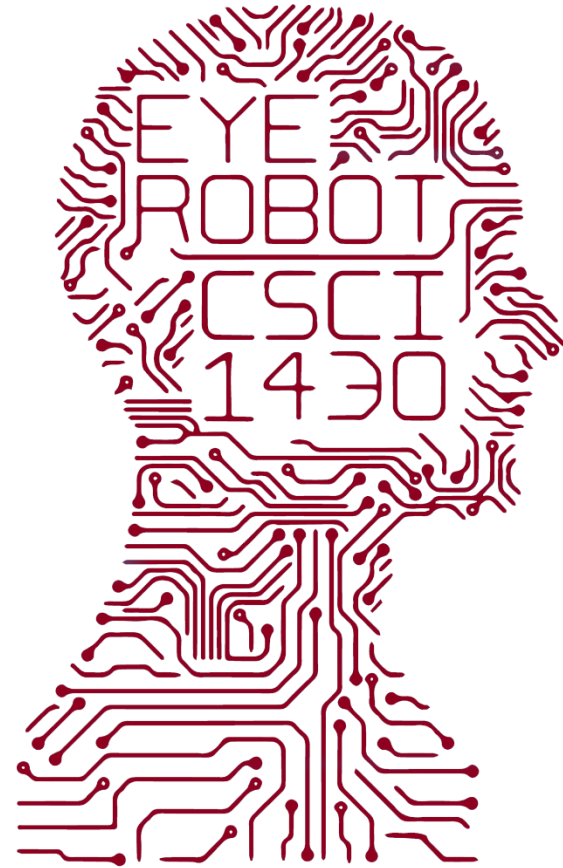


FUTURE VISION



COMPUTER VISION

Prismia.Chat <https://tinyurl.com/y26ragof>

Next Classes

- Spatial frequency
- Fourier transform and frequency domain
 - Frequency view of filtering
 - Hybrid images
 - Sampling

Overview of today's lecture

- Image downsampling.
- Aliasing.
- Gaussian image pyramid.
- Laplacian image pyramid.
- Fourier series.
- Frequency domain.
- Fourier transform.
- Frequency-domain filtering.
- Revisiting sampling.

Slide credits

Most of these slides were adapted directly from:

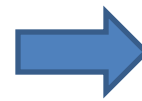
- Kris Kitani (15-463, Fall 2016).

Some slides were inspired or taken from:

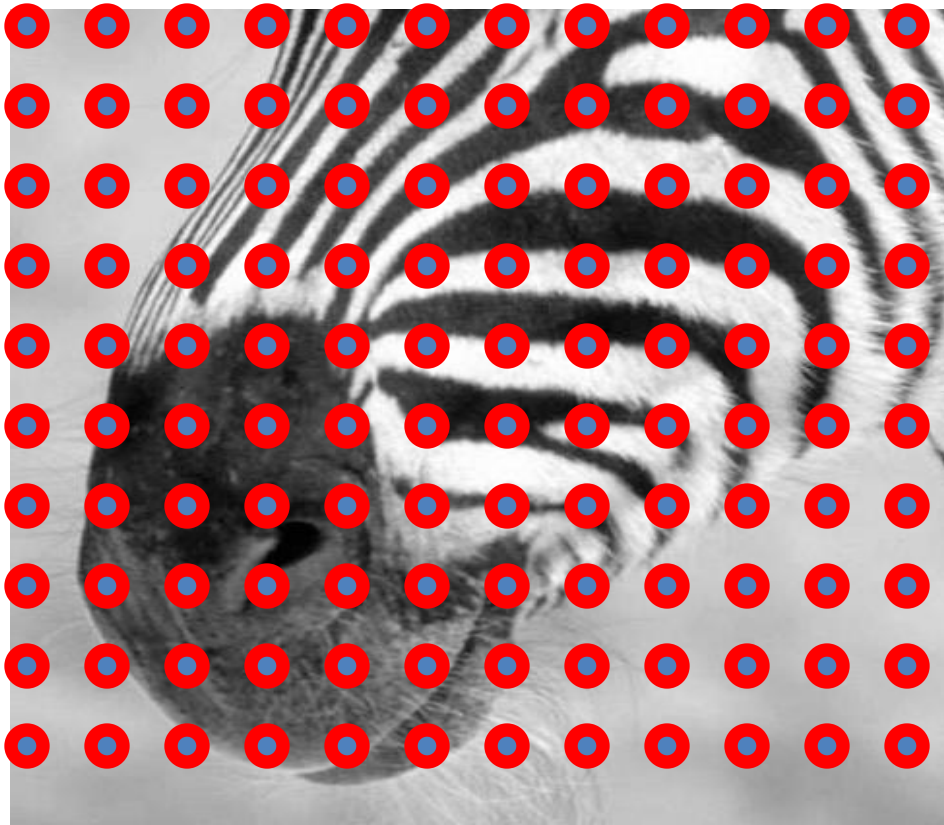
- Fredo Durand (MIT).
- Bernd Girod (Stanford University).
- James Hays (Georgia Tech).
- Steve Marschner (Cornell University).
- Steve Seitz (University of Washington).

Image downsampling

Why does a lower resolution image still make sense to us? What information do we lose?



Making lower resolution images: Subsampling by a factor of 2



Throw away every other row and
column to create a 1/2 size image



512

256

128

64

32

16

8



A 'bar' in the big images is a hair on the zebra's nose; in smaller images, a stripe; in the smallest, the animal's nose

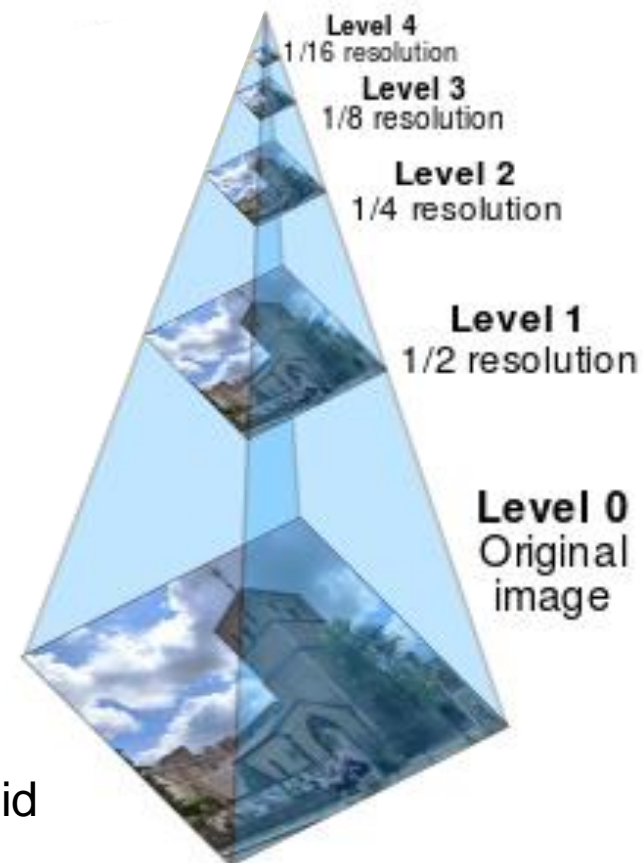


Image
pyramid

Algorithm for downsampling by factor of 2

1. Start with image of $w \times h$
2. Sample every other pixel
 - `im_small = image[::2, ::2]`
3. To build a pyramid,
repeat Steps 1 & 2
until `im_small` is 1 pixel large.

Numpy syntax:

`::2` -> start at 0,
end at 'end',
increase every 2,
until the end.

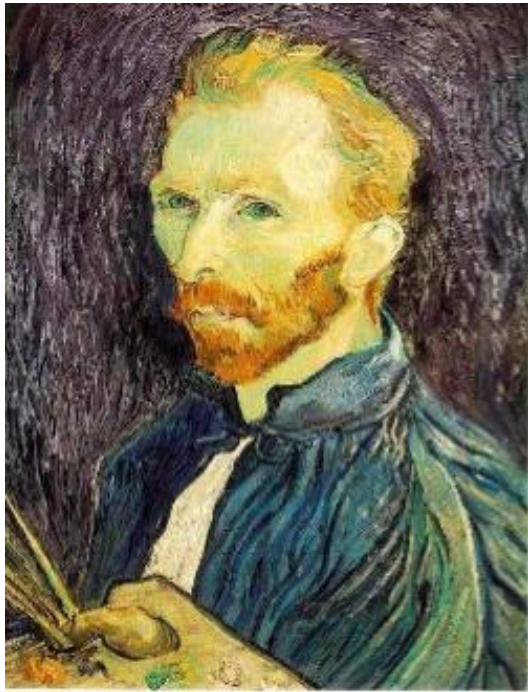
e.g.,
`0,2,4,6,...,w`

(if w is not even, then
this goes to $w-1$)

A close-up portrait of Vincent van Gogh, showing his face and upper torso. He has a thick, reddish-brown beard and mustache, and his hair is a mix of yellow and brown. He is wearing a dark blue jacket with a white collar. The background is a dark, textured brown. The painting is characterized by its visible brushstrokes and vibrant colors.

**This image is too big to fit on the screen.
How would you reduce it to half its size?**

Naïve image downsampling



1/2

Throw away half the rows and columns

delete even rows
delete even columns



1/4

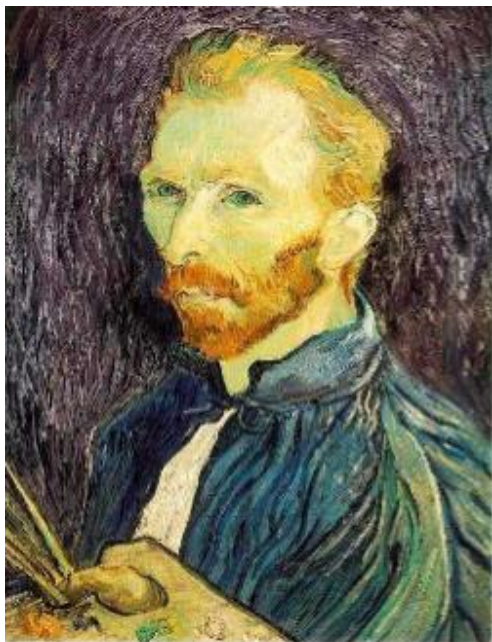
delete even rows
delete even columns



1/8

What is the problem with this approach?

Naïve image downsampling



1/2



1/4 (2x zoom)

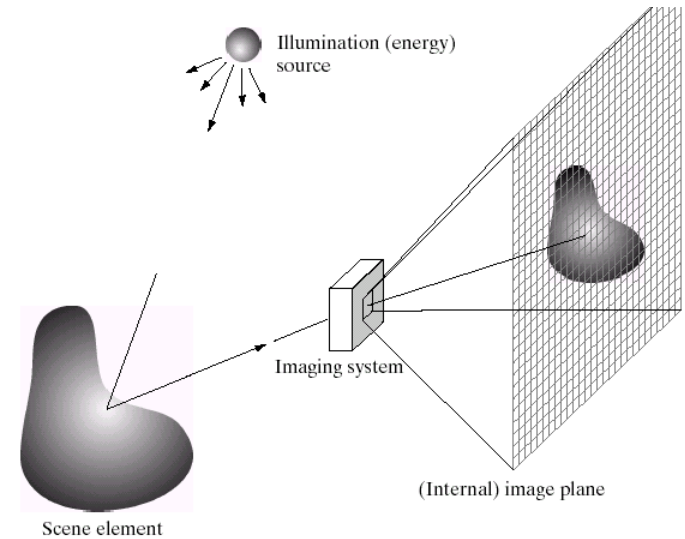


1/8 (4x zoom)

What is the 1/8 image so pixelated (and do you know what this effect is called)?

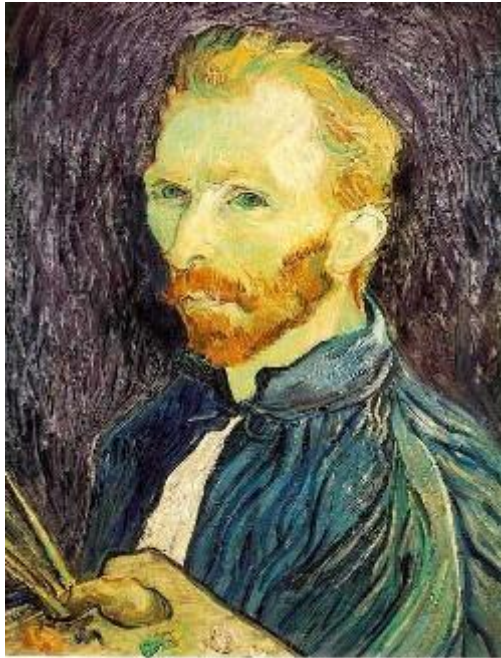
Aliasing

Reminder



Images are a *discrete*, or *sampled*, representation of a *continuous* world

Image sub-sampling



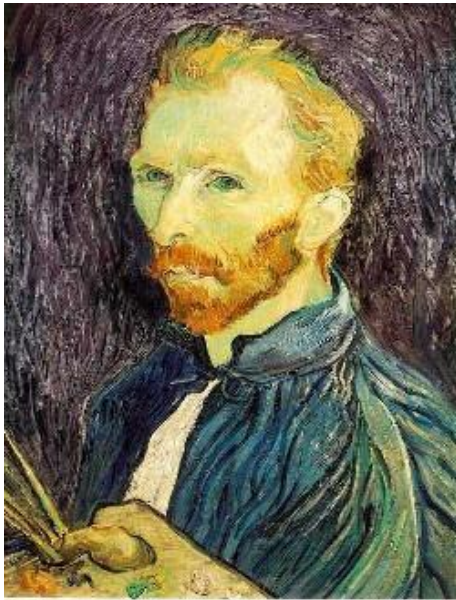
1/4



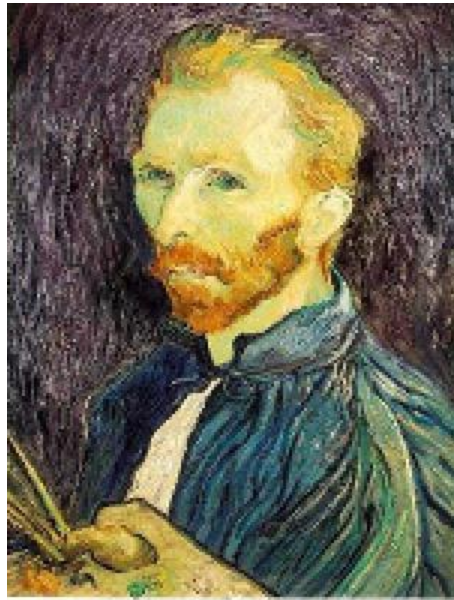
1/8

Throw away every other row and column to create a $1/2$ size image.

Subsampling without filtering



$1/2$



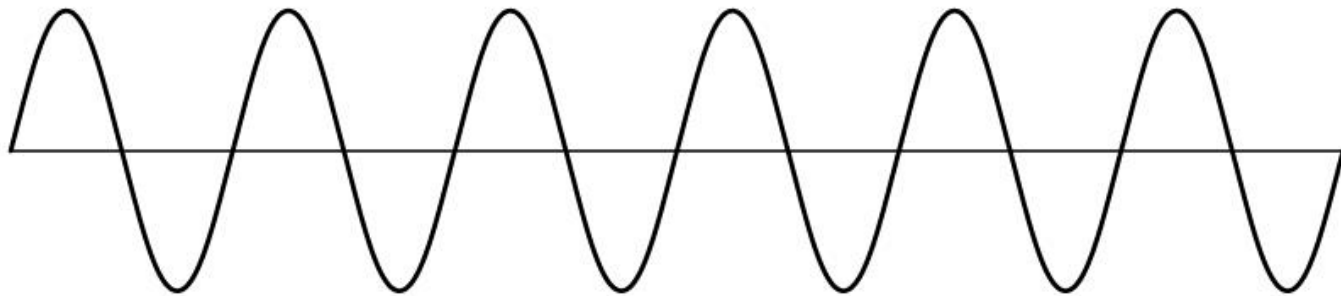
$1/4$ (2x subsample)



$1/8$ (4x subsample)

Sampling

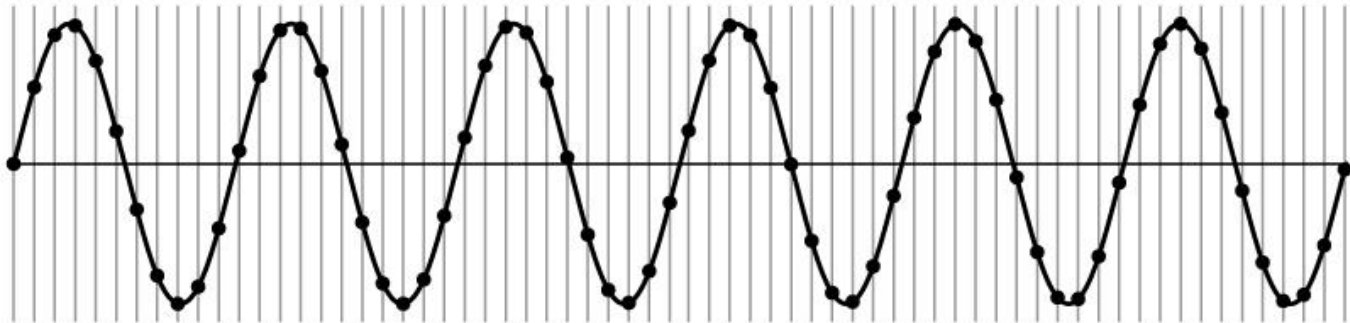
Very simple example: a sine wave



How would you discretize this signal?

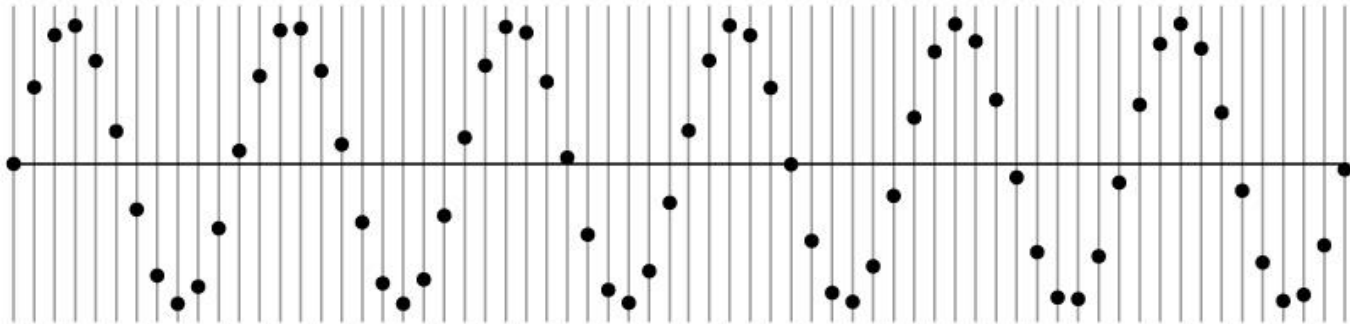
Sampling

Very simple example: a sine wave



Sampling

Very simple example: a sine wave

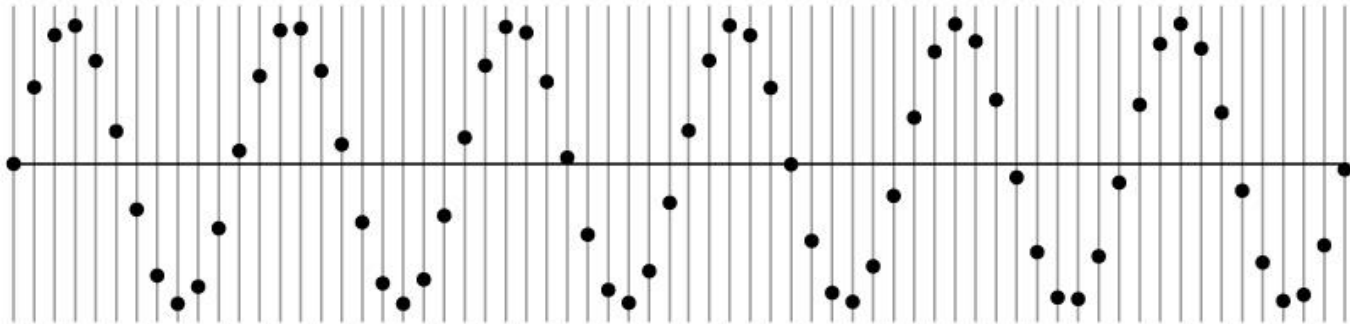


How many samples should I take?

Can I take as *many* samples as I want?

Sampling

Very simple example: a sine wave

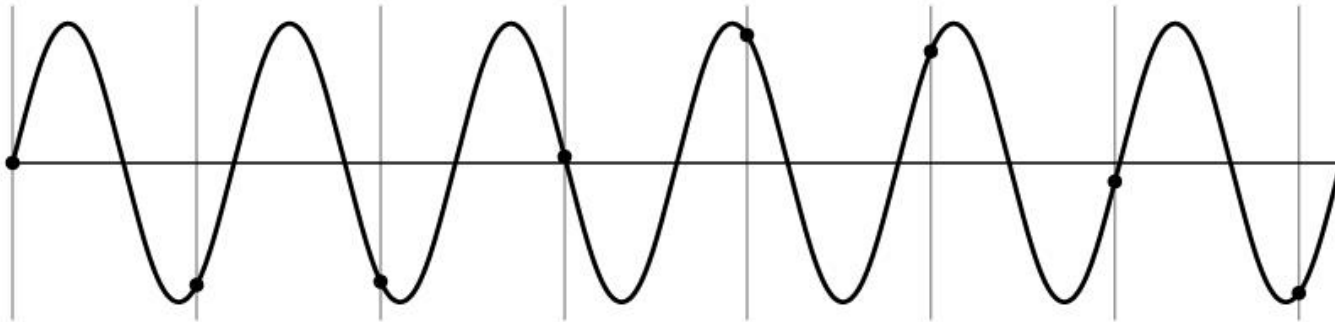


How many samples should I take?

Can I take as *few* samples as I want?

Undersampling

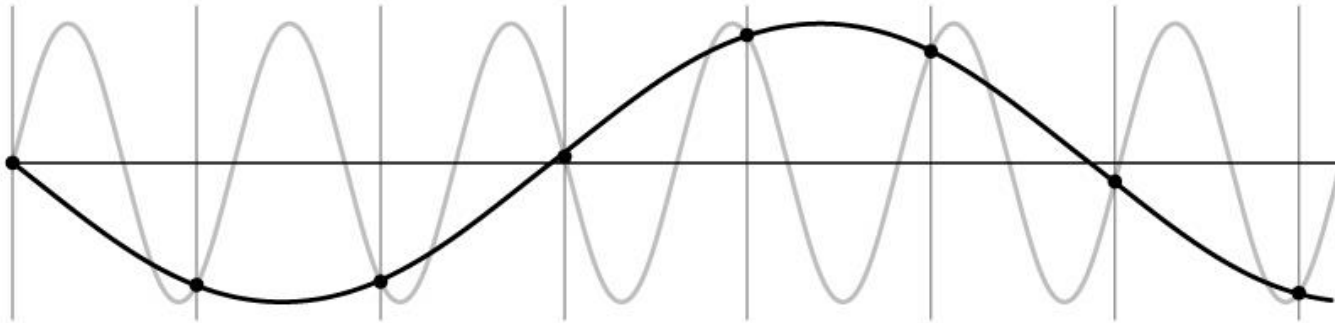
Very simple example: a sine wave



Unsurprising effect: information is lost.

Undersampling

Very simple example: a sine wave

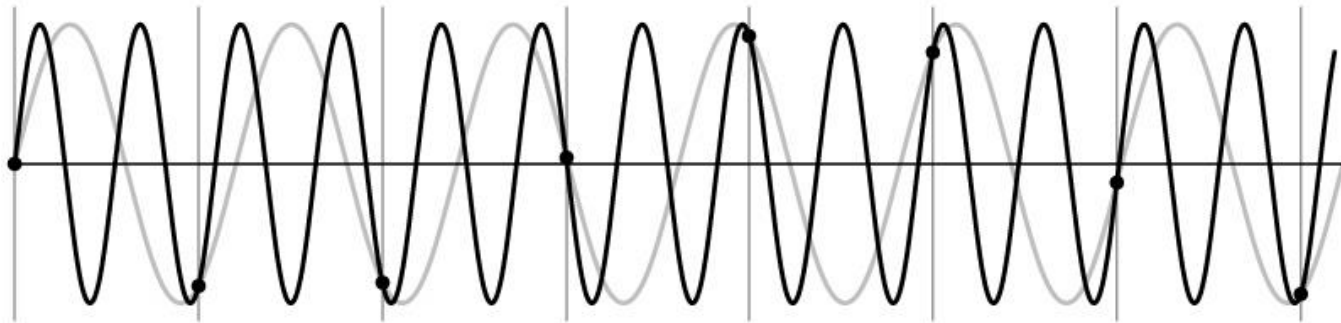


Unsurprising effect: information is lost.

Surprising effect: can confuse the signal with one of *lower* frequency.

Undersampling

Very simple example: a sine wave



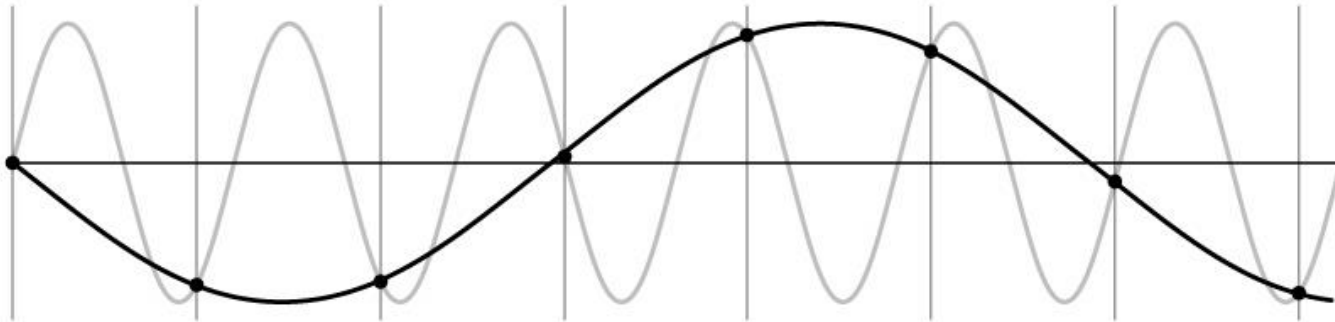
Unsurprising effect: information is lost.

Surprising effect: can confuse the signal with one of *lower* frequency.

Note: we could always confuse the signal with one of *higher* frequency.

Aliasing

Fancy term for: *Undersampling can disguise a signal as one of a lower frequency*

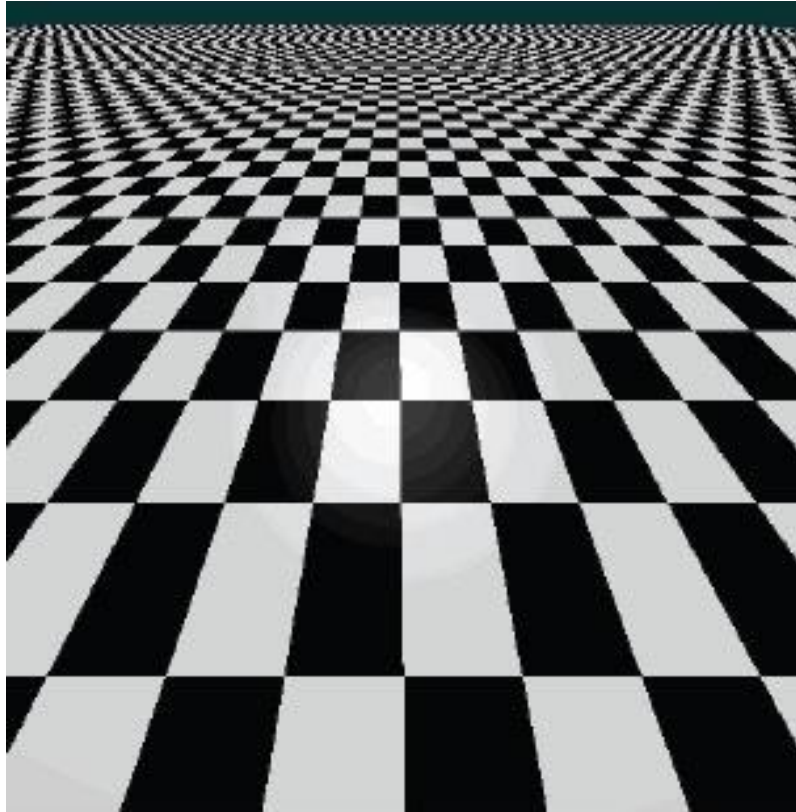


Unsurprising effect: information is lost.

Surprising effect: can confuse the signal with one of *lower* frequency.

Note: we could always confuse the signal with one of *higher* frequency.

Aliasing in textures



Aliasing in photographs

This is also known as “moire”

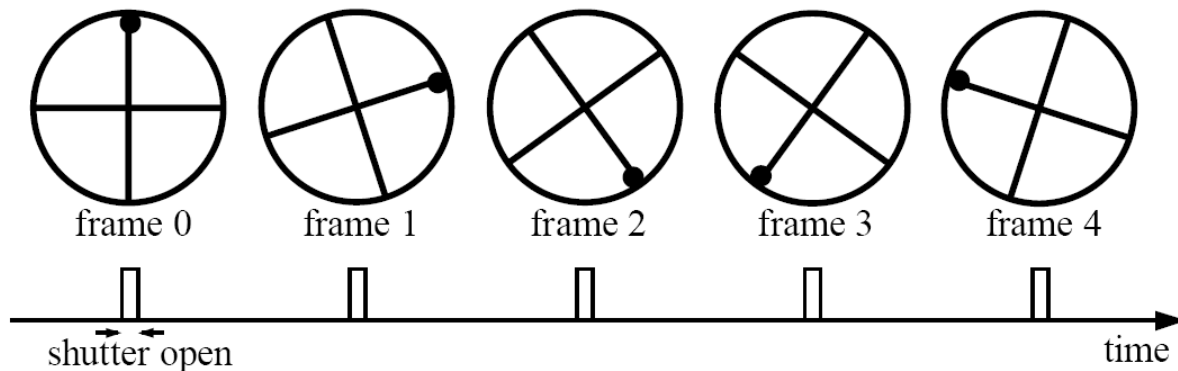


Temporal aliasing

Imagine a spoked wheel moving to the right (rotating clockwise).

Mark wheel with dot so we can see what's happening.

If camera shutter is only open for a fraction of a frame time (frame time = $1/30$ sec. for video, $1/24$ sec. for film):



Without dot, wheel appears to be rotating slowly backwards!
(counterclockwise)

Wagon wheel effect





Sampling and aliasing

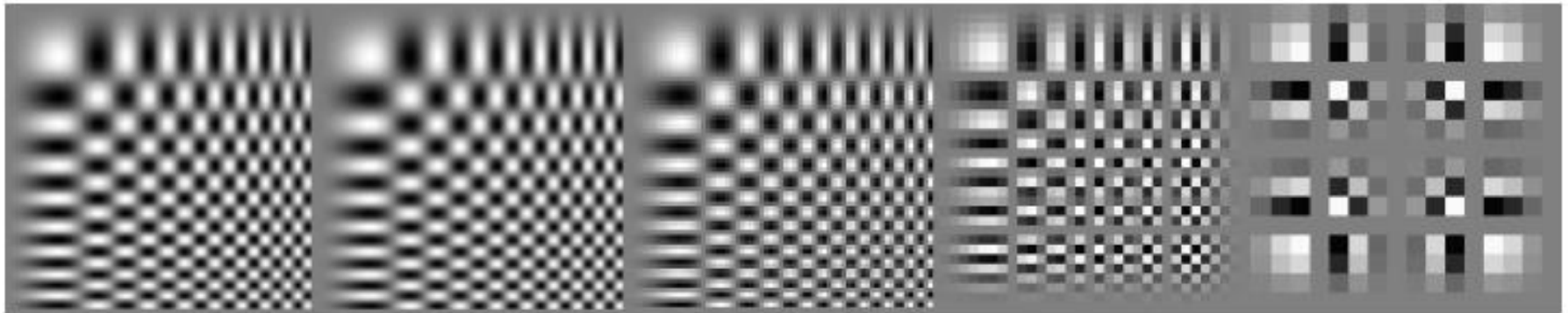
256x256

128x128

64x64

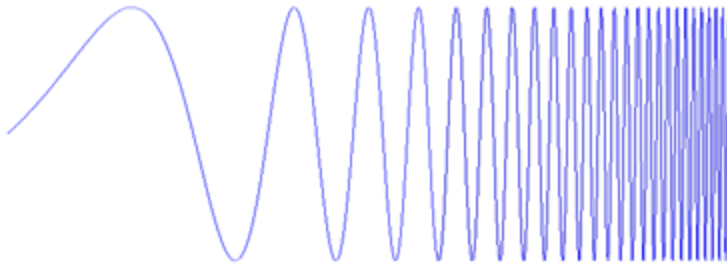
32x32

16x16

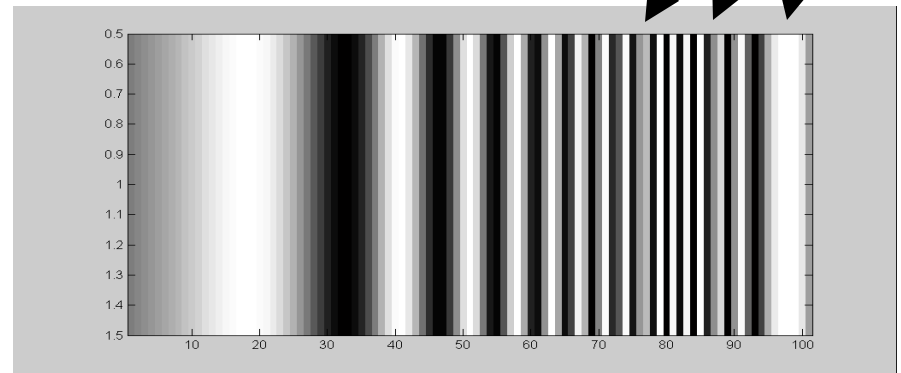


What's happening?

Input signal:



Plot as image:



Aliasing!
Not
enough
samples

```
x = 0:.05:5; plt.imshow(sin((2.^x).*x))
```

Aliasing:

- When two signals become indistinguishable from one another due to sampling.
- They are 'aliases' of one another.

Temporal Aliasing in Videos



Aliasing and Moiré patterns



Gong 96, 1932, Claude Tousignant, Musée des Beaux-Arts de Montréal

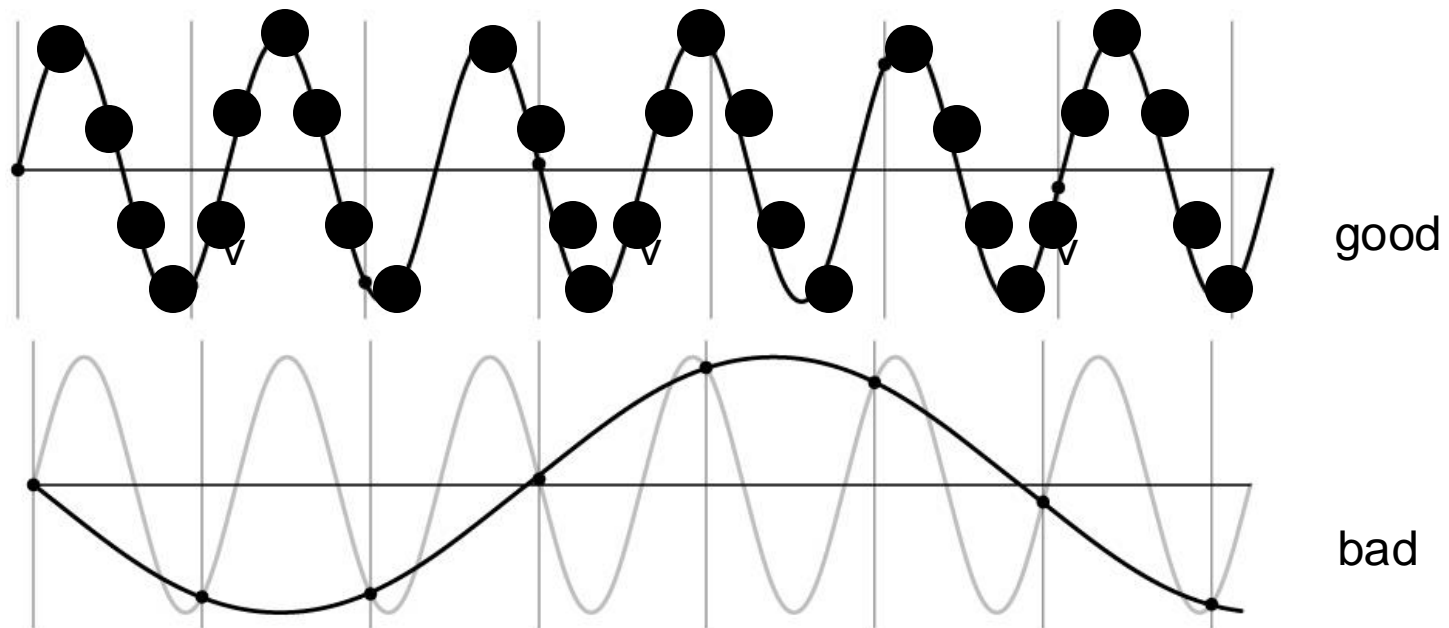


Severe Moiré pattern



Nyquist-Shannon Sampling Theorem

- When sampling a signal at discrete intervals, the sampling frequency must be $\geq 2 \times f_{\max}$
- f_{\max} = max frequency of the input signal
- This allows us to reconstruct the original perfectly from the sampled version



Anti-aliasing

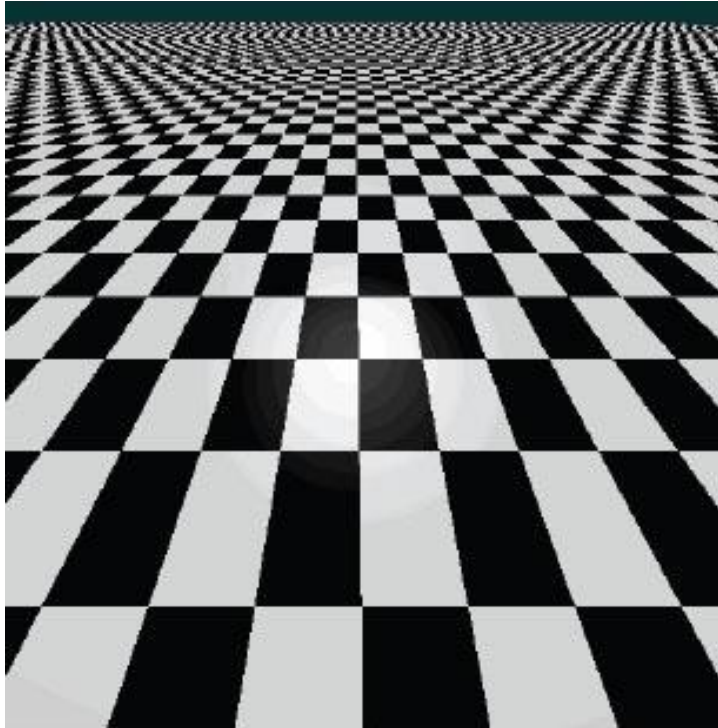
How would you deal with aliasing?

Anti-aliasing

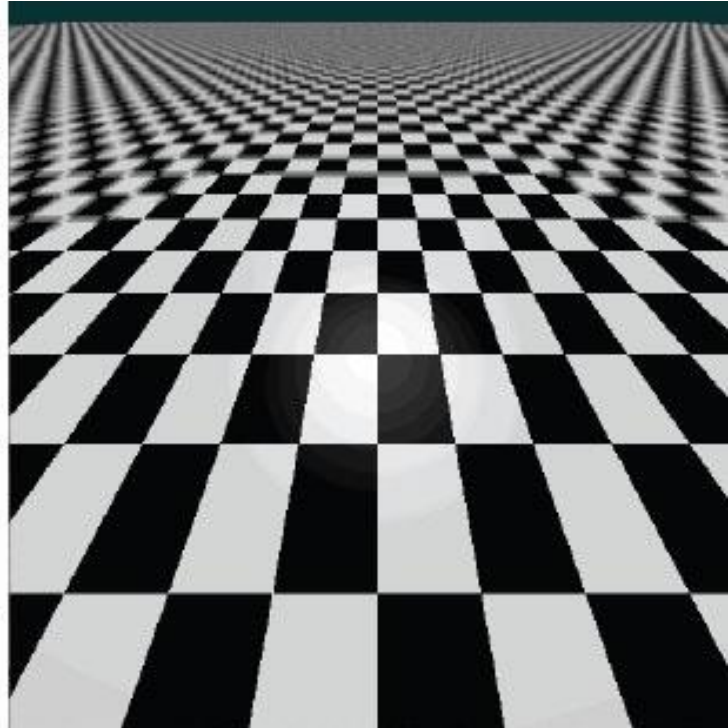
How would you deal with aliasing?

Approach 1: Oversample the signal

Anti-aliasing in textures



aliasing artifacts



anti-aliasing by oversampling

Anti-aliasing

How would you deal with aliasing?

Approach 1: Oversample the signal

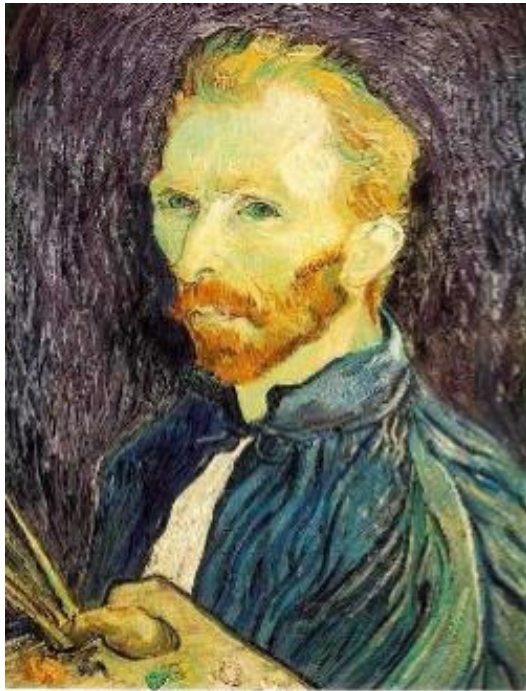
Approach 2: Smooth the signal

- Remove some of the detail effects that cause aliasing.
- Lose information, but better than aliasing artifacts.

How would you smooth a signal?

Better image downsampling

Apply a smoothing filter first, then throw away half the rows and columns



1/2

Gaussian filter
delete even rows
delete even columns



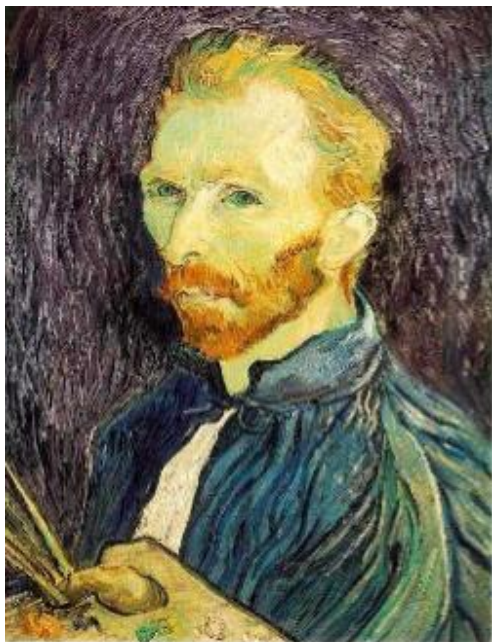
1/4

Gaussian filter
delete even rows
delete even columns



1/8

Better image downsampling



1/2

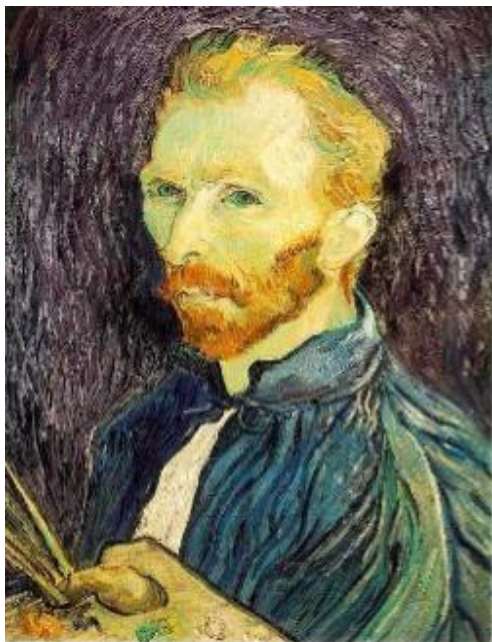


1/4 (2x zoom)



1/8 (4x zoom)

Naïve image downsampling



$1/2$



$1/4$ (2x zoom)



$1/8$ (4x zoom)

Anti-aliasing

Question 1: How much smoothing do I need to do to avoid aliasing?

Question 2: How many samples do I need to take to avoid aliasing?

Answer to both: Enough to reach the Nyquist limit.

Low-pass and high-pass filtering

Remove high frequencies with a *low pass* filter

- A blur filter!
- *Could also be called a 'high cut' filter (but nobody does)*

Low-pass and high-pass filtering

Remove high frequencies with a *low pass* filter

- A blur filter!
- *Could also be called a ‘high cut’ filter (but nobody does)*

Counterpart: *high pass* filter

- Only keeps the high frequencies
- Edge detection (Sobel) is an example high pass filter

Related: *band pass / band stop (or notch)* filter

- Only affect *specific* frequencies
- How could we construct one with linear filters?

Anti-aliasing

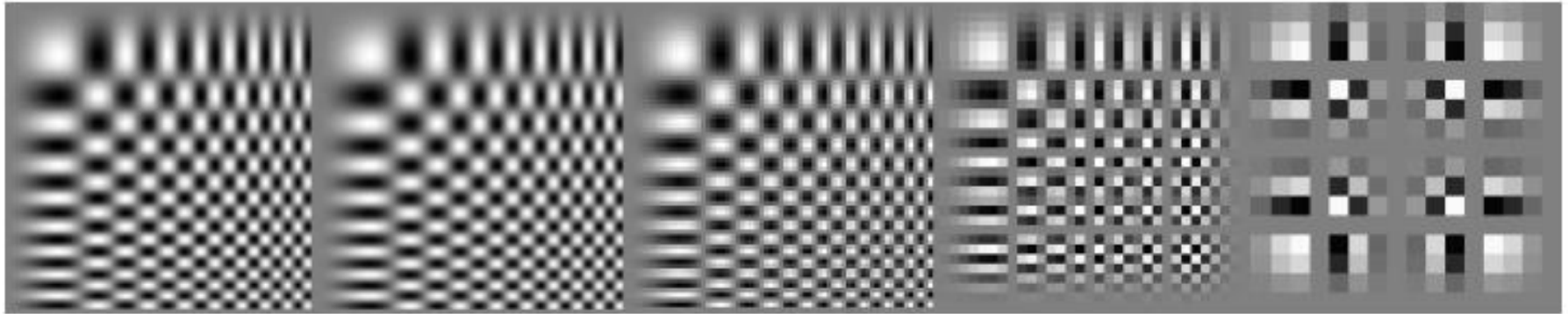
256x256

128x128

64x64

32x32

16x16



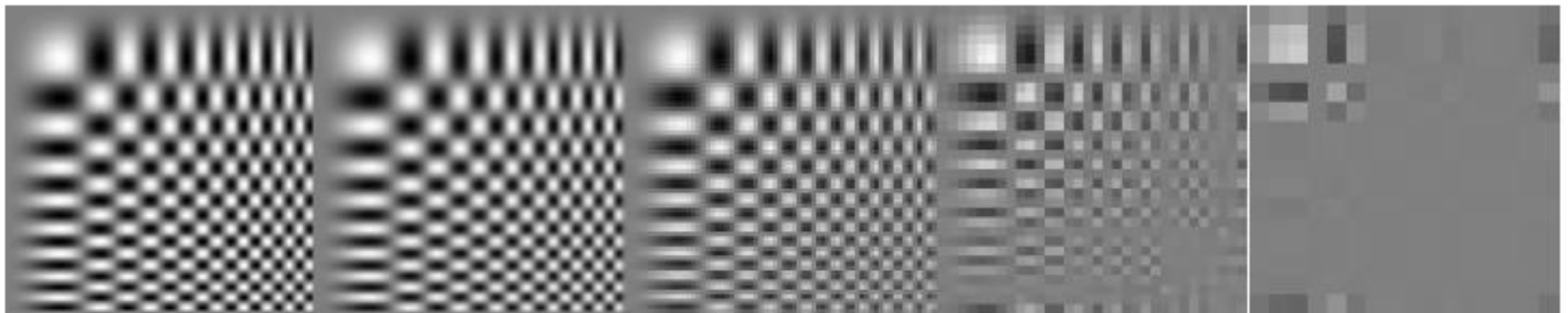
256x256

128x128

64x64

32x32

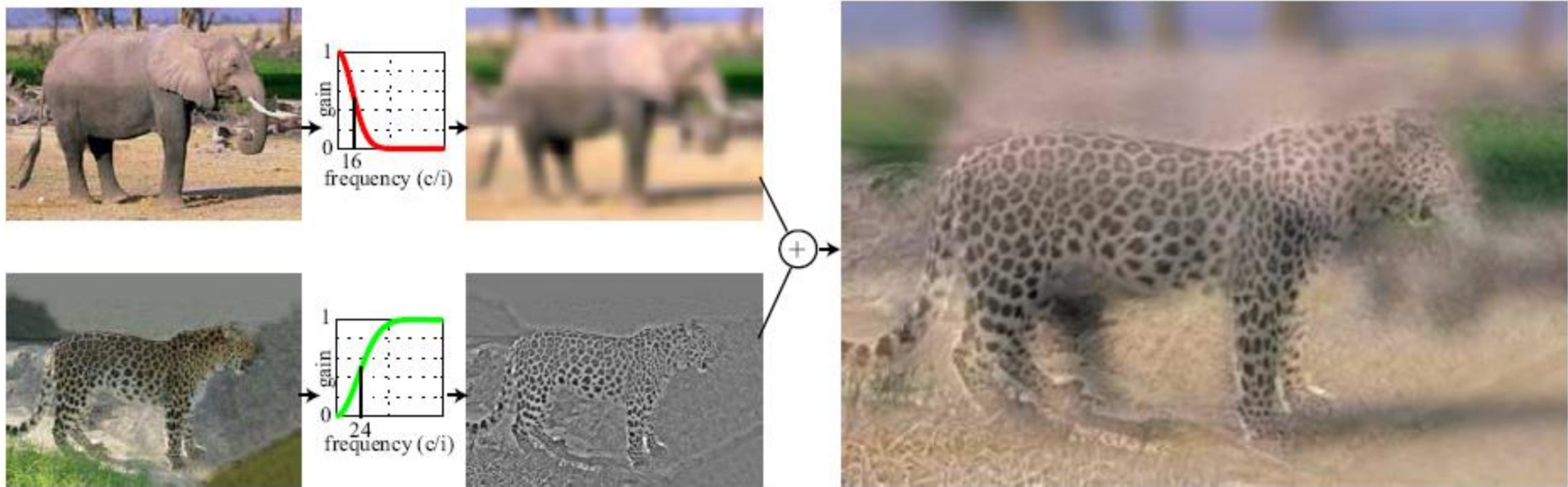
16x16



Algorithm for downsampling by factor of 2

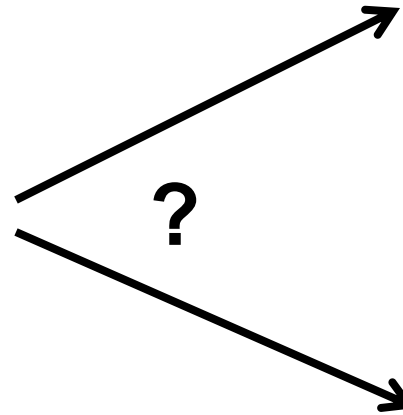
1. Start with image(h, w)
2. Apply low-pass filter
`im_blur = imfilter(image, fspecial('gaussian', 7, 1))`
3. Sample every other pixel
`im_small = im_blur(1:2:end, 1:2:end);`

Hybrid Images



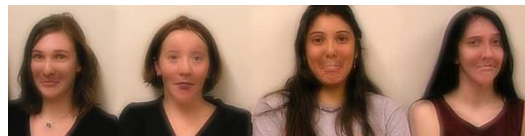
A. Oliva, A. Torralba, P.G. Schyns,
["Hybrid Images,"](#) SIGGRAPH 2006

Why do we get different, distance-dependent interpretations of hybrid images?



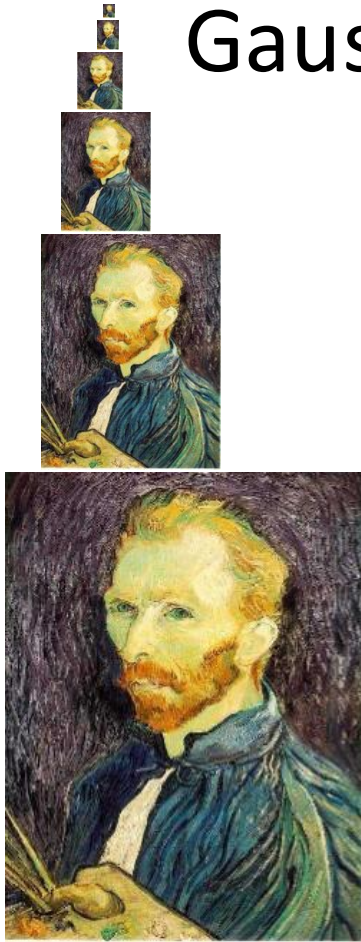
Application: Hybrid Images

When we see an image from far away, we are effectively subsampling it!



A. Oliva, A. Torralba, P.G. Schyns, SIGGRAPH 2006

Gaussian image pyramid



Gaussian image pyramid

The name of this sequence of subsampled images

Constructing a Gaussian pyramid

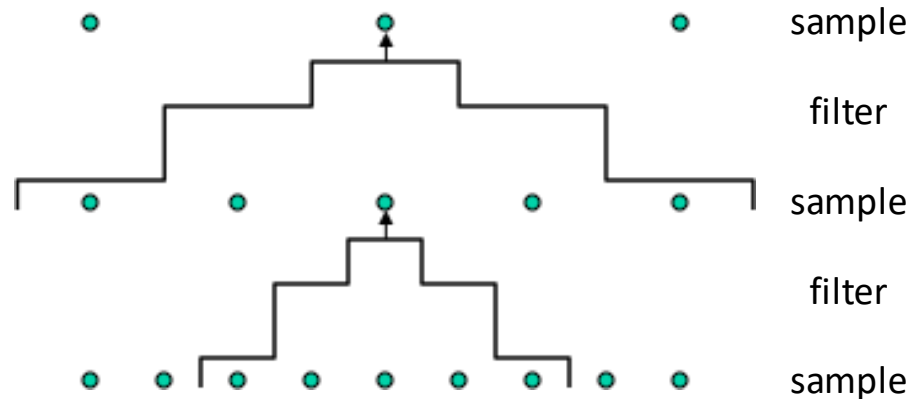
Algorithm

repeat:

 filter

 subsample

until min resolution
reached



Question: How much bigger than the original image is the whole pyramid?

Constructing a Gaussian pyramid

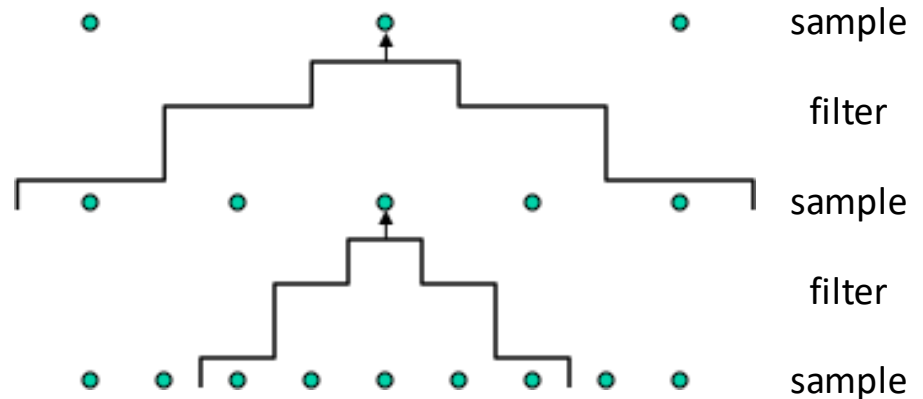
Algorithm

repeat:

 filter

 subsample

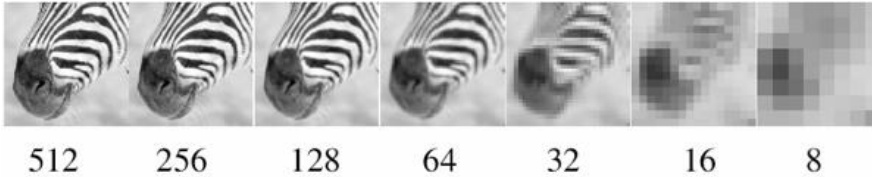
until min resolution
reached



Question: How much bigger than the original image is the whole pyramid?

Answer: Just $\frac{4}{3}$ times the size of the original image! (How did I come up with this number?)

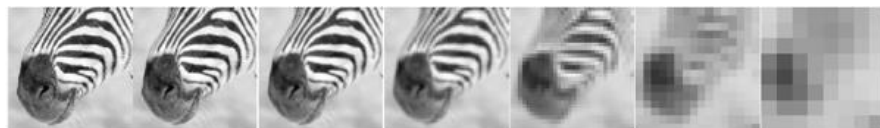
Some properties of the Gaussian pyramid



What happens to the details of the image?



Some properties of the Gaussian pyramid



512 256 128 64 32 16 8

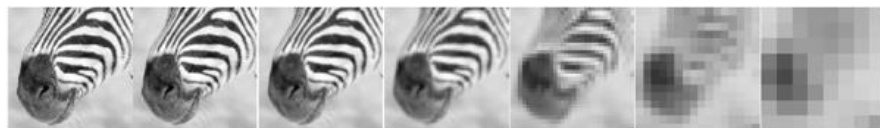
What happens to the details of the image?

- They get smoothed out as we move to higher levels.



What is preserved at the higher levels?

Some properties of the Gaussian pyramid



512 256 128 64 32 16 8



What happens to the details of the image?

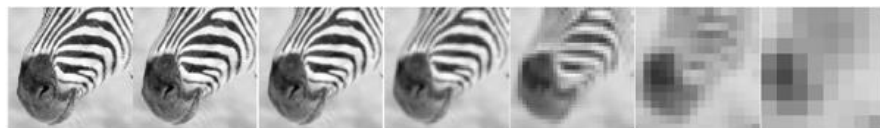
- They get smoothed out as we move to higher levels.

What is preserved at the higher levels?

- Mostly large uniform regions in the original image.

How would you reconstruct the original image from the image at the upper level?

Some properties of the Gaussian pyramid



512 256 128 64 32 16 8



What happens to the details of the image?

- They get smoothed out as we move to higher levels.

What is preserved at the higher levels?

- Mostly large uniform regions in the original image.

How would you reconstruct the original image from the image at the upper level?

- That's not possible.

Blurring is lossy



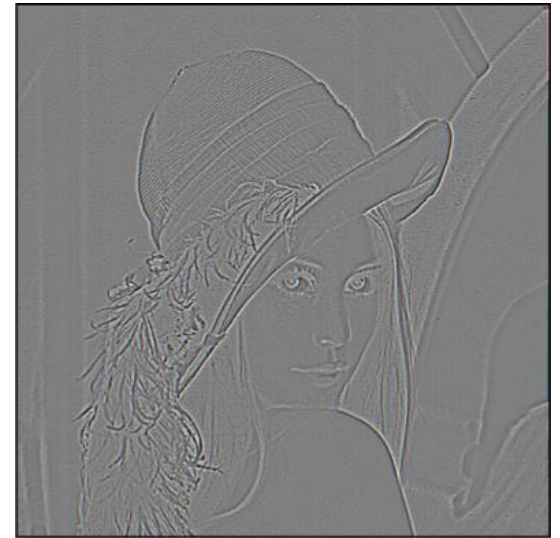
level 0

-



level 1 (before downsampling)

=



residual

What does the residual look like?

Blurring is lossy



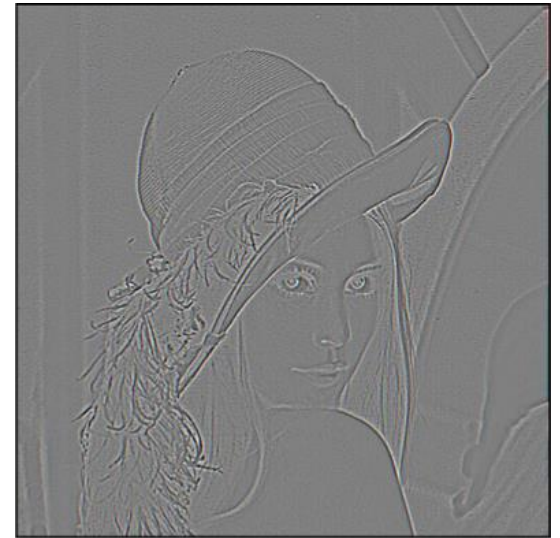
level 0

-



level 1 (before downsampling)

=

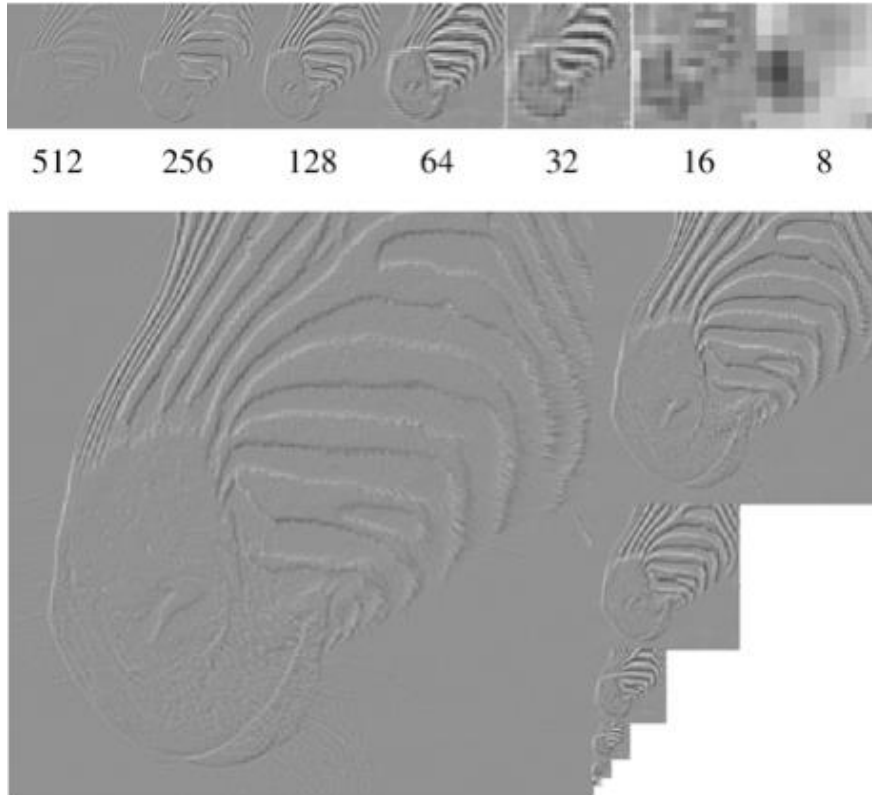


residual

Can we make a pyramid that is lossless?

Laplacian image pyramid

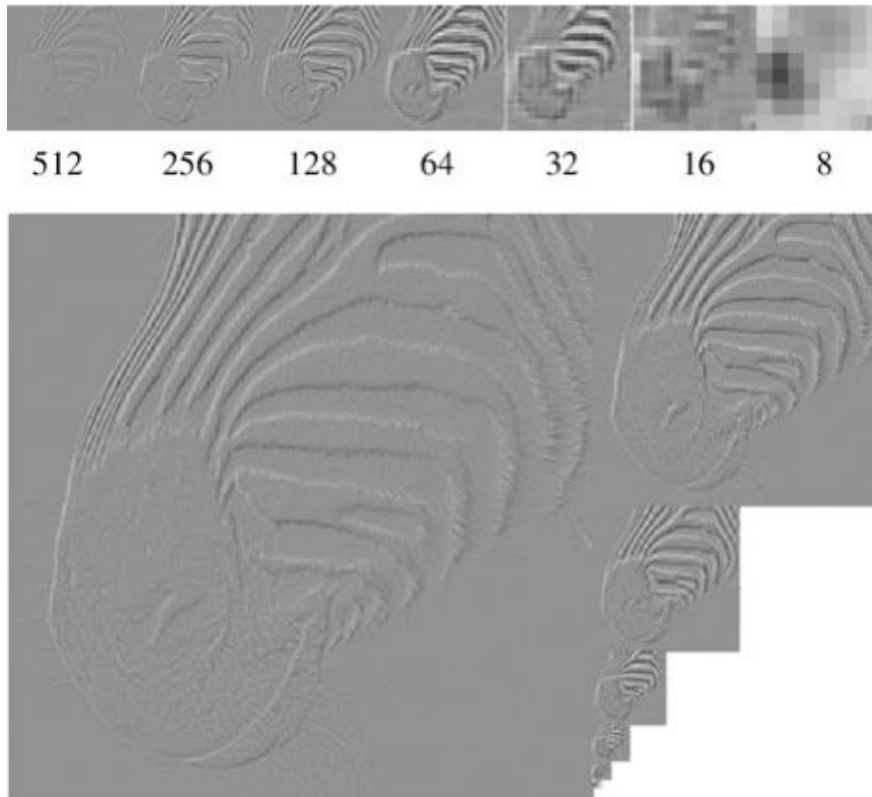
Laplacian image pyramid



At each level, retain the residuals instead of the blurred images themselves.

Can we reconstruct the original image using the pyramid?

Laplacian image pyramid



At each level, retain the residuals instead of the blurred images themselves.

Can we reconstruct the original image using the pyramid?

- Yes we can!



What do we need to store to be able to reconstruct the original image?

Let's start by looking at just one level



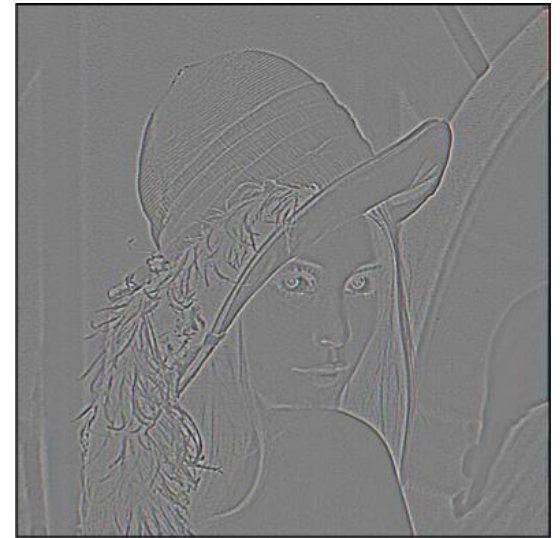
level 0

=



level 1 (upsampled)

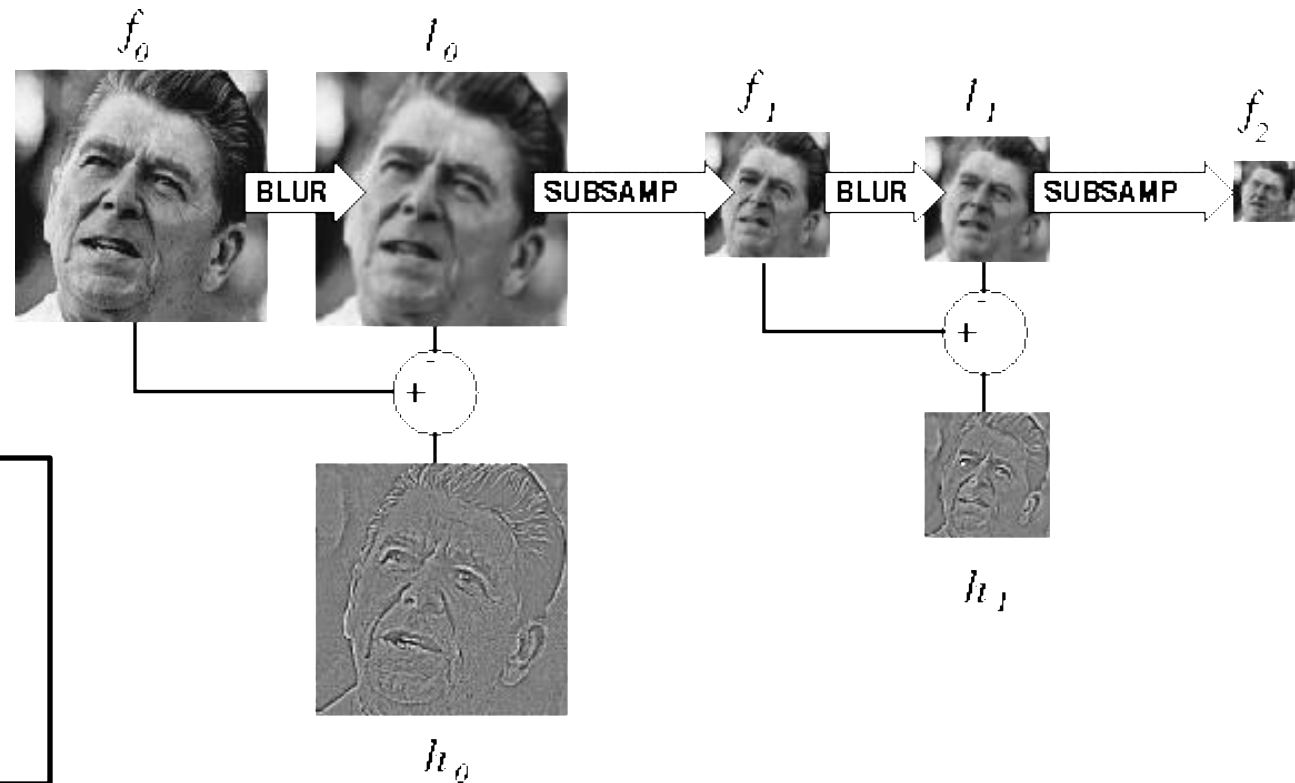
+



residual

Does this mean we need to store both residuals and the blurred copies of the original?

Constructing a Laplacian pyramid

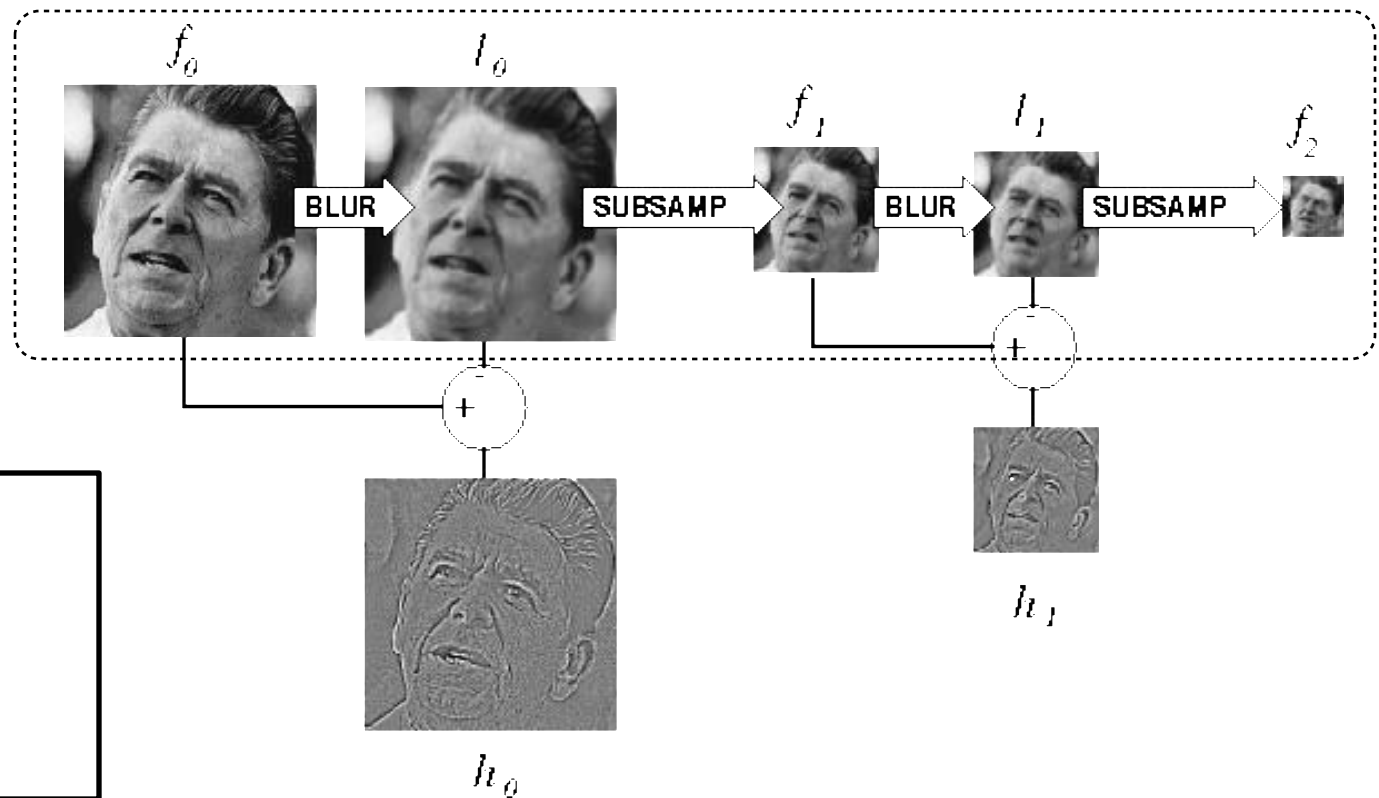


Algorithm

```
repeat:  
    filter  
    compute residual  
    subsample  
until min resolution  
reached
```

Constructing a Laplacian pyramid

What is this part?

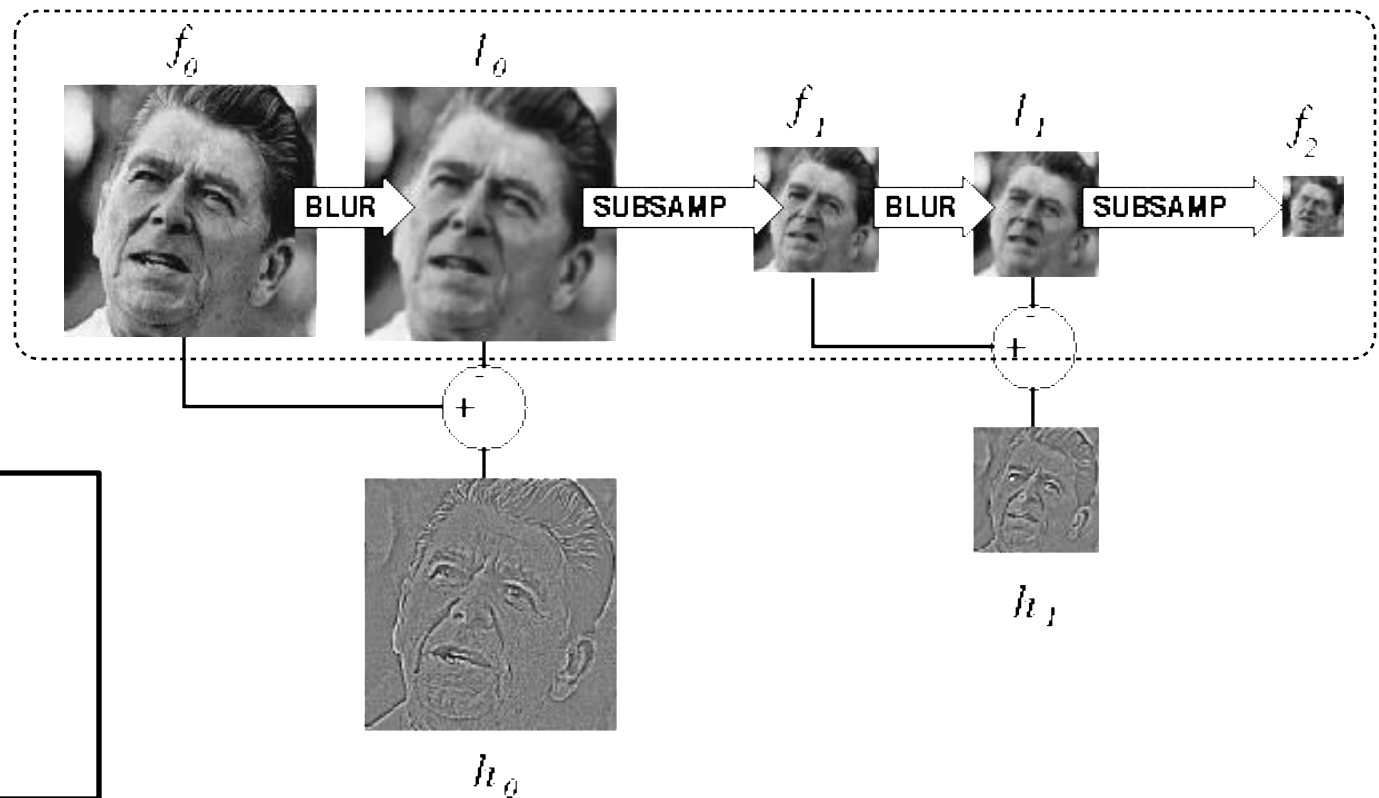


Algorithm

```
repeat:  
  filter  
  compute residual  
  subsample  
until min resolution  
reached
```

Constructing a Laplacian pyramid

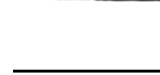
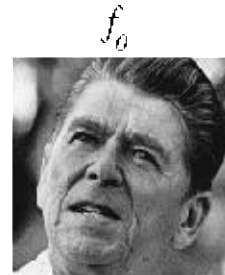
It's a Gaussian pyramid.



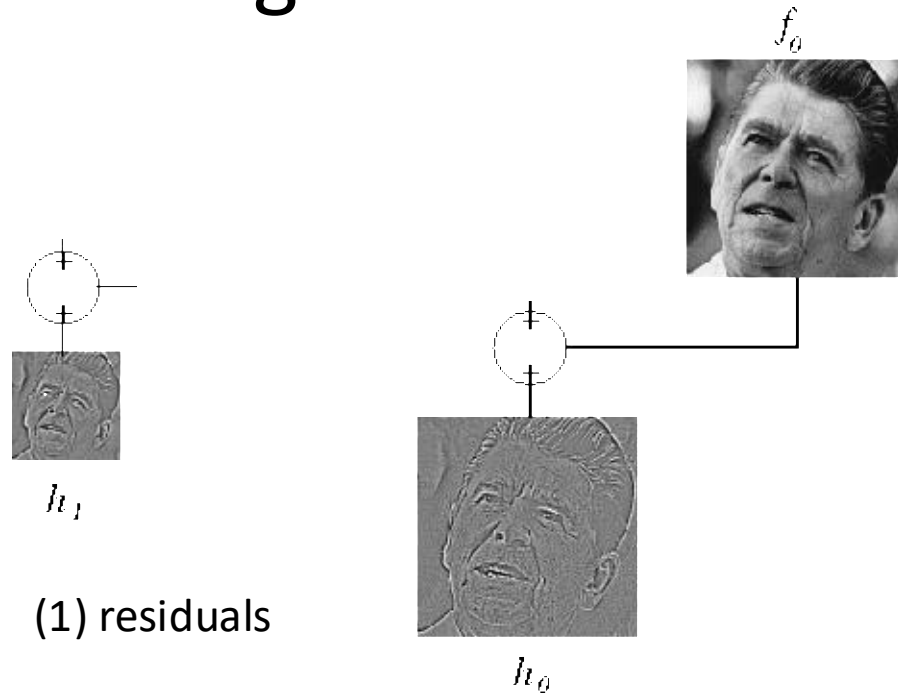
Algorithm

```
repeat:
  filter
  compute residual
  subsample
until min resolution
reached
```

What do we need to construct the original image?



What do we need to construct the original image?



What do we need to construct the original image?

(2) smallest image f_2



h_1

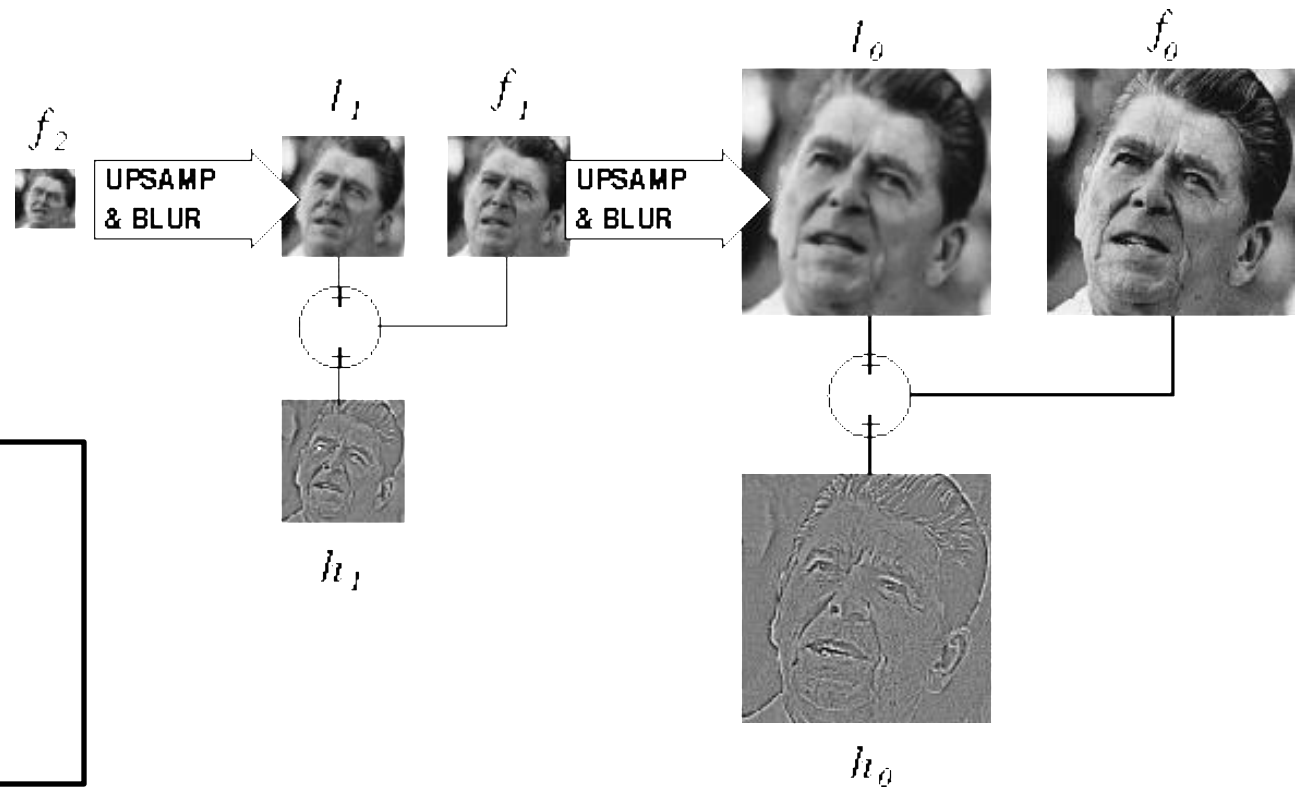
(1) residuals



h_0



Reconstructing the original image



Algorithm

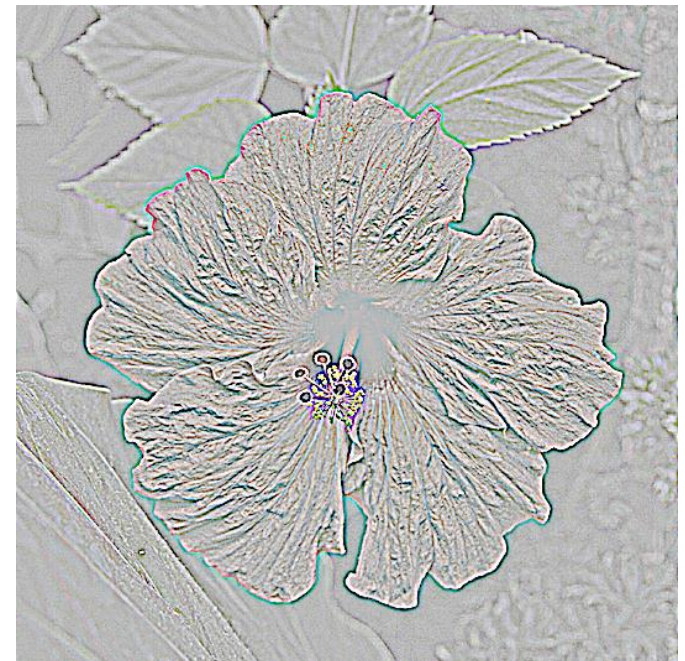
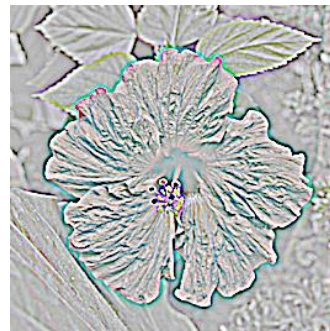
```
repeat:  
    upsample  
    sum with residual  
until orig resolution  
reached
```

Gaussian vs Laplacian Pyramid



Shown in opposite order for space.

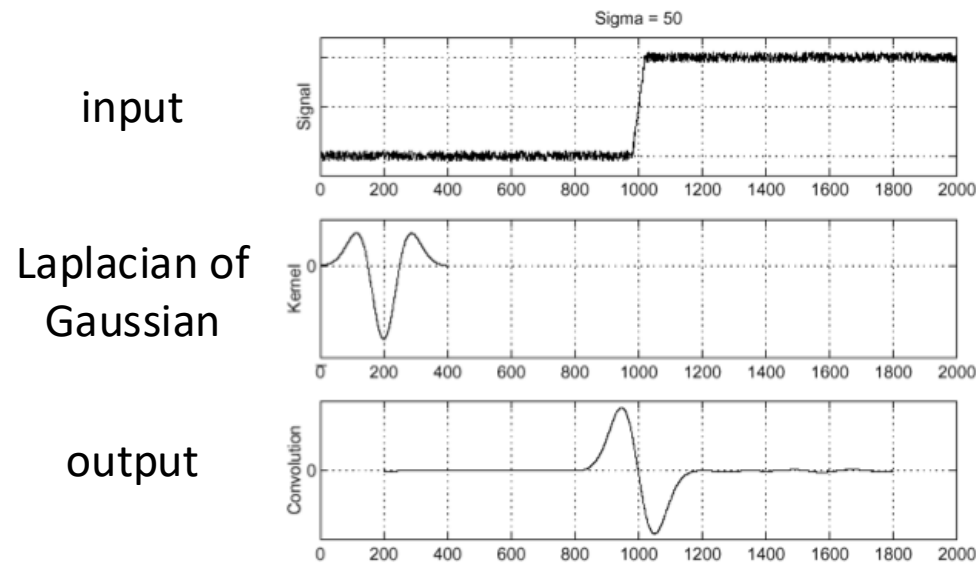
Which one takes more space to store?



Why is it called a Laplacian pyramid?

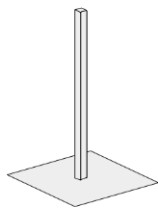
Reminder: Laplacian of Gaussian (LoG) filter

As with derivative, we can combine Laplace filtering with Gaussian filtering

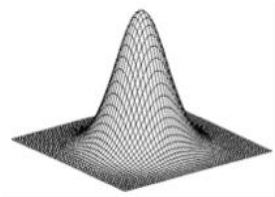


“zero crossings” at edges

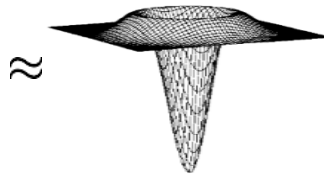
Why is it called a Laplacian pyramid?



unit

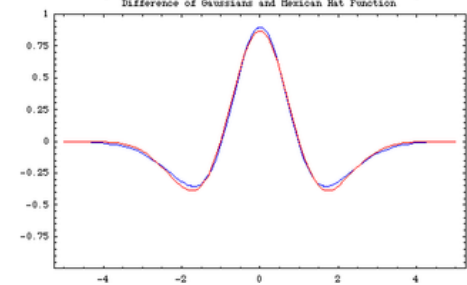
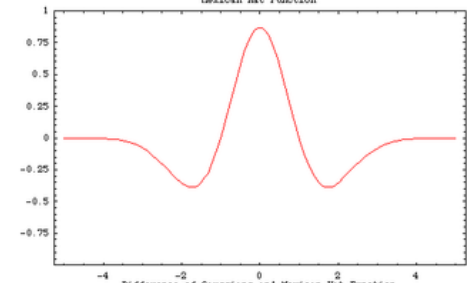
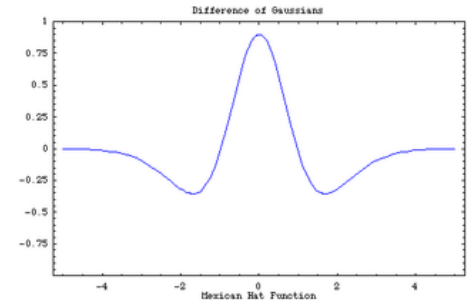


Gaussian

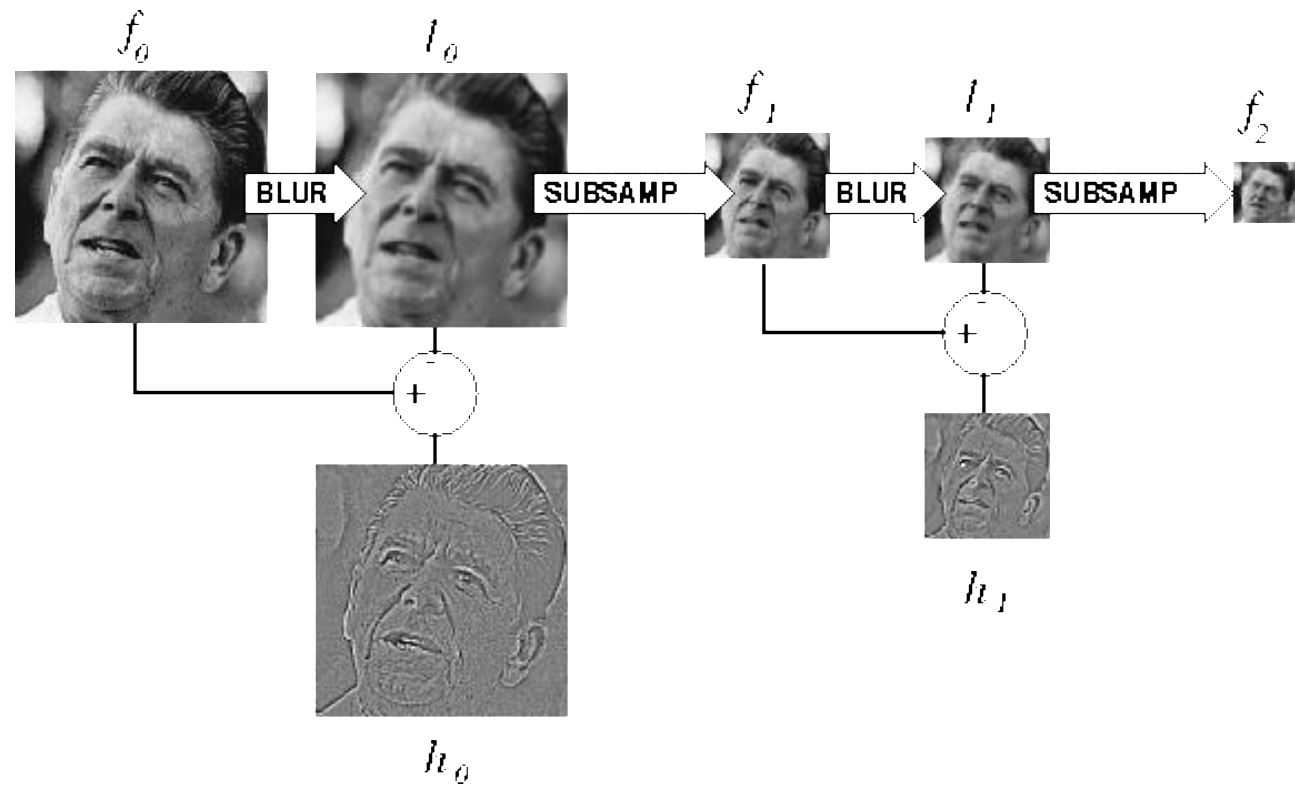


Laplacian

Difference of Gaussians approximates the Laplacian

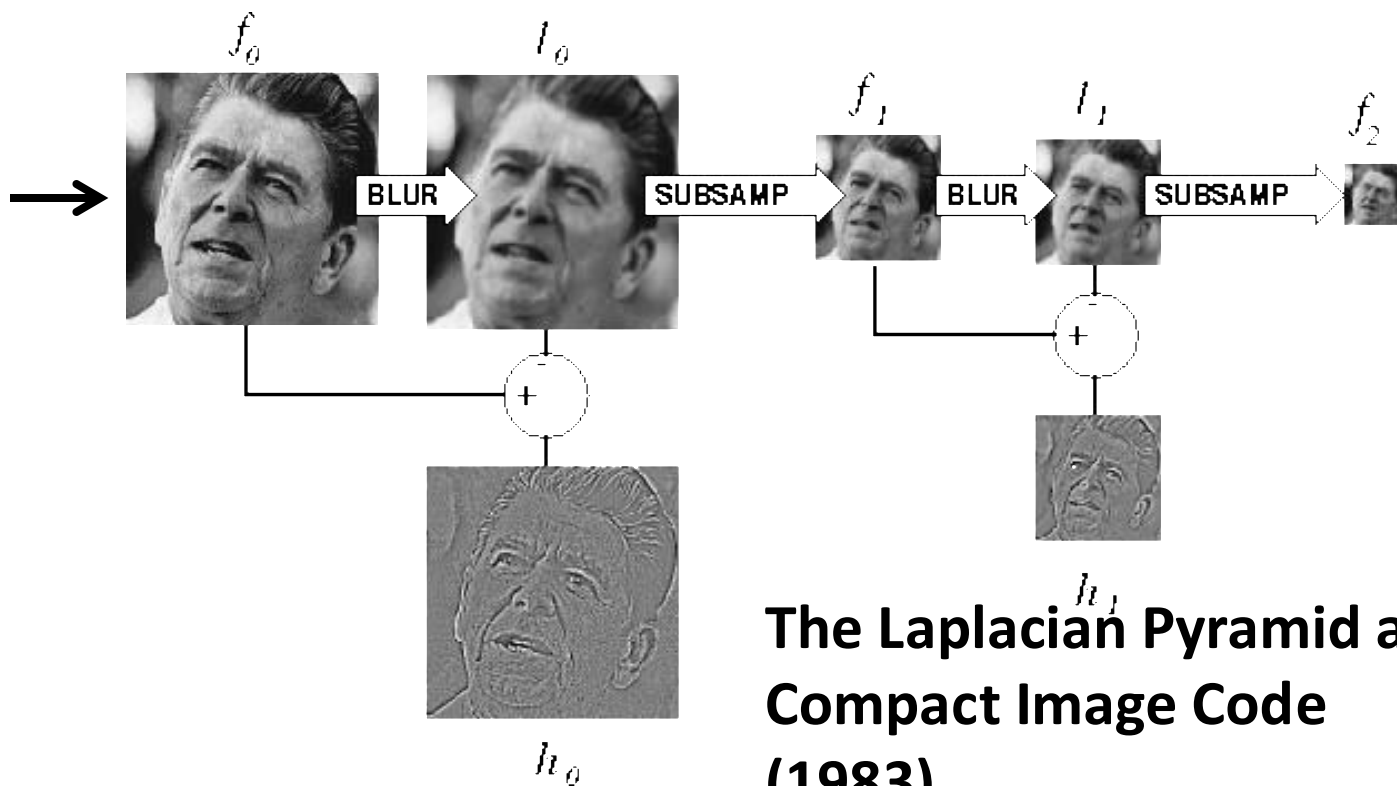


Why Reagan?



Why Reagan?

Ronald Reagan was
President when the
Laplacian pyramid
was invented



**The Laplacian Pyramid as a
Compact Image Code
(1983)**

Peter J. Burt , Edward H.
Adelson

Still used extensively



Still used extensively



foreground details enhanced, background details reduced



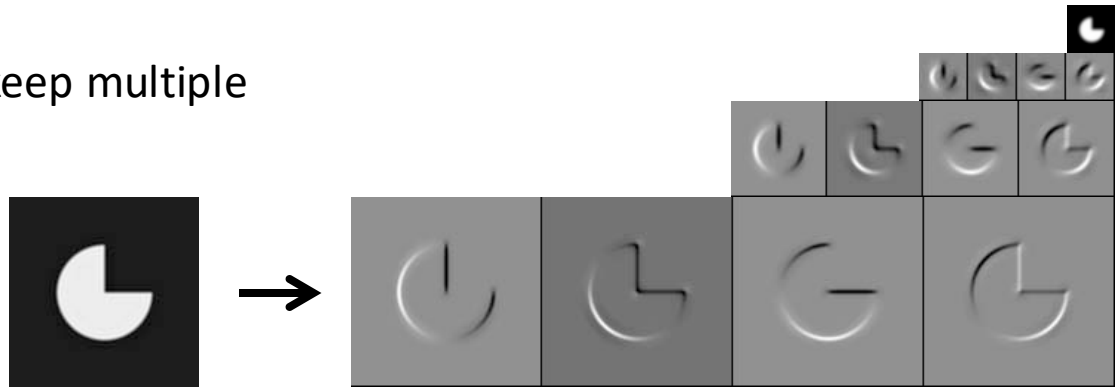
input image



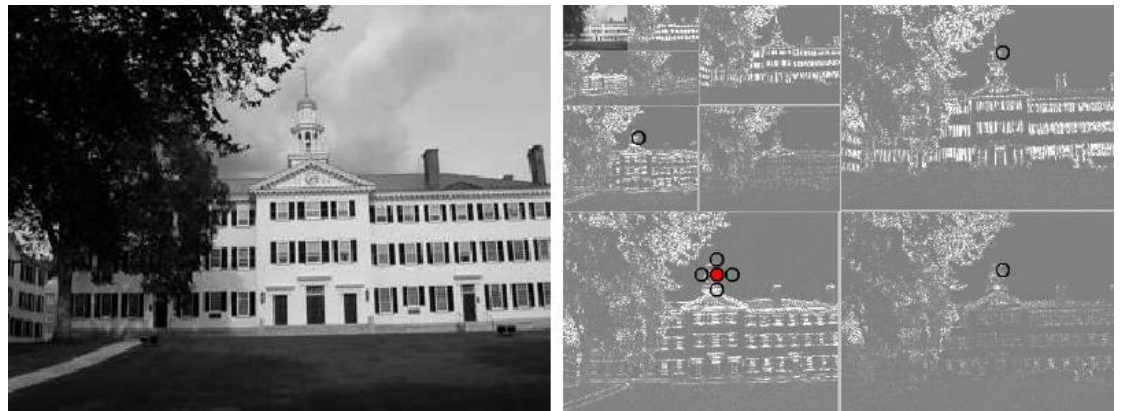
user-provided mask

Other types of pyramids

Steerable pyramid: At each level keep multiple versions, one for each direction.



Wavelets: Huge area in image processing (see 18-793).



What are image pyramids used for?

image compression



multi-scale
texture mapping

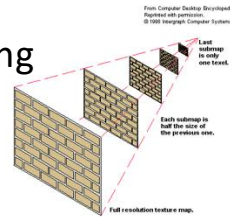
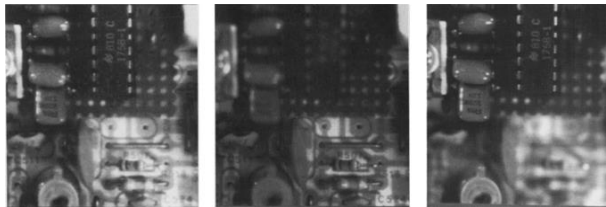


image blending



focal stack compositing



denoising



multi-scale detection



multi-scale registration

