TDA Analysis

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Intro: I began the semester with a lingering feeling of immersing myself into something intellectually stimulating. I stumbled across topology in my Real Analysis course fall of 2017. I generally enjoyed working on it and noticed the beautiful generalized, objective theory behind it. Since my field is data science and analytics, I figured it would be appropriate to combine two fields which I am genuinely interested in and go from through. Thus, I stumbled upon topological data analysis.

I reached out to several profession sources and eventually stumbled upon Dmitriy Mozorov at the Berkeley Institute of Data Science. He advised me in this research and was the source in my concrete understanding of the subject. To demonstrate my new found abilities in topological data analysis, I choose to apply my understanding to a project.

Abstract: I used a random forest to classify prices of Bitcoin data. The findings of the classified values were then put on a topological data analytic plot.

Topological Data Analysis

Problem: How well can TDA be used on cyrptocurrency data?

Testing on Binance API Data

Description: We provide daily cryptocurrency data (transaction count, on-chain transaction volume, value of created coins, price, market cap, and exchange volume) in CSV format. The data sample stretches back to December 2013. We explain the column titles and some shortcomings here.

Source: https://coinmetrics.io/data-downloads/ V1 date: Date on georgian calender.

V2 txVolume(USD): "on-chain transaction volume." Essentially a broad and largely unadjusted measure of the total value of outputs on the blockchain, on a given day.

V3 txCount: Number of transactions happening on the public blockchain a day. The is a broad estimation. More can be explained in the source as to why that is.

V4 marketcap(USD): The unit price multiplied by the number of units in circulation.

V5 Price: Open price, received from CoinMarketCap.

V6 exchangevolume(USD): The dollar value of the volume at exchanges. Also received from CoinMarketCap.

V7 generatedCoins: The number of new coins that have been brought into existence on that day

V8 Fees: Fees. One important peice of information is that the fees in this data are based on the native currency, not USD.

references used: -Gunnar Carlsson's "Topology and Data" https://web.stanford.edu/group/mmds/slides2008/carlsson.pdf

-Topological Methods for the Analysis of High Dimensional Data Sets and 3D Object Recognition: Gurjeet Singh, Facundo Mémoli and Gunnar Carlsson https://research.math.osu.edu/tgda/mapperPBG.pdf

Packages needed for the analysis

```
#library(diffusionMap), PROBLEM WITH "igraph" PACKAGE CANNOT LOAD
library(randomForest)
library(ggplot2)
library(reshape)
library(reshape2)
library(plyr)
#library(phom)
library(dplyr)
library(lubridate)
```

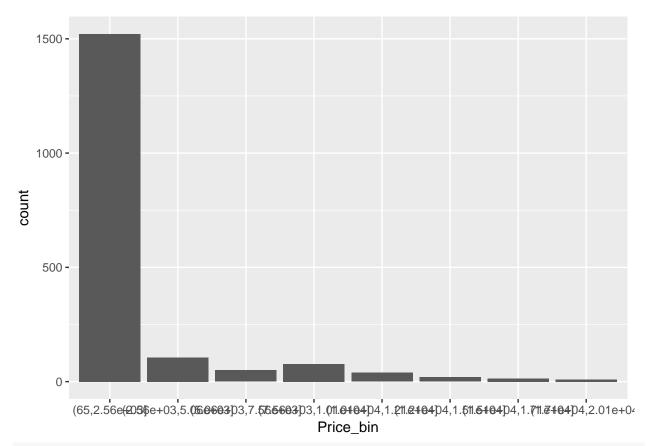
(1) Cleaning the data. As usual in analytics projects, data wrangling was necessary. The variables were put into strings in the original dataset so they had to be converted into variables in order to do any sort of analysis.

```
setwd("~/Documents/TDA/")
btc = read.csv("btc.csv", header = F)
btc = btc[-1,]
btc <- btc[1:8]
btc$V2 <- as.numeric(as.character(btc$V2))</pre>
btc$V3 <- as.numeric(as.character(btc$V3))</pre>
btc$V4 <- as.numeric(as.character(btc$V4))</pre>
btc$V5 <- as.numeric(as.character(btc$V5))</pre>
btc$V6 <- as.numeric(as.character(btc$V6))</pre>
btc$V7 <- as.numeric(as.character(btc$V7))</pre>
btc$V8 <- as.numeric(as.character(btc$V8))</pre>
breaks <- c(65, 2565, 5065, 7565, 10065, 12065, 15065, 17065, 20065)
btc <- btc %>%
  mutate(Price_bin = cut(V5, breaks)) #categorize the price of the coin into 12 bins.
head(btc) # see header to decode V1-V8;
             V1
                        ۷2
                              ٧3
                                         ۷4
                                                 V5 V6
                                                         ۷7
                                                                   ٧8
## 1 2013-05-01 108659660 52443 1542820000 139.00
                                                    0 3575 36.80600
## 2 2013-05-02 96958519 55169 1292190000 116.38
                                                    0 3425 54.40792
## 3 2013-05-03 84459697 55636 1180070000 106.25
                                                    0 3650 48.52677
## 4 2013-05-04 41545845 48595 1089890000 98.10 0 3900 43.41969
## 5 2013-05-05 56205930 49907 1254760000 112.90
                                                    0 3875 38.40896
## 6 2013-05-06 78921301 52523 1289470000 115.98 0 4250 51.88924
         Price bin
## 1 (65,2.56e+03]
## 2 (65,2.56e+03]
## 3 (65,2.56e+03]
## 4 (65,2.56e+03]
```

```
## 5 (65,2.56e+03]
## 6 (65,2.56e+03]
```

summary(btc)

```
V1
                           ٧2
                                               VЗ
##
   2013-05-01:
                 1
                     Min.
                           :3.379e+07
                                         Min. : 29566
##
   2013-05-02:
                 1
                     1st Qu.:2.362e+08
                                         1st Qu.: 71728
## 2013-05-03:
                     Median :6.326e+08
                                         Median :154048
## 2013-05-04:
                     Mean :2.580e+09
                                         Mean
                                               :162430
                 1
                     3rd Qu.:1.756e+09
##
   2013-05-05:
                                         3rd Qu.:234748
##
   2013-05-06:
                 1
                     Max. :4.835e+10
                                         Max.
                                                :490459
##
   (Other)
             :1828
##
         ۷4
                             ۷5
                                               V6
                                                                   ۷7
          :7.793e+08
                                                :0.000e+00
                                                                    :1000
##
   Min.
                       Min.
                                  68.5
                                         Min.
                                                             Min.
##
  1st Qu.:4.030e+09
                       1st Qu.: 282.5
                                         1st Qu.:1.713e+07
                                                             1st Qu.:2000
  Median :7.113e+09
                       Median : 530.1
                                         Median :4.720e+07
                                                             Median:3575
## Mean
         :2.915e+10
                       Mean : 1791.2
                                         Mean
                                               :1.103e+09
                                                             Mean
                                                                    :3230
##
   3rd Qu.:1.605e+10
                       3rd Qu.: 1013.5
                                         3rd Qu.:2.010e+08
                                                             3rd Qu.:4050
##
  Max.
         :3.261e+11
                              :19475.8
                                                :2.384e+10
                                                                    :6450
                       Max.
                                         Max.
                                                             Max.
##
##
         ٧8
                                    Price_bin
##
   Min.
          :
              7.856
                       (65,2.56e+03]
                                         :1521
   1st Qu.:
             15.406
                      (2.56e+03,5.06e+03]: 105
                      (7.56e+03,1.01e+04]: 77
  Median : 35.250
  Mean
         : 89.874
                      (5.06e+03,7.56e+03]: 50
##
   3rd Qu.: 84.965
##
                      (1.01e+04,1.21e+04]: 39
##
   Max. :1495.947
                      (1.21e+04,1.51e+04]: 19
##
                      (Other)
                                         : 23
ggplot(btc) + aes(x = Price_bin) + geom_bar() #examine how the bins are distributed
```



head(btc) # see header to decode V1-V8;

```
۷1
                      ٧2
                            VЗ
                                        ۷4
                                               V5 V6
## 1 2013-05-01 108659660 52443 1542820000 139.00
                                                  0 3575 36.80600
## 2 2013-05-02 96958519 55169 1292190000 116.38
                                                  0 3425 54.40792
## 3 2013-05-03 84459697 55636 1180070000 106.25 0 3650 48.52677
## 4 2013-05-04 41545845 48595 1089890000 98.10 0 3900 43.41969
## 5 2013-05-05 56205930 49907 1254760000 112.90 0 3875 38.40896
## 6 2013-05-06 78921301 52523 1289470000 115.98 0 4250 51.88924
        Price_bin
## 1 (65,2.56e+03]
## 2 (65,2.56e+03]
## 3 (65,2.56e+03]
## 4 (65,2.56e+03]
## 5 (65,2.56e+03]
## 6 (65,2.56e+03]
```

summary(btc) #what we're starting with

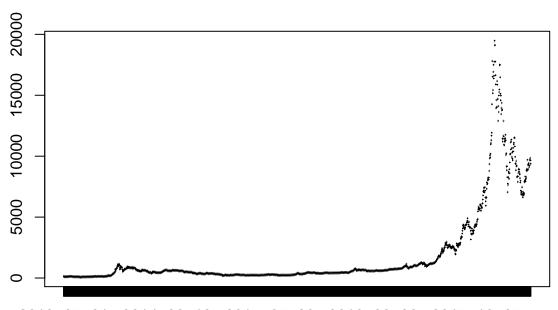
```
##
             ۷1
                            V2
                                                VЗ
   2013-05-01:
                           :3.379e+07
                                          Min. : 29566
##
                      Min.
   2013-05-02:
                      1st Qu.:2.362e+08
##
                 1
                                          1st Qu.: 71728
   2013-05-03:
                      Median :6.326e+08
                                          Median :154048
   2013-05-04:
                      Mean
                           :2.580e+09
                                          Mean
                                                 :162430
                 1
                      3rd Qu.:1.756e+09
                                          3rd Qu.:234748
##
   2013-05-05:
##
   2013-05-06:
                 1
                      Max. :4.835e+10
                                                 :490459
                                          Max.
##
   (Other)
              :1828
##
          ۷4
                              ۷5
                                                ۷6
                                                                    ۷7
```

```
Min.
           :7.793e+08
                        Min. :
                                 68.5
                                          Min.
                                                 :0.000e+00
                                                              Min.
                                                                      :1000
##
   1st Qu.:4.030e+09
                        1st Qu.: 282.5
                                          1st Qu.:1.713e+07
                                                              1st Qu.:2000
   Median :7.113e+09
                                                              Median:3575
                        Median : 530.1
                                          Median :4.720e+07
           :2.915e+10
                              : 1791.2
                                                 :1.103e+09
                                                                      :3230
##
   Mean
                        Mean
                                          Mean
                                                              Mean
##
   3rd Qu.:1.605e+10
                        3rd Qu.: 1013.5
                                          3rd Qu.:2.010e+08
                                                               3rd Qu.:4050
   Max.
          :3.261e+11
                               :19475.8
                                          Max.
                                                 :2.384e+10
                                                              Max.
                                                                      :6450
##
                        Max.
##
##
          V8
                                     Price_bin
##
   Min.
               7.856
                       (65,2.56e+03]
                                          :1521
              15.406
                       (2.56e+03,5.06e+03]: 105
##
   1st Qu.:
   Median :
              35.250
                       (7.56e+03,1.01e+04]: 77
##
   Mean
             89.874
                       (5.06e+03,7.56e+03]:
   3rd Qu.: 84.965
                       (1.01e+04,1.21e+04]: 39
##
##
          :1495.947
                       (1.21e+04,1.51e+04]: 19
   Max.
##
                       (Other)
                                             23
```

EDA

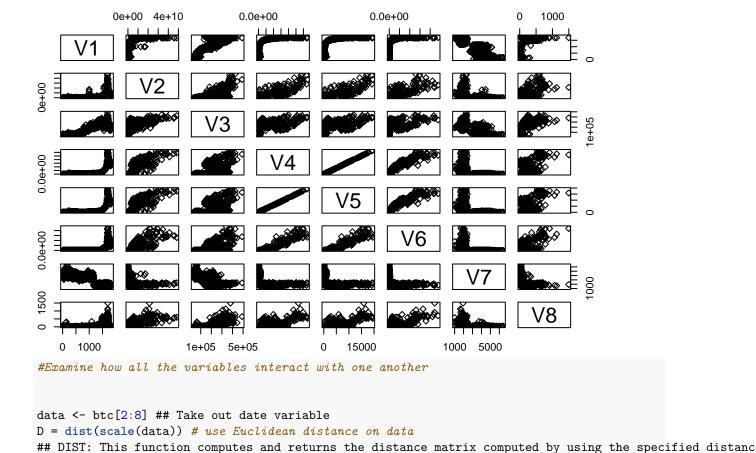
```
plot(x = btc$V1, y = btc$V5, main = "Price of bitcoin since 2013")
```

Price of bitcoin since 2013



2013-05-01 2014-06-10 2015-07-20 2016-08-28 2017-10-07

bitcoin data set



DIFFUSE: Description: Uses the pair-wise distance matrix for a data set to compute the diffusion map coefficients. Computes the Markov transition probability matrix, and its eigenvalues and left & right eigenvectors. Returns a 'dmap' object.

The following code cannot be run due to technical difficulties with the igraph package. However rather than putting it into a code chance I figured it'd be good to leave it here and work on it once Rstudio fixes the bugs in this package and updates it.

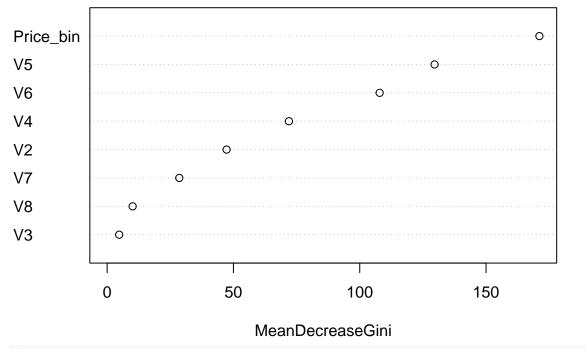
dmap = diffuse(D, eps.val=10, t=1, neigen=2) ## just run with the standard default settings plot(dmapX[,1], dmapX[,2], col=outcome,pch=paste(outcome), xlab="Diffusion Map Coordinate 1", ylab="Diffusion Map Coordinate 2", main="Diffusion Map of Bitcoin data")

2) Random Forest classifer to define distances.

```
bins = btc$Price_bin
data = btc[2:9]
rf_fit = randomForest(data, bins, ntree=10, proximity=TRUE)
print(rf_fit)
```

```
##
## Call:
##
    randomForest(x = data, y = bins, ntree = 10, proximity = TRUE)
                  Type of random forest: classification
##
##
                         Number of trees: 10
## No. of variables tried at each split: 2
##
           OOB estimate of error rate: 0.28%
## Confusion matrix:
                        (65,2.56e+03] (2.56e+03,5.06e+03] (5.06e+03,7.56e+03]
##
## (65,2.56e+03]
                                 1507
                                                       105
                                                                              0
## (2.56e+03,5.06e+03]
                                    0
## (5.06e+03,7.56e+03]
                                    0
                                                         0
                                                                             48
## (7.56e+03,1.01e+04]
                                                         0
                                    0
                                                                              0
## (1.01e+04,1.21e+04]
                                    0
                                                         0
                                                                              0
## (1.21e+04,1.51e+04]
                                    0
                                                         0
                                                                              0
## (1.51e+04,1.71e+04]
                                    0
                                                         0
                                                                              0
## (1.71e+04,2.01e+04]
                                    0
                                                                              0
##
                        (7.56e+03,1.01e+04] (1.01e+04,1.21e+04]
## (65,2.56e+03]
                                           0
## (2.56e+03,5.06e+03]
                                           0
                                                                0
## (5.06e+03,7.56e+03]
                                           1
                                                                0
## (7.56e+03,1.01e+04]
                                          77
                                                               0
## (1.01e+04,1.21e+04]
                                                               37
                                           0
                                                                2
## (1.21e+04,1.51e+04]
                                           0
## (1.51e+04,1.71e+04]
                                           0
                                                                0
## (1.71e+04,2.01e+04]
                                           0
                                                                0
                        (1.21e+04,1.51e+04] (1.51e+04,1.71e+04]
## (65,2.56e+03]
                                                                0
                                           0
                                                                0
## (2.56e+03,5.06e+03]
                                           0
## (5.06e+03,7.56e+03]
                                           0
                                                                0
## (7.56e+03,1.01e+04]
                                           0
                                                                0
                                                                0
## (1.01e+04,1.21e+04]
                                           1
## (1.21e+04,1.51e+04]
                                                                0
                                          16
## (1.51e+04,1.71e+04]
                                           0
                                                               14
## (1.71e+04,2.01e+04]
                                           0
                                                                0
##
                        (1.71e+04,2.01e+04] class.error
## (65,2.56e+03]
                                           0 0.0000000
## (2.56e+03,5.06e+03]
                                           0 0.0000000
## (5.06e+03,7.56e+03]
                                          0 0.02040816
## (7.56e+03,1.01e+04]
                                          0 0.0000000
## (1.01e+04,1.21e+04]
                                          0 0.02631579
## (1.21e+04,1.51e+04]
                                          1 0.15789474
## (1.51e+04,1.71e+04]
                                          0 0.00000000
## (1.71e+04,2.01e+04]
                                          9 0.00000000
varImpPlot(rf_fit)
```

rf fit



#version

D2 = 1-rf_fit\$proximity # use 1 - proximity

Due to the igraph package this code could not be run either.

 $dmap2 = diffuse(D2,eps.val=40,\ t=.01,\ neigen=2)\ \#original\ dmap1 = diffuse(D1,eps.val=.1,\ t=1,\ neigen=2)\ head(dmap2)$

cluster2 = hclust(dist(dmap2\$X[,1:2])) plot(cluster2); abline(h=2.0, col='red',lwd=3)

 $\operatorname{plot}(\operatorname{dmap}2X[,1],\operatorname{dmap}2X[,2],\operatorname{col=outcome},\operatorname{pch=paste}(\operatorname{outcome}), \ \operatorname{xlab="Diffusion Map Coordinate 1"}, \ \operatorname{ylab="Diffusion Map Coordinate 2"})$

dmap = diffuse(D3,eps.val=400, t=1, neigen=2) plot(dmap3X[,1], dmap3X[,2],col=outcome,pch=paste(outcome), xlab="Diffusion Map Coordinate 1", ylab="Diffusion Map Coordinate 2", main = "BTC Random Forest Prediction") ## using RF method we generate plot similar t

The actual TDA plot. Due to rstudio difficulties it could not be seen either

TDA_plot <- gvisBubbleChart(rf_fit, idvar="cluster", xvar="x", yvar="y", colorvar="count", size-var="count", options=list(title='BTC Clustered Data - TDA Exploration', hAxis='{minValue:-5, maxValue:6}', vAxis='{minValue:-2, maxValue:7}')) plot(TDA_plot)