

## *Recap*

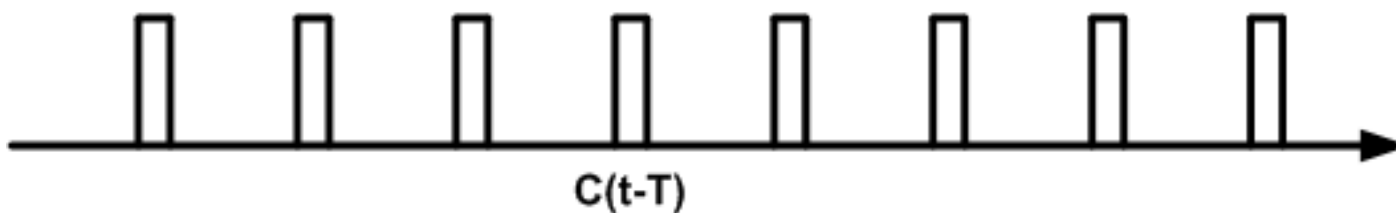
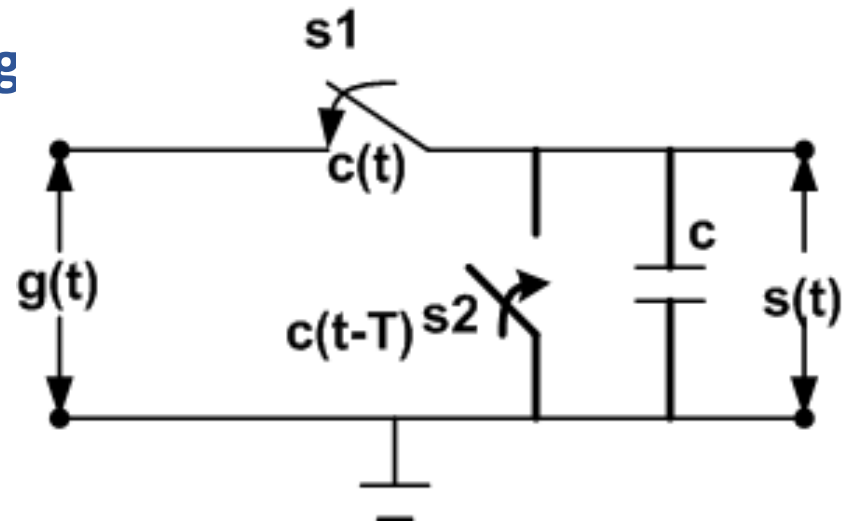
*Natural sampling*

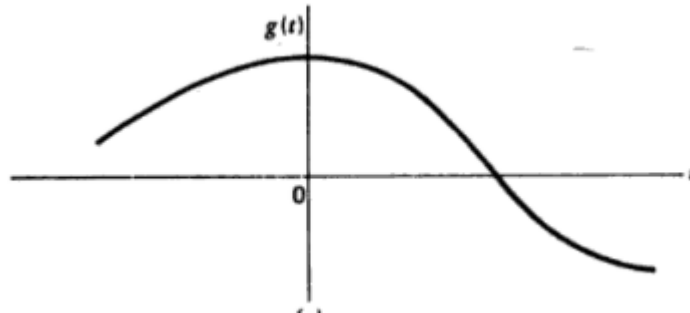
## *Topics for this session*

*Flat top sampling*

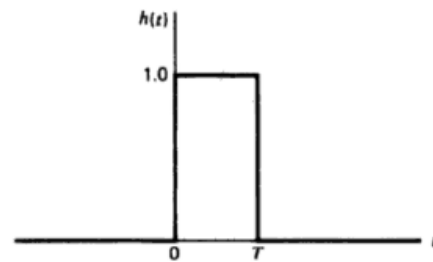
*Signal recovery – Sample and Hold circuit*

### •Flat-top sampling

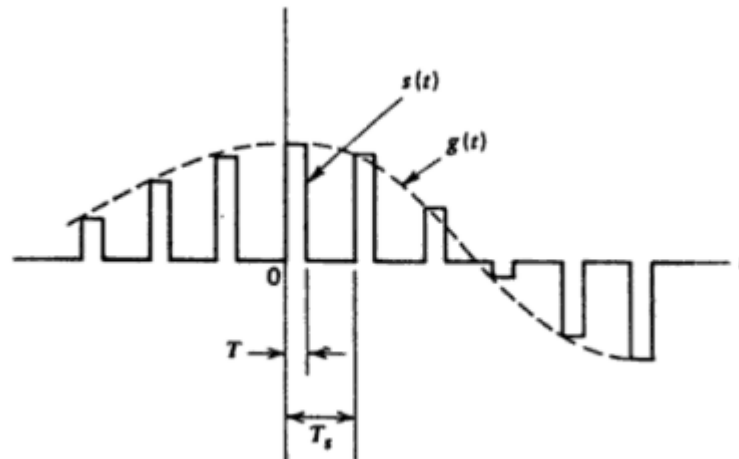




Analog signal



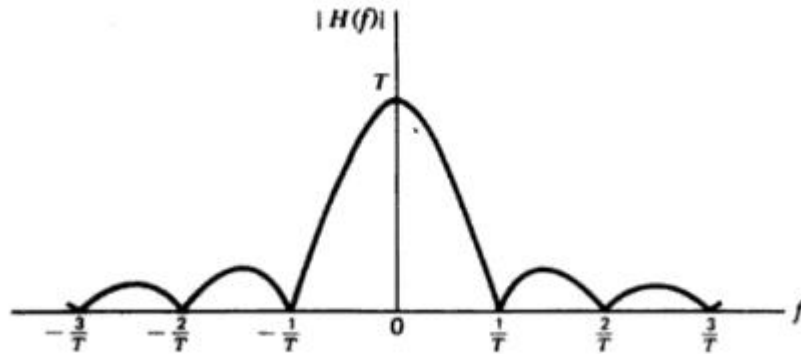
Rectangular pulse



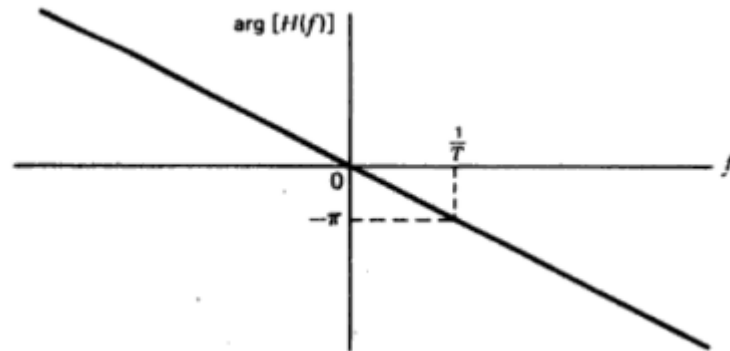
Flat-top samples

# DIGITAL COMMUNICATION

## Flat-top Sampling



Magnitude spectrum  
of  $H(f)$



Phase spectrum of  
 $H(f)$

$$s(t) = \sum_{n=-\infty}^{\infty} g(nT_s)h(t - nT_s)$$

$$h(t) = \text{rect}\left(\frac{t - \frac{T}{2}}{T}\right) = \text{rect}\left(\frac{t}{T} - \frac{1}{2}\right)$$

***$h(t)$  is rectangular pulse of unit amplitude and duration  $T$ .***

$$g_{\delta}(t) = \sum_{n=-\infty}^{\infty} g(nT_s)\delta(t - nT_s)$$

$$s(t) = g_{\delta}(t) * h(t)$$

$$s(t) = \sum_{n=-\infty}^{\infty} g(nT_s)h(t - nT_s)$$

### *Fourier Transform of $s(t)$*

$$S(f) = G_{\delta}(f)H(f)$$

$$S(f) = f_s \sum_{m=-\infty}^{\infty} G(f - mf_s)H(f)$$

### *Fourier Transform of $h(t)$*

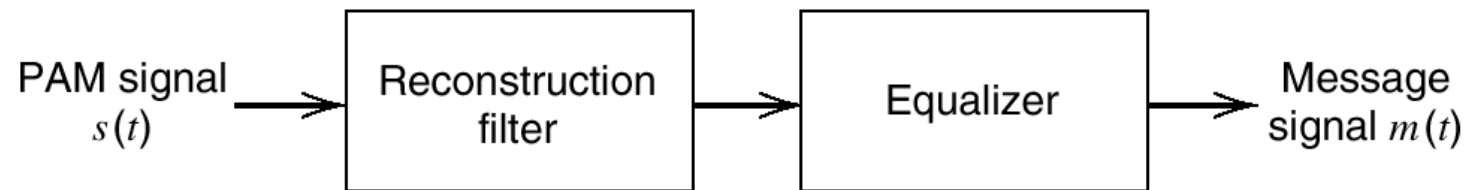
$$H(f) = T \sin c(fT) \exp(-j\pi fT)$$

amplitude distortion      delay =  $T/2$

### *Aperture effect*

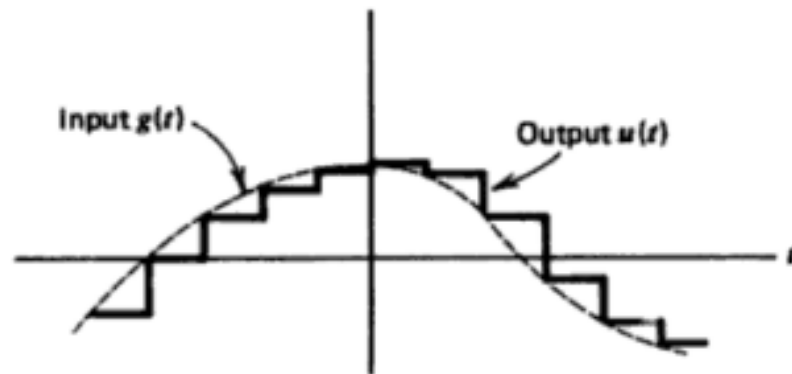
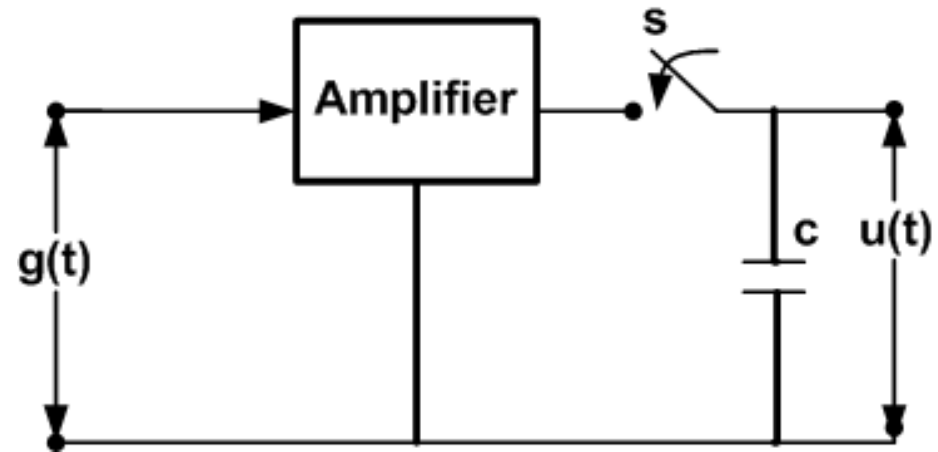
#### *Amplitude response of equalizer is*

$$\frac{1}{|H(f)|} = \frac{1}{T \sin c(fT)} = \frac{1}{T} \frac{\pi fT}{\sin(\pi fT)}$$



# DIGITAL COMMUNICATION

## Sample and Hold circuit



Idealized output waveform



*Output of sample and hold circuit  $u(t)$*

$$u(t) = \sum_{n=-\infty}^{\infty} g(nT_s)h(t - nT_s)$$

$$h(t) = \begin{cases} 1; & 0 \leq t \leq T_s \end{cases}$$

$$= \begin{cases} 0; & \text{otherwise} \end{cases}$$

*Spectrum of  $h(t)$*

$$H(f) = T_s \operatorname{sinc}(fT_s) \exp(-j\pi fT_s)$$

*Fourier transform of output  $u(t)$*

$$U(f) = f_s \sum_{m=-\infty}^{\infty} H(f)G(f - mf_s)$$

