

# LINEAR ALGEBRA AND ITS APPLICATIONS UE19MA251

# Reflection matrix H

The matrix H reflects every vector in R2 onto any 'O' line.

From the figure 
$$\overrightarrow{OA'} + \overrightarrow{A'B} = \overrightarrow{OB} - \overrightarrow{O}$$
 and  $\overrightarrow{OA'} + \overrightarrow{AB} = \overrightarrow{OB} - \overrightarrow{O}$ 

(Fine 
$$\overrightarrow{AB} = -\overrightarrow{AB}$$
)



# Reflection matrix H



#### Note:

. Two reflection brings back the osiginal.

- A reflection 25 its own Ermone.

# Reflection matrix H

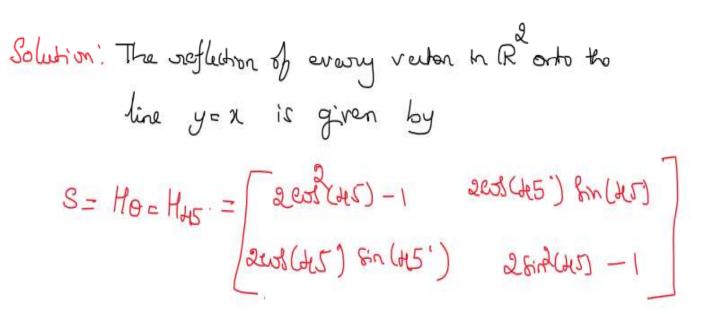
## To conclude....

Product of two transformations is another transformation by itself. Matrix multiplication is so defined that product of matrices corresponds to the product of the transformations that they represent.



## **Problems**

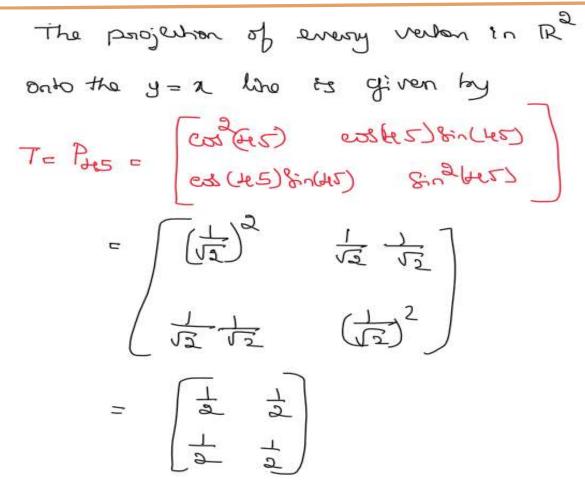
Find the matrix S that reflects every vector in  $R^2$  on the line y = x. Also find the matrix T which projects every vector in  $R^2$  on to the line y = x. Explain why ST = TS.







$$S = \begin{cases} 2\left(\frac{1}{12}\right)^{-1} & 2\left(\frac{1}{12}\right)^{-1} \\ 2\left(\frac{1}{12}\right)^{-1} & 2\left(\frac{1}{12}\right)^{-1} \end{cases}$$





$$S.T = \begin{bmatrix} 0 & 1 \\ 1 & 2 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1/2 & 1/2 \\ 1/2 & 1/2 \end{bmatrix}$$

$$TS = \begin{bmatrix} 1/2 & 1/2 \\ 1/2 & 1/2 \end{bmatrix}$$

$$= \begin{bmatrix} 1/2 & 1/2 \\ 1/2 & 1/2 \end{bmatrix}$$

$$= \begin{bmatrix} 1/2 & 1/2 \\ 1/2 & 1/2 \end{bmatrix}$$

$$= TS.$$

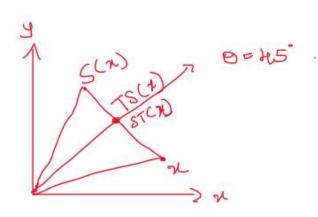


## **Problems**

ST is the exemposition of projecting any verbor of R2 onto y = x line than reflecting it onto y = x line.

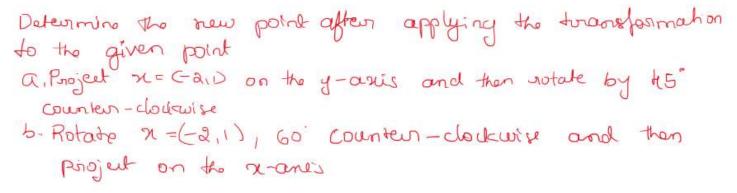
The is the composition of reflecting any vertor of R2 onto y = x line than projecting it onto y = x line than projecting it onto y = x line.

Both toranyformation produces the same output.





## **Problems**



### Solution'

$$= \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix}$$



## **Problems**

Rotation matrix to notate any verten of IR, by 45 counter clockwise about the origin (1 given by  $\Theta(45') = \frac{e\sigma(45)}{6n(45')} = \frac{e\sigma(45')}{6n(45')} = \frac{e\sigma(45')}{6n(45')}$ 

The projection of 9 = (-2(1)) on the y-anis and then softening about 0 = 45 counter clockwise is given

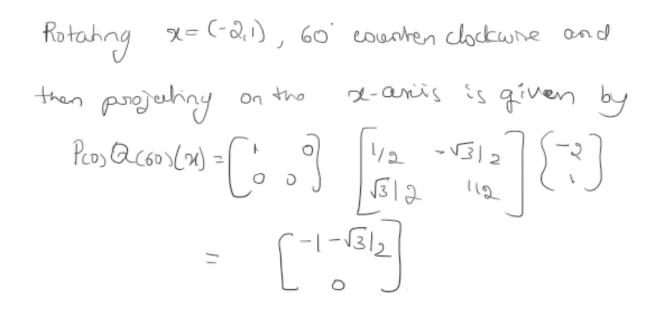


## **Problems**

60° counten chockwise is given by

Projection orabren to project any vector of R? onto









# **THANK YOU**