fail to reject the null and conclude that the survival curve of different races is not different in males. On the other hand, for females, the chi-squared statistics is 4.8 and p-value is 0.03 < 0.05, so we have enough evidence to reject the null and

conclude that the survival curves for different races is different in females.

Problem 3

```
data(larynx)
head(larynx)
     stage time age diagyr delta
##
## 1
         1 0.6 77
                        76
## 2
           1.3 53
                        71
                               1
## 3
         1 2.4 45
                        71
                               1
## 4
         1 2.5 57
                        78
## 5
         1 3.2 58
                        74
                               1
## 6
         1 3.2 51
                        77
data3 =
 larynx %>%
  mutate(z1 = if_else(stage == 2, 1, 0),
         z2 = if_else(stage == 3, 1, 0),
         z3 = if_else(stage == 4, 1, 0)) %>%
 rename(z4 = age)
fit = coxph(Surv(time, delta)~z1 + z2 + z3 + z4 + z1 * z4, data = data3, ties = "breslow")
summary(fit)
## Call:
## coxph(formula = Surv(time, delta) \sim z1 + z2 + z3 + z4 + z1 *
##
       z4, data = data3, ties = "breslow")
##
##
    n= 90, number of events= 50
##
##
               coef exp(coef)
                                 se(coef)
                                               z Pr(>|z|)
## z1
         -7.3820143 0.0006223 3.4027542 -2.169
                                                    0.0301 *
          0.6218044 1.8622853 0.3558078 1.748
## z2
                                                    0.0805 .
## z3
          1.7534270 5.7743576 0.4239595
                                           4.136 3.54e-05 ***
          0.0059729 1.0059908 0.0148792 0.401
                                                    0.6881
## z4
## z1:z4 0.1116674 1.1181409 0.0476728 2.342
                                                    0.0192 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
         exp(coef) exp(-coef) lower .95 upper .95
## z1
         0.0006223 1606.8231 7.900e-07
                                           0.4903
## z2
         1.8622853
                       0.5370 9.272e-01
                                           3.7403
                       0.1732 2.516e+00
## z3
         5.7743576
                                         13.2550
## z4
         1.0059908
                       0.9940 9.771e-01
                                           1.0358
## z1:z4 1.1181409
                       0.8943 1.018e+00
                                            1.2277
##
## Concordance= 0.682 (se = 0.04)
## Likelihood ratio test= 24.11
                                 on 5 df,
                                            p = 2e - 04
## Wald test
                        = 23.77
                                 on 5 df,
                                            p = 2e - 04
## Score (logrank) test = 27.98
                                on 5 df,
                                             p = 4e - 05
The proportional hazards model is:
```

 $h_i(t) = h_0(t)e^{-7.38Z_1 + 0.62Z_2 + 1.75Z_3 + 0.006Z_4 + 0.11Z_1 \times Z_4}$

Interpretations:

The hazard ratio for subjects of age k in Stage II versus subjects in Stage I of the same age is $e^{-7.38+0.11\times k}$.

The hazard ratio for subjects in Stage III versus subjects in Stage I is 1.86, keeping age at diagnosis constant.

The hazard ratio for subjects in Stage IV versus subjects in Stage I is 5.77, keeping age at diagnosis constant.

If the patients are not in stage II, the hazard ratio for one-year increase in age at diagnosis is 1.0059908, for patients in the same stage. If the patients are in stage II, the hazard ratio for one-year increase in age at diagnosis is $e^{0.006+0.112} = 1.12$.

The relative risk of dying is $e^{-7.38+0.11\times50}=0.153$ for a stage II patient of age 50 as compared to a stage I patient of the same age.