

Recap

Reconstruction

Topics for this session

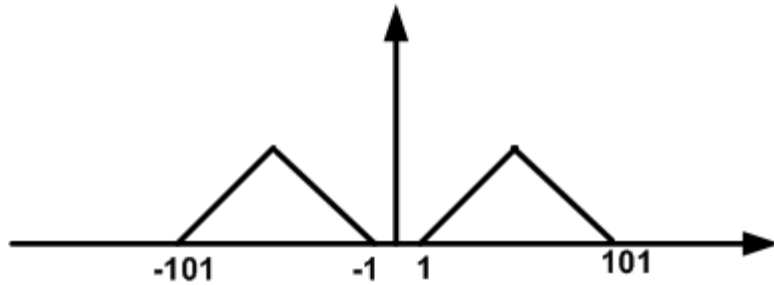
Quadrature sampling of band-pass signals

*Sampling of Band pass signals – software/digital radio used
to receive AM or FM signals*

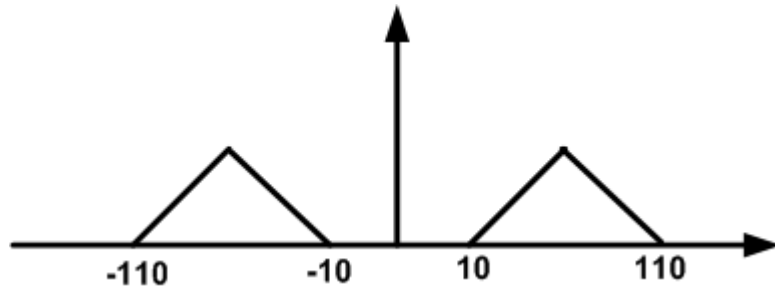
- Output of modulation
- For reconstruction $f_s \geq \text{Nyquist rate}$

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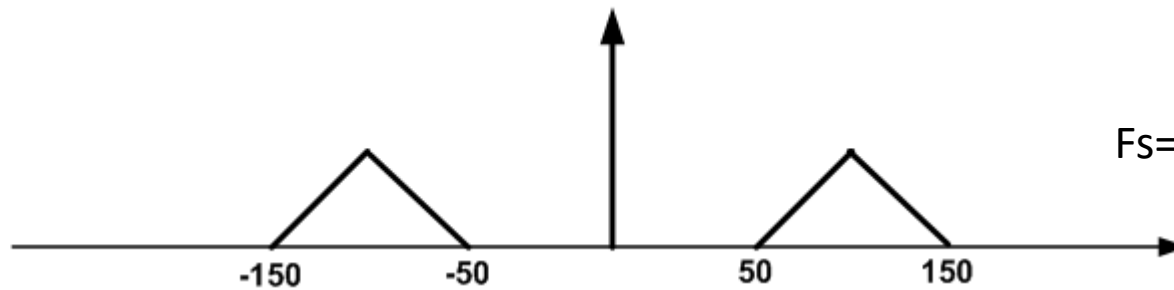
Quadrature Sampling of Band-pass signals



$F_s=202$



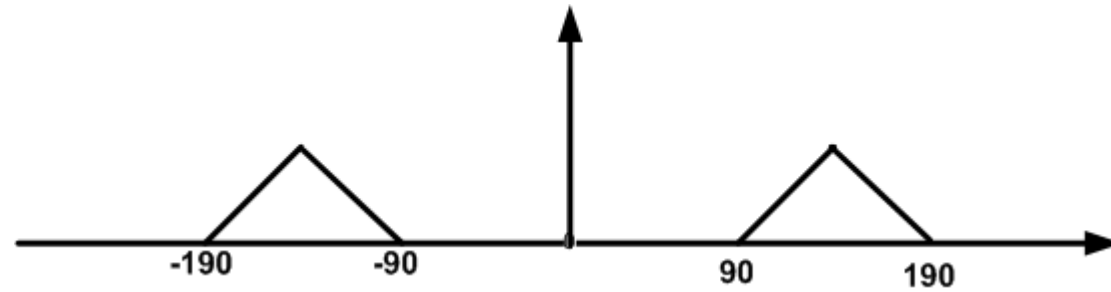
$F_s=220$



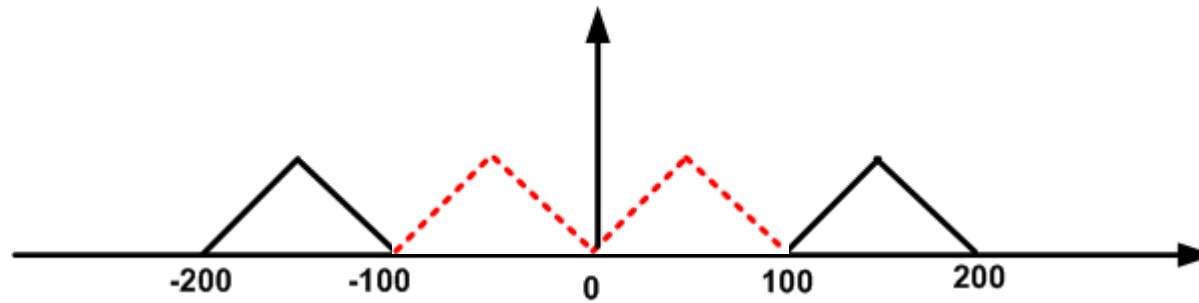
$F_s=300$

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Quadrature Sampling of Band-pass signals

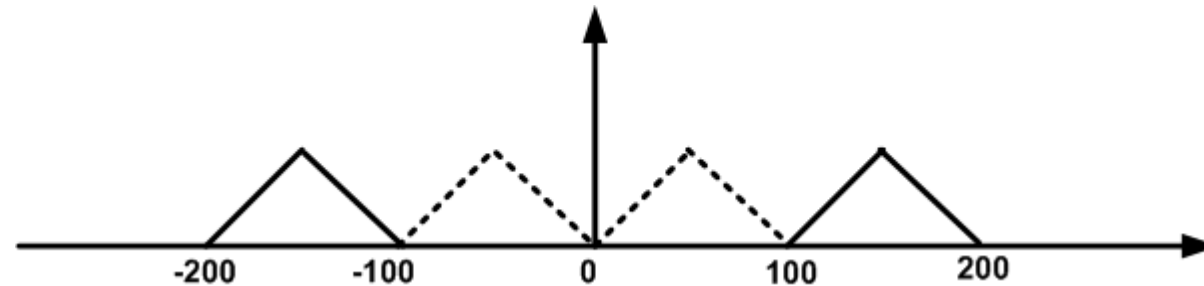


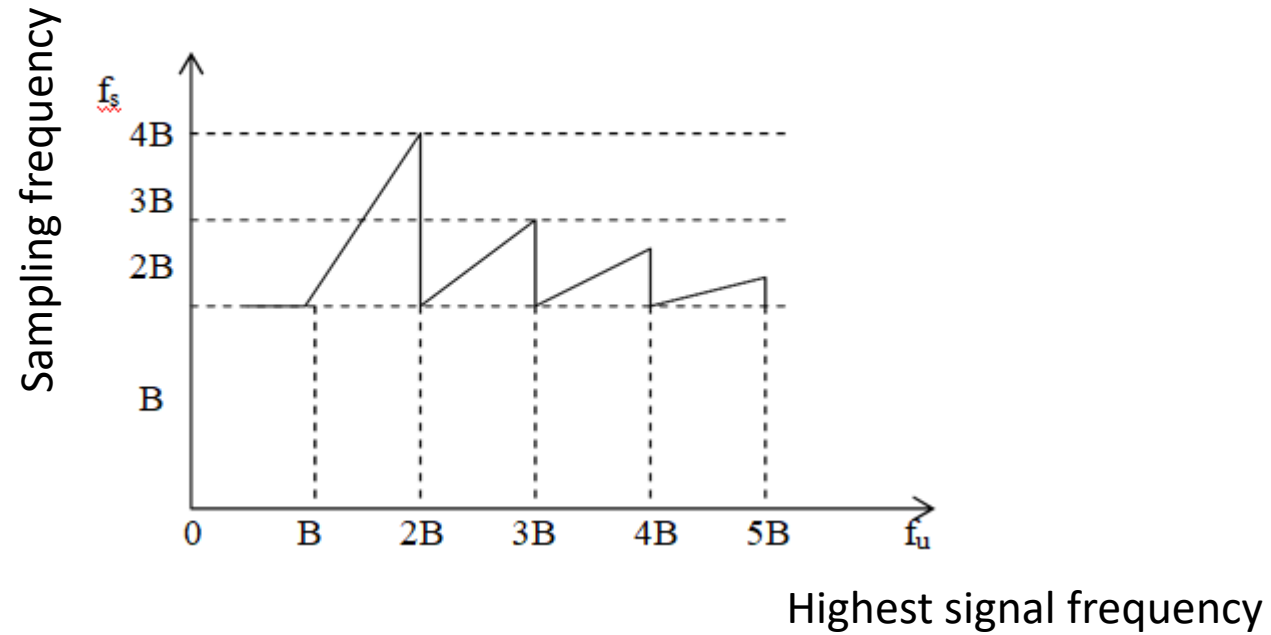
$F_s = 380$



$F_s = 400$

$F_s = 200$





f_s varies from $2W$ to $4W$

Canonical representation of Band-pass signal is

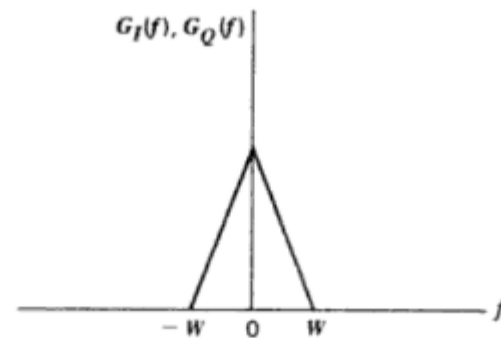
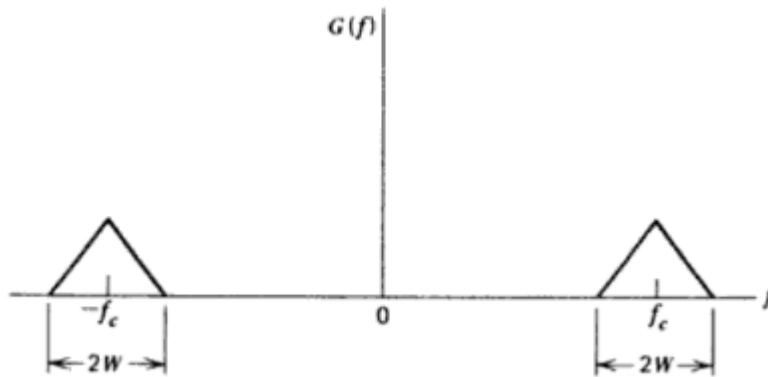
$$g(t) = g_I(t) \cos(2\pi f_c t) - g_Q(t) \sin(2\pi f_c t)$$

$g_I(t)$ - In-phase component

$g_Q(t)$ - Quadrature component

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Quadrature Sampling of Band-pass signals



$$\begin{aligned} g(t) \cdot 2 \cos(2\pi f_c t) &= g_I(t) 2 \cos^2(2\pi f_c t) - \\ &g_Q(t) 2 \cos(2\pi f_c t) \sin(2\pi f_c t) \\ &= g_I(t) [1 + \cos(4\pi f_c t)] - g_Q(t) \sin(4\pi f_c t) \end{aligned}$$

Low pass filter output is $g_I(t)$
In-phase component

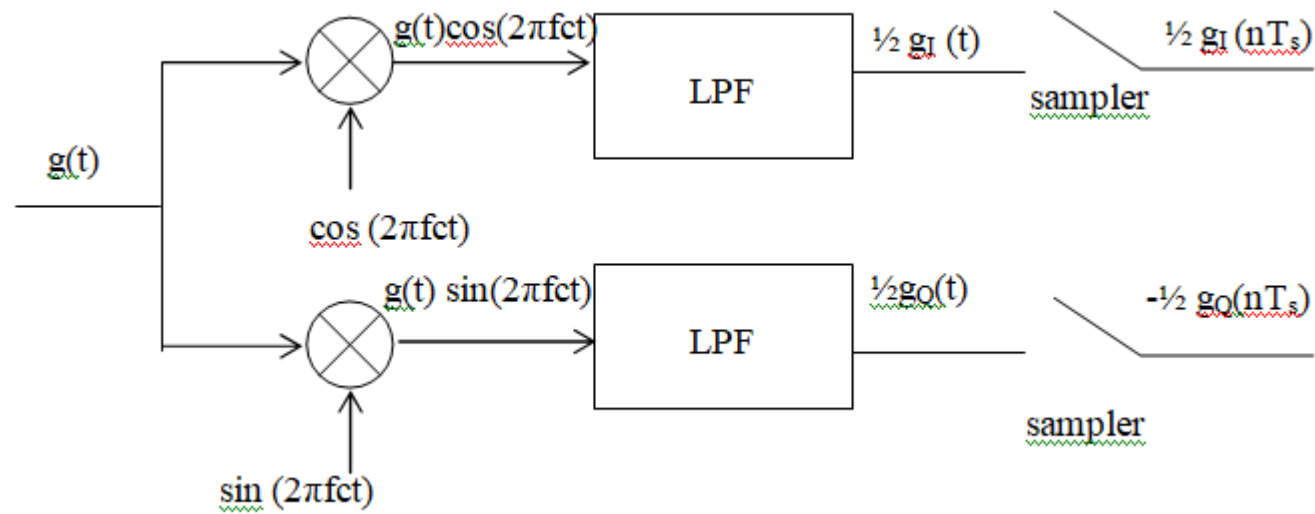
$$\begin{aligned} g(t) \cdot 2 \sin(2\pi f_c t) &= g_I(t) 2 \sin(2\pi f_c t) \cos(2\pi f_c t) - \\ &g_Q(t) 2 \sin^2(2\pi f_c t) \\ &= g_I(t) \sin(4\pi f_c t) - g_Q(t) [1 - \cos(4\pi f_c t)] \end{aligned}$$

Low pass filter output is $-g_Q(t)$

Quadrature component

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Quadrature Sampling of Band-pass signals



Reconstruction process

$$g_I(t) \cdot \cos(2\pi f_c t) - g_Q(t) \sin(2\pi f_c t) = g(t)$$

