Transformer Fundamentals with GPT-1

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Language Modeling

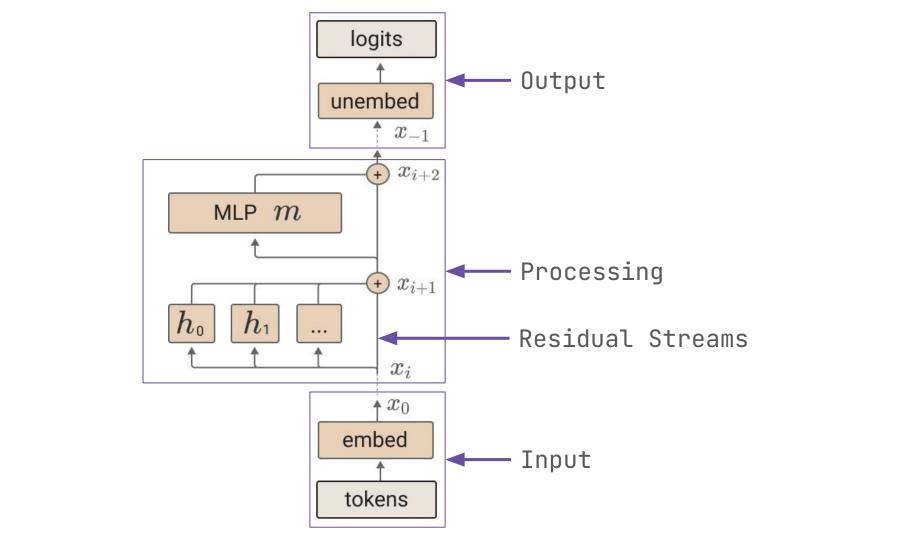
- Defn: A language model is a system that assigns probabilities to sequences of words, enabling it to generate, predict, or evaluate text.
- Old approaches:
 - N-gram models
 - Hidden Markov models
 - Feedforward neural networks
 - Recurrent neural networks
- "Attention Is All You Need" (2017, Google)
 - Encoder-Decoder Transformer
 - Translation

The GPT Family

- "Improving Language Understanding by Generative Pre-Training" (2018, OpenAI)
 - **G**enerative
 - Pre-trained
 - Transformer (decoder)
 - Specs:
 - 40 GB of text (~1 billion tokens)
 - 117 million parameters
- Descendents:
 - ChatGPT
 - Claude
 - Gemini
 - etc.

GPT: What to Know

- Input
 - Tokens
 - Embed
- Processing (transformer blocks)
 - Attention (multi-head self attention)
 - QK (scoring)
 - OV (mixing)
 - MLP
 - Residual stream (the information highway)
- Output
 - Unembed
 - Sampling

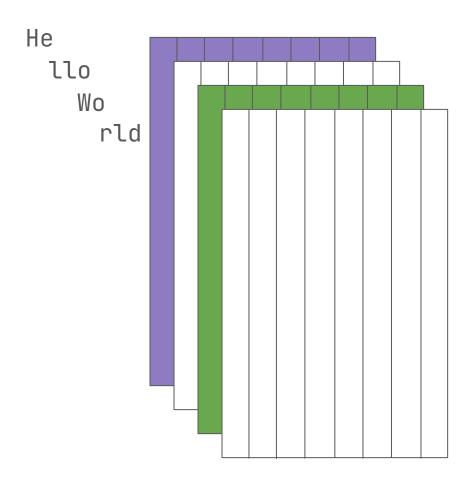


$$h_0 = UW_e + W_p$$

$$h_l = \texttt{transformer_block}(h_{l-1}) orall i \in [1,n]$$

$$P(u) = \texttt{softmax}(h_n W_e^T)$$

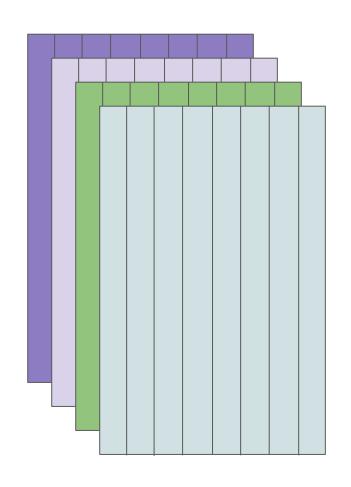
Initial Residual Streams



batch tokens dimension 1 4 8

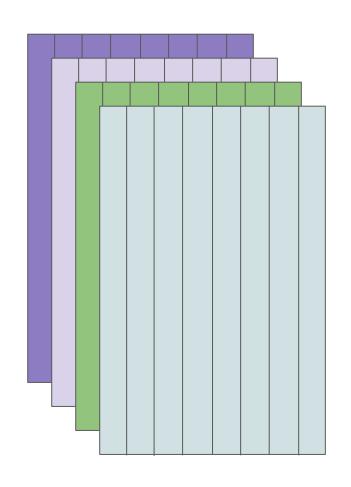
2 attention heads

	Не	llo	Wo	rld
Не	1	_	_	_
llo	.7	.3	_	_
Wo	.2	.2	.6	-
rld	.2	.2	.2	.4

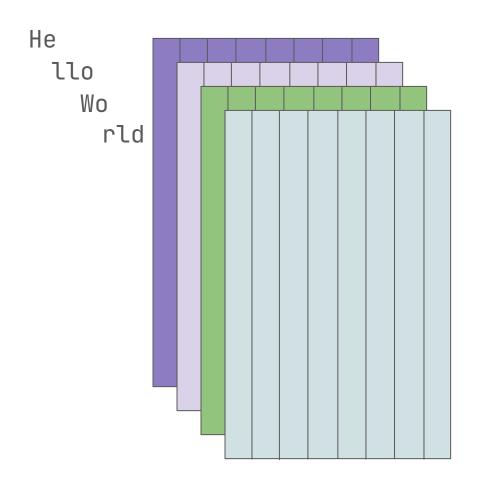


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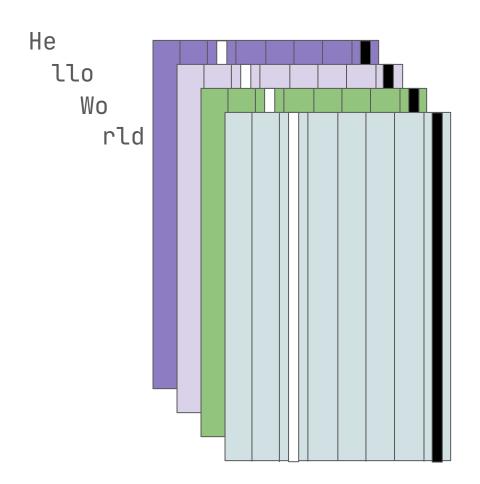


Residual Streams After Attention



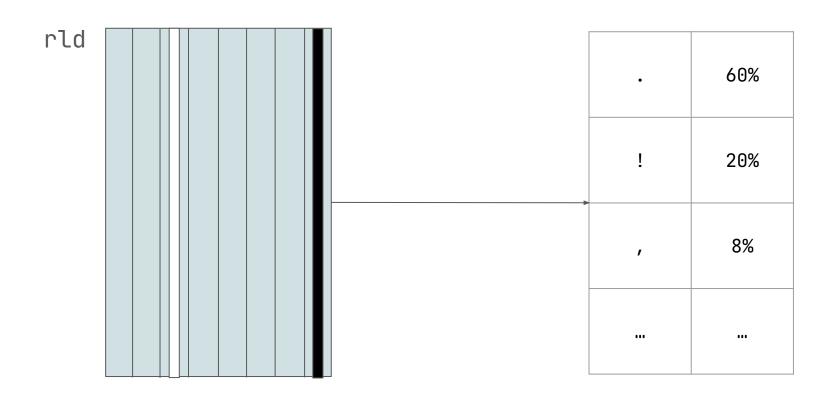
batch tokens dimension
1 4 8

Residual Streams After Attention and MLP



batch tokens dimension
1 4 8

Unembed



Resources / My path to this understanding

- A Mathematical Framework for Transformer Circuits: this paper has a section "Transformer Overview" that has influenced how I think about transformers more than anything else.
- The papers mentioned in previous slides: I found working through the GPT-1 paper really valuable. The "Attention is All You Need" paper is seminal and many people have created resources centering around it.
- YouTube: Serrano.Academy, Neel Nanda, Andrej Karpathy
- **Podcasts:** Machine Learning Street Talk, The Cognitive Revolution, Latent Space, + anything I can find with researchers from the frontier labs
- Hands on: I learned a lot from fine-tuning GPT-1
- Claude and ChatGPT