## TDA Analysis

## Yakub Akhmerov May 9, 2018

Intro: I began the semester with a lingering feeling of immersing myself into something intellectually stimulating. I stumbled across topology in my Real Analysis course fall of 2017. I generally enjoyed working on it and noticed the beautiful generalized, objective theory behind it. Since my field is data science and analytics, I figured it would be appropriate to combine two fields which I am genuinely interested in and go from through. Thus, I stumbled upon topological data analysis.

I reached out to several profession sources and eventually stumbled upon Dmitriy Mozorov at the Berkeley Institute of Data Science. He advised me in this research and was a great in my concrete understanding of the subject. To demonstrate my new found abilities in topological data analysis, I choose to apply my understanding to a project.

#### Topological Data Analysis

Problem: How well can TDA be used on cyrptocurrency data?

Testing on Binance API Data

Description: We provide daily cryptocurrency data (transaction count, on-chain transaction volume, value of created coins, price, market cap, and exchange volume) in CSV format. The data sample stretches back to December 2013. We explain the column titles and some shortcomings here.

Source: https://coinmetrics.io/data-downloads/## ID sample code number (not unique). #V1 date: Date on georgian calender. #V2 txVolume(USD): "on-chain transaction volume." Essentially a broad and largely unadjusted measure of the total value of outputs on the blockchain, on a given day. #V3 txCount: Number of transactions happening on the public blockchain a day. The is a broad estimation. More can be explained in the source as to why that is. #V4 marketcap(USD): The unit price multiplied by the number of units in circulation. #V5 Price: Open price, received from CoinMarketCap. #V6 exchangevolume(USD): The dollar value of the volume at exchanges. Also received from CoinMarketCap. #V7 generatedCoins: The number of new coins that have been brought into existence on that day #V8 Fees: Fees. One important peice of information is that the fees in this data are based on the native currency, not USD.

## Packages needed for the analysis

(1) Cleaning the data. A lot of wrangling needed to be done. The variables were put into strings in the original dataset so they had to be converted into variables in order to do any sort of analysis.

```
setwd("~/Documents/TDA/")
btc = read.csv("btc.csv", header = F)
btc = btc[-1,]
btc <- btc[1:8]</pre>
```

```
btc$V2 <- as.numeric(as.character(btc$V2))</pre>
btc$V3 <- as.numeric(as.character(btc$V3))</pre>
btc$V4 <- as.numeric(as.character(btc$V4))</pre>
btc$V5 <- as.numeric(as.character(btc$V5))</pre>
btc$V6 <- as.numeric(as.character(btc$V6))</pre>
btc$V7 <- as.numeric(as.character(btc$V7))</pre>
btc$V8 <- as.numeric(as.character(btc$V8))</pre>
breaks <- c(65, 2565, 5065, 7565, 10065, 12065, 15065, 17065, 20065)
btc <- btc %>%
  mutate(Price_bin = cut(V5, breaks)) #categorize the price of the coin into 12 bins.
head(btc) # see header to decode V1-V8;
             V1
                        ۷2
                              VЗ
                                          ۷4
                                                 V5 V6
                                                         ۷7
## 1 2013-05-01 108659660 52443 1542820000 139.00
                                                    0 3575 36.80600
## 2 2013-05-02 96958519 55169 1292190000 116.38
                                                     0 3425 54.40792
## 3 2013-05-03 84459697 55636 1180070000 106.25
                                                     0 3650 48.52677
## 4 2013-05-04 41545845 48595 1089890000 98.10
                                                     0 3900 43.41969
## 5 2013-05-05 56205930 49907 1254760000 112.90
                                                    0 3875 38.40896
## 6 2013-05-06 78921301 52523 1289470000 115.98 0 4250 51.88924
##
         Price bin
## 1 (65,2.56e+03]
## 2 (65,2.56e+03]
## 3 (65,2.56e+03]
## 4 (65,2.56e+03]
## 5 (65,2.56e+03]
## 6 (65,2.56e+03]
summary(btc)
                             V2
##
             V1
                                                  V3
                              :3.379e+07
##
    2013-05-01:
                  1
                      Min.
                                            Min.
                                                   : 29566
    2013-05-02:
                       1st Qu.:2.362e+08
                                            1st Qu.: 71728
                      Median :6.326e+08
##
    2013-05-03:
                                            Median :154048
                  1
##
    2013-05-04:
                  1
                      Mean
                              :2.580e+09
                                            Mean
                                                   :162430
##
    2013-05-05:
                      3rd Qu.:1.756e+09
                                            3rd Qu.:234748
                  1
##
    2013-05-06:
                   1
                      Max.
                              :4.835e+10
                                            Max.
                                                   :490459
##
    (Other)
              :1828
##
          ۷4
                               ۷5
                                                                       ۷7
##
           :7.793e+08
                                    68.5
                                                   :0.000e+00
                                                                        :1000
                         Min.
                                            Min.
   \mathtt{Min}.
                                                                 Min.
   1st Qu.:4.030e+09
                         1st Qu.: 282.5
                                            1st Qu.:1.713e+07
                                                                 1st Qu.:2000
##
   Median :7.113e+09
                         Median : 530.1
                                            Median :4.720e+07
                                                                 Median:3575
    Mean
           :2.915e+10
                         Mean
                                : 1791.2
                                            Mean
                                                   :1.103e+09
                                                                 Mean
                                                                        :3230
##
    3rd Qu.:1.605e+10
                         3rd Qu.: 1013.5
                                            3rd Qu.:2.010e+08
                                                                 3rd Qu.:4050
##
    Max.
           :3.261e+11
                         Max.
                                :19475.8
                                            Max.
                                                   :2.384e+10
                                                                 Max.
                                                                        :6450
##
##
          ٧8
                                      Price_bin
##
    Min.
          :
               7.856
                        (65,2.56e+03]
                                            :1521
             15.406
                        (2.56e+03,5.06e+03]: 105
    1st Qu.:
##
    Median :
              35.250
                        (7.56e+03,1.01e+04]: 77
           : 89.874
##
                        (5.06e+03,7.56e+03]: 50
   Mean
    3rd Qu.: 84.965
                        (1.01e+04,1.21e+04]: 39
## Max.
                        (1.21e+04,1.51e+04]: 19
           :1495.947
```

Mean

:162430

3rd Qu.:234748

1 Mean :2.580e+09

## 2013-05-05: 1 3rd Qu.:1.756e+09

##

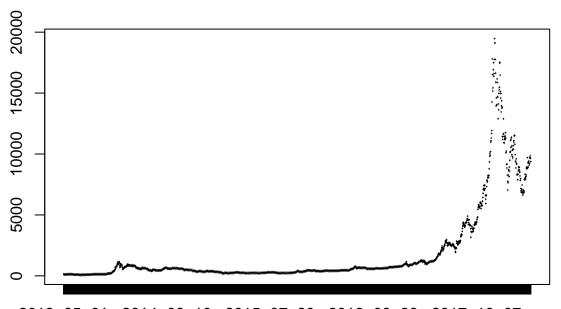
2013-05-04:

```
:4.835e+10
    2013-05-06:
                  1
                      Max.
                                           Max.
                                                   :490459
##
    (Other)
              :1828
##
          ٧4
                               ۷5
                                                  V6
                                                                       ۷7
           :7.793e+08
                                    68.5
                                                   :0.000e+00
                                                                        :1000
##
                        Min.
                                           Min.
                                                                 Min.
    Min.
##
    1st Qu.:4.030e+09
                         1st Qu.:
                                   282.5
                                            1st Qu.:1.713e+07
                                                                 1st Qu.:2000
    Median :7.113e+09
                         Median : 530.1
                                           Median :4.720e+07
                                                                 Median:3575
##
    Mean
          :2.915e+10
                         Mean
                               : 1791.2
                                                   :1.103e+09
                                                                 Mean
                                                                        :3230
                                           Mean
                         3rd Qu.: 1013.5
    3rd Qu.:1.605e+10
                                            3rd Qu.:2.010e+08
                                                                 3rd Qu.:4050
##
##
    Max.
           :3.261e+11
                         Max.
                                :19475.8
                                           Max.
                                                   :2.384e+10
                                                                 Max.
                                                                        :6450
##
##
          ۷8
                                      Price_bin
               7.856
                        (65,2.56e+03]
##
    Min.
                                            :1521
    1st Qu.:
              15.406
                        (2.56e+03,5.06e+03]: 105
##
    Median :
              35.250
                        (7.56e+03,1.01e+04]: 77
##
##
    Mean
          : 89.874
                        (5.06e+03,7.56e+03]:
##
    3rd Qu.: 84.965
                        (1.01e+04,1.21e+04]:
##
    Max.
           :1495.947
                        (1.21e+04,1.51e+04]:
                                              19
##
                        (Other)
                                               23
```

#### EDA

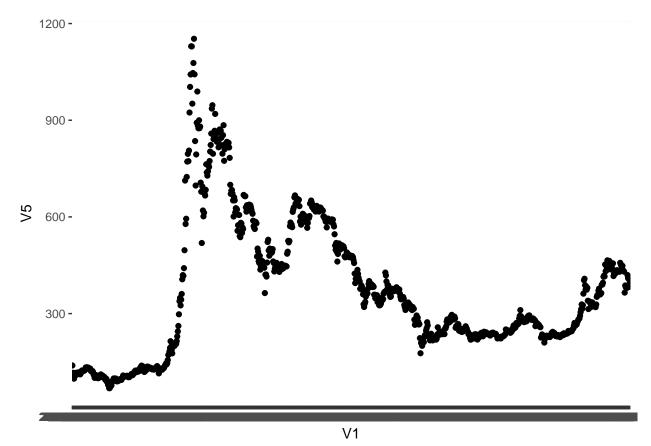
plot(x = btc\$V1, y = btc\$V5, main = "Price of bitcoin since 2013")

### Price of bitcoin since 2013



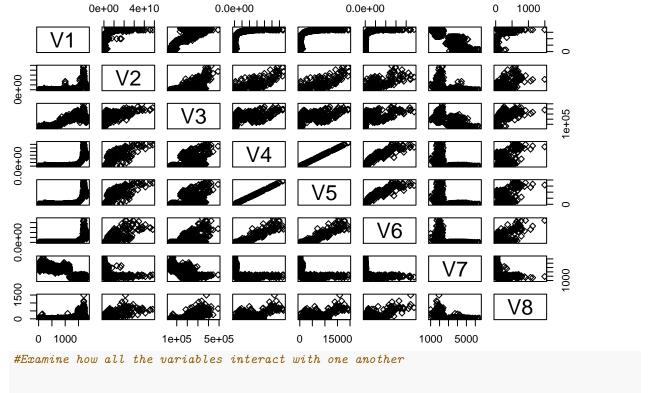
2013-05-01 2014-06-10 2015-07-20 2016-08-28 2017-10-07

 $ggplot(btc[1:1000,]) + aes(x=V1, y = V5) + geom_point()$ 



```
#Examine how the bins are distributed
plot(btc[1:8], main="bitcoin data set", pch=23, bg = c("red", "green")
        [unclass(btc$price)])
```

#### bitcoin data set



data <- btc[2:8] ## Take out date variable
D = dist(scale(data)) # use Euclidean distance on data
## DIST: This function computes and returns the distance matrix computed by using the specified distance</pre>

DIFFUSE: Description: Uses the pair-wise distance matrix for a data set to compute the diffusion map coefficients. Computes the Markov transition probability matrix, and its eigenvalues and left & right eigenvectors. Returns a 'dmap' object.

The following code cannot be run due to technical difficulties with the igraph package. However rather than putting it into a code chance I figured it'd be good to leave it here and work on it once Rstudio fixes the bugs in this package and updates it.

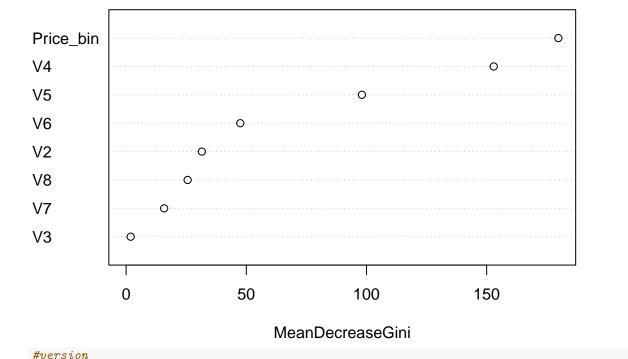
dmap = diffuse(D, eps.val=10, t=1, neigen=2) ## just run with the standard default settings plot(dmapX[,1], dmapX[,2], col=outcome,pch=paste(outcome), xlab="Diffusion Map Coordinate 1", ylab="Diffusion Map Coordinate 2", main="Diffusion Map of Bitcoin data")

# 2) OK - now Use random forest "Department" classifier to define distances

```
bins = btc$Price_bin
data = btc[2:9]
```

```
rf_fit = randomForest(data, bins, ntree=10, proximity=TRUE)
print(rf_fit)
##
## Call:
    randomForest(x = data, y = bins, ntree = 10, proximity = TRUE)
##
                  Type of random forest: classification
                         Number of trees: 10
##
## No. of variables tried at each split: 2
##
##
           OOB estimate of error rate: 0.44%
## Confusion matrix:
                        (65,2.56e+03] (2.56e+03,5.06e+03] (5.06e+03,7.56e+03]
##
## (65,2.56e+03]
                                 1496
                                                         0
                                                       104
                                                                              0
## (2.56e+03,5.06e+03]
                                    0
## (5.06e+03,7.56e+03]
                                    0
                                                         0
                                                                             48
## (7.56e+03,1.01e+04]
                                    0
                                                         0
                                                                              0
## (1.01e+04,1.21e+04]
                                                         0
                                                                              0
                                    0
                                                         0
## (1.21e+04,1.51e+04]
                                    0
                                                                              1
                                                         0
## (1.51e+04,1.71e+04]
                                    0
                                                                              0
                                                                              0
## (1.71e+04,2.01e+04]
                                    0
                        (7.56e+03,1.01e+04] (1.01e+04,1.21e+04]
## (65,2.56e+03]
                                           0
## (2.56e+03,5.06e+03]
                                          0
                                                                0
## (5.06e+03,7.56e+03]
                                                                0
                                           1
## (7.56e+03,1.01e+04]
                                         77
                                                                0
## (1.01e+04,1.21e+04]
                                                               37
## (1.21e+04,1.51e+04]
                                          0
                                                                0
## (1.51e+04,1.71e+04]
                                          0
                                                                0
## (1.71e+04,2.01e+04]
                                                                0
                                          0
##
                        (1.21e+04,1.51e+04] (1.51e+04,1.71e+04]
## (65,2.56e+03]
                                           0
                                                                0
## (2.56e+03,5.06e+03]
                                           0
                                                                0
                                                                0
## (5.06e+03,7.56e+03]
                                           0
## (7.56e+03,1.01e+04]
                                                                0
                                           0
                                                                0
## (1.01e+04,1.21e+04]
                                          0
## (1.21e+04,1.51e+04]
                                                                2
                                          16
## (1.51e+04,1.71e+04]
                                          2
                                                               11
                                          0
## (1.71e+04,2.01e+04]
                                                                0
##
                        (1.71e+04,2.01e+04] class.error
## (65,2.56e+03]
                                          0.00000000
## (2.56e+03,5.06e+03]
                                          0 0.0000000
## (5.06e+03,7.56e+03]
                                          0 0.02040816
## (7.56e+03,1.01e+04]
                                          0 0.0000000
## (1.01e+04,1.21e+04]
                                          0 0.05128205
## (1.21e+04,1.51e+04]
                                          0 0.15789474
                                          0 0.15384615
## (1.51e+04,1.71e+04]
## (1.71e+04,2.01e+04]
                                          9 0.00000000
varImpPlot(rf_fit)
```

#### rf fit



#### Due to the igraph package this code could not be run either.

D2 = 1-rf\_fit\$proximity # use 1 - proximity

dmap2 = diffuse(D2,eps.val=40, t=.01, neigen=2) #original dmap1 = diffuse(D1,eps.val=.1, t=1, neigen=2) head(dmap2)

cluster2 = hclust(dist(dmap2\$X[,1:2])) plot(cluster2); abline(h=2.0, col='red',lwd=3)

 $\operatorname{plot}(\operatorname{dmap}2X[,1],\operatorname{dmap}2X[,2],\operatorname{col=outcome},\operatorname{pch=paste}(\operatorname{outcome}), \ \operatorname{xlab="Diffusion Map Coordinate 1"}, \ \operatorname{ylab="Diffusion Map Coordinate 2"})$ 

dmap = diffuse(D3,eps.val=400, t=1, neigen=2) plot(dmap3X[,1], dmap3X[,2],col=outcome,pch=paste(outcome), xlab="Diffusion Map Coordinate 1", ylab="Diffusion Map Coordinate 2", main = "BTC Random Forest Prediction") ## using RF method we generate plot similar t

#### The actual TDA plot. Due to rstudio difficulties it could not be seen either

TDA\_plot <- gvisBubbleChart(rf\_fit, idvar="cluster", xvar="x", yvar="y", colorvar="count", size-var="count", options=list( title='BTC Clustered Data - TDA Exploration', hAxis='{minValue:-5, maxValue:6}', vAxis='{minValue:-2, maxValue:7}')) plot(TDA\_plot)