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# REDISTRIBUTION, PORK, AND ELECTIONS

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#### Abstract

Why might citizens vote against redistributive policies from which they would seem to benefit? Many scholars focus on 'wedge' issues such as religion or race, but another explanation might be geographically-based patronage—or pork. We examine the tension between redistribution and patronage with a model that combines partisan elections across multiple districts with legislation in spatial and divide-the-dollar environments. The model yields a unique equilibrium that describes the circumstances under which poor voters support right-wing parties that favor low taxes and redistribution, and under which rich voters support left-wing parties that favor high taxes and redistribution. The model suggests that one reason standard tax and transfer models of redistribution often do not capture empirical reality is that redistributive transfers are a less efficient tool for attracting votes than are more targeted policy programs. The model also underlines the central importance of party discipline during legislative bargaining in shaping the importance of redistribution in voter behavior, and it describes why right-wing parties should have an advantage over left-wing ones in majoritarian systems. (JEL: D72)

#### 1. Introduction

Since the classic work of Meltzer and Richard (1981), a standard assumption in political economy models of income redistribution is that political parties compete for votes using tax rates, where tax revenues fund transfers from rich to poor. These models predict a strong connection between income and the vote, with poor voters supporting left-wing parties that advocate high tax rates and redistribution levels, and rich voters supporting right-wing parties that oppose taxes and redistribution. Across democracies, however, this prediction of a strong income-vote relationship does not accurately describe actual voting behavior. Many voters in fact 'cross over'—poor voters support right-wing parties and rich voters support left-wing ones.

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For example, while income is an important predictor of the US vote (McCarty, Poole, and Rosenthal 2006), Gelman et al. (2008) estimate that over 40% of rich individuals supported the Democrats in the 2004 elections, and about 40% of poor individuals supported the Republicans. This paper develops a model of such crossover voting.

The standard explanation for crossover voting has been to invoke the importance of a second policy dimension that distracts voters from their economic self-interest (e.g., Roemer 1998). The 'culture wars' arguments in the United States, for example, hold that poor voters often support right-wing candidates because of their preferences on issues like gun control, religion, or abortion (e.g., Hunter 1991; Frank 2004). While such issues are clearly important to certain voters, recent empirical research provides scant support for these arguments (e.g., Bartels 2008; Ansolabehere, Rodden, and Snyder 2006). We therefore take a different approach, one that refocuses attention on the economic self-interest of voters, but that recognizes that many government transfers are not actually from rich to poor, but rather occur along other lines. Without a more complete picture of such transfers, it is difficult to determine whether particular voting decisions promote an individual's economic self-interest.

We focus specifically on geographically-targeted transfers to specific districts, or 'pork'. Scholars have long linked pork programs to election strategies and outcomes (e.g., Key 1984; Ramseyer and Rosenbluth 1993; McGillivray 2004). Policies in this category that come immediately to mind include monies for public works such as airports, roads, and bridges. But such programs are in fact the tip of the iceberg when it comes to policies that provide district-specific economic benefits. Whenever a government decides, for example, where to locate public offices, hospitals, universities, military bases, or nationalized industries, there is a significant impact on the local economy and on the location of jobs. Government subsidies, tariff policies, and investments in research typically also benefit geographic-specific institutions or industries (such as automobiles, alternative energy, or agriculture). The size and scope of all such programs is very large, and indeed comparable to that of redistributive programs. More importantly, their value to specific individuals can dwarf that of richto-poor transfer payments. Thus, a clear understanding of how voters make choices based on personal economic benefits requires one to examine the tension between targeted transfers and redistributive programs.

Our model considers an environment with elections across multiple districts and legislative bargaining. In each district, a majority of voters are either poor (and receive means-tested redistribution) or rich (and receive no redistributive transfers but pay taxes). Candidates in each district represent either a 'left' or 'right' party, with the former favoring higher redistribution. Crucially, candidates may not commit to future voting decisions, and therefore policies are determined by majority rule in the elected government. After the election, the party winning a majority of seats determines how the budget is divided between redistribution and pork, and legislative bargaining determines how the pork is apportioned across districts.

The basic insight of the equilibrium is that when voters expect the party with 'bad' redistributive policies to win at the national level, they may nonetheless crossover vote

for this party in order to obtain local pork. Poor voters, for example, may support right-wing parties in our model not because of preferences on abortion or some other policy unrelated to economic well-being, but rather because the total pork plus general redistribution the voter expects from the right-wing party exceeds that expected from the left. A key purpose of the model is to identify the circumstances under which such voting occurs.

In addition to this basic observation about crossover voting, three central arguments emerge from the analysis. First, the model underscores the fact that tax-and-transfer redistributive programs are relatively inefficient electoral tools for political parties. Such means-tested programs often reach only a minority of voters in a given district, and thus they may often fail to influence its pivotal voter's calculation. If the benefits of means-tested programs do reach the median voter in a given district, they typically must be spread quite thinly across many individuals in society, lowering their value relative to that of more targeted policies. And if individuals are mobile yet collect the same redistributive benefits regardless of where they live, then broad-based redistributive programs cause politicians to abdicate a great deal of political control over how benefits are distributed across districts. A more targeted approach to distributing government benefits avoids these inefficiencies.

Second, the effect of individual income on the vote, and thus the relative efficiency of pork as an electoral tool, depends crucially on the role of political parties in legislative bargaining over the distribution of pork across districts. In order for pork to affect voting decisions, voters must form expectations about how their vote will affect its distribution, which will depend in turn on whether parties can exercise discipline over their members in the legislature. When parties are 'strong' (i.e., highly disciplined), the majority party can exclude members of the minority party from pork, creating incentives for voters to support the winning party at the national level in order to obtain pork in their district. When parties are 'weak', and pork is distributed in a free-for-all fashion, the impact of the voting outcome on pork weakens, and voters therefore have a stronger incentive to vote their redistributive interests. This result is consistent with the findings of Huber and Stanig (2009), who find that income-based voting polarization between rich and poor is higher in the United States (a weak-party system) than in 22 of 23 strong-party countries in their study. The model therefore highlights the importance of considering how the structure of legislative politics affects voting on redistribution by constraining the ability of candidates to make credible promises to voters.

Third, the model suggests that although crossover voting by rich and poor can occur in equilibrium, there is an asymmetry in majoritarian systems that advantages the rich voters and the right-wing party. Since crossover voting occurs in order to obtain pork, and since the right-wing party spends a lower proportion of the budget on redistribution, it can devote a higher proportion of the budget to pork. The combination of more pork and the greater efficiency of pork for attracting voters implies that the incentives for the poor to crossover vote for the right are typically greater than are the incentives for the rich to crossover vote for the left. These incentives persist even when the left-wing party can raise taxes substantially to finance its programs. Our model

therefore provides an intuition for why right-wing parties should have an advantage over left-wing ones in plurality electoral systems.

Our model builds on an extensive body of work on elections, legislatures, and distributive politics. It is perhaps most closely related to a family of models originating with Lindbeck and Weibull (1987), which examines the electoral trade-off between distributive benefits and ideology. In their work, two parties with fixed ideological platforms compete for votes by offering transfers and taxes to groups of voters with heterogeneous ideological leanings. The well-known prediction is that pork should go to groups that contain many 'swing', or ideologically uncommitted, voters. Relevant variations on this framework include Dixit and Londregan (1998), who link ideology with income inequality, and Hassler et al. (2005), who model dynamic redistributive policy. Notably, Lopez-Rodriguez (2011) considers parties that have preferences for public goods and derives a right-wing advantage based on the right's ability to provide more pork.

Unlike the model presented here, these models assume that candidates can commit to transfer schedules, and do not explicitly address the consequences of geographically-based legislative representation. Some recent theories have developed the connection elections and government policy-making (e.g., Austen-Smith and Banks 1988; Baron and Diermeier 2001; Snyder and Ting 2003). In particular, Milesi-Ferretti, Perotti, and Rostagno (2002) allow parties to compete on transfers to specific groups as well as geographic constituencies. Their paper, however, assumes that electoral districts are homogeneous and focuses on electoral systems and the level of government spending. Thus it does not cover the question of crossover voting that is central here.

The policy outcomes in our model are related to those of a set of theories that explores the legislative or electoral trade-offs between universal and targetable programs. Jackson and Moselle (2002) consider the problem of simultaneous bargaining over spatial policy and pork in a legislature. The lack of a simple equilibrium solution in their work motivates our simplifying assumption that these two issues are considered separately in our legislature. Volden and Wiseman (2007) derive closed-form solutions in a legislative bargaining game over the distribution of particularistic benefits and a collective good. Christiansen (2013) extends their model to include the election of legislators with diverse preferences over particularistic and collective goods. Models of electoral systems and redistribution in this vein such as Persson and Tabellini (1999) and Lizzeri and Persico (2001) have emphasized the advantage of targetable as opposed to public goods.

Finally, our model joins a line of recent research that investigates how redistribution is affected not by a second dimension that is orthogonal to economic self-interest, but by the ability of governments to target transfers to specific groups on a basis other than income. Levy (2005), for example, examines the formation of electoral coalitions between the rich (who receive low taxes) and those poor who value education (who receive higher educational spending). Fernàndez and Levy (2008) examine how the number of ethnic groups affects the incentives of poor voters to support rightwing parties to obtain group-based benefits. Huber and Stanig (2011) develop a theory of transfers through religious organizations and their influence on general

redistribution, and Austen-Smith and Wallerstein (2006) examine how the ability to target transfers based on race affects redistribution. Although none of these models shares the institutional structure of our model or its focus on crossover voting, like our model, they each underscore the fact that the distribution of government resources occurs along pathways other than income-based redistribution. Further, they show that such pathways can affect the formation of electoral coalitions based on income, and the amount of income-based redistribution that occurs.

The remainder of the paper is organized as follows. Section 2 describes the basic structure of the model. Section 3 examines the unique equilibrium when parties are weak, and Section 4 examines the unique equilibrium when parties are strong. We then consider an extension where the left-wing party can offer very high taxes. Section 6 concludes.

### 2. The Model

Our model combines partisan elections across n (odd) constituencies with legislation in both spatial and divide-the-dollar policy environments. Each district or state, denoted  $S_1, \ldots, S_n$ , contains a continuum of voters of measure 1. There are two types of voters, denoted by  $t \in \{P, R\}$ , which correspond informally to 'poor' and 'rich', respectively. Let  $p_k^t$  be the proportion of voters of type t in  $S_k$ . The total number of type t voters in society is then  $n^t = \sum_{k=1}^n p_k^t$ . We refer to a district as 'rich' or 'poor' if the respective types are a majority of its population, and let  $d^R$  and  $d^P$  represent the number of rich and poor districts, respectively.

The legislature divides a government budget between two kinds of transfers. First, it determines the proportion 1-x to be spent on 'redistribution'. This is a means-tested income support or welfare program that benefits all (and only) poor voters equally. Second, it divides the remaining proportion x to 'pork', or direct transfers to districts that benefit all (and only) members of the targeted districts equally. This allocation is denoted by the n-vector  $\mathbf{y}$ . All spending is financed by a flat tax on rich citizens.

All election candidates and legislators belong to one of two (nonstrategic) parties, denoted  $P_L$  and  $P_R$ , which respectively represent 'Left' and 'Right'. Each party,  $P_j$ , has an exogenous platform  $\lambda_j \in [0, 1]$  that describes its members' relative commitment to pork and redistribution. Specifically, members of  $P_j$  have single-peaked preferences over x and ideally wish to devote proportion  $\lambda_j$  of the budget to pork. Party  $P_R$  prefers a smaller welfare system than  $P_L$ , which implies  $\lambda_R \geq \lambda_L$ . For the election in each district, each party has one candidate, and a winner is chosen by plurality rule. Within each party, candidates are identical across districts. The legislature is composed of the n winning candidates.

The district  $S_k$  legislator cares about both x and her district's share of pork  $y_k$ . While it is not necessary for the main results of the model, we assume for simplicity that each legislator has lexicographic preferences for x over  $y_k$ . Utility over pork is linear.

<sup>1.</sup> Many alternative utility functions would also generate our results. Lexicographic preferences simply ensure that a party  $P_i$  majority will choose  $x = \lambda_i$  when bargaining over x, as opposed to a more

Thus, legislators are primarily concerned with the level of redistribution in society, and secondarily concerned with pork. Since the model does not address candidate selection of campaign strategies, it is unnecessary to specify utilities for election candidates.

The model links party platforms and the government's budget in a way that allows  $P_L$  to 'advocate' larger overall budgets. The government budget is b(x) = 1 + (1 - 1)c)(1 – x). The parameter  $c \in [0, 1]$  therefore represents an exogenous constraint such as debt, existing social policy, the state of the economy, or international factors on the feasibility of tax increases, and thus on how much larger the government will be when  $P_L$  wins than when  $P_R$  wins. To see its role, note that at one extreme, if c = 1, the government's resources are fixed at 1 regardless of which party wins the election, and any increases in welfare spending come at the expense of pork. The parties' differing commitments to pork and redistribution are therefore all that distinguishes them from each other, and the setting becomes a divide-the-dollar framework common to models of distributive politics. As c declines, the government budget increases as the proportion of revenues devoted to welfare spending increases, which implies that for any pair of party platforms, the ideal level of total taxes and spending of  $P_L$  will grow relative to that of  $P_R$ . At the other extreme, where c=0, redistribution is funded entirely by incremental tax dollars. Observe that the total quantity of pork, xb(x), is increasing in x, and the total quantity of welfare spending, (1-x)b(x), is decreasing in x, which implies that the total amount of pork available to  $P_R$  is greater than that available to  $P_L$  for any c.

Although in principle c could be negative (and we explore this possibility in an extension in what follows), it makes sense to focus attention on parameterizations of c that reflect the existing empirical understanding of differences between left- and rightwing parties. Such research suggests that globalization, the size of the welfare state, and voter distaste for large deficits makes the effect of partisan control of government on the overall size of government either quite small or non-existent (e.g., Cusack 1997; Garrett and Lange 1991). It therefore makes little sense to allow c to be so small that the budget differences between the two parties becomes unrealistically large. When c=0 in our model, every extra dollar spent by the left on redistribution is funded by additional taxation, which probably allows the difference between left and right budgets to exceed what we actually observe empirically.<sup>2</sup>

Voters have quasilinear utility over money. In addition, voters receive ideological utility pertaining to outcomes unrelated to economic transfers, and this ideological dimension biases voters toward their most preferred party on the redistributive dimension. Let  $u^t(\lambda_j)$  be the ideological utility that a voter of type t receives if party  $P_i$  wins in the voter's district. We assume that voters have an ideological

cumbersome constrained maximum not equal to  $\lambda_j$ . The platform may also be viewed as each legislator's induced ideal value of x, after accounting for both ideology and anticipated pork.

<sup>2.</sup> For example, if  $P_L$  commits 55% of the budget to redistribution and  $P_R$  commits 45%, then when c = 0, the  $P_L$  budget would be 7% larger than that of  $P_R$ . This number is itself large, and to allow this difference to become even larger by allowing c < 0 is substantively questionable.

preference for the party that favors their redistributive interests; thus,  $u^P(\lambda_L) > u^P(\lambda_R)$  and  $u^R(\lambda_R) > u^R(\lambda_L)$ . Importantly, this gain in ideological utility from voting one's 'class' interest can be arbitrarily small, but its inclusion ensures that a voter will never crossover vote unless so doing yields a higher monetary payoff from the government. That is, if a voter expects to receive the same monetary payoff for any vote choice, she will not crossover vote. Including this ideological utility enables us to specify the voting strategies of voters who are indifferent with respect to monetary payoffs, and to do so in a way that clearly stacks the deck against crossover voting.

A district  $S_k$  voter's utility under a party  $P_i$  representative is therefore given by

$$u_k(x, \mathbf{y}; t) = \begin{cases} u^t(\lambda_j) + y_k + \frac{(1-x)b(x)}{n^P} & \text{if } t = P, \\ u^t(\lambda_j) + y_k - \frac{b(x)}{n^R} & \text{if } t = R. \end{cases}$$

The game begins with simultaneous elections in each district, where voters simultaneously choose between candidates from each party. After the election winners are determined, legislators bargain over the level of redistribution and the allocation of pork across districts. This bargaining takes place in two stages. First, legislators bargain over spatial policy. As already noted, legislators from the same party have identical preferences regarding redistribution. It is clear that in this stage, a wide variety of simple bargaining arrangements would lead to a median voter result. We therefore suppress the details of this stage, and allow the aggregate amount of redistribution to be  $1 - x = 1 - \lambda_j$ , where  $P_j$  is the party that wins a majority of districts. Second, legislators bargain over pork. Since legislators maximize the amount of pork that goes to their districts, this process pits them against each other, independent of party. We separate the two stages for analytical tractability; bargaining over both stages simultaneously can make the derivation of comparative statics almost intractable (Jackson and Moselle 2002).

We consider two different bargaining processes for pork, which capture the extremes of party discipline in the legislature. In the *weak-party* bargaining process, parties do not play a role in how members form coalitions, and legislators are free to bargain with any other legislator. Since bargaining involves the entire chamber, the election outcome has no impact on the distribution of pork. In the *strong-party* bargaining process, the majority party has unlimited proposal power and discipline. Because of perfect party discipline, the majority party can pass any legislation that is favored by a majority of its members, and therefore has no reason to offer pork to minority party legislators.

We are again agnostic about the details of the bargaining game at this stage, simply because many bargaining games predict equal ex-ante expected payoffs in games where all players have equal voting weight. This is true of the noncooperative models of Baron and Ferejohn (1989) and Morelli (1999), and also of power indices based on cooperative game theory, such as Shapley and Shubik (1954) and Banzhaf

(1968). Thus the weak-party bargaining process implies an ex-ante expected pork level of xb(x)/n for all districts. Likewise, the strong-party bargaining process implies an ex-ante expected pork level of  $xb(x)/\bar{n}$  in districts represented by the majority party, where  $\bar{n}$  is the total population of such districts. This quantity reflects the fact that districts not represented by the majority party must receive 0.

Because the outcome of the bargaining process can be reduced to an expected payoff, the model is effectively a simultaneous-move game amongst voters. We assume that voters choose as if they were pivotal in choosing their district's legislator. This implies that voters of the same type in a given district always vote the same way, and can therefore be treated as a single player. While Nash equilibria in this game are typically not unique, we can derive a unique prediction by considering coalitionproof Nash equilibria (CPNE).3 CPNE rule out Nash equilibria in which subsets of players may credibly deviate from a Nash equilibrium. The concept is weaker than that of a strong Nash equilibrium, which rules out any Nash equilibrium in which a subset of players may profitably deviate. By contrast, CPNE only rules out equilibria with self-enforcing deviations. A coalition of deviators is self-enforcing if no subset thereof would receive strictly higher payoffs from deviating in turn from the coalition's proposed alternative strategy profile. As Bernheim, Peleg, and Whinston (1987) show, all strong Nash equilibria are CPNE, but CPNE are not generally guaranteed to exist. In general, CPNE may exist when strong Nash do not, and as we show in Proposition 2, CPNE is sufficient to guarantee a unique level of crossover voting when Nash equilibria are not unique.4

Apart from its appealing technical properties, CPNE is attractive substantively to the extent that there exist mechanisms outside the model that coordinate voters with similar incomes. Collections of voters of the same type across different districts are often organized by interest groups, such as unions or industry associations. Such groups may be the primary beneficiaries of district-specific pork, and might coordinate their members' votes through endorsements or campaign contributions. In this context, coalition proofness simply reflects the incentive of groups to maximize their collective welfare by voting in a cohesive manner. Thus, a group will contemplate deviating from a proposed voting strategy if and only if such a deviation would not cause a subgroup to splinter.

### 3. Weak Parties

We begin with the weak-parties case, which will build intuition and serve as a benchmark for the subsequent analysis. In this environment, the distribution of pork is not controlled by the majority party. Instead, there is an 'open' bargaining process that allows all elected legislators an equal opportunity to gain pork for their districts. This

<sup>3.</sup> Bernheim, Peleg, and Whinston (1987) only define CPNE for games with finite populations, but since all voters vote as if pivotal in their district, our game effectively has 2n players.

<sup>4.</sup> This refinement is applied in a similar fashion by Alesina and Rosenthal (1996).

results in an ex-ante expected pork allocation of xb(x)/n regardless of the election winner.

To characterize voting strategies, note that poor voters always prefer a  $P_L$  victory on ideological grounds (i.e.,  $u^P(\lambda_L) > u^P(\lambda_R)$ ), while rich voters similarly prefer  $P_R$ . There are two cases to consider. First, if a poor voter perceives that her vote will not affect which party wins the election, then her vote will affect neither her expected redistribution benefit nor her expected pork allocation. She will therefore vote for  $P_L$  to secure the preferred ideological policy benefits from a friendly legislator. Second, if a poor voter resides in a pivotal district, her vote determines the national party winner. This generates a potential trade-off between the expected amounts of pork and redistribution. Comparing expected utilities, a poor voter chooses  $P_L$  if

$$u^{P}(\lambda_{L}) + \frac{\lambda_{L}b(\lambda_{L})}{n} + \frac{(1 - \lambda_{L})b(\lambda_{L})}{n^{P}} \ge u^{P}(\lambda_{R}) + \frac{\lambda_{R}b(\lambda_{R})}{n} + \frac{(1 - \lambda_{R})b(\lambda_{R})}{n^{P}}.$$
(1)

Since  $\lambda_L b(\lambda_L) \leq \lambda_R b(\lambda_R)$ , this condition is satisfied by the assumption that  $n^P < n$ . The calculation for rich voters is very similar. In a nonpivotal district, they effectively choose only on the basis of ideology and therefore always vote for  $P_R$ . In a pivotal district, a rich voter chooses  $P_R$  if

$$u^{R}(\lambda_{R}) + \frac{\lambda_{R}b(\lambda_{R})}{n} - \frac{b(\lambda_{R})}{n^{R}} \ge u^{R}(\lambda_{L}) + \frac{\lambda_{L}b(\lambda_{L})}{n} - \frac{b(\lambda_{R})}{n^{R}}.$$
 (2)

Since supporting  $P_R$  yields higher ideological utility, more pork, and lower taxes, this condition always holds.

We summarize these derivations in Proposition 1, which simply states that under weak parties, no crossover voting occurs. It is worth noting that the result does not require that poor (respectively, rich) voters strictly prefer  $P_L$  (respectively,  $P_R$ ) on ideological grounds.

PROPOSITION 1. When parties are weak, there is no crossover voting in equilibrium: rich voters support  $P_R$  and poor voters support  $P_L$ .

# 4. Strong Parties

We now consider the strong-party case. By controlling the legislative agenda and enforcing voting discipline, strong majority parties control the distribution of pork, and thus create crossover voting incentives by rich and poor. In contrast with the weak-party case, individuals may vote for the 'wrong' party—even when it gives them worse ideological policy, higher taxes (for the rich), or lower levels of redistribution (for the poor)—because so doing allows them to elect a legislator from the winning coalition, ensuring access to pork.

#### 4.1. Main Result

As before, poor voters prefer  $P_L$  on ideology and redistribution, and rich voters prefer  $P_R$  on these dimensions. However, both types of voters must now weigh these considerations against expectations of pork. To derive the equilibrium levels of support for each party, then, it is necessary to characterize the circumstances under which the rich and the poor will engage in crossover voting. The best responses for voters in each district will depend in part on whether that district is pivotal in determining the legislature's majority party.

Consider the optimal voting strategies in district  $S_k$ . Let  $w_{-k}$  represent the number of districts excluding  $S_k$  that are expected to vote for  $P_R$ . Also, let m = (n+1)/2 denote the size of the smallest majority of districts. Suppose initially that district  $S_k$ 's pivotal voter is rich. When would such a voter cross over and support  $P_L$ ? If the district is pivotal for the election outcome (i.e.,  $w_{-k} = m - 1$ ), then her expected utility from supporting the candidate from party  $P_i$  is

$$u^{R}(\lambda_{j}) + \frac{\lambda_{j}b(\lambda_{j})}{m} - \frac{b(\lambda_{j})}{n^{R}}.$$
 (3)

Since  $u^R(\lambda_R) > u^R(\lambda_L)$ ,  $\lambda_R b(\lambda_R)/m > \lambda_L b(\lambda_L)/m$ , and  $b(\lambda_R)/n^R \le b(\lambda_L)/n^R$ , the rich voter will never support  $P_L$ . That is, voting for the left would yield lower ideological utility, less pork, and potentially higher taxes than voting for the right, so crossover voting will not occur.

If instead a majority of other districts are expected to support  $P_R$  (i.e.,  $w_{-k} \ge m$ ), then a rich voter will not be pivotal in determining the legislative majority. She will cross over and support  $P_L$  only if

$$u^{R}(\lambda_{R}) + \frac{\lambda_{R}b(\lambda_{R})}{w_{-k} + 1} - \frac{b(\lambda_{R})}{n^{R}} < u^{R}(\lambda_{L}) - \frac{b(\lambda_{R})}{n^{R}}.$$

Since the rich voter gets more pork and higher ideological utility by supporting  $P_R$  (with no implications for taxes), this expression can obviously never be satisfied. Consequently, a rich voter might support  $P_L$  only if she lives in a nonpivotal district, and if a majority of districts are expected to support  $P_L$  (i.e., when  $w_{-k} < m - 1$ ). In this case, taxes again cancel out and a rich voter supports  $P_L$  if and only if

$$u^{R}(\lambda_{R}) - u^{R}(\lambda_{L}) < \frac{\lambda_{L}b(\lambda_{L})}{n - w_{L}}.$$
(4)

When  $w_{-k} < m-1$ , voting for  $P_L$  yields lower policy utility but more pork. The rich voter will vote for  $P_L$  if the loss in ideological utility is small relative to the gain in pork. Remark 1 combines these cases to summarize crossover voting behavior by voters in rich districts.

REMARK 1. Rich voters in a given district will support  $P_L$  if and only if a majority of other districts support  $P_L$  (i.e.,  $w_{-k} < m - 1$ ) and equation (4) holds.

Next, consider crossover voting by poor voters. In nonpivotal districts, their crossover voting incentives are similar to those of rich voters. If  $P_L$  is expected to win a majority of districts (i.e.,  $w_{-k} < m - 1$ ), then poor voters cannot influence the level of redistribution, and they obtain worse ideological policy and less pork by supporting  $P_R$ . That is, such poor voters will cross over and vote  $P_R$  only if

$$u^{P}(\lambda_{L}) + \frac{\lambda_{L}b(\lambda_{L})}{n - w_{-k}} < u^{P}(\lambda_{R}), \tag{5}$$

which clearly cannot be satisfied.

If poor voters are in a nonpivotal district but  $P_R$  is expected to win a majority of districts  $(w_{-k} \ge m)$ , then they again cannot influence the level of redistribution. In casting their vote, like the rich voter when  $P_L$  is expected to win a majority of districts, they must trade-off ideological policy from  $P_L$  against more pork from  $P_R$ . The poor voters in this case will cross over and vote for  $P_R$  if and only if

$$u^{P}(\lambda_{L}) - u^{P}(\lambda_{R}) < \frac{\lambda_{R}b(\lambda_{R})}{w_{-k} + 1}.$$
 (6)

The central difference between poor voters and rich voters occurs in pivotal districts. Recall that rich voters in a pivotal district will never vote for  $P_L$  because so doing results in worse ideological policy, less pork and potentially higher taxes. Poor voters in a pivotal district, by contrast, face a trade-off. If they support  $P_R$ , they receive *more* pork but less redistribution and worse ideological policy, so the poor voter in a pivotal district will cross over and support  $P_R$  if and only if

$$u^{P}(\lambda_{L}) + \frac{\lambda_{L}b(\lambda_{L})}{m} + \frac{(1 - \lambda_{L})b(\lambda_{L})}{n^{P}} < u^{P}(\lambda_{R}) + \frac{\lambda_{R}b(\lambda_{R})}{m} + \frac{(1 - \lambda_{R})b(\lambda_{R})}{n^{P}}.$$
(7)

Note that (7) implies (6) for  $w_{-k} = m - 1$ .

Remark 2 summarizes the crossover voting conditions for poor voters.

REMARK 2. Poor voters in a given district will support  $P_R$  if and only if either a majority of other districts support  $P_R$  (i.e.,  $w_{-k} \ge m$ ) and (6) holds, or if the district is pivotal (i.e.,  $w_{-k} = m - 1$ ) and (7) holds.

Together, Remarks 1 and 2 suggest two important implications of the equilibrium. First, Remark 1 indicates that rich voters will never cross over and support  $P_L$  when a majority of districts support  $P_R$ , and Remark 2 indicates that poor voters will never cross over and support  $P_R$  when there are a majority of districts supporting  $P_L$ . Thus, in any Nash equilibrium, the winning party must carry all like-minded districts. If  $P_L$  wins a legislative majority, then *all* districts for which poor voters are a majority must vote for  $P_L$ . Similarly, if  $P_R$  wins, all rich districts must vote for  $P_R$ . Second, the remarks suggest an important advantage that right-wing parties enjoy in pivotal districts. If a pivotal district has a majority of rich voters, then since these voters receive no redistribution and know that  $P_L$  offers less pork than  $P_R$ , they never face a trade-off

between ideological policy, pork, and redistribution. Rich voters in pivotal districts will therefore always support  $P_R$ , ensuring it of victory. By contrast, if a pivotal district has a majority of poor voters, then by (7), it is not certain that  $P_L$  will win because the poor voters may face a trade-off: supporting  $P_R$  will yield more pork, but supporting  $P_L$  will yield superior outcomes in ideological policy and redistribution. If the value of pork from  $P_R$  is relatively large, then poor voters may cross over and support  $P_R$  in a pivotal district.

We can now characterize the equilibrium levels of voter support for each party. It is useful to define explicitly the number of districts that will cross over if the 'wrong' party is expected to win. If  $P_R$  is expected to win a majority of seats, then Remark 2 indicates that the number of nonpivotal poor districts supporting  $P_R$  is

$$\bar{w} = \begin{cases} 0 & \text{if } u^{P}(\lambda_{L}) - u^{P}(\lambda_{R}) > \frac{\lambda_{R}b(\lambda_{R})}{d^{R} + 1}, \\ \max w \text{ s.t. } u^{P}(\lambda_{L}) - u^{P}(\lambda_{R}) < \frac{\lambda_{R}b(\lambda_{R})}{(d^{R} + w)} \\ & \text{if } u^{P}(\lambda_{L}) - u^{P}(\lambda_{R}) \in \left[\frac{\lambda_{R}b(\lambda_{R})}{n}, \frac{\lambda_{R}b(\lambda_{R})}{d^{R} + 1}\right] \\ d^{P} & \text{otherwise.} \end{cases}$$
(8)

Intuitively,  $\bar{w}$  is the size of the largest collection of poor districts such that poor voters contained within are willing to support  $P_R$ . Since  $\lambda_R b(\lambda_R)/(d^R + w)$  is decreasing in w,  $\bar{w}$  is uniquely defined. When the relative value of pork is sufficiently low, no districts crossover vote, and when the relative value of pork is sufficiently strong, all poor districts crossover vote.

Similarly, we define the (unique) number of nonpivotal rich districts that would support  $P_L$  if  $P_L$  is expected to win as

$$\underline{w} = \begin{cases}
0 & \text{if } u^{R}(\lambda_{R}) - u^{R}(\lambda_{L}) > \frac{\lambda_{L}b(\lambda_{L})}{d^{P} + 1}, \\
\max w \text{ s.t. } u^{R}(\lambda_{R}) - u^{R}(\lambda_{L}) < \frac{\lambda_{L}b(\lambda_{L})}{(d^{P} + w)} \\
& \text{if } u^{R}(\lambda_{R}) - u^{R}(\lambda_{L}) \in \left[\frac{\lambda_{L}b(\lambda_{L})}{n}, \frac{\lambda_{L}b(\lambda_{L})}{d^{P} + 1}\right] \\
d^{R} & \text{otherwise.} 
\end{cases} \tag{9}$$

Let  $w^*$  be the number of districts supporting the winning party. We can use  $\bar{w}$  and  $\underline{w}$  to characterize the unique winner and  $w^*$  in a coalition-proof Nash equilibrium. The CPNE are unique up to combinations of the districts supporting each party, and we therefore use the term 'unique' in this context.<sup>5</sup>

<sup>5.</sup> Since districts of a given type have pivotal voters with identical preferences, any combination of  $\bar{w}$  poor districts (or  $\underline{w}$  rich ones) could vote with the winners in equilibrium. If voters of a given type were ideologically heterogeneous, then  $\bar{w}$  and  $\underline{w}$  would not be unique and some combinations would be impossible in a coalition, since districts would differ in their propensities to crossover vote.

PROPOSITION 2. There is a unique coalition-proof Nash equilibrium, where

- (i) if  $d^R \ge m$  then  $P_R$  wins and  $w^* = d^R + \bar{w}$ ,
- (ii) if  $d^R < m$  and (7) is satisfied, then  $P_R$  wins and  $w^* = d^R + \bar{w}$ ,
- (iii) if  $d^R < m$  and (7) is not satisfied, then  $P_L$  wins and  $w^* = d^P + \underline{w}$ .

*Proof.* Notationally, let  $\mathcal{D}$  denote the set of all districts,  $\mathcal{W}$  a generic winning coalition of districts, and  $\mathcal{C}$  a subcoalition of deviators from a prescribed strategy profile.

Observe first that by equation (8), the number of poor districts supporting  $P_R$  in a Nash equilibrium cannot be greater than  $\bar{w}$  (otherwise, a poor district supporting  $P_R$  would prefer switching to  $P_L$ ) or less than  $\bar{w}$  (otherwise, a poor district supporting  $P_L$  would prefer switching to  $P_R$ ). Thus, only  $\bar{w}$  poor districts can support  $P_R$  in a Nash equilibrium. Likewise, by equation (9), the number of rich districts supporting  $P_L$  in a Nash equilibrium can only be  $\underline{w}$ . Thus, for any configuration of districts and voter preferences, a profile of voting strategies in which each citizen votes as if she were pivotal is a Nash equilibrium only if:  $P_R$  wins and  $w^* = d^R + \bar{w}$  (with all rich districts voting for  $P_R$ ), or  $P_L$  wins and  $w^* = d^P + \underline{w}$  (with all poor districts voting for  $P_L$ ).

For either of these two strategy profiles to be a CPNE, it must be both self-enforcing and undominated by another self-enforcing strategy profile. Showing that a strategy profile is self-enforcing requires showing that each subcoalition  $\mathcal C$  is playing a CPNE when holding the strategies of players not in  $\mathcal C$  constant. It is clear that neither of the two possible Nash equilibria Pareto dominates the other. Thus for each case, we consider whether either of the two possible Nash equilibria is self-enforcing.

(i) Suppose that a CPNE in which  $P_L$  wins exists. Then for any winning coalition of size  $|\mathcal{W}|$ , any subcoalition  $\mathcal{C}$  of  $|\mathcal{W}|-m+1$  rich districts would prefer to defect collectively to  $P_R$ . All such defectors would receive  $u^R(\lambda_R) + \lambda_R b(\lambda_R)/m - b(\lambda_R)/n^R$ , which is strictly higher than their payoff of  $u^R(\lambda_L) + \lambda_L b(\lambda_L)/|\mathcal{W}| - b(\lambda_L)/n^R$  in the original coalition. Members of an arbitrary proper subset of  $\mathcal{C}$  of size d would then receive  $u^R(\lambda_L) + \lambda_L b(\lambda_L)/(|d| + m - 1) - b(\lambda_L)/n^R$  by deviating back to  $P_L$ . Since it is not profitable for any member of  $\mathcal{C}$  to deviate back to  $P_L$ , the deviation by  $\mathcal{C}$  is self-enforcing, contradicting that a CPNE exists in which  $P_L$  wins.

To show that a  $P_R$  victory is a CPNE, observe first that by Remarks 1 and 2, and equation (8), the strategy profile under which  $\mathcal{W}$  contains all rich districts and  $\bar{w}$  poor districts voting for  $P_R$  is a Nash equilibrium. To show coalition proofness, consider any potential subcoalition of deviators  $\mathcal{C}$ . Suppose that  $\mathcal{C}$  contains at least one rich district. Remark 1 then implies that any profitable deviation must result in a  $P_L$  victory. By equation (3) and the previous argument, a subcoalition of  $\mathcal{C}$  of rich districts would have a self-enforcing deviation to form a minimal-winning  $P_R$  coalition. Thus  $\mathcal{C}$  can consist only of poor districts, and cannot affect  $P_R$ 's victory. By equation (8), no subcoalition of poor districts in  $\mathcal{W}$  can do better by switching to  $P_L$ , and no subcoalition of districts in  $\mathcal{D} \setminus \mathcal{W}$  can do better by switching to  $P_R$ . Finally, any  $\mathcal{C}$  containing poor districts from both  $\mathcal{W}$  and  $\mathcal{D} \setminus \mathcal{W}$  cannot strictly increase the payoffs of all poor voters in  $\mathcal{C}$ . The unique CPNE therefore has  $w^* = d^R + \bar{w}$  districts supporting  $P_R$ .

(ii) We first show that  $P_L$  cannot win in equilibrium when equation (7) is satisfied. Suppose otherwise. Because  $|\mathcal{W}| = m$  would imply that poor voters in pivotal districts vote for  $P_L$  in violation of (7), it follows that  $|\mathcal{W}| > m$ . The maximum payoff that poor voters from poor districts could therefore ever receive from a  $P_L$  majority would occur when  $|\mathcal{W}| = m + 1$ . Such a majority would yield poor voters in  $\mathcal{W}$  a utility of

$$u^{P}(\lambda_{L}) + \frac{\lambda_{L}b(\lambda_{L})}{m+1} + \frac{(1-\lambda_{L})b(\lambda_{L})}{n^{P}}$$
$$< u^{P}(\lambda_{L}) + \frac{\lambda_{L}b(\lambda_{L})}{m} + \frac{(1-\lambda_{L})b(\lambda_{L})}{n^{P}}.$$

But since by equation (7) we have

$$u^{P}(\lambda_{L}) + \frac{\lambda_{L}b(\lambda_{L})}{m} + \frac{(1 - \lambda_{L})b(\lambda_{L})}{/n^{P}}$$

$$< u^{P}(\lambda_{R}) + \frac{\lambda_{R}b(\lambda_{R})}{m} + \frac{(1 - \lambda_{R})b(\lambda_{R})}{n^{P}},$$

the utility to poor voters in poor districts from a minimal winning majority for  $P_R$  is greater than the utility from any possible  $P_L$  majority. From this it follows that if a majority of size  $|\mathcal{W}| \geq m+1$  formed for  $P_L$ , there would exist a subcoalition  $\mathcal{C}$  of  $|\mathcal{W}|-m+1$  poor districts that would prefer to defect collectively to  $P_R$ , thus inducing a minimum winning  $P_R$  majority. To show that the deviation by  $\mathcal{C}$  is self-enforcing, note again that by equation (7), there is no subset of  $\mathcal{C}$  that would prefer to defect back and support  $P_L$ , because all members prefer a minimum winning coalition for  $P_R$  to any winning coalition for  $P_L$ . This contradicts the existence of a CPNE where  $P_L$  wins.

It remains to show that a  $P_R$  victory with  $w^* = d^R + \bar{w}$  represents a CPNE. Observe first that equations (7) and (8) and Remarks 1 and 2 establish that it is a Nash equilibrium for  $\mathcal{W}$  to contain all rich districts and  $\bar{w} \geq m - d^R$  poor districts, all voting for  $P_R$ .

To show that this equilibrium is coalition-proof, there are two cases for a potential deviating coalition  $\mathcal{C}$ . First, suppose that  $P_R$  wins with the support of w' districts. Remark 1 then implies that no rich district can belong to  $\mathcal{C}$ , and hence  $\mathcal{C}$  can contain only poor districts. There are two subcases: either  $w^* \neq w'$  or  $w^* = w'$ . In the former subcase, equation (8) implies that at least one poor district in  $\mathcal{C}$  does strictly worse under the deviation. In the latter, the new strategy profile simply permutes the strategies of poor districts in the original profile, and thus not all districts in  $\mathcal{C}$  strictly benefit from the deviation.

Second, suppose that  $P_L$  wins. By an argument identical to that in the proof that  $P_L$  cannot win in a CPNE, there exists a self-enforcing deviation by a proper subset of districts in  $\mathcal{C}$  that would give  $P_R$  a minimum winning coalition. This deviation is better for poor districts in  $\mathcal{C}$  than any possible winning coalition for  $P_L$  when equation (7) is satisfied. It must therefore also be better for any rich district in  $\mathcal{C}$ .

Thus there does not exist a self-enforcing deviation for C. We conclude that in the unique CPNE,  $w^* = d^R + \bar{w}$ .

(iii) This proof is symmetric to that of case (i) and is therefore omitted.  $\Box$ 

Proposition 2 demonstrates that when parties are strong, crossover voting incentives exist for rich and poor alike, as voters in both income groups may have incentives to support the 'wrong' party in order to ensure access to pork. The extent to which this occurs depends on how voters weigh ideological policy, taxes, redistribution, and pork.

The general intuition for the model rests on the link between district-level voting incentives and national outcomes. Figure 1 illustrates this link. In the example, there are six poor districts and five rich districts. Suppose that if  $P_L$  is expected to win, one rich district would support  $P_L$  (i.e.,  $\underline{w}=1$ ), and if  $P_R$  is expected to win, three poor districts would support  $P_R$  (i.e.,  $\overline{w}=3$ ). The figure depicts the only two Nash equilibria that can exist in the case. In Nash Equilibrium 1,  $P_L$  wins with the support of all poor districts and one rich district. Similarly, in Nash Equilibrium 2, all rich districts must support  $P_R$ , joined by three poor districts.

Which one of these equilibria is the unique CPNE depends on whether a poor pivotal district prefers a  $P_L$  or  $P_R$  legislative majority. Suppose that a pivotal poor district would vote for  $P_R$ . Then Nash Equilibrium 1 is not a strong Nash equilibrium because one rich district and one poor district would prefer to switch to  $P_R$ . It also cannot be a CPNE because neither defecting district could have an incentive to defect back to supporting  $P_L$ : both defecting districts would be pivotal in maintaining a  $P_R$  majority, and both prefer  $P_R$  when they are pivotal. Now consider Nash Equilibrium 2. This equilibrium may not be strong, since three poor districts might prefer to switch jointly to  $P_L$ . That is, it may be better for the three poor districts to be part of a minimum winning coalition for  $P_L$  than part of an oversized coalition (of size 8) for  $P_R$ . Nash Equilibrium 2 is coalition-proof, however, since any such defection to  $P_L$  is vulnerable to defection back to  $P_R$ : any one of the three defecting poor districts would be pivotal and would thus prefer switching to  $P_R$ , regaining a winning coalition for that party. The example therefore illustrates how crossover voting by the poor can occur even when the poor have a majority of districts.

By the same logic, if a pivotal poor district prefers  $P_L$ , then Nash Equilibrium 2 is not a CPNE because the three poor districts supporting  $P_R$  would prefer switching to  $P_L$ . And Nash Equilibrium 1 is a CPNE: no coalition defecting from the majority would be stable because it would have to contain enough poor districts to change the majority to  $P_R$ , and in any such coalition, poor districts would defect back to supporting  $P_L$ . Thus crossover voting by the rich can occur when the poor control a majority of districts and a pivotal poor voter prefers  $P_L$ .

### 4.2. Implications

The equilibria described in Propositions 1 and 2 yield several insights about how the availability of district-based pork and income-based redistribution affects voting

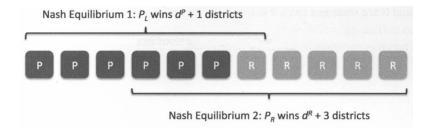


FIGURE 1. Nash equilibria when  $\bar{w} = 3$  and w = 1.

behavior and election outcomes. We focus here on how party discipline affects incomebased voting, the right-wing advantage that exists under strong parties, and the factors affecting crossover voting—and thus the size of legislative coalitions—in strong-party systems.

Party Discipline and Income-Based Voting. Propositions 1 and 2 make a simple but important point about how income and voting should be related across different types of party systems. If a voter believes that electoral outcomes will not affect the distribution of pork, then they can vote their redistributive interests, whereas if they believe that their access to government pork depends on their being represented by someone from the majority party, then they may vote against their redistributive interests to gain access to pork. We have argued that party discipline should play a central role in shaping these expectations. In systems where parties are weak and do not constrain legislative bargaining over pork, voters need not worry about how elections affect pork, and thus can vote their redistributive interests. In systems where a disciplined majority party controls the distribution of pork, both rich and (especially) poor voters will have incentives to cross over and vote for the 'wrong' party. We should therefore expect to see the strongest relationship between income and the vote in systems with weak parties.

From a voter's perspective, the benefits of party strength are ambiguous. Strong parties tend to help voters in the winning coalition, since they will not have to share pork with election losers. Thus, when a majority of districts are rich, a poor district must either forego pork entirely or elect an ideologically undesirable representative. By contrast, weak parties tend to help voters who expect to lose the election, and so a poor voter might prefer weak parties when poor districts are in the minority.

Party Discipline and the Right-Party Advantage. Since party strength affects voting incentives by conditioning expectations regarding pork, strong parties also create an asymmetry between crossover voting incentives for rich and poor, one that advantages right-wing parties. Because the right-wing party wants to limit redistribution, it has more government revenues available for pork—even if the left-wing party funds all the 'extra' redistribution it advocates with taxes on the rich (this follows from the fact

that  $\lambda_j b(\lambda_j)$  is increasing in  $\lambda_j$ ). This implies that poor voters have a greater incentive to cross over than do rich voters.

This fact has two implications for the right-wing party's electoral prospects. First, as Proposition 2 describes and Figure 1 illustrates, even if a majority of districts are poor, the right-wing party might win due to crossover voting by the poor. By contrast, if rich voters control a majority of districts, the left-wing party will never win. Second, left-wing coalitions are 'smaller' than right-wing coalitions. That is, given identical levels of ideological supporters across districts, a right-wing coalition would attract more crossover districts than a left-wing coalition. The following remark follows immediately from equations (8) and (9).

REMARK 3. The number of districts voting for  $P_L$  when  $P_L$  wins and d districts are poor is no greater than the number of districts voting for  $P_R$  when  $P_R$  wins and d districts are rich.

The analysis therefore suggests a different explanation for why right-wing parties have an advantage in majoritarian systems (e.g., Iversen and Soskice 2006), one that is grounded in distributive politics. It further suggests that this advantage should be contingent on the existence of strong parties. On this point, it is interesting to note that the Democrats in the 'weak-party' United States have controlled majorities in the US House of Representatives for much more time than have left-wing parties in 'strong-party' majoritarian systems like Australia, Britain, Canada, Ireland, Japan, and New Zealand (until 1993). Using data from Iversen and Soskice, for example, from 1945–1998, right-wing parties controlled government 74% of the time in these strongparty countries, whereas the left-wing Democrats controlled the US House in all but six years (or over 90% of the time).

Crossover Voting by the Pivotal Poor District when Parties are Strong. The effect of strong parties on voting outcomes depends to a large degree on the behavior of the poor voters in pivotal districts. Equation (7) determines how pivotal poor citizens vote and by extension whether  $P_R$  can win even in the face of a majority of poor districts. It is therefore useful to underscore two factors that affect whether this condition is satisfied. First, the value of general redistribution declines with the number of poor individuals, decreasing the relative value to pivotal poor voters of supporting  $P_L$  (and thus making it easier to satisfy (7)). Crossover voting therefore increases as the number of poor voters increases. Second, the budget constraint (c) influences the relative value of supporting  $P_L$ . When c is at its minimum, the budget constraint is weakest, and every dollar devoted to redistribution is paid for by additional taxes on the rich. As the budget constraint tightens (c) increases, so too does the budgetary trade-off between redistribution and pork. Under the most constrained budget (c = 1), there is a one-to-one trade-off between pork and general redistribution, so any resources for pork must be taken from the budget for redistribution. Thus, the relative value of supporting the

left-wing party declines—and incentives for crossover voting by the poor increase—as the budget constraint tightens.<sup>6</sup>

# 5. Can the Left Compete on Pork?

In the strong-party model, the right-wing advantage occurs in part because of the assumption that the left-wing party has a greater commitment to redistributive spending. A consequence of this assumption, embodied by the budget constraint parameter c, is that the right can always offer more pork and therefore attract more crossover votes. As already argued, we feel that assuming  $c \in [0, 1]$  is a very reasonable constraint on the ability of left parties to tax. But it is nonetheless worth asking whether the left can overcome the right-wing advantage by setting taxes so high with a negative c that it offers more redistribution and pork than the right-wing party.

The next remark establishes two effects of large budgets on  $P_L$ 's competitiveness. First, pivotal poor voters can be induced to vote always for  $P_L$  if c is sufficiently small and the left-wing platform is more moderate than the right-wing platform. Under these conditions  $P_L$  offers more pork (i.e.,  $\lambda_L b(\lambda_L) \ge \lambda_R b(\lambda_R)$ ), and as a result, equation (7) cannot be satisfied and poor voters will not allow  $P_R$  to win when a majority of districts are poor. Second, even when  $P_L$  can offer more pork than  $P_R$ , the symmetric condition to equation (7) for pivotal rich voters to cross over is difficult to satisfy. The necessary condition in the remark cannot hold, for example, if  $n^R < m$  (i.e., rich voters are not a large majority of the total population), or even if  $\lambda_L \le 1/2$  (i.e., the left-wing party spends less than half the budget on pork). The reason is that rich voters are taxed for the very large budget that would provide both more generous redistribution and more pork. This suppresses  $P_L$ 's pork advantage and also the rich voters' incentives to cross over.

PROPOSITION 3. For c < 0,

(i) pivotal poor voters vote for  $P_L$  if

$$\left|\lambda_L - \frac{1}{2}\right| \leq \left|\lambda_R - \frac{1}{2}\right| \quad and \quad c \leq \frac{\lambda_L(2 - \lambda_L) - \lambda_R(2 - \lambda_R)}{\lambda_L(1 - \lambda_L) - \lambda_R(1 - \lambda_R)},$$

(ii) pivotal rich voters vote for  $P_L$  only if

$$\lambda_L > \frac{1}{2}, \quad c < \frac{\lambda_L(2 - \lambda_L) - \lambda_R(2 - \lambda_R)}{\lambda_L(1 - \lambda_L) - \lambda_R(1 - \lambda_R)} \quad and \quad n^R > \frac{m}{\lambda_L}.$$

Proof.

(i) It is easily verified that if  $\lambda_L b(\lambda_L) \ge \lambda_R b(\lambda_R)$ , then equation (7) cannot be satisfied and pivotal poor voters will vote for  $P_L$ . This condition reduces to

$$\lambda_L(2-\lambda_L) - \lambda_R(2-\lambda_R) \ge [\lambda_L(1-\lambda_L) - \lambda_R(1-\lambda_R)]c. \tag{10}$$

<sup>6.</sup> The effect of polarization in party platforms  $(\lambda_i)$  on crossover voting by the poor is ambiguous.

The left-hand side of (10) is always negative. Thus when c < 0, (10) holds if and only if  $\lambda_L(1 - \lambda_L) \ge \lambda_R(1 - \lambda_R)$ , or equivalently  $|\lambda_L - 1/2| \le |\lambda_R - 1/2|$ , and  $c \le (\lambda_L(2 - \lambda_L) - \lambda_R(2 - \lambda_R))/(\lambda_L(1 - \lambda_L) - \lambda_R(1 - \lambda_R))$ .

(ii) From equation (3), a pivotal rich voter votes for  $P_L$  if

$$u^{R}(\lambda_{L}) + \frac{\lambda_{L}b(\lambda_{L})}{m} - \frac{b(\lambda_{L})}{n^{R}} > u^{R}(\lambda_{R}) + \frac{\lambda_{R}b(\lambda_{R})}{m} - \frac{b(\lambda_{R})}{n^{R}}.$$
 (11)

Noting that  $u^R(\lambda_R) > u^R(\lambda_L)$  and rearranging terms, (11) holds only if  $(\lambda_L b(\lambda_L) - \lambda_R b(\lambda_R))/m > (b(\lambda_L) - b(\lambda_R))/n^R$ . Since  $b(\lambda_L) - b(\lambda_R) > 0$ , this requires  $\lambda_L b(\lambda_L) > \lambda_R b(\lambda_R)$ , which is the same condition as in part (i), but with a strict inequality. Further, since  $\lambda_L \leq \lambda_R$ , (11) can hold only if

$$\frac{\lambda_L(b(\lambda_L) - b(\lambda_R))}{m} > \frac{b(\lambda_L) - b(\lambda_R)}{n^R}.$$
 (12)

Reducing yields the necessary condition  $n^R > m/\lambda_L$ . Finally,  $n^R > m/\lambda_L$  cannot be satisfied if  $\lambda_L \le 1/2$ , and so  $|\lambda_L - 1/2| \le |\lambda_R - 1/2|$  reduces to  $\lambda_L > 1/2$ .

The implications of this remark for the set of possible CPNE are significant. Applying the same equilibrium derivation as that in Proposition 2, there exist conditions—unrealistic ones in our view—when the left-wing party can negate the right-wing advantage with very high taxes and budgets. And unless some very constraining parameter restrictions are satisfied, when a majority of districts are rich, rich voters will not join a  $P_L$  coalition. More typically, the party whose natural constituents control a majority of districts will win. Thus, while an outsized left budget may indeed eliminate the right-wing advantage, it is more difficult for the left to gain a corresponding left-wing advantage.

### 6. Conclusion

When deciding how to vote, issues unrelated to economic well-being undoubtedly influence citizen choices. Our analysis, however, cautions against assuming *either* that this is the only reason why voters may support the 'wrong' party *or* that when voters vote against their redistributive interests, they are voting against their economic interests. Redistribution from rich to poor is but one way that governments distribute tax revenues, and voters may maximize their economic well-being by supporting a party that is not their most-preferred on that issue.

By focusing on pork-barrel politics, the model here explores one of the central ways that governments distribute revenues on a basis unrelated to individual income. A central intuition from the model concerns the importance of legislative party discipline in an environment where parties cannot commit to distributive platforms. When parties

<sup>7.</sup> Of course, equation (7) is also not always satisfied, though the analogous parameter restrictions on whether pivotal poor voters will cross over are less demanding than those for the rich.

are weak, voters expect the same level of pork no matter which party they support, and thus redistributive preferences are fundamental to vote choice. When parties are strong, by contrast, the winning party can exclude losers from pork. The stark contrast between winning and losing in this setting makes pork an especially efficient way to attract voters. This causes voters to weigh a trade-off between pork and income-based redistribution. The value of being included in the majority-controlled pork-coalition will often be decisive, resulting in crossover voting. Our model therefore suggests that crossover voting levels should be highest in systems where the majority party in the legislature can concentrate the distribution of pork in electorally supportive districts.

The analysis also brings into sharp relief an advantage that rich voters and right-wing parties should have in majoritarian systems with strong parties. Since the right-wing party can offer more pork, it benefits when voters have pork-based incentives to elect a legislator from the expected majority party. Rich voters in pivotal districts never support left-wing parties, but poor voters in pivotal districts may support right-wing parties. The incentives of poor voters to do so increases as the population of poor voters increases and as constraints on the government budget increase. These crossover voting incentives also imply that all things equal, right-wing legislative majorities should be larger than left-wing majorities.

Two limitations of our model suggest avenues for further research. First, the model treats party strength as exogenous. As the previous analysis suggests, party strength has implications for the expected payoffs of party members, and it would therefore be interesting to consider ways in which party strength might evolve in response to the electoral incentives posed in our model. Second, the model assumes that eligibility for redistribution—or the identity of the 'poor'—is exogenous. Analyzing endogenous determination of eligibility for redistribution programs may require a richer set of assumptions about voter types and taxation, but may make it possible to understand how politicians create electoral coalitions that transcend economic groups.

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