

Knowledge-Based Agents

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Agenda

Knowledge-Based Agents

Core Concepts

Propositional Logic

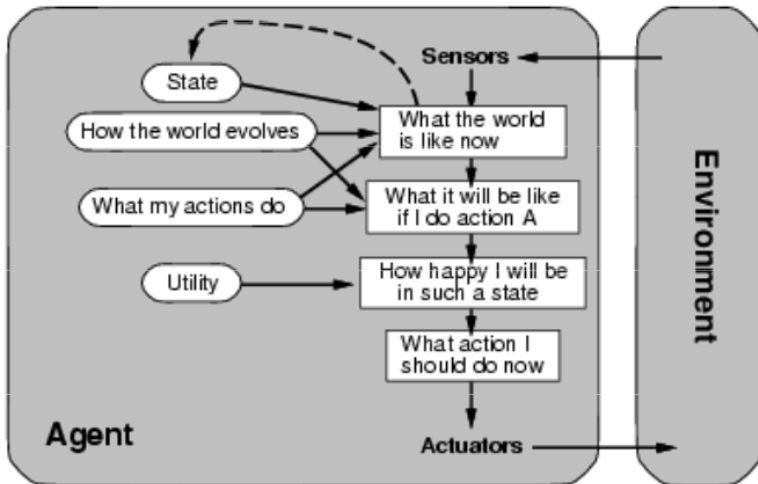
Debugging

Knowledge-Based Agents

Representations

- ▶ Atomic (Search)
- ▶ Factored (Constraints)
- ▶ **Structured** (TBD)

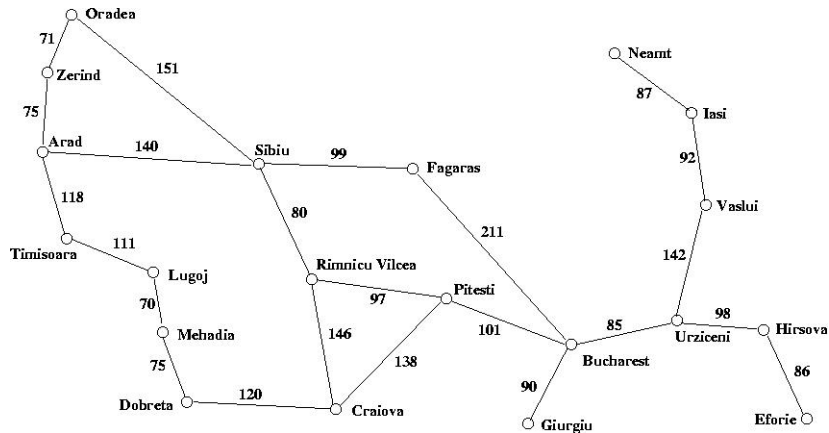
An Agent



The Goal

- ▶ Domain-General *Reasoning*,
- ▶ Applied to Domain-Specific *Knowledge*
- ▶ (In a Domain-General *Representation*)

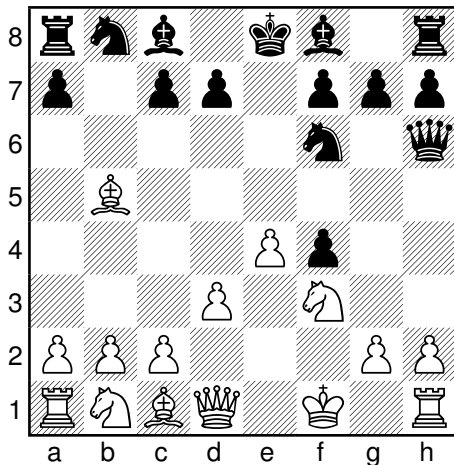
Implicit



Implicit

```
1  road(oradea,    zerind,    71).
2  road(zerind,    arad,      75).
3
4  city(arad,      46.16667, 21.3).
5  city(bucharest, 44.41667, 26.1).
6
7  twoWayRoad(City1, City2, Distance):-
8      road(City1, City2, Distance).
9  twoWayRoad(City1, City2, Distance):-
10     road(City2, City1, Distance).
11
12 move(City1, City2):- twoWayRoad(City1, City2, _).
13
14 move(City1, City2, Distance):-
15     twoWayRoad(City1, City2, Distance).
```


Chess Examples



1. C3.is clear
2. B3.is clear
3. A3.is clear
4. WKn1 in b1
5. Can move WKn1 to C3
6. \neg can move WQ to C3

Types of Reasoning

- ▶ Knowledge Representations:
 - ▶ Logic: propositional, predicate, temporal, fuzzy, probabilistic, etc. etc.
 - ▶ Networks of all kinds, including so-called Semantic Networks
 - ▶ Frames
 - ▶ Semantic Web: RDF, OWL, XML, etc.
 - ▶ English, Swahili, Urdu, etc. (for humans).
- ▶ Reasoning:
 - ▶ Logical inference
 - ▶ Temporal reasoning
 - ▶ Graph/subgraph matching
 - ▶ Analogical reasoning
 - ▶ Probabilistic inference

Assessment Criteria

► Assessment Criteria

- **Representational Adequacy**: the ability to represent *sufficient* kinds of knowledge in the domain.
- **Acquisitional Efficiency**: the ability to *easily* and *quickly* represent new knowledge in the formalism.

► Reasoning Methods

- **Inferential Adequacy**: the ability to manipulate representational structures to derive sufficient new ones
- **Inferential Efficiency**: the ability to derive new representational structures quickly

KB-Based Agent: Schema

```
1  class KB_Agent:
2      Knowledge_Base = {...}
3      Curr_Time      = 0
4
5      def get_action(Percept):
6          Percept_Seq = make_percept_sequence(
7              Percept, self.Curr_time)
8          tell(self.Knowledge_Base, Percept_Seq)
9          Query = make_action_query(self.Curr_Time)
10         Act = ask(self.Knowledge_Base, Query)
11         Act_Seq = make_action_sequence(
12             Act, self.Curr_Time)
13         tell(self.Knowledge_Base, Act_Seq)
14         self.Curr_Time += 1
15         return Act
```

Expert Systems

ANDES Physics Workbench - [s2e-Solution]

File Edit Diagram Variable View Help

A spherical ball with a mass of 2.00 kg rests in the notch shown below. If there is no friction between the ball and the walls, what is the magnitude of the force exerted on the ball by wall1?

Answer:

Variables

Name	Definition	Dir
T0	the instant depicted	
m=2 kg	mass of ball	
x	axis	$\theta x=0^\circ$
Fg	magnitude of the Weight Force on...	$\theta Fg...$
F1	magnitude of the Normal Force on...	$\theta F1...$
a	magnitude of the instantaneous A...	

1. $F_{g,y} + F_{1,y} = 0$

2.

3.

4.

5.

6.

7.

8.

9.

T: There is a force acting on the ball at T0 that you have not yet drawn.
Explain further OK

T: Notice that the ball is supported by a surface: wall2.
Explain further OK

T: When an object is supported by a surface, the surface exerts a normal force on it. The normal

For Help, press F1

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Image Credit: ubiquity.acm.org

Core Concepts

The basics

- ▶ *Statements* Individual facts, percepts, or information.
- ▶ *Knowledge* The *integration* of those statements to support reasoning.
- ▶ *Inference* The *induction* of new knowledge or *decisionmaking*.

Andes

ANDES Physics Workbench - [s2e-Solution]

File Edit Diagram Variable View Help

A spherical ball with a mass of 2.00 kg rests in the notch shown below. If there is no friction between the ball and the walls, what is the magnitude of the force exerted on the ball by wall1?

Answer:

$a=0$

Variables

Name	Definition	Dir
T0	the instant depicted	
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For Help, press F1

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Image Credit: ubiquity.acm.org

Problem

A spherical ball with a mass of 2.00 kg rests in the notch shown below. If there is no friction between the ball and the walls, what is the magnitude of the force exerted on the ball by wall1?

KB

- ▶ (DRAW-AXES 40)
- ▶ (EQN (= |Yc_Fn_BALL_WALL2_1_40| 0))
- ▶ (IMPLICIT-EQN (= |OFn_BALL_WALL2_1| (DNUM 40 |deg|)))
- ▶ (VECTOR (FORCE BALL WALL2 NORMAL :TIME 1) (DNUM 40 |deg|))
- ▶ (DEFINE-VAR (MASS BALL))
- ▶ (EQN (= |Yc_Fw_BALL_EARTH_1_40|
(* |Fw_BALL_EARTH_1| (SIN (- (DNUM 270 |deg|)
(DNUM 40 |deg|))))))

The basics

- ▶ **Sentences** (*statements*) in the knowledge base.
- ▶ **Syntax**: rules for well formed sentences.
- ▶ **Semantics**: rules for the meaning of the sentence or *truth in each possible world*.
- ▶ Sentences must be true *XOR* false in each possible world.
- ▶ **Model**: A fixed assignment of values to all possible sentences (possible world).
- ▶ A sentence **S** **satisfies** a model if it is true in it.
- ▶ **M is a model of S** if S satisfies it.

Propositional Logic

Basic Elements

- ▶ Set P of *propositional symbols*: p, q, r , etc.
- ▶ Two *truth values*: true, false
- ▶ *Logical Symbols*: $\neg, \wedge, \vee, \Rightarrow, \Leftrightarrow, \Box$
- ▶ *Punctuation*: $(), [], \{ \}$.

Propositions

- ▶ A symbol: a
- ▶ a negated proposition: $\neg P$
- ▶ Conjunction or Disjunction: $P_1 \wedge P_2, P_1 \vee P_2$
- ▶ An implication: $P_1 \Rightarrow P_2$
- ▶ A logical equivalence: $P_1 \Leftrightarrow P_2$.
- ▶ Note: Implication is not causation!

Semantics

- ▶ An *interpretation* is a specification of values (t—f) for all symbols:

$$m_i = \{s_0 = t, s_1 = f, \dots\} \quad (1)$$

- ▶ Sentence values are constructed *recursively* from symbols up.
- ▶ Or stored in truth-tables.
- ▶ A model for a proposition (p) is an interpretation in which p is true.
- ▶ A proposition p is *valid* if for any interpretation I , $I \models p$ i.e., every interpretation is a model.

Model Checking

- ▶ p is *satisfiable* if \exists an I s.t. $I \models p$.
- ▶ p is *unsatisfiable* no valid model can be found.
- ▶ Theorem proving can be handled via DFS or rule algorithms.
- ▶ What is wrong with that?

Theorem Proving

- ▶ *Logical Equivalence* $a \equiv b$ iff $(a \models b) \wedge (b \models a)$.
- ▶ *Valid (Tautology)* $\forall m : m \models p$
- ▶ *Deduction Theorem*: $(a \models b)$ iff $(a \rightarrow b)$.
- ▶ Thus: $(a \models b)$ iff $(a \wedge \neg b)$ is unsatisfiable.

Resolution

- ▶ Convert all Knowledge to CNF $((a \vee b \vee \dots) \wedge (c \vee \dots) \wedge \dots)$
- ▶ *Resolve* conflicting clauses to yield new information

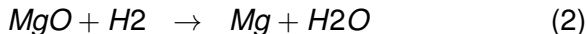
$$\frac{(a \vee b \vee \neg c) \wedge (f \vee c \vee \neg q)}{(a \vee b \vee f \vee \neg q)}$$

- ▶ This process is sound and complete.

Definite & Horn Clauses

- ▶ Resolution is powerful but unnecessary with *Horn Clauses*
- ▶ At most one variable is positive: $(x \vee \neg y \vee \dots)$
- ▶ These can be handled with implications $(p \wedge q) \rightarrow r$
- ▶ Can do Forward-chaining *data-driven* reasoning.
- ▶ And backward-chaining *goal-directed* reasoning.

Example: Chemistry



(5)

Assuming sufficient quantities of MgO, H₂, C, and O₂, prove that we can synthesize H₂CO₃.

Example: Chemistry (Propositional)

$$MgO \wedge H_2 \Rightarrow Mg \wedge H_2O \quad (6)$$

$$C \wedge O_2 \Rightarrow CO_2 \quad (7)$$

$$CO_2 \wedge H_2O \Rightarrow H_2CO_3 \quad (8)$$

$$MgO \quad (9)$$

$$H_2 \quad (10)$$

$$C \quad (11)$$

$$O_2 \quad (12)$$

$$\text{Conclusion} \quad H_2CO_3 \quad (13)$$

Example: Chemistry (CNF)

1. $\neg MgO \vee \neg H2 \vee Mg$

2. $\neg MgO \vee \neg H2 \vee H2O$

3. $\neg C \vee \neg O2 \vee CO2$

4. $\neg CO2 \vee \neg H2O \vee H2CO3$

5. MgO

6. $H2$

7. C

8. $O2$

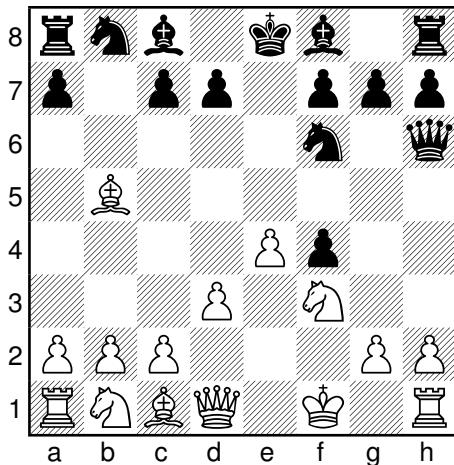
9. $\neg H2CO3$ Negated conclusion

Example: Chemistry (CNF)

- | | | |
|-----|---------------------------------------|--------|
| 10. | $\neg CO_2 \vee \neg H_2O$ | 4 + 9 |
| 11. | $\neg C \vee \neg O_2 \vee \neg H_2O$ | 3 + 10 |
| 12. | $\neg O_2 \vee \neg H_2O$ | 7 + 11 |
| 13. | $\neg H_2O$ | 8 + 12 |
| 14. | $\neg MgO \vee \neg H_2$ | 2 + 13 |
| 15. | $\neg H_2$ | 5 + 14 |
| 16. | \square | 6 + 15 |

Planning & Frames

We can even use this to do planning (sort of)



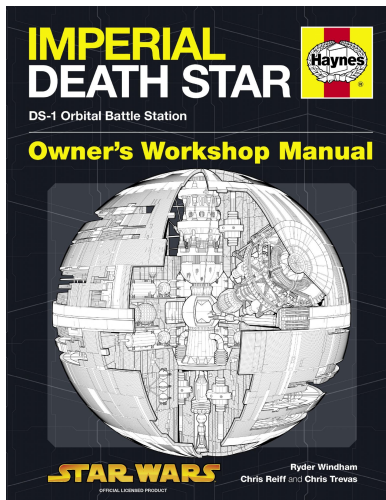
1. $clear_{C3}^{t1}$
2. $clear_{B3}^{t1}$
3. $clear_{A3}^{t1}$
4. $WKn1_{b1}^{t1}$
5. $Move_{Wkn1\ toc3} \Leftrightarrow (WKn1_{b1}^{t1} \wedge clear_{C3}^{t1})$

Debugging

Real Problem: Sherlock

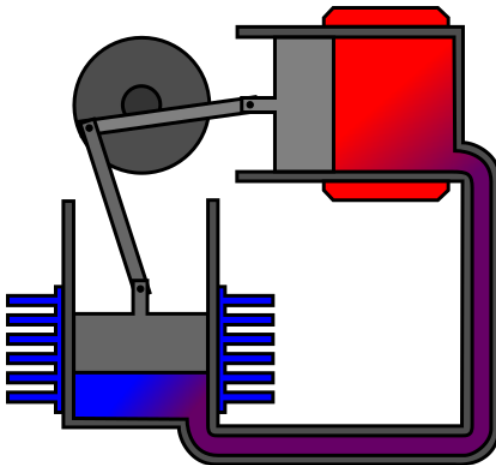
- ▶ The Sherlock system: Lesgold & Katz et al.
- ▶ Teaches basic diagnostic skills through modeling.
- ▶ Uses a logical model of student and system.
- ▶ Saved \$>500k in one instance.

Service Debugging



Source: <http://www.fine1steditions.co.uk>

Basic Piston engine.



Source: https://en.wikipedia.org/wiki/File:Alpha_Stirling_frame_12.svg