



DIGITAL IMAGE PROCESSING-1

Unit 3: Lecture 37

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Unit 3: Image Enhancement

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➤ Image Enhancement: Frequency domain methods

- 2D DFT and its properties
- Gaussian Filters
- Smoothing using frequency domain filters
- Correspondence between filtering in spatial and frequency domains

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This Session

- Image Enhancement: Frequency domain methods
 - Sharpening using frequency domain filters
 - Homomorphic Filtering

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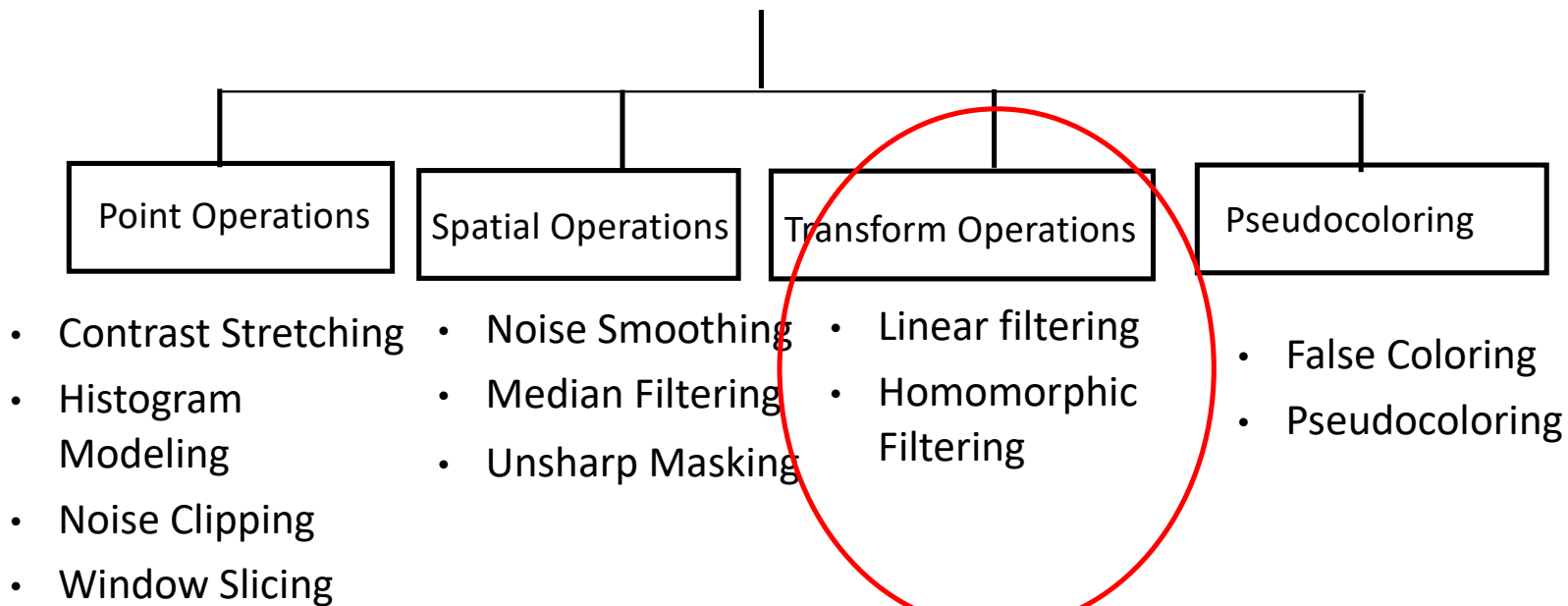
This Session

- Image Enhancement: Frequency domain methods
 - Sharpening using frequency domain filters
 - Homomorphic Filtering

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Types of Enhancement Techniques

Image Enhancement



Spatial Domain

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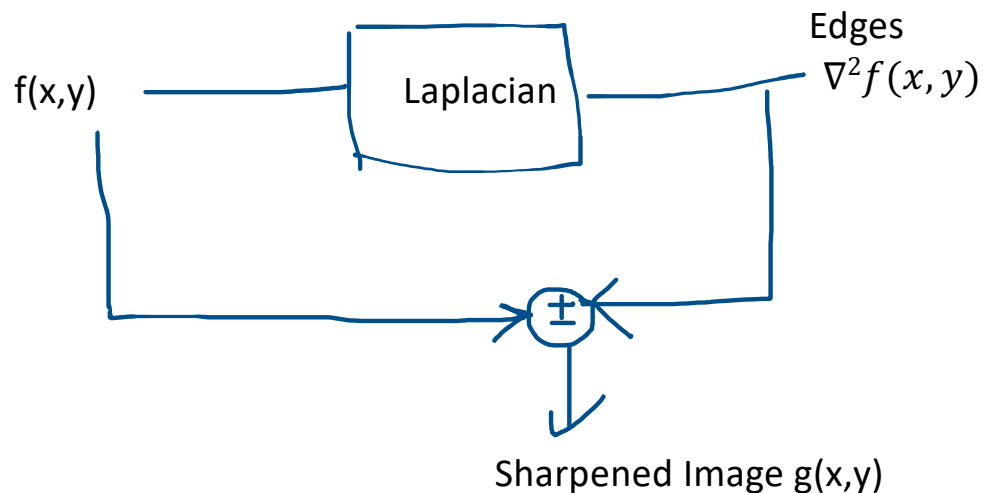
Image Sharpening in Frequency Domain

- Using Laplacian
- Unsharp Masking
- Highboost Filtering
 - To improve the visual quality while retaining the edge information extracted by HP filter

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Image Sharpening using Laplacian

- Laplacian operator is a derivative operation which highlights intensity discontinuities of an image and reduces slowly varying intensity values



$$f_s(x,y) = g(x,y) = f(x,y) \pm \nabla^2 f(x,y)$$

Subtract if center of mask is negative

Add if center of mask is positive

0	1	0
1	-4	1
0	1	0

0	-1	0
-1	4	-1
0	-1	0

With negative centre: $f_s(x,y) = f(x,y) - [-4f(x,y) + f(x+1,y) + f(x-1,y) + f(x,y-1) + f(x,y+1)]$

$$f_s(x,y) = f(x,y) + 4f(x,y) - f(x+1,y) - f(x-1,y) - f(x,y-1) - f(x,y+1)$$

$$= 5f(x,y) - f(x+1,y) - f(x-1,y) - f(x,y-1) - f(x,y+1)$$

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Image Sharpening using Laplacian

- Hence the sharpening mask in spatial domain is:

$$\begin{bmatrix} 0 & -1 & 0 \\ -1 & 5 & -1 \\ 0 & -1 & 0 \end{bmatrix}$$

$$g(x,y)=f(x,y) \pm \nabla^2 f(x,y)$$

- In frequency domain:

$$G(u,v) = F(u,v) - H(u,v)F(u,v)$$

$$\text{Or } G(u,v) = F(u,v)(1 - H(u,v))$$

$$\text{Now for a Laplacian } H(u,v) = -4\pi^2 (u^2 + v^2)$$

$$\text{Or } G(u,v) = F(u,v)(1 + 4\pi^2 D^2(u,v))$$

$$\text{For sharpening } H(u,v) = 1 + 4\pi^2 D^2(u,v)$$

Transfer function to sharpen images

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Image Sharpening using Laplacian

a b

FIGURE 4.56

(a) Original, blurry image.
(b) Image enhanced using the Laplacian in the frequency domain.

Compare with Fig. 3.46(d).
(Original image courtesy of NASA.)



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Unsharp masking in Frequency Domain

It is applied by **subtracting** an unsharp or **smoothed** or **low-pass filtered** version of an image from the **original** image.

$$f_{hp}(x,y) = f(x,y) - f_{lp}(x,y)$$

- Taking its Fourier Transform

$$F_{hp}(u,v) = F(u,v) - F_{lp}(u,v)$$

$$H_{hp}(u,v)F(u,v) = F(u,v) - H_{lp}(u,v)F(u,v) = (F(u,v)(1 - H_{lp}(u,v))$$

$$\text{Hence, } H_{hp}(u,v) = 1 - H_{lp}(u,v)$$

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Highboost Filtering in Frequency Domain

- To improve the visual quality while retaining the edge information extracted by HPF, we use highboost filters

$$g_{\text{mask}}(x, y) = f(x, y) - f_{\text{LP}}(x, y)$$

$$g(x, y) = f(x, y) + k g_{\text{mask}}(x, y)$$

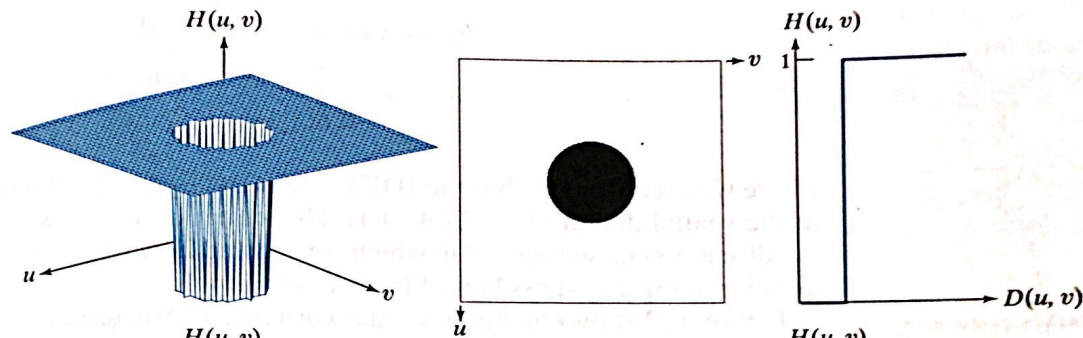
$$\text{Hence, } H_{\text{hp}}(u, v) = 1 + k(1 - H_{\text{lp}}(u, v))$$

$$g(x, y) = \mathfrak{F}^{-1} \{ [1 + k H_{\text{HP}}(u, v)] F(u, v) \}$$

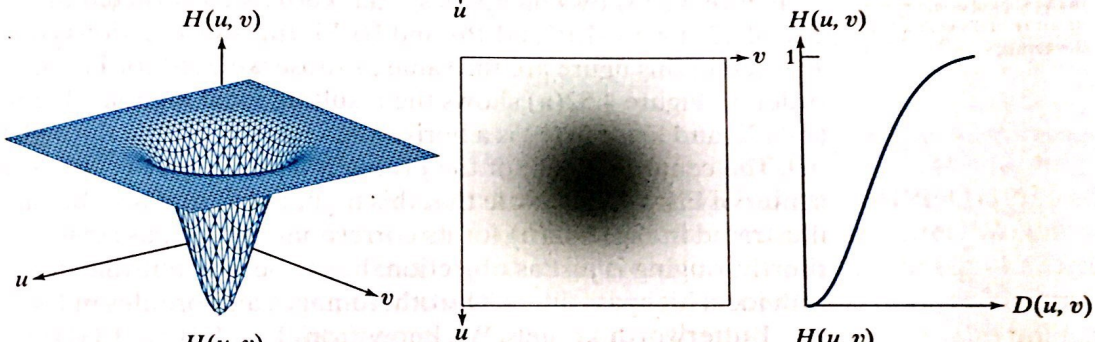
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Highpass Filters

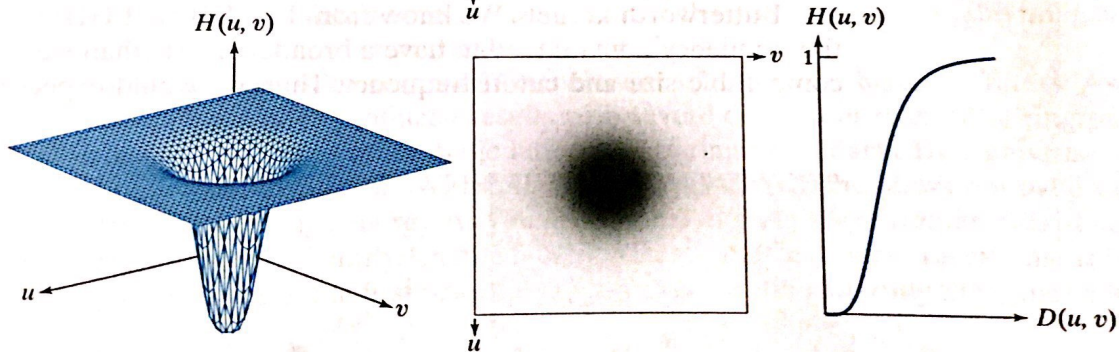
Ideal Highpass filter



Gaussian HP filter



Butterworth HP filter



$$H(u, v) = 1 - e^{-D^2(u, v)/2D_0^2} \quad (4-120)$$

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Homomorphic Filtering

- The illumination-reflectance model can be used to develop a frequency domain procedure for improving the appearance of an image
- Homomorphic filtering is a frequency domain approach to improve the appearance of an image by
 - Gray level range compression
 - Contrast enhancement
- An image captured by camera is formed by the multiplication of illumination and reflectance
$$f(x,y) = i(x,y).r(x,y)$$
- In some cases scene is not illuminated properly and some part of image appears very dark

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Homomorphic Filtering

- In order to improve these type of images reflectance and illumination has to be treated independently

$$F[f(x, y)] \neq F[i(x, y)] \times F[r(x, y)]$$

- Hence we take log on either side

$$\begin{aligned} z(x, y) &= \ln f(x, y) \\ &= \ln i(x, y) + \ln r(x, y) \end{aligned}$$

$$\begin{aligned} \mathfrak{F}[z(x, y)] &= \mathfrak{F}[\ln f(x, y)] \\ &= \mathfrak{F}[\ln i(x, y)] + \mathfrak{F}[\ln r(x, y)] \end{aligned}$$

$$Z(u, v) = F_i(u, v) + F_r(u, v)$$

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Homomorphic Filtering

- We can filter $Z(u,v)$ using a filter transfer function $H(u,v)$ so that

$$\begin{aligned} S(u,v) &= H(u,v)Z(u,v) \\ &= H(u,v)F_i(u,v) + H(u,v)F_r(u,v) \end{aligned}$$

- The filtered image in the spatial domain is then

$$\begin{aligned} s(x,y) &= \mathfrak{F}^{-1}[S(u,v)] \\ &= \mathfrak{F}^{-1}[H(u,v)F_i(u,v)] + \mathfrak{F}^{-1}[H(u,v)F_r(u,v)] \end{aligned}$$

$$s(x,y) = i'(x,y) + r'(x,y)$$

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Homomorphic Filtering

- Finally, because $z(x, y)$ was formed by taking the natural logarithm of the input image, we reverse the process by taking the exponential of the filtered result to form the output image:

$$\begin{aligned} g(x, y) &= e^{s(x, y)} \\ &= e^{i'(x, y)} e^{r'(x, y)} \\ &= i_0(x, y) r_0(x, y) \end{aligned}$$

where

$$i_0(x, y) = e^{i'(x, y)}$$

and

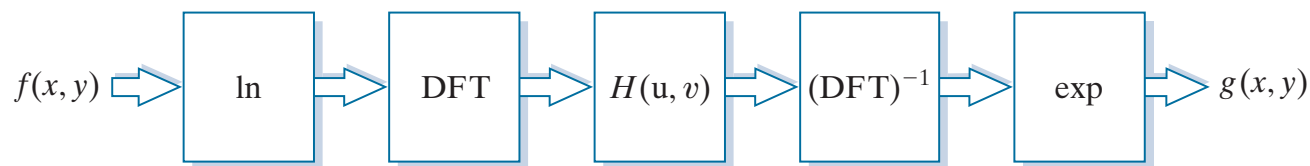
$$r_0(x, y) = e^{r'(x, y)}$$

are the illumination and reflectance components of the output (processed) image

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Steps Involved in Homomorphic Filtering

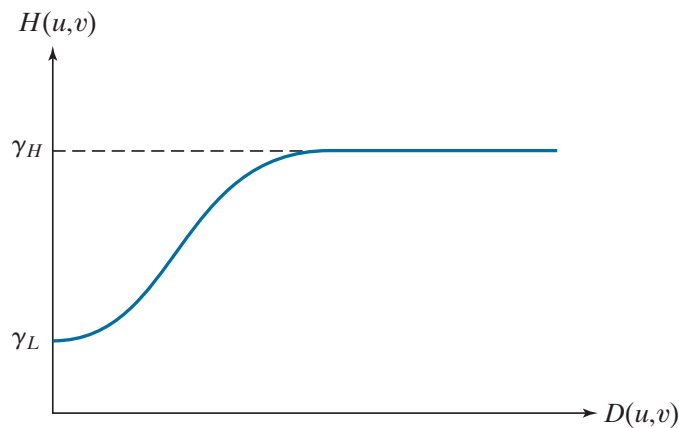
- Take natural log of input
- Take DFT on both sides
- Multiply with filter $H(u,v)$
- Take inverse DFT on both sides
- Take inverse log transformation to get enhanced image



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Steps Involved in Homomorphic Filtering

- In this particular application, the key to the approach is the separation of the illumination and reflectance components
- The *homomorphic filter transfer function*, $H(u,v)$, then can operate on these components separately



- Image Restoration



THANK YOU

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