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# Natural Language Processing

2

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# 322 Notation

323 As a general rule, words, word counts, and other types of observations are indicated with  
324 Roman letters ( $a, b, c$ ); parameters are indicated with Greek letters ( $\alpha, \beta, \theta$ ). Vectors are  
325 indicated with bold script for both random variables  $\mathbf{x}$  and parameters  $\boldsymbol{\theta}$ . Other useful  
326 notations are indicated in the table below.

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## Basics

---

$\exp x$	the base-2 exponent, $2^x$
$\log x$	the base-2 logarithm, $\log_2 x$
$\{x_n\}_{n=1}^N$	the set $\{x_1, x_2, \dots, x_N\}$
$x_i^j$	$x_i$ raised to the power $j$
$x_i^{(j)}$	indexing by both $i$ and $j$

---

## Linear algebra

---

$\mathbf{x}^{(i)}$	a column vector of feature counts for instance $i$ , often word counts
$\mathbf{x}_{j:k}$	elements $j$ through $k$ (inclusive) of a vector $\mathbf{x}$
$[\mathbf{x}; \mathbf{y}]$	vertical concatenation of two column vectors
$[\mathbf{x}, \mathbf{y}]$	horizontal concatenation of two column vectors
$\mathbf{e}_n$	a “one-hot” vector with a value of 1 at position $n$ , and zero everywhere else
$\boldsymbol{\theta}^\top$	the transpose of a column vector $\boldsymbol{\theta}$
$\boldsymbol{\theta} \cdot \mathbf{x}^{(i)}$	the dot product $\sum_{j=1}^N \theta_j \times x_j^{(i)}$
$\mathbf{X}$	a matrix
$x_{i,j}$	row $i$ , column $j$ of matrix $\mathbf{X}$
$\text{Diag}(\mathbf{x})$	a matrix with $\mathbf{x}$ on the diagonal, e.g., $\begin{pmatrix} x_1 & 0 & 0 \\ 0 & x_2 & 0 \\ 0 & 0 & x_3 \end{pmatrix}$
$\mathbf{X}^{-1}$	the inverse of matrix $\mathbf{X}$

---

**Text datasets**

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$w_m$	word token at position $m$
$N$	number of training instances
$M$	length of a sequence (of words or tags)
$V$	number of words in vocabulary
$y^{(i)}$	the true label for instance $i$
$\hat{y}$	a predicted label
$\mathcal{Y}$	the set of all possible labels
$K$	number of possible labels $K =  \mathcal{Y} $
$\square$	the start token
$\blacksquare$	the stop token
$\mathbf{y}^{(i)}$	a structured label for instance $i$ , such as a tag sequence
$\mathcal{Y}(\mathbf{w})$	the set of possible labelings for the word sequence $\mathbf{w}$
$\diamond$	the start tag
$\blacklozenge$	the stop tag

---

**Probabilities**

---

$\Pr(A)$	probability of event $A$
$\Pr(A   B)$	probability of event $A$ , conditioned on event $B$
$p_B(b)$	the marginal probability of random variable $B$ taking value $b$ ; written $p(b)$ when the choice of random variable is clear from context
$p_{B A}(b   a)$	the probability of random variable $B$ taking value $b$ , conditioned on $A$ taking value $a$ ; written $p(b   a)$ when clear from context
$A \sim p$	the random variable $A$ is distributed according to distribution $p$ . For example, $X \sim \mathcal{N}(0, 1)$ states that the random variable $X$ is drawn from a normal distribution with zero mean and unit variance.
$A   B \sim p$	conditioned on the random variable $B$ , $A$ is distributed according to $p$ . <sup>1</sup>

---

**Machine learning**

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$\Psi(\mathbf{x}^{(i)}, y)$	the score for assigning label $y$ to instance $i$
$\mathbf{f}(\mathbf{x}^{(i)}, y)$	the feature vector for instance $i$ with label $y$
$\theta$	a (column) vector of weights
$\ell^{(i)}$	loss on an individual instance $i$
$L$	objective function for an entire dataset
$\mathcal{L}$	log-likelihood of a dataset
$\lambda$	the amount of regularization

327 **Chapter 1**

328 **Introduction**

329 Natural language processing is the set of methods for making human language accessible  
330 to computers. In the past decade, natural language processing has become embedded  
331 in our daily lives: automatic machine translation is ubiquitous on the web and in social  
332 media; text classification keeps emails from collapsing under a deluge of spam; search  
333 engines have moved beyond string matching and network analysis to a high degree of  
334 linguistic sophistication; dialog systems provide an increasingly common and effective  
335 way to get and share information.

336 These diverse applications are based on a common set of ideas, drawing on algo-  
337 rithms, linguistics, logic, statistics, and more. The goal of this text is to provide a survey  
338 of these foundations. The technical fun starts in the next chapter; the rest of this current  
339 chapter situates natural language processing with respect to other intellectual disciplines,  
340 identifies some high-level themes in contemporary natural language processing, and ad-  
341 vises the reader on how best to approach the subject.

342 **1.1 Natural language processing and its neighbors**

343 One of the great pleasures of working in this field is the opportunity to draw on many  
344 other intellectual traditions, from formal linguistics to statistical physics. This section  
345 briefly situates natural language processing with respect to some of its closest neighbors.

346 **Computational Linguistics** Most of the meetings and journals that host natural lan-  
347 guage processing research bear the name “computational linguistics”, and the terms may  
348 be thought of as essentially synonymous. But while there is substantial overlap, there is  
349 an important difference in focus. In linguistics, language is the object of study. Compu-  
350 tational methods may be brought to bear, just as in scientific disciplines like computational  
351 biology and computational astronomy, but they play only a supporting role. In contrast,

352 natural language processing is focused on the design and analysis of computational al-  
 353 gorithms and representations for processing natural human language. The goal of natu-  
 354 ral language processing is to provide new computational capabilities around human lan-  
 355 guage: for example, extracting information from texts, translating between languages, an-  
 356 swering questions, holding a conversation, taking instructions, and so on. Fundamental  
 357 linguistic insights may be crucial for accomplishing these tasks, but success is ultimately  
 358 measured by whether and how well the job gets done.

359 **Machine Learning** Contemporary approaches to natural language processing rely heav-  
 360 ily on machine learning, which makes it possible to build complex computer programs  
 361 from examples. Machine learning provides an array of general techniques for tasks like  
 362 converting a sequence of discrete tokens in one vocabulary to a sequence of discrete to-  
 363 kens in another vocabulary — a generalization of what normal people might call “transla-  
 364 tion.” Much of today’s natural language processing research can be thought of as applied  
 365 machine learning. However, natural language processing has characteristics that distin-  
 366 guish it from many of machine learning’s other application domains.

- 367     • Unlike images or audio, text data is fundamentally discrete, with meaning created  
   368       by combinatorial arrangements of symbolic units. This is particularly consequential  
   369       for applications in which text is the output, such as translation and summarization,  
   370       because it is not possible to gradually approach an optimal solution.
- 371     • Although the set of words is discrete, new words are always being created. Further-  
   372       more, the distribution over words (and other linguistic elements) resembles that of a  
   373       **power law** (Zipf, 1949): there will be a few words that are very frequent, and a long  
   374       tail of words that are rare. A consequence is that natural language processing algo-  
   375       rithms must be especially robust to observations that do not occur in the training  
   376       data.
- 377     • Language is **recursive**: units such as words can combine to create phrases, which  
   378       can combine by the very same principles to create larger phrases. For example, a  
   379       **noun phrase** can be created by combining a smaller noun phrase with a **preposi-**  
   380       **tional phrase**, as in *the whiteness of the whale*. The prepositional phrase is created by  
   381       combining a preposition (in this case, *of*) with another noun phrase (*the whale*). In  
   382       this way, it is possible to create arbitrarily long phrases, such as,

383           (1.1) ...huge globular pieces of the whale of the bigness of a human head.<sup>1</sup>

384     The meaning of such a phrase must be analyzed in accord with the underlying hier-  
 385       archical structure. In this case, *huge globular pieces of the whale* acts as a single noun  
 386       phrase, which is conjoined with the prepositional phrase of *the bigness of a human*

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<sup>1</sup>Throughout the text, this notation will be used to introduce linguistic examples.

387        *head*. The interpretation would be different if instead, *huge globular pieces* were con-  
388        joined with the prepositional phrase *of the whale of the bigness of a human head* —  
389        implying a disappointingly small whale. Even though text appears as a sequence,  
390        machine learning methods must account for its implicit recursive structure.

391 **Artificial Intelligence** The goal of artificial intelligence is to build software and robots  
392 with the same range of abilities as humans (Russell and Norvig, 2009). Natural language  
393 processing is relevant to this goal in several ways. The capacity for language is one of the  
394 central features of human intelligence, and no artificial intelligence program could be said  
395 to be complete without the ability to communicate in words.<sup>2</sup>

396        Much of artificial intelligence research is dedicated to the development of systems  
397 that can reason from premises to a conclusion, but such algorithms are only as good as  
398 what they know (Dreyfus, 1992). Natural language processing is a potential solution to  
399 the “knowledge bottleneck”, by acquiring knowledge from natural language texts, and  
400 perhaps also from conversations; This idea goes all the way back to Turing’s 1949 pa-  
401 per *Computing Machinery and Intelligence*, which proposed the **Turing test** and helped to  
402 launch the field of artificial intelligence (Turing, 2009).

403        Conversely, reasoning is sometimes essential for basic tasks of language processing,  
404 such as determining who a pronoun refers to. **Winograd schemas** are examples in which  
405 a single word changes the likely referent of a pronoun, in a way that seems to require  
406 knowledge and reasoning to decode (Levesque et al., 2011). For example,

407        (1.2) The trophy doesn’t fit into the brown suitcase because **it** is too [small/large].  
408        When the final word is *small*, then the pronoun *it* refers to the suitcase; when the final  
409 word is *large*, then *it* refers to the trophy. Solving this example requires spatial reasoning;  
410 other schemas require reasoning about actions and their effects, emotions and intentions,  
411 and social conventions.

412        The Winograd schemas demonstrate that natural language understanding cannot be  
413 achieved in isolation from knowledge and reasoning. Yet the history of artificial intelli-  
414 gence has been one of increasing specialization: with the growing volume of research in  
415 subdisciplines such as natural language processing, machine learning, and computer vi-

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<sup>2</sup>This view is shared by some, but not all, prominent researchers in artificial intelligence. Michael Jordan, a specialist in machine learning, has said that if he had a billion dollars to spend on any large research project, he would spend it on natural language processing ([https://www.reddit.com/r/MachineLearning/comments/2fxi6v/ama\\_michael\\_i\\_jordan/](https://www.reddit.com/r/MachineLearning/comments/2fxi6v/ama_michael_i_jordan/)). On the other hand, in a public discussion about the future of artificial intelligence in February 2018, computer vision researcher Yann Lecun argued that despite its many practical applications, language is perhaps “number 300” in the priority list for artificial intelligence research, and that it would be a great achievement if AI could attain the capabilities of an orangutan, which do not include language (<http://www.abigailsee.com/2018/02/21/deep-learning-structure-and-innate-priors.html>).

416 sion, it is difficult for anyone to maintain expertise across the entire field. Still, recent work  
417 has demonstrated interesting connections between natural language processing and other  
418 areas of AI, including computer vision (e.g., Antol et al., 2015) and game playing (e.g.,  
419 Branavan et al., 2009). The dominance of machine learning throughout artificial intel-  
420 ligence has led to a broad consensus on representations such as graphical models and  
421 knowledge graphs, and on algorithms such as backpropagation and combinatorial opti-  
422 mization. Many of the algorithms and representations covered in this text are part of this  
423 consensus.

424 **Computer Science** The discrete and recursive nature of natural language invites the ap-  
425 plication of theoretical ideas from computer science. Linguists such as Chomsky and  
426 Montague have shown how formal language theory can help to explain the syntax and  
427 semantics of natural language. Theoretical models such as finite-state and pushdown au-  
428 tomata are the basis for many practical natural language processing systems. Algorithms  
429 for searching the combinatorial space of analyses of natural language utterances can be  
430 analyzed in terms of their computational complexity, and theoretically motivated approx-  
431 imations can sometimes be applied.

432 The study of computer systems is also relevant to natural language processing. Large  
433 datasets of unlabeled text are a natural application for parallelization techniques like  
434 MapReduce (Dean and Ghemawat, 2008; Lin and Dyer, 2010); high-volume data sources  
435 such as social media are a natural application for approximate streaming and sketching  
436 techniques (Goyal et al., 2009). When deep neural networks are implemented in pro-  
437 duction systems, it is possible to eke out speed gains using techniques such as reduced-  
438 precision arithmetic (Wu et al., 2016). Many classical natural language processing algo-  
439 rithms are not naturally suited to graphics processing unit (GPU) parallelization, suggest-  
440 ing directions for further research at the intersection of natural language processing and  
441 computing hardware (Yi et al., 2011).

442 **Speech Processing** Natural language is often communicated in spoken form, and speech  
443 recognition is the task of converting an audio signal to text. From one perspective, this is  
444 a signal processing problem, which might be viewed as a preprocessing step before nat-  
445 ural language processing can be applied. However, context plays a critical role in speech  
446 recognition by human listeners: knowledge of the surrounding words influences percep-  
447 tion and helps to correct for noise (Miller et al., 1951). For this reason, speech recognition  
448 is often integrated with text analysis, particularly with statistical **language models**, which  
449 quantify the probability of a sequence of text (see chapter 6). Beyond speech recognition,  
450 the broader field of speech processing includes the study of speech-based dialogue sys-  
451 tems, which are briefly discussed in chapter 19. Historically, speech processing has often  
452 been pursued in electrical engineering departments, while natural language processing

453 has been the purview of computer scientists. For this reason, the extent of interaction  
454 between these two disciplines is less than it might otherwise be.

455 **Others** Natural language processing plays a significant role in emerging interdisciplinary  
456 fields like **computational social science** and the **digital humanities**. Text classification  
457 (chapter 4), clustering (chapter 5), and information extraction (chapter 17) are particularly  
458 useful tools; another is probabilistic **topic models** (Blei, 2012), which are not covered in  
459 this text. **Information retrieval** (Manning et al., 2008) makes use of similar tools, and  
460 conversely, techniques such as latent semantic analysis (§ 14.3) have roots in information  
461 retrieval. **Text mining** is sometimes used to refer to the application of data mining tech-  
462 niques, especially classification and clustering, to text. While there is no clear distinction  
463 between text mining and natural language processing (nor between data mining and ma-  
464 chine learning), text mining is typically less concerned with linguistic structure, and more  
465 interested in fast, scalable algorithms.

## 466 1.2 Three themes in natural language processing

467 Natural language processing covers a diverse range of tasks, methods, and linguistic phe-  
468 nomena. But despite the apparent incommensurability between, say, the summarization  
469 of scientific articles (§ 16.3.4.1) and the identification of suffix patterns in Spanish verbs  
470 (§ 9.1.4.3), some general themes emerge. Each of these themes can be expressed as an  
471 opposition between two extreme viewpoints on how to process natural language, and in  
472 each case, existing approaches can be placed on a continuum between these two extremes.

### 473 1.2.1 Learning and knowledge

474 A recurring topic of debate is the relative importance of machine learning and linguistic  
475 knowledge. On one extreme, advocates of “natural language processing from scratch” (Col-  
476 lobert et al., 2011) propose to use machine learning to train end-to-end systems that trans-  
477 mute raw text into any desired output structure: e.g., a summary, database, or transla-  
478 tion. On the other extreme, the core work of natural language processing is sometimes  
479 taken to be transforming text into a stack of general-purpose linguistic structures: from  
480 subword units called **morphemes**, to word-level **parts-of-speech**, to tree-structured repre-  
481 sentations of grammar, and beyond, to logic-based representations of meaning. In theory,  
482 these general-purpose structures should then be able to support any desired application.

483 The end-to-end learning approach has been buoyed by recent results in computer vi-  
484 sion and speech recognition, in which advances in machine learning have swept away  
485 expert-engineered representations based on the fundamentals of optics and phonology (Krizhevsky  
486 et al., 2012; Graves and Jaitly, 2014). But while some amount of machine learning is an el-  
487 ement of nearly every contemporary approach to natural language processing, linguistic

488 representations such as syntax trees have not yet gone the way of the visual edge detector  
 489 or the auditory triphone. Linguists have argued for the existence of a “language faculty”  
 490 in all human beings, which encodes a set of abstractions specially designed to facilitate  
 491 the understanding and production of language. The argument for the existence of such  
 492 a language faculty is based on the observation that children learn language faster and  
 493 from fewer examples than would be reasonably possible, if language was learned from  
 494 experience alone.<sup>3</sup> Regardless of the cognitive validity of these arguments, it seems that  
 495 linguistic structures are particularly important in scenarios where training data is limited.

496 Moving away from the extreme ends of the continuum, there are a number of ways in  
 497 which knowledge and learning can be combined in natural language processing. Many  
 498 supervised learning systems make use of carefully engineered **features**, which transform  
 499 the data into a representation that can facilitate learning. For example, in a task like doc-  
 500 ument classification, it may be useful to identify each word’s **stem**, so that a learning  
 501 system can more easily generalize across related terms such as *whale*, *whales*, *whalers*, and  
 502 *whaling*. This is particularly important in the many languages that exceed English in the  
 503 complexity of the system of affixes that can attach to words. Such features could be ob-  
 504 tained from a hand-crafted resource, like a dictionary that maps each word to a single  
 505 root form. Alternatively, features can be obtained from the output of a general-purpose  
 506 language processing system, such as a parser or part-of-speech tagger, which may itself  
 507 be built on supervised machine learning.

508 Another synthesis of learning and knowledge is in model structure: building machine  
 509 learning models whose architectures are inspired by linguistic theories. For example, the  
 510 organization of sentences is often described as **compositional**, with meaning of larger  
 511 units gradually constructed from the meaning of their smaller constituents. This idea  
 512 can be built into the architecture of a deep neural network, which is then trained using  
 513 contemporary deep learning techniques (Dyer et al., 2016).

514 The debate about the relative importance of machine learning and linguistic knowl-  
 515 edge sometimes becomes heated. No machine learning specialist likes to be told that their  
 516 engineering methodology is unscientific alchemy;<sup>4</sup> nor does a linguist want to hear that  
 517 the search for general linguistic principles and structures has been made irrelevant by big  
 518 data. Yet there is clearly room for both types of research: we need to know how far we  
 519 can go with end-to-end learning alone, while at the same time, we continue the search for  
 520 linguistic representations that generalize across applications, scenarios, and languages.  
 521 For more on the history of this debate, see Church (2011); for an optimistic view of the  
 522 potential symbiosis between computational linguistics and deep learning, see Manning

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<sup>3</sup>The *Language Instinct* (Pinker, 2003) articulates these arguments in an engaging and popular style. For arguments against the innateness of language, see Elman et al. (1998).

<sup>4</sup>Ali Rahimi argued that much of deep learning research was similar to “alchemy” in a presentation at the 2017 conference on Neural Information Processing Systems. He was advocating for more learning theory, not more linguistics.

523 (2015).

524 **1.2.2 Search and learning**

525 Many natural language processing problems can be written mathematically in the form  
 526 of optimization,<sup>5</sup>

$$\hat{\mathbf{y}} = \operatorname{argmax}_{\mathbf{y} \in \mathcal{Y}(\mathbf{x})} \Psi(\mathbf{x}, \mathbf{y}; \boldsymbol{\theta}), \quad [1.1]$$

527 where,

- 528 •  $\mathbf{x}$  is the input, which is an element of a set  $\mathcal{X}$ ;
- 529 •  $\mathbf{y}$  is the output, which is an element of a set  $\mathcal{Y}(\mathbf{x})$ ;
- 530 •  $\Psi$  is a scoring function (also called the **model**), which maps from the set  $\mathcal{X} \times \mathcal{Y}$  to  
 531 the real numbers;
- 532 •  $\boldsymbol{\theta}$  is a vector of parameters for  $\Psi$ ;
- 533 •  $\hat{\mathbf{y}}$  is the predicted output, which is chosen to maximize the scoring function.

534 This basic structure can be used across a huge range of problems. For example, the  
 535 input  $\mathbf{x}$  might be a social media post, and the output  $\mathbf{y}$  might be a labeling of the emotional  
 536 sentiment expressed by the author (chapter 4); or  $\mathbf{x}$  could be a sentence in French, and the  
 537 output  $\mathbf{y}$  could be a sentence in Tamil (chapter 18); or  $\mathbf{x}$  might be a sentence in English,  
 538 and  $\mathbf{y}$  might be a representation of the syntactic structure of the sentence (chapter 10); or  
 539  $\mathbf{x}$  might be a news article and  $\mathbf{y}$  might be a structured record of the events that the article  
 540 describes (chapter 17).

541 By adopting this formulation, we make an implicit decision that language processing  
 542 algorithms will have two distinct modules:

543 **Search.** The search module is responsible for computing the argmax of the function  $\Psi$ . In  
 544 other words, it finds the output  $\hat{\mathbf{y}}$  that gets the best score with respect to the input  
 545  $\mathbf{x}$ . This is easy when the search space  $\mathcal{Y}(\mathbf{x})$  is small enough to enumerate, or when  
 546 the scoring function  $\Psi$  has a convenient decomposition into parts. In many cases,  
 547 we will want to work with scoring functions that do not have these properties, moti-  
 548 vating the use of more sophisticated search algorithms. Because the outputs are  
 549 usually discrete in language processing problems, search often relies on the machin-  
 550 ery of **combinatorial optimization**.

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<sup>5</sup>Throughout this text, equations will be numbered by square brackets, and linguistic examples will be numbered by parentheses.

551    **Learning.** The learning module is responsible for finding the parameters  $\theta$ . This is typ-  
 552    ically (but not always) done by processing a large dataset of labeled examples,  
 553     $\{(\mathbf{x}^{(i)}, \mathbf{y}^{(i)})\}_{i=1}^N$ . Like search, learning is also approached through the framework  
 554    of optimization, as we will see in chapter 2. Because the parameters are usually  
 555    continuous, learning algorithms generally rely on **numerical optimization**, search-  
 556    ing over vectors of real numbers for parameters that optimize some function of the  
 557    model and the labeled data. Some basic principles of numerical optimization are  
 558    reviewed in Appendix B.

559    The division of natural language processing into separate modules for search and  
 560    learning makes it possible to reuse generic algorithms across a range of different tasks  
 561    and models. This means that the work of natural language processing can be focused on  
 562    the design of the model  $\Psi$ , while reaping the benefits of decades of progress in search,  
 563    optimization, and learning. Much of this textbook will focus on specific classes of scoring  
 564    functions, and on the algorithms that make it possible to search and learn efficiently with  
 565    them.

566    When a model is capable of making subtle linguistic distinctions, it is said to be *expres-*  
 567    *sive*. Expressiveness is often traded off against the efficiency of search and learning. For  
 568    example, a word-to-word translation model makes search and learning easy, but it is not  
 569    expressive enough to distinguish good translations from bad ones. Unfortunately many  
 570    of the most important problems in natural language processing seem to require expres-  
 571    sive models, in which the complexity of search grows exponentially with the size of the  
 572    input. In these models, exact search is usually impossible. Intractability threatens the neat  
 573    modular decomposition between search and learning: if search requires a set of heuristic  
 574    approximations, then it may be advantageous to learn a model that performs well under  
 575    these specific heuristics. This has motivated some researchers to take a more integrated  
 576    approach to search and learning, as briefly mentioned in chapters 11 and 15.

### 577    1.2.3 Relational, compositional, and distributional perspectives

578    Any element of language — a word, a phrase, a sentence, or even a sound — can be  
 579    described from at least three perspectives. Consider the word *journalist*. A *journalist* is a  
 580    subcategory of a *profession*, and an *anchorwoman* is a subcategory of *journalist*; furthermore,  
 581    a *journalist* performs *journalism*, which is often, but not always, a subcategory of *writing*.  
 582    This relational perspective on meaning is the basis for semantic **ontologies** such as **Word-**  
 583    **Net** (Fellbaum, 2010), which enumerate the relations that hold between words and other  
 584    elementary semantic units. The power of the relational perspective is illustrated by the  
 585    following example:

586    (1.3) Umashanthi interviewed Ana. She works for the college newspaper.

587 Who works for the college newspaper? The word *journalist*, while not stated in the ex-  
588 ample, implicitly links the *interview* to the *newspaper*, making *Umashanthi* the most likely  
589 referent for the pronoun. (A general discussion of how to resolve pronouns is found in  
590 chapter 15.)

591 Yet despite the inferential power of the relational perspective, it is not easy to formalize  
592 computationally. Exactly which elements are to be related? Are *journalists* and *reporters*  
593 distinct, or should we group them into a single unit? Is the kind of *interview* performed by  
594 a journalist the same as the kind that one undergoes when applying for a job? Ontology  
595 designers face many such thorny questions, and the project of ontology design hearkens  
596 back to Borges' (1993) *Celestial Emporium of Benevolent Knowledge*, which divides animals  
597 into:

598 (a) belonging to the emperor; (b) embalmed; (c) tame; (d) suckling pigs; (e)  
599 sirens; (f) fabulous; (g) stray dogs; (h) included in the present classification;  
600 (i) frenzied; (j) innumerable; (k) drawn with a very fine camelhair brush; (l) et  
601 cetera; (m) having just broken the water pitcher; (n) that from a long way off  
602 resemble flies.

603 Difficulties in ontology construction have led some linguists to argue that there is no task-  
604 independent way to partition up word meanings (Kilgarriff, 1997).

605 Some problems are easier. Each member in a group of *journalists* is a *journalist*: the -s  
606 suffix distinguishes the plural meaning from the singular in most of the nouns in English.  
607 Similarly, a *journalist* can be thought of, perhaps colloquially, as someone who produces or  
608 works on a *journal*. (Taking this approach even further, the word *journal* derives from the  
609 French *jour+nal*, or *day+ly* = *daily*.) In this way, the meaning of a word is constructed from  
610 the constituent parts — the principle of **compositionality**. This principle can be applied  
611 to larger units: phrases, sentences, and beyond. Indeed, one of the great strengths of the  
612 compositional view of meaning is that it provides a roadmap for understanding entire  
613 texts and dialogues through a single analytic lens, grounding out in the smallest parts of  
614 individual words.

615 But alongside *journalists* and *anti-parliamentarians*, there are many words that seem to  
616 be linguistic atoms: think, for example, of *whale*, *blubber*, and *Nantucket*. Furthermore,  
617 idiomatic phrases like *kick the bucket* and *shoot the breeze* have meanings that are quite  
618 different from the sum of their parts (Sag et al., 2002). Composition is of little help for such  
619 words and expressions, but their meanings can be ascertained — or at least approximated  
620 — from the contexts in which they appear. Take, for example, *blubber*, which appears in  
621 such contexts as:

- 622 (1.4) The blubber served them as fuel.  
623 (1.5) ... extracting it from the blubber of the large fish ...

624 (1.6) Amongst oily substances, blubber has been employed as a manure.

625 These contexts form the **distributional properties** of the word *blubber*, and they link it to  
 626 words which can appear in similar constructions: *fat*, *pelts*, and *barnacles*. This distribu-  
 627 tional perspective makes it possible to learn about meaning from unlabeled data alone;  
 628 unlike relational and compositional semantics, no manual annotation or expert knowl-  
 629 edge is required. Distributional semantics is thus capable of covering a huge range of  
 630 linguistic phenomena. However, it lacks precision: *blubber* is similar to *fat* in one sense, to  
 631 *pelts* in another sense, and to *barnacles* in still another. The question of *why* all these words  
 632 tend to appear in the same contexts is left unanswered.

633 The relational, compositional, and distributional perspectives all contribute to our un-  
 634 derstanding of linguistic meaning, and all three appear to be critical to natural language  
 635 processing. Yet they are uneasy collaborators, requiring seemingly incompatible repre-  
 636 sentations and algorithmic approaches. This text presents some of the best known and  
 637 most successful methods for working with each of these representations, but it is hoped  
 638 that future research will reveal new ways to combine them.

### 639 1.3 Learning to do natural language processing

640 This text began with the notes that I use for teaching Georgia Tech’s undergraduate and  
 641 graduate courses on natural language processing, CS 4650 and 7650. There are several  
 642 other good resources (e.g., Manning and Schütze, 1999; Jurafsky and Martin, 2009; Smith,  
 643 2011; Collins, 2013), but the goal of this text is focus on a core subset of the field, uni-  
 644 fied by the concepts of learning and search. A remarkable thing about natural language  
 645 processing is that so many problems can be solved by a compact set of methods:

646 **Search.** Viterbi, CKY, minimum spanning tree, shift-reduce, integer linear programming,  
 647 beam search.

648 **Learning.** Naïve Bayes, logistic regression, perceptron, expectation-maximization, matrix  
 649 factorization, backpropagation, recurrent neural networks.

650 This text explains how these methods work, and how they can be applied to problems  
 651 that arise in the computer processing of natural language: document classification, word  
 652 sense disambiguation, sequence labeling (part-of-speech tagging and named entity recog-  
 653 nition), parsing, coreference resolution, relation extraction, discourse analysis, language  
 654 modeling, and machine translation.

#### 655 1.3.1 Background

656 Because natural language processing draws on many different intellectual traditions, al-  
 657 most everyone who approaches it feels underprepared in one way or another. Here is a

658 summary of what is expected, and where you can learn more:

659 **Mathematics and machine learning.** The text assumes a background in multivariate cal-  
660 culus and linear algebra: vectors, matrices, derivatives, and partial derivatives. You  
661 should also be familiar with probability and statistics. A review of basic proba-  
662 bility is found in Appendix A, and a minimal review of numerical optimization is  
663 found in Appendix B. For linear algebra, the online course and textbook from Strang  
664 (2016) are excellent sources of review material. Deisenroth et al. (2018) are currently  
665 preparing a textbook on *Mathematics for Machine Learning*, and several chapters can  
666 be found online.<sup>6</sup> For an introduction to probabilistic modeling and estimation, see  
667 James et al. (2013); for a more advanced and comprehensive discussion of the same  
668 material, the classic reference is Hastie et al. (2009).

669 **Linguistics.** This book assumes no formal training in linguistics, aside from elementary  
670 concepts like nouns and verbs, which you have probably encountered in the study  
671 of English grammar. Ideas from linguistics are introduced throughout the text as  
672 needed, including discussions of morphology and syntax (chapter 9), semantics  
673 (chapters 12 and 13), and discourse (chapter 16). Linguistic issues also arise in the  
674 application-focused chapters 4, 8, and 18. A short guide to linguistics for students  
675 of natural language processing is offered by Bender (2013); you are encouraged to  
676 start there, and then pick up a more comprehensive introductory textbook (e.g., Ak-  
677 majian et al., 2010; Fromkin et al., 2013).

678 **Computer science.** The book is targeted at computer scientists, who are assumed to have  
679 taken introductory courses on the analysis of algorithms and complexity theory. In  
680 particular, you should be familiar with asymptotic analysis of the time and memory  
681 costs of algorithms, and should have seen dynamic programming. The classic text  
682 on algorithms is offered by Cormen et al. (2009); for an introduction to the theory of  
683 computation, see Arora and Barak (2009) and Sipser (2012).

### 684 1.3.2 How to use this book

685 The textbook is organized into four main units:

686 **Learning.** This section builds up a set of machine learning tools that will be used through-  
687 out the rest of the textbook. Because the focus is on machine learning, the text  
688 representations and linguistic phenomena are mostly simple: “bag-of-words” text  
689 classification is treated as a model example. Chapter 4 describes some of the more  
690 linguistically interesting applications of word-based text analysis.

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<sup>6</sup><https://mml-book.github.io/>

691 **Sequences and trees.** This section introduces the treatment of language as a structured  
 692 phenomena. It describes sequence and tree representations and the algorithms that  
 693 they facilitate, as well as the limitations that these representations impose. Chapter  
 694 9 introduces finite state automata and briefly overviews a context-free account of  
 695 English syntax.

696 **Meaning.** This section takes a broad view of efforts to represent and compute meaning  
 697 from text, ranging from formal logic to neural word embeddings. It also includes  
 698 two topics that are closely related to semantics: resolution of ambiguous references,  
 699 and analysis of multi-sentence discourse structure.

700 **Applications.** The final section offers chapter-length treatments on three of the most prominent  
 701 applications of natural language processing: information extraction, machine  
 702 translation, and text generation. Each of these applications merits a textbook length  
 703 treatment of its own (Koehn, 2009; Grishman, 2012; Reiter and Dale, 2000); the chapters  
 704 here explain some of the most well known systems using the formalisms and  
 705 methods built up earlier in the book, while introducing methods such as neural attention.  
 706

707 Each chapter contains some advanced material, which is marked with an asterisk.  
 708 This material can be safely omitted without causing misunderstandings later on. But  
 709 even without these advanced sections, the text is too long for a single semester course, so  
 710 instructors will have to pick and choose among the chapters.

711 Chapters 2 and 3 provide building blocks that will be used throughout the book, and  
 712 chapter 4 describes some critical aspects of the practice of language technology. Lan-  
 713 guage models (chapter 6), sequence labeling (chapter 7), and parsing (chapter 10 and 11)  
 714 are canonical topics in natural language processing, and distributed word embeddings  
 715 (chapter 14) are so ubiquitous that students will complain if you leave them out. Of the  
 716 applications, machine translation (chapter 18) is the best choice: it is more cohesive than  
 717 information extraction, and more mature than text generation. In my experience, nearly  
 718 all students benefit from the review of probability in Appendix A.

- 719 • A course focusing on machine learning should add the chapter on unsupervised  
 720 learning (chapter 5). The chapters on predicate-argument semantics (chapter 13),  
 721 reference resolution (chapter 15), and text generation (chapter 19) are particularly  
 722 influenced by recent machine learning innovations, including deep neural networks  
 723 and learning to search.
- 724 • A course with a more linguistic orientation should add the chapters on applica-  
 725 tions of sequence labeling (chapter 8), formal language theory (chapter 9), semantics  
 726 (chapter 12 and 13), and discourse (chapter 16).

- 727 • For a course with a more applied focus — for example, a course targeting under-  
728 graduates — I recommend the chapters on applications of sequence labeling (chap-  
729 ter 8), predicate-argument semantics (chapter 13), information extraction (chapter 17),  
730 and text generation (chapter 19).

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745

## Part I

746

# Learning



747

## Chapter 2

748

# Linear text classification

749 We'll start with the problem of **text classification**: given a text document, assign it a dis-  
750 crete label  $y \in \mathcal{Y}$ , where  $\mathcal{Y}$  is the set of possible labels. This problem has many appli-  
751 cations, from spam filtering to analysis of electronic health records. Text classification is  
752 also a building block that is used throughout more complex natural language processing  
753 tasks.

754 To perform this task, the first question is how to represent each document. A common  
755 approach is to use a vector of word counts, e.g.,  $\mathbf{x} = [0, 1, 1, 0, 0, 2, 0, 1, 13, 0 \dots]^T$ , where  
756  $x_j$  is the count of word  $j$ . The length of  $\mathbf{x}$  is  $V \triangleq |\mathcal{V}|$ , where  $\mathcal{V}$  is the set of possible words  
757 in the vocabulary.

758 The object  $\mathbf{x}$  is a vector, but colloquially we call it a **bag of words**, because it includes  
759 only information about the count of each word, and not the order in which the words  
760 appear. We have thrown out grammar, sentence boundaries, paragraphs — everything  
761 but the words. Yet the bag of words model is surprisingly effective for text classification.  
762 If you see the word *freeee* in an email, is it a spam email? What if you see the word  
763 *Bayesian*? For many labeling problems, individual words can be strong predictors.

764 To predict a label from a bag-of-words, we can assign a score to each word in the  
765 vocabulary, measuring the compatibility with the label. In the spam filtering case, we  
766 might assign a positive score to the word *freeee* for the label SPAM, and a negative score  
767 to the word *Bayesian*. These scores are called **weights**, and they are arranged in a column  
768 vector  $\theta$ .

769 Suppose that you want a multiclass classifier, where  $K \triangleq |\mathcal{Y}| > 2$ . For example, we  
770 might want to classify news stories about sports, celebrities, music, and business. The goal  
771 is to predict a label  $\hat{y}$ , given the bag of words  $\mathbf{x}$ , using the weights  $\theta$ . For each label  $y \in \mathcal{Y}$ ,  
772 we compute a score  $\Psi(\mathbf{x}, y)$ , which is a scalar measure of the compatibility between the  
773 bag-of-words  $\mathbf{x}$  and the label  $y$ . In a linear bag-of-words classifier, this score is the vector

774 inner product between the weights  $\theta$  and the output of a **feature function**  $f(x, y)$ ,

$$\Psi(x, y) = \theta \cdot f(x, y). \quad [2.1]$$

775 As the notation suggests,  $f$  is a function of two arguments, the word counts  $x$  and the  
 776 label  $y$ , and it returns a vector output. For example, given arguments  $x$  and  $y$ , element  $j$   
 777 of this feature vector might be,

$$f_j(x, y) = \begin{cases} x_{freeee}, & \text{if } y = \text{SPAM} \\ 0, & \text{otherwise} \end{cases} \quad [2.2]$$

778 This function returns the count of the word *freeee* if the label is SPAM, and it returns zero  
 779 otherwise. The corresponding weight  $\theta_j$  then scores the compatibility of the word *freeee*  
 780 with the label SPAM. A positive score means that this word makes the label more likely.

To formalize this feature function, we define  $f(x, y)$  as a column vector,

$$f(x, y = 1) = [x; \underbrace{0; 0; \dots; 0}_{(K-1) \times V}] \quad [2.3]$$

$$f(x, y = 2) = [\underbrace{0; 0; \dots; 0}_V; x; \underbrace{0; 0; \dots; 0}_{(K-2) \times V}] \quad [2.4]$$

$$f(x, y = K) = [\underbrace{0; 0; \dots; 0}_{(K-1) \times V}; x], \quad [2.5]$$

781 where  $\underbrace{[0; 0; \dots; 0]}_{(K-1) \times V}$  is a column vector of  $(K - 1) \times V$  zeros, and the semicolon indicates  
 782 vertical concatenation. This arrangement is shown in Figure 2.1; the notation may seem  
 783 awkward at first, but it generalizes to an impressive range of learning settings.

Given a vector of weights,  $\theta \in \mathbb{R}^{V \times K}$ , we can now compute the score  $\Psi(x, y)$ . This  
 inner product gives a scalar measure of the compatibility of the observation  $x$  with label  
 $y$ .<sup>1</sup> For any document  $x$ , we predict the label  $\hat{y}$ ,

$$\hat{y} = \operatorname{argmax}_{y \in \mathcal{Y}} \Psi(x, y) \quad [2.6]$$

$$\Psi(x, y) = \theta \cdot f(x, y). \quad [2.7]$$

784 This inner product notation gives a clean separation between the *data* ( $x$  and  $y$ ) and the  
 785 *parameters* ( $\theta$ ). This notation also generalizes nicely to **structured prediction**, in which

---

<sup>1</sup>Only  $V \times (K - 1)$  features and weights are necessary. By stipulating that  $\Psi(x, y = K) = 0$  regardless of  $x$ , it is possible to implement any classification rule that can be achieved with  $V \times K$  features and weights. This is the approach taken in binary classification rules like  $y = \text{Sign}(\beta \cdot x + a)$ , where  $\beta$  is a vector of weights,  $a$  is an offset, and the label set is  $\mathcal{Y} = \{-1, 1\}$ . However, for multiclass classification, it is more concise to write  $\theta \cdot f(x, y)$  for all  $y \in \mathcal{Y}$ .

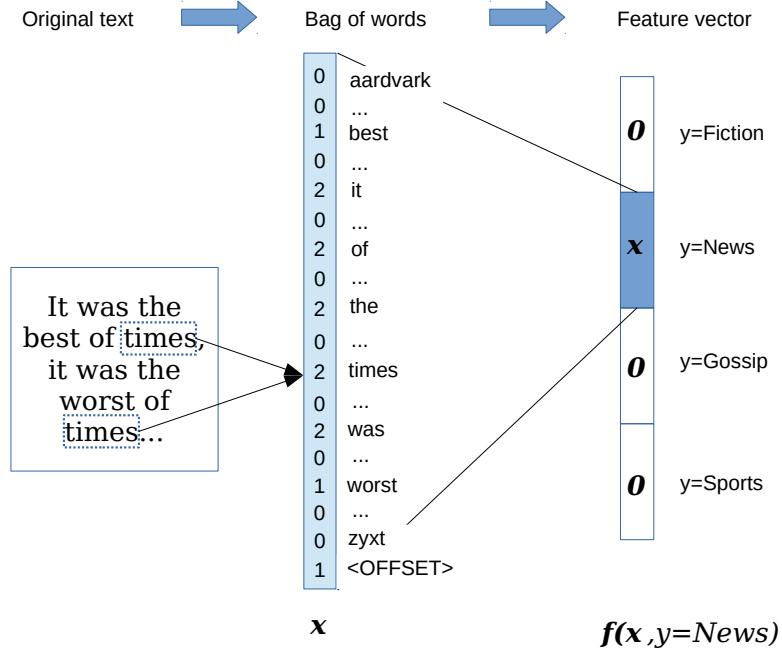


Figure 2.1: The bag-of-words and feature vector representations, for a hypothetical text classification task.

786 the space of labels  $\mathcal{Y}$  is very large, and we want to model shared substructures between  
 787 labels.

788 It is common to add an **offset feature** at the end of the vector of word counts  $\mathbf{x}$ , which  
 789 is always 1. We then have to also add an extra zero to each of the zero vectors, to make the  
 790 vector lengths match. This gives the entire feature vector  $\mathbf{f}(\mathbf{x}, y)$  a length of  $(V + 1) \times K$ .  
 791 The weight associated with this offset feature can be thought of as a bias for or against  
 792 each label. For example, if we expect most documents to be spam, then the weight for  
 793 the offset feature for  $y = \text{SPAM}$  should be larger than the weight for the offset feature for  
 794  $y = \text{HAM}$ .

Returning to the weights  $\theta$ , where do they come from? One possibility is to set them by hand. If we wanted to distinguish, say, English from Spanish, we can use English and Spanish dictionaries, and set the weight to one for each word that appears in the

associated dictionary. For example,<sup>2</sup>

$$\begin{array}{ll} \theta_{(E,bicycle)} = 1 & \theta_{(S,bicycle)} = 0 \\ \theta_{(E,bicicleta)} = 0 & \theta_{(S,bicicleta)} = 1 \\ \theta_{(E,con)} = 1 & \theta_{(S,con)} = 1 \\ \theta_{(E,ordinateur)} = 0 & \theta_{(S,ordinateur)} = 0. \end{array}$$

795 Similarly, if we want to distinguish positive and negative sentiment, we could use positive  
 796 and negative **sentiment lexicons** (see § 4.1.2), which are defined by social psychologists  
 797 (Tausczik and Pennebaker, 2010).

798 But it is usually not easy to set classification weights by hand, due to the large number  
 799 of words and the difficulty of selecting exact numerical weights. Instead, we will learn the  
 800 weights from data. Email users manually label messages as SPAM; newspapers label their  
 801 own articles as BUSINESS or STYLE. Using such **instance labels**, we can automatically  
 802 acquire weights using **supervised machine learning**. This chapter will discuss several  
 803 machine learning approaches for classification. The first is based on probability. For a  
 804 review of probability, consult Appendix A.

## 805 2.1 Naïve Bayes

806 The **joint probability** of a bag of words  $\mathbf{x}$  and its true label  $y$  is written  $p(\mathbf{x}, y)$ . Suppose  
 807 we have a dataset of  $N$  labeled instances,  $\{(\mathbf{x}^{(i)}, y^{(i)})\}_{i=1}^N$ , which we assume are **independ-**  
 808 **ent and identically distributed (IID)** (see § A.3). Then the joint probability of the entire  
 809 dataset, written  $p(\mathbf{x}^{(1:N)}, y^{(1:N)})$ , is equal to  $\prod_{i=1}^N p_{X,Y}(\mathbf{x}^{(i)}, y^{(i)})$ .<sup>3</sup>

What does this have to do with classification? One approach to classification is to set the weights  $\boldsymbol{\theta}$  so as to maximize the joint probability of a **training set** of labeled documents. This is known as **maximum likelihood estimation**:

$$\hat{\boldsymbol{\theta}} = \operatorname{argmax}_{\boldsymbol{\theta}} p(\mathbf{x}^{(1:N)}, y^{(1:N)}; \boldsymbol{\theta}) \quad [2.8]$$

$$= \operatorname{argmax}_{\boldsymbol{\theta}} \prod_{i=1}^N p(\mathbf{x}^{(i)}, y^{(i)}; \boldsymbol{\theta}) \quad [2.9]$$

$$= \operatorname{argmax}_{\boldsymbol{\theta}} \sum_{i=1}^N \log p(\mathbf{x}^{(i)}, y^{(i)}; \boldsymbol{\theta}). \quad [2.10]$$

---

<sup>2</sup>In this notation, each tuple (language, word) indexes an element in  $\boldsymbol{\theta}$ , which remains a vector.

<sup>3</sup>The notation  $p_{X,Y}(\mathbf{x}^{(i)}, y^{(i)})$  indicates the joint probability that random variables  $X$  and  $Y$  take the specific values  $\mathbf{x}^{(i)}$  and  $y^{(i)}$  respectively. The subscript will often be omitted when it is clear from context. For a review of random variables, see Appendix A.

---

**Algorithm 1** Generative process for the Naïve Bayes classifier

---

**for** Document  $i \in \{1, 2, \dots, N\}$  **do:**  
 Draw the label  $y^{(i)} \sim \text{Categorical}(\boldsymbol{\mu})$ ;  
 Draw the word counts  $\mathbf{x}^{(i)} | y^{(i)} \sim \text{Multinomial}(\boldsymbol{\phi}_{y^{(i)}})$ .

---

810 The notation  $p(\mathbf{x}^{(i)}, y^{(i)}; \boldsymbol{\theta})$  indicates that  $\boldsymbol{\theta}$  is a *parameter* of the probability function. The  
 811 product of probabilities can be replaced by a sum of log-probabilities because the log func-  
 812 tion is monotonically increasing over positive arguments, and so the same  $\boldsymbol{\theta}$  will maxi-  
 813 mize both the probability and its logarithm. Working with logarithms is desirable because  
 814 of numerical stability: on a large dataset, multiplying many probabilities can **underflow**  
 815 to zero.<sup>4</sup>

816 The probability  $p(\mathbf{x}^{(i)}, y^{(i)}; \boldsymbol{\theta})$  is defined through a **generative model** — an idealized  
 817 random process that has generated the observed data.<sup>5</sup> Algorithm 1 describes the gener-  
 818 ative model underlying the **Naïve Bayes** classifier, with parameters  $\boldsymbol{\theta} = \{\boldsymbol{\mu}, \boldsymbol{\phi}\}$ .

- 819 • The first line of this generative model encodes the assumption that the instances are  
 820 mutually independent: neither the label nor the text of document  $i$  affects the label  
 821 or text of document  $j$ .<sup>6</sup> Furthermore, the instances are identically distributed: the  
 822 distributions over the label  $y^{(i)}$  and the text  $\mathbf{x}^{(i)}$  (conditioned on  $y^{(i)}$ ) are the same  
 823 for all instances  $i$ .
- 824 • The second line of the generative model states that the random variable  $y^{(i)}$  is drawn  
 825 from a categorical distribution with parameter  $\boldsymbol{\mu}$ . Categorical distributions are like  
 826 weighted dice: the vector  $\boldsymbol{\mu} = [\mu_1, \mu_2, \dots, \mu_K]^\top$  gives the probabilities of each la-  
 827 bel, so that the probability of drawing label  $y$  is equal to  $\mu_y$ . For example, if  $\mathcal{Y} =$   
 828  $\{\text{POSITIVE}, \text{NEGATIVE}, \text{NEUTRAL}\}$ , we might have  $\boldsymbol{\mu} = [0.1, 0.7, 0.2]^\top$ . We require  
 829  $\sum_{y \in \mathcal{Y}} \mu_y = 1$  and  $\mu_y \geq 0, \forall y \in \mathcal{Y}$ .<sup>7</sup>
- 830 • The third line describes how the bag-of-words counts  $\mathbf{x}^{(i)}$  are generated. By writing  
 831  $\mathbf{x}^{(i)} | y^{(i)}$ , this line indicates that the word counts are conditioned on the label, so

---

<sup>4</sup>Throughout this text, you may assume all logarithms and exponents are base 2, unless otherwise indicated. Any reasonable base will yield an identical classifier, and base 2 is most convenient for working out examples by hand.

<sup>5</sup>Generative models will be used throughout this text. They explicitly define the assumptions underlying the form of a probability distribution over observed and latent variables. For a readable introduction to generative models in statistics, see Blei (2014).

<sup>6</sup>Can you think of any cases in which this assumption is too strong?

<sup>7</sup>Formally, we require  $\boldsymbol{\mu} \in \Delta^{K-1}$ , where  $\Delta^{K-1}$  is the  $K - 1$  **probability simplex**, the set of all vectors of  $K$  nonnegative numbers that sum to one. Because of the sum-to-one constraint, there are  $K - 1$  degrees of freedom for a vector of size  $K$ .

832 that the joint probability is factored using the chain rule,

$$p_{X,Y}(x^{(i)}, y^{(i)}) = p_{X|Y}(x^{(i)} | y^{(i)}) \times p_Y(y^{(i)}). \quad [2.11]$$

The specific distribution  $p_{X|Y}$  is the **multinomial**, which is a probability distribution over vectors of non-negative counts. The probability mass function for this distribution is:

$$p_{\text{mult}}(x; \phi) = B(x) \prod_{j=1}^V \phi_j^{x_j} \quad [2.12]$$

$$B(x) = \frac{(\sum_{j=1}^V x_j)!}{\prod_{j=1}^V (x_j)!} \quad [2.13]$$

833 As in the categorical distribution, the parameter  $\phi_j$  can be interpreted as a proba-  
 834 bility: specifically, the probability that any given token in the document is the word  
 835  $j$ . The multinomial distribution involves a product over words, with each term in  
 836 the product equal to the probability  $\phi_j$ , exponentiated by the count  $x_j$ . Words that  
 837 have zero count play no role in this product, because  $\phi_j^0 = 1$ . The term  $B(x)$  doesn't  
 838 depend on  $\phi$ , and can usually be ignored. Can you see why we need this term at  
 839 all?<sup>8</sup>

840 The notation  $p(x | y; \phi)$  indicates the conditional probability of word counts  $x$  given  
 841 label  $y$ , with parameter  $\phi$ , which is equal to  $p_{\text{mult}}(x; \phi_y)$ . By specifying the multino-  
 842 mial distribution, we describe the **multinomial naïve Bayes** classifier. Why “naïve”?  
 843 Because the multinomial distribution treats each word token independently: the  
 844 probability mass function factorizes across the counts.<sup>9</sup>

### 845 2.1.1 Types and tokens

846 A slight modification to the generative model of Naïve Bayes is shown in Algorithm 2.  
 847 Instead of generating a vector of counts of **types**,  $x$ , this model generates a *sequence of*  
 848 **tokens**,  $w = (w_1, w_2, \dots, w_M)$ . The distinction between types and tokens is critical:  $x_j \in$   
 849  $\{0, 1, 2, \dots, M\}$  is the count of word type  $j$  in the vocabulary, e.g., the number of times  
 850 the word *cannibal* appears;  $w_m \in \mathcal{V}$  is the identity of token  $m$  in the document, e.g.  $w_m =$   
 851 *cannibal*.

---

<sup>8</sup>Technically, a multinomial distribution requires a second parameter, the total number of word counts in  $x$ . In the bag-of-words representation is equal to the number of words in the document. However, this parameter is irrelevant for classification.

<sup>9</sup>You can plug in any probability distribution to the generative story and it will still be Naïve Bayes, as long as you are making the “naïve” assumption that the features are conditionally independent, given the label. For example, a multivariate Gaussian with diagonal covariance is naïve in exactly the same sense.

**Algorithm 2** Alternative generative process for the Naïve Bayes classifier

---

```

for Document  $i \in \{1, 2, \dots, N\}$  do:
    Draw the label  $y^{(i)} \sim \text{Categorical}(\boldsymbol{\mu})$ ;
    for Token  $m \in \{1, 2, \dots, M_i\}$  do:
        Draw the token  $w_m^{(i)} | y^{(i)} \sim \text{Categorical}(\boldsymbol{\phi}_{y^{(i)}})$ .

```

---

852     The probability of the sequence  $\mathbf{w}$  is a product of categorical probabilities. Algo-  
 853     rithm 2 makes a conditional independence assumption: each token  $w_m^{(i)}$  is independent  
 854     of all other tokens  $w_{n \neq m}^{(i)}$ , conditioned on the label  $y^{(i)}$ . This is identical to the “naïve”  
 855     independence assumption implied by the multinomial distribution, and as a result, the  
 856     optimal parameters for this model are identical to those in multinomial Naïve Bayes. For  
 857     any instance, the probability assigned by this model is proportional to the probability un-  
 858     der multinomial Naïve Bayes. The constant of proportionality is the factor  $B(\mathbf{x})$ , which  
 859     appears in the multinomial distribution. Because  $B(\mathbf{x}) \geq 1$ , the probability for a vector  
 860     of counts  $\mathbf{x}$  is at least as large as the probability for a list of words  $\mathbf{w}$  that induces the  
 861     same counts: there can be many word sequences that correspond to a single vector of  
 862     counts. For example, *man bites dog* and *dog bites man* correspond to an identical count vec-  
 863     tor,  $\{bites : 1, dog : 1, man : 1\}$ , and  $B(\mathbf{x})$  is equal to the total number of possible word  
 864     orderings for count vector  $\mathbf{x}$ .

865     Sometimes it is useful to think of instances as counts of types,  $\mathbf{x}$ ; other times, it is  
 866     better to think of them as sequences of tokens,  $\mathbf{w}$ . If the tokens are generated from a  
 867     model that assumes conditional independence, then these two views lead to probability  
 868     models that are identical, except for a scaling factor that does not depend on the label or  
 869     the parameters.

870 **2.1.2 Prediction**

The Naïve Bayes prediction rule is to choose the label  $y$  which maximizes  $\log p(\mathbf{x}, y; \boldsymbol{\mu}, \boldsymbol{\phi})$ :

$$\hat{y} = \underset{y}{\operatorname{argmax}} \log p(\mathbf{x}, y; \boldsymbol{\mu}, \boldsymbol{\phi}) \quad [2.14]$$

$$= \underset{y}{\operatorname{argmax}} \log p(\mathbf{x} | y; \boldsymbol{\phi}) + \log p(y; \boldsymbol{\mu}) \quad [2.15]$$

Now we can plug in the probability distributions from the generative story.

$$\log p(\mathbf{x} \mid y; \boldsymbol{\phi}) + \log p(y; \boldsymbol{\mu}) = \log \left[ B(\mathbf{x}) \prod_{j=1}^V \phi_{y,j}^{x_j} \right] + \log \mu_y \quad [2.16]$$

$$= \log B(\mathbf{x}) + \sum_{j=1}^V x_j \log \phi_{y,j} + \log \mu_y \quad [2.17]$$

$$= \log B(\mathbf{x}) + \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}, y), \quad [2.18]$$

where

$$\boldsymbol{\theta} = [\boldsymbol{\theta}^{(1)}; \boldsymbol{\theta}^{(2)}; \dots; \boldsymbol{\theta}^{(K)}] \quad [2.19]$$

$$\boldsymbol{\theta}^{(y)} = [\log \phi_{y,1}; \log \phi_{y,2}; \dots; \log \phi_{y,V}; \log \mu_y] \quad [2.20]$$

871 The feature function  $\mathbf{f}(\mathbf{x}, y)$  is a vector of  $V$  word counts and an offset, padded by  
 872 zeros for the labels not equal to  $y$  (see Equations 2.3-2.5, and Figure 2.1). This construction  
 873 ensures that the inner product  $\boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}, y)$  only activates the features whose weights are  
 874 in  $\boldsymbol{\theta}^{(y)}$ . These features and weights are all we need to compute the joint log-probability  
 875  $\log p(\mathbf{x}, y)$  for each  $y$ . This is a key point: through this notation, we have converted the  
 876 problem of computing the log-likelihood for a document-label pair  $(\mathbf{x}, y)$  into the compu-  
 877 tation of a vector inner product.

### 878 2.1.3 Estimation

879 The parameters of the categorical and multinomial distributions have a simple interpre-  
 880 tation: they are vectors of expected frequencies for each possible event. Based on this  
 881 interpretation, it is tempting to set the parameters empirically,

$$\phi_{y,j} = \frac{\text{count}(y, j)}{\sum_{j'=1}^V \text{count}(y, j')} = \frac{\sum_{i:y^{(i)}=y} x_j^{(i)}}{\sum_{j'=1}^V \sum_{i:y^{(i)}=y} x_{j'}^{(i)}}, \quad [2.21]$$

882 where  $\text{count}(y, j)$  refers to the count of word  $j$  in documents with label  $y$ .

883 Equation 2.21 defines the **relative frequency estimate** for  $\phi$ . It can be justified as a  
 884 **maximum likelihood estimate**: the estimate that maximizes the probability  $p(\mathbf{x}^{(1:N)}, y^{(1:N)}; \boldsymbol{\theta})$ .  
 885 Based on the generative model in Algorithm 1, the log-likelihood is,

$$\mathcal{L}(\boldsymbol{\phi}, \boldsymbol{\mu}) = \sum_{i=1}^N \log p_{\text{mult}}(\mathbf{x}^{(i)}; \boldsymbol{\phi}_{y^{(i)}}) + \log p_{\text{cat}}(y^{(i)}; \boldsymbol{\mu}), \quad [2.22]$$

which is now written as a function  $\mathcal{L}$  of the parameters  $\phi$  and  $\mu$ . Let's continue to focus on the parameters  $\phi$ . Since  $p(y)$  is constant with respect to  $\phi$ , we can drop it:

$$\mathcal{L}(\phi) = \sum_{i=1}^N \log p_{\text{mult}}(\mathbf{x}^{(i)}; \phi_{y^{(i)}}) = \sum_{i=1}^N \log B(\mathbf{x}^{(i)}) + \sum_{j=1}^V x_j^{(i)} \log \phi_{y^{(i)}, j}, \quad [2.23]$$

where  $B(\mathbf{x}^{(i)})$  is constant with respect to  $\phi$ .

Maximum-likelihood estimation chooses  $\phi$  to maximize the log-likelihood  $\mathcal{L}$ . However, the solution must obey the following constraints:

$$\sum_{j=1}^V \phi_{y,j} = 1 \quad \forall y \quad [2.24]$$

These constraints can be incorporated by adding a set of Lagrange multipliers to the objective (see Appendix B for more details). To solve for each  $\theta_y$ , we maximize the Lagrangian,

$$\ell(\phi_y) = \sum_{i:y^{(i)}=y} \sum_{j=1}^V x_j^{(i)} \log \phi_{y,j} - \lambda \left( \sum_{j=1}^V \phi_{y,j} - 1 \right). \quad [2.25]$$

Differentiating with respect to the parameter  $\phi_{y,j}$  yields,

$$\frac{\partial \ell(\phi_y)}{\partial \phi_{y,j}} = \sum_{i:y^{(i)}=y} x_j^{(i)} / \phi_{y,j} - \lambda. \quad [2.26]$$

The solution is obtained by setting each element in this vector of derivatives equal to zero,

$$\lambda \phi_{y,j} = \sum_{i:y^{(i)}=y} x_j^{(i)} \quad [2.27]$$

$$\phi_{y,j} \propto \sum_{i:y^{(i)}=y} x_j^{(i)} = \sum_{i=1}^N \delta(y^{(i)} = y) x_j^{(i)} = \text{count}(y, j), \quad [2.28]$$

where  $\delta(y^{(i)} = y)$  is a **delta function**, also sometimes called an **indicator function**, which returns one if  $y^{(i)} = y$ , and zero otherwise. Equation 2.28 shows three different notations for the same thing: a sum over the word counts for all documents  $i$  such that the label  $y^{(i)} = y$ . This gives a solution for each  $\phi_y$  up to a constant of proportionality. Now recall the constraint  $\sum_{j=1}^V \phi_{y,j} = 1$ , which arises because  $\phi_y$  represents a vector of probabilities for each word in the vocabulary. This constraint leads to an exact solution,

$$\phi_{y,j} = \frac{\text{count}(y, j)}{\sum_{j'=1}^V \text{count}(y, j')}. \quad [2.29]$$

This is equal to the relative frequency estimator from Equation 2.21. A similar derivation gives  $\mu_y \propto \sum_{i=1}^N \delta(y^{(i)} = y)$ .

893 **2.1.4 Smoothing and MAP estimation**

894 With text data, there are likely to be pairs of labels and words that never appear in the  
 895 training set, leaving  $\phi_{y,j} = 0$ . For example, the word *Bayesian* may have never yet ap-  
 896 peared in a spam email. But choosing a value of  $\phi_{\text{SPAM}, \text{Bayesian}} = 0$  would allow this single  
 897 feature to completely veto a label, since  $p(\text{SPAM} | \mathbf{x}) = 0$  if  $\mathbf{x}_{\text{Bayesian}} > 0$ .

898 This is undesirable, because it imposes high **variance**: depending on what data hap-  
 899 pens to be in the training set, we could get vastly different classification rules. One so-  
 900 lution is to **smooth** the probabilities, by adding a “pseudocount” of  $\alpha$  to each count, and  
 901 then normalizing.

$$\phi_{y,j} = \frac{\alpha + \text{count}(y, j)}{V\alpha + \sum_{j'=1}^V \text{count}(y, j')} \quad [2.30]$$

902 This is called **Laplace smoothing**.<sup>10</sup> The pseudocount  $\alpha$  is a **hyperparameter**, because it  
 903 controls the form of the log-likelihood function, which in turn drives the estimation of  $\phi$ .

904 Smoothing reduces variance, but it takes us away from the maximum likelihood esti-  
 905 mate: it imposes a **bias**. In this case, the bias points towards uniform probabilities. Ma-  
 906 chine learning theory shows that errors on heldout data can be attributed to the sum of  
 907 bias and variance (Mohri et al., 2012). Techniques for reducing variance typically increase  
 908 the bias, leading to a **bias-variance tradeoff**.

- 909     • Unbiased classifiers may **overfit** the training data, yielding poor performance on  
   910       unseen data.
- 911     • But if the smoothing is too large, the resulting classifier can **underfit** instead. In the  
   912       limit of  $\alpha \rightarrow \infty$ , there is zero variance: you get the same classifier, regardless of the  
   913       data. However, the bias is likely to be large.

914 **2.1.5 Setting hyperparameters**

915 How should we choose the best value of hyperparameters like  $\alpha$ ? Maximum likelihood  
 916 will not work: the maximum likelihood estimate of  $\alpha$  on the training set will always be  
 917  $\alpha = 0$ . In many cases, what we really want is **accuracy**: the number of correct predictions,  
 918 divided by the total number of predictions. (Other measures of classification performance  
 919 are discussed in § 4.4.) As we will see, it is hard to optimize for accuracy directly. But for  
 920 scalar hyperparameters like  $\alpha$  can be tuned by a simple heuristic called **grid search**: try a  
 921 set of values (e.g.,  $\alpha \in \{0.001, 0.01, 0.1, 1, 10\}$ ), compute the accuracy for each value, and  
 922 choose the setting that maximizes the accuracy.

---

<sup>10</sup>Laplace smoothing has a Bayesian justification, in which the generative model is extended to include  $\phi$  as a random variable. The resulting estimate is called **maximum a posteriori**, or MAP.

923     The goal is to tune  $\alpha$  so that the classifier performs well on *unseen* data. For this reason,  
924     the data used for hyperparameter tuning should not overlap the training set, where very  
925     small values of  $\alpha$  will be preferred. Instead, we hold out a **development set** (also called  
926     a **tuning set**) for hyperparameter selection. This development set may consist of a small  
927     fraction of the labeled data, such as 10%.

928     We also want to predict the performance of our classifier on unseen data. To do this,  
929     we must hold out a separate subset of data, called the **test set**. It is critical that the test set  
930     not overlap with either the training or development sets, or else we will overestimate the  
931     performance that the classifier will achieve on unlabeled data in the future. The test set  
932     should also not be used when making modeling decisions, such as the form of the feature  
933     function, the size of the vocabulary, and so on (these decisions are reviewed in chapter 4.)  
934     The ideal practice is to use the test set only once — otherwise, the test set is used to guide  
935     the classifier design, and test set accuracy will diverge from accuracy on truly unseen  
936     data. Because annotated data is expensive, this ideal can be hard to follow in practice,  
937     and many test sets have been used for decades. But in some high-impact applications like  
938     machine translation and information extraction, new test sets are released every year.

939     When only a small amount of labeled data is available, the test set accuracy can be  
940     unreliable. *K*-fold **cross-validation** is one way to cope with this scenario: the labeled  
941     data is divided into *K* folds, and each fold acts as the test set, while training on the other  
942     folds. The test set accuracies are then aggregated. In the extreme, each fold is a single data  
943     point; this is called **leave-one-out** cross-validation. To perform hyperparameter tuning in  
944     the context of cross-validation, another fold can be used for grid search. It is important  
945     not to repeatedly evaluate the cross-validated accuracy while making design decisions  
946     about the classifier, or you will overstate the accuracy on truly unseen data.

## 947 2.2 Discriminative learning

948     Naïve Bayes is easy to work with: the weights can be estimated in closed form, and the  
949     probabilistic interpretation makes it relatively easy to extend. However, the assumption  
950     that features are independent can seriously limit its accuracy. Thus far, we have defined  
951     the **feature function**  $f(\mathbf{x}, y)$  so that it corresponds to bag-of-words features: one feature  
952     per word in the vocabulary. In natural language, bag-of-words features violate the as-  
953     sumption of conditional independence — for example, the probability that a document  
954     will contain the word *naïve* is surely higher given that it also contains the word *Bayes* —  
955     but this violation is relatively mild.

956     However, good performance on text classification often requires features that are richer  
957     than the bag-of-words:

- 958       • To better handle out-of-vocabulary terms, we want features that apply to multiple

- 959 words, such as prefixes and suffixes (e.g., *anti*-, *un*-, *-ing*) and capitalization.
- 960 • We also want *n*-gram features that apply to multi-word units: **bigrams** (e.g., *not*  
 961      *good*, *not bad*), **trigrams** (e.g., *not so bad*, *lacking any decency*, *never before imagined*), and  
 962      beyond.

These features flagrantly violate the Naïve Bayes independence assumption. Consider what happens if we add a prefix feature. Under the Naïve Bayes assumption, we make the following approximation:<sup>11</sup>

$$\Pr(\text{word} = \textit{unfit}, \text{prefix} = \textit{un-} \mid y) \approx \Pr(\text{prefix} = \textit{un-} \mid y) \times \Pr(\text{word} = \textit{unfit} \mid y).$$

To test the quality of the approximation, we can manipulate the left-hand side by applying the chain rule,

$$\Pr(\text{word} = \textit{unfit}, \text{prefix} = \textit{un-} \mid y) = \Pr(\text{prefix} = \textit{un-} \mid \text{word} = \textit{unfit}, y) \quad [2.31]$$

$$\times \Pr(\text{word} = \textit{unfit} \mid y) \quad [2.32]$$

But  $\Pr(\text{prefix} = \textit{un-} \mid \text{word} = \textit{unfit}, y) = 1$ , since *un-* is guaranteed to be the prefix for the word *unfit*. Therefore,

$$\Pr(\text{word} = \textit{unfit}, \text{prefix} = \textit{un-} \mid y) = 1 \times \Pr(\text{word} = \textit{unfit} \mid y) \quad [2.33]$$

$$\gg \Pr(\text{prefix} = \textit{un-} \mid y) \times \Pr(\text{word} = \textit{unfit} \mid y), \quad [2.34]$$

963 because the probability of any given word starting with the prefix *un-* is much less than  
 964 one. Naïve Bayes will systematically underestimate the true probabilities of conjunctions  
 965 of positively correlated features. To use such features, we need learning algorithms that  
 966 do not rely on an independence assumption.

967 The origin of the Naïve Bayes independence assumption is the learning objective,  
 968  $p(\mathbf{x}^{(1:N)}, y^{(1:N)})$ , which requires modeling the probability of the observed text. In clas-  
 969 sification problems, we are always given  $\mathbf{x}$ , and are only interested in predicting the label  
 970  $y$ , so it seems unnecessary to model the probability of  $\mathbf{x}$ . **Discriminative learning** algo-  
 971 rithms focus on the problem of predicting  $y$ , and do not attempt to model the probability  
 972 of the text  $\mathbf{x}$ .

### 973 2.2.1 Perceptron

974 In Naïve Bayes, the weights can be interpreted as parameters of a probabilistic model. But  
 975 this model requires an independence assumption that usually does not hold, and limits  
 976 our choice of features. Why not forget about probability and learn the weights in an error-  
 977 driven way? The **perceptron** algorithm, shown in Algorithm 3, is one way to do this.

---

<sup>11</sup>The notation  $\Pr(\cdot)$  refers to the probability of an event, and  $p(\cdot)$  refers to the probability density or mass for a random variable (see Appendix A).

**Algorithm 3** Perceptron learning algorithm

---

```

1: procedure PERCEPTRON( $\mathbf{x}^{(1:N)}, y^{(1:N)}$ )
2:    $t \leftarrow 0$ 
3:    $\boldsymbol{\theta}^{(0)} \leftarrow \mathbf{0}$ 
4:   repeat
5:      $t \leftarrow t + 1$ 
6:     Select an instance  $i$ 
7:      $\hat{y} \leftarrow \operatorname{argmax}_y \boldsymbol{\theta}^{(t-1)} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y)$ 
8:     if  $\hat{y} \neq y^{(i)}$  then
9:        $\boldsymbol{\theta}^{(t)} \leftarrow \boldsymbol{\theta}^{(t-1)} + \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) - \mathbf{f}(\mathbf{x}^{(i)}, \hat{y})$ 
10:    else
11:       $\boldsymbol{\theta}^{(t)} \leftarrow \boldsymbol{\theta}^{(t-1)}$ 
12:    until tired
13:   return  $\boldsymbol{\theta}^{(t)}$ 

```

---

978 Here's what the algorithm says: if you make a mistake, increase the weights for fea-  
 979 tures that are active with the correct label  $y^{(i)}$ , and decrease the weights for features that  
 980 are active with the guessed label  $\hat{y}$ . This is an **online learning** algorithm, since the clas-  
 981 sifier weights change after every example. This is different from Naïve Bayes, which  
 982 computes corpus statistics and then sets the weights in a single operation — Naïve Bayes  
 983 is a **batch learning** algorithm. Algorithm 3 is vague about when this online learning pro-  
 984 cedure terminates. We will return to this issue shortly.

985 The perceptron algorithm may seem like a cheap heuristic: Naïve Bayes has a solid  
 986 foundation in probability, but the perceptron is just adding and subtracting constants from  
 987 the weights every time there is a mistake. Will this really work? In fact, there is some nice  
 988 theory for the perceptron, based on the concept of **linear separability**:

989 **Definition 1** (Linear separability). *The dataset  $\mathcal{D} = \{(\mathbf{x}^{(i)}, y^{(i)})\}_{i=1}^N$  is linearly separable iff  
 990 (if and only if) there exists some weight vector  $\boldsymbol{\theta}$  and some margin  $\rho$  such that for every instance  
 991  $(\mathbf{x}^{(i)}, y^{(i)})$ , the inner product of  $\boldsymbol{\theta}$  and the feature function for the true label,  $\boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)})$ , is  
 992 at least  $\rho$  greater than inner product of  $\boldsymbol{\theta}$  and the feature function for every other possible label,  
 993  $\boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y')$ .*

$$\exists \boldsymbol{\theta}, \rho > 0 : \forall (\mathbf{x}^{(i)}, y^{(i)}) \in \mathcal{D}, \quad \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) \geq \rho + \max_{y' \neq y^{(i)}} \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y'). \quad [2.35]$$

994 Linear separability is important because of the following guarantee: if your data is  
 995 linearly separable, then the perceptron algorithm will find a separator (Novikoff, 1962).<sup>12</sup>

<sup>12</sup>It is also possible to prove an upper bound on the number of training iterations required to find the

996 So while the perceptron may seem heuristic, it is guaranteed to succeed, if the learning  
 997 problem is easy enough.

998 How useful is this proof? Minsky and Papert (1969) famously proved that the simple  
 999 logical function of *exclusive-or* is not separable, and that a perceptron is therefore inca-  
 1000 pable of learning this function. But this is not just an issue for the perceptron: any linear  
 1001 classification algorithm, including Naïve Bayes, will fail on this task. In natural language  
 1002 classification problems usually involve high dimensional feature spaces, with thousands  
 1003 or millions of features. For these problems, it is very likely that the training data is indeed  
 1004 separable. And even if the data is not separable, it is still possible to place an upper bound  
 1005 on the number of errors that the perceptron algorithm will make (Freund and Schapire,  
 1006 1999).

### 1007 2.2.2 Averaged perceptron

1008 The perceptron iterates over the data repeatedly — until “tired”, as described in Algo-  
 1009 rithm 3. If the data is linearly separable, the perceptron will eventually find a separator,  
 1010 and we can stop once all training instances are classified correctly. But if the data is not  
 1011 linearly separable, the perceptron can *thrash* between two or more weight settings, never  
 1012 converging. In this case, how do we know that we can stop training, and how should  
 1013 we choose the final weights? An effective practical solution is to *average* the perceptron  
 1014 weights across all iterations.

1015 This procedure is shown in Algorithm 4. The learning algorithm is nearly identical,  
 1016 but we also maintain a vector of the sum of the weights,  $\mathbf{m}$ . At the end of the learning  
 1017 procedure, we divide this sum by the total number of updates  $t$ , to compute the average  
 1018 weights,  $\boldsymbol{\theta}$ . These average weights are then used for prediction. In the algorithm sketch,  
 1019 the average is computed from a running sum,  $\mathbf{m} \leftarrow \mathbf{m} + \boldsymbol{\theta}$ . However, this is inefficient,  
 1020 because it requires  $|\boldsymbol{\theta}|$  operations to update the running sum. When  $f(\mathbf{x}, y)$  is sparse,  
 1021  $|\boldsymbol{\theta}| \gg |f(\mathbf{x}, y)|$  for any individual  $(\mathbf{x}, y)$ . This means that computing the running sum will  
 1022 be much more expensive than computing of the update to  $\boldsymbol{\theta}$  itself, which requires only  
 1023  $2 \times |f(\mathbf{x}, y)|$  operations. One of the exercises is to sketch a more efficient algorithm for  
 1024 computing the averaged weights.

1025 Even if the data is not separable, the averaged weights will eventually converge. One  
 1026 possible stopping criterion is to check the difference between the average weight vectors  
 1027 after each pass through the data: if the norm of the difference falls below some predefined  
 1028 threshold, we can stop training. Another stopping criterion is to hold out some data,  
 1029 and to measure the predictive accuracy on this heldout data. When the accuracy on the  
 1030 heldout data starts to decrease, the learning algorithm has begun to **overfit** the training  
 1031 set. At this point, it is probably best to stop; this stopping criterion is known as **early  
 1032 stopping**.

---

separator. Proofs like this are part of the field of **statistical learning theory** (Mohri et al., 2012).

**Algorithm 4** Averaged perceptron learning algorithm

---

```

1: procedure AVG-PERCEPTRON( $\mathbf{x}^{(1:N)}, \mathbf{y}^{(1:N)}$ )
2:    $t \leftarrow 0$ 
3:    $\boldsymbol{\theta}^{(0)} \leftarrow 0$ 
4:   repeat
5:      $t \leftarrow t + 1$ 
6:     Select an instance  $i$ 
7:      $\hat{y} \leftarrow \operatorname{argmax}_y \boldsymbol{\theta}^{(t-1)} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y)$ 
8:     if  $\hat{y} \neq y^{(i)}$  then
9:        $\boldsymbol{\theta}^{(t)} \leftarrow \boldsymbol{\theta}^{(t-1)} + \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) - \mathbf{f}(\mathbf{x}^{(i)}, \hat{y})$ 
10:    else
11:       $\boldsymbol{\theta}^{(t)} \leftarrow \boldsymbol{\theta}^{(t-1)}$ 
12:     $\mathbf{m} \leftarrow \mathbf{m} + \boldsymbol{\theta}^{(t)}$ 
13:   until tired
14:    $\bar{\boldsymbol{\theta}} \leftarrow \frac{1}{t} \mathbf{m}$ 
15:   return  $\bar{\boldsymbol{\theta}}$ 

```

---

1033     **Generalization** is the ability to make good predictions on instances that are not in  
 1034     the training data. Averaging can be proven to improve generalization, by computing an  
 1035     upper bound on the generalization error (Freund and Schapire, 1999; Collins, 2002).

1036 **2.3 Loss functions and large-margin classification**

1037 Naïve Bayes chooses the weights  $\boldsymbol{\theta}$  by maximizing the joint log-likelihood  $\log p(\mathbf{x}^{(1:N)}, \mathbf{y}^{(1:N)})$ .  
 1038 By convention, optimization problems are generally formulated as minimization of a **loss**  
 1039 **function**. The input to a loss function is the vector of weights  $\boldsymbol{\theta}$ , and the output is a non-  
 1040 negative scalar, measuring the performance of the classifier on a training instance. The  
 1041 loss  $\ell(\boldsymbol{\theta}; \mathbf{x}^{(i)}, y^{(i)})$  is then a measure of the performance of the weights  $\boldsymbol{\theta}$  on the instance  
 1042  $(\mathbf{x}^{(i)}, y^{(i)})$ . The goal of learning is to minimize the sum of the losses across all instances in  
 1043 the training set.

We can trivially reformulate maximum likelihood as a loss function, by defining the

loss function to be the *negative log-likelihood*:

$$\log p(\mathbf{x}^{(1:N)}, y^{(1:N)}; \boldsymbol{\theta}) = \sum_{i=1}^N \log p(\mathbf{x}^{(i)}, y^{(i)}; \boldsymbol{\theta}) \quad [2.36]$$

$$\ell_{\text{NB}}(\boldsymbol{\theta}; \mathbf{x}^{(i)}, y^{(i)}) = -\log p(\mathbf{x}^{(i)}, y^{(i)}; \boldsymbol{\theta}) \quad [2.37]$$

$$\hat{\boldsymbol{\theta}} = \operatorname{argmin}_{\boldsymbol{\theta}} \sum_{i=1}^N \ell_{\text{NB}}(\boldsymbol{\theta}; \mathbf{x}^{(i)}, y^{(i)}) \quad [2.38]$$

$$= \operatorname{argmax}_{\boldsymbol{\theta}} \sum_{i=1}^N \log p(\mathbf{x}^{(i)}, y^{(i)}; \boldsymbol{\theta}). \quad [2.39]$$

1044 The problem of minimizing  $\ell_{\text{NB}}$  is thus identical to the problem of maximum-likelihood  
1045 estimation.

1046 Loss functions provide a general framework for comparing machine learning objec-  
1047 tives. For example, an alternative loss function is the **zero-one loss**,

$$\ell_{0-1}(\boldsymbol{\theta}; \mathbf{x}^{(i)}, y^{(i)}) = \begin{cases} 0, & y^{(i)} = \operatorname{argmax}_y \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y) \\ 1, & \text{otherwise} \end{cases} \quad [2.40]$$

1048 The zero-one loss is zero if the instance is correctly classified, and one otherwise. The  
1049 sum of zero-one losses is proportional to the error rate of the classifier on the training  
1050 data. Since a low error rate is often the ultimate goal of classification, this may seem  
1051 ideal. But the zero-one loss has several problems. One is that it is **non-convex**,<sup>13</sup> which  
1052 means that there is no guarantee that gradient-based optimization will be effective. A  
1053 more serious problem is that the derivatives are useless: the partial derivative with respect  
1054 to any parameter is zero everywhere, except at the points where  $\boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y) = \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, \hat{y})$   
1055 for some  $\hat{y}$ . At those points, the loss is discontinuous, and the derivative is undefined.

1056 The perceptron optimizes the following loss function:

$$\ell_{\text{PERCEPTRON}}(\boldsymbol{\theta}; \mathbf{x}^{(i)}, y^{(i)}) = \max_{y \in \mathcal{Y}} \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y) - \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}), \quad [2.41]$$

1057 When  $\hat{y} = y^{(i)}$ , the loss is zero; otherwise, it increases linearly with the gap between the  
1058 score for the predicted label  $\hat{y}$  and the score for the true label  $y^{(i)}$ . Plotting this loss against  
1059 the input  $\max_{y \in \mathcal{Y}} \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y) - \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)})$  gives a hinge shape, motivating the name  
1060 **hinge loss**.

---

<sup>13</sup>A function  $f$  is **convex** iff  $\alpha f(x_i) + (1-\alpha)f(x_j) \geq f(\alpha x_i + (1-\alpha)x_j)$ , for all  $\alpha \in [0, 1]$  and for all  $x_i$  and  $x_j$  on the domain of the function. In words, any weighted average of the output of  $f$  applied to any two points is larger than the output of  $f$  when applied to the weighted average of the same two points. Convexity implies that any local minimum is also a global minimum, and there are many effective techniques for optimizing convex functions (Boyd and Vandenberghe, 2004). See Appendix B for a brief review.

1061 To see why this is the loss function optimized by the perceptron, take the derivative  
 1062 with respect to  $\theta$ ,

$$\frac{\partial}{\partial \theta} \ell_{\text{PERCEPTRON}}(\theta; \mathbf{x}^{(i)}, y^{(i)}) = \mathbf{f}(\mathbf{x}^{(i)}, \hat{y}) - \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}). \quad [2.42]$$

1063 At each instance perceptron algorithm takes a step of magnitude one in the opposite direction  
 1064 of this **gradient**,  $\nabla_{\theta} \ell_{\text{PERCEPTRON}} = \frac{\partial}{\partial \theta} \ell_{\text{PERCEPTRON}}(\theta; \mathbf{x}^{(i)}, y^{(i)})$ . As we will see in § 2.5,  
 1065 this is an example of the optimization algorithm **stochastic gradient descent**, applied to  
 1066 the objective in Equation 2.41.

1067 **Breaking ties with subgradient descent** Careful readers will notice the tacit assumption  
 1068 that there is a unique  $\hat{y}$  that maximizes  $\theta \cdot \mathbf{f}(\mathbf{x}^{(i)}, y)$ . What if there are two or more labels  
 1069 that maximize this function? Consider binary classification: if the maximizer is  $y^{(i)}$ , then  
 1070 the gradient is zero, and so is the perceptron update; if the maximizer is  $\hat{y} \neq y^{(i)}$ , then the  
 1071 update is the difference  $\mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) - \mathbf{f}(\mathbf{x}^{(i)}, \hat{y})$ . The underlying issue is that the perceptron  
 1072 loss is not **smooth**, because the first derivative has a discontinuity at the hinge point,  
 1073 where the score for the true label  $y^{(i)}$  is equal to the score for some other label  $\hat{y}$ . At this  
 1074 point, there is no unique gradient; rather, there is a set of **subgradients**. A vector  $v$  is a  
 1075 subgradient of the function  $g$  at  $u_0$  iff  $g(u) - g(u_0) \geq v \cdot (u - u_0)$  for all  $u$ . Graphically,  
 1076 this defines the set of hyperplanes that include  $g(u_0)$  and do not intersect  $g$  at any other  
 1077 point. As we approach the hinge point from the left, the gradient is  $\mathbf{f}(\mathbf{x}, \hat{y}) - \mathbf{f}(\mathbf{x}, y)$ ; as we  
 1078 approach from the right, the gradient is 0. At the hinge point, the subgradients include all  
 1079 vectors that are bounded by these two extremes. In subgradient descent, *any* subgradient  
 1080 can be used (Bertsekas, 2012). Since both 0 and  $\mathbf{f}(\mathbf{x}, \hat{y}) - \mathbf{f}(\mathbf{x}, y)$  are subgradients at the  
 1081 hinge point, either one can be used in the perceptron update.

1082 **Perceptron versus Naïve Bayes** The perceptron loss function has some pros and cons  
 1083 with respect to the negative log-likelihood loss implied by Naïve Bayes.

- 1084 • Both  $\ell_{\text{NB}}$  and  $\ell_{\text{PERCEPTRON}}$  are convex, making them relatively easy to optimize. How-  
 1085 ever,  $\ell_{\text{NB}}$  can be optimized in closed form, while  $\ell_{\text{PERCEPTRON}}$  requires iterating over  
 1086 the dataset multiple times.
- 1087 •  $\ell_{\text{NB}}$  can suffer **infinite** loss on a single example, since the logarithm of zero probabil-  
 1088 ity is negative infinity. Naïve Bayes will therefore overemphasize some examples,  
 1089 and underemphasize others.
- 1090 •  $\ell_{\text{PERCEPTRON}}$  treats all correct answers equally. Even if  $\theta$  only gives the correct answer  
 1091 by a tiny margin, the loss is still zero.

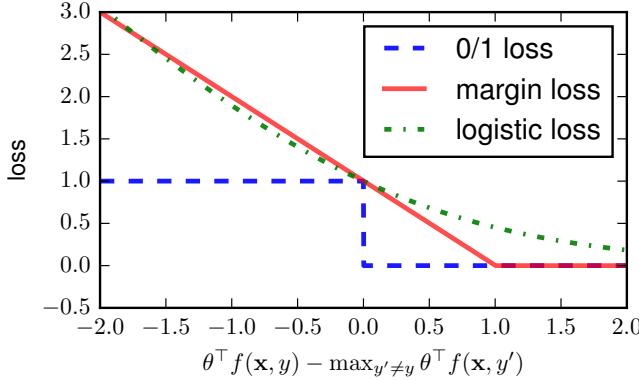


Figure 2.2: Margin, zero-one, and logistic loss functions.

1092 **2.3.1 Large margin classification**

1093 This last comment suggests a potential problem with the perceptron. Suppose a test ex-  
 1094 ample is very close to a training example, but not identical. If the classifier only gets the  
 1095 correct answer on the training example by a small margin, then it may get the test instance  
 1096 wrong. To formalize this intuition, define the **margin** as,

$$\gamma(\boldsymbol{\theta}; \mathbf{x}^{(i)}, y^{(i)}) = \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) - \max_{y \neq y^{(i)}} \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y). \quad [2.43]$$

The margin represents the difference between the score for the correct label  $y^{(i)}$ , and the score for the highest-scoring label. The intuition behind **large margin classification** is that it is not enough just to label the training data correctly — the correct label should be separated from other labels by a comfortable margin. This idea can be encoded into a loss function,

$$\ell_{\text{MARGIN}}(\boldsymbol{\theta}; \mathbf{x}^{(i)}, y^{(i)}) = \begin{cases} 0, & \gamma(\boldsymbol{\theta}; \mathbf{x}^{(i)}, y^{(i)}) \geq 1, \\ 1 - \gamma(\boldsymbol{\theta}; \mathbf{x}^{(i)}, y^{(i)}), & \text{otherwise} \end{cases} \quad [2.44]$$

$$= (1 - \gamma(\boldsymbol{\theta}; \mathbf{x}^{(i)}, y^{(i)}))_+, \quad [2.45]$$

1097 where  $(x)_+ = \max(0, x)$ . The loss is zero if there is a margin of at least 1 between the  
 1098 score for the true label and the best-scoring alternative  $\hat{y}$ . This is almost identical to the  
 1099 perceptron loss, but the hinge point is shifted to the right, as shown in Figure 2.2. The  
 1100 margin loss is a convex upper bound on the zero-one loss.

1101 **2.3.2 Support vector machines**

If a dataset is linearly separable, then there is some hyperplane  $\theta$  that correctly classifies all training instances with margin  $\rho$  (by Definition 1). This margin can be increased to any desired value by multiplying the weights by a constant. Now, for any datapoint  $(x^{(i)}, y^{(i)})$ , the geometric distance to the separating hyperplane is given by  $\frac{\gamma(\theta; x^{(i)}, y^{(i)})}{\|\theta\|_2}$ ,

where the denominator is the norm of the weights,  $\|\theta\|_2 = \sqrt{\sum_j \theta_j^2}$ . The geometric distance is sometimes called the **geometric margin**, in contrast to the **functional margin**  $\gamma(\theta; x^{(i)}, y^{(i)})$ . Both are shown in Figure 2.3. The geometric margin is a good measure of the robustness of the separator: if the functional margin is large, but the norm  $\|\theta\|_2$  is also large, then a small change in  $x^{(i)}$  could cause it to be misclassified. We therefore seek to maximize the minimum geometric margin, subject to the constraint that the functional margin is at least one:

$$\begin{aligned} \max_{\theta} . & \quad \min_i . & & \frac{\gamma(\theta; x^{(i)}, y^{(i)})}{\|\theta\|_2} \\ \text{s.t.} & \quad \gamma(\theta; x^{(i)}, y^{(i)}) \geq 1, \quad \forall i. & & [2.46] \end{aligned}$$

1102 This is a **constrained optimization** problem, where the second line describes constraints  
 1103 on the space of possible solutions  $\theta$ . In this case, the constraint is that the functional  
 1104 margin always be at least one, and the objective is that the minimum geometric margin  
 1105 be as large as possible.

Any scaling factor on  $\theta$  will cancel in the numerator and denominator of the geometric margin. This means that if the data is linearly separable at  $\rho$ , we can increase this margin to 1 by rescaling  $\theta$ . We therefore need only minimize the denominator  $\|\theta\|_2$ , subject to the constraint on the functional margin. The minimizer of  $\|\theta\|_2$  is also the minimizer of  $\frac{1}{2}\|\theta\|_2^2 = \frac{1}{2}\sum_{j=1}^V \theta_j^2$ , which is easier to work with. This gives the optimization problem,

$$\begin{aligned} \min_{\theta} . & \quad \frac{1}{2}\|\theta\|_2^2 \\ \text{s.t.} & \quad \gamma(\theta; x^{(i)}, y^{(i)}) \geq 1, \quad \forall i. & & [2.47] \end{aligned}$$

1106 This optimization problem is a **quadratic program**: the objective is a quadratic function  
 1107 of the parameters, and the constraints are all linear inequalities. The resulting classifier  
 1108 is better known as the **support vector machine**. The name derives from one of the  
 1109 solutions, which is to incorporate the constraints through Lagrange multipliers  $\alpha_i \geq 0, i =$   
 1110  $1, 2, \dots, N$ . The instances for which  $\alpha_i > 0$  are the **support vectors**; other instances are  
 1111 irrelevant to the classification boundary.



Figure 2.3: Functional and geometric margins for a binary classification problem. All separators that satisfy the margin constraint are shown. The separator with the largest geometric margin is shown in bold.

### 1112 2.3.3 Slack variables

If a dataset is not linearly separable, then there is no  $\theta$  that satisfies the margin constraint. To add more flexibility, we introduce a set of **slack variables**  $\xi_i \geq 0$ . Instead of requiring that the functional margin be greater than or equal to one, we require that it be greater than or equal to  $1 - \xi_i$ . Ideally there would not be any slack, so the slack variables are penalized in the objective function:

$$\begin{aligned} \min_{\theta, \xi} \quad & \frac{1}{2} \|\theta\|_2^2 + C \sum_{i=1}^N \xi_i \\ \text{s.t.} \quad & \gamma(\theta; \mathbf{x}^{(i)}, y^{(i)}) + \xi_i \geq 1, \quad \forall i \\ & \xi_i \geq 0, \quad \forall i. \end{aligned} \quad [2.48]$$

1113 The hyperparameter  $C$  controls the tradeoff between violations of the margin con-  
 1114 straint and the preference for a low norm of  $\theta$ . As  $C \rightarrow \infty$ , slack is infinitely expensive,  
 1115 and there is only a solution if the data is separable. As  $C \rightarrow 0$ , slack becomes free, and  
 1116 there is a trivial solution at  $\theta = 0$ . Thus,  $C$  plays a similar role to the smoothing parame-  
 1117 ter in Naïve Bayes (§ 2.1.4), trading off between a close fit to the training data and better  
 1118 generalization. Like the smoothing parameter of Naïve Bayes,  $C$  must be set by the user,  
 1119 typically by maximizing performance on a heldout development set.

1120 To solve the constrained optimization problem defined in Equation 2.48, we can first

1121 solve for the slack variables,

$$\xi_i \geq (1 - \gamma(\boldsymbol{\theta}; \mathbf{x}^{(i)}, y^{(i)}))_+. \quad [2.49]$$

The inequality is tight, because the slack variables are penalized in the objective, and there is no advantage to increasing them beyond the minimum value (Ratliff et al., 2007; Smith, 2011). The problem can therefore be transformed into the unconstrained optimization,

$$\min_{\boldsymbol{\theta}} \quad \frac{\lambda}{2} \|\boldsymbol{\theta}\|_2^2 + \sum_{i=1}^N (1 - \gamma(\boldsymbol{\theta}; \mathbf{x}^{(i)}, y^{(i)}))_+, \quad [2.50]$$

1122 where each  $\xi_i$  has been substituted by the right-hand side of Equation 2.49, and the factor  
 1123 of  $C$  on the slack variables has been replaced by an equivalent factor of  $\lambda = \frac{1}{C}$  on the  
 1124 norm of the weights.

1125 Now define the **cost** of a classification error as,<sup>14</sup>

$$c(y^{(i)}, \hat{y}) = \begin{cases} 1, & y^{(i)} \neq \hat{y} \\ 0, & \text{otherwise.} \end{cases} \quad [2.51]$$

Equation 2.50 can be rewritten using this cost function,

$$\min_{\boldsymbol{\theta}} \quad \frac{\lambda}{2} \|\boldsymbol{\theta}\|_2^2 + \sum_{i=1}^N \left( \max_{y \in \mathcal{Y}} (\boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y) + c(y^{(i)}, y)) - \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) \right)_+. \quad [2.52]$$

1126 This objective maximizes over all  $y \in \mathcal{Y}$ , in search of labels that are both *strong*, as mea-  
 1127 sured by  $\boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y)$ , and *wrong*, as measured by  $c(y^{(i)}, y)$ . This maximization is known  
 1128 as **cost-augmented decoding**, because it augments the maximization objective to favor  
 1129 high-cost predictions. If the highest-scoring label is  $y = y^{(i)}$ , then the margin constraint is  
 1130 satisfied, and the loss for this instance is zero. Cost-augmentation is only for learning: it  
 1131 is not applied when making predictions on unseen data.

Differentiating Equation 2.52 with respect to the weights gives,

$$\nabla_{\boldsymbol{\theta}} L_{\text{SVM}} = \lambda \boldsymbol{\theta} + \sum_{i=1}^N \mathbf{f}(\mathbf{x}^{(i)}, \hat{y}) - \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) \quad [2.53]$$

$$\hat{y} = \operatorname{argmax}_{y \in \mathcal{Y}} \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y) + c(y^{(i)}, y), \quad [2.54]$$

1132 where  $L_{\text{SVM}}$  refers to minimization objective in Equation 2.52. This gradient is very similar  
 1133 to the perceptron update. One difference is the additional term  $\lambda \boldsymbol{\theta}$ , which **regularizes** the

---

<sup>14</sup>We can also define specialized cost functions that heavily penalize especially undesirable errors (Tsacharidis et al., 2004). This idea is revisited in chapter 7.

1134 weights towards 0. The other difference is the cost  $c(y^{(i)}, y)$ , which is added to  $\theta \cdot \mathbf{f}(\mathbf{x}, y)$   
 1135 when choosing  $\hat{y}$  during training. This term derives from the margin constraint: large  
 1136 margin classifiers learn not only from instances that are incorrectly classified, but also  
 1137 from instances for which the correct classification decision was not sufficiently confident.

## 1138 2.4 Logistic regression

1139 Thus far, we have seen two broad classes of learning algorithms. Naïve Bayes is a prob-  
 1140 abilistic method, where learning is equivalent to estimating a joint probability distribu-  
 1141 tion. The perceptron and support vector machine are discriminative, error-driven algo-  
 1142 rithms: the learning objective is closely related to the number of errors on the training  
 1143 data. Probabilistic and error-driven approaches each have advantages: probability makes  
 1144 it possible to quantify uncertainty about the predicted labels, but the probability model of  
 1145 Naïve Bayes makes unrealistic independence assumptions that limit the features that can  
 1146 be used.

**Logistic regression** combines advantages of discriminative and probabilistic classi-  
 fiers. Unlike Naïve Bayes, which starts from the **joint probability**  $p_{X,Y}$ , logistic regression  
 defines the desired **conditional probability**  $p_{Y|X}$  directly. Think of  $\theta \cdot \mathbf{f}(\mathbf{x}, y)$  as a scoring  
 function for the compatibility of the base features  $\mathbf{x}$  and the label  $y$ . To convert this score  
 into a probability, we first exponentiate, obtaining  $\exp(\theta \cdot \mathbf{f}(\mathbf{x}, y))$ , which is guaranteed  
 to be non-negative. Next, we normalize, dividing over all possible labels  $y' \in \mathcal{Y}$ . The  
 resulting conditional probability is defined as,

$$p(y | \mathbf{x}; \theta) = \frac{\exp(\theta \cdot \mathbf{f}(\mathbf{x}, y))}{\sum_{y' \in \mathcal{Y}} \exp(\theta \cdot \mathbf{f}(\mathbf{x}, y'))}. \quad [2.55]$$

Given a dataset  $\mathcal{D} = \{(\mathbf{x}^{(i)}, y^{(i)})\}_{i=1}^N$ , the weights  $\theta$  are estimated by **maximum conditional likelihood**,

$$\log p(\mathbf{y}^{(1:N)} | \mathbf{x}^{(1:N)}; \theta) = \sum_{i=1}^N \log p(y^{(i)} | \mathbf{x}^{(i)}; \theta) \quad [2.56]$$

$$= \sum_{i=1}^N \theta \cdot \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) - \log \sum_{y' \in \mathcal{Y}} \exp(\theta \cdot \mathbf{f}(\mathbf{x}^{(i)}, y')). \quad [2.57]$$

1147 The final line is obtained by plugging in Equation 2.55 and taking the logarithm.<sup>15</sup> Inside

---

<sup>15</sup>The log-sum-exp term is a common pattern in machine learning. It is numerically unstable, because it will underflow if the inner product is small, and overflow if the inner product is large. Scientific computing libraries usually contain special functions for computing `logsumexp`, but with some thought, you should be able to see how to create an implementation that is numerically stable.

1148 the sum, we have the (additive inverse of the) **logistic loss**,

$$\ell_{\text{LOGREG}}(\boldsymbol{\theta}; \mathbf{x}^{(i)}, y^{(i)}) = -\boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) + \log \sum_{y' \in \mathcal{Y}} \exp(\boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y')) \quad [2.58]$$

1149 The logistic loss is shown in Figure 2.2. A key difference from the zero-one and hinge  
 1150 losses is that logistic loss is never zero. This means that the objective function can always  
 1151 be improved by assigning higher confidence to the correct label.

### 1152 2.4.1 Regularization

1153 As with the support vector machine, better generalization can be obtained by penalizing  
 1154 the norm of  $\boldsymbol{\theta}$ . This is done by adding a term of  $\frac{\lambda}{2} \|\boldsymbol{\theta}\|_2^2$  to the minimization objective.  
 1155 This is called  $L_2$  regularization, because  $\|\boldsymbol{\theta}\|_2^2$  is the squared  $L_2$  norm of the vector  $\boldsymbol{\theta}$ .  
 1156 Regularization forces the estimator to trade off performance on the training data against  
 1157 the norm of the weights, and this can help to prevent overfitting. Consider what would  
 1158 happen to the unregularized weight for a base feature  $j$  that is active in only one instance  
 1159  $\mathbf{x}^{(i)}$ : the conditional log-likelihood could always be improved by increasing the weight  
 1160 for this feature, so that  $\boldsymbol{\theta}_{(j,y^{(i)})} \rightarrow \infty$  and  $\boldsymbol{\theta}_{(j,\tilde{y} \neq y^{(i)})} \rightarrow -\infty$ , where  $(j, y)$  is the index of  
 1161 feature associated with  $x_j^{(i)}$  and label  $y$  in  $\mathbf{f}(\mathbf{x}^{(i)}, y)$ .

In § 2.1.4, we saw that smoothing the probabilities of a Naïve Bayes classifier can be justified in a hierarchical probabilistic model, in which the parameters of the classifier are themselves random variables, drawn from a prior distribution. The same justification applies to  $L_2$  regularization. In this case, the prior is a zero-mean Gaussian on each term of  $\boldsymbol{\theta}$ . The log-likelihood under a zero-mean Gaussian is,

$$\log N(\theta_j; 0, \sigma^2) \propto -\frac{1}{2\sigma^2} \theta_j^2, \quad [2.59]$$

1162 so that the regularization weight  $\lambda$  is equal to the inverse variance of the prior,  $\lambda = \frac{1}{\sigma^2}$ .

1163 **2.4.2 Gradients**

Logistic loss is minimized by optimization along the gradient. Here is the gradient with respect to the logistic loss on a single example,

$$\ell_{\text{LOGREG}} = -\boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) + \log \sum_{y' \in \mathcal{Y}} \exp(\boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y')) \quad [2.60]$$

$$\frac{\partial \ell}{\partial \boldsymbol{\theta}} = -\mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) + \frac{1}{\sum_{y'' \in \mathcal{Y}} \exp(\boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y''))} \times \sum_{y' \in \mathcal{Y}} \exp(\boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y')) \times \mathbf{f}(\mathbf{x}^{(i)}, y') \quad [2.61]$$

$$= -\mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) + \sum_{y' \in \mathcal{Y}} \frac{\exp(\boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y'))}{\sum_{y'' \in \mathcal{Y}} \exp(\boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y''))} \times \mathbf{f}(\mathbf{x}^{(i)}, y') \quad [2.62]$$

$$= -\mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) + \sum_{y' \in \mathcal{Y}} p(y' | \mathbf{x}^{(i)}; \boldsymbol{\theta}) \times \mathbf{f}(\mathbf{x}^{(i)}, y') \quad [2.63]$$

$$= -\mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) + E_{Y|X}[\mathbf{f}(\mathbf{x}^{(i)}, y)]. \quad [2.64]$$

1164 The final step employs the definition of a conditional expectation (§ A.5). The gradient of  
 1165 the logistic loss is equal to the difference between the expected counts under the current  
 1166 model,  $E_{Y|X}[\mathbf{f}(\mathbf{x}^{(i)}, y)]$ , and the observed feature counts  $\mathbf{f}(\mathbf{x}^{(i)}, y^{(i)})$ . When these two  
 1167 vectors are equal for a single instance, there is nothing more to learn from it; when they  
 1168 are equal in sum over the entire dataset, there is nothing more to learn from the dataset as  
 1169 a whole. The gradient of the hinge loss is nearly identical, but it involves the features of  
 1170 the predicted label under the current model,  $\mathbf{f}(\mathbf{x}^{(i)}, \hat{y})$ , rather than the expected features  
 1171  $E_{Y|X}[\mathbf{f}(\mathbf{x}^{(i)}, y)]$  under the conditional distribution  $p(y | \mathbf{x}; \boldsymbol{\theta})$ .

The regularizer contributes  $\lambda \boldsymbol{\theta}$  to the overall gradient:

$$L_{\text{LOGREG}} = \frac{\lambda}{2} \|\boldsymbol{\theta}\|_2^2 - \sum_{i=1}^N \left( \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) - \log \sum_{y' \in \mathcal{Y}} \exp \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y') \right) \quad [2.65]$$

$$\nabla_{\boldsymbol{\theta}} L_{\text{LOGREG}} = \lambda \boldsymbol{\theta} - \sum_{i=1}^N \left( \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) - E_{y|\mathbf{x}}[\mathbf{f}(\mathbf{x}^{(i)}, y)] \right). \quad [2.66]$$

1172 **2.5 Optimization**

1173 Each of the classification algorithms in this chapter can be viewed as an optimization  
 1174 problem:

- 1175 • In Naïve Bayes, the objective is the joint likelihood  $\log p(\mathbf{x}^{(1:N)}, \mathbf{y}^{(1:N)})$ . Maximum  
 1176 likelihood estimation yields a closed-form solution for  $\boldsymbol{\theta}$ .

- 1177 • In the support vector machine, the objective is the regularized margin loss,

$$L_{\text{SVM}} = \frac{\lambda}{2} \|\boldsymbol{\theta}\|_2^2 + \sum_{i=1}^N (\max_{y \in \mathcal{Y}} (\boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y) + c(y^{(i)}, y)) - \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}))_+, \quad [2.67]$$

1178 There is no closed-form solution, but the objective is convex. The perceptron algo-  
1179 rithm minimizes a similar objective.

- 1180 • In logistic regression, the objective is the regularized negative log-likelihood,

$$L_{\text{LOGREG}} = \frac{\lambda}{2} \|\boldsymbol{\theta}\|_2^2 - \sum_{i=1}^N \left( \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) - \log \sum_{y \in \mathcal{Y}} \exp(\boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y)) \right) \quad [2.68]$$

1181 Again, there is no closed-form solution, but the objective is convex.

1182 These learning algorithms are distinguished by *what* is being optimized, rather than  
1183 *how* the optimal weights are found. This decomposition is an essential feature of con-  
1184 temporary machine learning. The domain expert's job is to design an objective function  
1185 — or more generally, a **model** of the problem. If the model has certain characteristics,  
1186 then generic optimization algorithms can be used to find the solution. In particular, if an  
1187 objective function is differentiable, then gradient-based optimization can be employed;  
1188 if it is also convex, then gradient-based optimization is guaranteed to find the globally  
1189 optimal solution. The support vector machine and logistic regression have both of these  
1190 properties, and so are amenable to generic **convex optimization** techniques (Boyd and  
1191 Vandenberghe, 2004).

### 1192 2.5.1 Batch optimization

In **batch optimization**, each update to the weights is based on a computation involving the entire dataset. One such algorithm is **gradient descent**, which iteratively updates the weights,

$$\boldsymbol{\theta}^{(t+1)} \leftarrow \boldsymbol{\theta}^{(t)} - \eta^{(t)} \nabla_{\boldsymbol{\theta}} L, \quad [2.69]$$

1193 where  $\nabla_{\boldsymbol{\theta}} L$  is the gradient computed over the entire training set, and  $\eta^{(t)}$  is the **step size**  
1194 at iteration  $t$ . If the objective  $L$  is a convex function of  $\boldsymbol{\theta}$ , then this procedure is guaranteed  
1195 to terminate at the global optimum, for appropriate schedule of learning rates,  $\eta^{(t)}$ .<sup>16</sup>

---

<sup>16</sup>Specifically, the learning rate must have the following properties (Bottou et al., 2016):

$$\sum_{t=1}^{\infty} \eta^{(t)} = \infty \quad [2.70]$$

$$\sum_{t=1}^{\infty} (\eta^{(t)})^2 < \infty. \quad [2.71]$$

1196 In practice, gradient descent can be slow to converge, as the gradient can become  
 1197 infinitesimally small. Faster convergence can be obtained by second-order Newton opti-  
 1198 mization, which incorporates the inverse of the **Hessian matrix**,

$$H_{i,j} = \frac{\partial^2 L}{\partial \theta_i \partial \theta_j} \quad [2.72]$$

1199 The size of the Hessian matrix is quadratic in the number of features. In the bag-of-words  
 1200 representation, this is usually too big to store, let alone invert. **Quasi-Network optimiza-**  
 1201 **tion** techniques maintain a low-rank approximation to the inverse of the Hessian matrix.  
 1202 Such techniques usually converge more quickly than gradient descent, while remaining  
 1203 computationally tractable even for large feature sets. A popular quasi-Newton algorithm  
 1204 is **L-BFGS** (Liu and Nocedal, 1989), which is implemented in many scientific computing  
 1205 environments, such as `scipy` and `Matlab`.

1206 For any gradient-based technique, the user must set the learning rates  $\eta^{(t)}$ . While con-  
 1207 vergence proofs usually employ a decreasing learning rate, in practice, it is common to fix  
 1208  $\eta^{(t)}$  to a small constant, like  $10^{-3}$ . The specific constant can be chosen by experimentation,  
 1209 although there is research on determining the learning rate automatically (Schaul et al.,  
 1210 2013; Wu et al., 2018).

### 1211 2.5.2 Online optimization

1212 Batch optimization computes the objective on the entire training set before making an up-  
 1213 date. This may be inefficient, because at early stages of training, a small number of train-  
 1214 ing examples could point the learner in the correct direction. **Online learning** algorithms  
 1215 make updates to the weights while iterating through the training data. The theoretical  
 1216 basis for this approach is a stochastic approximation to the true objective function,

$$\sum_{i=1}^N \ell(\boldsymbol{\theta}; \mathbf{x}^{(i)}, y^{(i)}) \approx N \times \ell(\boldsymbol{\theta}; \mathbf{x}^{(j)}, y^{(j)}), \quad (\mathbf{x}^{(j)}, y^{(j)}) \sim \{(\mathbf{x}^{(i)}, y^{(i)})\}_{i=1}^N, \quad [2.73]$$

1217 where the instance  $(\mathbf{x}^{(j)}, y^{(j)})$  is sampled at random from the full dataset.

1218 In **stochastic gradient descent**, the approximate gradient is computed by randomly  
 1219 sampling a single instance, and an update is made immediately. This is similar to the  
 1220 perceptron algorithm, which also updates the weights one instance at a time. In **mini-**  
 1221 **batch** stochastic gradient descent, the gradient is computed over a small set of instances.  
 1222 A typical approach is to set the minibatch size so that the entire batch fits in memory on a  
 1223 graphics processing unit (GPU; Neubig et al., 2017). It is then possible to speed up learn-  
 1224 ing by parallelizing the computation of the gradient over each instance in the minibatch.

---

These properties can be obtained by the learning rate schedule  $\eta^{(t)} = \eta^{(0)} t^{-\alpha}$  for  $\alpha \in [1, 2]$ .

---

**Algorithm 5** Generalized gradient descent. The function BATCHER partitions the training set into  $B$  batches such that each instance appears in exactly one batch. In gradient descent,  $B = 1$ ; in stochastic gradient descent,  $B = N$ ; in minibatch stochastic gradient descent,  $1 < B < N$ .

---

```

1: procedure GRADIENT-DESCENT( $\mathbf{x}^{(1:N)}, \mathbf{y}^{(1:N)}, L, \eta^{(1:\infty)}$ , BATCHER,  $T_{\max}$ )
2:    $\boldsymbol{\theta} \leftarrow \mathbf{0}$ 
3:    $t \leftarrow 0$ 
4:   repeat
5:      $(\mathbf{b}^{(1)}, \mathbf{b}^{(2)}, \dots, \mathbf{b}^{(B)}) \leftarrow \text{BATCHER}(N)$ 
6:     for  $n \in \{1, 2, \dots, B\}$  do
7:        $t \leftarrow t + 1$ 
8:        $\boldsymbol{\theta}^{(t)} \leftarrow \boldsymbol{\theta}^{(t-1)} - \eta^{(t)} \nabla_{\boldsymbol{\theta}} L(\boldsymbol{\theta}^{(t-1)}; \mathbf{x}^{(b_1^{(n)}, b_2^{(n)}, \dots)}, \mathbf{y}^{(b_1^{(n)}, b_2^{(n)}, \dots)})$ 
9:       if Converged( $\boldsymbol{\theta}^{(1, 2, \dots, t)}$ ) then
10:        return  $\boldsymbol{\theta}^{(t)}$ 
11:   until  $t \geq T_{\max}$ 
12:   return  $\boldsymbol{\theta}^{(t)}$ 

```

---

1225     Algorithm 5 offers a generalized view of gradient descent. In standard gradient de-  
 1226     scendent, the batcher returns a single batch with all the instances. In stochastic gradient de-  
 1227     scent, it returns  $N$  batches with one instance each. In mini-batch settings, the batcher  
 1228     returns  $B$  minibatches,  $1 < B < N$ .

There are many other techniques for online learning, and the field is currently quite active (Bottou et al., 2016). Some algorithms use an adaptive step size, which can be different for every feature (Duchi et al., 2011). Features that occur frequently are likely to be updated frequently, so it is best to use a small step size; rare features will be updated infrequently, so it is better to take larger steps. The **AdaGrad** (adaptive gradient) algorithm achieves this behavior by storing the sum of the squares of the gradients for each feature, and rescaling the learning rate by its inverse:

$$\mathbf{g}_t = \nabla_{\boldsymbol{\theta}} L(\boldsymbol{\theta}^{(t)}; \mathbf{x}^{(i)}, y^{(i)}) \quad [2.74]$$

$$\theta_j^{(t+1)} \leftarrow \theta_j^{(t)} - \frac{\eta^{(t)}}{\sqrt{\sum_{t'=1}^t g_{t,j}^2}} g_{t,j}, \quad [2.75]$$

1229 where  $j$  iterates over features in  $\mathbf{f}(\mathbf{x}, y)$ .

1230     In most cases, the number of active features for any instance is much smaller than the  
 1231     number of weights. If so, the computation cost of online optimization will be dominated  
 1232     by the update from the regularization term,  $\lambda \boldsymbol{\theta}$ . The solution is to be “lazy”, updating  
 1233     each  $\theta_j$  only as it is used. To implement lazy updating, store an additional parameter  $\tau_j$ ,  
 1234     which is the iteration at which  $\theta_j$  was last updated. If  $\theta_j$  is needed at time  $t$ , the  $t - \tau$

1235 regularization updates can be performed all at once. This strategy is described in detail  
 1236 by Kummerfeld et al. (2015).

## 1237 2.6 \*Additional topics in classification

1238 Throughout this text, advanced topics will be marked with an asterisk.

### 1239 2.6.1 Feature selection by regularization

1240 In logistic regression and large-margin classification, generalization can be improved by  
 1241 regularizing the weights towards 0, using the  $L_2$  norm. But rather than encouraging  
 1242 weights to be small, it might be better for the model to be **sparse**: it should assign weights  
 1243 of exactly zero to most features, and only assign non-zero weights to features that are  
 1244 clearly necessary. This idea can be formalized by the  $L_0$  norm,  $L_0 = \|\theta\|_0 = \sum_j \delta(\theta_j \neq 0)$ ,  
 1245 which applies a constant penalty for each non-zero weight. This norm can be thought  
 1246 of as a form of **feature selection**: optimizing the  $L_0$ -regularized conditional likelihood is  
 1247 equivalent to trading off the log-likelihood against the number of active features. Reduc-  
 1248 ing the number of active features is desirable because the resulting model will be fast,  
 1249 low-memory, and should generalize well, since irrelevant features will be pruned away.  
 1250 Unfortunately, the  $L_0$  norm is non-convex and non-differentiable. Optimization under  $L_0$   
 1251 regularization is **NP-hard**, meaning that it can be solved efficiently only if P=NP (Ge et al.,  
 1252 2011).

1253 A useful alternative is the  $L_1$  norm, which is equal to the sum of the absolute values  
 1254 of the weights,  $\|\theta\|_1 = \sum_j |\theta_j|$ . The  $L_1$  norm is convex, and can be used as an approxima-  
 1255 tion to  $L_0$  (Tibshirani, 1996). Conveniently, the  $L_1$  norm also performs feature selection,  
 1256 by driving many of the coefficients to zero; it is therefore known as a **sparsity inducing**  
 1257 **regularizer**. The  $L_1$  norm does not have a gradient at  $\theta_j = 0$ , so we must instead optimize  
 1258 the  $L_1$ -regularized objective using **subgradient** methods. The associated stochastic sub-  
 1259 gradient descent algorithms are only somewhat more complex than conventional SGD;  
 1260 Sra et al. (2012) survey approaches for estimation under  $L_1$  and other regularizers.

1261 Gao et al. (2007) compare  $L_1$  and  $L_2$  regularization on a suite of NLP problems, finding  
 1262 that  $L_1$  regularization generally gives similar accuracy to  $L_2$  regularization, but that  $L_1$   
 1263 regularization produces models that are between ten and fifty times smaller, because more  
 1264 than 90% of the feature weights are set to zero.

### 1265 2.6.2 Other views of logistic regression

In binary classification, we can dispense with the feature function, and choose  $y$  based on  
 the inner product of  $\theta \cdot x$ . The conditional probability  $p_{Y|X}$  is obtained by passing this

inner product through a **logistic function**,

$$\sigma(a) \triangleq \frac{\exp(a)}{1 + \exp(a)} = (1 + \exp(-a))^{-1} \quad [2.76]$$

$$p(y | \mathbf{x}; \boldsymbol{\theta}) = \sigma(\boldsymbol{\theta} \cdot \mathbf{x}). \quad [2.77]$$

1266 This is the origin of the name **logistic regression**. Logistic regression can be viewed as  
 1267 part of a larger family of **generalized linear models** (GLMs), in which various other “link  
 1268 functions” convert between the inner product  $\boldsymbol{\theta} \cdot \mathbf{x}$  and the parameter of a conditional  
 1269 probability distribution.

1270 In the early NLP literature, logistic regression is frequently called **maximum entropy**  
 1271 classification (Berger et al., 1996). This name refers to an alternative formulation, in  
 1272 which the goal is to find the maximum entropy probability function that satisfies **moment-**  
 1273 **matching** constraints. These constraints specify that the empirical counts of each feature  
 1274 should match the expected counts under the induced probability distribution  $p_{Y|X;\boldsymbol{\theta}}$ .

$$\sum_{i=1}^N f_j(\mathbf{x}^{(i)}, y^{(i)}) = \sum_{i=1}^N \sum_{y \in \mathcal{Y}} p(y | \mathbf{x}^{(i)}; \boldsymbol{\theta}) f_j(\mathbf{x}^{(i)}, y), \quad \forall j \quad [2.78]$$

1275 The moment-matching constraint is satisfied exactly when the derivative of the condi-  
 1276 tional log-likelihood function (Equation 2.64) is equal to zero. However, the constraint  
 1277 can be met by many values of  $\boldsymbol{\theta}$ , so which should we choose?

1278 The **entropy** of the conditional probability distribution  $p_{Y|X}$  is,

$$H(p_{Y|X}) = - \sum_{\mathbf{x} \in \mathcal{X}} p_X(\mathbf{x}) \sum_{y \in \mathcal{Y}} p_{Y|X}(y | \mathbf{x}) \log p_{Y|X}(y | \mathbf{x}), \quad [2.79]$$

1279 where  $\mathcal{X}$  is the set of all possible feature vectors, and  $p_X(\mathbf{x})$  is the probability of observing  
 1280 the base features  $\mathbf{x}$ . The distribution  $p_X$  is unknown, but it can be estimated by summing  
 1281 over all the instances in the training set,

$$\tilde{H}(p_{Y|X}) = - \frac{1}{N} \sum_{i=1}^N \sum_{y \in \mathcal{Y}} p_{Y|X}(y | \mathbf{x}^{(i)}) \log p_{Y|X}(y | \mathbf{x}^{(i)}). \quad [2.80]$$

1282 If the entropy is large, the likelihood function is smooth across possible values of  $y$ ;  
 1283 if it is small, the likelihood function is sharply peaked at some preferred value; in the  
 1284 limiting case, the entropy is zero if  $p(y | x) = 1$  for some  $y$ . The maximum-entropy cri-  
 1285 terion chooses to make the weakest commitments possible, while satisfying the moment-  
 1286 matching constraints from Equation 2.78. The solution to this constrained optimization  
 1287 problem is identical to the maximum conditional likelihood (logistic-loss) formulation  
 1288 that was presented in § 2.4.

1289 **2.7 Summary of learning algorithms**

1290 It is natural to ask which learning algorithm is best, but the answer depends on what  
 1291 characteristics are important to the problem you are trying to solve.

1292 **Naïve Bayes** *Pros:* easy to implement; estimation is fast, requiring only a single pass over  
 1293 the data; assigns probabilities to predicted labels; controls overfitting with smoothing-  
 1294 ing parameter. *Cons:* often has poor accuracy, especially with correlated features.

1295 **Perceptron** *Pros:* easy to implement; online; error-driven learning means that accuracy  
 1296 is typically high, especially after averaging. *Cons:* not probabilistic; hard to know  
 1297 when to stop learning; lack of margin can lead to overfitting.

1298 **Support vector machine** *Pros:* optimizes an error-based metric, usually resulting in high  
 1299 accuracy; overfitting is controlled by a regularization parameter. *Cons:* not proba-  
 1300 bilistic.

1301 **Logistic regression** *Pros:* error-driven and probabilistic; overfitting is controlled by a reg-  
 1302 ularization parameter. *Cons:* batch learning requires black-box optimization; logistic  
 1303 loss can “overtrain” on correctly labeled examples.

1304 One of the main distinctions is whether the learning algorithm offers a probability  
 1305 over labels. This is useful in modular architectures, where the output of one classifier  
 1306 is the input for some other system. In cases where probability is not necessary, the sup-  
 1307 port vector machine is usually the right choice, since it is no more difficult to implement  
 1308 than the perceptron, and is often more accurate. When probability is necessary, logistic  
 1309 regression is usually more accurate than Naïve Bayes.

1310 **Additional resources**

1311 For more on classification, you can consult a textbook on machine learning (e.g., Mur-  
 1312 phy, 2012), although the notation will differ slightly from what is typical in natural lan-  
 1313 guage processing. Probabilistic methods are surveyed by Hastie et al. (2009), and Mohri  
 1314 et al. (2012) emphasize theoretical considerations. Online learning is a rapidly moving  
 1315 subfield of machine learning, and Bottou et al. (2016) describes progress through 2016.  
 1316 Kummerfeld et al. (2015) empirically review several optimization algorithms for large-  
 1317 margin learning. The python toolkit `scikit-learn` includes implementations of all of  
 1318 the algorithms described in this chapter (Pedregosa et al., 2011).

1319 **Exercises**

- 1320 1. Let  $\mathbf{x}$  be a bag-of-words vector such that  $\sum_{j=1}^V x_j = 1$ . Verify that the multinomial  
 1321 probability  $p_{\text{mult}}(\mathbf{x}; \phi)$ , as defined in Equation 2.12, is identical to the probability of  
 1322 the same document under a categorical distribution,  $p_{\text{cat}}(\mathbf{w}; \phi)$ .
2. Suppose you have a single feature  $x$ , with the following conditional distribution:

$$p(x | y) = \begin{cases} \alpha, & X = 0, Y = 0 \\ 1 - \alpha, & X = 1, Y = 0 \\ 1 - \beta, & X = 0, Y = 1 \\ \beta, & X = 1, Y = 1. \end{cases} \quad [2.81]$$

1323 Further suppose that the prior is uniform,  $\Pr(Y = 0) = \Pr(Y = 1) = \frac{1}{2}$ , and that  
 1324 both  $\alpha > \frac{1}{2}$  and  $\beta > \frac{1}{2}$ . Given a Naïve Bayes classifier with accurate parameters,  
 1325 what is the probability of making an error?

- 1326 3. Derive the maximum-likelihood estimate for the parameter  $\mu$  in Naïve Bayes.
- 1327 4. As noted in the discussion of averaged perceptron in § 2.2.2, the computation of the  
 1328 running sum  $\mathbf{m} \leftarrow \mathbf{m} + \boldsymbol{\theta}$  is unnecessarily expensive, requiring  $K \times V$  operations.  
 1329 Give an alternative way to compute the averaged weights  $\bar{\boldsymbol{\theta}}$ , with complexity that is  
 1330 independent of  $V$  and linear in the sum of feature sizes  $\sum_{i=1}^N |\mathbf{f}(\mathbf{x}^{(i)}, y^{(i)})|$ .
- 1331 5. Consider a dataset that is comprised of two identical instances  $\mathbf{x}^{(1)} = \mathbf{x}^{(2)}$  with  
 1332 distinct labels  $y^{(1)} \neq y^{(2)}$ . Assume all features are binary,  $x_j \in \{0, 1\}$  for all  $j$ .

1333 Now suppose that the averaged perceptron always trains on the instance  $(\mathbf{x}^{i(t)}, y^{i(t)})$ ,  
 1334 where  $i(t) = 2 - (t \bmod 2)$ , which is 1 when the training iteration  $t$  is odd, and 2  
 1335 when  $t$  is even. Further suppose that learning terminates under the following con-  
 1336 dition:

$$\epsilon \geq \max_j \left| \frac{1}{t} \sum_t \theta_j^{(t)} - \frac{1}{t-1} \sum_t \theta_j^{(t-1)} \right|. \quad [2.82]$$

1337 In words, the algorithm stops when the largest change in the averaged weights is  
 1338 less than or equal to  $\epsilon$ . Compute the number of iterations before the averaged per-  
 1339 ceptron terminates.

- 1340 6. The classification models in the text have a vector of weights for each possible label.  
 1341 While this is notationally convenient, it is overdetermined: for any linear classifier  
 1342 that can be obtained with  $K \times V$  weights, an equivalent classifier can be constructed  
 1343 using  $(K - 1) \times V$  weights.

- 1344     a) Describe how to construct this classifier. Specifically, if given a set of weights  
 1345        $\theta$  and a feature function  $f(\mathbf{x}, y)$ , explain how to construct alternative weights  
 1346       and feature function  $\theta'$  and  $f'(\mathbf{x}, y)$ , such that,

$$\forall y, y' \in \mathcal{Y}, \theta \cdot f(\mathbf{x}, y) - \theta \cdot f(\mathbf{x}, y') = \theta' \cdot f'(\mathbf{x}, y) - \theta' \cdot f'(\mathbf{x}, y'). \quad [2.83]$$

- 1347     b) Explain how your construction justifies the well-known alternative form for  
 1348       binary logistic regression,  $\Pr(Y = 1 \mid \mathbf{x}; \theta) = \frac{1}{1 + \exp(-\theta \cdot \mathbf{x})} = \sigma(\theta \cdot \mathbf{x})$ , where  $\sigma$   
 1349       is the sigmoid function.

- 1350     7. Prove that the margin loss is convex in  $\theta$ . Use this definition of the margin loss:

$$L(\theta) = -\theta \cdot f(\mathbf{x}, y^*) + \max_y \theta \cdot f(\mathbf{x}, y) + c(y^*, y), \quad [2.84]$$

1351     where  $y^*$  is the gold label. As a reminder, a function  $f$  is convex iff,

$$f(\alpha x_1 + (1 - \alpha)x_2) \leq \alpha f(x_1) + (1 - \alpha)f(x_2), \quad [2.85]$$

1352     for any  $x_1, x_2$  and  $\alpha \in [0, 1]$ .

- 1353     8. Suppose you have two labeled datasets  $D_1$  and  $D_2$ , with the same features and la-  
 1354       bels.

- 1355       • Let  $\theta^{(1)}$  be the unregularized logistic regression (LR) coefficients from training  
     1356       on dataset  $D_1$ .
- 1357       • Let  $\theta^{(2)}$  be the unregularized LR coefficients (same model) from training on  
     1358       dataset  $D_2$ .
- 1359       • Let  $\theta^*$  be the unregularized LR coefficients from training on the combined  
     1360       dataset  $D_1 \cup D_2$ .

Under these conditions, prove that for any feature  $j$ ,

$$\begin{aligned} \theta_j^* &\geq \min(\theta_j^{(1)}, \theta_j^{(2)}) \\ \theta_j^* &\leq \max(\theta_j^{(1)}, \theta_j^{(2)}). \end{aligned}$$

- 1361
- 1362     9. Let  $\hat{\theta}$  be the solution to an unregularized logistic regression problem, and let  $\theta^*$  be  
 1363       the solution to the same problem, with  $L_2$  regularization. Prove that  $\|\theta^*\|_2^2 \leq \|\hat{\theta}\|_2^2$ .
- 1364     10. If a function  $f$  is  $m$ -strongly convex, then for some  $m > 0$ , the following inequality  
 1365       holds for all  $x$  and  $y$  on the domain of the function:

$$f(y) \leq f(x) + (\nabla_x f) \cdot (y - x) + \frac{m}{2} \|y - x\|_2^2. \quad [2.86]$$

1366 Let  $f$  be a loss function  $L$ ; let  $x \triangleq \boldsymbol{\theta}^{(t)}$  be the parameters at iteration  $t$ ; and let  
1367  $y \triangleq \boldsymbol{\theta}^{(t+1)} = \boldsymbol{\theta}^{(t)} - \alpha \nabla_{\boldsymbol{\theta}} L$  be the updated parameters, where  $\alpha > 0$  is the learning  
1368 rate. Use the inequality above to prove that  $L(\boldsymbol{\theta}^{(t+1)}) \leq L(\boldsymbol{\theta}^{(t)})$  for an appropriately  
1369 chosen step size  $\alpha$ , which will depend on the constant  $m$ . Explain why this implies  
1370 that gradient descent converges, when applied to a strongly convex loss function  
1371 with a unique minimum.



1372 **Chapter 3**

1373 **Nonlinear classification**

1374 Linear classification may seem like all we need for natural language processing. The bag-  
1375 of-words representation is inherently high dimensional, and the number of features is  
1376 often larger than the number of training instances. This means that it is usually possible  
1377 to find a linear classifier that perfectly fits the training data. Moving to nonlinear classifi-  
1378 cation may therefore only increase the risk of overfitting. For many tasks, **lexical features**  
1379 (words) are meaningful in isolation, and can offer independent evidence about the in-  
1380 stance label — unlike computer vision, where individual pixels are rarely informative,  
1381 and must be evaluated holistically to make sense of an image. For these reasons, natu-  
1382 ral language processing has historically focused on linear classification to a greater extent  
1383 than other machine learning application domains.

1384 But in recent years, nonlinear classifiers have swept through natural language pro-  
1385 cessing, and are now the default approach for many tasks (Manning, 2016). There are at  
1386 least three reasons for this change.

- 1387 • There have been rapid advances in **deep learning**, a family of nonlinear meth-  
1388 ods that learn complex functions of the input through multiple layers of computa-  
1389 tion (Goodfellow et al., 2016).
- 1390 • Deep learning facilitates the incorporation of **word embeddings**, which are dense  
1391 vector representations of words. Word embeddings can be learned from large amounts  
1392 of unlabeled data, and enable generalization to words that do not appear in the an-  
1393notated training data (word embeddings are discussed in detail in chapter 14).
- 1394 • A third reason for the rise of deep nonlinear learning algorithms is hardware. Many  
1395 deep learning models can be implemented efficiently on graphics processing units  
1396 (GPUs), offering substantial performance improvements over CPU-based comput-  
1397 ing.

1398 This chapter focuses on **neural networks**, which are the dominant approach for non-

1399 linear classification in natural language processing today.<sup>1</sup> Historically, a few other non-  
 1400 linear learning methods have been applied to language data:

- 1401 • **Kernel methods** are generalizations of the **nearest-neighbor** classification rule, which  
 1402 classifies each instance by the label of the most similar example in the training  
 1403 set (Hastie et al., 2009). The application of the **kernel support vector machine** to  
 1404 information extraction is described in chapter 17.
- 1405 • **Decision trees** classify instances by checking a set of conditions. Scaling decision  
 1406 trees to bag-of-words inputs is difficult, but decision trees have been successful in  
 1407 problems such as coreference resolution (chapter 15), where more compact feature  
 1408 sets can be constructed (Soon et al., 2001).
- 1409 • **Boosting** and related **ensemble methods** work by combining the predictions of sev-  
 1410 eral “weak” classifiers, each of which may consider only a small subset of features.  
 1411 Boosting has been successfully applied to text classification (Schapire and Singer,  
 1412 2000) and syntactic analysis (Abney et al., 1999), and remains one of the most suc-  
 1413 cessful methods on machine learning competition sites such as Kaggle (Chen and  
 1414 Guestrin, 2016).

### 1415 3.1 Feedforward neural networks

1416 Consider the problem of building a classifier for movie reviews. The goal is to predict  
 1417 a label  $y \in \{\text{GOOD}, \text{BAD}, \text{OKAY}\}$  from a representation of the text of each document,  $x$ .  
 1418 But what makes a good movie? The story, acting, cinematography, soundtrack, and so  
 1419 on. Now suppose the training set contains labels for each of these additional features,  
 1420  $z = [z_1, z_2, \dots, z_{K_z}]^\top$ . With such information, we could build a two-step classifier:

- 1421 1. **Use the text  $x$  to predict the features  $z$ .** Specifically, train a logistic regression clas-  
 1422 sifier to compute  $p(z_k | x)$ , for each  $k \in \{1, 2, \dots, K_z\}$ .
- 1423 2. **Use the features  $z$  to predict the label  $y$ .** Again, train a logistic regression classifier  
 1424 to compute  $p(y | z)$ . On test data,  $z$  is unknown, so we use the probabilities  $p(z | x)$   
 1425 from the first layer as the features.

1426 This setup is shown in Figure 3.1, which describes the proposed classifier in a **compu-**  
 1427 **tation graph**: the text features  $x$  are connected to the middle layer  $z$ , which in turn is  
 1428 connected to the label  $y$ .

1429 Since each  $z_k \in \{0, 1\}$ , we can treat  $p(z_k | x)$  as a binary classification problem, using  
 1430 binary logistic regression:

$$\Pr(z_k = 1 | x; \Theta^{(x \rightarrow z)}) = \sigma(\boldsymbol{\theta}_k^{(x \rightarrow z)} \cdot x) = (1 + \exp(-\boldsymbol{\theta}_k^{(x \rightarrow z)} \cdot x))^{-1}, \quad [3.1]$$

---

<sup>1</sup>I will use “deep learning” and “neural networks” interchangeably.

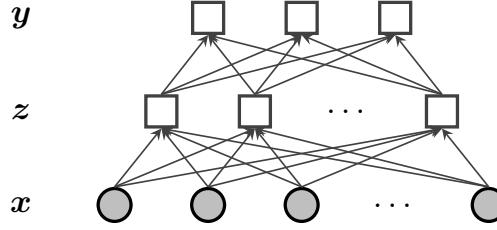


Figure 3.1: A feedforward neural network. Shaded circles indicate observed features, usually words; squares indicate nodes in the computation graph, which are computed from the information carried over the incoming arrows.

1431 where  $\sigma(\cdot)$  is the **sigmoid** function (shown in Figure 3.2), and the matrix  $\Theta^{(x \rightarrow z)} \in \mathbb{R}^{K_z \times V}$   
 1432 is constructed by stacking the weight vectors for each  $z_k$ ,

$$\Theta^{(x \rightarrow z)} = [\theta_1^{(x \rightarrow z)}, \theta_2^{(x \rightarrow z)}, \dots, \theta_{K_z}^{(x \rightarrow z)}]^\top. \quad [3.2]$$

1433 We will assume that  $x$  contains a term with a constant value of 1, so that a corresponding  
 1434 offset parameter is included in each  $\theta_k^{(x \rightarrow z)}$ .

1435 The output layer is computed by the multi-class logistic regression probability,

$$\Pr(y = j \mid z; \Theta^{(z \rightarrow y)}, b) = \frac{\exp(\theta_j^{(z \rightarrow y)} \cdot z + b_j)}{\sum_{j' \in \mathcal{Y}} \exp(\theta_{j'}^{(z \rightarrow y)} \cdot z + b_{j'})}, \quad [3.3]$$

1436 where  $b_j$  is an offset for label  $j$ , and the output weight matrix  $\Theta^{(z \rightarrow y)} \in \mathbb{R}^{K_y \times K_z}$  is again  
 1437 constructed by concatenation,

$$\Theta^{(z \rightarrow y)} = [\theta_1^{(z \rightarrow y)}, \theta_2^{(z \rightarrow y)}, \dots, \theta_{K_y}^{(z \rightarrow y)}]^\top. \quad [3.4]$$

1438 The vector of probabilities over each possible value of  $y$  is denoted,

$$p(y \mid z; \Theta^{(z \rightarrow y)}, b) = \text{SoftMax}(\Theta^{(z \rightarrow y)} z + b), \quad [3.5]$$

1439 where element  $j$  in the output of the **SoftMax** function is computed as in Equation 3.3.

We have now defined a multilayer classifier, which can be summarized as,

$$p(z \mid x; \Theta^{(x \rightarrow z)}) = \sigma(\Theta^{(x \rightarrow z)} x) \quad [3.6]$$

$$p(y \mid z; \Theta^{(z \rightarrow y)}, b) = \text{SoftMax}(\Theta^{(z \rightarrow y)} z + b), \quad [3.7]$$

1440 where  $\sigma(\cdot)$  is now applied **elementwise** to the vector of inner products,

$$\sigma(\Theta^{(x \rightarrow z)} x) = [\sigma(\theta_1^{(x \rightarrow z)} \cdot x), \sigma(\theta_2^{(x \rightarrow z)} \cdot x), \dots, \sigma(\theta_{K_z}^{(x \rightarrow z)} \cdot x)]^\top. \quad [3.8]$$

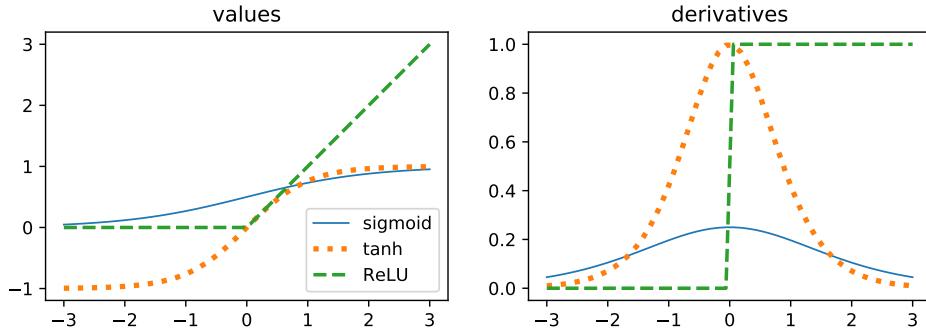


Figure 3.2: The sigmoid, tanh, and ReLU activation functions

Now suppose that the hidden features  $z$  are never observed, even in the training data. We can still construct the architecture in Figure 3.1. Instead of predicting  $y$  from a discrete vector of predicted values  $z$ , we use the probabilities  $\sigma(\theta_k \cdot x)$ . The resulting classifier is barely changed:

$$z = \sigma(\Theta^{(x \rightarrow z)} x) \quad [3.9]$$

$$p(y | x; \Theta^{(z \rightarrow y)}, b) = \text{SoftMax}(\Theta^{(z \rightarrow y)} z + b). \quad [3.10]$$

1441 This defines a classification model that predicts the label  $y \in \mathcal{Y}$  from the base features  $x$ ,  
1442 through a “hidden layer”  $z$ . This is a **feedforward neural network**.<sup>2</sup>

## 1443 3.2 Designing neural networks

1444 This feedforward neural network can be generalized in a number of ways.

### 1445 3.2.1 Activation functions

1446 If the hidden layer is viewed as a set of latent features, then the sigmoid function repre-  
1447 sents the extent to which each of these features is “activated” by a given input. However,  
1448 the hidden layer can be regarded more generally as a nonlinear transformation of the in-  
1449 put. This opens the door to many other activation functions, some of which are shown in  
1450 Figure 3.2. At the moment, the choice of activation functions is more art than science, but  
1451 a few points can be made about the most popular varieties:

- 1452 • The range of the sigmoid function is  $(0, 1)$ . The bounded range ensures that a cas-  
1453 cade of sigmoid functions will not “blow up” to a huge output, and this is impor-

---

<sup>2</sup>The architecture is sometimes called a **multilayer perceptron**, but this is misleading, because each layer is not a perceptron as defined in Algorithm 3.

tant for deep networks with several hidden layers. The derivative of the sigmoid is  $\frac{\partial}{\partial a} \sigma(a) = \sigma(a)(1 - \sigma(a))$ . This derivative becomes small at the extremes, which can make learning slow; this is called the **vanishing gradient** problem.

- The range of the **tanh activation function** is  $(-1, 1)$ : like the sigmoid, the range is bounded, but unlike the sigmoid, it includes negative values. The derivative is  $\frac{\partial}{\partial a} \tanh(a) = 1 - \tanh(a)^2$ , which is steeper than the logistic function near the origin (LeCun et al., 1998). The tanh function can also suffer from vanishing gradients at extreme values.
- The **rectified linear unit (ReLU)** is zero for negative inputs, and linear for positive inputs (Glorot et al., 2011),

$$\text{ReLU}(a) = \begin{cases} a, & a \geq 0 \\ 0, & \text{otherwise.} \end{cases} \quad [3.11]$$

The derivative is a step function, which is 1 if the input is positive, and zero otherwise. Once the activation is zero, the gradient is also zero. This can lead to the problem of **dead neurons**, where some ReLU nodes are zero for all inputs, throughout learning. A solution is the **leaky ReLU**, which has a small positive slope for negative inputs (Maas et al., 2013),

$$\text{Leaky-ReLU}(a) = \begin{cases} a, & a \geq 0 \\ .0001a, & \text{otherwise.} \end{cases} \quad [3.12]$$

Sigmoid and tanh are sometimes described as **squashing functions**, because they squash an unbounded input into a bounded range. Glorot and Bengio (2010) recommend against the use of the sigmoid activation in deep networks, because its mean value of  $\frac{1}{2}$  can cause the next layer of the network to be saturated, with very small gradients on their own parameters. Several other activation functions are reviewed by Goodfellow et al. (2016), who recommend ReLU as the “default option.”

### 3.2.2 Network structure

Deep networks stack up several hidden layers, with each  $z^{(d)}$  acting as the input to the next layer,  $z^{(d+1)}$ . As the total number of nodes in the network increases, so does its capacity to learn complex functions of the input. For a fixed number of nodes, an architectural decision is whether to emphasize width (large  $K_z$  at each layer) or depth (many layers). At present, this tradeoff is not well understood.<sup>3</sup>

---

<sup>3</sup>With even a single hidden layer, a neural network can approximate any continuous function on a closed and bounded subset of  $\mathbb{R}^N$  to an arbitrarily small non-zero error; see section 6.4.1 of Goodfellow et al. (2016) for a survey of these theoretical results. However, depending on the function to be approximated, the width

1481 It is also possible to “short circuit” a hidden layer, by propagating information directly  
 1482 from the input to the next higher level of the network. This is the idea behind **residual net-**  
 1483 **works**, which propagate information directly from the input to the subsequent layer (He  
 1484 et al., 2016),

$$z = f(\Theta^{(x \rightarrow z)} \mathbf{x}) + \mathbf{x}, \quad [3.13]$$

where  $f$  is any nonlinearity, such as sigmoid or ReLU. A more complex architecture is the **highway network** (Srivastava et al., 2015; Kim et al., 2016), in which an addition **gate** controls an interpolation between  $f(\Theta^{(x \rightarrow z)} \mathbf{x})$  and  $\mathbf{x}$ :

$$t = \sigma(\Theta^{(t)} \mathbf{x} + \mathbf{b}^{(t)}) \quad [3.14]$$

$$z = t \odot f(\Theta^{(x \rightarrow z)} \mathbf{x}) + (1 - t) \odot \mathbf{x}, \quad [3.15]$$

1485 where  $\odot$  refers to an elementwise vector product, and  $\mathbf{1}$  is a column vector of ones. The  
 1486 sigmoid function is applied elementwise to its input; recall that the output of this function  
 1487 is restricted to the range  $[0, 1]$ . Gating is also used in the **long short-term memory (LSTM)**,  
 1488 which is discussed in chapter 6. Residual and highway connections address a problem  
 1489 with deep architectures: repeated application of a nonlinear activation function can make  
 1490 it difficult to learn the parameters of the lower levels of the network, which are too distant  
 1491 from the supervision signal.

### 1492 3.2.3 Outputs and loss functions

In the multi-class classification example, a softmax output produces probabilities over each possible label. This aligns with a negative **conditional log-likelihood**,

$$-\mathcal{L} = -\sum_{i=1}^N \log p(y^{(i)} | \mathbf{x}^{(i)}; \Theta). \quad [3.16]$$

1493 where  $\Theta = \{\Theta^{(x \rightarrow z)}, \Theta^{(z \rightarrow y)}, \mathbf{b}\}$  is the entire set of parameters.

This loss can be written alternatively as follows:

$$\tilde{y}_j \triangleq \Pr(y = j | \mathbf{x}^{(i)}; \Theta) \quad [3.17]$$

$$-\mathcal{L} = -\sum_{i=1}^N e_{y^{(i)}} \cdot \log \tilde{y} \quad [3.18]$$

1494 where  $e_{y^{(i)}}$  is a **one-hot vector** of zeros with a value of 1 at position  $y^{(i)}$ . The inner product  
 1495 between  $e_{y^{(i)}}$  and  $\log \tilde{y}$  is also called the multinomial **cross-entropy**, and this terminology  
 1496 is preferred in many neural networks papers and software packages.

of the hidden layer may need to be arbitrarily large. Furthermore, the fact that a network has the capacity to approximate any given function does not say anything about whether it is possible to *learn* the function using gradient-based optimization.

It is also possible to train neural networks from other objectives, such as a margin loss. In this case, it is not necessary to use softmax at the output layer: an affine transformation of the hidden layer is enough:

$$\Psi(y; \mathbf{x}^{(i)}, \Theta) = \theta_y^{(z \rightarrow y)} \cdot \mathbf{z} + b_y \quad [3.19]$$

$$\ell_{\text{MARGIN}}(\Theta; \mathbf{x}^{(i)}, y^{(i)}) = \max_{y \neq y^{(i)}} \left( 1 + \Psi(y; \mathbf{x}^{(i)}, \Theta) - \Psi(y^{(i)}; \mathbf{x}^{(i)}, \Theta) \right)_+ \quad [3.20]$$

1497 In regression problems, the output is a scalar or vector (see § 4.1.2). For these problems, a  
1498 typical loss function is the squared error  $(y - \hat{y})^2$  or squared norm  $\|\mathbf{y} - \hat{\mathbf{y}}\|_2^2$ .

### 1499 3.2.4 Inputs and lookup layers

1500 In text classification, the input layer  $\mathbf{x}$  can refer to a bag-of-words vector, where  $x_j$  is  
1501 the count of word  $j$ . The input to the hidden unit  $z_k$  is then  $\sum_{j=1}^V \theta_{j,k}^{(x \rightarrow z)} x_j$ , and word  $j$  is  
1502 represented by the vector  $\theta_j^{(x \rightarrow z)}$ . This vector is sometimes described as the **embedding** of  
1503 word  $j$ , and can be learned from unlabeled data, using techniques discussed in chapter 14.  
1504 The columns of  $\Theta^{(x \rightarrow z)}$  are each  $K_z$ -dimensional word embeddings.

1505 Chapter 2 presented an alternative view of text documents, as a sequence of word  
1506 tokens,  $w_1, w_2, \dots, w_M$ . In a neural network, each word token  $w_m$  is represented with  
1507 a one-hot vector,  $e_{w_m} \in \mathbb{R}^V$ . The matrix-vector product  $\Theta^{(x \rightarrow z)} e_{w_m}$  returns the embed-  
1508 ding of word  $w_m$ . The complete document can be represented by horizontally concatenating  
1509 these one-hot vectors,  $\mathbf{W} = [e_{w_1}, e_{w_2}, \dots, e_{w_M}]$ , and the bag-of-words representation can  
1510 be recovered from the matrix-vector product  $\mathbf{W}\mathbf{1}$ , which simply sums each row over the  
1511 tokens  $m = \{1, 2, \dots, M\}$ . The matrix product  $\Theta^{(x \rightarrow z)} \mathbf{W}$  contains the horizontally con-  
1512 catenated embeddings of each word in the document, which will be useful as the starting  
1513 point for **convolutional neural networks** (see § 3.4). This is sometimes called a **lookup**  
1514 **layer**, because the first step is to lookup the embeddings for each word in the input text.

## 1515 3.3 Learning neural networks

The feedforward network in Figure 3.1 can now be written in a more general form,

$$\mathbf{z} \leftarrow f(\Theta^{(x \rightarrow z)} \mathbf{x}^{(i)}) \quad [3.21]$$

$$\tilde{\mathbf{y}} \leftarrow \text{SoftMax} \left( \Theta^{(z \rightarrow y)} \mathbf{z} + \mathbf{b} \right) \quad [3.22]$$

$$\ell^{(i)} \leftarrow -e_{y^{(i)}} \cdot \log \tilde{y}, \quad [3.23]$$

1516 where  $f$  is an elementwise activation function, such as  $\sigma$  or ReLU.

Let us now consider how to estimate the parameters  $\Theta^{(x \rightarrow z)}$ ,  $\Theta^{(z \rightarrow y)}$  and  $\mathbf{b}$ , using online gradient-based optimization. The simplest such algorithm is stochastic gradient descent (Algorithm 5). The relevant updates are,

$$\mathbf{b} \leftarrow \mathbf{b} - \eta^{(t)} \nabla_{\mathbf{b}} \ell^{(i)} \quad [3.24]$$

$$\boldsymbol{\theta}_k^{(z \rightarrow y)} \leftarrow \boldsymbol{\theta}_k^{(z \rightarrow y)} - \eta^{(t)} \nabla_{\boldsymbol{\theta}_k^{(z \rightarrow y)}} \ell^{(i)} \quad [3.25]$$

$$\boldsymbol{\theta}_n^{(x \rightarrow z)} \leftarrow \boldsymbol{\theta}_n^{(x \rightarrow z)} - \eta^{(t)} \nabla_{\boldsymbol{\theta}_n^{(x \rightarrow z)}} \ell^{(i)}, \quad [3.26]$$

where  $\eta^{(t)}$  is the learning rate on iteration  $t$ ,  $\ell^{(i)}$  is the loss at instance (or minibatch)  $i$ , and  $\boldsymbol{\theta}_n^{(x \rightarrow z)}$  is column  $n$  of the matrix  $\Theta^{(x \rightarrow z)}$ , and  $\boldsymbol{\theta}_k^{(z \rightarrow y)}$  is column  $k$  of  $\Theta^{(z \rightarrow y)}$ .

The gradients of the negative log-likelihood on  $\mathbf{b}$  and  $\boldsymbol{\theta}_k^{(z \rightarrow y)}$  are very similar to the gradients in logistic regression,

$$\nabla_{\boldsymbol{\theta}_k^{(z \rightarrow y)}} \ell^{(i)} = \left[ \frac{\partial \ell^{(i)}}{\partial \theta_{k,1}^{(z \rightarrow y)}}, \frac{\partial \ell^{(i)}}{\partial \theta_{k,2}^{(z \rightarrow y)}}, \dots, \frac{\partial \ell^{(i)}}{\partial \theta_{k,K_y}^{(z \rightarrow y)}} \right]^\top \quad [3.27]$$

$$\frac{\partial \ell^{(i)}}{\partial \theta_{k,j}^{(z \rightarrow y)}} = - \frac{\partial}{\partial \theta_{k,j}^{(z \rightarrow y)}} \left( \boldsymbol{\theta}_{y^{(i)}}^{(z \rightarrow y)} \cdot \mathbf{z} - \log \sum_{y \in \mathcal{Y}} \exp \boldsymbol{\theta}_y^{(z \rightarrow y)} \cdot \mathbf{z} \right) \quad [3.28]$$

$$= \left( \Pr(y = j \mid \mathbf{z}; \boldsymbol{\Theta}^{(z \rightarrow y)}, \mathbf{b}) - \delta(j = y^{(i)}) \right) z_k, \quad [3.29]$$

where  $\delta(j = y^{(i)})$  is a function that returns one when  $j = y^{(i)}$ , and zero otherwise. The gradient  $\nabla_{\mathbf{b}} \ell^{(i)}$  is similar to Equation 3.29.

The gradients on the input layer weights  $\Theta^{(x \rightarrow z)}$  are obtained by the chain rule of differentiation:

$$\frac{\partial \ell^{(i)}}{\partial \theta_{n,k}^{(x \rightarrow z)}} = \frac{\partial \ell^{(i)}}{\partial z_k} \frac{\partial z_k}{\partial \theta_{n,k}^{(x \rightarrow z)}} \quad [3.30]$$

$$= \frac{\partial \ell^{(i)}}{\partial z_k} \frac{\partial f(\boldsymbol{\theta}_k^{(x \rightarrow z)} \cdot \mathbf{x})}{\partial \theta_{n,k}^{(x \rightarrow z)}} \quad [3.31]$$

$$= \frac{\partial \ell^{(i)}}{\partial z_k} \times f'(\boldsymbol{\theta}_k^{(x \rightarrow z)} \cdot \mathbf{x}) \times x_n, \quad [3.32]$$

where  $f'(\boldsymbol{\theta}_k^{(x \rightarrow z)} \cdot \mathbf{x})$  is the derivative of the activation function  $f$ , applied at the input

$\theta_k^{(x \rightarrow z)} \cdot \mathbf{x}$ . For example, if  $f$  is the sigmoid function, then the derivative is,

$$\frac{\partial \ell^{(i)}}{\partial \theta_{n,k}^{(x \rightarrow z)}} = \frac{\partial \ell^{(i)}}{\partial z_k} \times \sigma(\theta_k^{(x \rightarrow z)} \cdot \mathbf{x}) \times (1 - \sigma(\theta_k^{(x \rightarrow z)} \cdot \mathbf{x})) \times x_n \quad [3.33]$$

$$= \frac{\partial \ell^{(i)}}{\partial z_k} \times z_k \times (1 - z_k) \times x_n. \quad [3.34]$$

1521 For intuition, consider each of the terms in the product.

- 1522 • If the negative log-likelihood  $\ell^{(i)}$  does not depend much on  $z_k$ ,  $\frac{\partial \ell^{(i)}}{\partial z_k} \rightarrow 0$ , then it  
1523 doesn't matter how  $z_k$  is computed, and so  $\frac{\partial \ell^{(i)}}{\partial \theta_{n,k}^{(x \rightarrow z)}} \rightarrow 0$ .
- 1524 • If  $z_k$  is near 1 or 0, then the curve of the sigmoid function (Figure 3.2) is nearly flat,  
1525 and changing the inputs will make little local difference. The term  $z_k \times (1 - z_k)$  is  
1526 maximized at  $z_k = \frac{1}{2}$ , where the slope of the sigmoid function is steepest.
- 1527 • If  $x_n = 0$ , then it does not matter how we set the weights  $\theta_{n,k}^{(x \rightarrow z)}$ , so  $\frac{\partial \ell^{(i)}}{\partial \theta_{n,k}^{(x \rightarrow z)}} = 0$ .

### 1528 3.3.1 Backpropagation

1529 In the equations above, the value  $\frac{\partial \ell^{(i)}}{\partial z_k}$  is reused in the derivatives with respect to each  
1530  $\theta_{n,k}^{(x \rightarrow z)}$ . It should therefore be computed once, and then cached. Furthermore, we should  
1531 only compute any derivative once we have already computed all of the necessary "inputs"  
1532 demanded by the chain rule of differentiation. This combination of sequencing, caching,  
1533 and differentiation is known as **backpropagation**. It can be generalized to any directed  
1534 acyclic **computation graph**.

1535 A computation graph is a declarative representation of a computational process. At  
1536 each node  $t$ , compute a value  $v_t$  by applying a function  $f_t$  to a (possibly empty) list of  
1537 parent nodes,  $\pi_t$ . For example, in a feedforward network with one hidden layer, there are  
1538 nodes for the input  $\mathbf{x}^{(i)}$ , the hidden layer  $\mathbf{z}$ , the predicted output  $\tilde{\mathbf{y}}$ , and the parameters  
1539  $\{\Theta^{(x \rightarrow z)}, \Theta^{(z \rightarrow y)}, \mathbf{b}\}$ . During training, there is also a node for the observed label  $y^{(i)}$  and  
1540 the loss  $\ell^{(i)}$ . Computation graphs have three main types of nodes:

1541 **Variables.** The variables include the *inputs*  $\mathbf{x}$ , the *hidden nodes*  $\mathbf{z}$ , the outputs  $\mathbf{y}$ , and the  
1542 loss function. Inputs are variables that do not have parents. Backpropagation com-  
1543 putes the gradients with respect to all variables except the inputs, but does not up-  
1544 date the variables during learning.

1545 **Parameters.** In a feedforward network, the parameters include the weights and offsets.  
1546 Parameter nodes do not have parents, and they are updated during learning.

---

**Algorithm 6** General backpropagation algorithm. In the computation graph  $G$ , every node contains a function  $f_t$  and a set of parent nodes  $\pi_t$ ; the inputs to the graph are  $x^{(i)}$ .

---

```

1: procedure BACKPROP( $G = \{f_t, \pi_t\}_{t=1}^T, x^{(i)}$ )
2:    $v_{t(n)} \leftarrow x_n^{(i)}$  for all  $n$  and associated computation nodes  $t(n)$ .
3:   for  $t \in \text{TOPOLOGICALSORT}(G)$  do  $\triangleright$  Forward pass: compute value at each node
4:     if  $|\pi_t| > 0$  then
5:        $v_t \leftarrow f_t(v_{\pi_{t,1}}, v_{\pi_{t,2}}, \dots, v_{\pi_{t,N_t}})$ 
6:      $g_{\text{objective}} = 1$   $\triangleright$  Backward pass: compute gradients at each node
7:     for  $t \in \text{REVERSE}(\text{TOPOLOGICALSORT}(G))$  do
8:        $g_t \leftarrow \sum_{t': t \in \pi_{t'}} g_{t'} \times \nabla_{v_t} v_{t'}$   $\triangleright$  Sum over all  $t'$  that are children of  $t$ , propagating
        the gradient  $g_{t'}$ , scaled by the local gradient  $\nabla_{v_t} v_{t'}$ 
9:   return  $\{g_1, g_2, \dots, g_T\}$ 

```

---

1547     **Objective.** The *objective* node is not the parent of any other node. Backpropagation begins  
 1548       by computing the gradient with respect to this node.

1549     If the computation graph is a directed acyclic graph, then it is possible to order the  
 1550       nodes with a topological sort, so that if node  $t$  is a parent of node  $t'$ , then  $t < t'$ . This  
 1551       means that the values  $\{v_t\}_{t=1}^T$  can be computed in a single forward pass. The topolog-  
 1552       ical sort is reversed when computing gradients: each gradient  $g_t$  is computed from the  
 1553       gradients of the children of  $t$ , implementing the chain rule of differentiation. The general  
 1554       backpropagation algorithm for computation graphs is shown in Algorithm 6, and illus-  
 1555       trated in Figure 3.3.

1556     While the gradients with respect to each parameter may be complex, they are com-  
 1557       posed of products of simple parts. For many networks, all gradients can be computed  
 1558       through **automatic differentiation**. This means that end users need only specify the feed-  
 1559       forward computation, and the gradients necessary for learning can be obtained automati-  
 1560       cally. There are many software libraries that perform automatic differentiation on compu-  
 1561       tation graphs, such as Torch (Collobert et al., 2011), TensorFlow (Abadi et al., 2016), and  
 1562       DyNet (Neubig et al., 2017). One important distinction between these libraries is whether  
 1563       they support **dynamic computation graphs**, in which the structure of the computation  
 1564       graph varies across instances. Static computation graphs are compiled in advance, and  
 1565       can be applied to fixed-dimensional data, such as bag-of-words vectors. In many natu-  
 1566       ral language processing problems, each input has a distinct structure, requiring a unique  
 1567       computation graph.

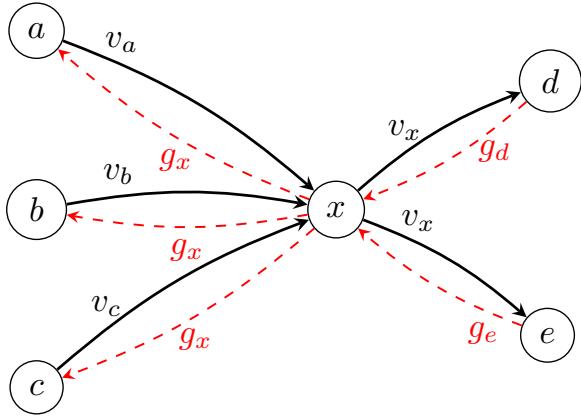


Figure 3.3: Backpropagation at a single node  $x$  in the computation graph. The values of the predecessors  $v_a, v_b, v_c$  are the inputs to  $x$ , which computes  $v_x$ , and passes it on to the successors  $d$  and  $e$ . The gradients at the successors  $g_d$  and  $g_e$  are passed back to  $x$ , where they are incorporated into the gradient  $g_x$ , which is then passed back to the predecessors  $a, b$ , and  $c$ .

### 1568 3.3.2 Regularization and dropout

1569 In linear classification, overfitting was addressed by augmenting the objective with a reg-  
 1570 ularization term,  $\lambda \|\theta\|_2^2$ . This same approach can be applied to feedforward neural net-  
 1571 works, penalizing each matrix of weights:

$$L = \sum_{i=1}^N \ell^{(i)} + \lambda_{z \rightarrow y} \|\Theta^{(z \rightarrow y)}\|_F^2 + \lambda_{x \rightarrow z} \|\Theta^{(x \rightarrow z)}\|_F^2, \quad [3.35]$$

1572 where  $\|\Theta\|_F^2 = \sum_{i,j} \theta_{i,j}^2$  is the squared **Frobenius norm**, which generalizes the  $L_2$  norm  
 1573 to matrices. The bias parameters  $b$  are not regularized, as they do not contribute to the  
 1574 sensitivity of the classifier to the inputs. In gradient-based optimization, the practical  
 1575 effect of Frobenius norm regularization is that the weights “decay” towards zero at each  
 1576 update, motivating the alternative name **weight decay**.

1577 Another approach to controlling model complexity is **dropout**, which involves ran-  
 1578 domly setting some computation nodes to zero during training (Srivastava et al., 2014).  
 1579 For example, in the feedforward network, on each training instance, with probability  $\rho$  we  
 1580 set each input  $x_n$  and each hidden layer node  $z_k$  to zero. Srivastava et al. (2014) recom-  
 1581 mend  $\rho = 0.5$  for hidden units, and  $\rho = 0.2$  for input units. Dropout is also incorporated  
 1582 in the gradient computation, so if node  $z_k$  is dropped, then none of the weights  $\theta_k^{(x \rightarrow z)}$  will  
 1583 be updated for this instance. Dropout prevents the network from learning to depend too  
 1584 much on any one feature or hidden node, and prevents **feature co-adaptation**, in which a

hidden unit is only useful in combination with one or more other hidden units. Dropout is a special case of **feature noising**, which can also involve adding Gaussian noise to inputs or hidden units (Holmstrom and Koistinen, 1992). Wager et al. (2013) show that dropout is approximately equivalent to “adaptive”  $L_2$  regularization, with a separate regularization penalty for each feature.

### 3.3.3 \*Learning theory

Chapter 2 emphasized the importance of **convexity** for learning: for convex objectives, the global optimum can be found efficiently. The negative log-likelihood and hinge loss are convex functions of the parameters of the output layer. However, the output of a feed-forward network is generally not a convex function of the parameters of the input layer,  $\Theta^{(x \rightarrow z)}$ . Feedforward networks can be viewed as function composition, where each layer is a function that is applied to the output of the previous layer. Convexity is generally not preserved in the composition of two convex functions — and furthermore, “squashing” activation functions like tanh and sigmoid are not convex.

The non-convexity of hidden layer neural networks can also be seen by permuting the elements of the hidden layer, from  $z = [z_1, z_2, \dots, z_{K_z}]$  to  $\tilde{z} = [z_{\pi(1)}, z_{\pi(2)}, \dots, z_{\pi(K_z)}]$ . This corresponds to applying  $\pi$  to the rows of  $\Theta^{(x \rightarrow z)}$  and the columns of  $\Theta^{(z \rightarrow y)}$ , resulting in permuted parameter matrices  $\Theta_\pi^{(x \rightarrow z)}$  and  $\Theta_\pi^{(z \rightarrow y)}$ . As long as this permutation is applied consistently, the loss will be identical,  $L(\Theta) = L(\Theta_\pi)$ : it is *invariant* to this permutation. However, the loss of the linear combination  $L(\alpha\Theta + (1 - \alpha)\Theta_\pi)$  will generally not be identical to the loss under  $\Theta$  or its permutations. If  $L(\Theta)$  is better than the loss at any points in the immediate vicinity, and if  $L(\Theta) = L(\Theta_\pi)$ , then the loss function does not satisfy the definition of convexity (see § 2.3). One of the exercises asks you to prove this more rigorously.

In practice, the existence of multiple optima is not necessarily problematic, if all such optima are permutations of the sort described in the previous paragraph. In contrast, “bad” local optima are better than their neighbors, but much worse than the global optimum. Fortunately, in large feedforward neural networks, most local optima are nearly as good as the global optimum (Choromanska et al., 2015), which helps to explain why backpropagation works in practice. More generally, a **critical point** is one at which the gradient is zero. Critical points may be local optima, but they may also be **saddle points**, which are local minima in some directions, but local *maxima* in other directions. For example, the equation  $x_1^2 - x_2^2$  has a saddle point at  $x = (0, 0)$ .<sup>4</sup> In large networks, the overwhelming majority of critical points are saddle points, rather than local minima or maxima (Dauphin et al., 2014). Saddle points can pose problems for gradient-based optimization, since learning will slow to a crawl as the gradient goes to zero. However, the noise introduced by

---

<sup>4</sup>Thanks to Rong Ge’s blogpost for this example, <http://www.offconvex.org/2016/03/22/saddlepoints/>

1621 stochastic gradient descent, and by feature noising techniques such as dropout, can help  
 1622 online optimization to escape saddle points and find high-quality optima (Ge et al., 2015).  
 1623 Other techniques address saddle points directly, using local reconstructions of the Hessian  
 1624 matrix (Dauphin et al., 2014) or higher-order derivatives (Anandkumar and Ge, 2016).

1625 **3.3.4 Tricks**

1626 Getting neural networks to work effectively sometimes requires heuristic “tricks” (Bottou,  
 1627 2012; Goodfellow et al., 2016; Goldberg, 2017b). This section presents some tricks that are  
 1628 especially important.

**Initialization** Initialization is not especially important for linear classifiers, since convexity ensures that the global optimum can usually be found quickly. But for multilayer neural networks, it is helpful to have a good starting point. One reason is that if the magnitude of the initial weights is too large, a sigmoid or tanh nonlinearity will be saturated, leading to a small gradient, and slow learning. Large gradients are also problematic. Initialization can help avoid these problems, by ensuring that the variance over the initial gradients is constant and bounded throughout the network. For networks with tanh activation functions, this can be achieved by sampling the initial weights from the following uniform distribution (Glorot and Bengio, 2010),

$$\theta_{i,j} \sim U \left[ -\frac{\sqrt{6}}{\sqrt{d_{\text{in}}(n) + d_{\text{out}}(n)}}, \frac{\sqrt{6}}{\sqrt{d_{\text{in}}(n) + d_{\text{out}}(n)}} \right], \quad [3.36]$$

[3.37]

1629 For the weights leading to a ReLU activation function, He et al. (2015) use similar argu-  
 1630 mentation to justify sampling from a zero-mean Gaussian distribution,

$$\theta_{i,j} \sim N(0, \sqrt{2/d_{\text{in}}(n)}) \quad [3.38]$$

Rather than initializing the weights independently, it can be beneficial to initialize each layer jointly as an **orthonormal matrix**, ensuring that  $\Theta^\top \Theta = \mathbb{I}$  (Saxe et al., 2014). Orthonormal matrices preserve the norm of the input, so that  $\|\Theta x\| = \|x\|$ , which prevents the gradients from exploding or vanishing. Orthogonality ensures that the hidden units are uncorrelated, so that they correspond to different features of the input. Orthonormal initialization can be performed by applying **singular value decomposition** to a matrix of

values sampled from a standard normal distribution:

$$a_{i,j} \sim N(0, 1) \quad [3.39]$$

$$\mathbf{A} = \{a_{i,j}\}_{i=1,j=1}^{d_{\text{in}}(j), d_{\text{out}}(j)} \quad [3.40]$$

$$\mathbf{U}, \mathbf{S}, \mathbf{V}^\top = \text{SVD}(\mathbf{A}) \quad [3.41]$$

$$\Theta^{(j)} \leftarrow \mathbf{U}. \quad [3.42]$$

1631 The matrix  $\mathbf{U}$  contains the **singular vectors** of  $\mathbf{A}$ , and is guaranteed to be orthonormal.  
 1632 For more on singular value decomposition, see chapter 14.

1633 Even with careful initialization, there can still be significant variance in the final re-  
 1634 sults. It can be useful to make multiple training runs, and select the one with the best  
 1635 performance on a heldout development set.

1636 **Clipping and normalizing the gradients** As already discussed, the magnitude of the  
 1637 gradient can pose problems for learning: too large, and learning can diverge, with suc-  
 1638 ccessive updates thrashing between increasingly extreme values; too small, and learning can  
 1639 grind to a halt. Several heuristics have been proposed to address this issue.

1640 • In **gradient clipping** (Pascanu et al., 2013), an upper limit is placed on the norm of  
 1641 the gradient, and the gradient is rescaled when this limit is exceeded,

$$\text{CLIP}(\hat{\mathbf{g}}) = \begin{cases} \mathbf{g} & \|\hat{\mathbf{g}}\| < \tau \\ \frac{\tau}{\|\mathbf{g}\|} \mathbf{g} & \text{otherwise.} \end{cases} \quad [3.43]$$

• In **batch normalization** (Ioffe and Szegedy, 2015), the inputs to each computation node are recentered by their mean and variance across all of the instances in the minibatch  $\mathcal{B}$  (see § 2.5.2). For example, in a feedforward network with one hidden layer, batch normalization would transform the inputs to the hidden layer as follows:

$$\boldsymbol{\mu}^{(\mathcal{B})} = \frac{1}{|\mathcal{B}|} \sum_{i \in \mathcal{B}} \mathbf{x}^{(i)} \quad [3.44]$$

$$\mathbf{s}^{(\mathcal{B})} = \frac{1}{|\mathcal{B}|} \sum_{i \in \mathcal{B}} (\mathbf{x}^{(i)} - \boldsymbol{\mu}^{(\mathcal{B})})^2 \quad [3.45]$$

$$\bar{\mathbf{x}}^{(i)} = (\mathbf{x}^{(i)} - \boldsymbol{\mu}^{(\mathcal{B})}) / \sqrt{\mathbf{s}^{(\mathcal{B})}}. \quad [3.46]$$

1642 Empirically, this speeds convergence of deep architectures. One explanation is that  
 1643 it helps to correct for changes in the distribution of activations during training.

- In **layer normalization** (Ba et al., 2016), the inputs to each nonlinear activation function are recentered across the layer:

$$\mathbf{a} = \Theta^{(x \rightarrow z)} \mathbf{x} \quad [3.47]$$

$$\mu = \frac{1}{K_z} \sum_{k=1}^{K_z} a_k \quad [3.48]$$

$$s = \frac{1}{K_z} \sum_{k=1}^{K_z} (a_k - \mu)^2 \quad [3.49]$$

$$z = (\mathbf{a} - \mu) / \sqrt{s}. \quad [3.50]$$

1644 Layer normalization has similar motivations to batch normalization, but it can be  
 1645 applied across a wider range of architectures and training conditions.

**Online optimization** The trend towards deep learning has spawned a cottage industry of **online optimization** algorithms, which attempt to improve on stochastic gradient descent. **AdaGrad** was reviewed in § 2.5.2; its main innovation is to set adaptive learning rates for each parameter by storing the sum of squared gradients. Rather than using the sum over the entire training history, we can keep a running estimate,

$$v_j^{(t)} = \beta v_j^{(t-1)} + (1 - \beta) g_{t,j}^2, \quad [3.51]$$

1646 where  $g_{t,j}$  is the gradient with respect to parameter  $j$  at time  $t$ , and  $\beta \in [0, 1]$ . This term  
 1647 places more emphasis on recent gradients, and is employed in the **AdaDelta** (Zeiler, 2012)  
 1648 and **Adam** (Kingma and Ba, 2014) optimizers. Online optimization and its theoretical  
 1649 background are reviewed by Bottou et al. (2016). **Early stopping**, mentioned in § 2.2.2,  
 1650 can help to avoid overfitting, by terminating training after reaching a plateau in the per-  
 1651 formance on a heldout validation set.

## 1652 3.4 Convolutional neural networks

1653 A basic weakness of the bag-of-words model is its inability to account for the ways in  
 1654 which words combine to create meaning, including even simple reversals such as *not*  
 1655 *pleasant, hardly a generous offer*, and *I wouldn't mind missing the flight*. Similarly, computer  
 1656 vision faces the challenge of identifying the semantics of images from pixel features that  
 1657 are uninformative in isolation. An earlier generation of computer vision research fo-  
 1658 cused on designing *filters* to aggregate local pixel-level features into more meaningful  
 1659 representations, such as edges and corners (e.g., Canny, 1987). Similarly, earlier NLP re-  
 1660 search attempted to capture multiword linguistic phenomena by hand-designed lexical  
 1661 patterns (Hobbs et al., 1997). In both cases, the output of the filters and patterns could

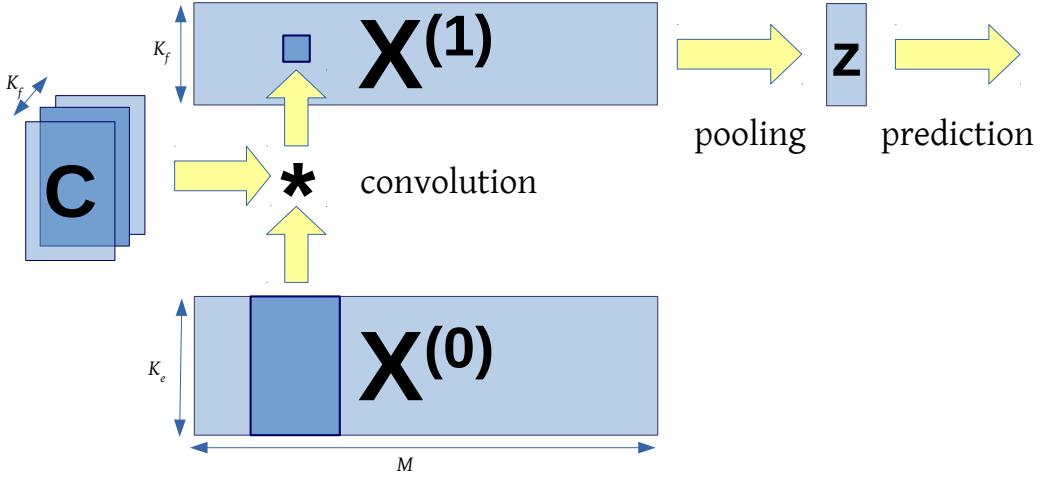


Figure 3.4: A convolutional neural network for text classification

then act as base features in a linear classifier. But rather than designing these feature extractors by hand, a better approach is to learn them, using the magic of backpropagation. This is the idea behind **convolutional neural networks**.

Following § 3.2.4, define the base layer of a neural network as,

$$\mathbf{X}^{(0)} = \Theta^{(x \rightarrow z)}[\mathbf{e}_{w_1}, \mathbf{e}_{w_2}, \dots, \mathbf{e}_{w_M}], \quad [3.52]$$

where  $\mathbf{e}_{w_m}$  is a column vector of zeros, with a 1 at position  $w_m$ . The base layer has dimension  $\mathbf{X}^{(0)} \in \mathbb{R}^{K_e \times M}$ , where  $K_e$  is the size of the word embeddings. To merge information across adjacent words, we *convolve*  $\mathbf{X}^{(0)}$  with a set of filter matrices  $\mathbf{C}^{(k)} \in \mathbb{R}^{K_e \times h}$ . Convolution is indicated by the symbol  $*$ , and is defined,

$$\mathbf{X}^{(1)} = f(\mathbf{b} + \mathbf{C} * \mathbf{X}^{(0)}) \implies x_{k,m}^{(1)} = f \left( b_k + \sum_{k'=1}^{K_e} \sum_{n=1}^h c_{k',n}^{(k)} \times x_{k',m+n-1}^{(0)} \right), \quad [3.53]$$

where  $f$  is an activation function such as tanh or ReLU, and  $\mathbf{b}$  is a vector of offsets. The convolution operation slides the matrix  $\mathbf{C}^{(k)}$  across the columns of  $\mathbf{X}^{(0)}$ ; at each position  $m$ , compute the elementwise product  $\mathbf{C}^{(k)} \odot \mathbf{X}_{m:m+h-1}^{(0)}$ , and take the sum.

A simple filter might compute a weighted average over nearby words,

$$\mathbf{C}^{(k)} = \begin{bmatrix} 0.5 & 1 & 0.5 \\ 0.5 & 1 & 0.5 \\ \dots & \dots & \dots \\ 0.5 & 1 & 0.5 \end{bmatrix}, \quad [3.54]$$

1670 thereby representing trigram units like *not so unpleasant*. In **one-dimensional convolution**,  
 1671 each filter matrix  $\mathbf{C}^{(k)}$  is constrained to have non-zero values only at row  $k$  (Kalchbrenner et al., 2014).

1673 To deal with the beginning and end of the input, the base matrix  $\mathbf{X}^{(0)}$  may be padded  
 1674 with  $h$  column vectors of zeros at the beginning and end; this is known as **wide convolution**. If padding is not applied, then the output from each layer will be  $h - 1$  units smaller  
 1675 than the input; this is known as **narrow convolution**. The filter matrices need not have  
 1676 identical filter widths, so more generally we could write  $h_k$  to indicate width of filter  
 1677  $\mathbf{C}^{(k)}$ . As suggested by the notation  $\mathbf{X}^{(0)}$ , multiple layers of convolution may be applied,  
 1678 so that  $\mathbf{X}^{(d)}$  is the input to  $\mathbf{X}^{(d+1)}$ .

After  $D$  convolutional layers, we obtain a matrix representation of the document  $\mathbf{X}^{(D)} \in \mathbb{R}^{K_z \times M}$ . If the instances have variable lengths, it is necessary to aggregate over all  $M$  word positions to obtain a fixed-length representation. This can be done by a **pooling** operation, such as max-pooling (Collobert et al., 2011) or average-pooling,

$$\mathbf{z} = \text{MaxPool}(\mathbf{X}^{(D)}) \implies z_k = \max(x_{k,1}^{(D)}, x_{k,2}^{(D)}, \dots, x_{k,M}^{(D)}) \quad [3.55]$$

$$\mathbf{z} = \text{AvgPool}(\mathbf{X}^{(D)}) \implies z_k = \frac{1}{M} \sum_{m=1}^M x_{k,m}^{(D)}. \quad [3.56]$$

1680 The vector  $\mathbf{z}$  can now act as a layer in a feedforward network, culminating in a prediction  
 1681  $\hat{y}$  and a loss  $\ell^{(i)}$ . The setup is shown in Figure 3.4.

Just as in feedforward networks, the parameters  $(\mathbf{C}^{(k)}, \mathbf{b}, \Theta)$  can be learned by backpropagating from the classification loss. This requires backpropagating through the max-pooling operation, which is a discontinuous function of the input. But because we need only a local gradient, backpropagation flows only through the argmax  $m$ :

$$\frac{\partial z_k}{\partial x_{k,m}^{(D)}} = \begin{cases} 1, & x_{k,m}^{(D)} = \max(x_{k,1}^{(D)}, x_{k,2}^{(D)}, \dots, x_{k,M}^{(D)}) \\ 0, & \text{otherwise.} \end{cases} \quad [3.57]$$

1682 The computer vision literature has produced a huge variety of convolutional architectures,  
 1683 and many of these bells and whistles can be applied to text data. One avenue for  
 1684 improvement is more complex pooling operations, such as  $k$ -max pooling (Kalchbrenner  
 1685 et al., 2014), which returns a matrix of the  $k$  largest values for each filter. Another innovation  
 1686 is the use of **dilated convolution** to build multiscale representations (Yu and Koltun,  
 1687 2016). At each layer, the convolutional operator applied in *strides*, skipping ahead by  $s$   
 1688 steps after each feature. As we move up the hierarchy, each layer is  $s$  times smaller than  
 1689 the layer below it, effectively summarizing the input. This idea is shown in Figure 3.5.  
 1690 Multi-layer convolutional networks can also be augmented with “shortcut” connections,  
 1691 as in the ResNet model from § 3.2.2 (Johnson and Zhang, 2017).

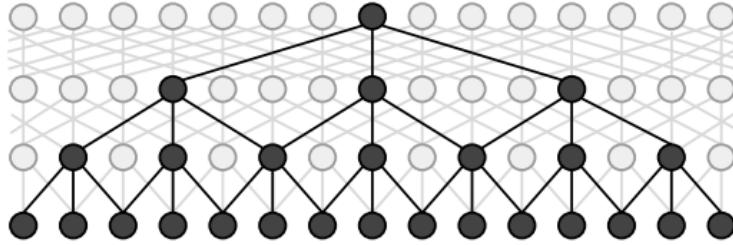


Figure 3.5: A dilated convolutional neural network captures progressively larger context through recursive application of the convolutional operator (Strubell et al., 2017) [todo: permission]

## 1692 Additional resources

1693 The deep learning textbook by Goodfellow et al. (2016) covers many of the topics in this  
 1694 chapter in more detail. For a comprehensive review of neural networks in natural lan-  
 1695 guage processing, see (Goldberg, 2017b). A seminal work on deep learning in natural  
 1696 language processing is the aggressively titled “Natural Language Processing (Almost)  
 1697 from Scratch”, which uses convolutional neural networks to perform a range of language  
 1698 processing tasks (Collobert et al., 2011). This chapter focuses on feedforward and con-  
 1699 volutional neural networks, but recurrent neural networks are one of the most important  
 1700 deep learning architectures for natural language processing. They are covered extensively  
 1701 in chapters 6 and 7.

1702 The role of deep learning in natural language processing research has caused angst  
 1703 in some parts of the natural language processing research community (e.g., Goldberg,  
 1704 2017a), especially as some of the more zealous deep learning advocates have argued that  
 1705 end-to-end learning from “raw” text can eliminate the need for linguistic constructs such  
 1706 as sentences, phrases, and even words (Zhang et al., 2015, originally titled *Text understand-  
 1707 ing from scratch*). These developments were surveyed by Manning (2016).

## 1708 Exercises

- 1709 1. Prove that the softmax and sigmoid functions are equivalent when the number of  
 1710 possible labels is two. Specifically, for any  $\Theta^{(z \rightarrow y)}$  (omitting the offset  $b$  for sim-  
 1711 plicity), show how to construct a vector of weights  $\theta$  such that,

$$\text{SoftMax}(\Theta^{(z \rightarrow y)} z)[0] = \sigma(\theta \cdot z). \quad [3.58]$$

- 1712 2. Design a feedforward network to compute the XOR function:

$$f(x_1, x_2) = \begin{cases} -1, & x_1 = 1, x_2 = 1 \\ 1, & x_1 = 1, x_2 = 0 \\ 1, & x_1 = 0, x_2 = 1 \\ -1, & x_1 = 0, x_2 = 0 \end{cases}. \quad [3.59]$$

1713 Your network should have a single output node which uses the Sign activation func-  
 1714 tion. Use a single hidden layer, with ReLU activation functions. Describe all weights  
 1715 and offsets.

- 1716 3. Consider the same network as above (with ReLU activations for the hidden layer),  
 1717 with an arbitrary differentiable loss function  $\ell(y^{(i)}, \tilde{y})$ , where  $\tilde{y}$  is the activation of  
 1718 the output node. Suppose all weights and offsets are initialized to zero. Prove that  
 1719 gradient-based optimization cannot learn the desired function from this initializa-  
 1720 tion.
- 1721 4. The simplest solution to the previous problem relies on the use of the ReLU activa-  
 1722 tion function at the hidden layer. Now consider a network with arbitrary activations  
 1723 on the hidden layer. Show that if the initial weights are any uniform constant, then  
 1724 it is not possible to learn the desired function.
- 1725 5. Consider a network in which: the base features are all binary,  $\mathbf{x} \in \{0, 1\}^M$ ; the  
 1726 hidden layer activation function is sigmoid,  $z_k = \sigma(\boldsymbol{\theta}_k \cdot \mathbf{x})$ ; and the initial weights  
 1727 are sampled independently from a standard normal distribution,  $\theta_{j,k} \sim N(0, 1)$ .

- 1728 • Show how the probability of a small initial gradient on any weight,  $\frac{\partial z_k}{\partial \theta_{j,k}} < \alpha$ ,  
 1729 depends on the size of the input  $M$ . **Hint:** use the lower bound,

$$\Pr(\sigma(\boldsymbol{\theta}_k \cdot \mathbf{x}) \times (1 - \sigma(\boldsymbol{\theta}_k \cdot \mathbf{x})) < \alpha) \geq 2 \Pr(\sigma(\boldsymbol{\theta}_k \cdot \mathbf{x}) < \alpha), \quad [3.60]$$

1730 and relate this probability to the variance  $V[\boldsymbol{\theta}_k \cdot \mathbf{x}]$ .

- 1731 • Design an alternative initialization that removes this dependence.

- 1732 6. Suppose that the parameters  $\Theta = \{\Theta^{(x \rightarrow z)}, \Theta(z \rightarrow y), \mathbf{b}\}$  are a local optimum of a  
 1733 feedforward network in the following sense: there exists some  $\epsilon > 0$  such that,

$$\begin{aligned} & \left( \|\tilde{\Theta}^{(x \rightarrow z)} - \Theta^{(x \rightarrow z)}\|_F^2 + \|\tilde{\Theta}^{(z \rightarrow y)} - \Theta^{(z \rightarrow y)}\|_F^2 + \|\tilde{\mathbf{b}} - \mathbf{b}\|_2^2 < \epsilon \right) \\ & \Rightarrow \left( L(\tilde{\Theta}) > L(\Theta) \right) \end{aligned} \quad [3.61]$$

1734 Define the function  $\pi$  as a permutation on the hidden units, as described in § 3.3.3,  
 1735 so that for any  $\Theta$ ,  $L(\Theta) = L(\Theta_\pi)$ . Prove that if a feedforward network has a local  
 optimum in the sense of Equation 3.61, then its loss is not a convex function of the  
 parameters  $\Theta$ , using the definition of convexity from § 2.3

- 1736     7. Consider a network with a single hidden layer, and a single output,

$$y = \theta^{(z \rightarrow y)} \cdot g(\Theta^{(x \rightarrow z)} x). \quad [3.62]$$

1737     Assume that  $g$  is the ReLU function. Prove that for any matrix of weights  $\Theta^{(x \rightarrow z)}$ , it  
1738     is permissible to rescale each row to have a norm of one, because an identical output  
1739     can be obtained by finding a corresponding rescaling of  $\theta^{(z \rightarrow y)}$ .

## 1740 Chapter 4

# 1741 Linguistic applications of 1742 classification

1743 Having learned some techniques for classification, this chapter shifts the focus from mathematics  
1744 to linguistic applications. Later in the chapter, we will consider the design decisions involved in text classification, as well as evaluation practices.

### 1746 4.1 Sentiment and opinion analysis

1747 A popular application of text classification is to automatically determine the **sentiment**  
1748 or **opinion polarity** of documents such as product reviews and social media posts. For  
1749 example, marketers are interested to know how people respond to advertisements, ser-  
1750 vices, and products (Hu and Liu, 2004); social scientists are interested in how emotions  
1751 are affected by phenomena such as the weather (Hannak et al., 2012), and how both opin-  
1752 ions and emotions spread over social networks (Coviello et al., 2014; Miller et al., 2011).  
1753 In the field of **digital humanities**, literary scholars track plot structures through the flow  
1754 of sentiment across a novel (Jockers, 2015).<sup>1</sup>

1755 Sentiment analysis can be framed as a direct application of document classification,  
1756 assuming reliable labels can be obtained. In the simplest case, sentiment analysis is a  
1757 two or three-class problem, with sentiments of POSITIVE, NEGATIVE, and possibly NEU-  
1758 TRAL. Such annotations could be annotated by hand, or obtained automatically through  
1759 a variety of means:

- 1760 • Tweets containing happy emoticons can be marked as positive, sad emoticons as  
1761 negative (Read, 2005; Pak and Paroubek, 2010).

---

<sup>1</sup>Comprehensive surveys on sentiment analysis and related problems are offered by Pang and Lee (2008) and Liu (2015).

- 1762     • Reviews with four or more stars can be marked as positive, two or fewer stars as  
 1763       negative (Pang et al., 2002).
- 1764     • Statements from politicians who are voting for a given bill are marked as positive  
 1765       (towards that bill); statements from politicians voting against the bill are marked as  
 1766       negative (Thomas et al., 2006).

1767     The bag-of-words model is a good fit for sentiment analysis at the document level: if  
 1768     the document is long enough, we would expect the words associated with its true senti-  
 1769     ment to overwhelm the others. Indeed, **lexicon-based sentiment analysis** avoids machine  
 1770     learning altogether, and classifies documents by counting words against positive and neg-  
 1771     ative sentiment word lists (Taboada et al., 2011).

1772     Lexicon-based classification is less effective for short documents, such as single-sentence  
 1773     reviews or social media posts. In these documents, linguistic issues like **negation** and **ir-**  
 1774     **realis** (Polanyi and Zaenen, 2006) — events that are hypothetical or otherwise non-factual  
 1775     — can make bag-of-words classification ineffective. Consider the following examples:

- 1776     (4.1) That's not bad for the first day.
- 1777     (4.2) This is not the worst thing that can happen.
- 1778     (4.3) It would be nice if you acted like you understood.
- 1779     (4.4) There is no reason at all to believe that the polluters are suddenly going to be-  
 1780       come reasonable. (Wilson et al., 2005)
- 1781     (4.5) This film should be brilliant. The actors are first grade. Stallone plays a happy,  
 1782       wonderful man. His sweet wife is beautiful and adores him. He has a fascinat-  
 1783       ing gift for living life fully. It sounds like a great plot, **however**, the film is a  
 1784       failure. (Pang et al., 2002)

1785     A minimal solution is to move from a bag-of-words model to a bag-of-**bigrams** model,  
 1786     where each base feature is a pair of adjacent words, e.g.,

$$(that's, not), (not, bad), (bad, for), \dots \quad [4.1]$$

1787     Bigrams can handle relatively straightforward cases, such as when an adjective is immedi-  
 1788       ately negated; trigrams would be required to extend to larger contexts (e.g., *not the worst*).  
 1789     But this approach will not scale to more complex examples like (4.4) and (4.5). More  
 1790     sophisticated solutions try to account for the syntactic structure of the sentence (Wilson  
 1791     et al., 2005; Socher et al., 2013), or apply more complex classifiers such as **convolutional**  
 1792     **neural networks** (Kim, 2014), which are described in chapter 3.

1793 **4.1.1 Related problems**

1794 **Subjectivity** Closely related to sentiment analysis is **subjectivity detection**, which re-  
1795 quires identifying the parts of a text that express subjective opinions, as well as other non-  
1796 factual content such as speculation and hypotheticals (Riloff and Wiebe, 2003). This can be  
1797 done by treating each sentence as a separate document, and then applying a bag-of-words  
1798 classifier: indeed, Pang and Lee (2004) do exactly this, using a training set consisting of  
1799 (mostly) subjective sentences gathered from movie reviews, and (mostly) objective sen-  
1800 tences gathered from plot descriptions. They augment this bag-of-words model with a  
1801 graph-based algorithm that encourages nearby sentences to have the same subjectivity  
1802 label.

1803 **Stance classification** In debates, each participant takes a side: for example, advocating  
1804 for or against proposals like adopting a vegetarian lifestyle or mandating free college ed-  
1805 ucation. The problem of stance classification is to identify the author’s position from the  
1806 text of the argument. In some cases, there is training data available for each position,  
1807 so that standard document classification techniques can be employed. In other cases, it  
1808 suffices to classify each document as whether it is in support or opposition of the argu-  
1809 ment advanced by a previous document (Anand et al., 2011). In the most challenging  
1810 case, there is no labeled data for any of the stances, so the only possibility is group docu-  
1811 ments that advocate the same position (Somasundaran and Wiebe, 2009). This is a form  
1812 of **unsupervised learning**, discussed in chapter 5.

1813 **Targeted sentiment analysis** The expression of sentiment is often more nuanced than a  
1814 simple binary label. Consider the following examples:

1815 (4.6) The vodka was good, but the meat was rotten.

1816 (4.7) Go to Heaven for the climate, Hell for the company. —Mark Twain

1817 These statements display a mixed overall sentiment: positive towards some entities (e.g.,  
1818 *the vodka*), negative towards others (e.g., *the meat*). **Targeted sentiment analysis** seeks to  
1819 identify the writer’s sentiment towards specific entities (Jiang et al., 2011). This requires  
1820 identifying the entities in the text and linking them to specific sentiment words — much  
1821 more than we can do with the classification-based approaches discussed thus far. For  
1822 example, Kim and Hovy (2006) analyze sentence-internal structure to determine the topic  
1823 of each sentiment expression.

1824 **Aspect-based opinion mining** seeks to identify the sentiment of the author of a review  
1825 towards predefined aspects such as PRICE and SERVICE, or, in the case of (4.7), CLIMATE  
1826 and COMPANY (Hu and Liu, 2004). If the aspects are not defined in advance, it may again  
1827 be necessary to employ **unsupervised learning** methods to identify them (e.g., Branavan  
1828 et al., 2009).

1829 **Emotion classification** While sentiment analysis is framed in terms of positive and neg-  
 1830 ative categories, psychologists generally regard **emotion** as more multifaceted. For ex-  
 1831 ample, Ekman (1992) argues that there are six basic emotions — happiness, surprise, fear,  
 1832 sadness, anger, and contempt — and that they are universal across human cultures. Alm  
 1833 et al. (2005) build a linear classifier for recognizing the emotions expressed in children’s  
 1834 stories. The ultimate goal of this work was to improve text-to-speech synthesis, so that  
 1835 stories could be read with intonation that reflected the emotional content. They used bag-  
 1836 of-words features, as well as features capturing the story type (e.g., jokes, folktales), and  
 1837 structural features that reflect the position of each sentence in the story. The task is diffi-  
 1838 cult: even human annotators frequently disagreed with each other, and the best classifiers  
 1839 achieved accuracy between 60-70%.

#### 1840 4.1.2 Alternative approaches to sentiment analysis

1841 **Regression** A more challenging version of sentiment analysis is to determine not just  
 1842 the class of a document, but its rating on a numerical scale (Pang and Lee, 2005). If the  
 1843 scale is continuous, it is most natural to apply **regression**, identifying a set of weights  $\theta$   
 1844 that minimize the squared error of a predictor  $\hat{y} = \theta \cdot x + b$ , where  $b$  is an offset. This  
 1845 approach is called **linear regression**, and sometimes **least squares**, because the regression  
 1846 coefficients  $\theta$  are determined by minimizing the squared error,  $(y - \hat{y})^2$ . If the weights are  
 1847 regularized using a penalty  $\lambda \|\theta\|_2^2$ , then it is **ridge regression**. Unlike logistic regression,  
 1848 both linear regression and ridge regression can be solved in closed form as a system of  
 1849 linear equations.

1850 **Ordinal ranking** In many problems, the labels are ordered but discrete: for example,  
 1851 product reviews are often integers on a scale of 1 – 5, and grades are on a scale of A – F.  
 1852 Such problems can be solved by discretizing the score  $\theta \cdot x$  into “ranks”,

$$\hat{y} = \underset{r: \theta \cdot x \geq b_r}{\operatorname{argmax}} r, \quad [4.2]$$

1853 where  $\mathbf{b} = [b_1 = -\infty, b_2, b_3, \dots, b_K]$  is a vector of boundaries. It is possible to learn the  
 1854 weights and boundaries simultaneously, using a perceptron-like algorithm (Crammer and  
 1855 Singer, 2001).

1856 **Lexicon-based classification** Sentiment analysis is one of the only NLP tasks where  
 1857 hand-crafted feature weights are still widely employed. In **lexicon-based classification** (Taboada  
 1858 et al., 2011), the user creates a list of words for each label, and then classifies each docu-  
 1859 ment based on how many of the words from each list are present. In our linear classifica-  
 1860 tion framework, this is equivalent to choosing the following weights:

$$\theta_{y,j} = \begin{cases} 1, & j \in \mathcal{L}_y \\ 0, & \text{otherwise,} \end{cases} \quad [4.3]$$

1861 where  $\mathcal{L}_y$  is the lexicon for label  $y$ . Compared to the machine learning classifiers discussed  
 1862 in the previous chapters, lexicon-based classification may seem primitive. However, su-  
 1863 pervised machine learning relies on large annotated datasets, which are time-consuming  
 1864 and expensive to produce. If the goal is to distinguish two or more categories in a new  
 1865 domain, it may be simpler to start by writing down a list of words for each category.

1866 An early lexicon was the *General Inquirer* (Stone, 1966). Today, popular sentiment lex-  
 1867 cons include sentiwordnet (Esuli and Sebastiani, 2006) and an evolving set of lexicons  
 1868 from Liu (2015). For emotions and more fine-grained analysis, *Linguistic Inquiry and Word*  
 1869 *Count* (LIWC) provides a set of lexicons (Tausczik and Pennebaker, 2010). The MPQA lex-  
 1870 icon indicates the polarity (positive or negative) of 8221 terms, as well as whether they are  
 1871 strongly or weakly subjective (Wiebe et al., 2005). A comprehensive comparison of senti-  
 1872 ment lexicons is offered by Ribeiro et al. (2016). Given an initial **seed lexicon**, it is possible  
 1873 to automatically expand the lexicon by looking for words that frequently co-occur with  
 1874 words in the seed set (Hatzivassiloglou and McKeown, 1997; Qiu et al., 2011).

## 1875 4.2 Word sense disambiguation

1876 Consider the the following headlines:

- 1877 (4.8) Iraqi head seeks arms
- 1878 (4.9) Prostitutes appeal to Pope
- 1879 (4.10) Drunk gets nine years in violin case<sup>2</sup>

1880 These headlines are ambiguous because they contain words that have multiple mean-  
 1881 ings, or **senses**. Word sense disambiguation is the problem of identifying the intended  
 1882 sense of each word token in a document. Word sense disambiguation is part of a larger  
 1883 field of research called **lexical semantics**, which is concerned with meanings of the words.

1884 At a basic level, the problem of word sense disambiguation is to identify the correct  
 1885 sense for each word token in a document. Part-of-speech ambiguity (e.g., noun versus  
 1886 verb) is usually considered to be a different problem, to be solved at an earlier stage.  
 1887 From a linguistic perspective, senses are not properties of words, but of **lemmas**, which  
 1888 are canonical forms that stand in for a set of inflected words. For example, *arm*/N is a  
 1889 lemma that includes the inflected form *arms*/N — the /N indicates that it we are refer-  
 1890 ring to the noun, and not its **homonym** *arm*/V, which is another lemma that includes  
 1891 the inflected verbs (*arm*/V, *arms*/V, *armed*/V, *arming*/V). Therefore, word sense disam-  
 1892 biguation requires first identifying the correct part-of-speech and lemma for each token,

---

<sup>2</sup>These examples, and many more, can be found at <http://www.ling.upenn.edu/~beatrice/humor/headlines.html>

1893 and then choosing the correct sense from the inventory associated with the corresponding  
 1894 lemma.<sup>3</sup> (Part-of-speech tagging is discussed in § 8.1.)

1895 **4.2.1 How many word senses?**

1896 Words sometimes have many more than two senses, as exemplified by the word *serve*:

- 1897 • [FUNCTION]: *The tree stump served as a table*
- 1898 • [CONTRIBUTE TO]: *His evasive replies only served to heighten suspicion*
- 1899 • [PROVIDE]: *We serve only the rawest fish*
- 1900 • [ENLIST]: *She served in an elite combat unit*
- 1901 • [JAIL]: *He served six years for a crime he didn't commit*
- 1902 • [LEGAL]: *They were served with subpoenas*<sup>4</sup>

1903 These sense distinctions are annotated in **WordNet** (<http://wordnet.princeton.edu>), a lexical semantic database for English. WordNet consists of roughly 100,000 **synsets**,  
 1904 which are groups of lemmas (or phrases) that are synonymous. An example synset is  
 1905 {*chump*<sup>1</sup>, *fool*<sup>2</sup>, *sucker*<sup>1</sup>, *mark*<sup>9</sup>}, where the superscripts index the sense of each lemma that  
 1906 is included in the synset: for example, there are at least eight other senses of *mark* that  
 1907 have different meanings, and are not part of this synset. A lemma is **polysemous** if it  
 1908 participates in multiple synsets.

1910 WordNet defines the scope of the word sense disambiguation problem, and, more  
 1911 generally, formalizes lexical semantic knowledge of English. (WordNets have been cre-  
 1912 ated for a few dozen other languages, at varying levels of detail.) Some have argued  
 1913 that WordNet's sense granularity is too fine (Ide and Wilks, 2006); more fundamentally,  
 1914 the premise that word senses can be differentiated in a task-neutral way has been criti-  
 1915 cized as linguistically naïve (Kilgarriff, 1997). One way of testing this question is to ask  
 1916 whether people tend to agree on the appropriate sense for example sentences: accord-  
 1917 ing to Mihalcea et al. (2004), people agree on roughly 70% of examples using WordNet  
 1918 senses; far better than chance, but less than agreement on other tasks, such as sentiment  
 1919 annotation (Wilson et al., 2005).

1920 **\*Other lexical semantic relations** Besides **synonymy**, WordNet also describes many  
 1921 other lexical semantic relationships, including:

- 1922 • **antonymy**: *x* means the opposite of *y*, e.g. FRIEND-ENEMY;

---

<sup>3</sup>Navigli (2009) provides a survey of approaches for word-sense disambiguation.

<sup>4</sup>Several of the examples are adapted from WordNet (Fellbaum, 2010).

- **hyponymy:**  $x$  is a special case of  $y$ , e.g. RED-COLOR; the inverse relationship is **hyperonymy**;
- **meronymy:**  $x$  is a part of  $y$ , e.g., WHEEL-BICYCLE; the inverse relationship is **holonymy**.

Classification of these relations can be performed by searching for characteristic patterns between pairs of words, e.g.,  $X$ , *such as*  $Y$ , which signals hyponymy (Hearst, 1992), or  $X$  *but*  $Y$ , which signals antonymy (Hatzivassiloglou and McKeown, 1997). Another approach is to analyze each term's **distributional statistics** (the frequency of its neighboring words). Such approaches are described in detail in chapter 14.

### 4.2.2 Word sense disambiguation as classification

How can we tell living *plants* from manufacturing *plants*? The context is often critical:

- (4.11) Town officials are hoping to attract new manufacturing plants through weakened environmental regulations.
- (4.12) The endangered plants play an important role in the local ecosystem.

It is possible to build a feature vector using the bag-of-words representation, by treating each context as a pseudo-document. The feature function is then,

$$\begin{aligned} f((\text{plant}, \text{The endangered plants play an ...}), y) = \\ \{(the, y) : 1, (\text{endangered}, y) : 1, (\text{play}, y) : 1, (\text{an}, y) : 1, \dots\} \end{aligned}$$

As in document classification, many of these features are irrelevant, but a few are very strong predictors. In this example, the context word *endangered* is a strong signal that the intended sense is biology rather than manufacturing. We would therefore expect a learning algorithm to assign high weight to (*endangered*, BIOLOGY), and low weight to (*endangered*, MANUFACTURING).<sup>5</sup>

It may also be helpful to go beyond the bag-of-words: for example, one might encode the position of each context word with respect to the target, e.g.,

$$\begin{aligned} f((\text{bank}, I \text{ went to the bank to deposit my paycheck}), y) = \\ \{(i - 3, \text{went}, y) : 1, (i + 2, \text{deposit}, y) : 1, (i + 4, \text{paycheck}, y) : 1\} \end{aligned}$$

These are called **collocation features**, and they give more information about the specific role played by each context word. This idea can be taken further by incorporating additional syntactic information about the grammatical role played by each context feature, such as the **dependency path** (see chapter 11).

---

<sup>5</sup>The context bag-of-words can be also used to perform word-sense disambiguation without machine learning: the Lesk (1986) algorithm selects the word sense whose dictionary definition best overlaps the local context.

Using such features, a classifier can be trained from labeled data. A **semantic concordance** is a corpus in which each open-class word (nouns, verbs, adjectives, and adverbs) is tagged with its word sense from the target dictionary or thesaurus. SemCor is a semantic concordance built from 234K tokens of the Brown corpus (Francis and Kucera, 1982), annotated as part of the WordNet project (Fellbaum, 2010). SemCor annotations look like this:

(4.13) As of Sunday<sup>1</sup><sub>N</sub> night<sup>1</sup><sub>N</sub> there was<sup>4</sup><sub>V</sub> no word<sup>2</sup><sub>N</sub> ...,

with the superscripts indicating the annotated sense of each polysemous word, and the subscripts indicating the part-of-speech.

As always, supervised classification is only possible if enough labeled examples can be accumulated. This is difficult in word sense disambiguation, because each polysemous lemma requires its own training set: having a good classifier for the senses of *serve* is no help towards disambiguating *plant*. For this reason, **unsupervised** and **semisupervised** methods are particularly important for word sense disambiguation (e.g., Yarowsky, 1995). These methods will be discussed in chapter 5. Unsupervised methods typically lean on the heuristic of “one sense per discourse”, which means that a lemma will usually have a single, consistent sense throughout any given document (Gale et al., 1992). Based on this heuristic, we can propagate information from high-confidence instances to lower-confidence instances in the same document (Yarowsky, 1995).

## 4.3 Design decisions for text classification

Text classification involves a number of design decisions. In some cases, the design decision is clear from the mathematics: if you are using regularization, then a regularization weight  $\lambda$  must be chosen. Other decisions are more subtle, arising only in the low level “plumbing” code that ingests and processes the raw data. Such decision can be surprisingly consequential for classification accuracy.

### 4.3.1 What is a word?

The bag-of-words representation presupposes that extracting a vector of word counts from text is unambiguous. But text documents are generally represented as sequences of characters (in an encoding such as ascii or unicode), and the conversion to bag-of-words presupposes a definition of the “words” that are to be counted.

#### 4.3.1.1 Tokenization

The first subtask for constructing a bag-of-words vector is **tokenization**: converting the text from a sequence of characters to a sequence of **word tokens**. A simple approach is

<b>Whitespace</b>	Isn't Ahab, Ahab? ;)
<b>Treebank</b>	Is n't Ahab , Ahab ? ; )
<b>Tweet</b>	Isn't Ahab , Ahab ? ;)
<b>TokTok</b> (Dehdari, 2014)	Isn ' t Ahab , Ahab ? ; )

Figure 4.1: The output of four `nltk` tokenizers, applied to the string *Isn't Ahab, Ahab? ;)*

1978 to define a subset of characters as whitespace, and then split the text on these tokens.  
 1979 However, whitespace-based tokenization is not ideal: we may want to split conjunctions  
 1980 like *isn't* and hyphenated phrases like *prize-winning* and *half-asleep*, and we likely want  
 1981 to separate words from commas and periods that immediately follow them. At the same  
 1982 time, it would be better not to split abbreviations like *U.S.* and *Ph.D.* In languages with  
 1983 Roman scripts, tokenization is typically performed using regular expressions, with mod-  
 1984 ules designed to handle each of these cases. For example, the `nltk` package includes a  
 1985 number of tokenizers (Loper and Bird, 2002); the outputs of four of the better-known tok-  
 1986 enizers are shown in Figure 4.1. Social media researchers have found that emoticons and  
 1987 other forms of orthographic variation pose new challenges for tokenization, leading to the  
 1988 development of special purpose tokenizers to handle these phenomena (O'Connor et al.,  
 1989 2010).

1990 Tokenization is a language-specific problem, and each language poses unique chal-  
 1991 lenges. For example, Chinese does not include spaces between words, nor any other  
 1992 consistent orthographic markers of word boundaries. A “greedy” approach is to scan the  
 1993 input for character substrings that are in a predefined lexicon. However, Xue et al. (2003)  
 1994 notes that this can be ambiguous, since many character sequences could be segmented in  
 1995 multiple ways. Instead, he trains a classifier to determine whether each Chinese character,  
 1996 or *hanzi*, is a word boundary. More advanced sequence labeling methods for word seg-  
 1997 mentation are discussed in § 8.4. Similar problems can occur in languages with alphabetic  
 1998 scripts, such as German, which does not include whitespace in compound nouns, yield-  
 1999 ing examples such as *Freundschaftsbezeugungen* (demonstration of friendship) and *Dilett-*  
 2000 *tantenaufdringlichkeiten* (the importunities of dilettantes). As Twain (1997) argues, “*These*  
 2001 *things are not words, they are alphabetic processions.*” Social media raises similar problems  
 2002 for English and other languages, with hashtags such as *#TrueLoveInFourWords* requiring  
 2003 decomposition for analysis (Brun and Roux, 2014).

### 2004 4.3.1.2 Normalization

2005 After splitting the text into tokens, the next question is which tokens are really distinct.  
 2006 Is it necessary to distinguish *great*, *Great*, and *GREAT*? Sentence-initial capitalization may  
 2007 be irrelevant to the classification task. Going further, the complete elimination of case  
 2008 distinctions will result in a smaller vocabulary, and thus smaller feature vectors. However,

<b>Original</b>	The	Williams	sisters	are	leaving	this	tennis	centre
<b>Porter stemmer</b>	the	william	sister	are	leav	thi	tenni	centr
<b>Lancaster stemmer</b>	the	william	sist	ar	leav	thi	ten	cent
<b>WordNet lemmatizer</b>	The	Williams	<b>sister</b>	are	leaving	this	tennis	centre

Figure 4.2: Sample outputs of the Porter (1980) and Lancaster (Paice, 1990) stemmers, and the WordNet lemmatizer

2009 case distinctions might be relevant in some situations: for example, *apple* is a delicious  
 2010 pie filling, while *Apple* is a company that specializes in proprietary dongles and power  
 2011 adapters.

2012 For Roman script, case conversion can be performed using unicode string libraries.  
 2013 Many scripts do not have case distinctions (e.g., the Devanagari script used for South  
 2014 Asian languages, the Thai alphabet, and Japanese kana), and case conversion for all scripts  
 2015 may not be available in every programming environment. (Unicode support is an im-  
 2016 portant distinction between Python’s versions 2 and 3, and is a good reason for mi-  
 2017 grating to Python 3 if you have not already done so. Compare the output of the code  
 2018 "\à l\’hôtel".upper() in the two language versions.)<sup>6</sup>

2019 Case conversion is a type of **normalization**, which refers to string transformations that  
 2020 remove distinctions that are irrelevant to downstream applications (Sproat et al., 2001).  
 2021 Other normalizations include the standardization of numbers (e.g., 1,000 to 1000) and  
 2022 dates (e.g., August 11, 2015 to 2015/11/08). Depending on the application, it may even be  
 2023 worthwhile to convert all numbers and dates to special tokens, !NUM and !DATE. In social  
 2024 media, there are additional orthographic phenomena that may be normalized, such as ex-  
 2025 pressive lengthening, e.g., *coooooool* (Aw et al., 2006; Yang and Eisenstein, 2013). Similarly,  
 2026 historical texts feature spelling variations that may need to be normalized to a contempo-  
 2027 rary standard form (Baron and Rayson, 2008).

2028 A more extreme form of normalization is to eliminate **inflectional affixes**, such as the  
 2029 *-ed* and *-s* suffixes in English. On this view, *bike*, *bikes*, *biking*, and *biked* all refer to the  
 2030 same underlying concept, so they should be grouped into a single feature. A **stemmer** is  
 2031 a program for eliminating affixes, usually by applying a series of regular expression sub-  
 2032 stitutions. Character-based stemming algorithms are necessarily approximate, as shown  
 2033 in Figure 4.2: the Lancaster stemmer incorrectly identifies *-ers* as an inflectional suffix of  
 2034 *sisters* (by analogy to *fix/fixer*), and both stemmers incorrectly identify *-s* as a suffix of *this*  
 2035 and *Williams*. Fortunately, even inaccurate stemming can improve bag-of-words classifi-  
 2036 cation models, by merging related strings and thereby reducing the vocabulary size.

2037 Accurately handling irregular orthography requires word-specific rules. **Lemmatizers**

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<sup>6</sup>[todo: I want to make this a footnote, but can’t figure out how.]

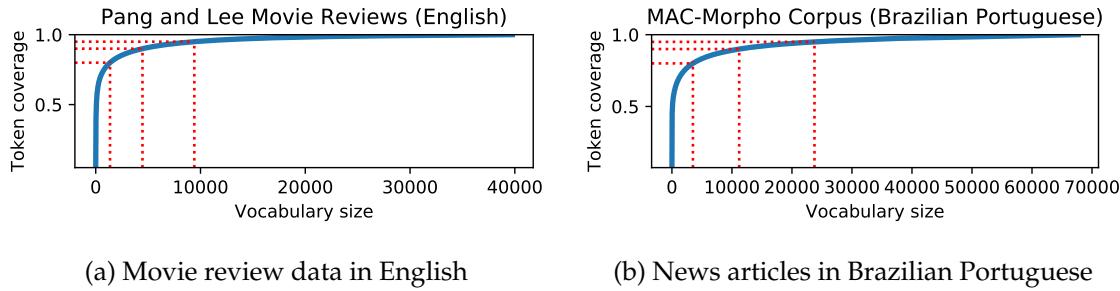


Figure 4.3: Tradeoff between token coverage (y-axis) and vocabulary size, on the `nltk` movie review dataset, after sorting the vocabulary by decreasing frequency. The red dashed lines indicate 80%, 90%, and 95% coverage.

2038 are systems that identify the underlying lemma of a given wordform. They must avoid the  
 2039 over-generalization errors of the stemmers in Figure 4.2, and also handle more complex  
 2040 transformations, such as *geese*→*goose*. The output of the WordNet lemmatizer is shown in  
 2041 the final line of Figure 4.2. Both stemming and lemmatization are language-specific: an  
 2042 English stemmer or lemmatizer is of little use on a text written in another language. The  
 2043 discipline of **morphology** relates to the study of word-internal structure, and is described  
 2044 in more detail in § 9.1.2.

2045 The value of normalization depends on the data and the task. Normalization re-  
 2046 duces the size of the feature space, which can help in generalization. However, there  
 2047 is always the risk of merging away linguistically meaningful distinctions. In supervised  
 2048 machine learning, regularization and smoothing can play a similar role to normalization  
 2049 — preventing the learner from overfitting to rare features — while avoiding the language-  
 2050 specific engineering required for accurate normalization. In unsupervised scenarios, such  
 2051 as content-based information retrieval (Manning et al., 2008) and topic modeling (Blei  
 2052 et al., 2003), normalization is more critical.

### 2053 4.3.2 How many words?

2054 Limiting the size of the feature vector reduces the memory footprint of the resulting mod-  
 2055 els, and increases the speed of prediction. Normalization can help to play this role, but  
 2056 a more direct approach is simply to limit the vocabulary to the  $N$  most frequent words  
 2057 in the dataset. For example, in the `movie-reviews` dataset provided with `nltk` (orig-  
 2058 inally from Pang et al., 2002), there are 39,768 word types, and 1.58M tokens. As shown  
 2059 in Figure 4.3a, the most frequent 4000 word types cover 90% of all tokens, offering an  
 2060 order-of-magnitude reduction in the model size. Such ratios are language-specific: in for  
 2061 example, in the Brazilian Portuguese Mac-Morpho corpus (Aluísio et al., 2003), attain-  
 2062 ing 90% coverage requires more than 10000 word types (Figure 4.3b). This reflects the

2063 morphological complexity of Portuguese, which includes many more inflectional suffixes  
 2064 than English.

2065 Eliminating rare words is not always advantageous for classification performance: for  
 2066 example, names, which are typically rare, play a large role in distinguishing topics of news  
 2067 articles. Another way to reduce the size of the feature space is to eliminate **stopwords** such  
 2068 as *the*, *to*, and *and*, which may seem to play little role in expressing the topic, sentiment,  
 2069 or stance. This is typically done by creating a **stoplist** (e.g., `nltk.corpus.stopwords`),  
 2070 and then ignoring all terms that match the list. However, corpus linguists and social psy-  
 2071 chologists have shown that seemingly inconsequential words can offer surprising insights  
 2072 about the author or nature of the text (Biber, 1991; Chung and Pennebaker, 2007). Further-  
 2073 more, high-frequency words are unlikely to cause overfitting in discriminative classifiers.  
 2074 As with normalization, stopword filtering is more important for unsupervised problems,  
 2075 such as term-based document retrieval.

2076 Another alternative for controlling model size is **feature hashing** (Weinberger et al.,  
 2077 2009). Each feature is assigned an index using a hash function. If a hash function that  
 2078 permits collisions is chosen (typically by taking the hash output modulo some integer),  
 2079 then the model can be made arbitrarily small, as multiple features share a single weight.  
 2080 Because most features are rare, accuracy is surprisingly robust to such collisions (Ganchev  
 2081 and Dredze, 2008).

### 2082 4.3.3 Count or binary?

2083 Finally, we may consider whether we want our feature vector to include the *count* of each  
 2084 word, or its *presence*. This gets at a subtle limitation of linear classification: it's worse to  
 2085 have two *failures* than one, but is it really twice as bad? Motivated by this intuition, Pang  
 2086 et al. (2002) use binary indicators of presence or absence in the feature vector:  $f_j(x, y) \in$   
 2087  $\{0, 1\}$ . They find that classifiers trained on these binary vectors tend to outperform feature  
 2088 vectors based on word counts. One explanation is that words tend to appear in clumps:  
 2089 if a word has appeared once in a document, it is likely to appear again (Church, 2000).  
 2090 These subsequent appearances can be attributed to this tendency towards repetition, and  
 2091 thus provide little additional information about the class label of the document.

## 2092 4.4 Evaluating classifiers

2093 In any supervised machine learning application, it is critical to reserve a held-out test set.  
 2094 This data should be used for only one purpose: to evaluate the overall accuracy of a single  
 2095 classifier. Using this data more than once would cause the estimated accuracy to be overly  
 2096 optimistic, because the classifier would be customized to this data, and would not perform  
 2097 as well as on unseen data in the future. It is usually necessary to set hyperparameters or

2098 perform feature selection, so you may need to construct a **tuning** or **development set** for  
 2099 this purpose, as discussed in § 2.1.5.

2100 There are a number of ways to evaluate classifier performance. The simplest is **accuracy**:  
 2101 the number of correct predictions, divided by the total number of instances,

$$\text{acc}(\mathbf{y}, \hat{\mathbf{y}}) = \frac{1}{N} \sum_i^N \delta(y^{(i)} = \hat{y}). \quad [4.4]$$

2102 Exams are usually graded by accuracy. Why are other metrics necessary? The main  
 2103 reason is **class imbalance**. Suppose you are building a classifier to detect whether an  
 2104 electronic health record (EHR) describes symptoms of a rare disease, which appears in  
 2105 only 1% of all documents in the dataset. A classifier that reports  $\hat{y} = \text{NEGATIVE}$  for  
 2106 all documents would achieve 99% accuracy, but would be practically useless. We need  
 2107 metrics that are capable of detecting the classifier's ability to discriminate between classes,  
 2108 even when the distribution is skewed.

2109 One solution is to build a **balanced test set**, in which each possible label is equally rep-  
 2110 resented. But in the EHR example, this would mean throwing away 98% of the original  
 2111 dataset! Furthermore, the detection threshold itself might be a design consideration: in  
 2112 health-related applications, we might prefer a very sensitive classifier, which returned a  
 2113 positive prediction if there is even a small chance that  $y^{(i)} = \text{POSITIVE}$ . In other applica-  
 2114 tions, a positive result might trigger a costly action, so we would prefer a classifier that  
 2115 only makes positive predictions when absolutely certain. We need additional metrics to  
 2116 capture these characteristics.

#### 2117 4.4.1 Precision, recall, and F-MEASURE

2118 For any label (e.g., positive for presence of symptoms of a disease), there are two possible  
 2119 errors:

- 2120 • **False positive**: the system incorrectly predicts the label.
- 2121 • **False negative**: the system incorrectly fails to predict the label.

2122 Similarly, for any label, there are two ways to be correct:

- 2123 • **True positive**: the system correctly predicts the label.
- 2124 • **True negative**: the system correctly predicts that the label does not apply to this  
 2125 instance.

Classifiers that make a lot of false positives are too sensitive; classifiers that make a  
 lot of false negatives are not sensitive enough. These two conditions are captured by the

metrics of **recall** and **precision**:

$$\text{RECALL}(\mathbf{y}, \hat{\mathbf{y}}, k) = \frac{\text{TP}}{\text{TP} + \text{FN}} \quad [4.5]$$

$$\text{PRECISION}(\mathbf{y}, \hat{\mathbf{y}}, k) = \frac{\text{TP}}{\text{TP} + \text{FP}}. \quad [4.6]$$

Recall and precision are both conditional likelihoods of a correct prediction, which is why their numerators are the same. Recall is conditioned on  $k$  being the correct label,  $y^{(i)} = k$ , so the denominator sums over true positive and false negatives. Precision is conditioned on  $k$  being the prediction, so the denominator sums over true positives and false positives. Note that true negatives are not considered in either statistic. The classifier that labels every document as “negative” would achieve zero recall; precision would be  $\frac{0}{0}$ .

Recall and precision are complementary. A high-recall classifier is preferred when false positives are cheaper than false negatives: for example, in a preliminary screening for symptoms of a disease, the cost of a false positive might be an additional test, while a false negative would result in the disease going untreated. Conversely, a high-precision classifier is preferred when false positives are more expensive: for example, in spam detection, a false negative is a relatively minor inconvenience, while a false positive might mean that an important message goes unread.

The ***F*-MEASURE** combines recall and precision into a single metric, using the harmonic mean:

$$\text{F-MEASURE}(\mathbf{y}, \hat{\mathbf{y}}, k) = \frac{2rp}{r + p}, \quad [4.7]$$

where  $r$  is recall and  $p$  is precision.<sup>7</sup>

**Evaluating multi-class classification** Recall, precision, and ***F*-MEASURE** are defined with respect to a specific label  $k$ . When there are multiple labels of interest (e.g., in word sense disambiguation or emotion classification), it is necessary to combine the ***F*-MEASURE** across each class. **Macro *F*-MEASURE** is the average ***F*-MEASURE** across several classes,

$$\text{Macro-}F(\mathbf{y}, \hat{\mathbf{y}}) = \frac{1}{|\mathcal{K}|} \sum_{k \in \mathcal{K}} \text{F-MEASURE}(\mathbf{y}, \hat{\mathbf{y}}, k) \quad [4.8]$$

In multi-class problems with unbalanced class distributions, the macro ***F*-MEASURE** is a balanced measure of how well the classifier recognizes each class. In **micro *F*-MEASURE**, we compute true positives, false positives, and false negatives for each class, and then add them up to compute a single recall, precision, and ***F*-MEASURE**. This metric is balanced across instances rather than classes, so it weights each class in proportion to its frequency — unlike macro ***F*-MEASURE**, which weights each class equally.

---

<sup>7</sup> $F$ -MEASURE is sometimes called  $F_1$ , and generalizes to  $F_\beta = \frac{(1+\beta^2)rp}{\beta^2p+r}$ . The  $\beta$  parameter can be tuned to emphasize recall or precision.

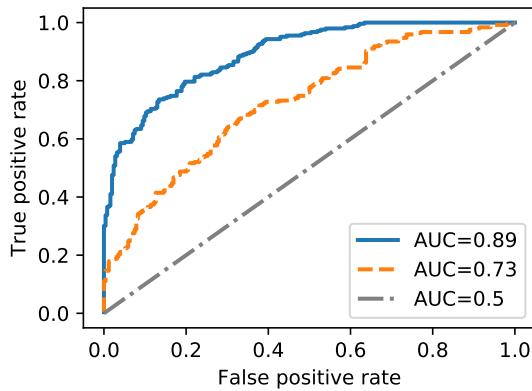


Figure 4.4: ROC curves for three classifiers of varying discriminative power, measured by AUC (area under the curve)

#### 2146 4.4.2 Threshold-free metrics

2147 In binary classification problems, it is possible to trade off between recall and precision by  
 2148 adding a constant “threshold” to the output of the scoring function. This makes it possible  
 2149 to trace out a curve, where each point indicates the performance at a single threshold. In  
 2150 the **receiver operating characteristic (ROC)** curve,<sup>8</sup> the *x*-axis indicates the **false positive**  
 2151 **rate**,  $\frac{FP}{FP+TN}$ , and the *y*-axis indicates the recall, or **true positive rate**. A perfect classifier  
 2152 attains perfect recall without any false positives, tracing a “curve” from the origin (0,0) to  
 2153 the upper left corner (0,1), and then to (1,1). In expectation, a non-discriminative classifier  
 2154 traces a diagonal line from the origin (0,0) to the upper right corner (1,1). Real classifiers  
 2155 tend to fall between these two extremes. Examples are shown in Figure 4.4.

2156 The ROC curve can be summarized in a single number by taking its integral, the **area**  
 2157 **under the curve (AUC)**. The AUC can be interpreted as the probability that a randomly-  
 2158 selected positive example will be assigned a higher score by the classifier than a randomly-  
 2159 selected negative example. A perfect classifier has AUC = 1 (all positive examples score  
 2160 higher than all negative examples); a non-discriminative classifier has AUC = 0.5 (given  
 2161 a randomly selected positive and negative example, either could score higher with equal  
 2162 probability); a perfectly wrong classifier would have AUC = 0 (all negative examples score  
 2163 higher than all positive examples). One advantage of AUC in comparison to *F*-MEASURE  
 2164 is that the baseline rate of 0.5 does not depend on the label distribution.

---

<sup>8</sup>The name “receiver operator characteristic” comes from the metric’s origin in signal processing applications (Peterson et al., 1954). Other threshold-free metrics include **precision-recall curves**, **precision-at-*k***, and **balanced *F*-MEASURE**; see Manning et al. (2008) for more details.

2165 **4.4.3 Classifier comparison and statistical significance**

2166 Natural language processing research and engineering often involves comparing different  
 2167 classification techniques. In some cases, the comparison is between algorithms, such as  
 2168 logistic regression versus averaged perceptron, or  $L_2$  regularization versus  $L_1$ . In other  
 2169 cases, the comparison is between feature sets, such as the bag-of-words versus positional  
 2170 bag-of-words (see § 4.2.2). **Ablation testing** involves systematically removing (ablating)  
 2171 various aspects of the classifier, such as feature groups, and testing the **null hypothesis**  
 2172 that the ablated classifier is as good as the full model.

2173 A full treatment of hypothesis testing is beyond the scope of this text, but this section  
 2174 contains a brief summary of the techniques necessary to compare classifiers. The main  
 2175 aim of hypothesis testing is to determine whether the difference between two statistics  
 2176 — for example, the accuracies of two classifiers — is likely to arise by chance. We will  
 2177 be concerned with chance fluctuations that arise due to the finite size of the test set.<sup>9</sup> An  
 2178 improvement of 10% on a test set with ten instances may reflect a random fluctuation that  
 2179 makes the test set more favorable to classifier  $c_1$  than  $c_2$ ; on another test set with a different  
 2180 ten instances, we might find that  $c_2$  does better than  $c_1$ . But if we observe the same 10%  
 2181 improvement on a test set with 1000 instances, this is highly unlikely to be explained  
 2182 by chance. Such a finding is said to be **statistically significant** at a level  $p$ , which is the  
 2183 probability of observing an effect of equal or greater magnitude when the null hypothesis  
 2184 is true. The notation  $p < .05$  indicates that the likelihood of an equal or greater effect is  
 2185 less than 5%, assuming the null hypothesis is true.<sup>10</sup>

2186 **4.4.3.1 The binomial test**

2187 The statistical significance of a difference in accuracy can be evaluated using classical tests,  
 2188 such as the **binomial test**.<sup>11</sup> Suppose that classifiers  $c_1$  and  $c_2$  disagree on  $N$  instances in a  
 2189 test set with binary labels, and that  $c_1$  is correct on  $k$  of those instances. Under the null hy-  
 2190 pothesis that the classifiers are equally accurate, we would expect  $k/N$  to be roughly equal  
 2191 to 1/2, and as  $N$  increases,  $k/N$  should be increasingly close to this expected value. These  
 2192 properties are captured by the **binomial distribution**, which is a probability over counts

---

<sup>9</sup>Other sources of variance include the initialization of non-convex classifiers such as neural networks, and the ordering of instances in online learning such as stochastic gradient descent and perceptron.

<sup>10</sup>Statistical hypothesis testing is useful only to the extent that the existing test set is representative of the instances that will be encountered in the future. If, for example, the test set is constructed from news documents, no hypothesis test can predict which classifier will perform best on documents from another domain, such as electronic health records.

<sup>11</sup>A well-known alternative to the binomial test is **McNemar's test**, which computes a **test statistic** based on the number of examples that are correctly classified by one system and incorrectly classified by the other. The null hypothesis distribution for this test statistic is known to be drawn from a chi-squared distribution with a single degree of freedom, so a  $p$ -value can be computed from the cumulative density function of this distribution (Dietterich, 1998). Both tests give similar results in most circumstances, but the binomial test is easier to understand from first principles.

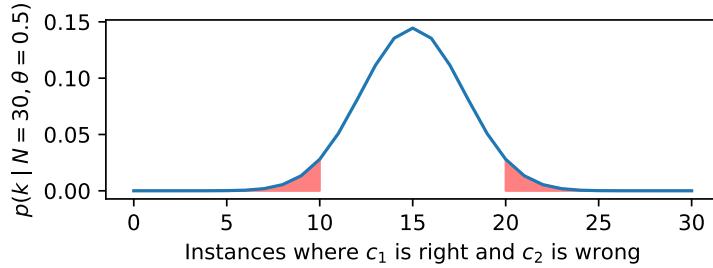


Figure 4.5: Probability mass function for the binomial distribution. The pink highlighted areas represent the cumulative probability for a significance test on an observation of  $k = 10$  and  $N = 30$ .

of binary random variables. We write  $k \sim \text{Binom}(\theta, N)$  to indicate that  $k$  is drawn from a binomial distribution, with parameter  $N$  indicating the number of random “draws”, and  $\theta$  indicating the probability of “success” on each draw. Each draw is an example on which the two classifiers disagree, and a “success” is a case in which  $c_1$  is right and  $c_2$  is wrong. (The label space is assumed to be binary, so if the classifiers disagree, exactly one of them is correct. The test can be generalized to multi-class classification by focusing on the examples in which exactly one classifier is correct.)

The probability mass function (PMF) of the binomial distribution is,

$$p_{\text{Binom}}(k; N, \theta) = \binom{N}{k} \theta^k (1 - \theta)^{N-k}, \quad [4.9]$$

with  $\theta^k$  representing the probability of the  $k$  successes,  $(1 - \theta)^{N-k}$  representing the probability of the  $N - k$  unsuccessful draws. The expression  $\binom{N}{k} = \frac{N!}{k!(N-k)!}$  is a binomial coefficient, representing the number of possible orderings of events; this ensures that the distribution sums to one over all  $k \in \{0, 1, 2, \dots, N\}$ .

Under the null hypothesis, when the classifiers disagree, each classifier is equally likely to be right, so  $\theta = \frac{1}{2}$ . Now suppose that among  $N$  disagreements,  $c_1$  is correct  $k < \frac{N}{2}$  times. The probability of  $c_1$  being correct  $k$  or fewer times is the **one-tailed p-value**, because it is computed from the area under the binomial probability mass function from 0 to  $k$ , as shown in the left tail of Figure 4.5. This **cumulative probability** is computed as a sum over all values  $i \leq k$ ,

$$\Pr_{\text{Binom}} \left( \text{count}(\hat{y}_2^{(i)} = y^{(i)} \neq \hat{y}_1^{(i)}) \leq k; N, \theta = \frac{1}{2} \right) = \sum_{i=0}^k p_{\text{Binom}} \left( i; N, \theta = \frac{1}{2} \right). \quad [4.10]$$

The one-tailed p-value applies only to the asymmetric null hypothesis that  $c_1$  is at least as accurate as  $c_2$ . To test the **two-tailed** null hypothesis that  $c_1$  and  $c_2$  are equally accu-

---

**Algorithm 7** Bootstrap sampling for classifier evaluation. The original test set is  $\{\mathbf{x}^{(1:N)}, \mathbf{y}^{(1:N)}\}$ , the metric is  $\delta(\cdot)$ , and the number of samples is  $M$ .

---

```

procedure BOOTSTRAP-SAMPLE( $\mathbf{x}^{(1:N)}, \mathbf{y}^{(1:N)}, \delta(\cdot), M$ )
    for  $t \in \{1, 2, \dots, M\}$  do
        for  $i \in \{1, 2, \dots, N\}$  do
             $j \sim \text{UniformInteger}(1, N)$ 
             $\tilde{\mathbf{x}}^{(i)} \leftarrow \mathbf{x}^{(j)}$ 
             $\tilde{\mathbf{y}}^{(i)} \leftarrow \mathbf{y}^{(j)}$ 
             $d^{(t)} \leftarrow \delta(\tilde{\mathbf{x}}^{(1:N)}, \tilde{\mathbf{y}}^{(1:N)})$ 
    return  $\{d^{(t)}\}_{t=1}^M$ 
```

---

2207 rate, we would take the sum of one-tailed  $p$ -values, where the second term is computed  
 2208 from the right tail of Figure 4.5. The binomial distribution is symmetric, so this can be  
 2209 computed by simply doubling the one-tailed  $p$ -value.

2210 Two-tailed tests are more stringent, but they are necessary in cases in which there is  
 2211 no prior intuition about whether  $c_1$  or  $c_2$  is better. For example, in comparing logistic  
 2212 regression versus averaged perceptron, a two-tailed test is appropriate. In an ablation  
 2213 test,  $c_2$  may contain a superset of the features available to  $c_1$ . If the additional features are  
 2214 thought to be likely to improve performance, then a one-tailed test would be appropriate,  
 2215 if chosen in advance. However, such a test can only prove that  $c_2$  is more accurate than  
 2216  $c_1$ , and not the reverse.

2217 **4.4.3.2 \*Randomized testing**

2218 The binomial test is appropriate for accuracy, but not for more complex metrics such as  
 2219  $F$ -MEASURE. To compute statistical significance for arbitrary metrics, we can apply ran-  
 2220 domization. Specifically, draw a set of  $M$  **bootstrap samples** (Efron and Tibshirani, 1993),  
 2221 by resampling instances from the original test set with replacement. Each bootstrap sam-  
 2222 ple is itself a test set of size  $N$ . Some instances from the original test set will not appear  
 2223 in any given bootstrap sample, while others will appear multiple times; but overall, the  
 2224 sample will be drawn from the same distribution as the original test set. We can then com-  
 2225 pute any desired evaluation on each bootstrap sample, which gives a distribution over the  
 2226 value of the metric. Algorithm 7 shows how to perform this computation.

2227 To compare the  $F$ -MEASURE of two classifiers  $c_1$  and  $c_2$ , we set the function  $\delta(\cdot)$  to  
 2228 compute the difference in  $F$ -MEASURE on the bootstrap sample. If the difference is less  
 2229 than or equal to zero in at least 5% of the samples, then we cannot reject the one-tailed  
 2230 null hypothesis that  $c_2$  is at least as good as  $c_1$  (Berg-Kirkpatrick et al., 2012). We may  
 2231 also be interested in the 95% **confidence interval** around a metric of interest, such as  
 2232 the  $F$ -MEASURE of a single classifier. This can be computed by sorting the output of

2233 Algorithm 7, and then setting the top and bottom of the 95% confidence interval to the  
2234 values at the 2.5% and 97.5% percentiles of the sorted outputs. Alternatively, you can fit  
2235 a normal distribution to the set of differences across bootstrap samples, and compute a  
2236 Gaussian confidence interval from the mean and variance.

2237 As the number of bootstrap samples goes to infinity,  $M \rightarrow \infty$ , the bootstrap estimate  
2238 is increasingly accurate. A typical choice for  $M$  is  $10^4$  or  $10^5$ ; larger numbers of samples  
2239 are necessary for smaller  $p$ -values. One way to validate your choice of  $M$  is to run the test  
2240 multiple times, and ensure that the  $p$ -values are similar; if not, increase  $M$  by an order of  
2241 magnitude. This is a heuristic measure of the **variance** of the test, which can decrease  
2242 with the square root  $\sqrt{M}$  (Robert and Casella, 2013).

#### 2243 4.4.4 \*Multiple comparisons

2244 Sometimes it is necessary to perform multiple hypothesis tests, such as when compar-  
2245 ing the performance of several classifiers on multiple datasets. Suppose you have five  
2246 datasets, and you compare four versions of your classifier against a baseline system, for a  
2247 total of 20 comparisons. Even if none of your classifiers is better than the baseline, there  
2248 will be some chance variation in the results, and in expectation you will get one statis-  
2249 tically significant improvement at  $p = 0.05 = \frac{1}{20}$ . It is therefore necessary to adjust the  
2250  $p$ -values when reporting the results of multiple comparisons.

2251 One approach is to require a threshold of  $\frac{\alpha}{m}$  to report a  $p$  value of  $p < \alpha$  when per-  
2252 forming  $m$  tests. This is known as the **Bonferroni correction**, and it limits the overall  
2253 probability of incorrectly rejecting the null hypothesis at  $\alpha$ . Another approach is to bound  
2254 the **false discovery rate** (FDR), which is the fraction of null hypothesis rejections that are  
2255 incorrect. Benjamini and Hochberg (1995) propose a  $p$ -value correction that bounds the  
2256 fraction of false discoveries at  $\alpha$ : sort the  $p$ -values of each individual test in ascending  
2257 order, and set the significance threshold equal to largest  $k$  such that  $p_k \leq \frac{k}{m}\alpha$ . If  $k > 1$ , the  
2258 FDR adjustment is more permissive than the Bonferroni correction.

## 2259 4.5 Building datasets

2260 Sometimes, if you want to build a classifier, you must first build a dataset of your own.  
2261 This includes selecting a set of documents or instances to annotate, and then performing  
2262 the annotations. The scope of the dataset may be determined by the application: if you  
2263 want to build a system to classify electronic health records, then you must work with a  
2264 corpus of records of the type that your classifier will encounter when deployed. In other  
2265 cases, the goal is to build a system that will work across a broad range of documents. In  
2266 this case, it is best to have a *balanced* corpus, with contributions from many styles and  
2267 genres. For example, the Brown corpus draws from texts ranging from government doc-  
2268 uments to romance novels (Francis, 1964), and the Google Web Treebank includes an-

2269 notations for five “domains” of web documents: question answers, emails, newsgroups,  
2270 reviews, and blogs (Petrov and McDonald, 2012).

### 2271 4.5.1 Metadata as labels

2272 Annotation is difficult and time-consuming, and most people would rather avoid it. It  
2273 is sometimes possible to exploit existing metadata to obtain labels for training a classi-  
2274 fier. For example, reviews are often accompanied by a numerical rating, which can be  
2275 converted into a classification label (see § 4.1). Similarly, the nationalities of social media  
2276 users can be estimated from their profiles (Dredze et al., 2013) or even the time zones of  
2277 their posts (Gouws et al., 2011). More ambitiously, we may try to classify the political af-  
2278 filiations of social media profiles based on their social network connections to politicians  
2279 and major political parties (Rao et al., 2010).

2280 The convenience of quickly constructing large labeled datasets without manual an-  
2281 notation is appealing. However this approach relies on the assumption that unlabeled  
2282 instances — for which metadata is unavailable — will be similar to labeled instances.  
2283 Consider the example of labeling the political affiliation of social media users based on  
2284 their network ties to politicians. If a classifier attains high accuracy on such a test set,  
2285 is it safe to assume that it accurately predicts the political affiliation of all social media  
2286 users? Probably not. Social media users who establish social network ties to politicians  
2287 may be more likely to mention politics in the text of their messages, as compared to the  
2288 average user, for whom no political metadata is available. If so, the accuracy on a test set  
2289 constructed from social network metadata would give an overly optimistic picture of the  
2290 method’s true performance on unlabeled data.

### 2291 4.5.2 Labeling data

2292 In many cases, there is no way to get ground truth labels other than manual annotation.  
2293 An annotation protocol should satisfy several criteria: the annotations should be *expressive*  
2294 enough to capture the phenomenon of interest; they should be *replicable*, meaning that  
2295 another annotator or team of annotators would produce very similar annotations if given  
2296 the same data; and they should be *scalable*, so that they can be produced relatively quickly.  
2297 Hovy and Lavid (2010) propose a structured procedure for obtaining annotations that  
2298 meet these criteria, which is summarized below.

- 2299 1. **Determine what the annotations are to include.** This is usually based on some  
2300 theory of the underlying phenomenon: for example, if the goal is to produce an-  
2301 notations about the emotional state of a document’s author, one should start with a  
2302 theoretical account of the types or dimensions of emotion (e.g., Mohammad and Tur-  
2303 ney, 2013). At this stage, the tradeoff between expressiveness and scalability should

2304 be considered: a full instantiation of the underlying theory might be too costly to  
2305 annotate at scale, so reasonable approximations should be considered.

- 2306 2. Optionally, one may **design or select a software tool to support the annotation**  
2307 **effort**. Existing general-purpose annotation tools include BRAT (Stenetorp et al.,  
2308 2012) and MMAX2 (Müller and Strube, 2006).
- 2309 3. **Formalize the instructions for the annotation task.** To the extent that the instruc-  
2310 tions are not explicit, the resulting annotations will depend on the intuitions of the  
2311 annotators. These intuitions may not be shared by other annotators, or by the users  
2312 of the annotated data. Therefore explicit instructions are critical to ensuring the an-  
2313 notations are replicable and usable by other researchers.
- 2314 4. **Perform a pilot annotation** of a small subset of data, with multiple annotators for  
2315 each instance. This will give a preliminary assessment of both the replicability and  
2316 scalability of the current annotation instructions. Metrics for computing the rate of  
2317 agreement are described below. Manual analysis of specific disagreements should  
2318 help to clarify the instructions, and may lead to modifications of the annotation task  
2319 itself. For example, if two labels are commonly conflated by annotators, it may be  
2320 best to merge them.
- 2321 5. **Annotate the data.** After finalizing the annotation protocol and instructions, the  
2322 main annotation effort can begin. Some, if not all, of the instances should receive  
2323 multiple annotations, so that inter-annotator agreement can be computed. In some  
2324 annotation projects, instances receive many annotations, which are then aggregated  
2325 into a “consensus” label (e.g., Danescu-Niculescu-Mizil et al., 2013). However, if the  
2326 annotations are time-consuming or require significant expertise, it may be preferable  
2327 to maximize scalability by obtaining multiple annotations for only a small subset of  
2328 examples.
- 2329 6. **Compute and report inter-annotator agreement, and release the data.** In some  
2330 cases, the raw text data cannot be released, due to concerns related to copyright or  
2331 privacy. In these cases, one solution is to publicly release **stand-off annotations**,  
2332 which contain links to document identifiers. The documents themselves can be re-  
2333 leased under the terms of a licensing agreement, which can impose conditions on  
2334 how the data is used. It is important to think through the potential consequences of  
2335 releasing data: people may make personal data publicly available without realizing  
2336 that it could be redistributed in a dataset and publicized far beyond their expecta-  
2337 tions (boyd and Crawford, 2012).

2338 **4.5.2.1 Measuring inter-annotator agreement**

2339 To measure the replicability of annotations, a standard practice is to compute the extent to  
 2340 which annotators agree with each other. If the annotators frequently disagree, this casts  
 2341 doubt on either their reliability or on the annotation system itself. For classification, one  
 2342 can compute the frequency with which the annotators agree; for rating scales, one can  
 2343 compute the average distance between ratings. These raw agreement statistics must then  
 2344 be compared with the rate of **chance agreement** — the level of agreement that would be  
 2345 obtained between two annotators who ignored the data.

2346 **Cohen's Kappa** is widely used for quantifying the agreement on discrete labeling  
 2347 tasks (Cohen, 1960; Carletta, 1996),<sup>12</sup>

$$\kappa = \frac{\text{agreement} - E[\text{agreement}]}{1 - E[\text{agreement}]}. \quad [4.11]$$

2348 The numerator is the difference between the observed agreement and the chance agree-  
 2349 ment, and the denominator is the difference between perfect agreement and chance agree-  
 2350 ment. Thus,  $\kappa = 1$  when the annotators agree in every case, and  $\kappa = 0$  when the annota-  
 2351 tors agree only as often as would happen by chance. Various heuristic scales have been  
 2352 proposed for determining when  $\kappa$  indicates “moderate”, “good”, or “substantial” agree-  
 2353 ment; for reference, Lee and Narayanan (2005) report  $\kappa \approx 0.45 - 0.47$  for annotations  
 2354 of emotions in spoken dialogues, which they describe as “moderate agreement”; Stolcke  
 2355 et al. (2000) report  $\kappa = 0.8$  for annotations of **dialogue acts**, which are labels for the pur-  
 2356 pose of each turn in a conversation.

2357 When there are two annotators, the expected chance agreement is computed as,

$$E[\text{agreement}] = \sum_k \hat{\Pr}(Y = k)^2, \quad [4.12]$$

2358 where  $k$  is a sum over labels, and  $\hat{\Pr}(Y = k)$  is the empirical probability of label  $k$  across  
 2359 all annotations. The formula is derived from the expected number of agreements if the  
 2360 annotations were randomly shuffled. Thus, in a binary labeling task, if one label is applied  
 2361 to 90% of instances, chance agreement is  $.9^2 + .1^2 = .82$ .

2362 **4.5.2.2 Crowdsourcing**

2363 Crowdsourcing is often used to rapidly obtain annotations for classification problems.  
 2364 For example, **Amazon Mechanical Turk** makes it possible to define “human intelligence  
 2365 tasks (hits)”, such as labeling data. The researcher sets a price for each set of annotations  
 2366 and a list of minimal qualifications for annotators, such as their native language and their

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<sup>12</sup> For other types of annotations, Krippendorff's alpha is a popular choice (Hayes and Krippendorff, 2007; Artstein and Poesio, 2008).

2367 satisfaction rate on previous tasks. The use of relatively untrained “crowdworkers” con-  
 2368 trasts with earlier annotation efforts, which relied on professional linguists (Marcus et al.,  
 2369 1993). However, crowdsourcing has been found to produce reliable annotations for many  
 2370 language-related tasks (Snow et al., 2008). Crowdsourcing is part of the broader field of  
 2371 **human computation** (Law and Ahn, 2011).

## 2372 Additional resources

2373 Many of the preprocessing issues discussed in this chapter also arise in information re-  
 2374 trieval. See (Manning et al., 2008, chapter 2) for discussion of tokenization and related  
 2375 algorithms.

## 2376 Exercises

2377 1. As noted in § 4.3.3, words tend to appear in clumps, with subsequent occurrences  
 2378 of a word being more probable. More concretely, if word  $j$  has probability  $\phi_{y,j}$   
 2379 of appearing in a document with label  $y$ , then the probability of two appearances  
 2380 ( $x_j^{(i)} = 2$ ) is greater than  $\phi_{y,j}^2$ .

2381 Suppose you are applying Naïve Bayes to a binary classification. Focus on a word  $j$   
 2382 which is more probable under label  $y = 1$ , so that,

$$\Pr(w = j \mid y = 1) > \Pr(w = j \mid y = 0). \quad [4.13]$$

2383 Now suppose that  $x_j^{(i)} > 1$ . All else equal, will the classifier overestimate or under-  
 2384 estimate the posterior  $\Pr(y = 1 \mid x)$ ?

2385 2. Prove that F-measure is never greater than the arithmetic mean of recall and pre-  
 2386 cision,  $\frac{r+p}{2}$ . Your solution should also show that F-measure is equal to  $\frac{r+p}{2}$  iff  $r = p$ .

2387 3. Given a binary classification problem in which the probability of the “positive” label  
 2388 is equal to  $\alpha$ , what is the expected *F*-MEASURE of a random classifier which ignores  
 2389 the data, and selects  $\hat{y} = +1$  with probability  $\frac{1}{2}$ ? (Assume that  $p(\hat{y}) \perp p(y)$ .) What is  
 2390 the expected *F*-MEASURE of a classifier that selects  $\hat{y} = +1$  with probability  $\alpha$  (also  
 2391 independent of  $y^{(i)}$ )? Depending on  $\alpha$ , which random classifier will score better?

2392 4. Suppose that binary classifiers  $c_1$  and  $c_2$  disagree on  $N = 30$  cases, and that  $c_1$  is  
 2393 correct in  $k = 10$  of those cases.

- 2394 • Write a program that uses primitive functions such as `exp` and `factorial` to com-  
 2395 pute the **two-tailed** *p*-value — you may use an implementation of the “choose”  
 2396 function if one is available. Verify your code against the output of a library for

- 2397 computing the binomial test or the binomial CDF, such as `scipy.stats.binom`  
 2398 in Python.
- 2399 • Then use a randomized test to try to obtain the same  $p$ -value. In each sample,  
 2400 draw from a binomial distribution with  $N = 30$  and  $\theta = \frac{1}{2}$ . Count the fraction  
 2401 of samples in which  $k \leq 10$ . This is the one-tailed  $p$ -value; double this to  
 2402 compute the two-tailed  $p$ -value.
  - 2403 • Try this with varying numbers of bootstrap samples:  $M \in \{100, 1000, 5000, 10000\}$ .  
 2404 For  $M = 100$  and  $M = 1000$ , run the test 10 times, and plot the resulting  $p$ -  
 2405 values.
  - 2406 • Finally, perform the same tests for  $N = 70$  and  $k = 25$ .
- 2407 5. SemCor 3.0 is a labeled dataset for word sense disambiguation. You can download  
 2408 it,<sup>13</sup> or access it in `nltk.corpora.semcor`.
- 2409 Choose a word that appears at least ten times in SemCor (*find*), and annotate its  
 2410 WordNet senses across ten randomly-selected examples, without looking at the ground  
 2411 truth. Use online WordNet to understand the definition of each of the senses.<sup>14</sup> Have  
 2412 a partner do the same annotations, and compute the raw rate of agreement, expected  
 2413 chance rate of agreement, and Cohen's kappa.
- 2414 6. Download the Pang and Lee movie review data, currently available from <http://www.cs.cornell.edu/people/pabo/movie-review-data/>. Hold out a  
 2415 randomly-selected 400 reviews as a test set.
- 2416 Download a sentiment lexicon, such as the one currently available from Bing Liu,  
 2417 <https://www.cs.uic.edu/~liub/FBS/sentiment-analysis.html>. Tokenize  
 2418 the data, and classify each document as positive iff it has more positive sentiment  
 2419 words than negative sentiment words. Compute the accuracy and *F*-MEASURE on  
 2420 detecting positive reviews on the test set, using this lexicon-based classifier.
- 2421 Then train a discriminative classifier (averaged perceptron or logistic regression) on  
 2422 the training set, and compute its accuracy and *F*-MEASURE on the test set.
- 2423 Determine whether the differences are statistically significant, using two-tailed hy-  
 2424 pothesis tests: Binomial for the difference in accuracy, and bootstrap for the differ-  
 2425 ence in macro-*F*-MEASURE.
- 2426 2427 The remaining problems will require you to build a classifier and test its properties. Pick  
 2428 a multi-class text classification dataset, such as RCV1<sup>15</sup>). Divide your data into training

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<sup>13</sup>e.g., [https://github.com/google-research-datasets/word\\_sense\\_disambiguation\\_corpora](https://github.com/google-research-datasets/word_sense_disambiguation_corpora) or <http://globalwordnet.org/wordnet-annotated-corpora/>

<sup>14</sup><http://wordnetweb.princeton.edu/perl/webwn>

<sup>15</sup>[http://www.ai.mit.edu/projects/jmlr/papers/volume5/lewis04a/lyrl2004\\_rcv1v2\\_README.htm](http://www.ai.mit.edu/projects/jmlr/papers/volume5/lewis04a/lyrl2004_rcv1v2_README.htm)

2429 (60%), development (20%), and test sets (20%), if no such division already exists. [todo:  
2430 this dataset is already tokenized, find something else]

2431 7. Compare various vocabulary sizes of  $10^2, 10^3, 10^4, 10^5$ , using the most frequent words  
2432 in each case (you may use any reasonable tokenizer). Train logistic regression clas-  
2433 sifiers for each vocabulary size, and apply them to the development set. Plot the  
2434 accuracy and Macro-*F*-MEASURE with the increasing vocabulary size. For each vo-  
2435 cabulary size, tune the regularizer to maximize accuracy on a subset of data that is  
2436 held out from the training set.

2437 8. Compare the following tokenization algorithms:

- 2438 • Whitespace, using a regular expression  
2439 • Penn Treebank  
2440 • Split input into five-character units, regardless of whitespace or punctuation

2441 Compute the token/type ratio for each tokenizer on the training data, and explain  
2442 what you find. Train your classifier on each tokenized dataset, tuning the regularizer  
2443 on a subset of data that is held out from the training data. Tokenize the development  
2444 set, and report accuracy and Macro-*F*-MEASURE.

2445 9. Apply the Porter and Lancaster stemmers to the training set, using any reasonable  
2446 tokenizer, and compute the token/type ratios. Train your classifier on the stemmed  
2447 data, and compute the accuracy and Macro-*F*-MEASURE on stemmed development  
2448 data, again using a held-out portion of the training data to tune the regularizer.

2449 10. Identify the best combination of vocabulary filtering, tokenization, and stemming  
2450 from the previous three problems. Apply this preprocessing to the test set, and  
2451 compute the test set accuracy and Macro-*F*-MEASURE. Compare against a baseline  
2452 system that applies no vocabulary filtering, whitespace tokenization, and no stem-  
2453 ming.

2454 Use the binomial test to determine whether your best-performing system is signifi-  
2455 cantly more accurate than the baseline.

2456 Use the bootstrap test with  $M = 10^4$  to determine whether your best-performing  
2457 system achieves significantly higher macro-*F*-MEASURE.



# 2458 Chapter 5

## 2459 Learning without supervision

2460 So far we've assumed the following setup:

- 2461 a **training set** where you get observations  $x$  and labels  $y$ ;
- 2462 a **test set** where you only get observations  $x$ .

2463 Without labeled data, is it possible to learn anything? This scenario is known as **unsu-**  
2464 **pervised learning**, and we will see that indeed it is possible to learn about the underlying  
2465 structure of unlabeled observations. This chapter will also explore some related scenarios:  
2466 **semi-supervised learning**, in which only some instances are labeled, and **domain adap-**  
2467 **tation**, in which the training data differs from the data on which the trained system will  
2468 be deployed.

### 2469 5.1 Unsupervised learning

2470 To motivate unsupervised learning, consider the problem of word sense disambiguation  
2471 (§ 4.2). Our goal is to classify each instance of a word, such as *bank* into a sense,

- 2472 bank#1: a financial institution
- 2473 bank#2: the land bordering a river

2474 It is difficult to obtain sufficient training data for word sense disambiguation, because  
2475 even a large corpus will contain only a few instances of all but the most common words.  
2476 Is it possible to learn anything about these different senses without labeled data?

2477 Word sense disambiguation is usually performed using feature vectors constructed  
2478 from the local context of the word to be disambiguated. For example, for the word

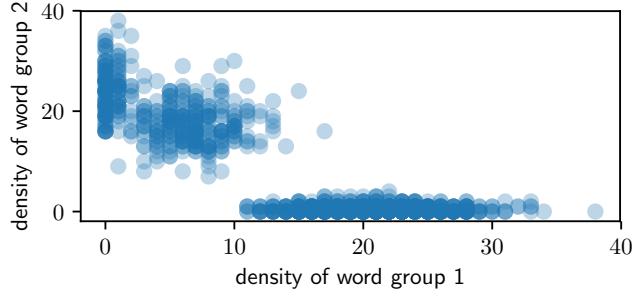


Figure 5.1: Counts of words from two different context groups

2479 *bank*, the immediate context might typically include words from one of the following two  
 2480 groups:

- 2481     1. *financial, deposits, credit, lending, capital, markets, regulated, reserve, liquid, assets*
- 2482     2. *land, water, geography, stream, river, flow, deposits, discharge, channel, ecology*

2483 Now consider a scatterplot, in which each point is a document containing the word *bank*.  
 2484 The location of the document on the  $x$ -axis is the count of words in group 1, and the  
 2485 location on the  $y$ -axis is the count for group 2. In such a plot, shown in Figure 5.1, two  
 2486 “blobs” might emerge, and these blobs correspond to the different senses of *bank*.

2487 Here’s a related scenario, from a different problem. Suppose you download thousands  
 2488 of news articles, and make a scatterplot, where each point corresponds to a document:  
 2489 the  $x$ -axis is the frequency of the group of words (*hurricane, winds, storm*); the  $y$ -axis is the  
 2490 frequency of the group (*election, voters, vote*). This time, three blobs might emerge: one  
 2491 for documents that are largely about a hurricane, another for documents largely about a  
 2492 election, and a third for documents about neither topic.

2493 These clumps represent the underlying structure of the data. But the two-dimensional  
 2494 scatter plots are based on groupings of context words, and in real scenarios these word  
 2495 lists are unknown. Unsupervised learning applies the same basic idea, but in a high-  
 2496 dimensional space with one dimension for every context word. This space can’t be di-  
 2497 rectly visualized, but the idea is the same: try to identify the underlying structure of the  
 2498 observed data, such that there are a few clusters of points, each of which is internally  
 2499 coherent. **Clustering** algorithms are capable of finding such structure automatically.

### 2500 5.1.1 ***K*-means clustering**

2501 Clustering algorithms assign each data point to a discrete cluster,  $z_i \in 1, 2, \dots, K$ . One of  
 2502 the best known clustering algorithms is ***K*-means**, an iterative algorithm that maintains

**Algorithm 8**  $K$ -means clustering algorithm

---

```

1: procedure  $K$ -MEANS( $\mathbf{x}_{1:N}, K$ )
2:   for  $i \in 1 \dots N$  do                                 $\triangleright$  initialize cluster memberships
3:      $z^{(i)} \leftarrow \text{RandomInt}(1, K)$ 
4:   repeat
5:     for  $k \in 1 \dots K$  do                           $\triangleright$  recompute cluster centers
6:        $\boldsymbol{\nu}_k \leftarrow \frac{1}{\delta(z^{(i)}=k)} \sum_{i=1}^N \delta(z^{(i)} = k) \mathbf{x}^{(i)}$ 
7:     for  $i \in 1 \dots N$  do                       $\triangleright$  reassigned instances to nearest clusters
8:        $z^{(i)} \leftarrow \operatorname{argmin}_k \|\mathbf{x}^{(i)} - \boldsymbol{\nu}_k\|^2$ 
9:   until converged
10:  return  $\{z^{(i)}\}$                                  $\triangleright$  return cluster assignments

```

---

2503 a cluster assignment for each instance, and a central (“mean”) location for each cluster.  
 2504  $K$ -means iterates between updates to the assignments and the centers:

- 2505 1. each instance is placed in the cluster with the closest center;  
 2506 2. each center is recomputed as the average over points in the cluster.

2507 This is formalized in Algorithm 8. The term  $\|\mathbf{x}^{(i)} - \boldsymbol{\nu}\|^2$  refers to the squared Euclidean  
 2508 norm,  $\sum_{j=1}^V (x_j^{(i)} - \nu_j)^2$ .

2509 **Soft  $K$ -means** is a particularly relevant variant. Instead of directly assigning each  
 2510 point to a specific cluster, soft  $K$ -means assigns each point a **distribution** over clusters  
 2511  $\mathbf{q}^{(i)}$ , so that  $\sum_{k=1}^K q^{(i)}(k) = 1$ , and  $\forall_k, q^{(i)}(k) \geq 0$ . The soft weight  $q^{(i)}(k)$  is computed from  
 2512 the distance of  $\mathbf{x}^{(i)}$  to the cluster center  $\boldsymbol{\nu}_k$ . In turn, the center of each cluster is computed  
 2513 from a **weighted average** of the points in the cluster,

$$\boldsymbol{\nu}_k = \frac{1}{\sum_{i=1}^N q^{(i)}(k)} \sum_{i=1}^N q^{(i)}(k) \mathbf{x}^{(i)}. \quad [5.1]$$

2514 We will now explore a probabilistic version of soft  $K$ -means clustering, based on **expectation**  
 2515 **maximization** (EM). Because EM clustering can be derived as an approximation to  
 2516 maximum-likelihood estimation, it can be extended in a number of useful ways.

2517    **5.1.2 Expectation Maximization (EM)**

Expectation maximization combines the idea of soft  $K$ -means with Naïve Bayes classification. To review, Naïve Bayes defines a probability distribution over the data,

$$\log p(\mathbf{x}, \mathbf{y}; \boldsymbol{\phi}, \boldsymbol{\mu}) = \sum_{i=1}^N \log \left( p(\mathbf{x}^{(i)} | y^{(i)}; \boldsymbol{\phi}) \times p(y^{(i)}; \boldsymbol{\mu}) \right) \quad [5.2]$$

Now suppose that you never observe the labels. To indicate this, we'll refer to the label of each instance as  $z^{(i)}$ , rather than  $y^{(i)}$ , which is usually reserved for observed variables. By marginalizing over the **latent** variables  $\mathbf{z}$ , we compute the marginal probability of the observed instances  $\mathbf{x}$ :

$$\log p(\mathbf{x}; \boldsymbol{\phi}, \boldsymbol{\mu}) = \sum_{i=1}^N \log p(\mathbf{x}^{(i)}; \boldsymbol{\phi}, \boldsymbol{\mu}) \quad [5.3]$$

$$= \sum_{i=1}^N \log \sum_{z=1}^K p(\mathbf{x}^{(i)}, z; \boldsymbol{\phi}, \boldsymbol{\mu}) \quad [5.4]$$

$$= \sum_{i=1}^N \log \sum_{z=1}^K p(\mathbf{x}^{(i)} | z; \boldsymbol{\phi}) \times p(z; \boldsymbol{\mu}). \quad [5.5]$$

2518    To estimate the parameters  $\boldsymbol{\phi}$  and  $\boldsymbol{\mu}$ , we can maximize the marginal likelihood in Equa-  
 2519    tion 5.5. Why is this the right thing to maximize? Without labels, discriminative learning  
 2520    is impossible — there's nothing to discriminate. So maximum likelihood is all we have.

2521    When the labels are observed, we can estimate the parameters of the Naïve Bayes  
 2522    probability model separately for each label. But marginalizing over the labels couples  
 2523    these parameters, making direct optimization of  $\log p(\mathbf{x})$  intractable. We will approximate  
 2524    the log-likelihood by introducing an *auxiliary variable*  $\mathbf{q}^{(i)}$ , which is a distribution over the  
 2525    label set  $\mathcal{Z} = \{1, 2, \dots, K\}$ . The optimization procedure will alternate between updates to  
 2526     $\mathbf{q}$  and updates to the parameters  $(\boldsymbol{\phi}, \boldsymbol{\mu})$ . Thus,  $\mathbf{q}^{(i)}$  plays here as in soft  $K$ -means.

To derive the updates for this optimization, multiply the right side of Equation 5.5 by

the ratio  $\frac{q^{(i)}(z)}{q^{(i)}(z)} = 1$ ,

$$\log p(\mathbf{x}; \phi, \mu) = \sum_{i=1}^N \log \sum_{z=1}^K p(\mathbf{x}^{(i)} | z; \phi) \times p(z; \mu) \times \frac{q^{(i)}(z)}{q^{(i)}(z)} \quad [5.6]$$

$$= \sum_{i=1}^N \log \sum_{z=1}^K q^{(i)}(z) \times p(\mathbf{x}^{(i)} | z; \phi) \times p(z; \mu) \times \frac{1}{q^{(i)}(z)} \quad [5.7]$$

$$= \sum_{i=1}^N \log E_{\mathbf{q}^{(i)}} \left[ \frac{p(\mathbf{x}^{(i)} | z; \phi) p(z; \mu)}{q^{(i)}(z)} \right], \quad [5.8]$$

where  $E_{\mathbf{q}^{(i)}} [f(z)] = \sum_{z=1}^K q^{(i)}(z) \times f(z)$  refers to the expectation of the function  $f$  under the distribution  $z \sim \mathbf{q}^{(i)}$ .

**Jensen's inequality** says that because  $\log$  is a concave function, we can push it inside the expectation, and obtain a lower bound.

$$\log p(\mathbf{x}; \phi, \mu) \geq \sum_{i=1}^N E_{\mathbf{q}^{(i)}} \left[ \log \frac{p(\mathbf{x}^{(i)} | z; \phi) p(z; \mu)}{q^{(i)}(z)} \right] \quad [5.9]$$

$$J \triangleq \sum_{i=1}^N E_{\mathbf{q}^{(i)}} \left[ \log p(\mathbf{x}^{(i)} | z; \phi) + \log p(z; \mu) - \log q^{(i)}(z) \right] \quad [5.10]$$

$$= \sum_{i=1}^N E_{\mathbf{q}^{(i)}} \left[ \log p(\mathbf{x}^{(i)}, z; \phi, \mu) \right] + H(\mathbf{q}^{(i)}) \quad [5.11]$$

We will focus on Equation 5.10, which is the lower bound on the marginal log-likelihood of the observed data,  $\log p(\mathbf{x})$ . Equation 5.11 shows the connection to the information theoretic concept of **entropy**,  $H(\mathbf{q}^{(i)}) = -\sum_{z=1}^K q^{(i)}(z) \log q^{(i)}(z)$ , which measures the average amount of information produced by a draw from the distribution  $q^{(i)}$ . The lower bound  $J$  is a function of two groups of arguments:

- the distributions  $\mathbf{q}^{(i)}$  for each instance;
- the parameters  $\mu$  and  $\phi$ .

The expectation-maximization (EM) algorithm maximizes the bound with respect to each of these arguments in turn, while holding the other fixed.

### 5.1.2.1 The E-step

The step in which we update  $\mathbf{q}^{(i)}$  is known as the **E-step**, because it updates the distribution under which the expectation is computed. To derive this update, first write out the

expectation in the lower bound as a sum,

$$J = \sum_{i=1}^N \sum_{z=1}^K q^{(i)}(z) \left[ \log p(\mathbf{x}^{(i)} | z; \boldsymbol{\phi}) + \log p(z; \boldsymbol{\mu}) - \log q^{(i)}(z) \right]. \quad [5.12]$$

When optimizing this bound, we must also respect a set of “sum-to-one” constraints,  $\sum_{z=1}^K q^{(i)}(z) = 1$  for all  $i$ . Just as in Naïve Bayes, this constraint can be incorporated into a Lagrangian:

$$J_q = \sum_{i=1}^N \sum_{z=1}^K q^{(i)}(z) \left( \log p(\mathbf{x}^{(i)} | z; \boldsymbol{\phi}) + \log p(z; \boldsymbol{\mu}) - \log q^{(i)}(z) \right) + \lambda^{(i)} \left( 1 - \sum_{z=1}^K q^{(i)}(z) \right), \quad [5.13]$$

where  $\lambda^{(i)}$  is the Lagrange multiplier for instance  $i$ .

The Lagrangian is maximized by taking the derivative and solving for  $q^{(i)}$ :

$$\frac{\partial J_q}{\partial q^{(i)}(z)} = \log p(\mathbf{x}^{(i)} | z; \boldsymbol{\phi}) + \log p(z; \boldsymbol{\mu}) - \log q^{(i)}(z) - 1 - \lambda^{(i)} \quad [5.14]$$

$$\log q^{(i)}(z) = \log p(\mathbf{x}^{(i)} | z; \boldsymbol{\phi}) + \log p(z; \boldsymbol{\mu}) - 1 - \lambda^{(i)} \quad [5.15]$$

$$q^{(i)}(z) \propto p(\mathbf{x}^{(i)} | z; \boldsymbol{\phi}) \times p(z; \boldsymbol{\mu}). \quad [5.16]$$

Applying the sum-to-one constraint gives an exact solution,

$$q^{(i)}(z) = \frac{p(\mathbf{x}^{(i)} | z; \boldsymbol{\phi}) \times p(z; \boldsymbol{\mu})}{\sum_{z'=1}^K p(\mathbf{x}^{(i)} | z'; \boldsymbol{\phi}) \times p(z'; \boldsymbol{\mu})} \quad [5.17]$$

$$= p(z | \mathbf{x}^{(i)}; \boldsymbol{\phi}, \boldsymbol{\mu}). \quad [5.18]$$

After normalizing, each  $q^{(i)}$  — which is the soft distribution over clusters for data  $\mathbf{x}^{(i)}$  — is set to the posterior probability  $p(z | \mathbf{x}^{(i)}; \boldsymbol{\phi}, \boldsymbol{\mu})$  under the current parameters. Although the Lagrange multipliers  $\lambda^{(i)}$  were introduced as additional parameters, they drop out during normalization.

### 5.1.2.2 The M-step

Next, we hold fixed the soft assignments  $q^{(i)}$ , and maximize with respect to the parameters,  $\boldsymbol{\phi}$  and  $\boldsymbol{\mu}$ . Let’s focus on the parameter  $\boldsymbol{\phi}$ , which parametrizes the likelihood  $p(\mathbf{x} | z; \boldsymbol{\phi})$ , and leave  $\boldsymbol{\mu}$  for an exercise. The parameter  $\boldsymbol{\phi}$  is a distribution over words for each cluster, so it is optimized under the constraint that  $\sum_{j=1}^V \phi_{z,j} = 1$ . To incorporate this

constraint, we introduce a set of Lagrange multipliers  $\{\lambda_z\}_{z=1}^K$ , and from the Lagrangian,

$$J_\phi = \sum_{i=1}^N \sum_{z=1}^K q^{(i)}(z) \left( \log p(\mathbf{x}^{(i)} | z; \boldsymbol{\phi}) + \log p(z; \mu) - \log q^{(i)}(z) \right) + \sum_{z=1}^K \lambda_z \left( 1 - \sum_{j=1}^V \phi_{z,j} \right). \quad [5.19]$$

2545 The term  $\log p(\mathbf{x}^{(i)} | z; \boldsymbol{\phi})$  is the conditional log-likelihood for the multinomial, which  
2546 expands to,

$$\log p(\mathbf{x}^{(i)} | z, \boldsymbol{\phi}) = C + \sum_{j=1}^V x_j \log \phi_{z,j}, \quad [5.20]$$

2547 where  $C$  is a constant with respect to  $\boldsymbol{\phi}$  — see Equation 2.12 in § 2.1 for more discussion  
2548 of this probability function.

Setting the derivative of  $J_\phi$  equal to zero,

$$\frac{\partial J_\phi}{\partial \phi_{z,j}} = \sum_{i=1}^N q^{(i)}(z) \times \frac{x_j^{(i)}}{\phi_{z,j}} - \lambda_z \quad [5.21]$$

$$\phi_{z,j} \propto \sum_{i=1}^N q^{(i)}(z) \times x_j^{(i)}. \quad [5.22]$$

Because  $\phi_z$  is constrained to be a probability distribution, the exact solution is computed as,

$$\phi_{z,j} = \frac{\sum_{i=1}^N q^{(i)}(z) \times x_j^{(i)}}{\sum_{j'=1}^V \sum_{i=1}^N q^{(i)}(z) \times x_{j'}^{(i)}} = \frac{E_q [\text{count}(z, j)]}{\sum_{j'=1}^V E_q [\text{count}(z, j')]} \quad [5.23]$$

2549 where the counter  $j \in \{1, 2, \dots, V\}$  indexes over base features, such as words.

2550 This update sets  $\phi_z$  equal to the relative frequency estimate of the *expected counts* under  
2551 the distribution  $q$ . As in supervised Naïve Bayes, we can smooth these counts by adding  
2552 a constant  $\alpha$ . The update for  $\mu$  is similar:  $\mu_z \propto \sum_{i=1}^N q^{(i)}(z) = E_q [\text{count}(z)]$ , which is the  
2553 expected frequency of cluster  $z$ . These probabilities can also be smoothed. In sum, the  
2554 M-step is just like Naïve Bayes, but with expected counts rather than observed counts.

2555 The multinomial likelihood  $p(\mathbf{x} | z)$  can be replaced with other probability distribu-  
2556 tions: for example, for continuous observations, a Gaussian distribution can be used. In  
2557 some cases, there is no closed-form update to the parameters of the likelihood. One ap-  
2558 proach is to run gradient-based optimization at each M-step; another is to simply take a  
2559 single step along the gradient step and then return to the E-step (Berg-Kirkpatrick et al.,  
2560 2010).

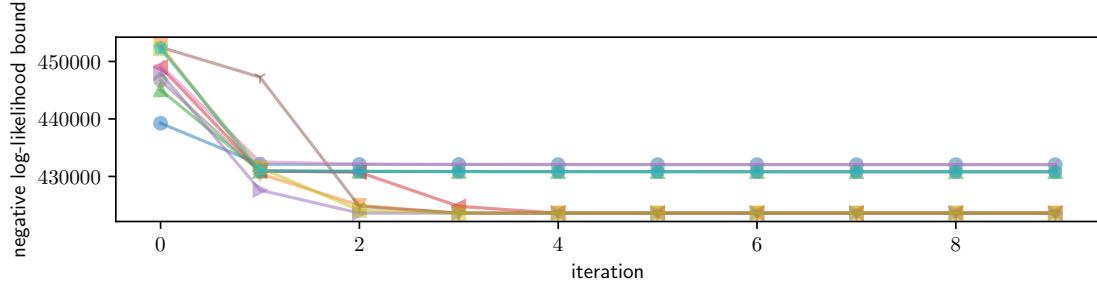


Figure 5.2: Sensitivity of expectation maximization to initialization. Each line shows the progress of optimization from a different random initialization.

### 2561 5.1.3 EM as an optimization algorithm

2562 Algorithms that alternate between updating subsets of the parameters are called **coordi-**  
 2563 **nate ascent** algorithms. The objective  $J$  (the lower bound on the marginal likelihood of  
 2564 the data) is separately convex in  $q$  and  $(\mu, \phi)$ , but it is not jointly convex in all terms; this  
 2565 condition is known as **biconvexity**. Each step of the expectation-maximization algorithm  
 2566 is guaranteed not to decrease the lower bound  $J$ , which means that EM will converge  
 2567 towards a solution at which no nearby points yield further improvements. This solution  
 2568 is a **local optimum** — it is as good or better than any of its immediate neighbors, but is  
 2569 *not* guaranteed to be optimal among all possible configurations of  $(q, \mu, \phi)$ .

2570 The fact that there is no guarantee of global optimality means that initialization is  
 2571 important: where you start can determine where you finish. To illustrate this point,  
 2572 Figure 5.2 shows the objective function for EM with ten different random initializations:  
 2573 while the objective function improves monotonically in each run, it converges to several  
 2574 different values.<sup>1</sup> For the convex objectives that we encountered in chapter 2, it was not  
 2575 necessary to worry about initialization, because gradient-based optimization guaranteed  
 2576 to reach the global minimum. But in expectation-maximization — and in the deep neural  
 2577 networks from chapter 3 — initialization matters.

2578 In **hard EM**, each  $q^{(i)}$  distribution assigns probability of 1 to a single label  $\hat{z}^{(i)}$ , and zero  
 2579 probability to all others (Neal and Hinton, 1998). This is similar in spirit to  $K$ -means clus-  
 2580 tering, and can outperform standard EM in some cases (Spitkovsky et al., 2010). Another  
 2581 variant of expectation maximization incorporates stochastic gradient descent (SGD): after  
 2582 performing a local E-step at each instance  $x^{(i)}$ , we immediately make a gradient update  
 2583 to the parameters  $(\mu, \phi)$ . This algorithm has been called **incremental expectation maxi-**  
 2584 **mization** (Neal and Hinton, 1998) and **online expectation maximization** (Sato and Ishii,  
 2585 2000; Cappé and Moulines, 2009), and is especially useful when there is no closed-form

<sup>1</sup>The figure shows the upper bound on the *negative* log-likelihood, because optimization is typically framed as minimization rather than maximization.

2586 optimum for the likelihood  $p(\mathbf{x} \mid z)$ , and in online settings where new data is constantly  
 2587 streamed in (see Liang and Klein, 2009, for a comparison for online EM variants).

2588 **5.1.4 How many clusters?**

2589 So far, we have assumed that the number of clusters  $K$  is given. In some cases, this as-  
 2590 sumption is valid. For example, a lexical semantic resource like WordNet might define the  
 2591 number of senses for a word. In other cases, the number of clusters could be a parameter  
 2592 for the user to tune: some readers want a coarse-grained clustering of news stories into  
 2593 three or four clusters, while others want a fine-grained clustering into twenty or more.  
 2594 But many times there is little extrinsic guidance for how to choose  $K$ .

2595 One solution is to choose the number of clusters to maximize a metric of clustering  
 2596 quality. The other parameters  $\mu$  and  $\phi$  are chosen to maximize the log-likelihood bound  
 2597  $J$ , so this might seem a potential candidate for tuning  $K$ . However,  $J$  will never decrease  
 2598 with  $K$ : if it is possible to obtain a bound of  $J_K$  with  $K$  clusters, then it is always possible  
 2599 to do at least as well with  $K + 1$  clusters, by simply ignoring the additional cluster and  
 2600 setting its probability to zero in  $q$  and  $\mu$ . It is therefore necessary to introduce a penalty  
 2601 for model complexity, so that fewer clusters are preferred. For example, the Akaike Infor-  
 2602 mation Crition (AIC; Akaike, 1974) is the linear combination of the number of parameters  
 2603 and the log-likelihood,

$$\text{AIC} = 2M - 2J, \quad [5.24]$$

2604 where  $M$  is the number of parameters. In an expectation-maximization clustering algo-  
 2605 rithm,  $M = K \times V + K$ . Since the number of parameters increases with the number of  
 2606 clusters  $K$ , the AIC may prefer more parsimonious models, even if they do not fit the data  
 2607 quite as well.

2608 Another choice is to maximize the **predictive likelihood** on heldout data. This data  
 2609 is not used to estimate the model parameters  $\phi$  and  $\mu$ , and so it is not the case that the  
 2610 likelihood on this data is guaranteed to increase with  $K$ . Figure 5.3 shows the negative  
 2611 log-likelihood on training and heldout data, as well as the AIC.

2612 \***Bayesian nonparametrics** An alternative approach is to treat the number of clusters as  
 2613 another latent variable. This requires statistical inference over a set of models with a vari-  
 2614 able number of clusters. This is not possible within the framework of expectation max-  
 2615 imization, but there are several alternative inference procedures which can be applied,  
 2616 including **Markov Chain Monte Carlo (MCMC)**, which is briefly discussed in § 5.5 (for  
 2617 more details, see Chapter 25 of Murphy, 2012). Bayesian nonparametrics have been ap-  
 2618 plied to the problem of unsupervised word sense induction, learning not only the word  
 2619 senses but also the number of senses per word (Reisinger and Mooney, 2010).

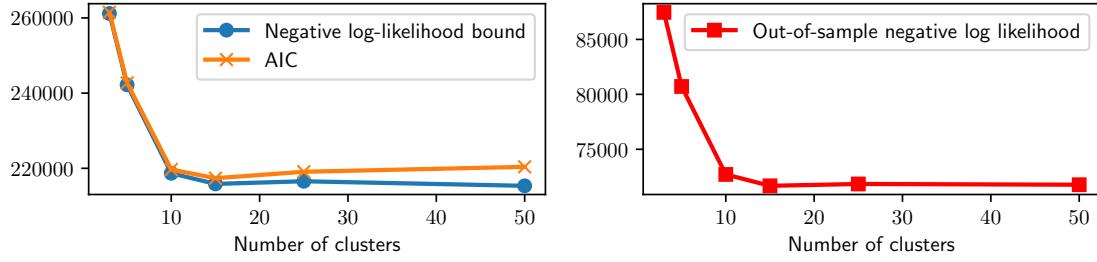


Figure 5.3: The negative log-likelihood and AIC for several runs of expectation maximization, on synthetic data. Although the data was generated from a model with  $K = 10$ , the optimal number of clusters is  $\hat{K} = 15$ , according to AIC and the heldout log-likelihood. The training set log-likelihood continues to improve as  $K$  increases.

## 2620 5.2 Applications of expectation-maximization

2621 EM is not really an “algorithm” like, say, quicksort. Rather, it is a framework for learning  
2622 with missing data. The recipe for using EM on a problem of interest is:

- 2623 • Introduce latent variables  $z$ , such that it is easy to write the probability  $P(x, z)$ . It  
2624 should also be easy to estimate the associated parameters, given knowledge of  $z$ .
- 2625 • Derive the E-step updates for  $q(z)$ , which is typically factored as  $q(z) = \prod_{i=1}^N q_{z(i)}(z^{(i)})$ ,  
2626 where  $i$  is an index over instances.
- 2627 • The M-step updates typically correspond to the soft version of a probabilistic super-  
2628 vised learning algorithm, like Naïve Bayes.

2629 This section discusses a few of the many applications of this general framework.

### 2630 5.2.1 Word sense induction

2631 The chapter began by considering the problem of word sense disambiguation when the  
2632 senses are not known in advance. Expectation-maximization can be applied to this prob-  
2633 lem by treating each cluster as a word sense. Each instance represents the use of an  
2634 ambiguous word, and  $x^{(i)}$  is a vector of counts for the other words that appear nearby:  
2635 Schütze (1998) uses all words within a 50-word window. The probability  $p(x^{(i)} | z)$  can be  
2636 set to the multinomial distribution, as in Naïve Bayes. The EM algorithm can be applied  
2637 directly to this data, yielding clusters that (hopefully) correspond to the word senses.

Better performance can be obtained by first applying truncated **singular value decom-  
position (SVD)** to the matrix of context-counts  $C_{ij} = \text{count}(i, j)$ , where  $\text{count}(i, j)$  is the

count of word  $j$  in the context of instance  $i$ . Truncated singular value decomposition approximates the matrix  $\mathbf{C}$  as a product of three matrices,  $\mathbf{U}, \mathbf{S}, \mathbf{V}$ , under the constraint that  $\mathbf{U}$  and  $\mathbf{V}$  are orthonormal, and  $\mathbf{S}$  is diagonal:

$$\begin{aligned} & \min_{\mathbf{U}, \mathbf{S}, \mathbf{V}} \|\mathbf{C} - \mathbf{USV}^\top\|_F \\ & \text{s.t. } \mathbf{U} \in \mathbb{R}^{V \times K}, \mathbf{UU}^\top = \mathbb{I} \\ & \quad \mathbf{S} = \text{Diag}(s_1, s_2, \dots, s_K) \\ & \quad \mathbf{V}^\top \in \mathbb{R}^{N_p \times K}, \mathbf{VV}^\top = \mathbb{I}, \end{aligned} \quad [5.25]$$

where  $\|\cdot\|_F$  is the Frobenius norm,  $\|X\|_F = \sqrt{\sum_{i,j} X_{i,j}^2}$ . The matrix  $\mathbf{U}$  contains the left singular vectors of  $\mathbf{C}$ , and the rows of this matrix can be used as low-dimensional representations of the count vectors  $\mathbf{c}_i$ . EM clustering can be made more robust by setting the instance descriptions  $\mathbf{x}^{(i)}$  equal to these rows, rather than using raw counts (Schütze, 1998). However, because the instances are now dense vectors of continuous numbers, the probability  $p(\mathbf{x}^{(i)} | z)$  must be defined as a multivariate Gaussian distribution.

In truncated singular value decomposition, the hyperparameter  $K$  is the truncation limit: when  $K$  is equal to the rank of  $\mathbf{C}$ , the norm of the difference between the original matrix  $\mathbf{C}$  and its reconstruction  $\mathbf{USV}^\top$  will be zero. Lower values of  $K$  increase the reconstruction error, but yield vector representations that are smaller and easier to learn from. Singular value decomposition is discussed in more detail in chapter 14.

## 5.2.2 Semi-supervised learning

Expectation-maximization can also be applied to the problem of **semi-supervised learning**: learning from both labeled and unlabeled data in a single model. Semi-supervised learning makes use of ground truth annotations, ensuring that each label  $y$  corresponds to the desired concept. By adding unlabeled data, it is possible cover a greater fraction of the features than would be possible using labeled data alone. Other methods for semi-supervised learning are discussed in § 5.3, but for now, let's approach the problem within the framework of expectation-maximization (Nigam et al., 2000).

Suppose we have labeled data  $\{(\mathbf{x}^{(i)}, y^{(i)})\}_{i=1}^{N_\ell}$ , and unlabeled data  $\{\mathbf{x}^{(i)}\}_{i=N_\ell+1}^{N_\ell+N_u}$ , where  $N_\ell$  is the number of labeled instances and  $N_u$  is the number of unlabeled instances. We can learn from the combined data by maximizing a lower bound on the joint log-likelihood,

$$\mathcal{L} = \sum_{i=1}^{N_\ell} \log p(\mathbf{x}^{(i)}, y^{(i)}; \boldsymbol{\mu}, \boldsymbol{\phi}) + \sum_{j=N_\ell+1}^{N_\ell+N_u} \log p(\mathbf{x}^{(j)}; \boldsymbol{\mu}, \boldsymbol{\phi}) \quad [5.26]$$

$$= \sum_{i=1}^{N_\ell} \left( \log p(\mathbf{x}^{(i)} | y^{(i)}; \boldsymbol{\phi}) + \log p(y^{(i)}; \boldsymbol{\mu}) \right) + \sum_{j=N_\ell+1}^{N_\ell+N_u} \log \sum_{y=1}^K p(\mathbf{x}^{(j)}, y; \boldsymbol{\mu}, \boldsymbol{\phi}). \quad [5.27]$$

**Algorithm 9** Generative process for the Naïve Bayes classifier with hidden components

---

**for** Document  $i \in \{1, 2, \dots, N\}$  **do**:

Draw the label  $y^{(i)} \sim \text{Categorical}(\mu)$ ;

Draw the component  $z^{(i)} \sim \text{Categorical}(\beta_{y^{(i)}})$ ;

Draw the word counts  $x^{(i)} | y^{(i)}, z^{(i)} \sim \text{Multinomial}(\phi_{z^{(i)}})$ .

---

2657 The left sum is identical to the objective in Naïve Bayes; the right sum is the marginal log-  
 2658 likelihood for expectation-maximization clustering, from Equation 5.5. We can construct a  
 2659 lower bound on this log-likelihood by introducing distributions  $q^{(j)}$  for all  $j \in \{N_\ell + 1, \dots, N_\ell + N_u\}$ .  
 2660 The E-step updates these distributions; the M-step updates the parameters  $\phi$  and  $\mu$ , us-  
 2661 ing the expected counts from the unlabeled data and the observed counts from the labeled  
 2662 data.

2663 A critical issue in semi-supervised learning is how to balance the impact of the labeled  
 2664 and unlabeled data on the classifier weights, especially when the unlabeled data is much  
 2665 larger than the labeled dataset. The risk is that the unlabeled data will dominate, caus-  
 2666 ing the parameters to drift towards a “natural clustering” of the instances — which may  
 2667 not correspond to a good classifier for the labeled data. One solution is to heuristically  
 2668 reweight the two components of Equation 5.26, tuning the weight of the two components  
 2669 on a heldout development set (Nigam et al., 2000).

2670 **5.2.3 Multi-component modeling**

2671 As a final application, let’s return to fully supervised classification. A classic dataset for  
 2672 text classification is 20 newsgroups, which contains posts to a set of online forums, called  
 2673 newsgroups. One of the newsgroups is `comp.sys.mac.hardware`, which discusses Ap-  
 2674 ple computing hardware. Suppose that within this newsgroup there are two kinds of  
 2675 posts: reviews of new hardware, and question-answer posts about hardware problems.  
 2676 The language in these *components* of the `mac.hardware` class might have little in com-  
 2677 mon; if so, it would be better to model these components separately, rather than treating  
 2678 their union as a single class. However, the component responsible for each instance is not  
 2679 directly observed.

2680 Recall that Naïve Bayes is based on a generative process, which provides a stochastic  
 2681 explanation for the observed data. In Naïve Bayes, each label is drawn from a categorical  
 2682 distribution with parameter  $\mu$ , and each vector of word counts is drawn from a multi-  
 2683 nomial distribution with parameter  $\phi_y$ . For multi-component modeling, we envision a  
 2684 slightly different generative process, incorporating both the observed label  $y^{(i)}$  and the  
 2685 latent component  $z^{(i)}$ . This generative process is shown in Algorithm 9. A new parameter  
 2686  $\beta_{y^{(i)}}$  defines the distribution of components, conditioned on the label  $y^{(i)}$ . The component,  
 2687 and not the class label, then parametrizes the distribution over words.

- 
- (5.1) ☺ Villeneuve a bel et bien **réussi** son pari de changer de perspectives tout en assurant une cohérence à la franchise.<sup>2</sup>
- (5.2) ☺ Il est également trop **long** et bancal dans sa narration, tiède dans ses intentions, et tirailé entre deux personnages et directions qui ne parviennent pas à coexister en harmonie.<sup>3</sup>
- (5.3) Denis Villeneuve a **réussi** une suite **parfaitemment** maîtrisée<sup>4</sup>
- (5.4) **Long, bavard**, hyper design, à peine agité (le comble de l'action : une bagarre dans la flotte), métaphysique et, surtout, ennuyeux jusqu'à la catalepsie.<sup>5</sup>
- (5.5) Une suite d'une écrasante puissance, mêlant **parfaitemment** le contemplatif au narratif.<sup>6</sup>
- (5.6) Le film impitoyablement **bavard** finit quand même par se taire quand se lève l'espèce de bouquet final où semble se déchaîner, comme en libre parcours de poulets décapiés, l'armée des graphistes numériques griffant nerveusement la palette graphique entre agonie et orgasme.<sup>7</sup>

---

Table 5.1: Labeled and unlabeled reviews of the films *Blade Runner 2049* and *Transformers: The Last Knight*.

The labeled data includes  $(\mathbf{x}^{(i)}, y^{(i)})$ , but not  $z^{(i)}$ , so this is another case of missing data. Again, we sum over the missing data, applying Jensen's inequality to as to obtain a lower bound on the log-likelihood,

$$\log p(\mathbf{x}^{(i)}, y^{(i)}) = \log \sum_{z=1}^{K_z} p(\mathbf{x}^{(i)}, y^{(i)}, z; \boldsymbol{\mu}, \boldsymbol{\phi}, \boldsymbol{\beta}) \quad [5.28]$$

$$\geq \log p(y^{(i)}; \boldsymbol{\mu}) + E_{q_{Z|Y}^{(i)}} [\log p(\mathbf{x}^{(i)} | z; \boldsymbol{\phi}) + \log p(z | y^{(i)}; \boldsymbol{\beta}) - \log q^{(i)}(z)]. \quad [5.29]$$

We are now ready to apply expectation maximization. As usual, the E-step updates the distribution over the missing data,  $q_{Z|Y}^{(i)}$ . The M-step updates the parameters,

$$\beta_{y,z} = \frac{E_q [\text{count}(y, z)]}{\sum_{z'=1}^{K_z} E_q [\text{count}(y, z')]} \quad [5.30]$$

$$\phi_{z,j} = \frac{E_q [\text{count}(z, j)]}{\sum_{j'=1}^V E_q [\text{count}(z, j')]} \quad [5.31]$$

## 2688 5.3 Semi-supervised learning

2689 In semi-supervised learning, the learner makes use of both labeled and unlabeled data.  
 2690 To see how this could help, suppose you want to do sentiment analysis in French. In Ta-

ble 5.1, there are two labeled examples, one positive and one negative. From this data, a learner could conclude that *réussi* is positive and *long* is negative. This isn't much! However, we can propagate this information to the unlabeled data, and potentially learn more.

- If we are confident that *réussi* is positive, then we might guess that (5.3) is also positive.
- That suggests that *parfaitement* is also positive.
- We can then propagate this information to (5.5), and learn from this words in this example.
- Similarly, we can propagate from the labeled data to (5.4), which we guess to be negative because it shares the word *long*. This suggests that *bavard* is also negative, which we propagate to (5.6).

Instances (5.3) and (5.4) were "similar" to the labeled examples for positivity and negativity, respectively. By using these instances to expand the models for each class, it became possible to correctly label instances (5.5) and (5.6), which didn't share any important features with the original labeled data. This requires a key assumption: that similar instances will have similar labels.

In § 5.2.2, we discussed how expectation maximization can be applied to semi-supervised learning. Using the labeled data, the initial parameters  $\phi$  would assign a high weight for *réussi* in the positive class, and a high weight for *long* in the negative class. These weights helped to shape the distributions  $q$  for instances (5.3) and (5.4) in the E-step. In the next iteration of the M-step, the parameters  $\phi$  are updated with counts from these instances, making it possible to correctly label the instances (5.5) and (5.6).

However, expectation-maximization has an important disadvantage: it requires using a generative classification model, which restricts the features that can be used for classification. In this section, we explore non-probabilistic approaches, which impose fewer restrictions on the classification model.

### 5.3.1 Multi-view learning

EM semi-supervised learning can be viewed as **self-training**: the labeled data guides the initial estimates of the classification parameters; these parameters are used to compute a label distribution over the unlabeled instances,  $q^{(i)}$ ; the label distributions are used to update the parameters. The risk is that self-training drifts away from the original labeled data. This problem can be ameliorated by **multi-view learning**. Here we take the assumption that the features can be decomposed into multiple "views", each of which is conditionally independent, given the label. For example, consider the problem of classifying a name as a person or location: one view is the name itself; another is the context in which it appears. This situation is illustrated in Table 5.2.

	$\boldsymbol{x}^{(1)}$	$\boldsymbol{x}^{(2)}$	$y$
1.	Peachtree Street	located on	LOC
2.	Dr. Walker	said	PER
3.	Zanzibar	located in	? → LOC
4.	Zanzibar	flew to	? → LOC
5.	Dr. Robert	recommended	? → PER
6.	Oprah	recommended	? → PER

Table 5.2: Example of multiview learning for named entity classification

2727     **Co-training** is an iterative multi-view learning algorithm, in which there are separate  
 2728 classifiers for each view (Blum and Mitchell, 1998). At each iteration of the algorithm, each  
 2729 classifier predicts labels for a subset of the unlabeled instances, using only the features  
 2730 available in its view. These predictions are then used as ground truth to train the classifiers  
 2731 associated with the other views. In the example shown in Table 5.2, the classifier on  $\boldsymbol{x}^{(1)}$   
 2732 might correctly label instance #5 as a person, because of the feature *Dr*; this instance would  
 2733 then serve as training data for the classifier on  $\boldsymbol{x}^{(2)}$ , which would then be able to correctly  
 2734 label instance #6, thanks to the feature *recommended*. If the views are truly independent,  
 2735 this procedure is robust to drift. Furthermore, it imposes no restrictions on the classifiers  
 2736 that can be used for each view.

2737     Word-sense disambiguation is particularly suited to multi-view learning, thanks to the  
 2738 heuristic of “one sense per discourse”: if a polysemous word is used more than once in  
 2739 a given text or conversation, all usages refer to the same sense (Gale et al., 1992). This  
 2740 motivates a multi-view learning approach, in which one view corresponds to the local  
 2741 context (the surrounding words), and another view corresponds to the global context at  
 2742 the document level (Yarowsky, 1995). The local context view is first trained on a small  
 2743 seed dataset. We then identify its most confident predictions on unlabeled instances. The  
 2744 global context view is then used to extend these confident predictions to other instances  
 2745 within the same documents. These new instances are added to the training data to the  
 2746 local context classifier, which is retrained and then applied to the remaining unlabeled  
 2747 data.

### 2748 5.3.2 Graph-based algorithms

2749     Another family of approaches to semi-supervised learning begins by constructing a graph,  
 2750 in which pairs of instances are linked with symmetric weights  $\omega_{i,j}$ , e.g.,

$$\omega_{i,j} = \exp(-\alpha \times \|\boldsymbol{x}^{(i)} - \boldsymbol{x}^{(j)}\|^2). \quad [5.32]$$

2751     The goal is to use this weighted graph to propagate labels from a small set of labeled  
 2752 instances to larger set of unlabeled instances.

2753 In **label propagation**, this is done through a series of matrix operations (Zhu et al.,  
 2754 2003). Let  $\mathbf{Q}$  be a matrix of size  $N \times K$ , in which each row  $\mathbf{q}^{(i)}$  describes the labeling  
 2755 of instance  $i$ . When ground truth labels are available, then  $\mathbf{q}^{(i)}$  is an indicator vector,  
 2756 with  $q_{y^{(i)}}^{(i)} = 1$  and  $q_{y' \neq y^{(i)}}^{(i)} = 0$ . Let us refer to the submatrix of rows containing labeled  
 2757 instances as  $\mathbf{Q}_L$ , and the remaining rows as  $\mathbf{Q}_U$ . The rows of  $\mathbf{Q}_U$  are initialized to assign  
 2758 equal probabilities to all labels,  $q_{i,k} = \frac{1}{K}$ .

2759 Now, let  $T_{i,j}$  represent the “transition” probability of moving from node  $j$  to node  $i$ ,

$$T_{i,j} \triangleq \Pr(j \rightarrow i) = \frac{\omega_{i,j}}{\sum_{k=1}^N \omega_{k,j}}. \quad [5.33]$$

We compute values of  $T_{i,j}$  for all instances  $j$  and all *unlabeled* instances  $i$ , forming a matrix  
 of size  $N_U \times N$ . If the dataset is large, this matrix may be expensive to store and manip-  
 ulate; a solution is to sparsify it, by keeping only the  $\kappa$  largest values in each row, and  
 setting all other values to zero. We can then “propagate” the label distributions to the  
 unlabeled instances,

$$\tilde{\mathbf{Q}}_U \leftarrow \mathbf{T}\mathbf{Q} \quad [5.34]$$

$$\mathbf{s} \leftarrow \tilde{\mathbf{Q}}_U \mathbf{1} \quad [5.35]$$

$$\mathbf{Q}_U \leftarrow \text{Diag}(\mathbf{s})^{-1} \tilde{\mathbf{Q}}_U. \quad [5.36]$$

2760 The expression  $\tilde{\mathbf{Q}}_U \mathbf{1}$  indicates multiplication of  $\tilde{\mathbf{Q}}_U$  by a column vector of ones, which is  
 2761 equivalent to computing the sum of each row of  $\tilde{\mathbf{Q}}_U$ . The matrix  $\text{Diag}(\mathbf{s})$  is a diagonal  
 2762 matrix with the elements of  $\mathbf{s}$  on the diagonals. The product  $\text{Diag}(\mathbf{s})^{-1} \tilde{\mathbf{Q}}_U$  has the effect  
 2763 of normalizing the rows of  $\tilde{\mathbf{Q}}_U$ , so that each row of  $\mathbf{Q}_U$  is a probability distribution over  
 2764 labels.

## 2765 5.4 Domain adaptation

2766 In many practical scenarios, the labeled data differs in some key respect from the data  
 2767 to which the trained model is to be applied. A classic example is in consumer reviews:  
 2768 we may have labeled reviews of movies (the **source domain**), but we want to predict the  
 2769 reviews of appliances (the **target domain**). A similar issues arise with genre differences:  
 2770 most linguistically-annotated data is news text, but application domains range from social  
 2771 media to electronic health records. In general, there may be several source and target  
 2772 domains, each with their own properties; however, for simplicity, this discussion will  
 2773 focus mainly on the case of a single source and target domain.

2774 The simplest approach is “direct transfer”: train a classifier on the source domain,  
 2775 and apply it directly to the target domain. The accuracy of this approach depends on the  
 2776 extent to which features are shared across domains. In review text, words like *outstanding*

and *disappointing* will apply across both movies and appliances; but others, like *terrifying*, may have meanings that are domain-specific. **Domain adaptation** algorithms attempt to do better than direct transfer, by learning from data in both domains. There are two main families of domain adaptation algorithms, depending on whether any labeled data is available in the target domain.

#### 5.4.1 Supervised domain adaptation

In supervised domain adaptation, there is a small amount of labeled data in the target domain, and a large amount of data in the source domain. The simplest approach would be to ignore domain differences, and simply merge the training data from the source and target domains. There are several other baseline approaches to dealing with this scenario (Daumé III, 2007):

**Interpolation.** Train a classifier for each domain, and combine their predictions. For example,

$$\hat{y} = \operatorname{argmax}_y \lambda_s \Psi_s(\mathbf{x}, y) + (1 - \lambda_s) \Psi_t(\mathbf{x}, y), \quad [5.37]$$

where  $\Psi_s$  and  $\Psi_t$  are the scoring functions from the source and target domain classifiers respectively, and  $\lambda_s$  is the interpolation weight.

**Prediction.** Train a classifier on the source domain data, use its prediction as an additional feature in a classifier trained on the target domain data.

**Priors.** Train a classifier on the source domain data, and use its weights as a prior distribution on the weights of the classifier for the target domain data. This is equivalent to regularizing the target domain weights towards the weights of the source domain classifier (Chelba and Acero, 2006),

$$\ell(\boldsymbol{\theta}_t) = \sum_{i=1}^N \ell^{(i)}(\mathbf{x}^{(i)}, y^{(i)}; \boldsymbol{\theta}_t) + \lambda \|\boldsymbol{\theta}_t - \boldsymbol{\theta}_s\|_2^2, \quad [5.38]$$

where  $\ell^{(i)}$  is the prediction loss on instance  $i$ , and  $\lambda$  is the regularization weight.

An effective and “frustratingly simple” alternative is EasyAdapt (Daumé III, 2007), which creates copies of each feature: one for each domain and one for the cross-domain setting. For example, a negative review of the film *Wonder Woman* begins, *As boring and flavorless as a three-day-old grilled cheese sandwich....*<sup>8</sup> The resulting bag-of-words feature

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<sup>8</sup><http://www.colesmithey.com/capsules/2017/06/wonder-woman.HTML>, accessed October 9, 2017.

vector would be,

$$\begin{aligned} \mathbf{f}(\mathbf{x}, y, d) = & \{(boring, -, \text{MOVIE}) : 1, (boring, -, *) : 1, \\ & (flavorless, -, \text{MOVIE}) : 1, (flavorless, -, *) : 1, \\ & (three-day-old, -, \text{MOVIE}) : 1, (three-day-old, -, *) : 1, \\ & \dots\}, \end{aligned}$$

with  $(boring, -, \text{MOVIE})$  indicating the word *boring* appearing in a negative labeled document in the MOVIE domain, and  $(boring, -, *)$  indicating the same word in a negative labeled document in *any* domain. It is up to the learner to allocate weight between the domain-specific and cross-domain features: for words that facilitate prediction in both domains, the learner will use the cross-domain features; for words that are relevant only to a single domain, the domain-specific features will be used. Any discriminative classifier can be used with these augmented features.<sup>9</sup>

#### 5.4.2 Unsupervised domain adaptation

In unsupervised domain adaptation, there is no labeled data in the target domain. Unsupervised domain adaptation algorithms cope with this problem by trying to make the data from the source and target domains as similar as possible. This is typically done by learning a **projection function**, which puts the source and target data in a shared space, in which a learner can generalize across domains. This projection is learned from data in both domains, and is applied to the base features — for example, the bag-of-words in text classification. The projected features can then be used both for training and for prediction.

##### 5.4.2.1 Linear projection

In linear projection, the cross-domain representation is constructed by a matrix-vector product,

$$\mathbf{g}(\mathbf{x}^{(i)}) = \mathbf{U}\mathbf{x}^{(i)}. \quad [5.39]$$

The projected vectors  $\mathbf{g}(\mathbf{x}^{(i)})$  can then be used as base features during both training (from the source domain) and prediction (on the target domain).

The projection matrix  $\mathbf{U}$  can be learned in a number of different ways, but many approaches focus on compressing and reconstructing the base features (Ando and Zhang, 2005). For example, we can define a set of **pivot features**, which are typically chosen because they appear in both domains: in the case of review documents, pivot features might include evaluative adjectives like *outstanding* and *disappointing* (Blitzer et al., 2007). For each pivot feature  $j$ , we define an auxiliary problem of predicting whether the feature is

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<sup>9</sup>EasyAdapt can be explained as a hierarchical Bayesian model, in which the weights for each domain are drawn from a shared prior (Finkel and Manning, 2009).

present in each example, using the remaining base features. Let  $\phi_j$  denote the weights of this classifier, and us horizontally concatenate the weights for each of the  $N_p$  pivot features into a matrix  $\Phi = [\phi_1, \phi_2, \dots, \phi_{N_p}]$ .

We then perform truncated singular value decomposition on  $\Phi$ , as described in § 5.2.1, obtaining  $\Phi \approx \mathbf{U}\mathbf{S}\mathbf{V}^\top$ . The rows of the matrix  $\mathbf{U}$  summarize information about each base feature: indeed, the truncated singular value decomposition identifies a low-dimension basis for the weight matrix  $\Phi$ , which in turn links base features to pivot features. Suppose that a base feature *reliable* occurs only in the target domain of appliance reviews. Nonetheless, it will have a positive weight towards some pivot features (e.g., *outstanding*, *recommended*), and a negative weight towards others (e.g., *worthless*, *unpleasant*). A base feature such as *watchable* might have the same associations with the pivot features, and therefore,  $\mathbf{u}_{\text{reliable}} \approx \mathbf{u}_{\text{watchable}}$ . The matrix  $\mathbf{U}$  can thus project the base features into a space in which this information is shared.

#### 5.4.2.2 Non-linear projection

Non-linear transformations of the base features can be accomplished by implementing the transformation function as a deep neural network, which is trained from an auxiliary objective.

**Denoising objectives** One possibility is to train a projection function to reconstruct a corrupted version of the original input. The original input can be corrupted in various ways: by the addition of random noise (Glorot et al., 2011; Chen et al., 2012), or by the deletion of features (Chen et al., 2012; Yang and Eisenstein, 2015). Denoising objectives share many properties of the linear projection method described above: they enable the projection function to be trained on large amounts of unlabeled data from the target domain, and allow information to be shared across the feature space, thereby reducing sensitivity to rare and domain-specific features.

**Adversarial objectives** The ultimate goal is for the transformed representations  $\mathbf{g}(\mathbf{x}^{(i)})$  to be domain-general. This can be made an explicit optimization criterion by computing the similarity of transformed instances both within and between domains (Tzeng et al., 2015), or by formulating an auxiliary classification task, in which the domain itself is treated as a label (Ganin et al., 2016). This setting is **adversarial**, because we want to learn a representation that makes this classifier perform poorly. At the same time, we want  $\mathbf{g}(\mathbf{x}^{(i)})$  to enable accurate predictions of the labels  $y^{(i)}$ .

To formalize this idea, let  $d^{(i)}$  represent the domain of instance  $i$ , and let  $\ell_d(\mathbf{g}(\mathbf{x}^{(i)}), d^{(i)}; \theta_d)$  represent the loss of a classifier (typically a deep neural network) trained to predict  $d^{(i)}$  from the transformed representation  $\mathbf{g}(\mathbf{x}^{(i)})$ , using parameters  $\theta_d$ . Analogously, let  $\ell_y(\mathbf{g}(\mathbf{x}^{(i)}), y^{(i)}; \theta_y)$  represent the loss of a classifier trained to predict the label  $y^{(i)}$  from  $\mathbf{g}(\mathbf{x}^{(i)})$ , using param-

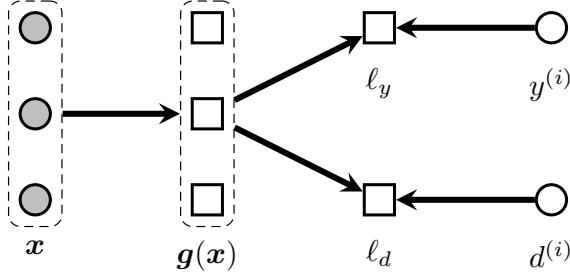


Figure 5.4: A schematic view of adversarial domain adaptation. The loss  $\ell_y$  is computed only for instances from the source domain, where labels  $y^{(i)}$  are available.

eters  $\theta_y$ . The transformation  $g$  can then be trained from two criteria: it should yield accurate predictions of the labels  $y^{(i)}$ , while making *inaccurate* predictions of the domains  $d^{(i)}$ . This can be formulated as a joint optimization problem,

$$\min_{f, \theta_g, \theta_y, \theta_d} \sum_{i=1}^{N_\ell+N_u} \ell_d(g(\mathbf{x}^{(i)}; \theta_g), d^{(i)}; \theta_d) - \sum_{i=1}^{N_\ell} \ell_y(g(\mathbf{x}^{(i)}), y^{(i)}; \theta_y), \quad [5.40]$$

where  $N_\ell$  is the number of labeled instances and  $N_u$  is the number of unlabeled instances, with the labeled instances appearing first in the dataset. This setup is shown in Figure 5.4. The loss can be optimized by stochastic gradient descent, jointly training the parameters of the non-linear transformation  $\theta_g$ , and the parameters of the prediction models  $\theta_d$  and  $\theta_y$ .

## 5.5 \*Other approaches to learning with latent variables

Expectation maximization provides a general approach to learning with latent variables, but it has limitations. One is the sensitivity to initialization; in practical applications, considerable attention may need to be devoted to finding a good initialization. A second issue is that EM tends to be easiest to apply in cases where the latent variables have a clear decomposition (in the cases we have considered, they decompose across the instances). For these reasons, it is worth briefly considering some alternatives to EM.

### 5.5.1 Sampling

In EM clustering, there is a distribution  $q^{(i)}$  for the missing data related to each instance. The M-step consists of updating the parameters of this distribution. An alternative is to draw samples of the latent variables. If the sampling distribution is designed correctly, this procedure will eventually converge to drawing samples from the true posterior over the missing data,  $p(z^{(1:N_z)} | \mathbf{x}^{(1:N_x)})$ . For example, in the case of clustering, the missing

2882 data  $\mathbf{z}^{(1:N_z)}$  is the set of cluster memberships,  $\mathbf{y}^{(1:N)}$ , so we draw samples from the pos-  
 2883 terior distribution over clusterings of the data. If a single clustering is required, we can  
 2884 select the one with the highest conditional likelihood,  $\hat{\mathbf{z}} = \operatorname{argmax}_{\mathbf{z}} p(\mathbf{z}^{(1:N_z)} | \mathbf{x}^{(1:N_x)})$ .

This general family of algorithms is called **Markov Chain Monte Carlo (MCMC)**: “Monte Carlo” because it is based on a series of random draws; “Markov Chain” because the sampling procedure must be designed such that each sample depends only on the previous sample, and not on the entire sampling history. **Gibbs sampling** is an MCMC algorithm in which each latent variable is sampled from its posterior distribution,

$$\mathbf{z}^{(n)} | \mathbf{x}, \mathbf{z}^{(-n)} \sim p(\mathbf{z}^{(n)} | \mathbf{x}, \mathbf{z}^{(-n)}), \quad [5.41]$$

where  $\mathbf{z}^{(-n)}$  indicates  $\{\mathbf{z} \setminus z^{(n)}\}$ , the set of all latent variables except for  $z^{(n)}$ . Repeatedly drawing samples over all latent variables constructs a Markov chain, and which is guaranteed to converge to a sequence of samples from,  $p(\mathbf{z}^{(1:N_z)} | \mathbf{x}^{(1:N_x)})$ . In probabilistic clustering, the sampling distribution has the following form,

$$p(z^{(i)} | \mathbf{x}, \mathbf{z}^{(-i)}) = \frac{p(\mathbf{x}^{(i)} | z^{(i)}; \boldsymbol{\phi}) \times p(z^{(i)}; \boldsymbol{\mu})}{\sum_{z=1}^K p(\mathbf{x}^{(i)} | z; \boldsymbol{\phi}) \times p(z; \boldsymbol{\mu})} \quad [5.42]$$

$$\propto \text{Multinomial}(\mathbf{x}^{(i)}; \boldsymbol{\phi}_{z^{(i)}}) \times \boldsymbol{\mu}_{z^{(i)}}. \quad [5.43]$$

2885 In this case, the sampling distribution does not depend on the other instances  $\mathbf{x}^{(-i)}, \mathbf{z}^{(-i)}$ :  
 2886 given the parameters  $\boldsymbol{\phi}$  and  $\boldsymbol{\mu}$ , the posterior distribution over each  $z^{(i)}$  can be computed  
 2887 from  $\mathbf{x}^{(i)}$  alone.

2888 In sampling algorithms, there are several choices for how to deal with the parameters.  
 2889 One possibility is to sample them too. To do this, we must add them to the generative  
 2890 story, by introducing a prior distribution. For the multinomial and categorical parameters  
 2891 in the EM clustering model, the **Dirichlet distribution** is a typical choice, since it defines  
 2892 a probability on exactly the set of vectors that can be parameters: vectors that sum to one  
 2893 and include only non-negative numbers.<sup>10</sup>

2894 To incorporate this prior, the generative model must augmented to indicate that each  
 2895  $\boldsymbol{\phi}_z \sim \text{Dirichlet}(\boldsymbol{\alpha}_\phi)$ , and  $\boldsymbol{\mu} \sim \text{Dirichlet}(\boldsymbol{\alpha}_\mu)$ . The hyperparameters  $\boldsymbol{\alpha}$  are typically set to

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<sup>10</sup>If  $\sum_i^K \theta_i = 1$  and  $\theta_i \geq 0$  for all  $i$ , then  $\boldsymbol{\theta}$  is said to be on the  $K - 1$  **simplex**. A Dirichlet distribution with parameter  $\boldsymbol{\alpha} \in \mathbb{R}_+^K$  has support over the  $K - 1$  simplex,

$$p_{\text{Dirichlet}}(\boldsymbol{\theta} | \boldsymbol{\alpha}) = \frac{1}{B(\boldsymbol{\alpha})} \prod_{i=1}^K \theta_i^{\alpha_i - 1} \quad [5.44]$$

$$B(\boldsymbol{\alpha}) = \frac{\prod_{i=1}^K \Gamma(\alpha_i)}{\Gamma(\sum_{i=1}^K \alpha_i)}, \quad [5.45]$$

with  $\Gamma(\cdot)$  indicating the gamma function, a generalization of the factorial function to non-negative reals.

2896 a constant vector  $\alpha = [\alpha, \alpha, \dots, \alpha]$ . When  $\alpha$  is large, the Dirichlet distribution tends to  
 2897 generate vectors that are nearly uniform; when  $\alpha$  is small, it tends to generate vectors that  
 2898 assign most of their probability mass to a few entries. Given prior distributions over  $\phi$   
 2899 and  $\mu$ , we can now include them in Gibbs sampling, drawing values for these parameters  
 2900 from posterior distributions that are conditioned on the other variables in the model.

2901 Unfortunately, sampling  $\phi$  and  $\mu$  usually leads to slow convergence, meaning that a  
 2902 large number of samples is required before the Markov chain breaks free from the initial  
 2903 conditions. The reason is that the sampling distributions for these parameters are tightly  
 2904 constrained by the cluster memberships  $y^{(i)}$ , which in turn are tightly constrained by the  
 2905 parameters. There are two solutions that are frequently employed:

- 2906 • **Empirical Bayesian** methods maintain  $\phi$  and  $\mu$  as parameters rather than latent  
 2907 variables. They still employ sampling in the E-step of the EM algorithm, but they  
 2908 update the parameters using expected counts that are computed from the samples  
 2909 rather than from parametric distributions. This EM-MCMC hybrid is also known  
 2910 as Monte Carlo Expectation Maximization (MCEM; Wei and Tanner, 1990), and is  
 2911 well-suited for cases in which it is difficult to compute  $q^{(i)}$  directly.
- 2912 • In **collapsed Gibbs sampling**, we analytically integrate  $\phi$  and  $\mu$  out of the model.  
 2913 The cluster memberships  $y^{(i)}$  are the only remaining latent variable; we sample them  
 2914 from the compound distribution,

$$p(y^{(i)} | \mathbf{x}^{(1:N)}, \mathbf{y}^{(-i)}; \alpha_\phi, \alpha_\mu) = \int_{\phi, \mu} p(\phi, \mu | \mathbf{y}^{(-i)}, \mathbf{x}^{(1:N)}; \alpha_\phi, \alpha_\mu) p(y^{(i)} | \mathbf{x}^{(1:N)}, \mathbf{y}^{(-i)}, \phi, \mu) d\phi d\mu. \quad [5.46]$$

2915 For multinomial and Dirichlet distributions, this integral can be computed in closed  
 2916 form.

2917 MCMC algorithms are guaranteed to converge to the true posterior distribution over  
 2918 the latent variables, but there is no way to know how long this will take. In practice, the  
 2919 rate of convergence depends on initialization, just as expectation-maximization depends  
 2920 on initialization to avoid local optima. Thus, while Gibbs Sampling and other MCMC  
 2921 algorithms provide a powerful and flexible array of techniques for statistical inference in  
 2922 latent variable models, they are not a panacea for the problems experienced by EM.

### 2923 5.5.2 Spectral learning

Another approach to learning with latent variables is based on the **method of moments**,  
 which makes it possible to avoid the problem of non-convex log-likelihood. Write  $\bar{\mathbf{x}}^{(i)}$  for  
 the normalized vector of word counts in document  $i$ , so that  $\bar{\mathbf{x}}^{(i)} = \mathbf{x}^{(i)} / \sum_{j=1}^V x_j^{(i)}$ . Then

we can form a matrix of word-word co-occurrence probabilities,

$$\mathbf{C} = \sum_{i=1}^N \bar{\mathbf{x}}^{(i)} (\bar{\mathbf{x}}^{(i)})^\top. \quad [5.47]$$

The expected value of this matrix under  $p(\mathbf{x} | \phi, \mu)$ , as

$$E[\mathbf{C}] = \sum_{i=1}^N \sum_{k=1}^K \Pr(Z^{(i)} = k; \boldsymbol{\mu}) \phi_k \phi_k^\top \quad [5.48]$$

$$= \sum_k^K N \mu_k \phi_k \phi_k^\top \quad [5.49]$$

$$= \Phi \text{Diag}(N\mu) \Phi^\top, \quad [5.50]$$

where  $\Phi$  is formed by horizontally concatenating  $\phi_1 \dots \phi_K$ , and  $\text{Diag}(N\mu)$  indicates a diagonal matrix with values  $N\mu_k$  at position  $(k, k)$ . Setting  $\mathbf{C}$  equal to its expectation gives,

$$\mathbf{C} = \Phi \text{Diag}(N\mu) \Phi^\top, \quad [5.51]$$

which is similar to the eigendecomposition  $\mathbf{C} = \mathbf{Q}\Lambda\mathbf{Q}^\top$ . This suggests that simply by finding the eigenvectors and eigenvalues of  $\mathbf{C}$ , we could obtain the parameters  $\phi$  and  $\mu$ , and this is what motivates the name **spectral learning**.

While moment-matching and eigendecomposition are similar in form, they impose different constraints on the solutions: eigendecomposition requires orthonormality, so that  $\mathbf{Q}\mathbf{Q}^\top = \mathbb{I}$ ; in estimating the parameters of a text clustering model, we require that  $\mu$  and the columns of  $\Phi$  are probability vectors. Spectral learning algorithms must therefore include a procedure for converting the solution into vectors that are non-negative and sum to one. One approach is to replace eigendecomposition (or the related singular value decomposition) with non-negative matrix factorization (Xu et al., 2003), which guarantees that the solutions are non-negative (Arora et al., 2013).

After obtaining the parameters  $\phi$  and  $\mu$ , the distribution over clusters can be computed from Bayes' rule:

$$p(z^{(i)} | \mathbf{x}^{(i)}; \phi, \mu) \propto p(\mathbf{x}^{(i)} | z^{(i)}; \phi) \times p(z^{(i)}; \mu). \quad [5.52]$$

Spectral learning yields provably good solutions without regard to initialization, and can be quite fast in practice. However, it is more difficult to apply to a broad family of generative models than more generic techniques like EM and Gibbs Sampling. For more on applying spectral learning across a range of latent variable models, see Anandkumar et al. (2014).

## 2942 Additional resources

2943 There are a number of other learning paradigms that deviate from supervised learning.

- 2944     • **Active learning:** the learner selects unlabeled instances and requests annotations (Set-
- 2945         tles, 2012).
- 2946     • **Multiple instance learning:** labels are applied to bags of instances, with a positive
- 2947         label applied if at least one instance in the bag meets the criterion (Dietterich et al.,
- 2948         1997; Maron and Lozano-Pérez, 1998).
- 2949     • **Constraint-driven learning:** supervision is provided in the form of explicit con-
- 2950         straints on the learner (Chang et al., 2007; Ganchev et al., 2010).
- 2951     • **Distant supervision:** noisy labels are generated from an external resource (Mintz
- 2952         et al., 2009, also see § 17.2.3).
- 2953     • **Multitask learning:** the learner induces a representation that can be used to solve
- 2954         multiple classification tasks (Collobert et al., 2011).
- 2955     • **Transfer learning:** the learner must solve a classification task that differs from the
- 2956         labeled data (Pan and Yang, 2010).

2957 Expectation maximization was introduced by Dempster et al. (1977), and is discussed

2958 in more detail by Murphy (2012). Like most machine learning treatments, Murphy focus

2959 on continuous observations and Gaussian likelihoods, rather than the discrete observa-

2960 tions typically encountered in natural language processing. Murphy (2012) also includes

2961 an excellent chapter on MCMC; for a textbook-length treatment, see Robert and Casella

2962 (2013). For still more on Bayesian latent variable models, see Barber (2012), and for ap-

2963 plications of Bayesian models to natural language processing, see Cohen (2016). Surveys

2964 are available for semi-supervised learning (Zhu and Goldberg, 2009) and domain adapta-

2965 tion (Søgaard, 2013), although both pre-date the current wave of interest in deep learning.

## 2966 Exercises

- 2967     1. Derive the expectation maximization update for the parameter  $\mu$  in the EM cluster-
- 2968         ing model.
- 2969     2. The expectation maximization lower bound  $\mathcal{J}$  is defined in Equation 5.10. Prove
- 2970         that the inverse  $-\mathcal{J}$  is convex in  $q$ . You can use the following facts about convexity:

  - 2971         •  $f(\mathbf{x})$  is convex in  $\mathbf{x}$  iff  $\alpha f(\mathbf{x}_1) + (1 - \alpha)f(\mathbf{x}_2) \geq f(\alpha\mathbf{x}_1 + (1 - \alpha)\mathbf{x}_2)$  for all
  - 2972              $\alpha \in [0, 1]$ .
  - 2973         • If  $f(\mathbf{x})$  and  $g(\mathbf{x})$  are both convex in  $\mathbf{x}$ , then  $f(\mathbf{x}) + g(\mathbf{x})$  is also convex in  $\mathbf{x}$ .

2974       •  $\log(x + y) \leq \log x + \log y.$

- 2975     3. Derive the E-step and M-step updates for the following generative model. You may  
2976     assume that the labels  $y^{(i)}$  are observed, but  $z_m^{(i)}$  is not.

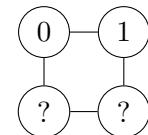
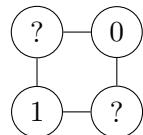
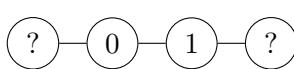
- 2977       • For each instance  $i$ ,

- 2978       – Draw label  $y^{(i)} \sim \text{Categorical}(\boldsymbol{\mu})$
- 2979       – For each token  $m \in \{1, 2, \dots, M^{(i)}\}$ 
  - 2980           \* Draw  $z_m^{(i)} \sim \text{Categorical}(\pi)$
  - 2981           \* If  $z_m^{(i)} = 0$ , draw the current token from a label-specific distribution,  
2982            $w_m^{(i)} \sim \phi_{y^{(i)}}$
  - 2983           \* If  $z_m^{(i)} = 1$ , draw the current token from a document-specific distribu-  
2984           tion,  $w_m^{(i)} \sim \nu^{(i)}$

- 2985     4. Use expectation-maximization clustering to train a word-sense induction system,  
2986     applied to the word *say*.

- 2987       • Import `nltk`, run `nltk.download()` and select `semcor`. Import `semcor`  
2988       from `nltk.corpus`.
- 2989       • The command `semcor.tagged_sentences(tag='sense')` returns an iterator  
2990       over sense-tagged sentences in the corpus. Each sentence can be viewed as  
2991       an iterator over `tree` objects. For `tree` objects that are sense-annotated words,  
2992       you can access the annotation as `tree.label()`, and the word itself with  
2993       `tree.leaves()`. So `semcor.tagged_sentences(tag='sense')[0][2].label()`  
2994       would return the sense annotation of the third word in the first sentence.
- 2995       • Extract all sentences containing the senses `say.v.01` and `say.v.02`.
- 2996       • Build bag-of-words vectors  $x^{(i)}$ , containing the counts of other words in those  
2997       sentences, including all words that occur in at least two sentences.
- 2998       • Implement and run expectation-maximization clustering on the merged data.
- 2999       • Compute the frequency with which each cluster includes instances of `say.v.01`  
3000       and `say.v.02`.

- 3001     5. Using the iterative updates in Equations 5.34-5.36, compute the outcome of the label  
3002     propagation algorithm for the following examples.



3003     The value inside the node indicates the label,  $y^{(i)} \in \{0, 1\}$ , with  $y^{(i)} = ?$  for unlabeled  
 3004     nodes. The presence of an edge between two nodes indicates  $w_{i,j} = 1$ , and the  
 3005     absence of an edge indicates  $w_{i,j} = 0$ . For the third example, you need only compute  
 3006     the first three iterations, and then you can guess at the solution in the limit.

3007     In the remaining exercises, you will try out some approaches for semisupervised learning  
 3008     and domain adaptation. You will need datasets in multiple domains. You can obtain  
 3009     product reviews in multiple domains here: [https://www.cs.jhu.edu/~mdredze/datasets/sentiment/processed\\_acl.tar.gz](https://www.cs.jhu.edu/~mdredze/datasets/sentiment/processed_acl.tar.gz). Choose a source and target domain,  
 3010     e.g. dvds and books, and divide the data for the target domain into training and test sets  
 3011     of equal size.

- 3013     6. First, quantify the cost of cross-domain transfer.
- 3014         • Train a logistic regression classifier on the source domain training set, and eval-  
 3015         uate it on the target domain test set.
  - 3016         • Train a logistic regression classifier on the target domain training set, and eval-  
 3017         uate it on the target domain test set. This is the “direct transfer” baseline.

3018     Compute the difference in accuracy, which is a measure of the transfer loss across  
 3019     domains.

- 3020     7. Next, apply the **label propagation** algorithm from § 5.3.2.

3021     As a baseline, using only 5% of the target domain training set, train a classifier, and  
 3022     compute its accuracy on the target domain test set.

3023     Next, apply label propagation:

- 3024         • Compute the label matrix  $\mathbf{Q}_L$  for the labeled data (5% of the target domain  
 3025         training set), with each row equal to an indicator vector for the label (positive  
 3026         or negative).
- 3027         • Iterate through the target domain instances, including both test and training  
 3028         data. At each instance  $i$ , compute all  $w_{ij}$ , using Equation 5.32, with  $\alpha = 0.01$ .  
 3029         Use these values to fill in column  $i$  of the transition matrix  $\mathbf{T}$ , setting all but the  
 3030         ten largest values to zero for each column  $i$ . Be sure to normalize the column  
 3031         so that the remaining values sum to one. You may need to use a sparse matrix  
 3032         for this to fit into memory.
- 3033         • Apply the iterative updates from Equations 5.34-5.36 to compute the outcome  
 3034         of the label propagation algorithm for the unlabeled examples.

3035     Select the test set instances from  $\mathbf{Q}_U$ , and compute the accuracy of this method.  
 3036     Compare with the supervised classifier trained only on the 5% sample of the target  
 3037     domain training set.

- 3038     8. Using only 5% of the target domain training data (and all of the source domain train-  
3039       ing data), implement one of the supervised domain adaptation baselines in § 5.4.1.  
3040       See if this improves on the “direct transfer” baseline from the previous problem
- 3041     9. Implement EasyAdapt (§ 5.4.1), again using 5% of the target domain training data  
3042       and all of the source domain data.
- 3043    10. Now try unsupervised domain adaptation, using the “linear projection” method  
3044       described in § 5.4.2. Specifically:
- 3045       • Identify 500 pivot features as the words with the highest frequency in the (com-  
3046          plete) training data for the source and target domains. Specifically, let  $x_i^d$  be the  
3047          count of the word  $i$  in domain  $d$ : choose the 500 words with the largest values  
3048          of  $\min(x_i^{\text{source}}, x_i^{\text{target}})$ .
  - 3049       • Train a classifier to predict each pivot feature from the remaining words in the  
3050          document.
  - 3051       • Arrange the features of these classifiers into a matrix  $\Phi$ , and perform truncated  
3052          singular value decomposition, with  $k = 20$
  - 3053       • Train a classifier from the source domain data, using the combined features  
3054           $\mathbf{x}^{(i)} \oplus \mathbf{U}^\top \mathbf{x}^{(i)}$  — these include the original bag-of-words features, plus the pro-  
3055          jected features.
  - 3056       • Apply this classifier to the target domain test set, and compute the accuracy.



3057

## Part II

3058

# Sequences and trees



3059 

# Chapter 6

3060 

## Language models

3061 In probabilistic classification, the problem is to compute the probability of a label, conditioned  
3062 on the text. Let's now consider the inverse problem: computing the probability of  
3063 text itself. Specifically, we will consider models that assign probability to a sequence of  
3064 word tokens,  $p(w_1, w_2, \dots, w_M)$ , with  $w_m \in \mathcal{V}$ . The set  $\mathcal{V}$  is a discrete vocabulary,

$$\mathcal{V} = \{aardvark, abacus, \dots, zither\}. \quad [6.1]$$

3065 Why would you want to compute the probability of a word sequence? In many applications,  
3066 the goal is to produce word sequences as output:

- 3067 • In **machine translation** (chapter 18), we convert from text in a source language to  
3068 text in a target language.
- 3069 • In **speech recognition**, we convert from audio signal to text.
- 3070 • In **summarization** (§ 16.3.4.1; § 19.2), we convert from long texts into short texts.
- 3071 • In **dialogue systems** (§ 19.3), we convert from the user's input (and perhaps an  
3072 external knowledge base) into a text response.

3073 In many of the systems for performing these tasks, there is a subcomponent that computes  
3074 the probability of the output text. The purpose of this component is to generate  
3075 texts that are more **fluent**. For example, suppose we want to translate a sentence from  
3076 Spanish to English.

3077 (6.1) El cafe negro me gusta mucho.

3078 Here is a literal word-for-word translation (a **gloss**):

3079 (6.2) The coffee black me pleases much.

3080 A good language model of English will tell us that the probability of this translation is  
 3081 low, in comparison with more grammatical alternatives,

$$p(\text{The coffee black me pleases much}) < p(\text{I love dark coffee}). \quad [6.2]$$

3082 How can we use this fact? Warren Weaver, one of the early leaders in machine trans-  
 3083 lation, viewed it as a problem of breaking a secret code (Weaver, 1955):

3084 When I look at an article in Russian, I say: 'This is really written in English,  
 3085 but it has been coded in some strange symbols. I will now proceed to decode.'

3086 This observation motivates a generative model (like Naïve Bayes):

3087 • The English sentence  $w^{(e)}$  is generated from a **language model**,  $p_e(w^{(e)})$ .

3088 • The Spanish sentence  $w^{(s)}$  is then generated from a **translation model**,  $p_{s|e}(w^{(s)} | w^{(e)})$ .

Given these two distributions, we can then perform translation by Bayes rule:

$$p_{e|s}(w^{(e)} | w^{(s)}) \propto p_{e,s}(w^{(e)}, w^{(s)}) \quad [6.3]$$

$$= p_{s|e}(w^{(s)} | w^{(e)}) \times p_e(w^{(e)}). \quad [6.4]$$

3089 This is sometimes called the **noisy channel model**, because it envisions English text  
 3090 turning into Spanish by passing through a noisy channel,  $p_{s|e}$ . What is the advantage of  
 3091 modeling translation this way, as opposed to modeling  $p_{e|s}$  directly? The crucial point is  
 3092 that the two distributions  $p_{s|e}$  (the translation model) and  $p_e$  (the language model) can be  
 3093 estimated from separate data. The translation model requires examples of correct trans-  
 3094 lations, but the language model requires only text in English. Such monolingual data is  
 3095 much more widely available. Furthermore, once estimated, the language model  $p_e$  can be  
 3096 reused in any application that involves generating English text, from summarization to  
 3097 speech recognition.

## 3098 6.1 *N*-gram language models

A simple approach to computing the probability of a sequence of tokens is to use a **relative frequency estimate**. For example, consider the quote, attributed to Picasso, "*computers are useless, they can only give you answers.*" We can estimate the probability of this sentence,

$$\begin{aligned} p(\text{Computers are useless, they can only give you answers}) \\ = \frac{\text{count}(\text{Computers are useless, they can only give you answers})}{\text{count}(\text{all sentences ever spoken})} \end{aligned} \quad [6.5]$$

3099 This estimator is **unbiased**: in the theoretical limit of infinite data, the estimate will  
 3100 be correct. But in practice, we are asking for accurate counts over an infinite number of  
 3101 events, since sequences of words can be arbitrarily long. Even with an aggressive upper  
 3102 bound of, say,  $M = 20$  tokens in the sequence, the number of possible sequences is  $V^{20}$ . A  
 3103 small vocabulary for English would have  $V = 10^4$ , so there are  $10^{80}$  possible sequences.  
 3104 Clearly, this estimator is very data-hungry, and suffers from high variance: even gram-  
 3105 matical sentences will have probability zero if have not occurred in the training data.<sup>1</sup> We  
 3106 therefore need to introduce bias to have a chance of making reliable estimates from finite  
 3107 training data. The language models that follow in this chapter introduce bias in various  
 3108 ways.

We begin with  $n$ -gram language models, which compute the probability of a sequence as the product of probabilities of subsequences. The probability of a sequence  $p(w) = p(w_1, w_2, \dots, w_M)$  can be refactored using the chain rule (see § A.2):

$$p(w) = p(w_1, w_2, \dots, w_M) \quad [6.6]$$

$$= p(w_1) \times p(w_2 | w_1) \times p(w_3 | w_2, w_1) \times \dots \times p(w_M | w_{M-1}, \dots, w_1) \quad [6.7]$$

Each element in the product is the probability of a word given all its predecessors. We can think of this as a *word prediction* task: given the context *Computers are*, we want to compute a probability over the next token. The relative frequency estimate of the probability of the word *useless* in this context is,

$$\begin{aligned} p(\text{useless} | \text{computers are}) &= \frac{\text{count}(\text{computers are useless})}{\sum_{x \in \mathcal{V}} \text{count}(\text{computers are } x)} \\ &= \frac{\text{count}(\text{computers are useless})}{\text{count}(\text{computers are})}. \end{aligned}$$

3109 We haven't made any approximations yet, and we could have just as well applied the  
 3110 chain rule in reverse order,

$$p(w) = p(w_M) \times p(w_{M-1} | w_M) \times \dots \times p(w_1 | w_2, \dots, w_M), \quad [6.8]$$

3111 or in any other order. But this means that we also haven't really made any progress:  
 3112 to compute the conditional probability  $p(w_M | w_{M-1}, w_{M-2}, \dots, w_1)$ , we would need to  
 3113 model  $V^{M-1}$  contexts. Such a distribution cannot be estimated from any realistic sample  
 3114 of text.

---

<sup>1</sup>Chomsky has famously argued that this is evidence against the very concept of probabilistic language models: no such model could distinguish the grammatical sentence *colorless green ideas sleep furiously* from the ungrammatical permutation *furiously sleep ideas green colorless*. Indeed, even the bigrams in these two examples are unlikely to occur — at least, not in texts written before Chomsky proposed this example.

To solve this problem,  $n$ -gram models make a crucial simplifying approximation: condition on only the past  $n - 1$  words.

$$p(w_m | w_{m-1} \dots w_1) \approx p(w_m | w_{m-1}, \dots, w_{m-n+1}) \quad [6.9]$$

This means that the probability of a sentence  $w$  can be approximated as

$$p(w_1, \dots, w_M) \approx \prod_{m=1}^M p(w_m | w_{m-1}, \dots, w_{m-n+1}) \quad [6.10]$$

To compute the probability of an entire sentence, it is convenient to pad the beginning and end with special symbols  $\square$  and  $\blacksquare$ . Then the bigram ( $n = 2$ ) approximation to the probability of *I like black coffee* is:

$$p(I \text{ like black coffee}) = p(I | \square) \times p(\text{like} | I) \times p(\text{black} | \text{like}) \times p(\text{coffee} | \text{black}) \times p(\blacksquare | \text{coffee}). \quad [6.11]$$

3115 This model requires estimating and storing the probability of only  $V^n$  events, which is  
 3116 exponential in the order of the  $n$ -gram, and not  $V^M$ , which is exponential in the length of  
 3117 the sentence. The  $n$ -gram probabilities can be computed by relative frequency estimation,

$$p(w_m | w_{m-1}, w_{m-2}) = \frac{\text{count}(w_{m-2}, w_{m-1}, w_m)}{\sum_{w'} \text{count}(w_{m-2}, w_{m-1}, w')} \quad [6.12]$$

3118 The hyperparameter  $n$  controls the size of the context used in each conditional proba-  
 3119 bility. If this is misspecified, the language model will perform poorly. Let's consider the  
 3120 potential problems concretely.

3121 **When  $n$  is too small.** Consider the following sentences:

- 3122     (6.3) **Gorillas** always like to groom **their** friends.  
 3123     (6.4) The **computer** that's on the 3rd floor of our office building **crashed**.

3124 In each example, the bolded words depend on each other: the likelihood of *their*  
 3125 depends on knowing that *gorillas* is plural, and the likelihood of *crashed* depends on  
 3126 knowing that the subject is a *computer*. If the  $n$ -grams are not big enough to capture  
 3127 this context, then the resulting language model would offer probabilities that are too  
 3128 low for these sentences, and too high for sentences that fail basic linguistic tests like  
 3129 number agreement.

3130 **When  $n$  is too big.** In this case, it is hard to get good estimates of the  $n$ -gram parameters from  
 3131 our dataset, because of data sparsity. To handle the *gorilla* example, it is necessary to  
 3132 model 6-grams, which means accounting for  $V^6$  events. Under a very small vocabulary of  $V = 10^4$ , this means estimating the probability of  $10^{24}$  distinct events.

3134 These two problems point to another **bias-variance tradeoff** (see § 2.1.4). A small  $n$ -  
 3135 gram size introduces high bias, and a large  $n$ -gram size introduces high variance. But  
 3136 in reality we often have both problems at the same time! Language is full of long-range  
 3137 dependencies that we cannot capture because  $n$  is too small; at the same time, language  
 3138 datasets are full of rare phenomena, whose probabilities we fail to estimate accurately  
 3139 because  $n$  is too large. One solution is to try to keep  $n$  large, while still making low-  
 3140 variance estimates of the underlying parameters. To do this, we will introduce a different  
 3141 sort of bias: **smoothing**.

## 3142 6.2 Smoothing and discounting

3143 Limited data is a persistent problem in estimating language models. In § 6.1, we presented  
 3144  $n$ -grams as a partial solution. sparse data can be a problem even for low-order  $n$ -grams;  
 3145 at the same time, many linguistic phenomena, like subject-verb agreement, cannot be in-  
 3146 corporated into language models without high-order  $n$ -grams. It is therefore necessary to  
 3147 add additional inductive biases to  $n$ -gram language models. This section covers some of  
 3148 the most intuitive and common approaches, but there are many more (Chen and Good-  
 3149 man, 1999).

### 3150 6.2.1 Smoothing

3151 A major concern in language modeling is to avoid the situation  $p(w) = 0$ , which could  
 3152 arise as a result of a single unseen n-gram. A similar problem arose in Naïve Bayes, and  
 3153 the solution was **smoothing**: adding imaginary “pseudo” counts. The same idea can be  
 3154 applied to  $n$ -gram language models, as shown here in the bigram case,

$$P_{\text{smooth}}(w_m \mid w_{m-1}) = \frac{\text{count}(w_{m-1}, w_m) + \alpha}{\sum_{w' \in \mathcal{V}} \text{count}(w_{m-1}, w') + V\alpha}. \quad [6.13]$$

3155 This basic framework is called **Lidstone smoothing**, but special cases have other names:

- 3156 • **Laplace smoothing** corresponds to the case  $\alpha = 1$ .
- 3157 • **Jeffreys-Perks law** corresponds to the case  $\alpha = 0.5$ . Manning and Schütze (1999)  
 3158 offer more insight on the justifications for this setting.

3159 To maintain normalization, anything that we add to the numerator ( $\alpha$ ) must also ap-  
 3160 pear in the denominator ( $V\alpha$ ). This idea is reflected in the concept of **effective counts**:

$$c_i^* = (c_i + \alpha) \frac{M}{M + V\alpha}, \quad [6.14]$$

	counts	unsmoothed probability	Lidstone smoothing, $\alpha = 0.1$		Discounting, $d = 0.1$	
			effective counts	smoothed probability	effective counts	smoothed probability
<i>impropriety</i>	8	0.4	7.826	0.391	7.9	0.395
<i>offense</i>	5	0.25	4.928	0.246	4.9	0.245
<i>damage</i>	4	0.2	3.961	0.198	3.9	0.195
<i>deficiencies</i>	2	0.1	2.029	0.101	1.9	0.095
<i>outbreak</i>	1	0.05	1.063	0.053	0.9	0.045
<i>infirmity</i>	0	0	0.097	0.005	0.25	0.013
<i>cephalopods</i>	0	0	0.097	0.005	0.25	0.013

Table 6.1: Example of Lidstone smoothing and absolute discounting in a bigram language model, for the context *(alleged, -)*, for a toy corpus with a total of twenty counts over the seven words shown. Note that discounting decreases the probability for all but the unseen words, while Lidstone smoothing increases the effective counts and probabilities for *deficiencies* and *outbreak*.

where  $c_i$  is the count of event  $i$ ,  $c_i^*$  is the effective count, and  $M = \sum_{i=1}^V c_i$  is the total number of tokens in the dataset  $(w_1, w_2, \dots, w_M)$ . This term ensures that  $\sum_{i=1}^V c_i^* = \sum_{i=1}^V c_i = M$ . The **discount** for each n-gram is then computed as,

$$d_i = \frac{c_i^*}{c_i} = \frac{(c_i + \alpha)}{c_i} \frac{M}{(M + V\alpha)}.$$

### 3161 6.2.2 Discounting and backoff

3162 Discounting “borrows” probability mass from observed  $n$ -grams and redistributes it. In  
 3163 Lidstone smoothing, the borrowing is done by increasing the denominator of the relative  
 3164 frequency estimates. The borrowed probability mass is then redistributed by increasing  
 3165 the numerator for all  $n$ -grams. Another approach would be to borrow the same amount  
 3166 of probability mass from all observed  $n$ -grams, and redistribute it among only the unob-  
 3167 served  $n$ -grams. This is called **absolute discounting**. For example, suppose we set an  
 3168 absolute discount  $d = 0.1$  in a bigram model, and then redistribute this probability mass  
 3169 equally over the unseen words. The resulting probabilities are shown in Table 6.1.

Discounting reserves some probability mass from the observed data, and we need not redistribute this probability mass equally. Instead, we can **backoff** to a lower-order language model: if you have trigrams, use trigrams; if you don’t have trigrams, use bigrams; if you don’t even have bigrams, use unigrams. This is called **Katz backoff**. In the simple

case of backing off from bigrams to unigrams, the bigram probabilities are computed as,

$$c^*(i, j) = c(i, j) - d \quad [6.15]$$

$$p_{\text{Katz}}(i | j) = \begin{cases} \frac{c^*(i, j)}{c(j)} & \text{if } c(i, j) > 0 \\ \alpha(j) \times \frac{p_{\text{unigram}}(i)}{\sum_{i': c(i', j)=0} p_{\text{unigram}}(i')} & \text{if } c(i, j) = 0. \end{cases} \quad [6.16]$$

3170     The term  $\alpha(j)$  indicates the amount of probability mass that has been discounted for  
 3171     context  $j$ . This probability mass is then divided across all the unseen events,  $\{i' : c(i', j) =$   
 3172     0\}, proportional to the unigram probability of each word  $i'$ . The discount parameter  $d$  can  
 3173     be optimized to maximize performance (typically held-out log-likelihood) on a develop-  
 3174     ment set.

### 3175     6.2.3 \*Interpolation

3176     Backoff is one way to combine different order  $n$ -gram models. An alternative approach  
 3177     is **interpolation**: setting the probability of a word in context to a weighted sum of its  
 3178     probabilities across progressively shorter contexts.

Instead of choosing a single  $n$  for the size of the  $n$ -gram, we can take the weighted average across several  $n$ -gram probabilities. For example, for an interpolated trigram model,

$$\begin{aligned} p_{\text{Interpolation}}(w_m | w_{m-1}, w_{m-2}) &= \lambda_3 p_3^*(w_m | w_{m-1}, w_{m-2}) \\ &\quad + \lambda_2 p_2^*(w_m | w_{m-1}) \\ &\quad + \lambda_1 p_1^*(w_m). \end{aligned}$$

3179     In this equation,  $p_n^*$  is the unsmoothed empirical probability given by an  $n$ -gram lan-  
 3180     guage model, and  $\lambda_n$  is the weight assigned to this model. To ensure that the interpolated  
 3181      $p(w)$  is still a valid probability distribution, the values of  $\lambda$  must obey the constraint,  
 3182      $\sum_{n=1}^{n_{\max}} \lambda_n = 1$ . But how to find the specific values?

3183     An elegant solution is **expectation maximization**. Recall from chapter 5 that we can  
 3184     think about EM as learning with *missing data*: we just need to choose missing data such  
 3185     that learning would be easy if it weren't missing. What's missing in this case? Think of  
 3186     each word  $w_m$  as drawn from an  $n$ -gram of unknown size,  $z_m \in \{1 \dots n_{\max}\}$ . This  $z_m$  is  
 3187     the missing data that we are looking for. Therefore, the application of EM to this problem  
 3188     involves the following **generative process**:

3189     **for** Each token  $w_m, m = 1, 2, \dots, M$  **do**:  
 3190        draw the  $n$ -gram size  $z_m \sim \text{Categorical}(\lambda)$ ;  
 3191        draw  $w_m \sim p_{z_m}^*(w_m | w_{m-1}, \dots, w_{m-z_m})$ .

If the missing data  $\{Z_m\}$  were known, then  $\lambda$  could be estimated as the relative frequency,

$$\lambda_z = \frac{\text{count}(Z_m = z)}{M} \quad [6.17]$$

$$\propto \sum_{m=1}^M \delta(Z_m = z). \quad [6.18]$$

But since we do not know the values of the latent variables  $Z_m$ , we impute a distribution  $q_m$  in the E-step, which represents the degree of belief that word token  $w_m$  was generated from a  $n$ -gram of order  $z_m$ ,

$$q_m(z) \triangleq \Pr(Z_m = z \mid \mathbf{w}_{1:m}; \lambda) \quad [6.19]$$

$$= \frac{p(w_m \mid \mathbf{w}_{1:m-1}, Z_m = z) \times p(z)}{\sum_{z'} p(w_m \mid \mathbf{w}_{1:m-1}, Z_m = z') \times p(z')} \quad [6.20]$$

$$\propto p_z^*(w_m \mid \mathbf{w}_{1:m-1}) \times \lambda_z. \quad [6.21]$$

In the M-step,  $\lambda$  is computed by summing the expected counts under  $q$ ,

$$\lambda_z \propto \sum_{m=1}^M q_m(z). \quad [6.22]$$

3193 A solution is obtained by iterating between updates to  $q$  and  $\lambda$ . The complete algorithm  
 3194 is shown in Algorithm 10.

---

**Algorithm 10** Expectation-maximization for interpolated language modeling
 

---

```

1: procedure ESTIMATE INTERPOLATED  $n$ -GRAM ( $\mathbf{w}_{1:M}, \{p_n^*\}_{n \in 1:n_{\max}}$ )
2:   for  $z \in \{1, 2, \dots, n_{\max}\}$  do ▷ Initialization
3:      $\lambda_z \leftarrow \frac{1}{n_{\max}}$ 
4:   repeat
5:     for  $m \in \{1, 2, \dots, M\}$  do ▷ E-step
6:       for  $z \in \{1, 2, \dots, n_{\max}\}$  do
7:          $q_m(z) \leftarrow p_z^*(w_m \mid \mathbf{w}_{1:m-1}) \times \lambda_z$ 
8:        $q_m \leftarrow \text{Normalize}(q_m)$ 
9:     for  $z \in \{1, 2, \dots, n_{\max}\}$  do ▷ M-step
10:       $\lambda_z \leftarrow \frac{1}{M} \sum_{m=1}^M q_m(z)$ 
11:    until tired
12:    return  $\lambda$ 
  
```

---

3195 **6.2.4 \*Kneser-Ney smoothing**

3196 Kneser-Ney smoothing is based on absolute discounting, but it redistributes the result-  
 3197 ing probability mass in a different way from Katz backoff. Empirical evidence points  
 3198 to Kneser-Ney smoothing as the state-of-art for  $n$ -gram language modeling (Goodman,  
 3199 2001). To motivate Kneser-Ney smoothing, consider the example: *I recently visited ..*  
 3200 Which of the following is more likely?

- 3201     • *Francisco*  
 3202     • *Duluth*

3203 Now suppose that both bigrams *visited Duluth* and *visited Francisco* are unobserved in  
 3204 the training data, and furthermore, the unigram probability  $p_1^*(\text{Francisco})$  is greater than  
 3205  $p^*(\text{Duluth})$ . Nonetheless we would still guess that  $p(\text{visited Duluth}) > p(\text{visited Francisco})$ ,  
 3206 because *Duluth* is a more “versatile” word: it can occur in many contexts, while *Francisco*  
 3207 usually occurs in a single context, following the word *San*. This notion of versatility is the  
 3208 key to Kneser-Ney smoothing.

Writing  $u$  for a context of undefined length, and  $\text{count}(w, u)$  as the count of word  $w$  in  
 context  $u$ , we define the Kneser-Ney bigram probability as

$$p_{KN}(w | u) = \begin{cases} \frac{\text{count}(w, u) - d}{\text{count}(u)}, & \text{count}(w, u) > 0 \\ \alpha(u) \times p_{\text{continuation}}(w), & \text{otherwise} \end{cases} \quad [6.23]$$

$$p_{\text{continuation}}(w) = \frac{|u : \text{count}(w, u) > 0|}{\sum_{w' \in \mathcal{V}} |u' : \text{count}(w', u') > 0|}. \quad [6.24]$$

First, note that we reserve probability mass using absolute discounting  $d$ , which is taken from all unobserved  $n$ -grams. The total amount of discounting in context  $u$  is  $d \times |w : \text{count}(w, u) > 0|$ , and we divide this probability mass equally among the unseen  $n$ -grams,

$$\alpha(u) = |w : \text{count}(w, u) > 0| \times \frac{d}{\text{count}(u)}. \quad [6.25]$$

3209 This is the amount of probability mass left to account for versatility, which we define via  
 3210 the *continuation probability*  $p_{\text{continuation}}(w)$  as proportional to the number of observed con-  
 3211 texts in which  $w$  appears. The numerator of the continuation probability is the number of  
 3212 contexts  $u$  in which  $w$  appears; the denominator normalizes the probability by summing  
 3213 the same quantity over all words  $w'$ .

3214 The idea of modeling versatility by counting contexts may seem heuristic, but there is  
 3215 an elegant theoretical justification from Bayesian nonparametrics (Teh, 2006). Kneser-Ney  
 3216 smoothing on  $n$ -grams was the dominant language modeling technique before the arrival  
 3217 of neural language models.

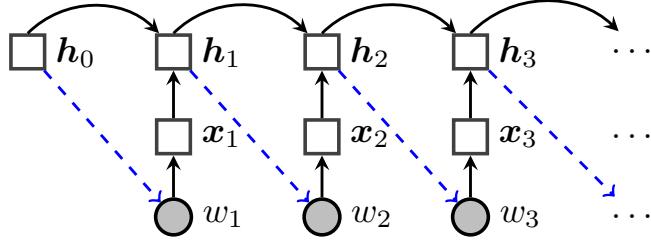


Figure 6.1: The recurrent neural network language model, viewed as an “unrolled” computation graph. Solid lines indicate direct computation, dotted blue lines indicate probabilistic dependencies, circles indicate random variables, and squares indicate computation nodes.

### 3218 6.3 Recurrent neural network language models

3219  $N$ -gram language models have been largely supplanted by **neural networks**. These mod-  
 3220 els do not make the  $n$ -gram assumption of restricted context; indeed, they can incorpo-  
 3221 rate arbitrarily distant contextual information, while remaining computationally and statisti-  
 3222 cally tractable.

3223 The first insight behind neural language models is to treat word prediction as a *dis-  
 3224 criminative* learning task.<sup>2</sup> The goal is to compute the probability  $p(w | u)$ , where  $w \in \mathcal{V}$  is  
 3225 a word, and  $u$  is the context, which depends on the previous words. Rather than directly  
 3226 estimating the word probabilities from (smoothed) relative frequencies, we can treat  
 3227 language modeling as a machine learning problem, and estimate parameters that maxi-  
 3228 mize the log conditional probability of a corpus.

3229 The second insight is to reparametrize the probability distribution  $p(w | u)$  as a func-  
 3230 tion of two dense  $K$ -dimensional numerical vectors,  $\beta_w \in \mathbb{R}^K$ , and  $v_u \in \mathbb{R}^K$ ,

$$p(w | u) = \frac{\exp(\beta_w \cdot v_u)}{\sum_{w' \in \mathcal{V}} \exp(\beta_{w'} \cdot v_u)}, \quad [6.26]$$

3231 where  $\beta_w \cdot v_u$  represents a dot product. As usual, the denominator ensures that the prob-  
 3232 ability distribution is properly normalized. This vector of probabilities is equivalent to  
 3233 applying the **softmax** transformation (see § 3.1) to the vector of dot-products,

$$p(\cdot | u) = \text{SoftMax}([\beta_1 \cdot v_u, \beta_2 \cdot v_u, \dots, \beta_V \cdot v_u]). \quad [6.27]$$

The word vectors  $\beta_w$  are parameters of the model, and are estimated directly. The context vectors  $v_u$  can be computed in various ways, depending on the model. A simple

---

<sup>2</sup>This idea predates neural language models (e.g., Rosenfeld, 1996; Roark et al., 2007).

but effective neural language model can be built from a **recurrent neural network** (RNN; Mikolov et al., 2010). The basic idea is to recurrently update the context vectors while moving through the sequence. Let  $\mathbf{h}_m$  represent the contextual information at position  $m$  in the sequence. RNN language models are defined,

$$\mathbf{x}_m \triangleq \phi_{w_m} \quad [6.28]$$

$$\mathbf{h}_m = \text{RNN}(\mathbf{x}_m, \mathbf{h}_{m-1}) \quad [6.29]$$

$$p(w_{m+1} | w_1, w_2, \dots, w_m) = \frac{\exp(\beta_{w_{m+1}} \cdot \mathbf{h}_m)}{\sum_{w' \in \mathcal{V}} \exp(\beta_{w'} \cdot \mathbf{h}_m)}, \quad [6.30]$$

where  $\phi$  is a matrix of **input word embeddings**, and  $\mathbf{x}_m$  denotes the embedding for word  $w_m$ . The conversion of  $w_m$  to  $\mathbf{x}_m$  is sometimes known as a **lookup layer**, because we simply lookup the embeddings for each word in a table; see § 3.2.4.

The **Elman unit** defines a simple recurrent operation (Elman, 1990),

$$\text{RNN}(\mathbf{x}_m, \mathbf{h}_{m-1}) \triangleq g(\Theta \mathbf{h}_{m-1} + \mathbf{x}_m), \quad [6.31]$$

where  $\Theta \in \mathbb{R}^{K \times K}$  is the recurrence matrix and  $g$  is a non-linear transformation function, often defined as the elementwise hyperbolic tangent  $\tanh$  (see § 3.1).<sup>3</sup> The  $\tanh$  acts as a **squashing function**, ensuring that each element of  $\mathbf{h}_m$  is constrained to the range  $[-1, 1]$ .

Although each  $w_m$  depends on only the context vector  $\mathbf{h}_{m-1}$ , this vector is in turn influenced by *all* previous tokens,  $w_1, w_2, \dots, w_{m-1}$ , through the recurrence operation:  $w_1$  affects  $\mathbf{h}_1$ , which affects  $\mathbf{h}_2$ , and so on, until the information is propagated all the way to  $\mathbf{h}_{m-1}$ , and then on to  $w_m$  (see Figure 6.1). This is an important distinction from  $n$ -gram language models, where any information outside the  $n$ -word window is ignored. In principle, the RNN language model can handle long-range dependencies, such as number agreement over long spans of text — although it would be difficult to know where exactly in the vector  $\mathbf{h}_m$  this information is represented. The main limitation is that information is attenuated by repeated application of the squashing function  $g$ . **Long short-term memories** (LSTMs), described below, are a variant of RNNs that address this issue, using memory cells to propagate information through the sequence without applying nonlinearities (Hochreiter and Schmidhuber, 1997).

The denominator in Equation 6.30 is a computational bottleneck, because it involves a sum over the entire vocabulary. One solution is to use a **hierarchical softmax** function, which computes the sum more efficiently by organizing the vocabulary into a tree (Mikolov et al., 2011). Another strategy is to optimize an alternative metric, such as **noise-contrastive estimation** (Gutmann and Hyvärinen, 2012), which learns by distinguishing observed instances from artificial instances generated from a noise distribution (Mnih and Teh, 2012). Both of these strategies are described in § 14.5.3.

<sup>3</sup>In the original Elman network, the sigmoid function was used in place of  $\tanh$ . For an illuminating mathematical discussion of the advantages and disadvantages of various nonlinearities in recurrent neural networks, see the lecture notes from Cho (2015).

3260 **6.3.1 Backpropagation through time**

3261 The recurrent neural network language model has the following parameters:

- 3262 •  $\phi_i \in \mathbb{R}^K$ , the “input” word vectors (these are sometimes called **word embeddings**,  
3263 since each word is embedded in a  $K$ -dimensional space);
- 3264 •  $\beta_i \in \mathbb{R}^K$ , the “output” word vectors;
- 3265 •  $\Theta \in \mathbb{R}^{K \times K}$ , the recurrence operator;
- 3266 •  $\mathbf{h}_0$ , the initial state.

3267 Each of these parameters can be estimated by formulating an objective function over the  
3268 training corpus,  $L(\mathbf{w})$ , and then applying **backpropagation** to obtain gradients on the  
3269 parameters from a minibatch of training examples (see § 3.3.1). Gradient-based updates  
3270 can be computed from an online learning algorithm such as stochastic gradient descent  
3271 (see § 2.5.2).

3272 The application of backpropagation to recurrent neural networks is known as **back-**  
3273 **propagation through time**, because the gradients on units at time  $m$  depend in turn on the  
3274 gradients of units at earlier times  $n < m$ . Let  $\ell_{m+1}$  represent the negative log-likelihood  
3275 of word  $m + 1$ ,

$$\ell_{m+1} = -\log p(w_{m+1} | w_1, w_2, \dots, w_m). \quad [6.32]$$

We require the gradient of this loss with respect to each parameter, such as  $\theta_{k,k'}$ , an individual element in the recurrence matrix  $\Theta$ . Since the loss depends on the parameters only through  $\mathbf{h}_m$ , we can apply the chain rule of differentiation,

$$\frac{\partial \ell_{m+1}}{\partial \theta_{k,k'}} = \frac{\partial \ell_{m+1}}{\partial \mathbf{h}_m} \frac{\partial \mathbf{h}_m}{\partial \theta_{k,k'}}. \quad [6.33]$$

The vector  $\mathbf{h}_m$  depends on  $\Theta$  in several ways. First,  $\mathbf{h}_m$  is computed by multiplying  $\Theta$  by the previous state  $\mathbf{h}_{m-1}$ . But the previous state  $\mathbf{h}_{m-1}$  also depends on  $\Theta$ :

$$\mathbf{h}_m = g(\mathbf{x}_m, \mathbf{h}_{m-1}) \quad [6.34]$$

$$\frac{\partial h_{m,k}}{\partial \theta_{k,k'}} = g'(\mathbf{x}_{m,k} + \boldsymbol{\theta}_k \cdot \mathbf{h}_{m-1})(h_{m-1,k'} + \boldsymbol{\theta}_k \cdot \frac{\partial \mathbf{h}_{m-1}}{\partial \theta_{k,k'}}), \quad [6.35]$$

3276 where  $g'$  is the local derivative of the nonlinear function  $g$ . The key point in this equation  
3277 is that the derivative  $\frac{\partial \mathbf{h}_m}{\partial \theta_{k,k'}}$  depends on  $\frac{\partial \mathbf{h}_{m-1}}{\partial \theta_{k,k'}}$ , which will depend in turn on  $\frac{\partial \mathbf{h}_{m-2}}{\partial \theta_{k,k'}}$ , and  
3278 so on, until reaching the initial state  $\mathbf{h}_0$ .

3279 Each derivative  $\frac{\partial \mathbf{h}_m}{\partial \theta_{k,k'}}$  will be reused many times: it appears in backpropagation from  
3280 the loss  $\ell_m$ , but also in all subsequent losses  $\ell_{n>m}$ . Neural network toolkits such as  
3281 Torch (Collobert et al., 2011) and DyNet (Neubig et al., 2017) compute the necessary

derivatives automatically, and cache them for future use. An important distinction from the feedforward neural networks considered in chapter 3 is that the size of the computation graph is not fixed, but varies with the length of the input. This poses difficulties for toolkits that are designed around static computation graphs, such as TensorFlow (Abadi et al., 2016).<sup>4</sup>

### 6.3.2 Hyperparameters

The RNN language model has several hyperparameters that must be tuned to ensure good performance. The model capacity is controlled by the size of the word and context vectors  $K$ , which play a role that is somewhat analogous to the size of the  $n$ -gram context. For datasets that are large with respect to the vocabulary (i.e., there is a large token-to-type ratio), we can afford to estimate a model with a large  $K$ , which enables more subtle distinctions between words and contexts. When the dataset is relatively small, then  $K$  must be smaller too, or else the model may “memorize” the training data, and fail to generalize. Unfortunately, this general advice has not yet been formalized into any concrete formula for choosing  $K$ , and trial-and-error is still necessary. Overfitting can also be prevented by **dropout**, which involves randomly setting some elements of the computation to zero (Srivastava et al., 2014), forcing the learner not to rely too much on any particular dimension of the word or context vectors. The dropout rate must also be tuned on development data.

### 6.3.3 Gated recurrent neural networks

In principle, recurrent neural networks can propagate information across infinitely long sequences. But in practice, repeated applications of the nonlinear recurrence function causes this information to be quickly attenuated. The same problem affects learning: back-propagation can lead to **vanishing gradients** that decay to zero, or **exploding gradients** that increase towards infinity (Bengio et al., 1994). The exploding gradient problem can be addressed by clipping gradients at some maximum value (Pascanu et al., 2013). The other issues must be addressed by altering the model itself.

The **long short-term memory (LSTM)** (Hochreiter and Schmidhuber, 1997) is a popular variant of RNNs that is more robust to these problems. This model augments the hidden state  $\mathbf{h}_m$  with a **memory cell**  $c_m$ . The value of the memory cell at each time  $m$  is a gated sum of two quantities: its previous value  $c_{m-1}$ , and an “update”  $\tilde{c}_m$ , which is computed from the current input  $x_m$  and the previous hidden state  $\mathbf{h}_{m-1}$ . The next state  $\mathbf{h}_m$  is then computed from the memory cell. Because the memory cell is not passed through a non-linear squashing function during the update, it is possible for information to propagate through the network over long distances.

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<sup>4</sup>See <https://www.tensorflow.org/tutorials/recurrent> (retrieved Feb 8, 2018).

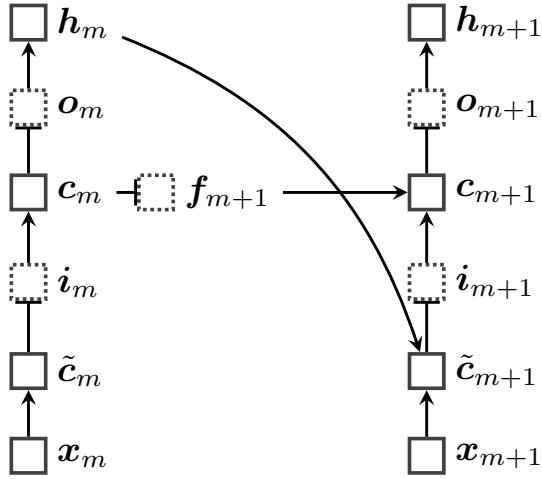


Figure 6.2: The long short-term memory (LSTM) architecture. Gates are shown in boxes with dotted edges. In an LSTM language model, each  $h_m$  would be used to predict the next word  $w_{m+1}$ .

The gates are functions of the input and previous hidden state. They are computed from elementwise sigmoid activations,  $\sigma(x) = (1 + \exp(-x))^{-1}$ , ensuring that their values will be in the range  $[0, 1]$ . They can therefore be viewed as soft, differentiable logic gates. The LSTM architecture is shown in Figure 6.2, and the complete update equations are:

$$f_{m+1} = \sigma(\Theta^{(h \rightarrow f)} h_m + \Theta^{(x \rightarrow f)} x_{m+1} + b_f) \quad \text{forget gate} \quad [6.36]$$

$$i_{m+1} = \sigma(\Theta^{(h \rightarrow i)} h_m + \Theta^{(x \rightarrow i)} x_{m+1} + b_i) \quad \text{input gate} \quad [6.37]$$

$$\tilde{c}_{m+1} = \tanh(\Theta^{(h \rightarrow c)} h_m + \Theta^{(x \rightarrow c)} x_{m+1}) \quad \text{update candidate} \quad [6.38]$$

$$c_{m+1} = f_{m+1} \odot c_m + i_{m+1} \odot \tilde{c}_{m+1} \quad \text{memory cell update} \quad [6.39]$$

$$o_{m+1} = \sigma(\Theta^{(h \rightarrow o)} h_m + \Theta^{(x \rightarrow o)} x_{m+1} + b_o) \quad \text{output gate} \quad [6.40]$$

$$h_{m+1} = o_{m+1} \odot \tanh(c_{m+1}) \quad \text{output.} \quad [6.41]$$

3316 The operator  $\odot$  is an elementwise (Hadamard) product. Each gate is controlled by a vec-  
 3317 tor of weights, which parametrize the previous hidden state (e.g.,  $\Theta^{(h \rightarrow f)}$ ) and the current  
 3318 input (e.g.,  $\Theta^{(x \rightarrow f)}$ ), plus a vector offset (e.g.,  $b_f$ ). The overall operation can be infor-  
 3319 mally summarized as  $(h_m, c_m) = \text{LSTM}(x_m, (h_{m-1}, c_{m-1}))$ , with  $(h_m, c_m)$  representing  
 3320 the LSTM state after reading token  $m$ .

3321 The LSTM outperforms standard recurrent neural networks across a wide range of  
 3322 problems. It was first used for language modeling by Sundermeyer et al. (2012), but can  
 3323 be applied more generally: the vector  $h_m$  can be treated as a complete representation of

3324 the input sequence up to position  $m$ , and can be used for any labeling task on a sequence  
 3325 of tokens, as we will see in the next chapter.

3326 There are several LSTM variants, of which the Gated Recurrent Unit (Cho et al., 2014)  
 3327 is one of the more well known. Many software packages implement a variety of RNN  
 3328 architectures, so choosing between them is simple from a user’s perspective. Jozefowicz  
 3329 et al. (2015) provide an empirical comparison of various modeling choices circa 2015.

## 3330 6.4 Evaluating language models

3331 Language modeling is not usually an application in itself: language models are typically  
 3332 components of larger systems, and they would ideally be evaluated **extrinsically**. This  
 3333 means evaluating whether the language model improves performance on the application  
 3334 task, such as machine translation or speech recognition. But this is often hard to do, and  
 3335 depends on details of the overall system which may be irrelevant to language modeling.  
 3336 In contrast, **intrinsic evaluation** is task-neutral. Better performance on intrinsic metrics  
 3337 may be expected to improve extrinsic metrics across a variety of tasks, but there is always  
 3338 the risk of over-optimizing the intrinsic metric. This section discusses some intrinsic met-  
 3339 rics, but keep in mind the importance of performing extrinsic evaluations to ensure that  
 3340 intrinsic performance gains carry over to the applications that we care about.

### 3341 6.4.1 Held-out likelihood

The goal of probabilistic language models is to accurately measure the probability of sequences of word tokens. Therefore, an intrinsic evaluation metric is the likelihood that the language model assigns to **held-out data**, which is not used during training. Specifically, we compute,

$$\ell(\mathbf{w}) = \sum_{m=1}^M \log p(w_m | w_{m-1}, \dots, w_1), \quad [6.42]$$

3342 treating the entire held-out corpus as a single stream of tokens.

3343 Typically, unknown words are mapped to the  $\langle \text{UNK} \rangle$  token. This means that we have  
 3344 to estimate some probability for  $\langle \text{UNK} \rangle$  on the training data. One way to do this is to fix  
 3345 the vocabulary  $\mathcal{V}$  to the  $V - 1$  words with the highest counts in the training data, and then  
 3346 convert all other tokens to  $\langle \text{UNK} \rangle$ . Other strategies for dealing with out-of-vocabulary  
 3347 terms are discussed in § 6.5.

3348 **6.4.2 Perplexity**

Held-out likelihood is usually presented as **perplexity**, which is a deterministic transformation of the log-likelihood into an information-theoretic quantity,

$$\text{Perplex}(\mathbf{w}) = 2^{-\frac{\ell(\mathbf{w})}{M}}, \quad [6.43]$$

3349 where  $M$  is the total number of tokens in the held-out corpus.

3350 Lower perplexities correspond to higher likelihoods, so lower scores are better on this  
3351 metric — it is better to be less perplexed. Here are some special cases:

- 3352 • In the limit of a perfect language model, probability 1 is assigned to the held-out  
3353 corpus, with  $\text{Perplex}(\mathbf{w}) = 2^{-\frac{1}{M} \log_2 1} = 2^0 = 1$ .
- 3354 • In the opposite limit, probability zero is assigned to the held-out corpus, which cor-  
3355 responds to an infinite perplexity,  $\text{Perplex}(\mathbf{w}) = 2^{-\frac{1}{M} \log_2 0} = 2^\infty = \infty$ .
- 3356 • Assume a uniform, unigram model in which  $p(w_i) = \frac{1}{V}$  for all words in the vocab-  
3357 uary. Then,

$$\begin{aligned} \log_2(\mathbf{w}) &= \sum_{m=1}^M \log_2 \frac{1}{V} = - \sum_{m=1}^M \log_2 V = -M \log_2 V \\ \text{Perplex}(\mathbf{w}) &= 2^{\frac{1}{M} M \log_2 V} \\ &= 2^{\log_2 V} \\ &= V. \end{aligned}$$

3358 This is the “worst reasonable case” scenario, since you could build such a language  
3359 model without even looking at the data.

3360 In practice, language models tend to give perplexities in the range between 1 and  $V$ .  
3361 A small benchmark dataset is the **Penn Treebank**, which contains roughly a million to-  
3362 kens; its vocabulary is limited to 10,000 words, with all other tokens mapped a special  
3363  $\langle \text{UNK} \rangle$  symbol. On this dataset, a well-smoothed 5-gram model achieves a perplexity of  
3364 141 (Mikolov and Zweig, Mikolov and Zweig), and an LSTM language model achieves  
3365 perplexity of roughly 80 (Zaremba, Sutskever, and Vinyals, Zaremba et al.). Various en-  
3366 hancements to the LSTM architecture can bring the perplexity below 60 (Merity et al.,  
3367 2018). A larger-scale language modeling dataset is the 1B Word Benchmark (Chelba et al.,  
3368 2013), which contains text from Wikipedia. On this dataset, a perplexities of around 25  
can be obtained by averaging together multiple LSTM language models (Jozefowicz et al.,  
2016).

3369 **6.5 Out-of-vocabulary words**

3370 So far, we have assumed a **closed-vocabulary** setting — the vocabulary  $\mathcal{V}$  is assumed to be  
 3371 a finite set. In realistic application scenarios, this assumption may not hold. Consider, for  
 3372 example, the problem of translating newspaper articles. The following sentence appeared  
 3373 in a Reuters article on January 6, 2017:<sup>5</sup>

3374 The report said U.S. intelligence agencies believe Russian military intelligence,  
 3375 the **GRU**, used intermediaries such as **WikiLeaks**, **DCLeaks.com** and the **Guc-**  
 3376 **cifer** 2.0 "persona" to release emails...

3377 Suppose that you trained a language model on the Gigaword corpus,<sup>6</sup> which was released  
 3378 in 2003. The bolded terms either did not exist at this date, or were not widely known; they  
 3379 are unlikely to be in the vocabulary. The same problem can occur for a variety of other  
 3380 terms: new technologies, previously unknown individuals, new words (e.g., *hashtag*), and  
 3381 numbers.

3382 One solution is to simply mark all such terms with a special token,  $\langle \text{UNK} \rangle$ . While  
 3383 training the language model, we decide in advance on the vocabulary (often the  $K$  most  
 3384 common terms), and mark all other terms in the training data as  $\langle \text{UNK} \rangle$ . If we do not want  
 3385 to determine the vocabulary size in advance, an alternative approach is to simply mark  
 3386 the first occurrence of each word type as  $\langle \text{UNK} \rangle$ .

3387 But it is often better to make distinctions about the likelihood of various unknown words.  
 3388 This is particularly important in languages that have rich morphological systems, with  
 3389 many inflections for each word. For example, Portuguese is only moderately complex  
 3390 from a morphological perspective, yet each verb has dozens of inflected forms (see Fig-  
 3391 ure 4.3b). In such languages, there will be many word types that we do not encounter in a  
 3392 corpus, which are nonetheless predictable from the morphological rules of the language.  
 3393 To use a somewhat contrived English example, if *transfenestrate* is in the vocabulary, our  
 3394 language model should assign a non-zero probability to the past tense *transfenestrated*,  
 3395 even if it does not appear in the training data.

3396 One way to accomplish this is to supplement word-level language models with **character-**  
 3397 **level language models**. Such models can use  $n$ -grams or RNNs, but with a fixed vocab-  
 3398 uary equal to the set of ASCII or Unicode characters. For example Ling et al. (2015)  
 3399 propose an LSTM model over characters, and Kim (2014) employ a **convolutional neural**  
 3400 **network** (LeCun and Bengio, 1995). A more linguistically motivated approach is to seg-  
 3401 ment words into meaningful subword units, known as **morphemes** (see chapter 9). For

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<sup>5</sup>Bayoumy, Y. and Strobel, W. (2017, January 6). U.S. intel report: Putin directed cy-  
 ber campaign to help Trump. *Reuters*. Retrieved from <http://www.reuters.com/article/us-usa-russia-cyber-idUSKBN14Q1T8> on January 7, 2017.

<sup>6</sup><https://catalog.ldc.upenn.edu/LDC2003T05>

3402 example, Botha and Blunsom (2014) induce vector representations for morphemes, which  
 3403 they build into a log-bilinear language model; Bhatia et al. (2016) incorporate morpheme  
 3404 vectors into an LSTM.

## 3405 Additional resources

3406 A variety of neural network architectures have been applied to language modeling. No-  
 3407 table earlier non-recurrent architectures include the neural probabilistic language model (Ben-  
 3408 gio et al., 2003) and the log-bilinear language model (Mnih and Hinton, 2007). Much more  
 3409 detail on these models can be found in the text by Goodfellow et al. (2016).

## 3410 Exercises

- 3411 1. Prove that  $n$ -gram language models give valid probabilities if the  $n$ -gram probabili-  
 3412 ties are valid. Specifically, assume that,

$$\sum_{w_m}^V p(w_m | w_{m-1}, w_{m-2}, \dots, w_{m-n+1}) = 1 \quad [6.44]$$

3413 for all contexts  $(w_{m-1}, w_{m-2}, \dots, w_{m-n+1})$ . Prove that  $\sum_w p_n(w) = 1$  for all  $w \in \mathcal{V}^*$ ,  
 3414 where  $p_n$  is the probability under an  $n$ -gram language model. Your proof should  
 3415 proceed by induction. You should handle the start-of-string case  $p(w_1 | \underbrace{\square, \dots, \square}_{n-1})$ ,

3416 but you need not handle the end-of-string token.

- 3417 2. First, show that RNN language models are valid using a similar proof technique to  
 3418 the one in the previous problem.

3419 Next, let  $p_r(w)$  indicate the probability of  $w$  under RNN  $r$ . An ensemble of RNN  
 3420 language models computes the probability,

$$p(w) = \frac{1}{R} \sum_{r=1}^R p_r(w). \quad [6.45]$$

3421 Does an ensemble of RNN language models compute a valid probability?

- 3422 3. Consider a unigram language model over a vocabulary of size  $V$ . Suppose that a  
 3423 word appears  $m$  times in a corpus with  $M$  tokens in total. With Lidstone smoothing  
 3424 of  $\alpha$ , for what values of  $m$  is the smoothed probability greater than the unsmoothed  
 3425 probability?

- 3426 4. Consider a simple language in which each token is drawn from the vocabulary  $\mathcal{V}$   
 3427 with probability  $\frac{1}{V}$ , independent of all other tokens.

3428 Given a corpus of size  $M$ , what is the expectation of the fraction of all possible  
 3429 bigrams that have zero count? You may assume  $V$  is large enough that  $\frac{1}{V} \approx \frac{1}{V-1}$ .

- 3430 5. Continuing the previous problem, determine the value of  $M$  such that the fraction  
 3431 of bigrams with zero count is at most  $\epsilon \in (0, 1)$ . As a hint, you may use the approxi-  
 3432 mation  $\ln(1 + \alpha) \approx \alpha$  for  $\alpha \approx 0$ .

- 3433 6. In real languages, words probabilities are neither uniform nor independent.

- 3434 • Assume that word probabilities are independent but not uniform, so that in  
 3435 general  $p(w) \neq \frac{1}{V}$ . Prove that the expected fraction of unseen bigrams will be  
 3436 higher than in the IID case.
- 3437 • Assume that word probabilities are neither independent nor uniform. Again,  
 3438 prove that the expected fraction of unseen bigrams will be higher than in the  
 3439 IID case. [todo: double check]

- 3440 7. Consider a recurrent neural network with a single hidden unit and a sigmoid acti-  
 3441 vation,  $h_m = \sigma(\theta h_{m-1} + x_m)$ . Prove that if  $|\theta| < 1$ , then the gradient  $\frac{\partial h_m}{\partial h_{m-k}}$  goes to  
 3442 zero as  $k \rightarrow \infty$ .<sup>7</sup>

- 3443 8. **Zipf's law** states that if the word types in a corpus are sorted by frequency, then the  
 3444 frequency of the word at rank  $r$  is proportional to  $r^{-s}$ , where  $s$  is a free parameter,  
 3445 usually around 1. (Another way to view Zipf's law is that a plot of log frequency  
 3446 against log rank will be linear.) Solve for  $s$  using the counts of the first and second  
 3447 most frequent words,  $c_1$  and  $c_2$ .

- 3448 9. Download the wikitext-2 dataset.<sup>8</sup> Read and tokenize the training data, e.g. with the  
 3449 CountVectorizer class from scikit-learn. Estimate the Zipf's law coefficient  
 3450 by,

$$\hat{s} = \exp \left( \frac{(\log \mathbf{r}) \cdot (\log \mathbf{c})}{\|\log \mathbf{r}\|_2^2} \right), \quad [6.46]$$

3451 where  $\mathbf{r} = [1, 2, 3, \dots]$  is the vector of ranks of all words in the corpus, and  $\mathbf{c} =$   
 3452  $[c_1, c_2, c_3, \dots]$  is the vector of counts of all words in the corpus, sorted in descending  
 3453 order.

<sup>7</sup>This proof generalizes to vector hidden units by considering the largest eigenvector of the matrix  $\Theta$  (Pascanu et al., 2013).

<sup>8</sup>Currently available at [https://github.com/pytorch/examples/tree/master/word\\_language\\_model/data/wikitext-2](https://github.com/pytorch/examples/tree/master/word_language_model/data/wikitext-2)

- 3454 Make a log-log plot of the observed counts, and the expected counts according to  
3455 Zipf's law. The sum  $\sum_{r=1}^{\infty} r^s = \zeta(s)$  is the Riemann zeta function, available in  
3456 python's `scipy` library as `scipy.special.zeta`.
- 3457 10. Using the Pytorch library, train an LSTM language model from the Wikitext train-  
3458 ing corpus. After each epoch of training, compute its perplexity on the Wikitext  
3459 validation corpus. For this exercise, you can focus on the  $10^4$  most frequent words  
3460 in the training corpus, and label everything else as `<UNK>`. Stop training when the  
3461 perplexity stops improving.

## 3462 Chapter 7

# 3463 Sequence labeling

3464 The goal of sequence labeling is to assign tags to words, or more generally, to assign  
3465 discrete labels to discrete elements in a sequence. There are many applications of se-  
3466 quence labeling in natural language processing, and chapter 8 presents an overview. For  
3467 now, we'll focus on the classic problem of **part-of-speech tagging**, which requires tagging  
3468 each word by its grammatical category. Coarse-grained grammatical categories include  
3469 **NOUNs**, which describe things, properties, or ideas, and **VERBs**, which describe actions  
3470 and events. Consider a simple input:

3471 (7.1) They can fish.

3472 A dictionary of coarse-grained part-of-speech tags might include **NOUN** as the only valid  
3473 tag for *they*, but both **NOUN** and **VERB** as potential tags for *can* and *fish*. An accurate se-  
3474 quence labeling algorithm should select the verb tag for both *can* and *fish* in (7.1), but it  
3475 should select noun for the same two words in the phrase *can of fish*.

### 3476 7.1 Sequence labeling as classification

One way to solve a tagging problem is to turn it into a classification problem. Let  $f((\mathbf{w}, m), y)$  indicate the feature function for tag  $y$  at position  $m$  in the sequence  $\mathbf{w} = (w_1, w_2, \dots, w_M)$ . A simple tagging model would have a single base feature, the word itself:

$$f((\mathbf{w} = \text{they can fish}, m = 1), \text{N}) = (\text{they}, \text{N}) \quad [7.1]$$

$$f((\mathbf{w} = \text{they can fish}, m = 2), \text{V}) = (\text{can}, \text{V}) \quad [7.2]$$

$$f((\mathbf{w} = \text{they can fish}, m = 3), \text{V}) = (\text{fish}, \text{V}). \quad [7.3]$$

3477 Here the feature function takes three arguments as input: the sentence to be tagged (e.g.,  
3478 *they can fish*), the proposed tag (e.g., N or V), and the index of the token to which this tag

3479 is applied. This simple feature function then returns a single feature: a tuple including  
 3480 the word to be tagged and the tag that has been proposed. If the vocabulary size is  $V$   
 3481 and the number of tags is  $K$ , then there are  $V \times K$  features. Each of these features must  
 3482 be assigned a weight. These weights can be learned from a labeled dataset using a clas-  
 3483 sification algorithm such as perceptron, but this isn't necessary in this case: it would be  
 3484 equivalent to define the classification weights directly, with  $\theta_{w,y} = 1$  for the tag  $y$  most  
 3485 frequently associated with word  $w$ , and  $\theta_{w,y} = 0$  for all other tags.

However, it is easy to see that this simple classification approach cannot correctly tag both *they can fish* and *can of fish*, because *can* and *fish* are grammatically ambiguous. To handle both of these cases, the tagger must rely on context, such as the surrounding words. We can build context into the feature set by incorporating the surrounding words as additional features:

$$\begin{aligned} f((\mathbf{w} = \text{they can fish}, 1), \mathbf{N}) = & \{(w_m = \text{they}, y_m = \mathbf{N}), \\ & (w_{m-1} = \square, y_m = \mathbf{N}), \\ & (w_{m+1} = \text{can}, y_m = \mathbf{N})\} \end{aligned} \quad [7.4]$$

$$\begin{aligned} f((\mathbf{w} = \text{they can fish}, 2), \mathbf{V}) = & \{(w_m = \text{can}, y_m = \mathbf{V}), \\ & (w_{m-1} = \text{they}, y_m = \mathbf{V}), \\ & (w_{m+1} = \text{fish}, y_m = \mathbf{V})\} \end{aligned} \quad [7.5]$$

$$\begin{aligned} f((\mathbf{w} = \text{they can fish}, 3), \mathbf{V}) = & \{(w_m = \text{fish}, y_m = \mathbf{V}), \\ & (w_{m-1} = \text{can}, y_m = \mathbf{V}), \\ & (w_{m+1} = \blacksquare, y_m = \mathbf{V})\}. \end{aligned} \quad [7.6]$$

3486 These features contain enough information that a tagger should be able to choose the  
 3487 right tag for the word *fish*: words that come after *can* are likely to be verbs, so the feature  
 3488  $(w_{m-1} = \text{can}, y_m = \mathbf{V})$  should have a large positive weight.

3489 However, even with this enhanced feature set, it may be difficult to tag some se-  
 3490 quences correctly. One reason is that there are often relationships between the tags them-  
 3491 selves. For example, in English it is relatively rare for a verb to follow another verb —  
 3492 particularly if we differentiate MODAL verbs like *can* and *should* from more typical verbs,  
 3493 like *give*, *transcend*, and *befuddle*. We would like to incorporate preferences against tag se-  
 3494 quences like VERB-VERB, and in favor of tag sequences like NOUN-VERB. The need for  
 3495 such preferences is best illustrated by a **garden path sentence**:

3496 (7.2) The old man the boat.

3497 Grammatically, the word *the* is a DETERMINER. When you read the sentence, what  
 3498 part of speech did you first assign to *old*? Typically, this word is an ADJECTIVE — abbrevi-  
 3499 ated as J — which is a class of words that modify nouns. Similarly, *man* is usually a noun.  
 3500 The resulting sequence of tags is D J N D N. But this is a mistaken “garden path” inter-  
 3501 pretation, which ends up leading nowhere. It is unlikely that a determiner would directly

follow a noun,<sup>1</sup> and it is particularly unlikely that the entire sentence would lack a verb. The only possible verb in (7.2) is the word *man*, which can refer to the act of maintaining and piloting something — often boats. But if *man* is tagged as a verb, then *old* is seated between a determiner and a verb, and must be a noun. And indeed, adjectives often have a second interpretation as nouns when used in this way (e.g., *the young*, *the restless*). This reasoning, in which the labeling decisions are intertwined, cannot be applied in a setting where each tag is produced by an independent classification decision.

## 7.2 Sequence labeling as structure prediction

As an alternative, think of the entire sequence of tags as a label itself. For a given sequence of words  $\mathbf{w} = (w_1, w_2, \dots, w_M)$ , there is a set of possible taggings  $\mathcal{Y}(\mathbf{w}) = \mathcal{Y}^M$ , where  $\mathcal{Y} = \{\text{N, V, D, ...}\}$  refers to the set of individual tags, and  $\mathcal{Y}^M$  refers to the set of tag sequences of length  $M$ . We can then treat the sequence labeling problem as a classification problem in the label space  $\mathcal{Y}(\mathbf{w})$ ,

$$\hat{\mathbf{y}} = \underset{\mathbf{y} \in \mathcal{Y}(\mathbf{w})}{\operatorname{argmax}} \Psi(\mathbf{w}, \mathbf{y}), \quad [7.7]$$

where  $\mathbf{y} = (y_1, y_2, \dots, y_M)$  is a sequence of  $M$  tags, and  $\Psi$  is a scoring function on pairs of sequences,  $V^M \times \mathcal{Y}^M \rightarrow \mathbb{R}$ . Such a function can include features that capture the relationships between tagging decisions, such as the preference that determiners not follow nouns, or that all sentences have verbs.

Given that the label space is exponentially large in the length of the sequence  $M$ , can it ever be practical to perform tagging in this way? The problem of making a series of interconnected labeling decisions is known as **inference**. Because natural language is full of interrelated grammatical structures, inference is a crucial aspect of natural language processing. In English, it is not unusual to have sentences of length  $M = 20$ ; part-of-speech tag sets vary in size from 10 to several hundred. Taking the low end of this range, we have  $|\mathcal{Y}(\mathbf{w}_{1:M})| \approx 10^{20}$ , one hundred billion billion possible tag sequences. Enumerating and scoring each of these sequences would require an amount of work that is exponential in the sequence length, so inference is intractable.

However, the situation changes when we restrict the scoring function. Suppose we choose a function that decomposes into a sum of local parts,

$$\Psi(\mathbf{w}, \mathbf{y}) = \sum_{m=1}^{M+1} \psi(\mathbf{w}, y_m, y_{m-1}, m), \quad [7.8]$$

where each  $\psi(\cdot)$  scores a local part of the tag sequence. Note that the sum goes up to  $M+1$ , so that we can include a score for a special end-of-sequence tag,  $\psi(\mathbf{w}_{1:M}, \diamond, y_M, M+1)$ . We also define a special tag to begin the sequence,  $y_0 \triangleq \diamond$ .

<sup>1</sup>The main exception occurs with ditransitive verbs, such as *They gave the winner a trophy*.

3531 In a linear model, local scoring function can be defined as a dot product of weights  
 3532 and features,

$$\psi(\mathbf{w}_{1:M}, y_m, y_{m-1}, m) = \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{w}, y_m, y_{m-1}, m). \quad [7.9]$$

3533 The feature vector  $\mathbf{f}$  can consider the entire input  $\mathbf{w}$ , and can look at pairs of adjacent  
 3534 tags. This is a step up from per-token classification: the weights can assign low scores  
 3535 to infelicitous tag pairs, such as noun-determiner, and high scores for frequent tag pairs,  
 3536 such as determiner-noun and noun-verb.

In the example *they can fish*, a minimal feature function would include features for word-tag pairs (sometimes called **emission features**) and tag-tag pairs (sometimes called **transition features**):

$$\mathbf{f}(\mathbf{w} = \text{they can fish}, \mathbf{y} = \text{N V V}) = \sum_{m=1}^{M+1} \mathbf{f}(\mathbf{w}, y_m, y_{m-1}, m) \quad [7.10]$$

$$\begin{aligned} &= \mathbf{f}(\mathbf{w}, \text{N}, \diamond, 1) \\ &\quad + \mathbf{f}(\mathbf{w}, \text{V}, \text{N}, 2) \\ &\quad + \mathbf{f}(\mathbf{w}, \text{V}, \text{V}, 3) \\ &\quad + \mathbf{f}(\mathbf{w}, \blacklozenge, \text{V}, 4) \end{aligned} \quad [7.11]$$

$$\begin{aligned} &= (w_m = \text{they}, y_m = \text{N}) + (y_m = \text{N}, y_{m-1} = \diamond) \\ &\quad + (w_m = \text{can}, y_m = \text{V}) + (y_m = \text{V}, y_{m-1} = \text{N}) \\ &\quad + (w_m = \text{fish}, y_m = \text{V}) + (y_m = \text{V}, y_{m-1} = \text{V}) \\ &\quad + (y_m = \blacklozenge, y_{m-1} = \text{V}). \end{aligned} \quad [7.12]$$

3537 There are seven active features for this example: one for each word-tag pair, and one  
 3538 for each tag-tag pair, including a final tag  $y_{M+1} = \blacklozenge$ . These features capture the two main  
 3539 sources of information for part-of-speech tagging in English: which tags are appropriate  
 3540 for each word, and which tags tend to follow each other in sequence. Given appropriate  
 3541 weights for these features, taggers can achieve high accuracy, even for difficult cases like  
 3542 *the old man the boat*. We will now discuss how this restricted scoring function enables  
 3543 efficient inference, through the **Viterbi algorithm** (Viterbi, 1967).

3544 **7.3 The Viterbi algorithm**

By decomposing the scoring function into a sum of local parts, it is possible to rewrite the tagging problem as follows:

$$\hat{\mathbf{y}} = \operatorname{argmax}_{\mathbf{y} \in \mathcal{Y}(\mathbf{w})} \Psi(\mathbf{w}, \mathbf{y}) \quad [7.13]$$

$$= \operatorname{argmax}_{\mathbf{y}_{1:M}} \sum_{m=1}^{M+1} \psi(\mathbf{w}, y_m, y_{m-1}, m) \quad [7.14]$$

$$= \operatorname{argmax}_{\mathbf{y}_{1:M}} \sum_{m=1}^{M+1} s_m(y_m, y_{m-1}), \quad [7.15]$$

3545 where the final line simplifies the notation with the shorthand,

$$s_m(y_m, y_{m-1}) \triangleq \psi(\mathbf{w}_{1:M}, y_m, y_{m-1}, m). \quad [7.16]$$

This inference problem can be solved efficiently using **dynamic programming**, an algorithmic technique for reusing work in recurrent computations. We begin by solving an auxiliary problem: rather than finding the best tag sequence, we compute the *score* of the best tag sequence,

$$\max_{\mathbf{y}_{1:M}} \Psi(\mathbf{w}, \mathbf{y}_{1:M}) = \max_{\mathbf{y}_{1:M}} \sum_{m=1}^{M+1} s_m(y_m, y_{m-1}). \quad [7.17]$$

This score involves a maximization over all tag sequences of length  $M$ , written  $\max_{\mathbf{y}_{1:M}}$ . This maximization can be broken into two pieces,

$$\max_{\mathbf{y}_{1:M}} \Psi(\mathbf{w}, \mathbf{y}_{1:M}) = \max_{y_M} \max_{\mathbf{y}_{1:M-1}} \sum_{m=1}^{M+1} s_m(y_m, y_{m-1}), \quad [7.18]$$

which says that we maximize over the final tag  $y_M$ , and we maximize over all “prefixes”,  $\mathbf{y}_{1:M-1}$ . Within the sum of scores, only the final term  $s_{M+1}(\blacklozenge, y_M)$  depends on  $y_M$ , so we can pull this term out of the second maximization,

$$\max_{\mathbf{y}_{1:M}} \Psi(\mathbf{w}, \mathbf{y}_{1:M}) = \max_{y_M} s_{M+1}(\blacklozenge, y_M) + \max_{\mathbf{y}_{1:M-1}} \sum_{m=1}^M s_m(y_m, y_{m-1}). \quad [7.19]$$

This same reasoning can be applied recursively to the second term of Equation 7.19, pulling out  $s_M(y_M, y_{M-1})$ , and so on. We can formalize this idea by defining an auxiliary

---

**Algorithm 11** The Viterbi algorithm. Each  $s_m(k, k')$  is a local score for tag  $y_m = k$  and  $y_{m-1} = k'$ .

---

```

for  $k \in \{0, \dots, K\}$  do
     $v_1(k) = s_1(k, \diamond)$ 
for  $m \in \{2, \dots, M\}$  do
    for  $k \in \{0, \dots, K\}$  do
         $v_m(k) = \max_{k'} s_m(k, k') + v_{m-1}(k')$ 
         $b_m(k) = \operatorname{argmax}_{k'} s_m(k, k') + v_{m-1}(k')$ 
     $y_M = \operatorname{argmax}_k s_{M+1}(\blacklozenge, k) + v_M(k)$ 
    for  $m \in \{M-1, \dots, 1\}$  do
         $y_m = b_m(y_{m+1})$ 
return  $\mathbf{y}_{1:M}$ 
```

---

variable called the **Viterbi variable**,

$$v_m(y_m) \triangleq \max_{\mathbf{y}_{1:m-1}} \sum_{n=1}^m s_n(y_n, y_{n-1}) \quad [7.20]$$

$$= \max_{y_{m-1}} s_m(y_m, y_{m-1}) + \max_{\mathbf{y}_{1:m-2}} \sum_{n=1}^{m-1} s_n(y_n, y_{n-1}) \quad [7.21]$$

$$= \max_{y_{m-1}} s_m(y_m, y_{m-1}) + v_{m-1}(y_{m-1}). \quad [7.22]$$

3546 The variable  $v_m(k)$  represents the score of the best sequence of length  $m$  ending in tag  $k$ .

Each set of Viterbi variables is computed from the local score  $s_m(y_m, y_{m-1})$ , and from the previous set of Viterbi variables. The initial condition of the recurrence is simply the first score,

$$v_1(y_1) \triangleq s_1(y_1, \diamond). \quad [7.23]$$

The maximum overall score for the sequence is then the final Viterbi variable,

$$\max_{\mathbf{y}_{1:M}} \Psi(\mathbf{w}_{1:M}, \mathbf{y}_{1:M}) = v_{M+1}(\blacklozenge). \quad [7.24]$$

3547 Thus, the score of the best labeling for the sequence can be computed in a single forward  
 3548 sweep: first compute all variables  $v_1(\cdot)$  from Equation 7.23, and then compute all variables  
 3549  $v_2(\cdot)$  from the recurrence in Equation 7.22, continuing until the final variable  $v_{M+1}(\blacklozenge)$ .

3550 The Viterbi variables can be arranged in a structure known as a **trellis**, shown in Fig-  
 3551 ure 7.1. Each column indexes a token  $m$  in the sequence, and each row indexes a tag in  
 3552  $\mathcal{Y}$ ; every  $v_{m-1}(k)$  is connected to every  $v_m(k')$ , indicating that  $v_m(k')$  is computed from  
 3553  $v_{m-1}(k)$ . Special nodes are set aside for the start and end states.

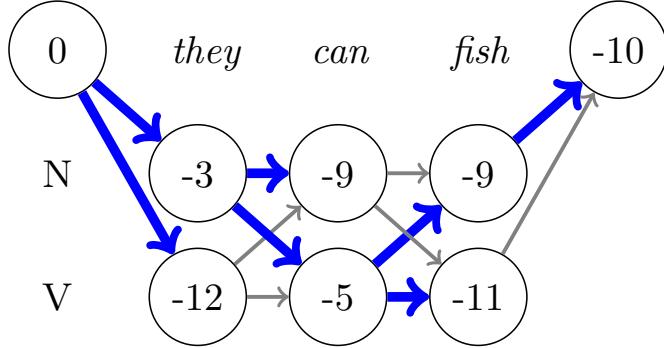


Figure 7.1: The trellis representation of the Viterbi variables, for the example *they can fish*, using the weights shown in Table 7.1.

3554 Our real goal is to find the best scoring sequence, not simply to compute its score.  
 3555 But solving the auxiliary problem gets us almost all the way there. Recall that each  $v_m(k)$   
 3556 represents the score of the best tag sequence ending in that tag  $k$  in position  $m$ . To compute  
 3557 this, we maximize over possible values of  $y_{m-1}$ . If we keep track of the “argmax” tag that  
 3558 maximizes this choice at each step, then we can walk backwards from the final tag, and  
 3559 recover the optimal tag sequence. This is indicated in Figure 7.1 by the solid blue lines,  
 3560 which we trace back from the final position. These backward pointers are written  $b_m(k)$ ,  
 3561 indicating the optimal tag  $y_{m-1}$  on the path to  $Y_m = k$ .

3562 The complete Viterbi algorithm is shown in Algorithm 11. When computing the initial  
 3563 Viterbi variables  $v_1(\cdot)$ , the special tag  $\diamond$  indicates the start of the sequence. When comput-  
 3564 ing the final tag  $Y_M$ , another special tag,  $\blacklozenge$  indicates the end of the sequence. These special  
 3565 tags enable the use of transition features for the tags that begin and end the sequence: for  
 3566 example, conjunctions are unlikely to end sentences in English, so we would like a low  
 3567 score for  $s_{M+1}(\blacklozenge, CC)$ ; nouns are relatively likely to appear at the beginning of sentences,  
 3568 so we would like a high score for  $s_1(N, \diamond)$ , assuming the noun tag is compatible with the  
 3569 first word token  $w_1$ .

3570 **Complexity** If there are  $K$  tags and  $M$  positions in the sequence, then there are  $M \times K$   
 3571 Viterbi variables to compute. Computing each variable requires finding a maximum over  
 3572  $K$  possible predecessor tags. The total time complexity of populating the trellis is there-  
 3573 fore  $\mathcal{O}(MK^2)$ , with an additional factor for the number of active features at each position.  
 3574 After completing the trellis, we simply trace the backwards pointers to the beginning of  
 3575 the sequence, which takes  $\mathcal{O}(M)$  operations.

	<i>they</i>	<i>can</i>	<i>fish</i>	
N	-2	-3	-3	
V	-10	-1	-3	

(a) Weights for emission features.

	N	V	♦
◊	-1	-2	$-\infty$
N	-3	-1	-1
V	-1	-3	-1

(b) Weights for transition features. The “from” tags are on the columns, and the “to” tags are on the rows.

Table 7.1: Feature weights for the example trellis shown in Figure 7.1. Emission weights from  $\diamond$  and ♦ are implicitly set to  $-\infty$ .3576 **7.3.1 Example**

3577 Consider the minimal tagset  $\{N, V\}$ , corresponding to nouns and verbs. Even in this  
 3578 tagset, there is considerable ambiguity: for example, the words *can* and *fish* can each take  
 3579 both tags. Of the  $2 \times 2 \times 2 = 8$  possible taggings for the sentence *they can fish*, four are  
 3580 possible given these possible tags, and two are grammatical.<sup>2</sup>

3581 The values in the trellis in Figure 7.1 are computed from the feature weights defined in  
 3582 Table 7.1. We begin with  $v_1(N)$ , which has only one possible predecessor, the start tag  $\diamond$ .  
 3583 This score is therefore equal to  $s_1(N, \diamond) = -2 - 1 = -3$ , which is the sum of the scores for  
 3584 the emission and transition features respectively; the backpointer is  $b_1(N) = \diamond$ . The score  
 3585 for  $v_1(V)$  is computed in the same way:  $s_1(V, \diamond) = -10 - 2 = -12$ , and again  $b_1(V) = \diamond$ .  
 3586 The backpointers are represented in the figure by thick lines.

Things get more interesting at  $m = 2$ . The score  $v_2(N)$  is computed by maximizing over the two possible predecessors,

$$v_2(N) = \max(v_1(N) + s_2(N, N), v_1(V) + s_2(N, V)) \quad [7.25]$$

$$= \max(-3 - 3 - 3, -12 - 3 - 1) = -9 \quad [7.26]$$

$$b_2(N) = N. \quad [7.27]$$

This continues until reaching  $v_4(\diamond)$ , which is computed as,

$$v_4(\diamond) = \max(v_3(N) + s_4(\diamond, N), v_3(V) + s_4(\diamond, V)) \quad [7.28]$$

$$= \max(-9 + 0 - 1, -11 + 0 - 1) \quad [7.29]$$

$$= -10, \quad [7.30]$$

3587 so  $b_4(\diamond) = N$ . As there is no emission  $w_4$ , the emission features have scores of zero.

---

<sup>2</sup>The tagging *they/N can/V fish/N* corresponds to the scenario of putting fish into cans, or perhaps of firing them.

3588 To compute the optimal tag sequence, we walk backwards from here, next checking  
 3589  $b_3(N) = V$ , and then  $b_2(V) = N$ , and finally  $b_1(N) = \diamond$ . This yields  $y = (N, V, N)$ , which  
 3590 corresponds to the linguistic interpretation of the fishes being put into cans.

3591 **7.3.2 Higher-order features**

3592 The Viterbi algorithm was made possible by a restriction of the scoring function to local  
 3593 parts that consider only pairs of adjacent tags. We can think of this as a bigram language  
 3594 model over tags. A natural question is how to generalize Viterbi to tag trigrams, which  
 3595 would involve the following decomposition:

$$\Psi(\mathbf{w}, \mathbf{y}) = \sum_{m=1}^{M+2} f(\mathbf{w}, y_m, y_{m-1}, y_{m-2}, m), \quad [7.31]$$

3596 where  $y_{-1} = \diamond$  and  $y_{M+2} = \blacklozenge$ .

3597 One solution is to create a new tagset  $\mathcal{Y}^{(2)}$  from the Cartesian product of the original  
 3598 tagset with itself,  $\mathcal{Y}^{(2)} = \mathcal{Y} \times \mathcal{Y}$ . The tags in this product space are ordered pairs, rep-  
 3599 resenting adjacent tags at the token level: for example, the tag  $(N, V)$  would represent a  
 3600 noun followed by a verb. Transitions between such tags must be consistent: we can have a  
 3601 transition from  $(N, V)$  to  $(V, N)$  (corresponding to the tag sequence  $N V N$ ), but not from  
 3602  $(N, V)$  to  $(N, N)$ , which would not correspond to any coherent tag sequence. This con-  
 3603 straint can be enforced in feature weights, with  $\theta_{((a,b),(c,d))} = -\infty$  if  $b \neq c$ . The remaining  
 3604 feature weights can encode preferences for and against various tag trigrams.

3605 In the Cartesian product tag space, there are  $K^2$  tags, suggesting that the time com-  
 3606 plexity will increase to  $\mathcal{O}(MK^4)$ . However, it is unnecessary to max over predecessor tag  
 3607 bigrams that are incompatible with the current tag bigram. By exploiting this constraint,  
 3608 it is possible to limit the time complexity to  $\mathcal{O}(MK^3)$ . The space complexity grows to  
 3609  $\mathcal{O}(MK^2)$ , since the trellis must store all possible predecessors of each tag. In general, the  
 3610 time and space complexity of higher-order Viterbi grows exponentially with the order of  
 3611 the tag  $n$ -grams that are considered in the feature decomposition.

3612 **7.4 Hidden Markov Models**

3613 The Viterbi sequence labeling algorithm is built on the scores  $s_m(y, y')$ . We will now  
 3614 discuss how these scores can be estimated probabilistically. Recall from § 2.1 that the  
 3615 probabilistic Naïve Bayes classifier selects the label  $y$  to maximize  $p(y | \mathbf{x}) \propto p(y, \mathbf{x})$ . In  
 3616 probabilistic sequence labeling, our goal is similar: select the tag sequence that maximizes  
 3617  $p(y | \mathbf{w}) \propto p(y, \mathbf{w})$ . The locality restriction in Equation 7.8 can be viewed as a conditional  
 3618 independence assumption on the random variables  $y$ .

**Algorithm 12** Generative process for the hidden Markov model

---

```

 $y_0 \leftarrow \diamond,$     $m \leftarrow 1$ 
repeat
     $y_m \sim \text{Categorical}(\lambda_{y_{m-1}})$             $\triangleright$  sample the current tag
     $w_m \sim \text{Categorical}(\phi_{y_m})$             $\triangleright$  sample the current word
until  $y_m = \blacklozenge$             $\triangleright$  terminate when the stop symbol is generated

```

---

3619    Naïve Bayes was introduced as a generative model — a probabilistic story that ex-  
 3620    plains the observed data as well as the hidden label. A similar story can be constructed  
 3621    for probabilistic sequence labeling: first, the tags are drawn from a prior distribution; next,  
 3622    the tokens are drawn from a conditional likelihood. However, for inference to be tractable,  
 3623    additional independence assumptions are required. First, the probability of each token  
 3624    depends only on its tag, and not on any other element in the sequence:

$$p(w | y) = \prod_{m=1}^M p(w_m | y_m). \quad [7.32]$$

3625    Second, each tag  $y_m$  depends only on its predecessor,

$$p(y) = \prod_{m=1}^M p(y_m | y_{m-1}), \quad [7.33]$$

3626    where  $y_0 = \diamond$  in all cases. Due to this **Markov assumption**, probabilistic sequence labeling  
 3627    models are known as **hidden Markov models** (HMMs).

3628    The generative process for the hidden Markov model is shown in Algorithm 12. Given  
 3629    the parameters  $\lambda$  and  $\phi$ , we can compute  $p(w, y)$  for any token sequence  $w$  and tag se-  
 3630    quence  $y$ . The HMM is often represented as a **graphical model** (Wainwright and Jordan,  
 3631    2008), as shown in Figure 7.2. This representation makes the independence assumptions  
 3632    explicit: if a variable  $v_1$  is probabilistically conditioned on another variable  $v_2$ , then there  
 3633    is an arrow  $v_2 \rightarrow v_1$  in the diagram. If there are no arrows between  $v_1$  and  $v_2$ , they  
 3634    are **conditionally independent**, given each variable's **Markov blanket**. In the hidden  
 3635    Markov model, the Markov blanket for each tag  $y_m$  includes the “parent”  $y_{m-1}$ , and the  
 3636    “children”  $y_{m+1}$  and  $w_m$ .<sup>3</sup>

3637    It is important to reflect on the implications of the HMM independence assumptions.  
 3638    A non-adjacent pair of tags  $y_m$  and  $y_n$  are conditionally independent; if  $m < n$  and we  
 3639    are given  $y_{n-1}$ , then  $y_m$  offers no additional information about  $y_n$ . However, if we are  
 3640    not given any information about the tags in a sequence, then all tags are probabilistically  
 3641    coupled.

---

<sup>3</sup>In general graphical models, a variable's Markov blanket includes its parents, children, and its children's other parents (Murphy, 2012).

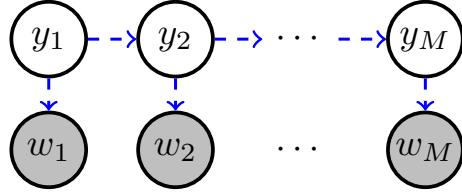


Figure 7.2: Graphical representation of the hidden Markov model. Arrows indicate probabilistic dependencies.

### 3642 7.4.1 Estimation

3643 The hidden Markov model has two groups of parameters:

3644 **Emission probabilities.** The probability  $p_e(w_m | y_m; \phi)$  is the emission probability, since  
3645 the words are treated as probabilistically “emitted”, conditioned on the tags.

3646 **Transition probabilities.** The probability  $p_t(y_m | y_{m-1}; \lambda)$  is the transition probability,  
3647 since it assigns probability to each possible tag-to-tag transition.

Both of these groups of parameters are typically computed from smoothed relative frequency estimation on a labeled corpus (see § 6.2 for a review of smoothing). The unsmoothed probabilities are,

$$\begin{aligned}\phi_{k,i} &\triangleq \Pr(W_m = i | Y_m = k) = \frac{\text{count}(W_m = i, Y_m = k)}{\text{count}(Y_m = k)} \\ \lambda_{k,k'} &\triangleq \Pr(Y_m = k' | Y_{m-1} = k) = \frac{\text{count}(Y_m = k', Y_{m-1} = k)}{\text{count}(Y_{m-1} = k)}.\end{aligned}$$

3648 Smoothing is more important for the emission probability than the transition probability,  
3649 because the vocabulary is much larger than the number of tags.

### 3650 7.4.2 Inference

3651 The goal of inference in the hidden Markov model is to find the highest probability tag  
3652 sequence,

$$\hat{y} = \underset{y}{\operatorname{argmax}} p(y | w). \quad [7.34]$$

3653 As in Naïve Bayes, it is equivalent to find the tag sequence with the highest *log*-probability,  
3654 since the logarithm is a monotonically increasing function. It is furthermore equivalent  
3655 to maximize the joint probability  $p(y, w) = p(y | w) \times p(w) \propto p(y | w)$ , which is pro-  
3656 portional to the conditional probability. Putting these observations together, the inference

3657 problem can be reformulated as,

$$\hat{\mathbf{y}} = \operatorname{argmax}_{\mathbf{y}} \log p(\mathbf{y}, \mathbf{w}). \quad [7.35]$$

We can now apply the HMM independence assumptions:

$$\log p(\mathbf{y}, \mathbf{w}) = \log p(\mathbf{y}) + \log p(\mathbf{w} \mid \mathbf{y}) \quad [7.36]$$

$$= \sum_{m=1}^{M+1} \log p_Y(y_m \mid y_{m-1}) + \log p_{W|Y}(w_m \mid y_m) \quad [7.37]$$

$$= \sum_{m=1}^{M+1} \log \lambda_{y_m, y_{m-1}} + \log \phi_{y_m, w_m} \quad [7.38]$$

$$= \sum_{m=1}^{M+1} s_m(y_m, y_{m-1}), \quad [7.39]$$

where,

$$s_m(y_m, y_{m-1}) \triangleq \log \lambda_{y_m, y_{m-1}} + \log \phi_{y_m, w_m}, \quad [7.40]$$

3658 and,

$$\phi_{\diamond, w} = \begin{cases} 1, & w = \blacksquare \\ 0, & \text{otherwise,} \end{cases} \quad [7.41]$$

3659 which ensures that the stop tag  $\diamond$  can only be applied to the final token  $\blacksquare$ .

This derivation shows that HMM inference can be viewed as an application of the Viterbi decoding algorithm, given an appropriately defined scoring function. The local score  $s_m(y_m, y_{m-1})$  can be interpreted probabilistically,

$$s_m(y_m, y_{m-1}) = \log p_y(y_m \mid y_{m-1}) + \log p_{w|y}(w_m \mid y_m) \quad [7.42]$$

$$= \log p(y_m, w_m \mid y_{m-1}). \quad [7.43]$$

Now recall the definition of the Viterbi variables,

$$v_m(y_m) = \max_{y_{m-1}} s_m(y_m, y_{m-1}) + v_{m-1}(y_{m-1}) \quad [7.44]$$

$$= \max_{y_{m-1}} \log p(y_m, w_m \mid y_{m-1}) + v_{m-1}(y_{m-1}). \quad [7.45]$$

By setting  $v_{m-1}(y_{m-1}) = \max_{\mathbf{y}_{1:m-2}} \log p(\mathbf{y}_{1:m-1}, \mathbf{w}_{1:m-1})$ , we obtain the recurrence,

$$v_m(y_m) = \max_{y_{m-1}} \log p(y_m, w_m \mid y_{m-1}) + \max_{\mathbf{y}_{1:m-2}} \log p(\mathbf{y}_{1:m-1}, \mathbf{w}_{1:m-1}) \quad [7.46]$$

$$= \max_{\mathbf{y}_{1:m-1}} \log p(y_m, w_m \mid y_{m-1}) + \log p(\mathbf{y}_{1:m-1}, \mathbf{w}_{1:m-1}) \quad [7.47]$$

$$= \max_{\mathbf{y}_{1:m-1}} \log p(\mathbf{y}_{1:m}, \mathbf{w}_{1:m}). \quad [7.48]$$

In words, the Viterbi variable  $v_m(y_m)$  is the log probability of the best tag sequence ending in  $y_m$ , joint with the word sequence  $w_{1:m}$ . The log probability of the best complete tag sequence is therefore,

$$\max_{\mathbf{y}_{1:M}} \log p(\mathbf{y}_{1:M+1}, \mathbf{w}_{1:M+1}) = v_{M+1}(\spadesuit) \quad [7.49]$$

**\*Viterbi as an example of the max-product algorithm** The Viterbi algorithm can also be implemented using probabilities, rather than log-probabilities. In this case, each  $v_m(y_m)$  is equal to,

$$v_m(y_m) = \max_{\mathbf{y}_{1:m-1}} p(\mathbf{y}_{1:m-1}, y_m, \mathbf{w}_{1:m}) \quad [7.50]$$

$$= \max_{y_{m-1}} p(y_m, w_m | y_{m-1}) \times \max_{\mathbf{y}_{1:m-2}} p(\mathbf{y}_{1:m-2}, y_{m-1}, \mathbf{w}_{1:m-1}) \quad [7.51]$$

$$= \max_{y_{m-1}} p(y_m, w_m | y_{m-1}) \times v_{m-1}(y_{m-1}) \quad [7.52]$$

$$= p_{w|y}(w_m | y_m) \times \max_{y_{m-1}} p_y(y_m | y_{m-1}) \times v_{m-1}(y_{m-1}). \quad [7.53]$$

3660 Each Viterbi variable is computed by *maximizing* over a set of *products*. Thus, the Viterbi  
 3661 algorithm is a special case of the **max-product algorithm** for inference in graphical mod-  
 3662 els (Wainwright and Jordan, 2008). However, the product of probabilities tends towards  
 3663 zero over long sequences, so the log-probability version of Viterbi is recommended in  
 3664 practical implementations.

## 3665 7.5 Discriminative sequence labeling with features

3666 Today, hidden Markov models are rarely used for supervised sequence labeling. This is  
 3667 because HMMs are limited to only two phenomena:

- 3668 • word-tag compatibility, via the emission probability  $p_{W|Y}(w_m | y_m)$ ;
- 3669 • local context, via the transition probability  $p_Y(y_m | y_{m-1})$ .

3670 The Viterbi algorithm permits the inclusion of richer information in the local scoring func-  
 3671 tion  $\psi(\mathbf{w}_{1:M}, y_m, y_{m-1}, m)$ , which can be defined as a weighted sum of arbitrary local *fea-*  
 3672 *tures*,

$$\psi(\mathbf{w}, y_m, y_{m-1}, m) = \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{w}, y_m, y_{m-1}, m), \quad [7.54]$$

3673 where  $\mathbf{f}$  is a locally-defined feature function, and  $\boldsymbol{\theta}$  is a vector of weights.

The local decomposition of the scoring function  $\Psi$  is reflected in a corresponding decomposition of the feature function:

$$\Psi(\mathbf{w}, \mathbf{y}) = \sum_{m=1}^{M+1} \psi(\mathbf{w}, y_m, y_{m-1}, m) \quad [7.55]$$

$$= \theta \cdot \mathbf{f}(\mathbf{w}, y_m, y_{m-1}, m) \quad [7.56]$$

$$= \theta \cdot \sum_{m=1}^{M+1} \mathbf{f}(\mathbf{w}, y_m, y_{m-1}, m) \quad [7.57]$$

$$= \theta \cdot \mathbf{f}^{(\text{global})}(\mathbf{w}, \mathbf{y}_{1:M}), \quad [7.58]$$

3674 where  $\mathbf{f}^{(\text{global})}(\mathbf{w}, \mathbf{y})$  is a global feature vector, which is a sum of local feature vectors,

$$\mathbf{f}^{(\text{global})}(\mathbf{w}, \mathbf{y}) = \sum_{m=1}^{M+1} \mathbf{f}(\mathbf{w}_{1:M}, y_m, y_{m-1}, m), \quad [7.59]$$

3675 with  $y_{M+1} = \diamond$  and  $y_0 = \diamond$  by construction.

3676 Let's now consider what additional information these features might encode.

3677 **Word affix features.** Consider the problem of part-of-speech tagging on the first four  
3678 lines of the poem *Jabberwocky* (Carroll, 1917):

3679 (7.3) 'Twas brillig, and the slithy toves  
3680       Did gyre and gimble in the wabe:  
3681       All mimsy were the borogoves,  
3682       And the mome raths outgrabe.

3683 Many of these words were made up by the author of the poem, so a corpus would offer  
3684 no information about their probabilities of being associated with any particular part of  
3685 speech. Yet it is not so hard to see what their grammatical roles might be in this passage.  
3686 Context helps: for example, the word *slithy* follows the determiner *the*, so it is probably a  
3687 noun or adjective. Which do you think is more likely? The suffix *-thy* is found in a number  
3688 of adjectives, like *frothy*, *healthy*, *pithy*, *worthy*. It is also found in a handful of nouns — e.g.,  
3689 *apathy*, *sympathy* — but nearly all of these have the longer coda *-pathy*, unlike *slithy*. So the  
3690 suffix gives some evidence that *slithy* is an adjective, and indeed it is: later in the text we  
3691 find that it is a combination of the adjectives *lithe* and *slimy*.<sup>4</sup>

---

<sup>4</sup>Morphology is the study of how words are formed from smaller linguistic units. chapter 9 touches on computational approaches to morphological analysis. See Bender (2013) for an overview of the underlying linguistic principles, and Haspelmath and Sims (2013) or Lieber (2015) for a full treatment.

3692 **Fine-grained context.** The hidden Markov model captures contextual information in the  
 3693 form of part-of-speech tag bigrams. But sometimes, the necessary contextual information  
 3694 is more specific. Consider the noun phrases *this fish* and *these fish*. Many part-of-speech  
 3695 tagsets distinguish between singular and plural nouns, but do not distinguish between  
 3696 singular and plural determiners; for example, the well known **Penn Treebank** tagset fol-  
 3697 lows these conventions. A hidden Markov model would be unable to correctly label *fish* as  
 3698 singular or plural in both of these cases, because it only has access to two features: the pre-  
 3699 ceding tag (determiner in both cases) and the word (*fish* in both cases). The classification-  
 3700 based tagger discussed in § 7.1 had the ability to use preceding and succeeding words as  
 3701 features, and it can also be incorporated into a Viterbi-based sequence labeler as a local  
 3702 feature.

**Example.** Consider the tagging D J N (determiner, adjective, noun) for the sequence *the slithy toves*, so that

$$\begin{aligned} \mathbf{w} &= \text{the slithy toves} \\ \mathbf{y} &= \text{D J N}. \end{aligned}$$

Let's create the feature vector for this example, assuming that we have word-tag features (indicated by  $W$ ), tag-tag features (indicated by  $T$ ), and suffix features (indicated by  $M$ ). You can assume that you have access to a method for extracting the suffix *-thy* from *slithy*, *-es* from *toves*, and  $\emptyset$  from *the*, indicating that this word has no suffix.<sup>5</sup> The resulting feature vector is,

$$\begin{aligned} \mathbf{f}(\text{the slithy toves, D J N}) &= \mathbf{f}(\text{the slithy toves, D}, \diamond, 1) \\ &\quad + \mathbf{f}(\text{the slithy toves, J}, \text{D}, 2) \\ &\quad + \mathbf{f}(\text{the slithy toves, N}, \text{J}, 3) \\ &\quad + \mathbf{f}(\text{the slithy toves}, \blacklozenge, \text{N}, 4) \\ &= \{(T : \diamond, \text{D}), (W : \text{the}, \text{D}), (M : \emptyset, \text{D}), \\ &\quad (T : \text{D}, \text{J}), (W : \text{slithy}, \text{J}), (M : \text{-thy}, \text{J}), \\ &\quad (T : \text{J}, \text{N}), (W : \text{toves}, \text{N}), (M : \text{-es}, \text{N}) \\ &\quad (T : \text{N}, \blacklozenge)\}. \end{aligned}$$

3703 These examples show that local features can incorporate information that lies beyond  
 3704 the scope of a hidden Markov model. Because the features are local, it is possible to apply  
 3705 the Viterbi algorithm to identify the optimal sequence of tags. The remaining question

---

<sup>5</sup>Such a system is called a **morphological segmenter**. The task of morphological segmentation is briefly described in § 9.1.4.4; a well known segmenter is **Morfessor** (Creutz and Lagus, 2007). In real applications, a typical approach is to include features for all orthographic suffixes up to some maximum number of characters: for *slithy*, we would have suffix features for *-y*, *-hy*, and *-thy*.

3706 is how to estimate the weights on these features. § 2.2 presented three main types of  
 3707 discriminative classifiers: perceptron, support vector machine, and logistic regression.  
 3708 Each of these classifiers has a structured equivalent, enabling it to be trained from labeled  
 3709 sequences rather than individual tokens.

### 3710 7.5.1 Structured perceptron

The perceptron classifier is trained by increasing the weights for features that are associated with the correct label, and decreasing the weights for features that are associated with incorrectly predicted labels:

$$\hat{y} = \operatorname{argmax}_{y \in \mathcal{Y}} \theta \cdot f(\mathbf{x}, y) \quad [7.60]$$

$$\theta^{(t+1)} \leftarrow \theta^{(t)} + f(\mathbf{x}, y) - f(\mathbf{x}, \hat{y}). \quad [7.61]$$

We can apply exactly the same update in the case of structure prediction,

$$\hat{\mathbf{y}} = \operatorname{argmax}_{\mathbf{y} \in \mathcal{Y}(\mathbf{w})} \theta \cdot f(\mathbf{w}, \mathbf{y}) \quad [7.62]$$

$$\theta^{(t+1)} \leftarrow \theta^{(t)} + f(\mathbf{w}, \mathbf{y}) - f(\mathbf{w}, \hat{\mathbf{y}}). \quad [7.63]$$

3711 This learning algorithm is called **structured perceptron**, because it learns to predict the  
 3712 structured output  $\mathbf{y}$ . The only difference is that instead of computing  $\hat{y}$  by enumerating  
 3713 the entire set  $\mathcal{Y}$ , the Viterbi algorithm is used to efficiently search the set of possible tag-  
 3714 gings,  $\mathcal{Y}^M$ . Structured perceptron can be applied to other structured outputs as long as  
 3715 efficient inference is possible. As in perceptron classification, weight averaging is crucial  
 3716 to get good performance (see § 2.2.2).

**Example** For the example *they can fish*, suppose that the reference tag sequence is  $\mathbf{y}^{(i)} =$   
 N V V, but the tagger incorrectly returns the tag sequence  $\hat{\mathbf{y}} = \text{N V N}$ . Assuming a model  
 with features for emissions  $(w_m, y_m)$  and transitions  $(y_{m-1}, y_m)$ , the corresponding structured  
 perceptron update is:

$$\theta_{(fish,V)} \leftarrow \theta_{(fish,V)} + 1, \quad \theta_{(fish,N)} \leftarrow \theta_{(fish,N)} - 1 \quad [7.64]$$

$$\theta_{(V,V)} \leftarrow \theta_{(V,V)} + 1, \quad \theta_{(V,N)} \leftarrow \theta_{(V,N)} - 1 \quad [7.65]$$

$$\theta_{(V,\blacklozenge)} \leftarrow \theta_{(V,\blacklozenge)} + 1, \quad \theta_{(N,\blacklozenge)} \leftarrow \theta_{(N,\blacklozenge)} - 1. \quad [7.66]$$

### 3717 7.5.2 Structured support vector machines

3718 Large-margin classifiers such as the support vector machine improve on the perceptron by  
 3719 pushing the classification boundary away from the training instances. The same idea can

3720 be applied to sequence labeling. A support vector machine in which the output is a struc-  
 3721 tured object, such as a sequence, is called a **structured support vector machine** (Tsochan-  
 3722 taridis et al., 2004).<sup>6</sup>

3723 In classification, we formalized the large-margin constraint as,

$$\forall \mathbf{y} \neq \mathbf{y}^{(i)}, \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}, \mathbf{y}^{(i)}) - \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}, \mathbf{y}) \geq 1, \quad [7.67]$$

3724 requiring a margin of at least 1 between the scores for all labels  $\mathbf{y}$  that are not equal to the  
 3725 correct label  $\mathbf{y}^{(i)}$ . The weights  $\boldsymbol{\theta}$  are then learned by constrained optimization (see § 2.3.2).

3726 This idea can be applied to sequence labeling by formulating an equivalent set of con-  
 3727 straints for all possible labelings  $\mathcal{Y}(\mathbf{w})$  for an input  $\mathbf{w}$ . However, there are two problems.  
 3728 First, in sequence labeling, some predictions are more wrong than others: we may miss  
 3729 only one tag out of fifty, or we may get all fifty wrong. We would like our learning algo-  
 3730 rithm to be sensitive to this difference. Second, the number of constraints is equal to the  
 3731 number of possible labelings, which is exponentially large in the length of the sequence.

3732 The first problem can be addressed by adjusting the constraint to require larger mar-  
 3733 gins for more serious errors. Let  $c(\mathbf{y}^{(i)}, \hat{\mathbf{y}}) \geq 0$  represent the *cost* of predicting label  $\hat{\mathbf{y}}$  when  
 3734 the true label is  $\mathbf{y}^{(i)}$ . We can then generalize the margin constraint,

$$\forall \mathbf{y}, \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{w}^{(i)}, \mathbf{y}^{(i)}) - \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{w}^{(i)}, \mathbf{y}) \geq c(\mathbf{y}^{(i)}, \mathbf{y}). \quad [7.68]$$

3735 This cost-augmented margin constraint specializes to the constraint in Equation 7.67 if we  
 3736 choose the delta function  $c(\mathbf{y}^{(i)}, \mathbf{y}) = \delta((\mathbf{y}^{(i)} \neq \mathbf{y}))$ . A more expressive cost function is  
 3737 the **Hamming cost**,

$$c(\mathbf{y}^{(i)}, \mathbf{y}) = \sum_{m=1}^M \delta(y_m^{(i)} \neq y_m), \quad [7.69]$$

3738 which computes the number of errors in  $\mathbf{y}$ . By incorporating the cost function as the  
 3739 margin constraint, we require that the true labeling be separated from the alternatives by  
 3740 a margin that is proportional to the number of incorrect tags in each alternative labeling.

The second problem is that the number of constraints is exponential in the length  
 of the sequence. This can be addressed by focusing on the prediction  $\hat{\mathbf{y}}$  that *maximally*  
 violates the margin constraint. This prediction can be identified by solving the following  
**cost-augmented decoding** problem:

$$\hat{\mathbf{y}} = \operatorname{argmax}_{\mathbf{y} \neq \mathbf{y}^{(i)}} \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{w}^{(i)}, \mathbf{y}) - \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{w}^{(i)}, \mathbf{y}^{(i)}) + c(\mathbf{y}^{(i)}, \mathbf{y}) \quad [7.70]$$

$$= \operatorname{argmax}_{\mathbf{y} \neq \mathbf{y}^{(i)}} \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{w}^{(i)}, \mathbf{y}) + c(\mathbf{y}^{(i)}, \mathbf{y}), \quad [7.71]$$

---

<sup>6</sup>This model is also known as a **max-margin Markov network** (Taskar et al., 2003), emphasizing that the scoring function is constructed from a sum of components, which are Markov independent.

3741 where in the second line we drop the term  $\theta \cdot f(\mathbf{w}^{(i)}, \mathbf{y}^{(i)})$ , which is constant in  $\mathbf{y}$ .

We can now reformulate the margin constraint for sequence labeling,

$$\theta \cdot f(\mathbf{w}^{(i)}, \mathbf{y}^{(i)}) - \max_{\mathbf{y} \in \mathcal{Y}(\mathbf{w})} (\theta \cdot f(\mathbf{w}^{(i)}, \mathbf{y}) + c(\mathbf{y}^{(i)}, \mathbf{y})) \geq 0. \quad [7.72]$$

3742 If the score for  $\theta \cdot f(\mathbf{w}^{(i)}, \mathbf{y}^{(i)})$  is greater than the cost-augmented score for all alternatives,  
 3743 then the constraint will be met. The name “cost-augmented decoding” is due to the fact  
 3744 that the objective includes the standard decoding problem,  $\max_{\hat{\mathbf{y}} \in \mathcal{Y}(\mathbf{w})} \theta \cdot f(\mathbf{w}, \hat{\mathbf{y}})$ , plus  
 3745 an additional term for the cost. Essentially, we want to train against predictions that are  
 3746 strong and wrong: they should score highly according to the model, yet incur a large loss  
 3747 with respect to the ground truth. Training adjusts the weights to reduce the score of these  
 3748 predictions.

3749 For cost-augmented decoding to be tractable, the cost function must decompose into  
 3750 local parts, just as the feature function  $f(\cdot)$  does. The Hamming cost, defined above,  
 3751 obeys this property. To perform cost-augmented decoding using the Hamming cost, we  
 3752 need only to add features  $f_m(y_m) = \delta(y_m \neq y_m^{(i)})$ , and assign a constant weight of 1 to  
 3753 these features. Decoding can then be performed using the Viterbi algorithm.<sup>7</sup>

As with large-margin classifiers, it is possible to formulate the learning problem in an unconstrained form, by combining a regularization term on the weights and a Lagrangian for the constraints:

$$\min_{\theta} \frac{1}{2} \|\theta\|_2^2 - C \left( \sum_i \theta \cdot f(\mathbf{w}^{(i)}, \mathbf{y}^{(i)}) - \max_{\mathbf{y} \in \mathcal{Y}(\mathbf{w}^{(i)})} [\theta \cdot f(\mathbf{w}^{(i)}, \mathbf{y}) + c(\mathbf{y}^{(i)}, \mathbf{y})] \right), \quad [7.73]$$

3754 In this formulation,  $C$  is a parameter that controls the tradeoff between the regularization  
 3755 term and the margin constraints. A number of optimization algorithms have been  
 3756 proposed for structured support vector machines, some of which are discussed in § 2.3.2.  
 3757 An empirical comparison by Kummerfeld et al. (2015) shows that stochastic subgradient  
 3758 descent — which is essentially a cost-augmented version of the structured perceptron —  
 3759 is highly competitive.

### 3760 7.5.3 Conditional random fields

3761 The **conditional random field** (CRF; Lafferty et al., 2001) is a conditional probabilistic  
 3762 model for sequence labeling; just as structured perceptron is built on the perceptron clas-  
 3763 sifier, conditional random fields are built on the logistic regression classifier.<sup>8</sup> The basic

---

<sup>7</sup>Are there cost functions that do not decompose into local parts? Suppose we want to assign a constant loss  $c$  to any prediction  $\hat{\mathbf{y}}$  in which  $k$  or more predicted tags are incorrect, and zero loss otherwise. This loss function is combinatorial over the predictions, and thus we cannot decompose it into parts.

<sup>8</sup>The name “conditional random field” is derived from **Markov random fields**, a general class of models in which the probability of a configuration of variables is proportional to a product of scores across pairs (or

3764 probability model is,

$$p(\mathbf{y} \mid \mathbf{w}) = \frac{\exp(\Psi(\mathbf{w}, \mathbf{y}))}{\sum_{\mathbf{y}' \in \mathcal{Y}(\mathbf{w})} \exp(\Psi(\mathbf{w}, \mathbf{y}'))}. \quad [7.74]$$

3765 This is almost identical to logistic regression, but because the label space is now tag  
 3766 sequences, we require efficient algorithms for both **decoding** (searching for the best tag  
 3767 sequence given a sequence of words  $\mathbf{w}$  and a model  $\theta$ ) and for **normalizing** (summing  
 3768 over all tag sequences). These algorithms will be based on the usual locality assumption  
 3769 on the scoring function,  $\Psi(\mathbf{w}, \mathbf{y}) = \sum_{m=1}^{M+1} \psi(\mathbf{w}, y_m, y_{m-1}, m)$ .

3770 **7.5.3.1 Decoding in CRFs**

Decoding — finding the tag sequence  $\hat{\mathbf{y}}$  that maximizes  $p(\mathbf{y} \mid \mathbf{w})$  — is a direct application of the Viterbi algorithm. The key observation is that the decoding problem does not depend on the denominator of  $p(\mathbf{y} \mid \mathbf{w})$ ,

$$\begin{aligned} \hat{\mathbf{y}} &= \operatorname{argmax}_{\mathbf{y}} \log p(\mathbf{y} \mid \mathbf{w}) \\ &= \operatorname{argmax}_{\mathbf{y}} \Psi(\mathbf{y}, \mathbf{w}) - \log \sum_{\mathbf{y}' \in \mathcal{Y}(\mathbf{w})} \exp \Psi(\mathbf{y}', \mathbf{w}) \\ &= \operatorname{argmax}_{\mathbf{y}} \Psi(\mathbf{y}, \mathbf{w}) = \operatorname{argmax}_{\mathbf{y}} \sum_{m=1}^{M+1} s_m(y_m, y_{m-1}). \end{aligned}$$

3771 This is identical to the decoding problem for structured perceptron, so the same Viterbi  
 3772 recurrence as defined in Equation 7.22 can be used.

3773 **7.5.3.2 Learning in CRFs**

As with logistic regression, the weights  $\theta$  are learned by minimizing the regularized negative log-probability,

$$\ell = \frac{\lambda}{2} \|\theta\|^2 - \sum_{i=1}^N \log p(\mathbf{y}^{(i)} \mid \mathbf{w}^{(i)}; \theta) \quad [7.75]$$

$$= \frac{\lambda}{2} \|\theta\|^2 - \sum_{i=1}^N \theta \cdot f(\mathbf{w}^{(i)}, \mathbf{y}^{(i)}) + \log \sum_{\mathbf{y}' \in \mathcal{Y}(\mathbf{w}^{(i)})} \exp (\theta \cdot f(\mathbf{w}^{(i)}, \mathbf{y}')), \quad [7.76]$$

---

more generally, cliques) of variables in a **factor graph**. In sequence labeling, the pairs of variables include all adjacent tags ( $y_m, y_{m-1}$ ). The probability is *conditioned* on the words  $\mathbf{w}$ , which are always observed, motivating the term “conditional” in the name.

3774 where  $\lambda$  controls the amount of regularization. The final term in Equation 7.76 is a sum  
 3775 over all possible labelings. This term is the log of the denominator in Equation 7.74, some-  
 3776 times known as the **partition function**.<sup>9</sup> There are  $|\mathcal{Y}|^M$  possible labelings of an input of  
 3777 size  $M$ , so we must again exploit the decomposition of the scoring function to compute  
 3778 this sum efficiently.

The sum  $\sum_{\mathbf{y} \in \mathcal{Y}^{w(i)}} \exp \Psi(\mathbf{y}, \mathbf{w})$  can be computed efficiently using the **forward recurrence**, which is closely related to the Viterbi recurrence. We first define a set of **forward variables**,  $\alpha_m(y_m)$ , which is equal to the sum of the scores of all paths leading to tag  $y_m$  at position  $m$ :

$$\alpha_m(y_m) \triangleq \sum_{\mathbf{y}_{1:m-1}} \exp \sum_{n=1}^m s_n(y_n, y_{n-1}) \quad [7.77]$$

$$= \sum_{\mathbf{y}_{1:m-1}} \prod_{n=1}^m \exp s_n(y_n, y_{n-1}). \quad [7.78]$$

Note the similarity to the definition of the Viterbi variable,  $v_m(y_m) = \max_{\mathbf{y}_{1:m-1}} \sum_{n=1}^m s_n(y_n, y_{n-1})$ . In the hidden Markov model, the Viterbi recurrence had an alternative interpretation as the max-product algorithm (see Equation 7.53); analogously, the forward recurrence is known as the **sum-product algorithm**, because of the form of [7.78]. The forward variable can also be computed through a recurrence:

$$\alpha_m(y_m) = \sum_{\mathbf{y}_{1:m-1}} \prod_{n=1}^m \exp s_n(y_n, y_{n-1}) \quad [7.79]$$

$$= \sum_{y_{m-1}} (\exp s_m(y_m, y_{m-1})) \sum_{\mathbf{y}_{1:m-2}} \prod_{n=1}^{m-1} \exp s_n(y_n, y_{n-1}) \quad [7.80]$$

$$= \sum_{y_{m-1}} (\exp s_m(y_m, y_{m-1})) \times \alpha_{m-1}(y_{m-1}). \quad [7.81]$$

Using the forward recurrence, it is possible to compute the denominator of the conditional probability,

$$\sum_{\mathbf{y} \in \mathcal{Y}(\mathbf{w})} \Psi(\mathbf{w}, \mathbf{y}) = \sum_{\mathbf{y}_{1:M}} s_{M+1}(\blacklozenge, y_M) \prod_{m=1}^M s_m(y_m, y_{m-1}) \quad [7.82]$$

$$= \alpha_{M+1}(\blacklozenge). \quad [7.83]$$

---

<sup>9</sup>The terminology of “potentials” and “partition functions” comes from statistical mechanics (Bishop, 2006).

The conditional log-likelihood can be rewritten,

$$\ell = \frac{\lambda}{2} \|\boldsymbol{\theta}\|^2 - \sum_{i=1}^N \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{w}^{(i)}, \mathbf{y}^{(i)}) + \log \alpha_{M+1}(\blacklozenge). \quad [7.84]$$

- 3779 Probabilistic programming environments, such as `Torch` (Collobert et al., 2011) and `dynet` (Neu-  
 3780 big et al., 2017), can compute the gradient of this objective using automatic differentiation.  
 3781 The programmer need only implement the forward algorithm as a computation graph.

As in logistic regression, the gradient of the likelihood with respect to the parameters is a difference between observed and expected feature counts:

$$\frac{d\ell}{d\theta_j} = \lambda \theta_j + \sum_{i=1}^N E[f_j(\mathbf{w}^{(i)}, \mathbf{y})] - f_j(\mathbf{w}^{(i)}, \mathbf{y}^{(i)}), \quad [7.85]$$

- 3782 where  $f_j(\mathbf{w}^{(i)}, \mathbf{y}^{(i)})$  refers to the count of feature  $j$  for token sequence  $\mathbf{w}^{(i)}$  and tag se-  
 3783 quence  $\mathbf{y}^{(i)}$ . The expected feature counts are computed “under the hood” when automatic  
 3784 differentiation is applied to Equation 7.84 (Eisner, 2016).

3785 Before the widespread use of automatic differentiation, it was common to compute  
 3786 the feature expectations from marginal tag probabilities  $p(y_m | \mathbf{w})$ . These marginal prob-  
 3787 abilities are sometimes useful on their own, and can be computed using the **forward-**  
 3788 **backward algorithm**. This algorithm combines the forward recurrence with an equivalent  
 3789 **backward recurrence**, which traverses the input from  $w_M$  back to  $w_1$ .

### 3790 7.5.3.3 \*Forward-backward algorithm

Marginal probabilities over tag bigrams can be written as,<sup>10</sup>

$$\Pr(Y_{m-1} = k', Y_m = k | \mathbf{w}) = \frac{\sum_{\mathbf{y}: Y_m=k, Y_{m-1}=k'} \prod_{n=1}^M \exp s_n(y_n, y_{n-1})}{\sum_{\mathbf{y}'} \prod_{n=1}^M \exp s_n(y'_n, y'_{n-1})}. \quad [7.86]$$

The numerator sums over all tag sequences that include the transition  $(Y_{m-1} = k') \rightarrow (Y_m = k)$ . Because we are only interested in sequences that include the tag bigram, this sum can be decomposed into three parts: the *prefixes*  $\mathbf{y}_{1:m-1}$ , terminating in  $Y_{m-1} = k'$ ; the

---

<sup>10</sup>Recall the notational convention of upper-case letters for random variables, e.g.  $Y_m$ , and lower case letters for specific values, e.g.,  $y_m$ , so that  $Y_m = k$  is interpreted as the event of random variable  $Y_m$  taking the value  $k$ .

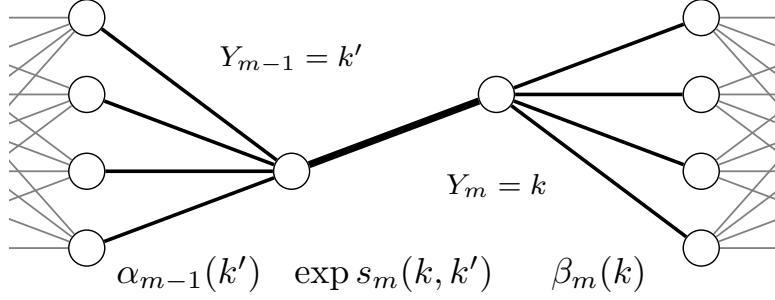


Figure 7.3: A schematic illustration of the computation of the marginal probability  $\Pr(Y_{m-1} = k', Y_m = k)$ , using the forward score  $\alpha_{m-1}(k')$  and the backward score  $\beta_m(k)$ .

transition  $(Y_{m-1} = k') \rightarrow (Y_m = k)$ ; and the suffixes  $\mathbf{y}_{m:M}$ , beginning with the tag  $Y_m = k$ :

$$\sum_{\mathbf{y}: Y_m = k, Y_{m-1} = k'} \prod_{n=1}^M \exp s_n(y_n, y_{n-1}) = \sum_{\mathbf{y}_{1:m-1}: Y_{m-1} = k'} \prod_{n=1}^{m-1} \exp s_n(y_n, y_{n-1}) \times \exp s_m(k, k') \times \sum_{\mathbf{y}_{m:M}: Y_m = k} \prod_{n=m+1}^{M+1} \exp s_n(y_n, y_{n-1}). \quad [7.87]$$

The result is product of three terms: a score that sums over all the ways to get to the position  $(Y_{m-1} = k')$ , a score for the transition from  $k'$  to  $k$ , and a score that sums over all the ways of finishing the sequence from  $(Y_m = k)$ . The first term of Equation 7.87 is equal to the **forward variable**,  $\alpha_{m-1}(k')$ . The third term — the sum over ways to finish the sequence — can also be defined recursively, this time moving over the trellis from right to left, which is known as the **backward recurrence**:

$$\beta_m(k) \triangleq \sum_{\mathbf{y}_{m:M}: Y_m = k} \prod_{n=m}^{M+1} \exp s_n(y_n, y_{n-1}) \quad [7.88]$$

$$= \sum_{k' \in \mathcal{Y}} \exp s_{m+1}(k', k) \sum_{\mathbf{y}_{m+1:M}: Y_m = k'} \prod_{n=m+1}^{M+1} \exp s_n(y_n, y_{n-1}) \quad [7.89]$$

$$= \sum_{k' \in \mathcal{Y}} \exp s_{m+1}(k', k) \times \beta_{m+1}(k'). \quad [7.90]$$

<sup>3791</sup> To understand this computation, compare with the forward recurrence in Equation 7.81.

In practice, numerical stability demands that we work in the log domain,

$$\log \alpha_m(k) = \log \sum_{k' \in \mathcal{Y}} \exp (\log s_m(k, k') + \log \alpha_{m-1}(k')) \quad [7.91]$$

$$\log \beta_{m-1}(k) = \log \sum_{k' \in \mathcal{Y}} \exp (\log s_m(k', k) + \log \beta_m(k')). \quad [7.92]$$

The application of the forward and backward probabilities is shown in Figure 7.3. Both the forward and backward recurrences operate on the trellis, which implies a space complexity  $\mathcal{O}(MK)$ . Because both recurrences require computing a sum over  $K$  terms at each node in the trellis, their time complexity is  $\mathcal{O}(MK^2)$ .

## 7.6 Neural sequence labeling

In neural network approaches to sequence labeling, we construct a vector representation for each tagging decision, based on the word and its context. Neural networks can perform tagging as a per-token classification decision, or they can be combined with the Viterbi algorithm to tag the entire sequence globally.

### 7.6.1 Recurrent neural networks

Recurrent neural networks (RNNs) were introduced in chapter 6 as a language modeling technique, in which the context at token  $m$  is summarized by a recurrently-updated vector,

$$\mathbf{h}_m = g(\mathbf{x}_m, \mathbf{h}_{m-1}), \quad m = 1, 2, \dots, M,$$

where  $\mathbf{x}_m$  is the vector **embedding** of the token  $w_m$  and the function  $g$  defines the recurrence. The starting condition  $\mathbf{h}_0$  is an additional parameter of the model. The long short-term memory (LSTM) is a more complex recurrence, in which a memory cell is through a series of gates, avoiding repeated application of the non-linearity. Despite these bells and whistles, both models share the basic architecture of recurrent updates across a sequence, and both will be referred to as RNNs here.

A straightforward application of RNNs to sequence labeling is to score each tag  $y_m$  as a linear function of  $\mathbf{h}_m$ :

$$\psi_m(y) = \beta_y \cdot \mathbf{h}_m \quad [7.93]$$

$$\hat{y}_m = \underset{y}{\operatorname{argmax}} \psi_m(y). \quad [7.94]$$

The score  $\psi_m(y)$  can also be converted into a probability distribution using the usual softmax operation,

$$p(y | \mathbf{w}_{1:m}) = \frac{\exp \psi_m(y)}{\sum_{y' \in \mathcal{Y}} \exp \psi_m(y')}. \quad [7.95]$$

3810 Using this transformation, it is possible to train the tagger from the negative log-likelihood  
 3811 of the tags, as in a conditional random field. Alternatively, a hinge loss or margin loss  
 3812 objective can be constructed from the raw scores  $\psi_m(y)$ .

The hidden state  $\mathbf{h}_m$  accounts for information in the input leading up to position  $m$ , but it ignores the subsequent tokens, which may also be relevant to the tag  $y_m$ . This can be addressed by adding a second RNN, in which the input is reversed, running the recurrence from  $w_M$  to  $w_1$ . This is known as a **bidirectional recurrent neural network** (Graves and Schmidhuber, 2005), and is specified as:

$$\overleftarrow{\mathbf{h}}_m = g(\mathbf{x}_m, \overleftarrow{\mathbf{h}}_{m+1}), \quad m = 1, 2, \dots, M. \quad [7.96]$$

3813 The hidden states of the left-to-right RNN are denoted  $\overrightarrow{\mathbf{h}}_m$ . The left-to-right and right-to-  
 3814 left vectors are concatenated,  $\mathbf{h}_m = [\overleftarrow{\mathbf{h}}_m; \overrightarrow{\mathbf{h}}_m]$ . The scoring function in Equation 7.93 is  
 3815 applied to this concatenated vector.

3816 Bidirectional RNN tagging has several attractive properties. Ideally, the representa-  
 3817 tion  $\mathbf{h}_m$  summarizes the useful information from the surrounding context, so that it is not  
 3818 necessary to design explicit features to capture this information. If the vector  $\mathbf{h}_m$  is an ad-  
 3819 equate summary of this context, then it may not even be necessary to perform the tagging  
 3820 jointly: in general, the gains offered by joint tagging of the entire sequence are diminished  
 3821 as the individual tagging model becomes more powerful. Using backpropagation, the  
 3822 word vectors  $\mathbf{x}$  can be trained “end-to-end”, so that they capture word properties that are  
 3823 useful for the tagging task. Alternatively, if limited labeled data is available, we can use  
 3824 word embeddings that are “pre-trained” from unlabeled data, using a language modeling  
 3825 objective (as in § 6.3) or a related word embedding technique (see chapter 14). It is even  
 3826 possible to combine both fine-tuned and pre-trained embeddings in a single model.

3827 **Neural structure prediction** The bidirectional recurrent neural network incorporates in-  
 3828 formation from throughout the input, but each tagging decision is made independently.  
 3829 In some sequence labeling applications, there are very strong dependencies between tags:  
 3830 it may even be impossible for one tag to follow another. In such scenarios, the tagging  
 3831 decision must be made jointly across the entire sequence.

3832 Neural sequence labeling can be combined with the Viterbi algorithm by defining the  
 3833 local scores as:

$$s_m(y_m, y_{m-1}) = \beta_{y_m} \cdot \mathbf{h}_m + \eta_{y_{m-1}, y_m}, \quad [7.97]$$

3834 where  $\mathbf{h}_m$  is the RNN hidden state,  $\beta_{y_m}$  is a vector associated with tag  $y_m$ , and  $\eta_{y_{m-1}, y_m}$   
 3835 is a scalar parameter for the tag transition  $(y_{m-1}, y_m)$ . These local scores can then be  
 3836 incorporated into the Viterbi algorithm for inference, and into the forward algorithm for  
 3837 training. This model is shown in Figure 7.4. It can be trained from the conditional log-  
 3838 likelihood objective defined in Equation 7.76, backpropagating to the tagging parameters

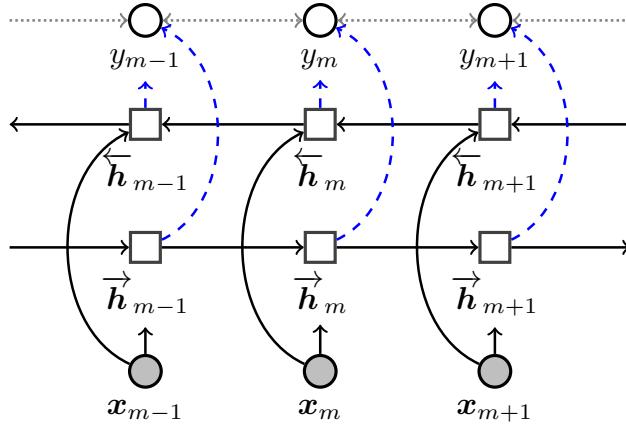


Figure 7.4: Bidirectional LSTM for sequence labeling. The solid lines indicate computation, the dashed lines indicate probabilistic dependency, and the dotted lines indicate the optional additional probabilistic dependencies between labels in the biLSTM-CRF.

3839  $\beta$  and  $\eta$ , as well as the parameters of the RNN. This model is called the **LSTM-CRF**, due  
 3840 to its combination of aspects of the long short-term memory and conditional random field  
 3841 models (Huang et al., 2015).

3842 The LSTM-CRF is especially effective on the task of **named entity recognition** (Lample  
 3843 et al., 2016), a sequence labeling task that is described in detail in § 8.3. This task has strong  
 3844 dependencies between adjacent tags, so structure prediction is especially important.

### 3845 7.6.2 Character-level models

3846 As in language modeling, rare and unseen words are a challenge: if we encounter a word  
 3847 that was not in the training data, then there is no obvious choice for the word embed-  
 3848 ding  $x_m$ . One solution is to use a generic **unseen word** embedding for all such words.  
 3849 However, in many cases, properties of unseen words can be guessed from their spellings.  
 3850 For example, *whimsical* does not appear in the Universal Dependencies (UD) English Tree-  
 3851 bank, yet the suffix *-al* makes it likely to be adjective; by the same logic, *unflinchingly* is  
 3852 likely to be an adverb, and *barnacle* is likely to be a noun.

3853 In feature-based models, these morphological properties were handled by suffix fea-  
 3854 tures; in a neural network, they can be incorporated by constructing the embeddings of  
 3855 unseen words from their spellings or morphology. One way to do this is to incorporate  
 3856 an additional layer of bidirectional RNNs, one for each word in the vocabulary (Ling  
 3857 et al., 2015). For each such character-RNN, the inputs are the characters, and the output  
 3858 is the concatenation of the final states of the left-facing and right-facing passes,  $\phi_w =$

[ $\vec{h}_{N_w}^{(w)}; \overleftarrow{h}_0^{(w)}$ ], where  $\vec{h}_{N_w}^{(w)}$  is the final state of the right-facing pass for word  $w$ , and  $N_w$  is the number of characters in the word. The character RNN model is trained by back-propagation from the tagging objective. On the test data, the trained RNN is applied to out-of-vocabulary words (or all words), yielding inputs to the word-level tagging RNN. Other approaches to compositional word embeddings are described in § 14.7.1.

### 7.6.3 Convolutional Neural Networks for Sequence Labeling

One disadvantage of recurrent neural networks is that the architecture requires iterating through the sequence of inputs and predictions: each hidden vector  $h_m$  must be computed from the previous hidden vector  $h_{m-1}$ , before predicting the tag  $y_m$ . These iterative computations are difficult to parallelize, and fail to exploit the speedups offered by **graphics processing units (GPUs)** on operations such as matrix multiplication. **Convolutional neural networks** achieve better computational performance by predicting each label  $y_m$  from a set of matrix operations on the neighboring word embeddings,  $x_{m-k:m+k}$  (Collobert et al., 2011). Because there is no hidden state to update, the predictions for each  $y_m$  can be computed in parallel. For more on convolutional neural networks, see § 3.4. Character-based word embeddings can also be computed using convolutional neural networks (Santos and Zadrozny, 2014).

## 7.7 \*Unsupervised sequence labeling

In unsupervised sequence labeling, the goal is to induce a hidden Markov model from a corpus of *unannotated* text ( $w^{(1)}, w^{(2)}, \dots, w^{(N)}$ ), where each  $w^{(i)}$  is a sequence of length  $M^{(i)}$ . This is an example of the general problem of **structure induction**, which is the unsupervised version of structure prediction. The tags that result from unsupervised sequence labeling might be useful for some downstream task, or they might help us to better understand the language’s inherent structure. For part-of-speech tagging, it is common to use a tag dictionary that lists the allowed tags for each word, simplifying the problem (Christodoulopoulos et al., 2010).

Unsupervised learning in hidden Markov models can be performed using the **Baum-Welch algorithm**, which combines the forward-backward algorithm (§ 7.5.3.3) with expectation-maximization (EM; § 5.1.2). In the M-step, the HMM parameters from expected counts:

$$\Pr(W = i \mid Y = k) = \phi_{k,i} = \frac{E[\text{count}(W = i, Y = k)]}{E[\text{count}(Y = k)]}$$

$$\Pr(Y_m = k \mid Y_{m-1} = k') = \lambda_{k',k} = \frac{E[\text{count}(Y_m = k, Y_{m-1} = k')]}{E[\text{count}(Y_{m-1} = k')]} \quad 3884$$

3885 The expected counts are computed in the E-step, using the forward and backward  
 3886 recurrences. The local scores follow the usual definition for hidden Markov models,

$$s_m(k, k') = \log p_E(w_m | Y_m = k; \phi) + \log p_T(Y_m = k | Y_{m-1} = k'; \lambda). \quad [7.98]$$

The expected transition counts for a single instance are,

$$E[\text{count}(Y_m = k, Y_{m-1} = k') | \mathbf{w}] = \sum_{m=1}^M \Pr(Y_{m-1} = k', Y_m = k | \mathbf{w}) \quad [7.99]$$

$$= \frac{\sum_{\mathbf{y}: Y_m=k, Y_{m-1}=k'} \prod_{n=1}^M \exp s_n(y_n, y_{n-1})}{\sum_{\mathbf{y}'} \prod_{n=1}^M \exp s_n(y'_n, y'_{n-1})}. \quad [7.100]$$

As described in § 7.5.3.3, these marginal probabilities can be computed from the forward-backward recurrence,

$$\Pr(Y_{m-1} = k', Y_m = k | \mathbf{w}) = \frac{\alpha_{m-1}(k') \times s_m(k, k') \times \beta_m(k)}{\alpha_{M+1}(\blacklozenge)}. \quad [7.101]$$

In a hidden Markov model, each element of the forward-backward computation has a special interpretation:

$$\alpha_{m-1}(k') = p(Y_{m-1} = k', \mathbf{w}_{1:m-1}) \quad [7.102]$$

$$s_m(k, k') = p(Y_m = k, w_m | Y_{m-1} = k') \quad [7.103]$$

$$\beta_m(k) = p(\mathbf{w}_{m+1:M} | Y_m = k). \quad [7.104]$$

Applying the conditional independence assumptions of the hidden Markov model (defined in Algorithm 12), the product is equal to the joint probability of the tag bigram and the entire input,

$$\begin{aligned} \alpha_{m-1}(k') \times s_m(k, k') \times \beta_m(k) &= p(Y_{m-1} = k', \mathbf{w}_{1:m-1}) \\ &\quad \times p(Y_m = k, w_m | Y_{m-1} = k') \\ &\quad \times p(\mathbf{w}_{m+1:M} | Y_m = k) \\ &= p(Y_{m-1} = k', Y_m = k, \mathbf{w}_{1:M}). \end{aligned} \quad [7.105]$$

Dividing by  $\alpha_{M+1}(\blacklozenge) = p(\mathbf{w}_{1:M})$  gives the desired probability,

$$\frac{\alpha_{m-1}(k') \times s_m(k, k') \times \beta_m(k)}{\alpha_{M+1}(\blacklozenge)} = \frac{p(Y_{m-1} = k', Y_m = k, \mathbf{w}_{1:M})}{p(\mathbf{w}_{1:M})} \quad [7.106]$$

$$= \Pr(Y_{m-1} = k', Y_m = k | \mathbf{w}_{1:M}). \quad [7.107]$$

3887 The expected emission counts can be computed in a similar manner, using the product  
 3888  $\alpha_m(k) \times \beta_m(k)$ .

3889 **7.7.1 Linear dynamical systems**

3890 The forward-backward algorithm can be viewed as Bayesian state estimation in a discrete  
 3891 state space. In a continuous state space,  $\mathbf{y}_m \in \mathbb{R}^K$ , the equivalent algorithm is the **Kalman**  
 3892 **smoother**. It also computes marginals  $p(\mathbf{y}_m | \mathbf{x}_{1:M})$ , using a similar two-step algorithm  
 3893 of forward and backward passes. Instead of computing a trellis of values at each step, the  
 3894 Kalman smoother computes a probability density function  $q_{\mathbf{y}_m}(\mathbf{y}_m; \boldsymbol{\mu}_m, \Sigma_m)$ , character-  
 3895 ized by a mean  $\boldsymbol{\mu}_m$  and a covariance  $\Sigma_m$  around the latent state. Connections between the  
 3896 Kalman Smoother and the forward-backward algorithm are elucidated by Minka (1999)  
 3897 and Murphy (2012).

3898 **7.7.2 Alternative unsupervised learning methods**

As noted in § 5.5, expectation-maximization is just one of many techniques for structure induction. One alternative is to use **Markov Chain Monte Carlo (MCMC)** sampling algorithms, which are briefly described in § 5.5.1. For the specific case of sequence labeling, Gibbs sampling can be applied by iteratively sampling each tag  $y_m$  conditioned on all the others (Finkel et al., 2005):

$$p(y_m | \mathbf{y}_{-m}, \mathbf{w}_{1:M}) \propto p(w_m | y_m) p(y_m | \mathbf{y}_{-m}). \quad [7.108]$$

3899 Gibbs Sampling has been applied to unsupervised part-of-speech tagging by Goldwater  
 3900 and Griffiths (2007). **Beam sampling** is a more sophisticated sampling algorithm, which  
 3901 randomly draws entire sequences  $\mathbf{y}_{1:M}$ , rather than individual tags  $y_m$ ; this algorithm  
 3902 was applied to unsupervised part-of-speech tagging by Van Gael et al. (2009). Spectral  
 3903 learning (see § 5.5.2) can also be applied to sequence labeling. By factoring matrices of  
 3904 co-occurrence counts of word bigrams and trigrams (Song et al., 2010; Hsu et al., 2012), it  
 3905 is possible to obtain globally optimal estimates of the transition and emission parameters,  
 3906 under mild assumptions.

3907 **7.7.3 Semiring Notation and the Generalized Viterbi Algorithm**

The Viterbi and Forward recurrences can each be performed over probabilities or log probabilities, yielding a total of four closely related recurrences. These four recurrence scan in fact be expressed as a single recurrence in a more general notation, known as **semiring algebra**. Let the symbol  $\oplus$  represent generalized addition, and the symbol  $\otimes$  represent generalized multiplication.<sup>11</sup> Given these operators, we can denote a general-

---

<sup>11</sup>In a semiring, the addition and multiplication operators must both obey associativity, and multiplication must distribute across addition; the addition operator must be commutative; there must be additive and multiplicative identities  $\bar{0}$  and  $\bar{1}$ , such that  $a \oplus \bar{0} = a$  and  $a \otimes \bar{1} = a$ ; and there must be a multiplicative annihilator  $\bar{0}$ , such that  $a \otimes \bar{0} = \bar{0}$ .

ized Viterbi recurrence as,

$$v_m(k) = \bigoplus_{k' \in \mathcal{Y}} s_m(k, k') \otimes v_{m-1}(k'). \quad [7.109]$$

3908     Each recurrence that we have seen so far is a special case of this generalized Viterbi  
 3909     recurrence:

- 3910     • In the max-product Viterbi recurrence over probabilities, the  $\oplus$  operation corre-  
 3911         sponds to maximization, and the  $\otimes$  operation corresponds to multiplication.
- 3912     • In the forward recurrence over probabilities, the  $\oplus$  operation corresponds to addi-  
 3913         tion, and the  $\otimes$  operation corresponds to multiplication.
- 3914     • In the max-product Viterbi recurrence over log-probabilities, the  $\oplus$  operation corre-  
 3915         sponds to maximization, and the  $\otimes$  operation corresponds to addition.<sup>12</sup>
- 3916     • In the forward recurrence over log-probabilities, the  $\oplus$  operation corresponds to log-  
 3917         addition,  $a \oplus b = \log(e^a + e^b)$ . The  $\otimes$  operation corresponds to addition.

3918     The mathematical abstraction offered by semiring notation can be applied to the soft-  
 3919     ware implementations of these algorithms, yielding concise and modular implementa-  
 3920     tions. For example, in the OPENFST library, generic operations are parametrized by the  
 3921     choice of semiring (Allauzen et al., 2007).

## 3922 Exercises

- 3923     1. Extend the example in § 7.3.1 to the sentence *they can can fish*, meaning that “they can  
 3924         put fish into cans.” Build the trellis for this example using the weights in Table 7.1,  
 3925         and identify the best-scoring tag sequence. If the scores for noun and verb are tied,  
 3926         then you may assume that the backpointer always goes to noun.
- 3927     2. Using the tagset  $\mathcal{Y} = \{N, V\}$ , and the feature set  $f(\mathbf{w}, y_m, y_{m-1}, m) = \{(w_m, y_m), (y_m, y_{m-1})\}$ ,  
 3928         show that there is no set of weights such that the correct tagging is obtained for both  
 3929         *they can fish* (N V V) and *they can can fish* (N V V N).
- 3930     3. Work out what happens if you train a structured perceptron on the two exam-  
 3931         ples mentioned in the previous problem, using the transition and emission features  
 3932          $(y_m, y_{m-1})$  and  $(y_m, w_m)$ . Initialize all weights at 0, and assume that the Viterbi algo-  
 3933         rithm always chooses *N* when the scores for the two tags are tied, so that the initial  
 3934         prediction for *they can fish* is N N N.

---

<sup>12</sup>This is sometimes called the **tropical semiring**, in honor of the Brazilian mathematician Imre Simon.

- 3935     4. Consider the garden path sentence, *The old man the boat*. Given word-tag and tag-tag  
 3936       features, what inequality in the weights must hold for the correct tag sequence to  
 3937       outscore the garden path tag sequence for this example?
- 3938     5. Using the weights in Table 7.1, explicitly compute the log-probabilities for all pos-  
 3939       sible taggings of the input *fish can*. Verify that the forward algorithm recovers the  
 3940       aggregate log probability.
- 3941     6. Sketch out an algorithm for a variant of Viterbi that returns the top- $n$  label se-  
 3942       quences. What is the time and space complexity of this algorithm?
- 3943     7. Show how to compute the marginal probability  $\Pr(y_{m-2} = k, y_m = k' \mid \mathbf{w}_{1:M})$ , in  
 3944       terms of the forward and backward variables, and the potentials  $s_n(y_n, y_{n-1})$ .
- 3945     8. Suppose you receive a stream of text, where some of tokens have been replaced at  
 3946       random with *NOISE*. For example:
- 3947       • Source: *I try all things, I achieve what I can*
  - 3948       • Message received: *I try NOISE NOISE, I NOISE what I NOISE*
- 3949     Assume you have access to a pre-trained bigram language model, which gives prob-  
 3950       abilities  $p(w_m \mid w_{m-1})$ . These probabilities can be assumed to be non-zero for all  
 3951       bigrams.
- 3952     a) Show how to use the Viterbi algorithm to try to recover the source by maxi-  
 3953       mizing the bigram language model log-probability. Specifically, set the scores  
 3954        $s_m(y_m, y_{m-1})$  so that the Viterbi algorithm selects a sequence of words that  
 3955       maximizes the bigram language model log-probability, *while leaving the non-*  
 3956       *noise tokens intact*. Your solution should not modify the logic of the Viterbi  
 3957       algorithm, it should only set the scores  $s_m(y_m, y_{m-1})$ .
- 3958     b) An alternative solution is to iterate through the text from  $m \in \{1, 2, \dots, M\}$ ,  
 3959       replacing each noise token with the word that maximizes  $P(w_m \mid w_{m-1})$  ac-  
 3960       cording to the bigram language model. Given an upper bound on the expected  
 3961       fraction of tokens for which the two approaches will disagree.
- 3962     9. Let  $\alpha(\cdot)$  and  $\beta(\cdot)$  indicate the forward and backward variables as defined in § 7.5.3.3.  
 3963       Prove that  $\alpha_{M+1}(\blacklozenge) = \beta_0(\lozenge) = \sum_y \alpha_m(y) \beta_m(y), \forall m \in \{1, 2, \dots, M\}$ .
- 3964     10. Consider an RNN tagging model with a tanh activation function on the hidden  
 3965       layer, and a hinge loss on the output. (The problem also works for the margin loss  
 3966       and negative log-likelihood.) Suppose you initialize all parameters to zero: this in-  
 3967       cludes the word embeddings that make up  $x$ , the transition matrix  $\Theta$ , the output  
 3968       weights  $\beta$ , and the initial hidden state  $h_0$ .

- 3969        a) Prove that for any data and for any gradient-based learning algorithm, all pa-  
3970              rameters will be stuck at zero.
- 3971        b) Would a sigmoid activation function avoid this problem?



## 3972 Chapter 8

# 3973 Applications of sequence labeling

3974 Sequence labeling has applications throughout natural language processing. This chapter  
3975 focuses on part-of-speech tagging, morpho-syntactic attribute tagging, named entity  
3976 recognition, and tokenization. It also touches briefly on two applications to interactive  
3977 settings: dialogue act recognition and the detection of code-switching points between  
3978 languages.

### 3979 8.1 Part-of-speech tagging

3980 The **syntax** of a language is the set of principles under which sequences of words are  
3981 judged to be grammatically acceptable by fluent speakers. One of the most basic syntactic  
3982 concepts is the **part-of-speech** (POS), which refers to the syntactic role of each word in a  
3983 sentence. This concept was used informally in the previous chapter, and you may have  
3984 some intuitions from your own study of English. For example, in the sentence *We like*  
3985 *vegetarian sandwiches*, you may already know that *we* and *sandwiches* are nouns, *like* is a  
3986 verb, and *vegetarian* is an adjective. These labels depend on the context in which the word  
3987 appears: in *she eats like a vegetarian*, the word *like* is a preposition, and the word *vegetarian*  
3988 is a noun.

3989 Parts-of-speech can help to disentangle or explain various linguistic problems. Recall  
3990 Chomsky's proposed distinction in chapter 6:

- 3991 (8.1) Colorless green ideas sleep furiously.
- 3992 (8.2) \*Ideas colorless furiously green sleep.

3993 One difference between these two examples is that the first contains part-of-speech transitions  
3994 that are typical in English: adjective to adjective, adjective to noun, noun to verb, and verb  
3995 to adverb. The second example contains transitions that are unusual: noun to adjective  
3996 and adjective to verb. The ambiguity in a headline like,

3997 (8.3) Teacher Strikes Idle Children

3998 can also be explained in terms of parts of speech: in the interpretation that was likely  
 3999 intended, *strikes* is a noun and *idle* is a verb; in the alternative explanation, *strikes* is a verb  
 4000 and *idle* is an adjective.

4001 Part-of-speech tagging is often taken as a early step in a natural language processing  
 4002 pipeline. Indeed, parts-of-speech provide features that can be useful for many of the  
 4003 tasks that we will encounter later, such as parsing (chapter 10), coreference resolution  
 4004 (chapter 15), and relation extraction (chapter 17).

4005 **8.1.1 Parts-of-Speech**

4006 The **Universal Dependencies** project (UD) is an effort to create syntactically-annotated  
 4007 corpora across many languages, using a single annotation standard (Nivre et al., 2016). As  
 4008 part of this effort, they have designed a part-of-speech **tagset**, which is meant to capture  
 4009 word classes across as many languages as possible.<sup>1</sup> This section describes that inventory,  
 4010 giving rough definitions for each of tags, along with supporting examples.

4011 Part-of-speech tags are **morphosyntactic**, rather than **semantic**, categories. This means  
 4012 that they describe words in terms of how they pattern together and how they are inter-  
 4013 nally constructed (e.g., what suffixes and prefixes they include). For example, you may  
 4014 think of a noun as referring to objects or concepts, and verbs as referring to actions or  
 4015 events. But events can also be nouns:

4016 (8.4) ... the **howling** of the **shrieking** storm.

4017 Here *howling* and *shrieking* are events, but grammatically they act as a noun and adjective  
 4018 respectively.

4019 **8.1.1.1 The Universal Dependency part-of-speech tagset**

4020 The UD tagset is broken up into three groups: open class tags, closed class tags, and  
 4021 “others.”

4022 **Open class tags** Nearly all languages contain nouns, verbs, adjectives, and adverbs.<sup>2</sup>  
 4023 These are all **open word classes**, because new words can easily be added to them. The  
 4024 UD tagset includes two other tags that are open classes: proper nouns and interjections.

4025 • **Nouns** (UD tag: NOUN) tend to describe entities and concepts, e.g.,

---

<sup>1</sup>The UD tagset builds on earlier work from Petrov et al. (2012), in which a set of twelve universal tags was identified by creating mappings from tagsets for individual languages.

<sup>2</sup>One prominent exception is Korean, which some linguists argue does not have adjectives Kim (2002).

4026 (8.5) **Toes** are scarce among veteran **blubber men**.

4027 In English, nouns tend to follow determiners and adjectives, and can play the subject  
4028 role in the sentence. They can be marked for the plural number by an -s suffix.

4029 • **Proper nouns** (PROPN) are tokens in names, which uniquely specify a given entity,

4030 (8.6) “**Moby Dick?**” shouted **Ahab**.

4031 • **Verbs** (VERB), according to the UD guidelines, “typically signal events and ac-  
4032 tions.” But they are also defined grammatically: they “can constitute a minimal  
4033 predicate in a clause, and govern the number and types of other constituents which  
4034 may occur in a clause.”<sup>3</sup>

4035 (8.7) “**Moby Dick?**” shouted Ahab.

4036 (8.8) Shall we **keep chasing** this murderous fish?

4037 English verbs tend to come in between the subject and some number of direct ob-  
4038 jects, depending on the verb. They can be marked for **tense** and **aspect** using suffixes  
4039 such as *-ed* and *-ing*. (These suffixes are an example of **inflectional morphology**,  
4040 which is discussed in more detail in § 9.1.4.)

4041 • **Adjectives** (ADJ) describe properties of entities,

4042 (8.9) Shall we keep chasing this **murderous** fish?

4043 (8.10) Toes are **scarce** among **veteran** blubber men.

4044 In the second example, *scarce* is a predicative adjective, linked to the subject by the  
4045 **copula verb** *are*. In contrast, *murderous* and *veteran* are attributive adjectives, modi-  
4046 fying the noun phrase in which they are embedded.

4047 • **Adverbs** (ADV) describe properties of events, and may also modify adjectives or  
4048 other adverbs:

4049 (8.11) It is not down on any map; true places **never** are.

4050 (8.12) ... **treacherously** hidden beneath the loveliest tints of azure

4051 (8.13) Not drowned **entirely**, though.

4052 • **Interjections** (INTJ) are used in exclamations, e.g.,

4053 (8.14) **Aye aye!** it was that accursed white whale that razed me.

---

<sup>3</sup><http://universaldependencies.org/u/pos/VERB.html>

4054 **Closed class tags** Closed word classes rarely receive new members. They are sometimes  
 4055 referred to as **function words** — as opposed to **content words** — as they have little lexical  
 4056 meaning of their own, but rather, help to organize the components of the sentence.

- 4057 • **Adpositions** (ADP) describe the relationship between a complement (usually a noun  
 4058 phrase) and another unit in the sentence, typically a noun or verb phrase.

4059 (8.15) Toes are scarce **among** veteran blubber men.

4060 (8.16) It is not **down on** any map.

4061 (8.17) Give not thyself **up** then.

4062 As the examples show, English generally uses prepositions, which are adpositions  
 4063 that appear before their complement. (An exception is *ago*, as in, *we met three days*  
 4064 *ago*). Postpositions are used in other languages, such as Japanese and Turkish.

- 4065 • **Auxiliary verbs** (AUX) are a closed class of verbs that add information such as  
 4066 tense, aspect, person, and number.

4067 (8.18) **Shall** we keep chasing this murderous fish?

4068 (8.19) What the white whale was to Ahab, **has been** hinted.

4069 (8.20) Ahab **must** use tools.

4070 (8.21) Meditation and water **are** wedded forever.

4071 (8.22) Toes **are** scarce among veteran blubber men.

4072 The final example is a copula verb, which is also tagged as an auxiliary in the UD  
 4073 corpus.

- 4074 • **Coordinating conjunctions** (CCONJ) express relationships between two words or  
 4075 phrases, which play a parallel role:

4076 (8.23) Meditation **and** water are wedded forever.

- 4077 • **Subordinating conjunctions** (SCONJ) link two clauses, making one syntactically  
 4078 subordinate to the other:

4079 (8.24) It is the easiest thing in the world for a man to look as **if** he had a great  
 4080 secret in him.

4081 Note that

- 4082 • **Pronouns** (PRON) are words that substitute for nouns or noun phrases.

4083 (8.25) Be **it what it will**, I'll go to **it** laughing.

4084 (8.26) I try all things, I achieve **what** I can.

4085 The example includes the personal pronouns *I* and *it*, as well as the relative pronoun  
4086 *what*. Other pronouns include *myself*, *somebody*, and *nothing*.

- 4087 • **Determiners** (DET) provide additional information about the nouns or noun phrases  
4088 that they modify:

4089 (8.27) What **the** white whale was to Ahab, has been hinted.

4090 (8.28) It is not down on **any** map.

4091 (8.29) I try **all** things ...

4092 (8.30) Shall we keep chasing **this** murderous fish?

4093 Determiners include articles (*the*), possessive determiners (*their*), demonstratives  
4094 (*this murderous fish*), and quantifiers (*any map*).

- 4095 • **Numerals** (NUM) are an infinite but closed class, which includes integers, fractions,  
4096 and decimals, regardless of whether spelled out or written in numerical form.

4097 (8.31) How then can this **one** small heart beat.

4098 (8.32) I am going to put him down for the **three hundredth**.

- 4099 • **Particles** (PART) are a catch-all of function words that combine with other words or  
4100 phrases, but do not meet the conditions of the other tags. In English, this includes  
4101 the infinitival *to*, the possessive marker, and negation.

4102 (8.33) Better **to** sleep with a sober cannibal than a drunk Christian.

4103 (8.34) So man's insanity is heaven's sense

4104 (8.35) It is **not** down on any map

4105 As the second example shows, the possessive marker is not considered part of the  
4106 same token as the word that it modifies, so that *man's* is split into two tokens. (Tok-  
4107 enization is described in more detail in § 8.4.) A non-English example of a particle  
4108 is the Japanese question marker *ka*:<sup>4</sup>

4109 (8.36) Sensei desu ka

Teacher is ?

4110 Is she a teacher?

---

<sup>4</sup>In this notation, the first line is the transliterated Japanese text, the second line is a token-to-token **gloss**, and the third line is the translation.

4111   **Other** The remaining UD tags include punctuation (PUN) and symbols (SYM). Punc-  
 4112 tuation is purely structural — e.g., commas, periods, colons — while symbols can carry  
 4113 content of their own. Examples of symbols include dollar and percentage symbols, math-  
 4114 ematical operators, emoticons, emojis, and internet addresses. A final catch-all tag is X,  
 4115 which is used for words that cannot be assigned another part-of-speech category. The X  
 4116 tag is also used in cases of **code switching** (between languages), described in § 8.5.

4117   **8.1.1.2 Other tagsets**

4118 Prior to the Universal Dependency treebank, part-of-speech tagging was performed us-  
 4119 ing language-specific tagsets. The dominant tagset for English was designed as part of  
 4120 the **Penn Treebank** (PTB), and it includes 45 tags — more than three times as many as  
 4121 the UD tagset. This granularity is reflected in distinctions between singular and plural  
 4122 nouns, verb tenses and aspects, possessive and non-possessive pronouns, comparative  
 4123 and superlative adjectives and adverbs (e.g., *faster, fastest*), and so on. The Brown corpus  
 4124 includes a tagset that is even more detailed, with 87 tags Francis (1964), including special  
 4125 tags for individual auxiliary verbs such as *be, do, and have*.

4126   Different languages make different distinctions, and so the PTB and Brown tagsets are  
 4127 not appropriate for a language such as Chinese, which does not mark the verb tense (Xia,  
 4128 2000); nor for Spanish, which marks every combination of person and number in the  
 4129 verb ending; nor for German, which marks the case of each noun phrase. Each of these  
 4130 languages requires more detail than English in some areas of the tagset, and less in other  
 4131 areas. The strategy of the Universal Dependencies corpus is to design a coarse-grained  
 4132 tagset to be used across all languages, and then to additionally annotate language-specific  
 4133 **morphosyntactic attributes**, such as number, tense, and case. The attribute tagging task  
 4134 is described in more detail in § 8.2.

4135   Social media such as Twitter have been shown to require tagsets of their own (Gimpel  
 4136 et al., 2011). Such corpora contain some tokens that are not equivalent to anything en-  
 4137 countered in a typical written corpus: e.g., emoticons, URLs, and hashtags. Social media  
 4138 also includes dialectal words like *gonna* ('going to', e.g. *We gonna be fine*) and *Ima* ('I'm  
 4139 going to', e.g., *Ima tell you one more time*), which can be analyzed either as non-standard  
 4140 orthography (making tokenization impossible), or as lexical items in their own right. In  
 4141 either case, it is clear that existing tags like NOUN and VERB cannot handle cases like *Ima*,  
 4142 which combine aspects of the noun and verb. Gimpel et al. (2011) therefore propose a new  
 4143 set of tags to deal with these cases.

4144   **8.1.2 Accurate part-of-speech tagging**

4145 Part-of-speech tagging is the problem of selecting the correct tag for each word in a sen-  
 4146 tence. Success is typically measured by accuracy on an annotated test set, which is simply  
 4147 the fraction of tokens that were tagged correctly.

## 4148 8.1.2.1 Baselines

4149 A simple baseline for part-of-speech tagging is to choose the most common tag for each  
4150 word. For example, in the Universal Dependencies treebank, the word *talk* appears 96  
4151 times, and 85 of those times it is labeled as a VERB: therefore, this baseline will always  
4152 predict VERB for this word. For words that do not appear in the training corpus, the base-  
4153 line simply guesses the most common tag overall, which is NOUN. In the Penn Treebank,  
4154 this simple baseline obtains accuracy above 92%. A more rigorous evaluation is the accu-  
4155 racy on **out-of-vocabulary words**, which are not seen in the training data. Tagging these  
4156 words correctly requires attention to the context and the word's internal structure.

## 4157 8.1.2.2 Contemporary approaches

4158 Conditional random fields and structured perceptron perform at or near the state-of-the-  
4159 art for part-of-speech tagging in English. For example, (Collins, 2002) achieved 97.1%  
4160 accuracy on the Penn Treebank, using a structured perceptron with the following base  
4161 features (originally introduced by Ratnaparkhi (1996)):

- 4162 • current word,  $w_m$
- 4163 • previous words,  $w_{m-1}, w_{m-2}$
- 4164 • next words,  $w_{m+1}, w_{m+2}$
- 4165 • previous tag,  $y_{m-1}$
- 4166 • previous two tags,  $(y_{m-1}, y_{m-2})$
- 4167 • for rare words:
  - 4168 – first  $k$  characters, up to  $k = 4$
  - 4169 – last  $k$  characters, up to  $k = 4$
  - 4170 – whether  $w_m$  contains a number, uppercase character, or hyphen.

4171 Similar results for the PTB data have been achieved using conditional random fields (CRFs;  
4172 Toutanova et al., 2003).

4173 More recent work has demonstrated the power of neural sequence models, such as the  
4174 **long short-term memory (LSTM)** (§ 7.6). Plank et al. (2016) apply a CRF and a bidirec-  
4175 tional LSTM to twenty-two languages in the UD corpus, achieving an average accuracy  
4176 of 94.3% for the CRF, and 96.5% with the bi-LSTM. Their neural model employs three  
4177 types of embeddings: fine-tuned word embeddings, which are updated during training;  
4178 pre-trained word embeddings, which are never updated, but which help to tag out-of-  
4179 vocabulary words; and character-based embeddings. The character-based embeddings  
4180 are computed by running an LSTM on the individual characters in each word, thereby  
4181 capturing common orthographic patterns such as prefixes, suffixes, and capitalization.  
4182 Extensive evaluations show that these additional embeddings are crucial to their model's  
4183 success.

word	PTB tag	UD tag	UD attributes
<i>The</i>	DT	DET	DEFINITE=DEF PRONTYPE=ART
<i>German</i>	JJ	ADJ	DEGREE=POS
<i>Expressionist</i>	NN	NOUN	NUMBER=SING
<i>movement</i>	NN	NOUN	NUMBER=SING
<i>was</i>	VBD	AUX	MOOD=IND NUMBER=SING PERSON=3 TENSE=PAST VERBFORM=FIN
<i>destroyed</i>	VBN	VERB	TENSE=PAST VERBFORM=PART VOICE=PASS
<i>as</i>	IN	ADP	
<i>a</i>	DT	DET	DEFINITE=IND PRONTYPE=ART
<i>result</i>	NN	NOUN	NUMBER=SING
.	.	PUNCT	

Figure 8.1: UD and PTB part-of-speech tags, and UD morphosyntactic attributes. Example selected from the UD 1.4 English corpus.

## 4184 8.2 Morphosyntactic Attributes

4185 There is considerably more to say about a word than whether it is a noun or a verb: in En-  
 4186 glish, verbs are distinguish by features such tense and aspect, nouns by number, adjectives  
 4187 by degree, and so on. These features are language-specific: other languages distinguish  
 4188 other features, such as **case** (the role of the noun with respect to the action of the sen-  
 4189 tence, which is marked in languages such as Latin and German<sup>5</sup>) and **evidentiality** (the  
 4190 source of information for the speaker’s statement, which is marked in languages such as  
 4191 Turkish). In the UD corpora, these attributes are annotated as feature-value pairs for each  
 4192 token.<sup>6</sup>

4193 An example is shown in Figure 8.1. The determiner *the* is marked with two attributes:  
 4194 **PRONTYPE=ART**, which indicates that it is an **article** (as opposed to another type of deter-

<sup>5</sup>Case is marked in English for some personal pronouns, e.g., *She saw her, They saw them*.

<sup>6</sup>The annotation and tagging of morphosyntactic attributes can be traced back to earlier work on Turkish (Oflazer and Kuruöz, 1994) and Czech (Hajič and Hladká, 1998). MULTEXT-East was an early multilingual corpus to include morphosyntactic attributes (Dimitrova et al., 1998).

miner or pronominal modifier), and DEFINITE=DEF, which indicates that it is a **definite article** (referring to a specific, known entity). The verbs are each marked with several attributes. The auxiliary verb *was* is third-person, singular, past tense, finite (conjugated), and indicative (describing an event that has happened or is currently happenings); the main verb *destroyed* is in participle form (so there is no additional person and number information), past tense, and passive voice. Some, but not all, of these distinctions are reflected in the PTB tags VBD (past-tense verb) and VBN (past participle).

While there are thousands of papers on part-of-speech tagging, there is comparatively little work on automatically labeling morphosyntactic attributes. Faruqui et al. (2016) train a support vector machine classification model, using a minimal feature set that includes the word itself, its prefixes and suffixes, and type-level information listing all possible morphosyntactic attributes for each word and its neighbors. Mueller et al. (2013) use a conditional random field (CRF), in which the tag space consists of all observed combinations of morphosyntactic attributes (e.g., the tag would be DEF+ART for the word *the* in Figure 8.1). This massive tag space is managed by decomposing the feature space over individual attributes, and pruning paths through the trellis. More recent work has employed bidirectional LSTM sequence models. For example, Pinter et al. (2017) train a bidirectional LSTM sequence model. The input layer and hidden vectors in the LSTM are shared across attributes, but each attribute has its own output layer, culminating in a softmax over all attribute values, e.g.  $y_t^{\text{NUMBER}} \in \{\text{SING}, \text{PLURAL}, \dots\}$ . They find that character-level information is crucial, especially when the amount of labeled data is limited.

Evaluation is performed by first computing recall and precision for each attribute. These scores can then be averaged at either the type or token level to obtain micro- or macro-*F*-MEASURE. Pinter et al. (2017) evaluate on 23 languages in the UD treebank, reporting a median micro-*F*-MEASURE of 0.95. Performance is strongly correlated with the size of the labeled dataset for each language, with a few outliers: for example, Chinese is particularly difficult, because although the dataset is relatively large ( $10^5$  tokens in the UD 1.4 corpus), only 6% of tokens have any attributes, offering few useful labeled instances.

### 8.3 Named Entity Recognition

A classical problem in information extraction is to recognize and extract mentions of **named entities** in text. In news documents, the core entity types are people, locations, and organizations; more recently, the task has been extended to include amounts of money, percentages, dates, and times. In item 8.37 (Figure 8.2), the named entities include: *The U.S. Army*, an organization; *Atlanta*, a location; and *May 14, 1864*, a date. Named entity recognition is also a key task in **biomedical natural language processing**, with entity types including proteins, DNA, RNA, and cell lines (e.g., Collier et al., 2000; Ohta et al., 2002). Figure 8.2 shows an example from the GENIA corpus of biomedical research ab-

- (8.37) *The U.S. Army captured Atlanta on May 14, 1864*  
 B-ORG I-ORG I-ORG O B-LOC O B-DATE I-DATE I-DATE I-DATE  
 (8.38) *Number of glucocorticoid receptors in lymphocytes and ...*  
 O O B-PROTEIN I-PROTEIN O B-CELLTYPE O ...

Figure 8.2: BIO notation for named entity recognition. Example (8.38) is drawn from the GENIA corpus of biomedical documents (Ohta et al., 2002).

4233 stracts.

4234 A standard approach to tagging named entity spans is to use discriminative sequence  
 4235 labeling methods such as conditional random fields. However, the named entity recogni-  
 4236 tion (NER) task would seem to be fundamentally different from sequence labeling tasks  
 4237 like part-of-speech tagging: rather than tagging each token, the goal is to recover *spans*  
 4238 of tokens, such as *The United States Army*.

4239 This is accomplished by the **BIO notation**, shown in Figure 8.2. Each token at the  
 4240 beginning of a name span is labeled with a B- prefix; each token within a name span is la-  
 4241 beled with an I- prefix. These prefixes are followed by a tag for the entity type, e.g. B-LOC  
 4242 for the beginning of a location, and I-PROTEIN for the inside of a protein name. Tokens  
 4243 that are not parts of name spans are labeled as O. From this representation, the entity  
 4244 name spans can be recovered unambiguously. This tagging scheme is also advantageous  
 4245 for learning: tokens at the beginning of name spans may have different properties than  
 4246 tokens within the name, and the learner can exploit this. This insight can be taken even  
 4247 further, with special labels for the last tokens of a name span, and for unique tokens in  
 4248 name spans, such as *Atlanta* in the example in Figure 8.2. This is called BILOU notation,  
 4249 and it can yield improvements in supervised named entity recognition (Ratinov and Roth,  
 4250 2009).

**Feature-based sequence labeling** Named entity recognition was one of the first applications of conditional random fields (McCallum and Li, 2003). The use of Viterbi decoding restricts the feature function  $f(\mathbf{w}, \mathbf{y})$  to be a sum of local features,  $\sum_m f(\mathbf{w}, y_m, y_{m-1}, m)$ , so that each feature can consider only local adjacent tags. Typical features include tag transitions, word features for  $w_m$  and its neighbors, character-level features for prefixes and suffixes, and “word shape” features for capitalization and other orthographic properties. As an example, base features for the word *Army* in the example in (8.37) include:

(CURR-WORD:*Army*, PREV-WORD:*U.S.*, NEXT-WORD:*captured*, PREFIX-1:*A-*,  
 PREFIX-2:*Ar-*, SUFFIX-1:*-y*, SUFFIX-2:*-my*, SHAPE:*Xxxx*)

4251 Another source of features is to use **gazetteers**: lists of known entity names. For example,  
 4252 the U.S. Social Security Administration provides a list of tens of thousands of given names

- (1) 日文 章魚 怎麼 說?  
 Japanese octopus how say  
 How to say octopus in Japanese?
- (2) 日 文章 魚 怎麼 說?  
 Japan essay fish how say

Figure 8.3: An example of tokenization ambiguity in Chinese (Sproat et al., 1996)

4253 — more than could be observed in any annotated corpus. Tokens or spans that match an  
 4254 entry in a gazetteer can receive special features; this provides a way to incorporate hand-  
 4255 crafted resources such as name lists in a learning-driven framework.

4256 **Neural sequence labeling for NER** Current research has emphasized neural sequence  
 4257 labeling, using similar LSTM models to those employed in part-of-speech tagging (Ham-  
 4258 merton, 2003; Huang et al., 2015; Lample et al., 2016). The bidirectional LSTM-CRF (Fig-  
 4259 ure 7.4 in § 7.6) does particularly well on this task, due to its ability to model tag-to-tag  
 4260 dependencies. However, Strubell et al. (2017) show that **convolutional neural networks**  
 4261 can be equally accurate, with significant improvement in speed due to the efficiency of  
 4262 implementing ConvNets on **graphics processing units (GPUs)**. The key innovation in  
 4263 this work was the use of **dilated convolution**, which is described in more detail in § 3.4.

## 4264 8.4 Tokenization

4265 A basic problem for text analysis, first discussed in § 4.3.1, is to break the text into a se-  
 4266 quence of discrete tokens. For alphabetic languages such as English, deterministic scripts  
 4267 suffice to achieve accurate tokenization. However, in logographic writing systems such  
 4268 as Chinese script, words are typically composed of a small number of characters, with-  
 4269 out intervening whitespace. The tokenization must be determined by the reader, with  
 4270 the potential for occasional ambiguity, as shown in Figure 8.3. One approach is to match  
 4271 character sequences against a known dictionary (e.g., Sproat et al., 1996), using additional  
 4272 statistical information about word frequency. However, no dictionary is completely com-  
 4273 prehensive, and dictionary-based approaches can struggle with such out-of-vocabulary  
 4274 words.

4275 Chinese tokenization has therefore been approached as a supervised sequence label-  
 4276 ing problem. Xue et al. (2003) train a logistic regression classifier to make independent  
 4277 segmentation decisions while moving a sliding window across the document. A set of  
 4278 rules is then used to convert these individual classification decisions into an overall tok-  
 4279 enization of the input. However, these individual decisions may be globally suboptimal,  
 4280 motivating a structure prediction approach. Peng et al. (2004) train a conditional random

4281 field to predict labels of START or NONSTART on each character. More recent work has  
 4282 employed neural network architectures. For example, Chen et al. (2015) use an LSTM-  
 4283 CRF architecture, as described in § 7.6: they construct a trellis, in which each tag is scored  
 4284 according to the hidden state of an LSTM, and tag-tag transitions are scored according  
 4285 to learned transition weights. The best-scoring segmentation is then computed by the  
 4286 Viterbi algorithm.

4287 8.5 Code switching

4288 Multilingual speakers and writers do not restrict themselves to a single language. **Code**  
4289 **switching** is the phenomenon of switching between languages in speech and text (Auer,  
4290 2013; Poplack, 1980). Written code switching has become more common in online social  
4291 media, as in the following extract from the website of Canadian President Justin Trudeau:<sup>7</sup>

- 4292 (8.39) *Although everything written on this site est disponible en anglais  
is available in English  
and in French, my personal videos seront bilingues  
will be bilingual*

4294 Accurately analyzing such texts requires first determining which languages are being  
4295 used. Furthermore, quantitative analysis of code switching can provide insights on the  
4296 languages themselves and their relative social positions.

Code switching can be viewed as a sequence labeling problem, where the goal is to label each token as a candidate switch point. In the example above, the words *est*, *and*, and *seront* would be labeled as switch points. Solorio and Liu (2008) detect English-Spanish switch points using a supervised classifier, with features that include the word, its part-of-speech in each language (according to a supervised part-of-speech tagger), and the probabilities of the word and part-of-speech in each language. Nguyen and Dogruöz (2013) apply a conditional random field to the problem of detecting code switching between Turkish and Dutch.

Code switching is a special case of the more general problem of word level language identification, which Barman et al. (2014) address in the context of trilingual code switching between Bengali, English, and Hindi. They further observe an even more challenging phenomenon: intra-word code switching, such as the use of English suffixes with Bengali roots. They therefore mark each token as either (1) belonging to one of the three languages; (2) a mix of multiple languages; (3) “universal” (e.g., symbols, numbers, emoticons); or (4) undefined.

<sup>7</sup>As quoted in <http://blogues.lapresse.ca/lagace/2008/09/08/justin-trudeau-really-parfait-bilingue/>, accessed August 21, 2017.

Speaker	Dialogue Act	Utterance
A	YES-NO-QUESTION	<i>So do you go college right now?</i>
A	ABANDONED	<i>Are yo-</i>
B	YES-ANSWER	<i>Yeah,</i>
B	STATEMENT	<i>It's my last year [laughter].</i>
A	DECLARATIVE-QUESTION	<i>You're a, so you're a senior now.</i>
B	YES-ANSWER	<i>Yeah,</i>
B	STATEMENT	<i>I'm working on my projects trying to graduate [laughter]</i>
A	APPRECIATION	<i>Oh, good for you.</i>
B	BACKCHANNEL	<i>Yeah.</i>

Figure 8.4: An example of dialogue act labeling (Stolcke et al., 2000)

## 4312 8.6 Dialogue acts

4313 The sequence labeling problems that we have discussed so far have been over sequences  
 4314 of word tokens or characters (in the case of tokenization). However, sequence labeling  
 4315 can also be performed over higher-level units, such as **utterances**. **Dialogue acts** are la-  
 4316 bels over utterances in a dialogue, corresponding roughly to the speaker’s intention —  
 4317 the utterance’s **illocutionary force** (Austin, 1962). For example, an utterance may state a  
 4318 proposition (*it is not down on any map*), pose a question (*shall we keep chasing this murderous*  
 4319 *fish?*), or provide a response (*aye aye!*). Stolcke et al. (2000) describe how a set of 42 dia-  
 4320 logue acts were annotated for the 1,155 conversations in the Switchboard corpus (Godfrey  
 4321 et al., 1992).<sup>8</sup>

4322 An example is shown in Figure 8.4. The annotation is performed over UTTERANCES,  
 4323 with the possibility of multiple utterances per **conversational turn** (in cases such as inter-  
 4324 ruptions, an utterance may split over multiple turns). Some utterances are clauses (e.g., *So*  
 4325 *do you go to college right now?*), while others are single words (e.g., *yeah*). Stolcke et al. (2000)  
 4326 report that hidden Markov models (HMMs) achieve 96% accuracy on supervised utter-  
 4327 ance segmentation. The labels themselves reflect the conversational goals of the speaker:  
 4328 the utterance *yeah* functions as an answer in response to the question *you’re a senior now*,  
 4329 but in the final line of the excerpt, it is a **backchannel** (demonstrating comprehension).

4330 For task of dialogue act labeling, Stolcke et al. (2000) apply a hidden Markov model.  
 4331 The probability  $p(w_m | y_m)$  must generate the entire sequence of words in the utterance,  
 4332 and it is modeled as a trigram language model (§ 6.1). Stolcke et al. (2000) also account  
 4333 for acoustic features, which capture the **prosody** of each utterance — for example, tonal  
 4334 and rhythmic properties of speech, which can be used to distinguish dialogue acts such

<sup>8</sup>Dialogue act modeling is not restricted to speech; it is relevant in any interactive conversation. For example, Jeong et al. (2009) annotate a more limited set of **speech acts** in a corpus of emails and online forums.

4335 as questions and answers. These features are handled with an additional emission distribution,  
 4336  $p(a_m | y_m)$ , which is modeled with a probabilistic decision tree (Murphy, 2012).  
 4337 While acoustic features yield small improvements overall, they play an important role in  
 4338 distinguish questions from statements, and agreements from backchannels.

4339 Recurrent neural architectures for dialogue act labeling have been proposed by Kalch-  
 4340 brenner and Blunsom (2013) and Ji et al. (2016), with strong empirical results. Both models  
 4341 are recurrent at the utterance level, so that each complete utterance updates a hidden state.  
 4342 The recurrent-convolutional network of Kalchbrenner and Blunsom (2013) uses convolu-  
 4343 tion to obtain a representation of each individual utterance, while Ji et al. (2016) use a  
 4344 second level of recurrence, over individual words. This enables their method to also func-  
 4345 tion as a language model, giving probabilities over sequences of words in a document.

## 4346 Exercises

4347 1. Using the Universal Dependencies part-of-speech tags, annotate the following sen-  
 4348 tences. You may examine the UD tagging guidelines. Tokenization is shown with  
 4349 whitespace. Don't forget about punctuation.

4350 (8.40) I try all things , I achieve what I can .

4351 (8.41) It was that accursed white whale that razed me .

4352 (8.42) Better to sleep with a sober cannibal , than a drunk Christian .

4353 (8.43) Be it what it will , I 'll go to it laughing .

4354 2. Select three short sentences from a recent news article, and annotate them for UD  
 4355 part-of-speech tags. Ask a friend to annotate the same three sentences without look-  
 4356 ing at your annotations. Compute the rate of agreement, using the Kappa metric  
 4357 defined in § 4.5.2.1. Then work together to resolve any disagreements.

4358 3. Choose one of the following morphosyntactic attributes: MOOD, TENSE, VOICE. Re-  
 4359 search the definition of this attribute on the universal dependencies website, <http://universaldependencies.org/u/feat/index.html>. Returning to the ex-  
 4360 amples in the first exercise, annotate all verbs for your chosen attribute. It may be  
 4361 helpful to consult examples from an English-language universal dependencies cor-  
 4362 pus, available at [https://github.com/UniversalDependencies/UD\\_English-EWT/](https://github.com/UniversalDependencies/UD_English-EWT/)  
 4364 tree/master.

4365 4. Download a dataset annotated for universal dependencies, such as the English Tree-  
 4366 bank at [https://github.com/UniversalDependencies/UD\\_English-EWT/](https://github.com/UniversalDependencies/UD_English-EWT/)  
 4367 tree/master. This corpus is already segmented into training, development, and  
 4368 test data.

- 4369       a) First, train a logistic regression or SVM classifier using character suffixes: char-  
4370           acter n-grams up to length 4. Compute the recall, precision, and *F*-MEASURE  
4371           on the development data.
- 4372       b) Next, augment your classifier using the same character suffixes of the preced-  
4373           ing and succeeding tokens. Again, evaluate your classifier on heldout data.
- 4374       c) Optionally, train a Viterbi-based sequence labeling model, using a toolkit such  
4375           as CRFSuite (<http://www.chokkan.org/software/crfsuite/>) or your  
4376           own Viterbi implementation. This is more likely to be helpful for attributes  
4377           in which agreement is required between adjacent words. For example, in Ro-  
4378           mance languages, determiners, nouns, and adjectives must agree in gender and  
4379           number.
- 4380     5. Provide BIO-style annotation of the named entities (person, place, organization,  
4381           date, or product) in the following expressions:
- 4382       (8.44) The third mate was Flask, a native of Tisbury, in Martha's Vineyard.
- 4383       (8.45) Its official Nintendo announced today that they Will release the Nintendo  
4384           3DS in north America march 27 (Ritter et al., 2011).
- 4385       (8.46) Jessica Reif, a media analyst at Merrill Lynch & Co., said, "If they can get  
4386           up and running with exclusive programming within six months, it doesn't  
4387           set the venture back that far."<sup>9</sup>
- 4388     6. Run the examples above through the online version of a named entity recogni-  
4389           tion tagger, such as the Allen NLP system here: <http://demo.allennlp.org/named->  
4390           entity-recognition. Do the predicted tags match your annotations?
- 4391     7. Build a whitespace tokenizer for English:
- 4392       a) Using the NLTK library, download the complete text to the novel *Alice in Won-*  
4393           *derland* (Carroll, 1865). Hold out the final 1000 words as a test set.
- 4394       b) Label each alphanumeric character as a segmentation point,  $y_m = 1$  if  $m$  is  
4395           the final character of a token. Label every other character as  $y_m = 0$ . Then  
4396           concatenate all the tokens in the training and test sets. Make sure that the num-  
4397           ber of labels  $\{y_m\}_{m=1}^M$  is identical to the number of characters  $\{c_m\}_{m=1}^M$  in your  
4398           concatenated datasets.
- 4399       c) Train a logistic regression classifier to predict  $y_m$ , using the surrounding char-  
4400           acters  $c_{m-5:m+5}$  as features. After training the classifier, run it on the test set,  
4401           using the predicted segmentation points to re-tokenize the text.

---

<sup>9</sup>From the Message Understanding Conference (MUC-7) dataset (Chinchor and Robinson, 1997).

- 4402       d) Compute the per-character segmentation accuracy on the test set. You should  
4403       be able to get at least 88% accuracy.  
4404       e) Print out a sample of segmented text from the test set, e.g.

4405       Thereareno mice in the air , I ' m afraid , but y oumight cat  
4406       chabat , and that ' s very like a mouse , youknow . But  
4407       docatseat bats , I wonder ?'

- 4408       8. Perform the following extensions to the previous problem:

- 4409       a) Train a conditional random field sequence labeler, by incorporating the tag bi-  
4410       grams  $(y_{m-1}, y_m)$  as additional features. You may use a structured prediction li-  
4411       brary such as CRFSuite (<http://www.chokkan.org/software/crfsuite/>),  
4412       or you may want to implement Viterbi yourself. Compare the accuracy with  
4413       your classification-based approach.
- 4414       b) Optionally, compute the token-level performance. Treating the original tok-  
4415       enization as ground truth, compute the number of true positives (tokens that  
4416       are in both the ground truth and predicted tokenization), false positives (tokens  
4417       that are in the predicted tokenization but not the ground truth), and false neg-  
4418       atives (tokens that are in the ground truth but not the predicted tokenization).  
4419       Compute the F-measure.  
4420       Hint: to match predicted and ground truth tokens, add “anchors” for the start  
4421       character of each token. The number of true positives is then the size of the  
4422       intersection of the sets of predicted and ground truth tokens.
- 4423       c) Apply the same methodology in a more practical setting: tokenization of Chi-  
4424       nese, which is written without whitespace. You can find annotated datasets at  
4425       <http://alias-i.com/lingpipe/demos/tutorial/chineseTokens/read-me.html>.

4427 **Chapter 9**

4428 **Formal language theory**

4429 We have now seen methods for learning to label individual words, vectors of word counts,  
4430 and sequences of words; we will soon proceed to more complex structural transfor-  
4431 mations. Most of these techniques could apply to counts or sequences from any discrete vo-  
4432 cabulary; there is nothing fundamentally linguistic about, say, a hidden Markov model.  
4433 This raises a basic question that this text has not yet considered: what is a language?

4434 This chapter will take the perspective of **formal language theory**, in which a language  
4435 is defined as a set of **strings**, each of which is a sequence of elements from a finite alphabet.  
4436 For interesting languages, there are an infinite number of strings that are in the language,  
4437 and an infinite number of strings that are not. For example:

- 4438 • the set of all even-length sequences from the alphabet  $\{a, b\}$ , e.g.,  $\{\emptyset, aa, ab, ba, bb, aaaa, aaab, \dots\}$ ;
- 4439 • the set of all sequences from the alphabet  $\{a, b\}$  that contain *aaa* as a substring, e.g.,  
4440  $\{aaa, aaaa, baaa, aaab, \dots\}$ ;
- 4441 • the set of all sequences of English words (drawn from a finite dictionary) that con-  
4442 tain at least one verb (a finite subset of the dictionary);
- 4443 • the `python` programming language.

4444 Formal language theory defines classes of languages and their computational prop-  
4445 erties. Of particular interest is the computational complexity of solving the **membership**  
4446 **problem** — determining whether a string is in a language. The chapter will focus on  
4447 three classes of formal languages: regular, context-free, and “mildly” context-sensitive  
4448 languages.

4449 A key insight of 20th century linguistics is that formal language theory can be usefully  
4450 applied to natural languages such as English, by designing formal languages that cap-  
4451 ture as many properties of the natural language as possible. For many such formalisms, a  
4452 useful linguistic analysis comes as a byproduct of solving the membership problem. The

4453 membership problem can be generalized to the problems of *scoring* strings for their ac-  
 4454 ceptability (as in language modeling), and of **transducing** one string into another (as in  
 4455 translation).

## 4456 9.1 Regular languages

4457 Sooner or later, most computer scientists will write a **regular expression**. If you have,  
 4458 then you have defined a **regular language**, which is any language that can be defined by  
 4459 a regular expression. Formally, a regular expression can include the following elements:

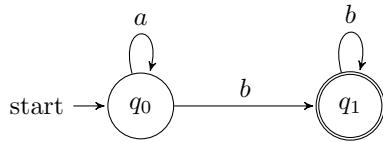
- 4460 • A **literal character** drawn from some finite alphabet  $\Sigma$ .
- 4461 • The **empty string**  $\epsilon$ .
- 4462 • The concatenation of two regular expressions  $RS$ , where  $R$  and  $S$  are both regular  
 4463 expressions. The resulting expression accepts any string that can be decomposed  
 4464  $x = yz$ , where  $y$  is accepted by  $R$  and  $z$  is accepted by  $S$ .
- 4465 • The alternation  $R \mid S$ , where  $R$  and  $S$  are both regular expressions. The resulting  
 4466 expression accepts a string  $x$  if it is accepted by  $R$  or it is accepted by  $S$ .
- 4467 • The **Kleene star**  $R^*$ , which accepts any string  $x$  that can be decomposed into a se-  
 4468 quence of strings which are all accepted by  $R$ .
- 4469 • Parenthesization ( $(R)$ ), which is used to limit the scope of the concatenation, alterna-  
 4470 tion, and Kleene star operators.

4471 Here are some example regular expressions:

- 4472 • The set of all even length strings on the alphabet  $\{a, b\}$ :  $((aa)|(ab)|(ba)|(bb))^*$
- 4473 • The set of all sequences of the alphabet  $\{a, b\}$  that contain  $aaa$  as a substring:  $(a|b)^*aaa(a|b)^*$
- 4474 • The set of all sequences of English words that contain at least one verb:  $W^*VW^*$ ,  
 4475 where  $W$  is an alternation between all words in the dictionary, and  $V$  is an alterna-  
 4476 tion between all verbs ( $V \subseteq W$ ).

4477 This list does not include a regular expression for the Python programming language,  
 4478 because this language is not regular — there is no regular expression that can capture its  
 4479 syntax. We will discuss why towards the end of this section.

4480 Regular languages are **closed** under union, intersection, and concatenation. This means,  
 4481 for example, that if two languages  $L_1$  and  $L_2$  are regular, then so are the languages  $L_1 \cup L_2$ ,  
 4482  $L_1 \cap L_2$ , and the language of strings that can be decomposed as  $s = tu$ , with  $s \in L_1$  and  
 4483  $t \in L_2$ . Regular languages are also closed under negation: if  $L$  is regular, then so is the  
 4484 language  $\bar{L} = \{s \notin L\}$ .

Figure 9.1: State diagram for the finite state acceptor  $M_1$ .4485 **9.1.1 Finite state acceptors**

4486 A regular expression defines a regular language, but does not give an algorithm for de-  
 4487 termining whether a string is in the language that it defines. **Finite state automata** are  
 4488 theoretical models of computation on regular languages, which involve transitions be-  
 4489 tween a finite number of states. The most basic type of finite state automaton is the **finite**  
 4490 **state acceptor (FSA)**, which describes the computation involved in testing if a string is  
 4491 a member of a language. Formally, a finite state acceptor is a tuple  $M = (Q, \Sigma, q_0, F, \delta)$ ,  
 4492 consisting of:

- 4493 • a finite alphabet  $\Sigma$  of input symbols;
- 4494 • a finite set of states  $Q = \{q_0, q_1, \dots, q_n\}$ ;
- 4495 • a start state  $q_0 \in Q$ ;
- 4496 • a set of final states  $F \subseteq Q$ ;
- 4497 • a transition function  $\delta : Q \times (\Sigma \cup \{\epsilon\}) \rightarrow 2^Q$ . The transition function maps from a  
 4498 state and an input symbol (or empty string  $\epsilon$ ) to a *set* of possible resulting states.

4499 A **path** in  $M$  is a sequence of transitions,  $\pi = t_1, t_2, \dots, t_N$ , where each  $t_i$  traverses an  
 4500 arc in the transition function  $\delta$ . The finite state acceptor  $M$  accepts a string  $\omega$  if there is  
 4501 a **accepting path**, in which the initial transition  $t_1$  begins at the start state  $q_0$ , the final  
 4502 transition  $t_N$  terminates in a final state in  $Q$ , and the entire input  $\omega$  is consumed.

4503 **9.1.1.1 Example**

Consider the following FSA,  $M_1$ .

$$\Sigma = \{a, b\} \quad [9.1]$$

$$Q = \{q_0, q_1\} \quad [9.2]$$

$$F = \{q_1\} \quad [9.3]$$

$$\delta = \{(q_0, a) \rightarrow q_0, (q_0, b) \rightarrow q_1, (q_1, b) \rightarrow q_1\}. \quad [9.4]$$

4504 This FSA defines a language over an alphabet of two symbols,  $a$  and  $b$ . The transition  
 4505 function  $\delta$  is written as a set of arcs:  $(q_0, a) \rightarrow q_0$  says that if the machine is in state

4506  $q_0$  and reads symbol  $a$ , it stays in  $q_0$ . Figure 9.1 provides a graphical representation of  
 4507  $M_1$ . Because each pair of initial state and symbol has at most one resulting state,  $M_1$  is  
 4508 **deterministic**: each string  $\omega$  induces at most one accepting path. Note that there are no  
 4509 transitions for the symbol  $a$  in state  $q_1$ ; if  $a$  is encountered in  $q_1$ , then the acceptor is stuck,  
 4510 and the input string is rejected.

4511 What strings does  $M_1$  accept? The start state is  $q_0$ , and we have to get to  $q_1$ , since this  
 4512 is the only final state. Any number of  $a$  symbols can be consumed in  $q_0$ , but a  $b$  symbol is  
 4513 required to transition to  $q_1$ . Once there, any number of  $b$  symbols can be consumed, but  
 4514 an  $a$  symbol cannot. So the regular expression corresponding to the language defined by  
 4515  $M_1$  is  $a^*bb^*$ .

#### 4516 9.1.1.2 Computational properties of finite state acceptors

4517 The key computational question for finite state acceptors is: how fast can we determine  
 4518 whether a string is accepted? For deterministic FSAs, this computation can be performed  
 4519 by Dijkstra's algorithm, with time complexity  $\mathcal{O}(V \log V + E)$ , where  $V$  is the number of  
 4520 vertices in the FSA, and  $E$  is the number of edges (Cormen et al., 2009). Non-deterministic  
 4521 FSAs (NFSAs) can include multiple transitions from a given symbol and state. Any NSFA  
 4522 can be converted into a deterministic FSA, but the resulting automaton may have a num-  
 4523 ber of states that is exponential in the number of size of the original NFSFA (Mohri et al.,  
 4524 2002).

#### 4525 9.1.2 Morphology as a regular language

4526 Many words have internal structure, such as prefixes and suffixes that shape their mean-  
 4527 ing. The study of word-internal structure is the domain of **morphology**, of which there  
 4528 are two main types:

- 4529   • **Derivational morphology** describes the use of affixes to convert a word from one  
 4530 grammatical category to another (e.g., from the noun *grace* to the adjective *graceful*),  
 4531 or to change the meaning of the word (e.g., from *grace* to *disgrace*).
- 4532   • **Inflectional morphology** describes the addition of details such as gender, number,  
 4533 person, and tense (e.g., the *-ed* suffix for past tense in English).

4534 Morphology is a rich topic in linguistics, deserving of a course in its own right.<sup>1</sup> The  
 4535 focus here will be on the use of finite state automata for morphological analysis. The

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<sup>1</sup>A good starting point would be a chapter from a linguistics textbook (e.g., Akmajian et al., 2010; Bender, 2013). A key simplification in this chapter is the focus on affixes at the sole method of derivation and inflection. English makes use of affixes, but also incorporates **apophony**, such as the inflection of *foot* to *feet*. Semitic languages like Arabic and Hebrew feature a template-based system of morphology, in which roots are triples of consonants (e.g., *ktb*), and words are created by adding vowels: *kataba* (Arabic: he wrote), *kutub* (books), *maktab* (desk). For more detail on morphology, see texts from Haspelmath and Sims (2013) and Lieber (2015).

4536 current section deals with derivational morphology; inflectional morphology is discussed  
4537 in § 9.1.4.3.

4538 Suppose that we want to write a program that accepts only those words that are con-  
4539 structed in accordance with the rules of English derivational morphology:

- 4540 (9.1) grace, graceful, gracefully, \*gracelyful  
4541 (9.2) disgrace, \*ungrace, disgraceful, disgracefully  
4542 (9.3) allure, \*allureful, alluring, alluringly  
4543 (9.4) fairness, unfair, \*disfair, fairly

4544 (Recall that the asterisk indicates that a linguistic example is judged unacceptable by flu-  
4545 ent speakers of a language.) These examples cover only a tiny corner of English deriva-  
4546 tional morphology, but a number of things stand out. The suffix *-ful* converts the nouns  
4547 *grace* and *disgrace* into adjectives, and the suffix *-ly* converts adjectives into adverbs. These  
4548 suffixes must be applied in the correct order, as shown by the unacceptability of *\*grace-*  
4549 *lyful*. The *-ful* suffix works for only some words, as shown by the use of *alluring* as the  
4550 adjectival form of *allure*. Other changes are made with prefixes, such as the derivation  
4551 of *disgrace* from *grace*, which roughly corresponds to a negation; however, *fair* is negated  
4552 with the *un-* prefix instead. Finally, while the first three examples suggest that the direc-  
4553 tion of derivation is noun → adjective → adverb, the example of *fair* suggests that the  
4554 adjective can also be the base form, with the *-ness* suffix performing the conversion to a  
4555 noun.

4556 Can we build a computer program that accepts only well-formed English words, and  
4557 rejects all others? This might at first seem trivial to solve with a brute-force attack: simply  
4558 make a dictionary of all valid English words. But such an approach fails to account for  
4559 morphological **productivity** — the applicability of existing morphological rules to new  
4560 words and names, such as *Trump* to *Trumpy* and *Trumpkin*, and *Clinton* to *Clintonian* and  
4561 *Clintonite*. We need an approach that represents morphological rules explicitly, and for  
4562 this we will try a finite state acceptor.

4563 The dictionary approach can be implemented as a finite state acceptor, with the vo-  
4564 cabulary  $\Sigma$  equal to the vocabulary of English, and a transition from the start state to the  
4565 accepting state for each word. But this would of course fail to generalize beyond the origi-  
4566 nal vocabulary, and would not capture anything about the **morphotactic** rules that govern  
4567 derivations from new words. The first step towards a more general approach is shown in  
4568 Figure 9.2, which is the state diagram for a finite state acceptor in which the vocabulary  
4569 consists of **morphemes**, which include **stems** (e.g., *grace*, *allure*) and **affixes** (e.g., *dis-*, *-ing*,  
4570 *-ly*). This finite state acceptor consists of a set of paths leading away from the start state,  
4571 with derivational affixes added along the path. Except for  $q_{\text{neg}}$ , the states on these paths  
4572 are all final, so the FSA will accept *disgrace*, *disgraceful*, and *disgracefully*, but not *dis-*.

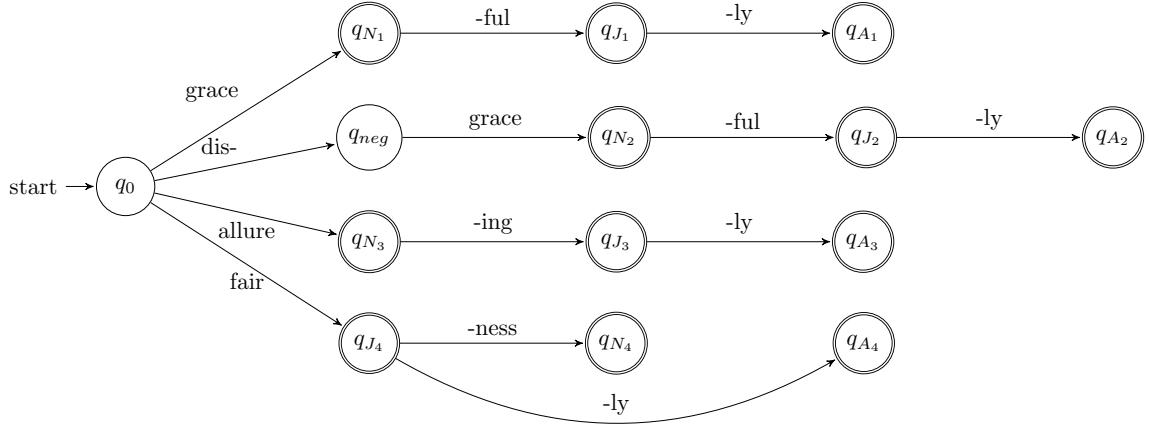


Figure 9.2: A finite state acceptor for a fragment of English derivational morphology. Each path represents possible derivations from a single root form.

4573     This FSA can be **minimized** to the form shown in Figure 9.3, which makes the general-  
 4574     ity of the finite state approach more apparent. For example, the transition from  $q_0$  to  
 4575      $q_{J_2}$  can be made to accept not only *fair* but any single-morpheme (**monomorphemic**) ad-  
 4576     jective that takes *-ness* and *-ly* as suffixes. In this way, the finite state acceptor can easily  
 4577     be extended: as new word stems are added to the vocabulary, their derived forms will be  
 4578     accepted automatically. Of course, this FSA would still need to be extended considerably  
 4579     to cover even this small fragment of English morphology. As shown by cases like *music*  
 4580     → *musical*, *athlete* → *athletic*, English includes several classes of nouns, each with its own  
 4581     rules for derivation.

4582     The FSAs shown in Figure 9.2 and 9.3 accept *allureing*, not *alluring*. This reflects a dis-  
 4583     tinction between morphology — the question of which morphemes to use, and in what  
 4584     order — and **orthography** — the question of how the morphemes are rendered in written  
 4585     language. Just as orthography requires dropping the *e* preceding the *-ing* suffix, **phonol-**  
 4586     **ogy** imposes a related set of constraints on how words are rendered in speech. As we will  
 4587     see soon, these issues are handled through **finite state transducers**, which are finite state  
 4588     automata that take inputs and produce outputs.

### 4589     9.1.3 Weighted finite state acceptors

4590     According to the FSA treatment of morphology, every word is either in or out of the lan-  
 4591     guage, with no wiggle room. Perhaps you agree that *musicky* and *fishful* are not valid  
 4592     English words; but if forced to choose, you probably find *a fishful stew* or *a musicky trib-*  
 4593     *ute* preferable to *behaving disgracelyful*. Rather than asking whether a word is acceptable,  
 4594     we might like to ask how acceptable it is. Aronoff (1976, page 36) puts it another way:

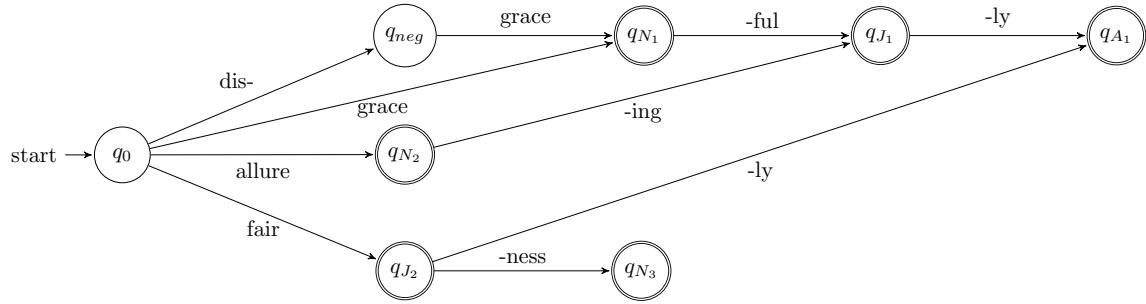


Figure 9.3: Minimization of the finite state acceptor shown in Figure 9.2.

4595 “Though many things are possible in morphology, some are more possible than others.”  
 4596 But finite state acceptors give no way to express preferences among technically valid  
 4597 choices.

4598 **Weighted finite state acceptors (WFSAs)** are generalizations of FSAs, in which each  
 4599 accepting path is assigned a score, computed from the transitions, the initial state, and the  
 4600 final state. Formally, a weighted finite state acceptor  $M = (Q, \Sigma, \lambda, \rho, \delta)$  consists of:

- 4601 • a finite set of states  $Q = \{q_0, q_1, \dots, q_n\}$ ;
- 4602 • a finite alphabet  $\Sigma$  of input symbols;
- 4603 • an initial weight function,  $\lambda : Q \rightarrow \mathbb{R}$ ;
- 4604 • a final weight function  $\rho : Q \rightarrow \mathbb{R}$ ;
- 4605 • a transition function  $\delta : Q \times \Sigma \times Q \rightarrow \mathbb{R}$ .

4606 WFSAs depart from the FSA formalism in three ways: every state can be an initial  
 4607 state, with score  $\lambda(q)$ ; every state can be an accepting state, with score  $\rho(q)$ ; transitions are  
 4608 possible between any pair of states on any input, with a score  $\delta(q_i, \omega, q_j)$ . Nonetheless,  
 4609 FSAs can be viewed as a special case: for any FSA  $M$  we can build an equivalent WFSA  
 4610 by setting  $\lambda(q) = \infty$  for all  $q \neq q_0$ ,  $\rho(q) = \infty$  for all  $q \notin F$ , and  $\delta(q_i, \omega, q_j) = \infty$  for all  
 4611 transitions  $\{(q_1, \omega) \rightarrow q_2\}$  that are not permitted by the transition function of  $M$ .

4612 The total score for any path  $\pi = t_1, t_2, \dots, t_N$  is equal to the sum of these scores,

$$d(\pi) = \lambda(\text{from-state}(t_1)) + \sum_n^N \delta(t_n) + \rho(\text{to-state}(t_N)). \quad [9.5]$$

4613 A **shortest-path algorithm** is used to find the minimum-cost path through a WFSA for  
 4614 string  $\omega$ , with time complexity  $\mathcal{O}(E + V \log V)$ , where  $E$  is the number of edges and  $V$  is  
 4615 the number of vertices (Cormen et al., 2009).<sup>2</sup>

<sup>2</sup>Shortest-path algorithms find the path with the minimum cost. In many cases, the path weights are log

4616 **9.1.3.1 N-gram language models as WFSAs**

4617 In **n-gram language models** (see § 6.1), the probability of a sequence of tokens  $w_1, w_2, \dots, w_M$   
 4618 is modeled as,

$$p(w_1, \dots, w_M) \approx \prod_{m=1}^M p_n(w_m | w_{m-1}, \dots, w_{m-n+1}). \quad [9.6]$$

The log probability under an  $n$ -gram language model can be modeled in a WFSA. First consider a unigram language model. We need only a single state  $q_0$ , with transition scores  $\delta(q_0, \omega, q_0) = \log p_1(\omega)$ . The initial and final scores can be set to zero. Then the path score for  $w_1, w_2, \dots, w_M$  is equal to,

$$0 + \sum_m^M \delta(q_0, w_m, q_0) + 0 = \sum_m^M \log p_1(w_m). \quad [9.7]$$

For an  $n$ -gram language model with  $n > 1$ , we need probabilities that condition on the past history. For example, in a bigram language model, the transition weights must represent  $\log p_2(w_m | w_{m-1})$ . The transition scoring function must somehow “remember” the previous word or words. This can be done by adding more states: to model the bigram probability  $p_2(w_m | w_{m-1})$ , we need a state for every possible  $w_{m-1}$  — a total of  $V$  states. The construction indexes each state  $q_i$  by a context event  $w_{m-1} = i$ . The weights are then assigned as follows:

$$\begin{aligned} \delta(q_i, \omega, q_j) &= \begin{cases} \log \Pr(w_m = j | w_{m-1} = i), & \omega = j \\ -\infty, & \omega \neq j \end{cases} \\ \lambda(q_i) &= \log \Pr(w_1 = i | w_0 = \square) \\ \rho(q_i) &= \log \Pr(w_{M+1} = \blacksquare | w_M = i). \end{aligned}$$

4619 The transition function is designed to ensure that the context is recorded accurately:  
 4620 we can move to state  $j$  on input  $\omega$  only if  $\omega = j$ ; otherwise, transitioning to state  $j$  is  
 4621 forbidden by the weight of  $-\infty$ . The initial weight function  $\lambda(q_i)$  is the log probability of  
 4622 receiving  $i$  as the first token, and the final weight function  $\rho(q_i)$  is the log probability of  
 4623 receiving an “end-of-string” token after observing  $w_M = i$ .

4624 **9.1.3.2 \*Semiring weighted finite state acceptors**

4625 The  $n$ -gram language model WFSA is deterministic: each input has exactly one accepting  
 4626 path, for which the WFSA computes a score. In non-deterministic WFSAs, a given input

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probabilities, so we want the path with the maximum score, which can be accomplished by making each local score into a *negative* log-probability. The remainder of this section will refer to **best-path algorithms**, which are assumed to “do the right thing.”

4627 may have multiple accepting paths. In some applications, the score for the input is ag-  
 4628 gregated across all such paths. Such aggregate scores can be computed by generalizing  
 4629 WFSAs with **semiring notation**, first introduced in § 7.7.3.

4630 Let  $d(\pi)$  represent the total score for path  $\pi = t_1, t_2, \dots, t_N$ , which is computed as,

$$d(\pi) = \lambda(\text{from-state}(t_1)) \otimes \delta(t_1) \otimes \delta(t_2) \otimes \dots \otimes \delta(t_N) \otimes \rho(\text{to-state}(t_N)). \quad [9.8]$$

4631 This is a generalization of Equation 9.5 to semiring notation, using the semiring multipli-  
 4632 cation operator  $\otimes$  in place of addition.

4633 Now let  $s(\omega)$  represent the total score for all paths  $\Pi(\omega)$  that consume input  $\omega$ ,

$$s(\omega) = \bigoplus_{\pi \in \Pi(\omega)} d(\pi). \quad [9.9]$$

4634 Here, semiring addition ( $\oplus$ ) is used to combine the scores of multiple paths.

4635 The generalization to semirings covers a number of useful special cases. In the log-  
 4636 probability semiring, multiplication is defined as  $\log p(x) \otimes \log p(y) = \log p(x) + \log p(y)$ ,  
 4637 and addition is defined as  $\log p(x) \oplus \log p(y) = \log(p(x) + p(y))$ . Thus,  $s(\omega)$  represents  
 4638 the log-probability of accepting input  $\omega$ , marginalizing over all paths  $\pi \in \Pi(\omega)$ . In the  
 4639 **boolean semiring**, the  $\otimes$  operator is logical conjunction, and the  $\oplus$  operator is logical  
 4640 disjunction. This reduces to the special case of unweighted finite state acceptors, where  
 4641 the score  $s(\omega)$  is a boolean indicating whether there exists any accepting path for  $\omega$ . In  
 4642 the **tropical semiring**, the  $\oplus$  operator is a maximum, so the resulting score is the score of  
 4643 the best-scoring path through the WFSAs. The OpenFST toolkit uses semirings and poly-  
 4644 morphism to implement general algorithms for weighted finite state automata (Allauzen  
 4645 et al., 2007).

### 4646 9.1.3.3 \*Interpolated $n$ -gram language models

4647 Recall from § 6.2.3 that an **interpolated  $n$ -gram language model** combines the probabili-  
 4648 ties from multiple  $n$ -gram models. For example, an interpolated bigram language model  
 4649 computes probability,

$$\hat{p}(w_m | w_{m-1}) = \lambda_1 p_1(w_m) + \lambda_2 p_2(w_m | w_{m-1}), \quad [9.10]$$

4650 with  $\hat{p}$  indicating the interpolated probability,  $p_2$  indicating the bigram probability, and  
 4651  $p_1$  indicating the unigram probability. We set  $\lambda_2 = (1 - \lambda_1)$  so that the probabilities sum  
 4652 to one.

4653 Interpolated bigram language models can be implemented using a non-deterministic  
 4654 WFSAs (Knight and May, 2009). The basic idea is shown in Figure 9.4. In an interpolated  
 4655 bigram language model, there is one state for each element in the vocabulary — in this

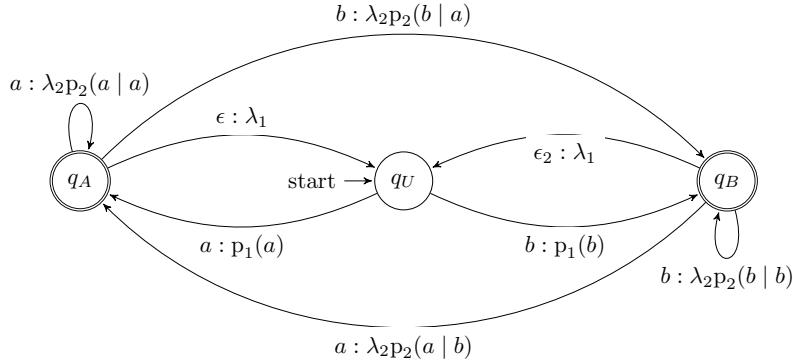


Figure 9.4: WFSA implementing an interpolated bigram/unigram language model, on the alphabet  $\Sigma = \{a, b\}$ . For simplicity, the WFSA is constrained to force the first token to be generated from the unigram model, and does not model the emission of the end-of-sequence token.

4656 case, the states  $q_A$  and  $q_B$  — which capture the contextual conditioning in the bigram  
 4657 probabilities. To model unigram probabilities, there is an additional state  $q_U$ , which “for-  
 4658 gets” the context. Transitions out of  $q_U$  involve unigram probabilities,  $p_1(a)$  and  $p_2(b)$ ;  
 4659 transitions into  $q_U$  emit the empty symbol  $\epsilon$ , and have probability  $\lambda_1$ , reflecting the inter-  
 4660 polation weight for the unigram model. The interpolation weight for the bigram model is  
 4661 included in the weight of the transition  $q_A \rightarrow q_B$ .

4662 The epsilon transitions into  $q_U$  make this WFSA non-deterministic. Consider the score  
 4663 for the sequence  $(a, b, b)$ . The initial state is  $q_U$ , so the symbol  $a$  is generated with score  
 4664  $p_1(a)$ <sup>3</sup> Next, we can generate  $b$  from the unigram model by taking the transition  $q_A \rightarrow q_B$ ,  
 4665 with score  $\lambda_2 p_2(b | a)$ . Alternatively, we can take a transition back to  $q_U$  with score  $\lambda_1$ ,  
 4666 and then emit  $b$  from the unigram model with score  $p_1(b)$ . To generate the final  $b$  token,  
 4667 we face the same choice: emit it directly from the self-transition to  $q_B$ , or transition to  $q_U$   
 4668 first.

The total score for the sequence  $(a, b, b)$  is the semiring sum over all accepting paths,

$$\begin{aligned}
 s(a, b, b) &= (p_1(a) \otimes \lambda_2 p_2(b | a) \otimes \lambda_2 p_2(b | b)) \\
 &\oplus (p_1(a) \otimes \lambda_1 \otimes p_1(b) \otimes \lambda_2 p_2(b | b)) \\
 &\oplus (p_1(a) \otimes \lambda_2 p_2(b | a) \otimes p_1(b) \otimes p_1(b)) \\
 &\oplus (p_1(a) \otimes \lambda_1 \otimes p_1(b) \otimes p_1(b) \otimes p_1(b)). \tag{[9.11]}
 \end{aligned}$$

4669 Each line in Equation 9.11 represents the probability of a specific path through the WFSA.  
 4670 In the probability semiring,  $\otimes$  is multiplication, so that each path is the product of each

<sup>3</sup>We could model the sequence-initial bigram probability  $p_2(a | \square)$ , but for simplicity the WFSA does not admit this possibility, which would require another state.

4671 transition weight, which are themselves probabilities. The  $\oplus$  operator is addition, so that  
 4672 the total score is the sum of the scores (probabilities) for each path. This corresponds to  
 4673 the probability under the interpolated bigram language model.

4674 **9.1.4 Finite state transducers**

4675 Finite state acceptors can determine whether a string is in a regular language, and weighted  
 4676 finite state acceptors can compute a score for every string over a given alphabet. **Finite**  
 4677 **state transducers** (FSTs) extend the formalism further, by adding an output symbol to each  
 4678 transition. Formally, a finite state transducer is a tuple  $T = (Q, \Sigma, \Omega, \lambda, \rho, \delta)$ , with  $\Omega$  repre-  
 4679 senting an output vocabulary and the transition function  $\delta : Q \times (\Sigma \cup \epsilon) \times (\Omega \cup \epsilon) \times Q \rightarrow \mathbb{R}$   
 4680 mapping from states, input symbols, and output symbols to states. The remaining ele-  
 4681 ments ( $Q, \Sigma, \lambda, \rho$ ) are identical to their definition in weighted finite state acceptors (§ 9.1.3).  
 4682 Thus, each path through the FST  $T$  transduces the input string into an output.

4683 **9.1.4.1 String edit distance**

The **edit distance** between two strings  $s$  and  $t$  is a measure of how many operations are required to transform one string into another. There are several ways to compute edit distance, but one of the most popular is the **Levenshtein edit distance**, which counts the minimum number of insertions, deletions, and substitutions. This can be computed by a one-state weighted finite state transducer, in which the input and output alphabets are identical. For simplicity, consider the alphabet  $\Sigma = \Omega = \{a, b\}$ . The edit distance can be computed by a one-state transducer with the following transitions,

$$\delta(q, a, a, q) = \delta(q, b, b, q) = 0 \quad [9.12]$$

$$\delta(q, a, b, q) = \delta(q, b, a, q) = 1 \quad [9.13]$$

$$\delta(q, a, \epsilon, q) = \delta(q, b, \epsilon, q) = 1 \quad [9.14]$$

$$\delta(q, \epsilon, a, q) = \delta(q, \epsilon, b, q) = 1. \quad [9.15]$$

4684 The state diagram is shown in Figure 9.5.

4685 For a given string pair, there are multiple paths through the transducer: the best-  
 4686 scoring path from *dessert* to *desert* involves a single deletion, for a total score of 1; the  
 4687 worst-scoring path involves seven deletions and six additions, for a score of 13.

4688 **9.1.4.2 The Porter stemmer**

The Porter (1980) stemming algorithm is a “lexicon-free” algorithm for stripping suffixes from English words, using a sequence of character-level rules. Each rule can be described

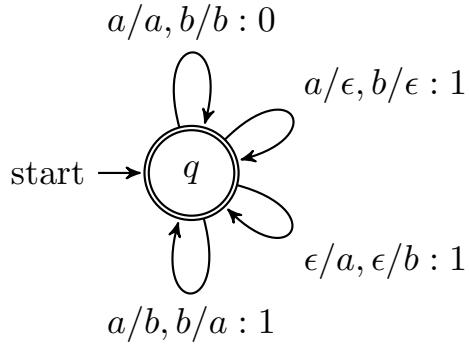


Figure 9.5: State diagram for the Levenshtein edit distance finite state transducer. The label  $x/y : c$  indicates a cost of  $c$  for a transition with input  $x$  and output  $y$ .

by an unweighted finite state transducer. The first rule is:

-sses → -ss e.g., *dresses* → *dress* [9.16]

-ies → -i e.g., *parties* → *parti* [9.17]

-ss → -ss e.g., *dress* → *dress* [9.18]

-s → ε e.g., *cats* → *cat* [9.19]

4689 The final two lines appear to conflict; they are meant to be interpreted as an instruction  
 4690 to remove a terminal *-s* unless it is part of an *-ss* ending. A state diagram to handle just  
 4691 these final two lines is shown in Figure 9.6. Make sure you understand how this finite  
 4692 state transducer handles *cats*, *steps*, *bass*, and *basses*.

#### 4693 9.1.4.3 Inflectional morphology

4694 In **inflectional morphology**, word **lemmas** are modified to add grammatical information  
 4695 such as tense, number, and case. For example, many English nouns are pluralized by the  
 4696 suffix *-s*, and many verbs are converted to past tense by the suffix *-ed*. English's inflectional  
 4697 morphology is considerably simpler than many of the world's languages. For example,  
 4698 Romance languages (derived from Latin) feature complex systems of verb suffixes which  
 4699 must agree with the person and number of the verb, as shown in Table 9.1.

4700 The task of **morphological analysis** is to read a form like *canto*, and output an analysis  
 4701 like CANTAR+VERB+PRESIND+1P+SING, where +PRESIND describes the tense as present  
 4702 indicative, +1P indicates the first-person, and +SING indicates the singular number. The  
 4703 task of **morphological generation** is the reverse, going from CANTAR+VERB+PRESIND+1P+SING  
 4704 to *canto*. Finite state transducers are an attractive solution, because they can solve both  
 4705 problems with a single model (Beesley and Karttunen, 2003). As an example, Figure 9.7  
 4706 shows a fragment of a finite state transducer for Spanish inflectional morphology. The

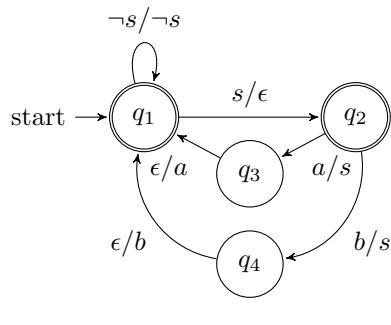


Figure 9.6: State diagram for final two lines of step 1a of the Porter stemming diagram. States  $q_3$  and  $q_4$  “remember” the observations  $a$  and  $b$  respectively; the ellipsis  $\dots$  represents additional states for each symbol in the input alphabet. The notation  $\neg s / \neg s$  is not part of the FST formalism; it is a shorthand to indicate a set of self-transition arcs for every input/output symbol except  $s$ .

infinitive	cantar (to sing)	comer (to eat)	vivir (to live)
yo (1st singular)	canto	como	vivo
tu (2nd singular)	cantas	comes	vives
él, ella, usted (3rd singular)	canta	come	vive
nosotros (1st plural)	cantamos	comemos	vivimos
vosotros (2nd plural, informal)	cantáis	coméis	vívís
ellos, ellas (3rd plural); ustedes (2nd plural)	cantan	comen	viven

Table 9.1: Spanish verb inflections for the present indicative tense. Each row represents a person and number, and each column is a regular example from a class of verbs, as indicated by the ending of the infinitive form.

4707 input vocabulary  $\Sigma$  corresponds to the set of letters used in Spanish spelling, and the out-  
 4708 put vocabulary  $\Omega$  corresponds to these same letters, plus the vocabulary of morphological  
 4709 features (e.g., +SING, +VERB). In Figure 9.7, there are two paths that take *canto* as input,  
 4710 corresponding to the verb and noun meanings; the choice between these paths could be  
 4711 guided by a part-of-speech tagger. By **inversion**, the inputs and outputs for each trans-  
 4712 ition are switched, resulting in a finite state generator, capable of producing the correct  
 4713 **surface form** for any morphological analysis.

4714 Finite state morphological analyzers and other unweighted transducers can be de-  
 4715 signed by hand. The designer’s goal is to avoid **overgeneration** — accepting strings or  
 4716 making transductions that are not valid in the language — as well as **undergeneration** —

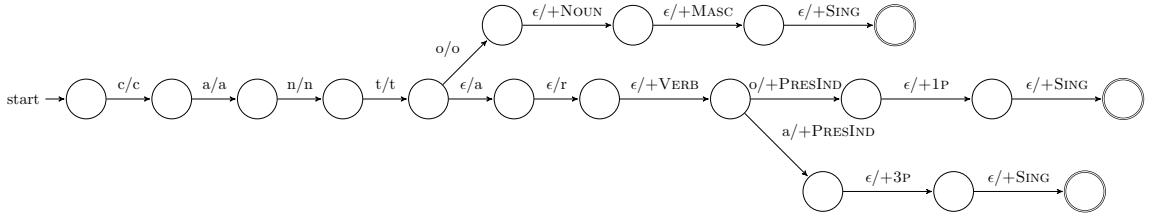


Figure 9.7: Fragment of a finite state transducer for Spanish morphology. There are two accepting paths for the input *canto*: *canto+NOUN+MASC+SING* (masculine singular noun, meaning a song), and *cantar+VERB+PRESIND+1P+SING* (I sing). There is also an accepting path for *canta*, with output *cantar+VERB+PRESIND+3P+SING* (he/she sings).

4717 failing to accept strings or transductions that are valid. For example, a pluralization trans-  
 4718 ducer that does not accept *foot/feet* would undergenerate. Suppose we “fix” the transducer  
 4719 to accept this example, but as a side effect, it now accepts *boot/beet*; the transducer would  
 4720 then be said to overgenerate. A transducer that accepts *foot/foots* but not *foot/feet* would  
 4721 both overgenerate and undergenerate.

#### 4722 9.1.4.4 Finite state composition

4723 Designing finite state transducers to capture the full range of morphological phenomena  
 4724 in any real language is a huge task. Modularization is a classic computer science approach  
 4725 for this situation: decompose a large and unwieldy problem into a set of subproblems,  
 4726 each of which will hopefully have a concise solution. Finite state automata can be mod-  
 4727 ularized through **composition**: feeding the output of one transducer  $T_1$  as the input to  
 4728 another transducer  $T_2$ , written  $T_2 \circ T_1$ . Formally, if there exists some  $y$  such that  $(x, y) \in T_1$   
 4729 (meaning that  $T_1$  produces output  $y$  on input  $x$ ), and  $(y, z) \in T_2$ , then  $(x, z) \in (T_2 \circ T_1)$ .  
 4730 Because finite state transducers are closed under composition, there is guaranteed to be  
 4731 a single finite state transducer that  $T_3 = T_2 \circ T_1$ , which can be constructed as a machine  
 4732 with one state for each pair of states in  $T_1$  and  $T_2$  (Mohri et al., 2002).

4733 **Example: Morphology and orthography** In English morphology, the suffix *-ed* is added  
 4734 to signal the past tense for many verbs: *cook*→*cooked*, *want*→*wanted*, etc. However, English  
 4735 **orthography** dictates that this process cannot produce a spelling with consecutive *e*'s, so  
 4736 that *bake*→*baked*, not *bakeed*. A modular solution is to build separate transducers for mor-  
 4737 phology and orthography. The morphological transducer  $T_M$  transduces from *bake+PAST*  
 4738 to *bake+ed*, with the *+* symbol indicating a segment boundary. The input alphabet of  $T_M$   
 4739 includes the lexicon of words and the set of morphological features; the output alphabet  
 4740 includes the characters *a-z* and the *+* boundary marker. Next, an orthographic transducer  
 4741  $T_O$  is responsible for the transductions *cook+ed*→*cooked*, and *bake+ed*→*baked*. The input  
 4742 alphabet of  $T_O$  must be the same as the output alphabet for  $T_M$ , and the output alphabet

4743 is simply the characters *a-z*. The composed transducer ( $T_O \circ T_M$ ) then transduces from  
 4744 *bake*+PAST to the spelling *baked*. The design of  $T_O$  is left as an exercise.

**Example: Hidden Markov models** Hidden Markov models (chapter 7) can be viewed as weighted finite state transducers, and they can be constructed by transduction. Recall that a hidden Markov model defines a joint probability over words and tags,  $p(w, y)$ , which can be computed as a path through a **trellis** structure. This trellis is itself a weighted finite state acceptor, with edges between all adjacent nodes  $q_{m-1,i} \rightarrow q_{m,j}$  on input  $Y_m = j$ . The edge weights are log-probabilities,

$$\delta(q_{m-1,i}, Y_m = j, q_{m,j}) = \log p(w_m, Y_m = j | Y_{m-1} = i) \quad [9.20]$$

$$= \log p(w_m | Y_m = j) + \log \Pr(Y_m = j | Y_{m-1} = i). \quad [9.21]$$

4745 Because there is only one possible transition for each tag  $Y_m$ , this WFSA is deterministic.  
 4746 The score for any tag sequence  $\{y_m\}_{m=1}^M$  is the sum of these log-probabilities, correspond-  
 4747 ing to the total log probability  $\log p(w, y)$ . Furthermore, the trellis can be constructed by  
 4748 the composition of simpler FSTs.

- 4749 • First, construct a “transition” transducer to represent a bigram probability model  
 4750 over tag sequences,  $T_T$ . This transducer is almost identical to the  $n$ -gram language  
 4751 model acceptor in § 9.1.3.1: there is one state for each tag, and the edge weights  
 4752 equal to the transition log-probabilities,  $\delta(q_i, j, j, q_j) = \log \Pr(Y_m = j | Y_{m-1} = i)$ .  
 4753 Note that  $T_T$  is a transducer, with identical input and output at each arc; this makes  
 4754 it possible to compose  $T_T$  with other transducers.
- 4755 • Next, construct an “emission” transducer to represent the probability of words given  
 4756 tags,  $T_E$ . This transducer has only a single state, with arcs for each word/tag pair,  
 4757  $\delta(q_0, i, j, q_0) = \log \Pr(W_m = j | Y_m = i)$ . The input vocabulary is the set of all tags,  
 4758 and the output vocabulary is the set of all words.
- 4759 • The composition  $T_E \circ T_T$  is a finite state transducer with one state per tag, as shown  
 4760 in Figure 9.8. Each state has  $V \times K$  outgoing edges, representing transitions to each  
 4761 of the  $K$  other states, with outputs for each of the  $V$  words in the vocabulary. The  
 4762 weights for these edges are equal to,

$$\delta(q_i, Y_m = j, w_m, q_j) = \log p(w_m, Y_m = j | Y_{m-1} = i). \quad [9.22]$$

- 4763 • The trellis is a structure with  $M \times K$  nodes, for each of the  $M$  words to be tagged and  
 4764 each of the  $K$  tags in the tagset. It can be built by composition of  $(T_E \circ T_T)$  against an  
 4765 unweighted **chain FSA**  $M_A(w)$  that is specially constructed to accept only a given  
 4766 input  $w_1, w_2, \dots, w_M$ , shown in Figure 9.9. The trellis for input  $w$  is built from the  
 4767 composition  $M_A(w) \circ (T_E \circ T_T)$ . Composing with the unweighted  $M_A(w)$  does not  
 4768 affect the edge weights from  $(T_E \circ T_T)$ , but it selects the subset of paths that generate  
 4769 the word sequence  $w$ .

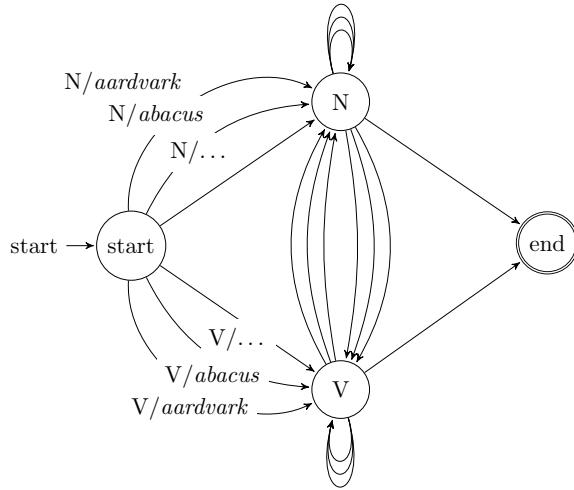


Figure 9.8: Finite state transducer for hidden Markov models, with a small tagset of nouns and verbs. For each pair of tags (including self-loops), there is an edge for every word in the vocabulary. For simplicity, input and output are only shown for the edges from the start state. Weights are also omitted from the diagram; for each edge from  $q_i$  to  $q_j$ , the weight is equal to  $\log p(w_m, Y_m = j \mid Y_{m-1} = i)$ , except for edges to the end state, which are equal to  $\log \Pr(Y_m = \diamond \mid Y_{m-1} = i)$ .

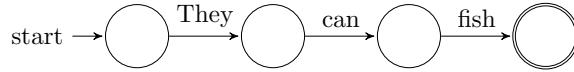


Figure 9.9: Chain finite state acceptor for the input *They can fish*.

#### 4770 9.1.5 \*Learning weighted finite state automata

4771 In generative models such as  $n$ -gram language models and hidden Markov models, the  
 4772 edge weights correspond to log probabilities, which can be obtained from relative fre-  
 4773 quency estimation. However, in other cases, we wish to learn the edge weights from in-  
 4774 put/output pairs. This is difficult in non-deterministic finite state automata, because we  
 4775 do not observe the specific arcs that are traversed in accepting the input, or in transducing  
 4776 from input to output. The path through the automaton is a **latent variable**.

4777 Chapter 5 presented one method for learning with latent variables: expectation max-  
 4778 imization (EM). This involves computing a distribution  $q(\cdot)$  over the latent variable, and  
 4779 iterating between updates to this distribution and updates to the parameters — in this  
 4780 case, the arc weights. The **forward-backward algorithm** (§ 7.5.3.3) describes a dynamic  
 4781 program for computing a distribution over arcs in the trellis structure of a hidden Markov

model, but this is a special case of the more general problem for finite state automata. Eisner (2002) describes an **expectation semiring**, which enables the expected number of transitions across each arc to be computed through a semiring shortest-path algorithm. Alternative approaches for generative models include Markov Chain Monte Carlo (Chiang et al., 2010) and spectral learning (Balle et al., 2011).

Further afield, we can take a perceptron-style approach, with each arc corresponding to a feature. The classic perceptron update would update the weights by subtracting the difference between the feature vector corresponding to the predicted path and the feature vector corresponding to the correct path. Since the path is not observed, we resort to a **hidden variable perceptron**. The model is described formally in § 12.4, but the basic idea is to compute an update from the difference between the features from the predicted path and the features for the best-scoring path that generates the correct output.

## 9.2 Context-free languages

Beyond the class of regular languages lie the context-free languages. An example of a language that is context-free but not finite state is the set of arithmetic expressions with balanced parentheses. Intuitively, to accept only strings in this language, an FSA would have to “count” the number of left parentheses, and make sure that they are balanced against the number of right parentheses. An arithmetic expression can be arbitrarily long, yet by definition an FSA has a finite number of states. Thus, for any FSA, there will be a string that with too many parentheses to count. More formally, the **pumping lemma** is a proof technique for showing that languages are not regular. It is typically demonstrated for the simpler case  $a^n b^n$ , the language of strings containing a sequence of  $a$ 's, and then an equal-length sequence of  $b$ 's.<sup>4</sup>

There are at least two arguments for the relevance of non-regular formal languages to linguistics. First, there are natural language phenomena that are argued to be isomorphic to  $a^n b^n$ . For English, the classic example is **center embedding**, shown in Figure 9.10. The initial expression *the dog* specifies a single dog. Embedding this expression into *the cat ... chased* specifies a particular cat — the one chased by the dog. This cat can then be embedded again to specify a goat, in the less felicitous but arguably grammatical expression, *the goat the cat the dog chased kissed*, which refers to the goat who was kissed by the cat which was chased by the dog. Chomsky (1957) argues that to be grammatical, a center-embedded construction must be balanced: if it contains  $n$  noun phrases (e.g., *the cat*), they must be followed by exactly  $n - 1$  verbs. An FSA that could recognize such expressions would also be capable of recognizing the language  $a^n b^n$ . Because we can prove that no FSA exists for  $a^n b^n$ , no FSA can exist for center embedded constructions either. En-

---

<sup>4</sup>Details of the proof can be found in an introductory computer science theory textbook (e.g., Sipser, 2012).

---

			the dog	
	the cat	the dog	chased	
the goat	the cat	the dog	chased	kissed
			...	

---

Figure 9.10: Three levels of center embedding

4817 glish includes center embedding, and so the argument goes, English grammar as a whole  
 4818 cannot be regular.<sup>5</sup>

4819 A more practical argument for moving beyond regular languages is modularity. Many  
 4820 linguistic phenomena — especially in syntax — involve constraints that apply at long  
 4821 distance. Consider the problem of determiner-noun number agreement in English: we  
 4822 can say *the coffee* and *these coffees*, but not *\*these coffee*. By itself, this is easy enough to model  
 4823 in an FSA. However, fairly complex modifying expressions can be inserted between the  
 4824 determiner and the noun:

- 4825 (9.5) the burnt coffee
- 4826 (9.6) the badly-ground coffee
- 4827 (9.7) the burnt and badly-ground Italian coffee
- 4828 (9.8) these burnt and badly-ground Italian coffees
- 4829 (9.9) \*these burnt and badly-ground Italian coffee

4830 Again, an FSA can be designed to accept modifying expressions such as *burnt and badly-*  
 4831 *ground Italian*. Let's call this FSA  $F_M$ . To reject the final example, a finite state acceptor  
 4832 must somehow "remember" that the determiner was plural when it reaches the noun *cof-*  
 4833 *fee* at the end of the expression. The only way to do this is to make two identical copies  
 4834 of  $F_M$ : one for singular determiners, and one for plurals. While this is possible in the  
 4835 finite state framework, it is inconvenient — especially in languages where more than one  
 4836 attribute of the noun is marked by the determiner. **Context-free languages** facilitate mod-  
 4837 ularity across such long-range dependencies.

### 4838 9.2.1 Context-free grammars

4839 Context-free languages are specified by **context-free grammars (CFGs)**, which are tuples  
 4840  $(N, \Sigma, R, S)$  consisting of:

---

<sup>5</sup>The claim that arbitrarily deep center-embedded expressions are grammatical has drawn skepticism. Corpus evidence shows that embeddings of depth greater than two are exceedingly rare (Karlsson, 2007), and that embeddings of depth greater than three are completely unattested. If center-embedding is capped at some finite depth, then it is regular.

$$\begin{aligned}
 S &\rightarrow S \text{ OP } S \mid \text{NUM} \\
 \text{OP} &\rightarrow + \mid - \mid \times \mid \div \\
 \text{NUM} &\rightarrow \text{NUM DIGIT} \mid \text{DIGIT} \\
 \text{DIGIT} &\rightarrow 0 \mid 1 \mid 2 \mid \dots \mid 9
 \end{aligned}$$

Figure 9.11: A context-free grammar for arithmetic expressions

- 4841 • a finite set of **non-terminals**  $N$ ;
- 4842 • a finite alphabet  $\Sigma$  of **terminal symbols**;
- 4843 • a set of **production rules**  $R$ , each of the form  $A \rightarrow \beta$ , where  $A \in N$  and  $\beta \in (\Sigma \cup N)^*$ ;
- 4844 • a designated start symbol  $S$ .

4845 In the production rule  $A \rightarrow \beta$ , the left-hand side (LHS)  $A$  must be a non-terminal;  
 4846 the right-hand side (RHS) can be a sequence of terminals or non-terminals,  $\{n, \sigma\}^*, n \in$   
 4847  $N, \sigma \in \Sigma$ . A non-terminal can appear on the left-hand side of many production rules.  
 4848 A non-terminal can appear on both the left-hand side and the right-hand side; this is a  
 4849 **recursive production**, and is analogous to self-loops in finite state automata. The name  
 4850 “context-free” is based on the property that the production rule depends only on the LHS,  
 4851 and not on its ancestors or neighbors; this is analogous to Markov property of finite state  
 4852 automata, in which the behavior at each step depends only on the current state, on not on  
 4853 the path by which that state was reached.

4854 A **derivation**  $\tau$  is a sequence of steps from the start symbol  $S$  to a surface string  $w \in \Sigma^*$ ,  
 4855 which is the **yield** of the derivation. A string  $w$  is in a context-free language if there is  
 4856 some derivation from  $S$  yielding  $w$ . **Parsing** is the problem of finding a derivation for a  
 4857 string in a grammar. Algorithms for parsing are described in chapter 10.

4858 Like regular expressions, context-free grammars define the language but not the com-  
 4859 putation necessary to recognize it. The context-free analogues to finite state acceptors are  
 4860 **pushdown automata**, a theoretical model of computation in which input symbols can be  
 4861 pushed onto a stack with potentially infinite depth. For more details, see Sipser (2012).

### 4862 9.2.1.1 Example

4863 Figure 9.11 shows a context-free grammar for arithmetic expressions such as  $1 + 2 \div 3 - 4$ .  
 4864 In this grammar, the terminal symbols include the digits  $\{1, 2, \dots, 9\}$  and the op-  
 4865 erators  $\{+, -, \times, \div\}$ . The rules include the  $|$  symbol, a notational convenience that makes  
 4866 it possible to specify multiple right-hand sides on a single line: the statement  $A \rightarrow x | y$

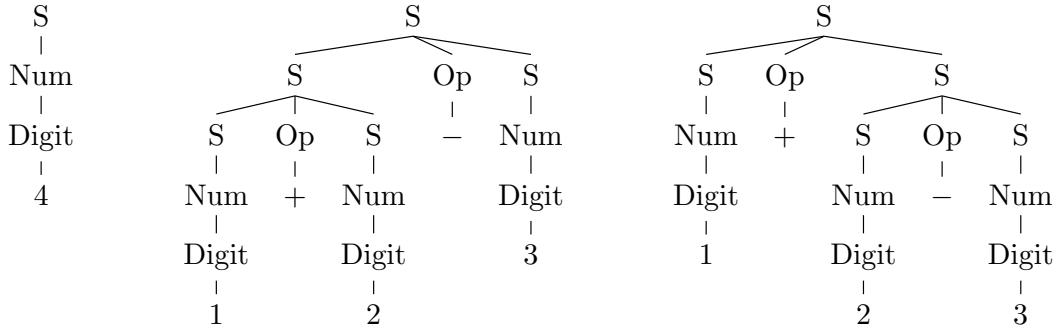


Figure 9.12: Some example derivations from the arithmetic grammar in Figure 9.11

4867 defines *two* productions,  $A \rightarrow x$  and  $A \rightarrow y$ . This grammar is recursive: the non-termals  $S$   
4868 and  $\text{NUM}$  can produce themselves.

4869 Derivations are typically shown as trees, with production rules applied from the top  
4870 to the bottom. The tree on the left in Figure 9.12 describes the derivation of a single digit,  
4871 through the sequence of productions  $S \rightarrow \text{NUM} \rightarrow \text{DIGIT} \rightarrow 4$  (these are all **unary produc-**  
4872 **tions**, because the right-hand side contains a single element). The other two trees in  
4873 Figure 9.12 show alternative derivations of the string  $1 + 2 - 3$ . The existence of multiple  
4874 derivations for a string indicates that the grammar is **ambiguous**.

Context-free derivations can also be written out according to the pre-order tree traversal.<sup>6</sup> For the two derivations of  $1 + 2 - 3$  in Figure 9.12, the notation is:

$$(S (S (S (\text{Num} (Digit 1))) (\text{Op} +) (S (\text{Num} (Digit 2))))) (\text{Op} -) (S (\text{Num} (Digit 3)))) \quad [9.23]$$

$$(S (S (\text{Num} (Digit 1))) (\text{Op} +) (S (\text{Num} (Digit 2)) (\text{Op} -) (S (\text{Num} (Digit 3)))))). \quad [9.24]$$

#### 4875 9.2.1.2 Grammar equivalence and Chomsky Normal Form

A single context-free language can be expressed by more than one context-free grammar. For example, the following two grammars both define the language  $a^n b^n$  for  $n > 0$ .

$$\begin{aligned} S &\rightarrow aSb \mid ab \\ S &\rightarrow aSb \mid aabb \mid ab \end{aligned}$$

4876 Two grammars are **weakly equivalent** if they generate the same strings. Two grammars  
4877 are **strongly equivalent** if they generate the same strings via the same derivations. The  
4878 grammars above are only weakly equivalent.

<sup>6</sup>This is a depth-first left-to-right search that prints each node the first time it is encountered (Cormen et al., 2009, chapter 12).

In **Chomsky Normal Form (CNF)**, the right-hand side of every production includes either two non-terminals, or a single terminal symbol:

$$A \rightarrow BC$$

$$A \rightarrow a$$

- 4879 All CFGs can be converted into a CNF grammar that is weakly equivalent. To convert a  
 4880 grammar into CNF, we first address productions that have more than two non-terminals  
 4881 on the RHS by creating new “dummy” non-terminals. For example, if we have the pro-  
 4882 duction,

$$W \rightarrow X Y Z, \quad [9.25]$$

it is replaced with two productions,

$$W \rightarrow X W \setminus X \quad [9.26]$$

$$W \setminus X \rightarrow Y Z. \quad [9.27]$$

- 4883 In these productions,  $W \setminus X$  is a new dummy non-terminal. This transformation **binarizes**  
 4884 the grammar, which is critical for efficient bottom-up parsing, as we will see in chapter 10.  
 4885 Productions whose right-hand side contains a mix of terminal and non-terminal symbols  
 4886 can be replaced in a similar fashion.

- 4887 Unary non-terminal productions  $A \rightarrow B$  are replaced as follows: identify all produc-  
 4888 tions  $B \rightarrow \alpha$ , and add  $A \rightarrow \alpha$  to the grammar. For example, in the grammar described in  
 4889 Figure 9.11, we would replace  $\text{NUM} \rightarrow \text{DIGIT}$  with  $\text{NUM} \rightarrow 1 \mid 2 \mid \dots \mid 9$ . However, we  
 4890 keep the production  $\text{NUM} \rightarrow \text{NUM DIGIT}$ , which is a valid binary production.

### 4891 9.2.2 Natural language syntax as a context-free language

- 4892 Context-free grammars are widely used to represent **syntax**, which is the set of rules that  
 4893 determine whether an utterance is judged to be grammatical. If this representation were  
 4894 perfectly faithful, then a natural language such as English could be transformed into a  
 4895 formal language, consisting of exactly the (infinite) set of strings that would be judged to  
 4896 be grammatical by a fluent English speaker. We could then build parsing software that  
 4897 would automatically determine if a given utterance were grammatical.<sup>7</sup>

- 4898 Contemporary theories generally do *not* consider natural languages to be context-free  
 4899 (see § 9.3), yet context-free grammars are widely used in natural language parsing. The  
 4900 reason is that context-free representations strike a good balance: they cover a broad range  
 4901 of syntactic phenomena, and they can be parsed efficiently. This section therefore de-  
 4902 scribes how to handle a core fragment of English syntax in context-free form, following

---

<sup>7</sup>You are encouraged to move beyond this cursory treatment of syntax by consulting a textbook on linguistics (e.g., Akmajian et al., 2010; Bender, 2013).

4903 the conventions of the **Penn Treebank** (PTB; Marcus et al., 1993), a large-scale annotation  
 4904 of English language syntax. The generalization to “mildly” context-sensitive languages is  
 4905 discussed in § 9.3.

4906 The Penn Treebank annotation is a **phrase-structure grammar** of English. This means  
 4907 that sentences are broken down into **constituents**, which are contiguous sequences of  
 4908 words that function as coherent units for the purpose of linguistic analysis. Constituents  
 4909 generally have a few key properties:

4910 **Movement.** Constituents can often be moved around sentences as units.

- 4911 (9.10) Abigail gave (her brother) (a fish).  
 4912 (9.11) Abigail gave (a fish) to (her brother).

4913 In contrast, *gave her* and *brother a* cannot easily be moved while preserving gram-  
 4914 maticality.

4915 **Substitution.** Constituents can be substituted by other phrases of the same type.

- 4916 (9.12) Max thanked (his older sister).  
 4917 (9.13) Max thanked (her).

4918 In contrast, substitution is not possible for other contiguous units like *Max thanked*  
 4919 and *thanked his*.

4920 **Coordination.** Coordinators like *and* and *or* can conjoin constituents.

- 4921 (9.14) (Abigail) and (her younger brother) bought a fish.  
 4922 (9.15) Abigail (bought a fish) and (gave it to Max).  
 4923 (9.16) Abigail (bought) and (greedily ate) a fish.

4924 Units like *brother bought* and *bought a* cannot easily be coordinated.

4925 These examples argue for units such as *her brother* and *bought a fish* to be treated as con-  
 4926 stituents. Other sequences of words in these examples, such as *Abigail gave* and *brother*  
*a fish*, cannot be moved, substituted, and coordinated in these ways. In phrase-structure  
 4927 grammar, constituents are nested, so that *the senator from New Jersey* contains the con-  
 4928 stituent *from New Jersey*, which in turn contains *New Jersey*. The sentence itself is the max-  
 4929 imal constituent; each word is a minimal constituent, derived from a unary production  
 4930 from a part-of-speech tag. Between part-of-speech tags and sentences are **phrases**. In  
 4931 phrase-structure grammar, phrases have a type that is usually determined by their **head**  
 4932 **word**: for example, a **noun phrase** corresponds to a noun and the group of words that

4934 modify it, such as *her younger brother*; a **verb phrase** includes the verb and its modifiers,  
4935 such as *bought a fish* and *greedily ate it*.

4936 In context-free grammars, each phrase type is a non-terminal, and each constituent is  
4937 the substring that the non-terminal yields. Grammar design involves choosing the right  
4938 set of non-terminals. Fine-grained non-terminals make it possible to represent more fine-  
4939 grained linguistic phenomena. For example, by distinguishing singular and plural noun  
4940 phrases, it is possible to have a grammar of English that generates only sentences that  
4941 obey subject-verb agreement. However, enforcing subject-verb agreement is considerably  
4942 more complicated in languages like Spanish, where the verb must agree in both person  
4943 and number with subject. In general, grammar designers must trade off between **over-**  
4944 **generation** — a grammar that permits ungrammatical sentences — and **undergeneration**  
4945 — a grammar that fails to generate grammatical sentences. Furthermore, if the grammar is  
4946 to support manual annotation of syntactic structure, it must be simple enough to annotate  
4947 efficiently.

### 4948 9.2.3 A phrase-structure grammar for English

4949 To better understand how phrase-structure grammar works, let's consider the specific  
4950 case of the Penn Treebank grammar of English. The main phrase categories in the Penn  
4951 Treebank (PTB) are based on the main part-of-speech classes: noun phrase (NP), verb  
4952 phrase (VP), prepositional phrase (PP), adjectival phrase (ADJP), and adverbial phrase  
4953 (ADVP). The top-level category is S, which conveniently stands in for both "sentence"  
4954 and the "start" symbol. **Complement clauses** (e.g., *I take the good old fashioned ground that*  
4955 *the whale is a fish*) are represented by the non-terminal SBAR. The terminal symbols in  
4956 the grammar are individual words, which are generated from unary productions from  
4957 part-of-speech tags (the PTB tagset is described in § 8.1).

4958 This section explores the productions from the major phrase-level categories, explaining  
4959 how to generate individual tag sequences. The production rules are approached in a  
4960 "theory-driven" manner: first the syntactic properties of each phrase type are described,  
4961 and then some of the necessary production rules are listed. But it is important to keep  
4962 in mind that the Penn Treebank was produced in a "data-driven" manner. After the set  
4963 of non-terminals was specified, annotators were free to analyze each sentence in what-  
4964 ever way seemed most linguistically accurate, subject to some high-level guidelines. The  
4965 grammar of the Penn Treebank is simply the set of productions that were required to ana-  
4966 lyze the several million words of the corpus. By design, the grammar overgenerates — it  
4967 does not exclude ungrammatical sentences.

4968 **9.2.3.1 Sentences**

The most common production rule for sentences is,

$$S \rightarrow NP VP \quad [9.28]$$

which accounts for simple sentences like *Abigail ate the kimchi* — as we will see, the direct object *the kimchi* is part of the verb phrase. But there are more complex forms of sentences as well:

$$S \rightarrow ADVP NP VP \quad \begin{matrix} Unfortunately Abigail ate the kimchi. \\ Abigail ate the kimchi and Max had a burger. \end{matrix} \quad [9.29]$$

$$S \rightarrow S CC S \quad \begin{matrix} Abigail ate the kimchi and Max had a burger. \\ Eat the kimchi. \end{matrix} \quad [9.30]$$

$$S \rightarrow VP \quad \begin{matrix} Eat the kimchi. \end{matrix} \quad [9.31]$$

- 4969 where ADVP is an adverbial phrase (e.g., *unfortunately*, *very unfortunately*) and CC is a  
 4970 coordinating conjunction (e.g., *and*, *but*).<sup>8</sup>

4971 **9.2.3.2 Noun phrases**

Noun phrases refer to entities, real or imaginary, physical or abstract: *Asha*, *the steamed dumpling*, *parts and labor*, *nobody*, *the whiteness of the whale*, and *the rise of revolutionary syndicalism in the early twentieth century*. Noun phrase productions include “bare” nouns, which may optionally follow determiners, as well as pronouns:

$$NP \rightarrow NN | NNS | NNP | PRP \quad [9.32]$$

$$NP \rightarrow DET NN | DET NNS | DET NNP \quad [9.33]$$

- 4972 The tags NN, NNS, and NNP refer to singular, plural, and proper nouns; PRP refers to  
 4973 personal pronouns, and DET refers to determiners. The grammar also contains terminal  
 4974 productions from each of these tags, e.g.,  $PRP \rightarrow I | you | we | \dots$ .

Noun phrases may be modified by adjectival phrases (ADJP; e.g., *the small Russian dog*) and numbers (CD; e.g., *the five pastries*), each of which may optionally follow a determiner:

$$NP \rightarrow ADJP NN | ADJP NNS | DET ADJP NN | DET ADJP NNS \quad [9.34]$$

$$NP \rightarrow CD NNS | DET CD NNS | \dots \quad [9.35]$$

Some noun phrases include multiple nouns, such as *the liberation movement* and *an antelope horn*, necessitating additional productions:

$$NP \rightarrow NN NN | NN NNS | DET NN NN | \dots \quad [9.36]$$

---

<sup>8</sup>Notice that the grammar does not include the recursive production  $S \rightarrow ADVP S$ . It may be helpful to think about why this production would cause the grammar to overgenerate.

4975 These multiple noun constructions can be combined with adjectival phrases and cardinal  
 4976 numbers, leading to a large number of additional productions.

Recursive noun phrase productions include coordination, prepositional phrase attachment, subordinate clauses, and verb phrase adjuncts:

$NP \rightarrow NP\ CC\ NP$	<i>e.g., the red and the black</i>	[9.37]
$NP \rightarrow NP\ PP$	<i>e.g., the President of the Georgia Institute of Technology</i>	[9.38]
$NP \rightarrow NP\ SBAR$	<i>e.g., a whale which he had wounded</i>	[9.39]
$NP \rightarrow NP\ VP$	<i>e.g., a whale taken near Shetland</i>	[9.40]

4977 These recursive productions are a major source of ambiguity, because the VP and PP non-  
 4978 terminals can also generate NP children. Thus, the *the President of the Georgia Institute of*  
 4979 *Technology* can be derived in two ways, as can *a whale taken near Shetland in October*.

4980 But aside from these few recursive productions, the noun phrase fragment of the Penn  
 4981 Treebank grammar is relatively flat, containing a large of number of productions that go  
 4982 from NP directly to a sequence of parts-of-speech. If noun phrases had more internal  
 4983 structure, the grammar would need fewer rules, which, as we will see, would make pars-  
 4984 ing faster and machine learning easier. Vadas and Curran (2011) propose to add additional  
 4985 structure in the form of a new non-terminal called a **nominal modifier** (NML), e.g.,

4986 (9.17) (NP (NN crude) (NN oil) (NNS prices)) (PTB analysis)  
 4987 (NP (NML (NN crude) (NN oil)) (NNS prices)) (NML-style analysis)

4988 Another proposal is to treat the determiner as the head of a **determiner phrase** (DP;  
 4989 Abney, 1987). There are linguistic arguments for and against determiner phrases (e.g.,  
 4990 Van Eynde, 2006). From the perspective of context-free grammar, DPs enable more struc-  
 4991 tured analyses of some constituents, e.g.,

4992 (9.18) (NP (DT the) (JJ white) (NN whale)) (PTB analysis)  
 4993 (DP (DT the) (NP (JJ white) (NN whale))) (DP-style analysis).

### 4994 9.2.3.3 Verb phrases

Verb phrases describe actions, events, and states of being. The PTB tagset distinguishes several classes of verb inflections: base form (VB; *she likes to snack*), present-tense third-person singular (VBZ; *she snacks*), present tense but not third-person singular (VBP; *they snack*), past tense (VBD; *they snacked*), present participle (VBG; *they are snacking*), and past participle (VBN; *they had snacked*).<sup>9</sup> Each of these forms can constitute a verb phrase on its

---

<sup>9</sup>This tagset is specific to English: for example, VBP is a meaningful category only because English morphology distinguishes third-person singular from all person-number combinations.

own:

$$VP \rightarrow VB \mid VBZ \mid VBD \mid VBN \mid VBG \mid VBP \quad [9.41]$$

More complex verb phrases can be formed by a number of recursive productions, including the use of coordination, modal verbs (MD; *she should snack*), and the infinitival *to* (TO):

$VP \rightarrow MD \ VP$	<i>She will snack</i>	[9.42]
$VP \rightarrow VBD \ VP$	<i>She had snacked</i>	[9.43]
$VP \rightarrow VBZ \ VP$	<i>She has been snacking</i>	[9.44]
$VP \rightarrow VBN \ VP$	<i>She has been snacking</i>	[9.45]
$VP \rightarrow TO \ VP$	<i>She wants to snack</i>	[9.46]
$VP \rightarrow VP \ CC \ VP$	<i>She buys and eats many snacks</i>	[9.47]

- 4995 Each of these productions uses recursion, with the VP non-terminal appearing in both the  
 4996 LHS and RHS. This enables the creation of complex verb phrases, such as *She will have*  
 4997 *wanted to have been snacking*.

Transitive verbs take noun phrases as direct objects, and ditransitive verbs take two direct objects:

$VP \rightarrow VBZ \ NP$	<i>She teaches algebra</i>	[9.48]
$VP \rightarrow VBG \ NP$	<i>She has been teaching algebra</i>	[9.49]
$VP \rightarrow VBD \ NP \ NP$	<i>She taught her brother algebra</i>	[9.50]

These productions are *not* recursive, so a unique production is required for each verb part-of-speech. They also do not distinguish transitive from intransitive verbs, so the resulting grammar overgenerates examples like *\*She sleeps sushi* and *\*She learns Boyang algebra*. Sentences can also be direct objects:

$VP \rightarrow VBZ \ S$	<i>Asha wants to eat the kimchi</i>	[9.51]
$VP \rightarrow VBZ \ SBAR$	<i>Asha knows that Boyang eats the kimchi</i>	[9.52]

- 4998 The first production overgenerates, licensing sentences like *\*Asha sees Boyang eats the kimchi*.  
 4999 This problem could be addressed by designing a more specific set of sentence non-  
 5000 terminals, indicating whether the main verb can be conjugated.

Verbs can also be modified by prepositional phrases and adverbial phrases:

$VP \rightarrow VBZ \ PP$	<i>She studies at night</i>	[9.53]
$VP \rightarrow VBZ \ ADVP$	<i>She studies intensively</i>	[9.54]
$VP \rightarrow ADVP \ VBG$	<i>She is not studying</i>	[9.55]

5001 Again, because these productions are not recursive, the grammar must include produc-  
 5002 tions for every verb part-of-speech.

A special set of verbs, known as **copula**, can take **predicative adjectives** as direct ob-  
 jects:

$VP \rightarrow VBZ\ ADJP$  *She is hungry* [9.56]

$VP \rightarrow VBP\ ADJP$  *Success seems increasingly unlikely* [9.57]

5003 The PTB does not have a special non-terminal for copular verbs, so this production gen-  
 5004 erates non-grammatical examples such as *\*She eats tall*.

**Particles** (PRT as a phrase; RP as a part-of-speech) work to create phrasal verbs:

$VP \rightarrow VB\ PRT$  *She told them to fuck off* [9.58]

$VP \rightarrow VBD\ PRT\ NP$  *They gave up their ill-gotten gains* [9.59]

5005 As the second production shows, particle productions are required for all configurations  
 5006 of verb parts-of-speech and direct objects.

#### 5007 9.2.3.4 Other constituents

The remaining constituents require far fewer productions. **Prepositional phrases** almost  
 always consist of a preposition and a noun phrase,

$PP \rightarrow IN\ NP$  *the whiteness of the whale* [9.60]

$PP \rightarrow TO\ NP$  *What the white whale was to Ahab, has been hinted.* [9.61]

Similarly, complement clauses consist of a complementizer (usually a preposition, pos-  
 sibly null) and a sentence,

$SBAR \rightarrow IN\ S$  *She said that it was spicy* [9.62]

$SBAR \rightarrow S$  *She said it was spicy* [9.63]

Adverbial phrases are usually bare adverbs ( $ADVP \rightarrow RB$ ), with a few exceptions:

$ADVP \rightarrow RB\ RBR$  *They went considerably further* [9.64]

$ADVP \rightarrow ADVP\ PP$  *They went considerably further than before* [9.65]

5008 The tag RBR is a comparative adverb.

Adjectival phrases extend beyond bare adjectives ( $\text{ADJP} \rightarrow \text{JJ}$ ) in a number of ways:

$\text{ADJP} \rightarrow \text{RB JJ}$	<i>very hungry</i>	[9.66]
$\text{ADJP} \rightarrow \text{RBR JJ}$	<i>more hungry</i>	[9.67]
$\text{ADJP} \rightarrow \text{JJS JJ}$	<i>best possible</i>	[9.68]
$\text{ADJP} \rightarrow \text{RB JJR}$	<i>even bigger</i>	[9.69]
$\text{ADJP} \rightarrow \text{JJ CC JJ}$	<i>high and mighty</i>	[9.70]
$\text{ADJP} \rightarrow \text{JJ JJ}$	<i>West German</i>	[9.71]
$\text{ADJP} \rightarrow \text{RB VBN}$	<i>previously reported</i>	[9.72]

5009 The tags JJR and JJS refer to comparative and superlative adjectives respectively.

All of these phrase types can be coordinated:

$\text{PP} \rightarrow \text{PP CC PP}$	<i>on time and under budget</i>	[9.73]
$\text{ADVP} \rightarrow \text{ADVP CC ADVP}$	<i>now and two years ago</i>	[9.74]
$\text{ADJP} \rightarrow \text{ADJP CC ADJP}$	<i>quaint and rather deceptive</i>	[9.75]
$\text{SBar} \rightarrow \text{SBar CC SBar}$	<i>whether they want control</i>	[9.76]
	<i>or whether they want exports</i>	

## 5010 9.2.4 Grammatical ambiguity

5011 Context-free parsing is useful not only because it determines whether a sentence is gram-  
 5012 matical, but mainly because the constituents and their relations can be applied to tasks  
 5013 such as information extraction (chapter 17) and sentence compression (Jing, 2000; Clarke  
 5014 and Lapata, 2008). However, the **ambiguity** of wide-coverage natural language grammars  
 5015 poses a serious problem for such potential applications. As an example, Figure 9.13 shows  
 5016 two possible analyses for the simple sentence *We eat sushi with chopsticks*, depending on  
 5017 whether the *chopsticks* modify *eat* or *sushi*. Realistic grammars can license thousands or  
 5018 even millions of parses for individual sentences. **Weighted context-free grammars** solve  
 5019 this problem by attaching weights to each production, and selecting the derivation with  
 5020 the highest score. This is the focus of chapter 10.

## 5021 9.3 \*Mildly context-sensitive languages

5022 Beyond context-free languages lie **context-sensitive languages**, in which the expansion  
 5023 of a non-terminal depends on its neighbors. In the general class of context-sensitive  
 5024 languages, computation becomes much more challenging: the membership problem for  
 5025 context-sensitive languages is PSPACE-complete. Since PSPACE contains the complexity  
 5026 class NP (problems that can be solved in polynomial time on a non-deterministic Turing

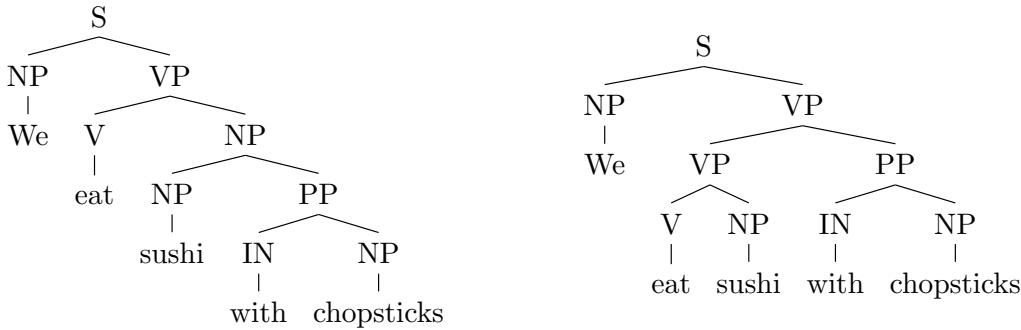


Figure 9.13: Two derivations of the same sentence

5027 machine), PSPACE-complete problems cannot be solved efficiently if  $P \neq NP$ . Thus, de-  
 5028 signing an efficient parsing algorithm for the full class of context-sensitive languages is  
 5029 probably hopeless.<sup>10</sup>

5030 However, Joshi (1985) identifies a set of properties that define **mildly context-sensitive**  
 5031 **languages**, which are a strict subset of context-sensitive languages. Like context-free lan-  
 5032 guages, mildly context-sensitive languages are efficiently parseable. However, the mildly  
 5033 context-sensitive languages include non-context-free languages, such as the “copy lan-  
 5034 guage”  $\{ww \mid w \in \Sigma^*\}$  and the language  $a^m b^n c^m d^n$ . Both are characterized by **cross-**  
 5035 **serial dependencies**, linking symbols at long distance across the string.<sup>11</sup> For example, in  
 5036 the language  $a^n b^m c^n d^m$ , each  $a$  symbol is linked to exactly one  $c$  symbol, regardless of the  
 5037 number of intervening  $b$  symbols.

### 5038 9.3.1 Context-sensitive phenomena in natural language

5039 Such phenomena are occasionally relevant to natural language. A classic example is found  
 5040 in Swiss-German (Shieber, 1985), in which sentences such as *we let the children help Hans*  
 5041 *paint the house* are realized by listing all nouns before all verbs, i.e., *we the children Hans the*  
 5042 *house let help paint*. Furthermore, each noun’s determiner is dictated by the noun’s **case**  
 5043 **marking** (the role it plays with respect to the verb). Using an argument that is analogous  
 5044 to the earlier discussion of center-embedding (§ 9.2), Shieber argues that these case mark-  
 5045 ing constraints are a cross-serial dependency, homomorphic to  $a^m b^n c^m d^n$ , and therefore  
 5046 not context-free.

<sup>10</sup>If  $P \neq NP$ , then it contains problems that cannot be solved in polynomial time on a non-deterministic Turing machine; equivalently, solutions to these problems cannot even be checked in polynomial time (Arora and Barak, 2009).

<sup>11</sup>A further condition of the set of mildly-context-sensitive languages is *constant growth*: if the strings in the language are arranged by length, the gap in length between any pair of adjacent strings is bounded by some language specific constant. This condition excludes languages such as  $\{a^{2^n} \mid n \geq 0\}$ .

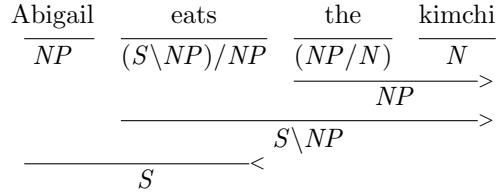


Figure 9.14: A syntactic analysis in CCG involving forward and backward function application

As with the move from regular to context-free languages, mildly context-sensitive languages can be motivated by expedience. While infinite sequences of cross-serial dependencies cannot be handled by context-free grammars, even finite sequences of cross-serial dependencies are more convenient to handle using a mildly context-sensitive formalism like **tree-adjoining grammar** (TAG) and **combinatory categorial grammar** (CCG). Furthermore, TAG-inspired parsers have been shown to be particularly effective in parsing the Penn Treebank (Collins, 1997; Carreras et al., 2008), and CCG plays a leading role in current research on semantic parsing (Zettlemoyer and Collins, 2005). Furthermore, these two formalisms are weakly equivalent: any language that can be specified in TAG can also be specified in CCG, and vice versa (Joshi et al., 1991). The remainder of the chapter gives a brief overview of CCG, but you are encouraged to consult Joshi and Schabes (1997) and Steedman and Baldridge (2011) for more detail on TAG and CCG respectively.

### 9.3.2 Combinatory categorial grammar

In combinatory categorial grammar, structural analyses are built up through a small set of generic combinatorial operations, which apply to immediately adjacent sub-structures. These operations act on the categories of the sub-structures, producing a new structure with a new category. The basic categories include S (sentence), NP (noun phrase), VP (verb phrase) and N (noun). The goal is to label the entire span of text as a sentence, S.

Complex categories, or types, are constructed from the basic categories, parentheses, and forward and backward slashes: for example,  $S/NP$  is a complex type, indicating a sentence that is lacking a noun phrase to its right;  $S\backslash NP$  is a sentence lacking a noun phrase to its left. Complex types act as functions, and the most basic combinatory operations are function application to either the right or left neighbor. For example, the type of a verb phrase, such as *eats*, would be  $S\backslash NP$ . Applying this function to a subject noun phrase to its left results in an analysis of *Abigail eats* as category S, indicating a successful parse.

Transitive verbs must first be applied to the direct object, which in English appears to the right of the verb, before the subject, which appears on the left. They therefore have the more complex type  $(S\backslash NP)/NP$ . Similarly, the application of a determiner to the noun at

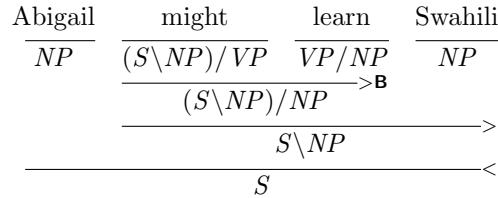


Figure 9.15: A syntactic analysis in CCG involving function composition (example modified from Steedman and Baldridge, 2011)

5076 its right results in a noun phrase, so determiners have the type NP/N. Figure 9.14 pro-  
 5077 vides an example involving a transitive verb and a determiner. A key point from this  
 5078 example is that it can be trivially transformed into phrase-structure tree, by treating each  
 5079 function application as a constituent phrase. Indeed, when CCG's only combinatory op-  
 5080 erators are forward and backward function application, it is equivalent to context-free  
 5081 grammar. However, the location of the "effort" has changed. Rather than designing good  
 5082 productions, the grammar designer must focus on the **lexicon** — choosing the right cate-  
 5083 gories for each word. This makes it possible to parse a wide range of sentences using only  
 5084 a few generic combinatory operators.

5085 Things become more interesting with the introduction of two additional operators:  
 5086 **composition** and **type-raising**. Function composition enables the combination of com-  
 5087 plex types:  $X/Y \circ Y/Z \Rightarrow_B X/Z$  (forward composition) and  $Y\backslash Z \circ X\backslash Y \Rightarrow_B X\backslash Z$  (back-  
 5088 ward composition).<sup>12</sup> Composition makes it possible to "look inside" complex types, and  
 5089 combine two adjacent units if the "input" for one is the "output" for the other. Figure 9.15  
 5090 shows how function composition can be used to handle modal verbs. While this sen-  
 5091 tence can be parsed using only function application, the composition-based analysis is  
 5092 preferable because the unit *might learn* functions just like a transitive verb, as in the exam-  
 5093 ple *Abigail studies Swahili*. This in turn makes it possible to analyze conjunctions such as  
 5094 *Abigail studies and might learn Swahili*, attaching the direct object *Swahili* to the entire con-  
 5095 joined verb phrase *studies and might learn*. The Penn Treebank grammar fragment from  
 5096 § 9.2.3 would be unable to handle this case correctly: the direct object *Swahili* could attach  
 5097 only to the second verb *learn*.

5098 Type raising converts an element of type  $X$  to a more complex type:  $X \Rightarrow_T T/(T\backslash X)$   
 5099 (forward type-raising to type  $T$ ), and  $X \Rightarrow_T T\backslash(T/X)$  (backward type-raising to type  
 5100  $T$ ). Type-raising makes it possible to reverse the relationship between a function and its  
 5101 argument — by transforming the argument into a function over functions over arguments!  
 5102 An example may help. Figure 9.15 shows how to analyze an object relative clause, *a story*  
 5103 *that Abigail tells*. The problem is that *tells* is a transitive verb, expecting a direct object to  
 5104 its right. As a result, *Abigail tells* is not a valid constituent. The issue is resolved by raising

<sup>12</sup>The subscript **B** follows notation from Curry and Feys (1958).

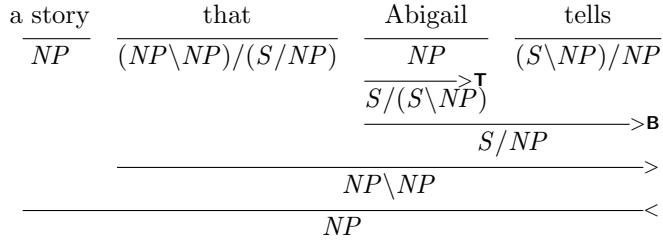


Figure 9.16: A syntactic analysis in CCG involving an object relative clause (based on slides from Alex Clark)

5105 *Abigail* from NP to the complex type  $(S / NP) \setminus NP$ . This function can then be combined  
 5106 with the transitive verb *tells* by forward composition, resulting in the type  $(S / NP)$ , which  
 5107 is a sentence lacking a direct object to its right.<sup>13</sup> From here, we need only design the  
 5108 lexical entry for the complementizer *that* to expect a right neighbor of type  $(S / NP)$ , and  
 5109 the remainder of the derivation can proceed by function application.

5110 Composition and type-raising give CCG considerable power and flexibility, but at a  
 5111 price. The simple sentence *Abigail tells Max* can be parsed in two different ways: by func-  
 5112 tion application (first forming the verb phrase *tells Max*), and by type-raising and compo-  
 5113 sition (first forming the non-constituent *Abigail tells*). This **derivational ambiguity** does  
 5114 not affect the resulting linguistic analysis, so it is sometimes known as **spurious ambi-**  
 5115 **guity**. Hockenmaier and Steedman (2007) present a translation algorithm for converting  
 5116 the Penn Treebank into CCG derivations, using composition and type-raising only when  
 5117 necessary.

## 5118 Exercises

- 5119 1. Sketch out the state diagram for finite-state acceptors for the following languages  
 5120 on the alphabet  $\{a, b\}$ .
- 5121 a) Even-length strings. (Be sure to include 0 as an even number.)
- 5122 b) Strings that contain *aaa* as a substring.
- 5123 c) Strings containing an even number of *a* and an odd number of *b* symbols.
- 5124 d) Strings in which the substring *bbb* must be terminal if it appears — the string  
 5125 need not contain *bbb*, but if it does, nothing can come after it.
- 5126 2. Levenshtein edit distance is the number of insertions, substitutions, or deletions  
 5127 required to convert one string to another.

---

<sup>13</sup>The missing direct object would be analyzed as a **trace** in CFG-like approaches to syntax, including the Penn Treebank.

- 5128        a) Define a finite-state acceptor that accepts all strings with edit distance 1 from  
 5129            the target string, *target*.  
 5130        b) Now think about how to generalize your design to accept all strings with edit  
 5131            distance from the target string equal to  $d$ . If the target string has length  $\ell$ , what  
 5132            is the minimal number of states required?
- 5133     3. Construct an FSA in the style of Figure 9.3, which handles the following examples:

- 5134        • *nation*/N, *national*/ADJ, *nationalize*/V, *nationalizer*/N  
 5135        • *America*/N, *American*/ADJ, *Americanize*/V, *Americanizer*/N

5136     Be sure that your FSA does not accept any further derivations, such as *\*nationalizeral*  
 5137     and *\*Americanizern*.

- 5138     4. Show how to construct a trigram language model in a weighted finite-state acceptor.  
 5139     Make sure that you handle the edge cases at the beginning and end of the sequence  
 5140     accurately.
- 5141     5. Extend the FST in Figure 9.6 to handle the other two parts of rule 1a of the Porter  
 5142     stemmer: *-sses* → *ss*, and *-ies* → *-i*.

- 5143     6. § 9.1.4.4 describes  $T_O$ , a transducer that captures English orthography by transduc-  
 5144        ing *cook + ed* → *cooked* and *bake + ed* → *baked*. Design an unweighted finite-state  
 5145        transducer that captures this property of English orthography.

5146     Next, augment the transducer to appropriately model the suffix *-s* when applied to  
 5147     words ending in *s*, e.g. *kiss+s* → *kisses*.

- 5148     7. Add parenthesization to the grammar in Figure 9.11 so that it is no longer ambigu-  
 5149     ous.
- 5150     8. Construct three examples — a noun phrase, a verb phrase, and a sentence — which  
 5151        can be derived from the Penn Treebank grammar fragment in § 9.2.3, yet are not  
 5152        grammatical. Avoid reusing examples from the text. Optionally, propose corrections  
 5153        to the grammar to avoid generating these cases.

- 5154     9. Produce parses for the following sentences, using the Penn Treebank grammar frag-  
 5155        ment from § 9.2.3.

- 5156        (9.19) This aggression will not stand.  
 5157        (9.20) I can get you a toe.  
 5158        (9.21) Sometimes you eat the bar and sometimes the bar eats you.

5159     Then produce parses for three short sentences from a news article from this week.

5160 10. \* One advantage of CCG is its flexibility in handling coordination:

5161 (9.22) *Abigail and Max speak Swahili*

5162 (9.23) *Abigail speaks and Max understands Swahili*

Define the lexical entry for *and* as

$$\text{and} := (X/X) \setminus X, \quad [9.77]$$

5163 where  $X$  can refer to any type. Using this lexical entry, show how to parse the two  
5164 examples above. In the second example, *Swahili* should be combined with the coor-  
5165 dination *Abigail speaks and Max understands*, and not just with the verb *understands*.

5166 

## Chapter 10

5167 

# Context-free parsing

5168 Parsing is the task of determining whether a string can be derived from a given context-  
5169 free grammar, and if so, how. The parse structure can answer basic questions of who-did-  
5170 what-to-whom, and is useful for various downstream tasks, such as semantic analysis  
5171 (chapter 12 and 13) and information extraction (chapter 17).

For a given input and grammar, how many parse trees are there? Consider a minimal context-free grammar with only one non-terminal,  $X$ , and the following productions:

$$\begin{aligned} X \rightarrow & X \ X \\ X \rightarrow & aardvark \mid abacus \mid \dots \mid zyther \end{aligned}$$

The second line indicates unary productions to every nonterminal in  $\Sigma$ . In this grammar, the number of possible derivations for a string  $w$  is equal to the number of binary bracketings, e.g.,

$$(((w_1 w_2) w_3) w_4) w_5), \quad (((w_1 (w_2 w_3)) w_4) w_5), \quad ((w_1 (w_2 (w_3 w_4))) w_5), \quad \dots$$

5172 The number of such bracketings is a **Catalan number**, which grows super-exponentially  
5173 in the length of the sentence,  $C_n = \frac{(2n)!}{(n+1)n!}$ . As with sequence labeling, it is only possible to  
5174 exhaustively search the space of parses by resorting to locality assumptions, which make it  
5175 possible to search efficiently by reusing shared substructures with dynamic programming.  
5176 This chapter focuses on a bottom-up dynamic programming algorithm, which enables  
5177 exhaustive search of the space of possible parses, but imposes strict limitations on the  
5178 form of scoring function. These limitations can be relaxed by abandoning exhaustive  
5179 search. Non-exact search methods will be briefly discussed at the end of this chapter, and  
5180 one of them — **transition-based parsing** — will be the focus of chapter 11.

S	$\rightarrow$	NP VP
NP	$\rightarrow$	NP PP   <i>we</i>   <i>sushi</i>   <i>chopsticks</i>
PP	$\rightarrow$	IN NP
IN	$\rightarrow$	<i>with</i>
VP	$\rightarrow$	V NP   VP PP
V	$\rightarrow$	<i>eat</i>

Table 10.1: A toy example context-free grammar

## 5181 10.1 Deterministic bottom-up parsing

5182 The **CKY algorithm**<sup>1</sup> is a bottom-up approach to parsing in a context-free grammar. It  
 5183 efficiently tests whether a string is in a language, without enumerating all possible parses.  
 5184 The algorithm first forms small constituents, and then tries to merge them into larger  
 5185 constituents.

5186 To understand the algorithm, consider the input, *We eat sushi with chopsticks*. According-  
 5187 ing to the toy grammar in Table 10.1, each terminal symbol can be generated by exactly  
 5188 one unary production, resulting in the sequence NP V NP IN NP. The next step is to  
 5189 try to apply binary productions to merge adjacent symbols into larger constituents: for  
 5190 example, V NP can be merged into a verb phrase (VP), and IN NP can be merged into  
 5191 a prepositional phrase (PP). Bottom-up parsing searches for a series of mergers that ulti-  
 5192 mately results in the start symbol S covering the entire input.

5193 The CKY algorithm systematizes this search by incrementally constructing a table  $t$  in  
 5194 which each cell  $t[i, j]$  contains the set of nonterminals that can derive the span  $w_{i+1:j}$ . The  
 5195 algorithm fills in the upper right triangle of the table; it begins with the diagonal, which  
 5196 corresponds to substrings of length 1, and then computes derivations for progressively  
 5197 larger substrings, until reaching the upper right corner  $t[0, M]$ , which corresponds to the  
 5198 entire input,  $w_{1:M}$ . If the start symbol S is in  $t[0, M]$ , then the string  $w$  is in the language  
 5199 defined by the grammar. This process is detailed in Algorithm 13, and the resulting data  
 5200 structure is shown in Figure 10.1. Informally, here's how it works:

- 5201 • Begin by filling in the diagonal: the cells  $t[m - 1, m]$  for all  $m \in \{1, 2, \dots, M\}$ . These  
 5202 cells are filled with terminal productions that yield the individual tokens; for the  
 5203 word  $w_2 = \text{sushi}$ , we fill in  $t[1, 2] = \{\text{NP}\}$ , and so on.
- 5204 • Then fill in the next diagonal, in which each cell corresponds to a subsequence of  
 5205 length two:  $t[0, 2], t[1, 3], \dots, t[M - 2, M]$ . These cells are filled in by looking for  
 5206 binary productions capable of producing at least one entry in each of the cells corre-

---

<sup>1</sup>The name is for Cocke-Kasami-Younger, the inventors of the algorithm. It is a special case **chart parsing**, because its stores reusable computations in a chart-like data structure.

---

**Algorithm 13** The CKY algorithm for parsing a sequence  $w \in \Sigma^*$  in a context-free grammar  $G = (N, \Sigma, R, S)$ , with non-terminals  $N$ , production rules  $R$ , and start symbol  $S$ . The grammar is assumed to be in Chomsky normal form (§ 9.2.1.2). The function  $\text{PICKFROM}(b[i, j, X])$  selects an element of the set  $b[i, j, X]$  arbitrarily. All values of  $t$  and  $b$  are initialized to  $\emptyset$ .

---

```

1: procedure CKY( $w, G = (N, \Sigma, R, S)$ )
2:   for  $m \in \{1 \dots M\}$  do
3:      $t[m - 1, m] \leftarrow \{X : (X \rightarrow w_m) \in R\}$ 
4:   for  $\ell \in \{2, 3, \dots, M\}$  do                                 $\triangleright$  Iterate over constituent lengths
5:     for  $m \in \{0, 1, \dots, M - \ell\}$  do           $\triangleright$  Iterate over left endpoints
6:       for  $k \in \{m + 1, m + 2, \dots, m + \ell - 1\}$  do       $\triangleright$  Iterate over split points
7:         for  $(X \rightarrow Y Z) \in R$  do           $\triangleright$  Iterate over rules
8:           if  $Y \in t[m, k] \wedge Z \in t[k, m + \ell]$  then
9:              $t[m, m + \ell] \leftarrow t[m, m + \ell] \cup X$            $\triangleright$  Add non-terminal to table
10:             $b[m, m + \ell, X] \leftarrow b[m, m + \ell, X] \cup (Y, Z, k)$        $\triangleright$  Add back-pointers
11:   if  $S \in t[0, M]$  then
12:     return TRACEBACK( $S, 0, M, b$ )
13:   else
14:     return  $\emptyset$ 
15: procedure TRACEBACK( $X, i, j, b$ )
16:   if  $j = i + 1$  then
17:     return  $X$ 
18:   else
19:      $(Y, Z, k) \leftarrow \text{PICKFROM}(b[i, j, X])$ 
20:     return  $X \rightarrow (\text{TRACEBACK}(Y, i, k, b), \text{TRACEBACK}(Z, k, j, b))$ 

```

---

5207 sponding to left and right children. For example, the cell  $t[1, 3]$  includes VP because  
 5208 the grammar includes the production  $\text{VP} \rightarrow \text{V NP}$ , and the chart contains  $\text{V} \in t[1, 2]$   
 5209 and  $\text{NP} \in t[2, 3]$ .

- 5210 • At the next diagonal, the entries correspond to spans of length three. At this level,  
 5211 there is an additional decision at each cell: where to split the left and right children.  
 5212 The cell  $t[i, j]$  corresponds to the subsequence  $w_{i+1:j}$ , and we must choose some  
 5213 *split point*  $i < k < j$ , so that  $w_{i+1:k}$  is the left child and  $w_{k+1:j}$  is the right child. We  
 5214 consider all possible  $k$ , looking for productions that generate elements in  $t[i, k]$  and  
 5215  $t[k, j]$ ; the left-hand side of all such productions can be added to  $t[i, j]$ . When it is  
 5216 time to compute  $t[i, j]$ , the cells  $t[i, k]$  and  $t[k, j]$  are guaranteed to be complete, since  
 5217 these cells correspond to shorter sub-strings of the input.

- 5218 • The process continues until we reach  $t[0, M]$ .

5219 Figure 10.1 shows the chart that arises from parsing the sentence *We eat sushi with chop-*  
 5220 *sticks* using the grammar defined above.

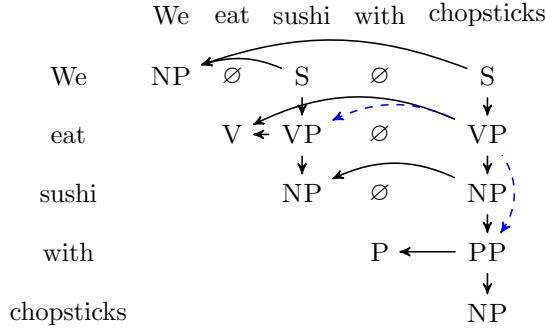


Figure 10.1: An example completed CKY chart. The solid and dashed lines show the back pointers resulting from the two different derivations of VP in position  $t[1, 5]$ .

### 5221 10.1.1 Recovering the parse tree

5222 As with the Viterbi algorithm, it is possible to identify a successful parse by storing and  
 5223 traversing an additional table of back-pointers. If we add an entry  $X$  to cell  $t[i, j]$  by using  
 5224 the production  $X \rightarrow YZ$  and the split point  $k$ , then we store the back-pointer  $b[i, j, X] =$   
 5225  $(Y, Z, k)$ . Once the table is complete, we can recover a parse by tracing this pointers,  
 5226 starting at  $b[0, M, S]$ , and stopping when they ground out at terminal productions.

5227 For ambiguous sentences, there will be multiple paths to reach  $S \in t[0, M]$ . For exam-  
 5228 ple, in Figure 10.1, the goal state  $S \in t[0, M]$  is reached through the state  $VP \in t[1, 5]$ , and  
 5229 there are two different ways to generate this constituent: one with *(eat sushi)* and *(with  
 5230 chopsticks)* as children, and another with *(eat)* and *(sushi with chopsticks)* as children. The  
 5231 presence of multiple paths indicates that the input can be generated by the grammar in  
 5232 more than one way. In Algorithm 13, one of these derivations is selected arbitrarily. As  
 5233 discussed in § 10.3, **weighted context-free grammars** can select a single parse that maxi-  
 5234 mizes a scoring function.

### 5235 10.1.2 Non-binary productions

5236 The CKY algorithm assumes that all productions with non-terminals on the right-hand  
 5237 side (RHS) are binary. But in real grammars, such as the one considered in chapter 9,  
 5238 there will be productions with more than two elements on the right-hand side, and other  
 5239 productions with only a single element.

- 5240 • Productions with more than two elements on the right-hand side can be **binarized**  
 5241 by creating additional non-terminals, as described in § 9.2.1.2. For example, given  
 5242 the production  $VP \rightarrow V NP NP$  (for ditransitive verbs), we can convert to  $VP \rightarrow$   
 5243  $VP_{ditrans}/NP NP$ , and then add the production  $VP_{ditrans}/NP \rightarrow V NP$ .

- What about unary productions like  $VP \rightarrow V$ ? In practice, this is handled by making a second pass on each diagonal, in which each cell  $t[i, j]$  is augmented with all possible unary productions capable of generating each item already in the cell — formally,  $t[i, j]$  is extended to its **unary closure**. Suppose the example grammar in Table 10.1 were extended to include the production  $VP \rightarrow V$ , enabling sentences with intransitive verb phrases, like *we eat*. Then the cell  $t[1, 2]$  — corresponding to the word *eat* — would first include the set  $\{V\}$ , and would be augmented to the set  $\{V, VP\}$  during this second pass.

### 10.1.3 Complexity

For an input of length  $M$  and a grammar with  $R$  productions and  $N$  non-terminals, the space complexity of the CKY algorithm is  $\mathcal{O}(M^2N)$ : the number of cells in the chart is  $\mathcal{O}(M^2)$ , and each cell must hold  $\mathcal{O}(N)$  elements. The time complexity is  $\mathcal{O}(M^3R)$ : each cell is computed by searching over  $\mathcal{O}(M)$  split points, with  $R$  possible productions for each split point. Both the time and space complexity are considerably worse than the Viterbi algorithm, which is linear in the length of the input.

## 10.2 Ambiguity

Syntactic ambiguity is endemic to natural language. Here are a few broad categories:

- **Attachment ambiguity:** e.g., *We eat sushi with chopsticks, I shot an elephant in my pajamas*. In these examples, the prepositions (*with, in*) can attach to either the verb or the direct object.
- **Modifier scope:** e.g., *southern food store, plastic cup holder*. In these examples, the first word could be modifying the subsequent adjective, or the final noun.
- **Particle versus preposition:** e.g., *The puppy tore up the staircase*. Phrasal verbs like *tore up* often include particles which could also act as prepositions. This has structural implications: if *up* is a preposition, then *up the staircase* is a prepositional phrase; if *up* is a particle, then *the staircase* is the direct object to the verb.
- **Complement structure:** e.g., *The students complained to the professor that they didn't understand*. This is another form of attachment ambiguity, where the complement *that they didn't understand* could attach to the main verb (*complained*), or to the indirect object (*the professor*).
- **Coordination scope:** e.g., *"I see," said the blind man, as he picked up the hammer and saw*. In this example, the lexical ambiguity for *saw* enables it to be coordinated either with the noun *hammer* or the verb *picked up*.

These forms of ambiguity can combine, so that seemingly simple headlines like *Fed raises interest rates* have dozens of possible analyses even in a minimal grammar. In a broad coverage grammar, typical sentences can have millions of parses. While careful grammar design can chip away at this ambiguity, a better strategy is to combine broad coverage parsers with data driven strategies for identifying the correct analysis.

### 10.2.1 Parser evaluation

Before continuing to parsing algorithms that are able to handle ambiguity, we stop to consider how to measure parsing performance. Suppose we have a set of *reference parses* — the ground truth — and a set of *system parses* that we would like to score. A simple solution would be per-sentence accuracy: the parser is scored by the proportion of sentences on which the system and reference parses exactly match.<sup>2</sup> But as any good student knows, it is better to get *partial credit*, which we can assign to analyses that correctly match parts of the reference parse. The PARSEval metrics (Grishman et al., 1992) score each system parse via:

**Precision:** the fraction of constituents in the system parse that match a constituent in the reference parse.

**Recall:** the fraction of constituents in the reference parse that match a constituent in the system parse.

In **labeled precision** and **recall**, the system must also match the phrase type for each constituent; in **unlabeled precision** and **recall**, it is only required to match the constituent structure. As in chapter 4, the precision and recall can be combined into an *F*-MEASURE,  $F = \frac{2 \times P \times R}{P + R}$ .

In Figure 10.2, suppose that the left tree is the system parse and the right tree is the reference parse. We have the following spans:

- $S \rightarrow w_{1:5}$  is *true positive*, because it appears in both trees.
- $VP \rightarrow w_{2:5}$  is *true positive* as well.
- $NP \rightarrow w_{3:5}$  is *false positive*, because it appears only in the system output.
- $PP \rightarrow w_{4:5}$  is *true positive*, because it appears in both trees.
- $VP \rightarrow w_{2:3}$  is *false negative*, because it appears only in the reference.

---

<sup>2</sup>Most parsing papers do not report results on this metric, but Finkel et al. (2008) find that a strong parser finds the exact correct parse on 35% of sentences of length  $\leq 40$ , and on 62% of parses of length  $\leq 15$  in the Penn Treebank.

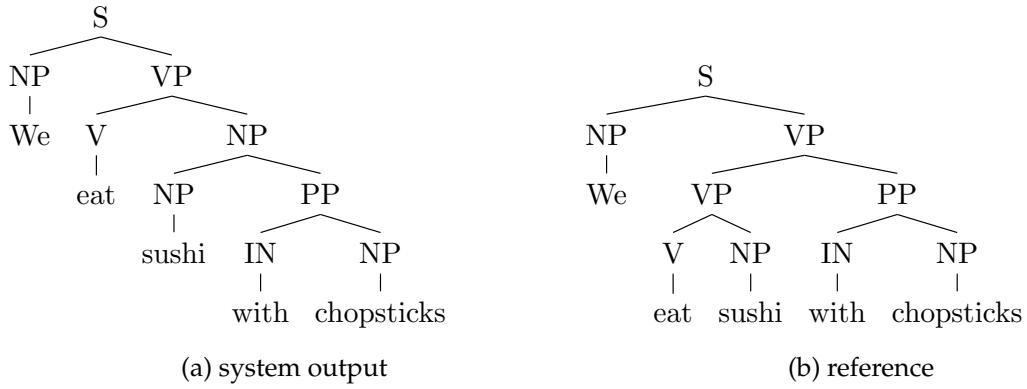


Figure 10.2: Two possible analyses from the grammar in Table 10.1

5306 The labeled and unlabeled precision of this parse is  $\frac{3}{4} = 0.75$ , and the recall is  $\frac{3}{4} = 0.75$ , for  
 5307 an F-measure of 0.75. For an example in which precision and recall are not equal, suppose  
 5308 the reference parse instead included the production  $VP \rightarrow V NP PP$ . In this parse, the  
 5309 reference does not contain the constituent  $w_{2:3}$ , so the recall would be 1.<sup>3</sup>

## 5310 10.2.2 Local solutions

5311 Some ambiguity can be resolved locally. Consider the following examples,

5312 (10.1) We met the President on Monday.

5313 (10.2) We met the President of Mexico.

Each case ends with a preposition, which can be attached to the verb *met* or the noun phrase *the president*. This ambiguity can be resolved by using a labeled corpus to compare the likelihood of observing the preposition alongside each candidate attachment point,

$$p(on \mid met) \geq p(on \mid President) \quad [10.1]$$

$$p(of \mid met) \geq p(of \mid President). \quad [10.2]$$

5314 A comparison of these probabilities would successfully resolve this case (Hindle and  
5315 Rooth, 1993). Other cases, such as the example ... *eat sushi with chopsticks*, require consider-  
5316 ing the object of the preposition — consider the alternative ... *eat sushi with soy sauce*. With  
5317 sufficient labeled data, the problem of prepositional phrase attachment can be treated as  
5318 a classification task (Ratnaparkhi et al., 1994).

---

<sup>3</sup>While the grammar must be binarized before applying the CKY algorithm, evaluation is performed on the original parses. It is therefore necessary to “unbinarize” the output of a CKY-based parser, converting it back to the original grammar.

5319     However, there are inherent limitations to local solutions. While toy examples may  
 5320   have just a few ambiguities to resolve, realistic sentences have thousands or millions of  
 5321   possible parses. Furthermore, attachment decisions are interdependent, as shown in the  
 5322   garden path example:

5323   (10.3) Cats scratch people with claws with knives.

5324   We may want to attach *with claws* to *scratch*, as would be correct in the shorter sentence  
 5325   in *cats scratch people with claws*. But this leaves nowhere to attach *with knives*. The cor-  
 5326   rect interpretation can be identified only by considering the attachment decisions jointly.  
 5327   The huge number of potential parses may seem to make exhaustive search impossible.  
 5328   But as with sequence labeling, locality assumptions make it possible to search this space  
 5329   efficiently.

### 5330   10.3 Weighted Context-Free Grammars

5331   Let us define a derivation  $\tau$  as a set of **anchored productions**,

$$\tau = \{X \rightarrow \alpha, (i, j, k)\}, \quad [10.3]$$

5332   with  $X$  corresponding to the left-hand side non-terminal and  $\alpha$  corresponding to the right-  
 5333   hand side. For grammars in Chomsky normal form,  $\alpha$  is either a pair of non-terminals or  
 5334   a terminal symbol. The indices  $i, j, k$  anchor the production in the input, with  $X$  deriving  
 5335   the span  $w_{i+1:j}$ . For binary productions,  $w_{i+1:k}$  indicates the span of the left child, and  
 5336    $w_{k+1:j}$  indicates the span of the right child; for unary productions,  $k$  is ignored. For an  
 5337   input  $w$ , the optimal parse is then,

$$\hat{\tau} = \underset{\tau \in \mathcal{T}(w)}{\operatorname{argmax}} \Psi(\tau), \quad [10.4]$$

5338   where  $\mathcal{T}(w)$  is the set of derivations that yield the input  $w$ .

5339   The scoring function  $\Psi$  decomposes across anchored productions,

$$\Psi(\tau) = \sum_{(X \rightarrow \alpha, (i, j, k)) \in \tau} \psi(X \rightarrow \alpha, (i, j, k)). \quad [10.5]$$

5340   This is a locality assumption, akin to the assumption in Viterbi sequence labeling. In this  
 5341   case, the assumption states that the overall score is a sum over scores of productions,  
 5342   which are computed independently. In a **weighted context-free grammar** (WCFG), the  
 5343   score of each anchored production  $X \rightarrow (\alpha, i, j, k)$  is simply  $\psi(X \rightarrow \alpha)$ , ignoring the  
 5344   anchors  $(i, j, k)$ . In other parsing models, the anchors can be used to access features of the  
 5345   input, while still permitting efficient bottom-up parsing.

		$\psi(\cdot)$	$\exp \psi(\cdot)$
S	$\rightarrow \text{NP VP}$	0	1
NP	$\rightarrow \text{NP PP}$	-1	$\frac{1}{2}$
	$\rightarrow \text{we}$	-2	$\frac{1}{4}$
	$\rightarrow \text{sushi}$	-3	$\frac{1}{8}$
	$\rightarrow \text{chopsticks}$	-3	$\frac{1}{8}$
PP	$\rightarrow \text{IN NP}$	0	1
IN	$\rightarrow \text{with}$	0	1
VP	$\rightarrow \text{V NP}$	-1	$\frac{1}{2}$
	$\rightarrow \text{VP PP}$	-2	$\frac{1}{4}$
	$\rightarrow \text{MD V}$	-2	$\frac{1}{4}$
V	$\rightarrow \text{eat}$	0	1

Table 10.2: An example weighted context-free grammar (WCFG). The weights are chosen so that  $\exp \psi(\cdot)$  sums to one over right-hand sides for each non-terminal; this is required by probabilistic context-free grammars, but not by WCFGs in general.

**Example** Consider the weighted grammar shown in Table 10.2, and the analysis in Figure 10.2b.

$$\begin{aligned} \Psi(\tau) &= \psi(S \rightarrow \text{NP VP}) + \psi(VP \rightarrow \text{VP PP}) + \psi(VP \rightarrow \text{V NP}) + \psi(PP \rightarrow \text{IN NP}) \\ &\quad + \psi(NP \rightarrow \text{We}) + \psi(V \rightarrow \text{eat}) + \psi(NP \rightarrow \text{sushi}) + \psi(IN \rightarrow \text{with}) + \psi(NP \rightarrow \text{chopsticks}) \end{aligned} \quad [10.6]$$

$$= 0 - 2 - 1 + 0 - 2 + 0 - 3 + 0 - 3 = -11. \quad [10.7]$$

5346 In the alternative parse in Figure 10.2a, the production  $VP \rightarrow VP PP$  (with score -2) is  
 5347 replaced with the production  $NP \rightarrow NP PP$  (with score -1); all other productions are the  
 5348 same. As a result, the score for this parse is -10.

5349 This example hints at a big problem with WCFG parsing on non-terminals such as  
 5350  $NP$ ,  $VP$ , and  $PP$ : a WCFG will *always* prefer either  $VP$  or  $NP$  attachment, without regard  
 5351 to what is being attached! This problem is addressed in § 10.5.

### 5352 10.3.1 Parsing with weighted context-free grammars

5353 The optimization problem in Equation 10.4 can be solved by modifying the CKY algo-  
 5354 rithm. In the deterministic CKY algorithm, each cell  $t[i, j]$  stored a set of non-terminals  
 5355 capable of deriving the span  $w_{i+1:j}$ . We now augment the table so that the cell  $t[i, j, X]$   
 5356 is the *score of the best derivation of  $w_{i+1:j}$  from non-terminal  $X$* . This score is computed  
 5357 recursively: for the anchored binary production  $(X \rightarrow Y Z, (i, j, k))$ , we compute:

---

**Algorithm 14** CKY algorithm for parsing a string  $w \in \Sigma^*$  in a weighted context-free grammar  $(N, \Sigma, R, S)$ , where  $N$  is the set of non-terminals and  $R$  is the set of weighted productions. The grammar is assumed to be in Chomsky normal form (§ 9.2.1.2). The function TRACEBACK is defined in Algorithm 13.

---

```

procedure WCKY( $w, G = (N, \Sigma, R, S)$ )
  for all  $i, j, X$  do ▷ Initialization
     $t[i, j, X] \leftarrow 0$ 
     $b[i, j, X] \leftarrow \emptyset$ 
  for  $m \in \{1, 2, \dots, M\}$  do
    for all  $X \in N$  do
       $t[m, m + 1, X] \leftarrow \psi(X \rightarrow w_m, (m, m + 1, m))$ 
  for  $\ell \in \{2, 3, \dots, M\}$  do
    for  $m \in \{0, 1, \dots, M - \ell\}$  do
      for  $k \in \{m + 1, m + 2, \dots, m + \ell - 1\}$  do
         $t[m, m + \ell, X] \leftarrow \max_{k, Y, Z} \psi(X \rightarrow Y Z, (m, m + \ell, k)) + t[m, k, Y] + t[k, m + \ell, Z]$ 
         $b[m, m + \ell, X] \leftarrow \operatorname{argmax}_{k, Y, Z} \psi(X \rightarrow Y Z, (m + \ell, k)) + t[m, k, Y] + t[k, m + \ell, Z]$ 
  return TRACEBACK( $S, 0, M, b$ )

```

---

- 5358     • the score of the anchored production,  $\psi(X \rightarrow Y Z, (i, j, k))$ ;
- 5359     • the score of the best derivation of the left child,  $t[i, k, Y]$ ;
- 5360     • the score of the best derivation of the right child,  $t[k, j, Z]$ .

5361 These scores are combined by addition. As in the unscored CKY algorithm, the table  
 5362 is constructed by considering spans of increasing length, so the scores for spans  $t[i, k, Y]$   
 5363 and  $t[k, j, Z]$  are guaranteed to be available at the time we compute the score  $t[i, j, X]$ . The  
 5364 value  $t[0, M, S]$  is the score of the best derivation of  $w$  from the grammar. Algorithm 14  
 5365 formalizes this procedure.

5366 As in unweighted CKY, the parse is recovered from the table of back pointers  $b$ , where  
 5367 each  $b[i, j, X]$  stores the argmax split point  $k$  and production  $X \rightarrow Y Z$  in the derivation of  
 5368  $w_{i+1:j}$  from  $X$ . The best parse can be obtained by tracing these pointers backwards from  
 5369  $b[0, M, S]$ , all the way to the terminal symbols. This is analogous to the computation of the  
 5370 best sequence of labels in the Viterbi algorithm by tracing pointers backwards from the  
 5371 end of the trellis. Note that we need only store back-pointers for the *best* path to  $t[i, j, X]$ ;  
 5372 this follows from the locality assumption that the global score for a parse is a combination  
 5373 of the local scores of each production in the parse.

**Example** Let's revisit the parsing table in Figure 10.1. In a weighted CFG, each cell would include a score for each non-terminal; non-terminals that cannot be generated are

---

**Algorithm 15** Generative model for derivations from probabilistic context-free grammars in Chomsky Normal Form (CNF).

---

```

procedure DRAWSUBTREE(X)
    sample  $(X \rightarrow \alpha) \sim p(\alpha | X)$ 
    if  $\alpha = (Y Z)$  then
        return DRAWSUBTREE(Y)  $\cup$  DRAWSUBTREE(Z)
    else
        return  $(X \rightarrow \alpha)$             $\triangleright$  In CNF, all unary productions yield terminal symbols

```

---

assumed to have a score of  $-\infty$ . The first diagonal contains the scores of unary productions:  $t[0, 1, \text{NP}] = -2$ ,  $t[1, 2, \text{V}] = 0$ , and so on. At the next diagonal, we compute the scores for spans of length 2:  $t[1, 3, \text{VP}] = -1 + 0 - 3 = -4$ ,  $t[3, 5, \text{PP}] = 0 + 0 - 3 = -3$ , and so on. Things get interesting when we reach the cell  $t[1, 5, \text{VP}]$ , which contains the score for the derivation of the span  $w_{2:5}$  from the non-terminal VP. This score is computed as a max over two alternatives,

$$t[1, 5, \text{VP}] = \max(\psi(\text{VP} \rightarrow \text{VP PP}, (1, 3, 5)) + t[1, 3, \text{VP}] + t[3, 5, \text{PP}], \\ \psi(\text{VP} \rightarrow \text{V NP}, (1, 2, 5)) + t[1, 2, \text{V}] + t[2, 5, \text{NP}]) \quad [10.8]$$

$$= \max(-2 - 4 - 3, -1 + 0 - 7) = -8. \quad [10.9]$$

5374 Since the second case is the argmax, we set the back-pointer  $b[1, 5, \text{VP}] = (\text{V}, \text{NP}, 2)$ , enabling  
5375 the optimal derivation to be recovered.

### 5376 10.3.2 Probabilistic context-free grammars

5377 **Probabilistic context-free grammars (PCFGs)** are a special case of weighted context-  
5378 free grammars that arises when the weights correspond to probabilities. Specifically, the  
5379 weight  $\psi(X \rightarrow \alpha, (i, j, k)) = \log p(\alpha | X)$ , where the probability of the right-hand side  
5380  $\alpha$  is conditioned on the non-terminal  $X$ . These probabilities must be normalized over all  
5381 possible right-hand sides, so that  $\sum_\alpha p(\alpha | X) = 1$ , for all  $X$ . For a given parse  $\tau$ , the prod-  
5382 uct of the probabilities of the productions is equal to  $p(\tau)$ , under the **generative model**  
5383  $\tau \sim \text{DRAWSUBTREE}(S)$ , where the function DRAWSUBTREE is defined in Algorithm 15.

5384 The conditional probability of a parse given a string is,

$$p(\tau | w) = \frac{p(\tau)}{\sum_{\tau' \in \mathcal{T}(w)} p(\tau')} = \frac{\exp \Psi(\tau)}{\sum_{\tau' \in \mathcal{T}(w)} \exp \Psi(\tau')}, \quad [10.10]$$

5385 where  $\Psi(\tau) = \sum_{X \rightarrow \alpha, (i, j, k) \in \tau} \psi(X \rightarrow \alpha)$ ; the anchor is ignored. Because the probability  
5386 is monotonic in the score  $\Psi(\tau)$ , the maximum likelihood parse can be identified by the  
5387 CKY algorithm without modification. If a normalized probability  $p(\tau | w)$  is required,  
5388 the denominator of Equation 10.10 can be computed by the **inside recurrence**, described  
5389 below.

**Example** The WCFG in Table 10.2 is designed so that the weights are log-probabilities, satisfying the constraint  $\sum_{\alpha} \exp \psi(X \rightarrow \alpha) = 1$ . As noted earlier, there are two parses in  $\mathcal{T}$ (*we eat sushi with chopsticks*), with scores  $\Psi(\tau_1) = \log p(\tau_1) = -10$  and  $\Psi(\tau_2) = \log p(\tau_2) = -11$ . Therefore, the conditional probability  $p(\tau_1 | \mathbf{w})$  is equal to,

$$p(\tau_1 | \mathbf{w}) = \frac{p(\tau_1)}{p(\tau_1) + p(\tau_2)} = \frac{\exp \Psi(\tau_1)}{\exp \Psi(\tau_1) + \exp \Psi(\tau_2)} = \frac{2^{-10}}{2^{-10} + 2^{-11}} = \frac{2}{3}. \quad [10.11]$$

5390 **The inside recurrence** The denominator of Equation 10.10 can be viewed as a language  
5391 model, summing over all valid derivations of the string  $\mathbf{w}$ ,

$$p(\mathbf{w}) = \sum_{\tau': \text{yield}(\tau') = \mathbf{w}} p(\tau'). \quad [10.12]$$

Just as the CKY algorithm makes it possible to maximize over all such analyses, with a few modifications it can also compute their sum. Each cell  $t[i, j, X]$  must store the log probability of deriving  $\mathbf{w}_{i+1:j}$  from non-terminal  $X$ . To compute this, we replace the maximization over split points  $k$  and productions  $X \rightarrow Y Z$  with a “log-sum-exp” operation, which exponentiates the log probabilities of the production and the children, sums them in probability space, and then converts back to the log domain:

$$t[i, j, X] = \log \sum_{k, Y, Z} \exp (\psi(X \rightarrow Y Z) + t[i, k, Y] + t[k, j, Z]) \quad [10.13]$$

$$= \log \sum_{k, Y, Z} \exp (\log p(Y Z | X) + \log p(Y \rightarrow \mathbf{w}_{i+1:k}) + \log p(Z \rightarrow \mathbf{w}_{k+1:j})) \quad [10.14]$$

$$= \log \sum_{k, Y, Z} p(Y Z | X) \times p(Y \rightarrow \mathbf{w}_{i+1:k}) \times p(Z \rightarrow \mathbf{w}_{k+1:j}) \quad [10.15]$$

$$= \log \sum_{k, Y, Z} p(Y Z, \mathbf{w}_{i+1:k}, \mathbf{w}_{k+1:j} | X) \quad [10.16]$$

$$= \log p(X \rightarrow \mathbf{w}_{i+1:j}). \quad [10.17]$$

5392 This is called the **inside recurrence**, because it computes the probability of each subtree  
5393 as a combination of the probabilities of the smaller subtrees that are inside of it. The  
5394 name implies a corresponding **outside recurrence**, which computes the probability of  
5395 a non-terminal  $X$  spanning  $\mathbf{w}_{i+1:j}$ , joint with the outside context  $(\mathbf{w}_{1:i}, \mathbf{w}_{j+1:M})$ . This  
5396 recurrence is described in § 10.4.3. The inside and outside recurrences are analogous to the  
5397 forward and backward recurrences in probabilistic sequence labeling (see § 7.5.3.3). They  
5398 can be used to compute the marginal probabilities of individual anchored productions,  
5399  $p(X \rightarrow \alpha, (i, j, k) | \mathbf{w})$ , summing over all possible derivations of  $\mathbf{w}$ .

5400 **10.3.3 \*Semiring weighted context-free grammars**

The weighted and unweighted CKY algorithms can be unified with the inside recurrence using the same semiring notation described in § 7.7.3. The generalized recurrence is:

$$t[i, j, X] = \bigoplus_{k, Y, Z} \psi(X \rightarrow Y Z, (i, j, k)) \otimes t[i, k, Y] \otimes t[k, j, Z]. \quad [10.18]$$

5401 This recurrence subsumes all of the algorithms that we have encountered in this chapter.

5402 **Unweighted CKY.** When  $\psi(X \rightarrow \alpha, (i, j, k))$  is a *Boolean truth value*  $\{\top, \perp\}$ ,  $\otimes$  is logical  
5403 conjunction, and  $\bigoplus$  is logical disjunction, then we derive the CKY recurrence for  
5404 unweighted context-free grammars, discussed in § 10.1 and Algorithm 13.

5405 **Weighted CKY.** When  $\psi(X \rightarrow \alpha, (i, j, k))$  is a scalar score,  $\otimes$  is addition, and  $\bigoplus$  is maxi-  
5406 maximization, then we derive the CKY recurrence for weighted context-free grammars,  
5407 discussed in § 10.3 and Algorithm 14. When  $\psi(X \rightarrow \alpha, (i, j, k)) = \log p(\alpha \mid X)$ ,  
5408 this same setting derives the CKY recurrence for finding the maximum likelihood  
5409 derivation in a probabilistic context-free grammar.

5410 **Inside recurrence.** When  $\psi(X \rightarrow \alpha, (i, j, k))$  is a log probability,  $\otimes$  is addition, and  $\bigoplus =$   
5411  $\log \sum \exp$ , then we derive the inside recurrence for probabilistic context-free gram-  
5412 mmars, discussed in § 10.3.2. It is also possible to set  $\psi(X \rightarrow \alpha, (i, j, k))$  directly equal  
5413 to the probability  $p(\alpha \mid X)$ . In this case,  $\otimes$  is multiplication, and  $\bigoplus$  is addition.  
5414 While this may seem more intuitive than working with log probabilities, there is the  
5415 risk of underflow on long inputs.

5416 Regardless of how the scores are combined, the key point is the locality assumption:  
5417 the score for a derivation is the combination of the independent scores for each anchored  
5418 production, and these scores do not depend on any other part of the derivation. For exam-  
5419 ple, if two non-terminals are siblings, the scores of productions from these non-terminals  
5420 are computed independently. This locality assumption is analogous to the first-order  
5421 Markov assumption in sequence labeling, where the score for transitions between tags  
5422 depends only on the previous tag and current tag, and not on the history. As with se-  
5423 quence labeling, this assumption makes it possible to find the optimal parse efficiently; its  
5424 linguistic limitations are discussed in § 10.5.

5425 **10.4 Learning weighted context-free grammars**

5426 Like sequence labeling, context-free parsing is a form of structure prediction. As a result,  
5427 WCFGs can be learned using the same set of algorithms: generative probabilistic models,  
5428 structured perceptron, maximum conditional likelihood, and maximum margin learning.

5429 In all cases, learning requires a **treebank**, which is a dataset of sentences labeled with  
 5430 context-free parses. Parsing research was catalyzed by the **Penn Treebank** (Marcus et al.,  
 5431 1993), the first large-scale dataset of this type (see § 9.2.2). Phrase structure treebanks exist  
 5432 for roughly two dozen other languages, with coverage mainly restricted to European and  
 5433 East Asian languages, plus Arabic and Urdu.

5434 **10.4.1 Probabilistic context-free grammars**

Probabilistic context-free grammars are similar to hidden Markov models, in that they are generative models of text. In this case, the parameters of interest correspond to probabilities of productions, conditional on the left-hand side. As with hidden Markov models, these parameters can be estimated by relative frequency:

$$\psi(X \rightarrow \alpha) = \log p(X \rightarrow \alpha) \quad [10.19]$$

$$\hat{p}(X \rightarrow \alpha) = \frac{\text{count}(X \rightarrow \alpha)}{\text{count}(X)}. \quad [10.20]$$

5435 For example, the probability of the production  $NP \rightarrow DET\ NN$  is the corpus count of  
 5436 this production, divided by the count of the non-terminal  $NP$ . This estimator applies  
 5437 to terminal productions as well: the probability of  $NN \rightarrow whale$  is the count of how often  
 5438 *whale* appears in the corpus as generated from an  $NN$  tag, divided by the total count of the  
 5439  $NN$  tag. Even with the largest treebanks — currently on the order of one million tokens  
 5440 — it is difficult to accurately compute probabilities of even moderately rare events, such  
 5441 as  $NN \rightarrow whale$ . Therefore, smoothing is critical for making PCFGs effective.

5442 **10.4.2 Feature-based parsing**

5443 The scores for each production can be computed as an inner product of weights and fea-  
 5444 tures,

$$\psi(X \rightarrow \alpha) = \boldsymbol{\theta} \cdot \mathbf{f}(X, \alpha, (i, j, k), \mathbf{w}), \quad [10.21]$$

5445 where the feature vector  $\mathbf{f}(X, \alpha)$  is a function of the left-hand side  $X$ , the right-hand side  
 5446  $\alpha$ , the anchor indices  $(i, j, k)$ , and the input  $\mathbf{w}$ .

5447 The basic feature  $\mathbf{f}(X, \alpha, (i, j, k)) = \{(X, \alpha)\}$  encodes only the identity of the pro-  
 5448 duction itself, which is a discriminatively-trained model with the same expressiveness as  
 5449 a PCFG. Features on anchored productions can include the words that border the span  
 5450  $w_i, w_{j+1}$ , the word at the split point  $w_{k+1}$ , the presence of a verb or noun in the left child  
 5451 span  $w_{i+1:k}$ , and so on (Durrett and Klein, 2015). Scores on anchored productions can be  
 5452 incorporated into CKY parsing without any modification to the algorithm, because it is  
 5453 still possible to compute each element of the table  $t[i, j, X]$  recursively from its immediate  
 5454 children.

5455 Other features can be obtained by grouping elements on either the left-hand or right-  
 5456 hand side: for example it can be particularly beneficial to compute additional features  
 5457 by clustering terminal symbols, with features corresponding to groups of words with  
 5458 similar syntactic properties. The clustering can be obtained from unlabeled datasets that  
 5459 are much larger than any treebank, improving coverage. Such methods are described in  
 5460 chapter 14.

Feature-based parsing models can be estimated using the usual array of discriminative learning techniques. For example, a structure perceptron update can be computed as (Carreras et al., 2008),

$$\mathbf{f}(\tau, \mathbf{w}^{(i)}) = \sum_{(X \rightarrow \alpha, (i, j, k)) \in \tau} \mathbf{f}(X, \alpha, (i, j, k), \mathbf{w}^{(i)}) \quad [10.22]$$

$$\hat{\tau} = \operatorname{argmax}_{\tau \in \mathcal{T}(\mathbf{w})} \theta \cdot \mathbf{f}(\tau, \mathbf{w}^{(i)}) \quad [10.23]$$

$$\theta \leftarrow \mathbf{f}(\tau^{(i)}, \mathbf{w}^{(i)}) - \mathbf{f}(\hat{\tau}, \mathbf{w}^{(i)}). \quad [10.24]$$

5461 A margin-based objective can be optimized by selecting  $\hat{\tau}$  through cost-augmented decoding (§ 2.3.2), enforcing a margin of  $\Delta(\hat{\tau}, \tau)$  between the hypothesis and the reference parse,  
 5462 where  $\Delta$  is a non-negative cost function, such as the Hamming loss (Stern et al., 2017). It  
 5463 is also possible to train feature-based parsing models by conditional log-likelihood, as  
 5464 described in the next section.

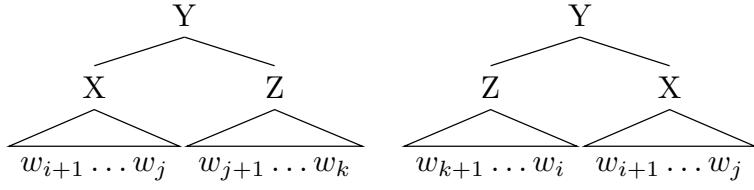
### 5466 10.4.3 \*Conditional random field parsing

5467 The score of a derivation  $\Psi(\tau)$  can be converted into a probability by normalizing over all  
 5468 possible derivations,

$$p(\tau | \mathbf{w}) = \frac{\exp \Psi(\tau)}{\sum_{\tau' \in \mathcal{T}(\mathbf{w})} \exp \Psi(\tau')}. \quad [10.25]$$

5469 Using this probability, a WCFG can be trained by maximizing the conditional log-likelihood  
 5470 of a labeled corpus.

5471 Just as in logistic regression and the conditional random field over sequences, the  
 5472 gradient of the conditional log-likelihood is the difference between the observed and ex-  
 5473 pected counts of each feature. The expectation  $E_{\tau|\mathbf{w}}[\mathbf{f}(\tau, \mathbf{w}^{(i)}); \theta]$  requires summing over  
 5474 all possible parses, and computing the marginal probabilities of anchored productions,  
 5475  $p(X \rightarrow \alpha, (i, j, k) | \mathbf{w})$ . In CRF sequence labeling, marginal probabilities over tag bigrams  
 5476 are computed by the two-pass **forward-backward algorithm** (§ 7.5.3.3). The analogue for  
 5477 context-free grammars is the **inside-outside algorithm**, in which marginal probabilities  
 5478 are computed from terms generated by an upward and downward pass over the parsing  
 5479 chart:

Figure 10.3: The two cases faced by the outside recurrence in the computation of  $\beta(i, j, X)$ 

- The upward pass is performed by the **inside recurrence**, which is described in § 10.3.2. Each inside variable  $\alpha(i, j, X)$  is the score of deriving  $w_{i+1:j}$  from the non-terminal  $X$ . In a PCFG, this corresponds to the log-probability  $\log p(w_{i+1:j} \mid X)$ . This is computed by the recurrence,

$$\alpha(i, j, X) \triangleq \log \sum_{(X \rightarrow Y \ Z)} \sum_{k=i+1}^j \exp (\psi(X \rightarrow Y \ Z, (i, j, k)) + \alpha(i, k, Y) + \alpha(k, j, Z)). \quad [10.26]$$

5480 The initial condition of this recurrence is  $\alpha(m - 1, m, X) = \psi(X \rightarrow w_m)$ . The de-  
5481 nominator  $\sum_{\tau \in \mathcal{T}(w)} \exp \Psi(\tau)$  is equal to  $\exp \alpha(0, M, S)$ .

- The downward pass is performed by the **outside recurrence**, which recursively populates the same table structure, starting at the root of the tree. Each outside variable  $\beta(i, j, X)$  is the score of having a phrase of type  $X$  covering the span  $(i + 1 : j)$ , joint with the exterior context  $w_{1:i}$  and  $w_{j+1:M}$ . In a PCFG, this corresponds to the log probability  $\log p((X, i + 1, j), w_{1:i}, w_{j+1:M})$ . Each outside variable is computed by the recurrence,

$$\exp \beta(i, j, X) \triangleq \sum_{(Y \rightarrow X \ Z)} \sum_{k=j+1}^M \exp [\psi(Y \rightarrow X \ Z, (i, k, j)) + \alpha(j, k, Z) + \beta(i, k, Y)] \quad [10.27]$$

$$+ \sum_{(Y \rightarrow Z \ X)} \sum_{k=0}^{i-1} \exp [\psi(Y \rightarrow Z \ X, (k, i, j)) + \alpha(k, i, Z) + \beta(k, j, Y)]. \quad [10.28]$$

5482 The first line of Equation 10.28 is the score under the condition that  $X$  is a left child  
5483 of its parent, which spans  $w_{i+1:k}$ , with  $k > j$ ; the second line is the score under the  
5484 condition that  $X$  is a right child of its parent  $Y$ , which spans  $w_{k+1:j}$ , with  $k < i$ .  
5485 The two cases are shown in Figure 10.3. In each case, we sum over all possible  
5486 productions with  $X$  on the right-hand side. The parent  $Y$  is bounded on one side

5487 by either  $i$  or  $j$ , depending on whether  $X$  is a left or right child of  $Y$ ; we must sum  
 5488 over all possible values for the other boundary. The initial conditions for the outside  
 5489 recurrence are  $\beta(0, M, S) = 0$  and  $\beta(0, M, X \neq S) = -\infty$ .

The marginal probability of a non-terminal  $X$  over span  $w_{i+1:j}$  is written  $p(X \rightsquigarrow w_{i+1:j} | w)$ , and can be computed from the inside and outside scores,

$$p(X \rightsquigarrow w_{i+1:j} | w) = \frac{p(X \rightsquigarrow w_{i+1:j}, w)}{p(w)} \quad [10.29]$$

$$= \frac{p(w_{i+1:j} | X) \times p(X, w_{1:i}, w_{j+1:M})}{p(w)} \quad [10.30]$$

$$= \frac{\exp(\alpha(i, j, X) + \beta(i, j, X))}{\exp \alpha(0, M, S)}. \quad [10.31]$$

5490 Marginal probabilities of individual productions can be computed similarly (see exercise  
 5491 2). These marginal probabilities can be used for training a conditional random field parser,  
 5492 and also for the task of unsupervised **grammar induction**, in which a PCFG is estimated  
 5493 from a dataset of unlabeled text (Lari and Young, 1990; Pereira and Schabes, 1992).

#### 5494 10.4.4 Neural context-free grammars

5495 Recent work has applied neural representations to parsing, representing each span with  
 5496 a dense numerical vector (Socher et al., 2013; Durrett and Klein, 2015; Cross and Huang,  
 5497 2016).<sup>4</sup> For example, the anchor  $(i, j, k)$  and sentence  $w$  can be associated with a fixed-  
 5498 length column vector,

$$\mathbf{v}_{(i,j,k)} = [\mathbf{u}_{w_{i-1}}; \mathbf{u}_{w_i}; \mathbf{u}_{w_{j-1}}; \mathbf{u}_{w_j}; \mathbf{u}_{w_{k-1}}; \mathbf{u}_{w_k}], \quad [10.32]$$

where  $\mathbf{u}_{w_i}$  is a word embedding associated with the word  $w_i$ . The vector  $\mathbf{v}_{i,j,k}$  can then be passed through a feedforward neural network, and used to compute the score of the anchored production. For example, this score can be computed as a bilinear product (Durrett and Klein, 2015),

$$\tilde{\mathbf{v}}_{(i,j,k)} = \text{FeedForward}(\mathbf{v}_{(i,j,k)}) \quad [10.33]$$

$$\psi(X \rightarrow \alpha, (i, j, k)) = \tilde{\mathbf{v}}_{(i,j,k)}^\top \Theta \mathbf{f}(X \rightarrow \alpha), \quad [10.34]$$

5499 where  $\mathbf{f}(X \rightarrow \alpha)$  is a vector of discrete features of the production, and  $\Theta$  is a parameter  
 5500 matrix. The matrix  $\Theta$  and the parameters of the feedforward network can be learned by  
 5501 backpropagating from an objective such as the margin loss or the negative conditional  
 5502 log-likelihood.

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<sup>4</sup>Earlier work on neural constituent parsing used transition-based parsing algorithms (§ 10.6.2) rather than CKY-style chart parsing (Henderson, 2004; Titov and Henderson, 2007).

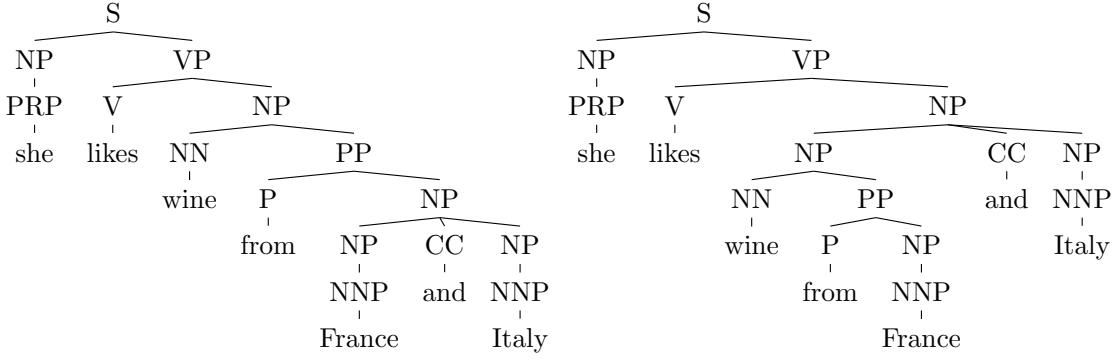


Figure 10.4: The left parse is preferable because of the conjunction of phrases headed by *France* and *Italy*, but these parses cannot be distinguished by a WCFG.

## 5503 10.5 Grammar refinement

5504 The locality assumptions underlying CFG parsing depend on the granularity of the non-  
 5505 terminals. For the Penn Treebank non-terminals, there are several reasons to believe that  
 5506 these assumptions are too strong to enable accurate parsing (Johnson, 1998):

- 5507 • The context-free assumption is too strict: for example, the probability of the produc-  
 5508 tion  $NP \rightarrow NP\ PP$  is much higher (in the PTB) if the parent of the noun phrase is a  
 5509 verb phrase (indicating that the NP is a direct object) than if the parent is a sentence  
 5510 (indicating that the NP is the subject of the sentence).
- 5511 • The Penn Treebank non-terminals are too coarse: there are many kinds of noun  
 5512 phrases and verb phrases, and accurate parsing sometimes requires knowing the  
 5513 difference. As we have already seen, when faced with prepositional phrase at-  
 5514 tachment ambiguity, a weighted CFG will either always choose NP attachment (if  
 5515  $\psi(NP \rightarrow NP\ PP) > \psi(VP \rightarrow VP\ PP)$ ), or it will always choose VP attachment. To  
 5516 get more nuanced behavior, more fine-grained non-terminals are needed.
- 5517 • More generally, accurate parsing requires some amount of **semantics** — understand-  
 5518 ing the meaning of the text to be parsed. Consider the example *cats scratch people with*  
 5519 *claws*: knowledge of about *cats*, *claws*, and scratching is necessary to correctly resolve  
 5520 the attachment ambiguity.

5521 An extreme example is shown in Figure 10.4. The analysis on the left is preferred  
 5522 because of the conjunction of similar entities *France* and *Italy*. But given the non-terminals  
 5523 shown in the analyses, there is no way to differentiate these two parses, since they include  
 5524 exactly the same productions. What is needed seems to be more precise non-terminals.  
 5525 One possibility would be to rethink the linguistics behind the Penn Treebank, and ask

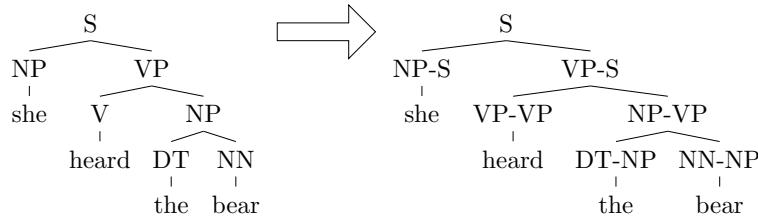


Figure 10.5: Parent annotation in a CFG derivation

5526 the annotators to try again. But the original annotation effort took five years, and there  
 5527 is a little appetite for another annotation effort of this scope. Researchers have therefore  
 5528 turned to automated techniques.

### 5529 10.5.1 Parent annotations and other tree transformations

The key assumption underlying context-free parsing is that productions depend only on the identity of the non-terminal on the left-hand side, and not on its ancestors or neighbors. The validity of this assumption is an empirical question, and it depends on the non-terminals themselves: ideally, every noun phrase (and verb phrase, etc) would be distributionally identical, so the assumption would hold. But in the Penn Treebank, the observed probability of productions often depends on the parent of the left-hand side. For example, noun phrases are more likely to be modified by prepositional phrases when they are in the object position (e.g., *they amused the students from Georgia*) than in the subject position (e.g., *the students from Georgia amused them*). This means that the  $\text{NP} \rightarrow \text{NP PP}$  production is more likely if the entire constituent is the child of a VP than if it is the child of S. The observed statistics are (Johnson, 1998):

$$\Pr(\text{NP} \rightarrow \text{NP PP}) = 11\% \quad [10.35]$$

$$\Pr(\text{NP under S} \rightarrow \text{NP PP}) = 9\% \quad [10.36]$$

$$\Pr(\text{NP under VP} \rightarrow \text{NP PP}) = 23\%. \quad [10.37]$$

5530 This phenomenon can be captured by **parent annotation** (Johnson, 1998), in which each  
 5531 non-terminal is augmented with the identity of its parent, as shown in Figure 10.5). This is  
 5532 sometimes called **vertical Markovization**, since a Markov dependency is introduced be-  
 5533 tween each node and its parent (Klein and Manning, 2003). It is analogous to moving from  
 5534 a bigram to a trigram context in a hidden Markov model. In principle, parent annotation  
 5535 squares the size of the set of non-terminals, which could make parsing considerably less  
 5536 efficient. But in practice, the increase in the number of non-terminals that actually appear  
 5537 in the data is relatively modest (Johnson, 1998).

5538 Parent annotation weakens the WCFG locality assumptions. This improves accuracy  
 5539 by enabling the parser to make more fine-grained distinctions, which better capture real  
 5540 linguistic phenomena. However, each production is more rare, and so careful smoothing  
 5541 or regularization is required to control the variance over production scores.

### 5542 10.5.2 Lexicalized context-free grammars

5543 The examples in § 10.2.2 demonstrate the importance of individual words in resolving  
 5544 parsing ambiguity: the preposition *on* is more likely to attach to *met*, while the preposition  
 5545 *of* is more likely to attachment to *President*. But of all word pairs, which are relevant to  
 5546 attachment decisions? Consider the following variants on the original examples:

- 5547 (10.4) We met the President of Mexico.
- 5548 (10.5) We met the first female President of Mexico.
- 5549 (10.6) They had supposedly met the President on Monday.

5550 The underlined words are the **head words** of their respective phrases: *met* heads the verb  
 5551 phrase, and *President* heads the direct object noun phrase. These heads provide useful  
 5552 semantic information. But they break the context-free assumption, which states that the  
 5553 score for a production depends only on the parent and its immediate children, and not  
 5554 the substructure under each child.

The incorporation of head words into context-free parsing is known as **lexicalization**,  
 and is implemented in rules of the form,

$$\text{NP}(\text{President}) \rightarrow \text{NP}(\text{President}) \text{ PP}(of) \quad [10.38]$$

$$\text{NP}(\text{President}) \rightarrow \text{NP}(\text{President}) \text{ PP}(on). \quad [10.39]$$

5555 Lexicalization was a major step towards accurate PCFG parsing. It requires solving three  
 5556 problems: identifying the heads of all constituents in a treebank; parsing efficiently while  
 5557 keeping track of the heads; and estimating the scores for lexicalized productions.

#### 5558 10.5.2.1 Identifying head words

5559 The head of a constituent is the word that is the most useful for determining how that  
 5560 constituent is integrated into the rest of the sentence.<sup>5</sup> The head word of a constituent is  
 5561 determined recursively: for any non-terminal production, the head of the left-hand side  
 5562 must be the head of one of the children. The head is typically selected according to a set of  
 5563 deterministic rules, sometimes called **head percolation rules**. In many cases, these rules  
 5564 are straightforward: the head of a noun phrase in a  $\text{NP} \rightarrow \text{DET NN}$  production is the head

---

<sup>5</sup>This is a pragmatic definition, befitting our goal of using head words to improve parsing; for a more formal definition, see (Bender, 2013, chapter 7).

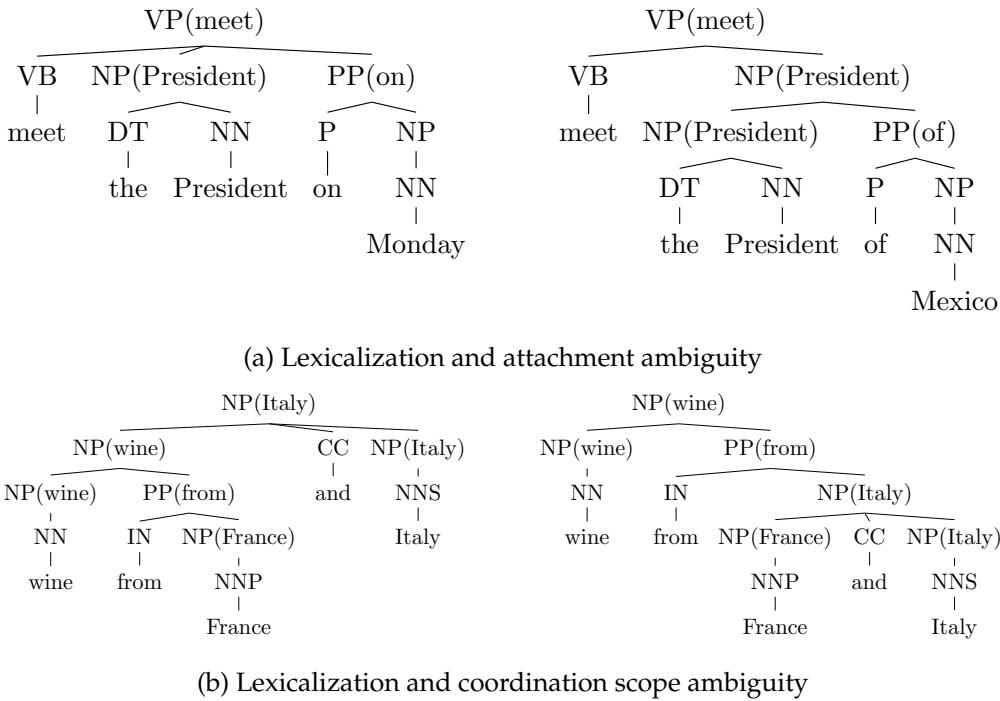


Figure 10.6: Examples of lexicalization

5565 of the noun; the head of a sentence in a  $S \rightarrow NP\ VP$  production is the head of the verb  
 5566 phrase.

5567 Table 10.3 shows a fragment of the head percolation rules used in many English pars-  
 5568 ing systems. The meaning of the first rule is that to find the head of an  $S$  constituent, first  
 5569 look for the rightmost  $VP$  child; if you don't find one, then look for the rightmost  $SBAR$   
 5570 child, and so on down the list. Verb phrases are headed by left verbs (the head of *can plan*  
 5571 *on walking* is *planned*, since the modal verb *can* is tagged *MD*); noun phrases are headed by  
 5572 the rightmost noun-like non-terminal (so the head of *the red cat* is *cat*),<sup>6</sup> and prepositional  
 5573 phrases are headed by the preposition (the head of *at Georgia Tech* is *at*). Some of these  
 5574 rules are somewhat arbitrary — there's no particular reason why the head of *cats and dogs*  
 5575 should be *dogs* — but the point here is just to get some lexical information that can support  
 5576 parsing, not to make deep claims about syntax. Figure 10.6 shows the application of these  
 5577 rules to two of the running examples.

<sup>6</sup>The noun phrase non-terminal is sometimes treated as a special case. Collins (1997) uses a heuristic that looks for the rightmost child which is a noun-like part-of-speech (e.g., *NN*, *NNP*), a possessive marker, or a superlative adjective (e.g., *the greatest*). If no such child is found, the heuristic then looks for the *leftmost*  $NP$ . If there is no child with tag  $NP$ , the heuristic then applies another priority list, this time from right to left.

Non-terminal	Direction	Priority
S	right	VP SBAR ADJP UCP NP
VP	left	VBD VBN MD VBZ TO VB VP VBG VBP ADJP NP
NP	right	N* EX \$ CD QP PRP ...
PP	left	IN TO FW

Table 10.3: A fragment of head percolation rules for English, from <http://www.cs.columbia.edu/~mcollins/papers/heads>

### 5578 10.5.2.2 Parsing lexicalized context-free grammars

5579 A naïve application of lexicalization would simply increase the set of non-terminals by  
 5580 taking the cross-product with the set of terminal symbols, so that the non-terminals now  
 5581 include symbols like  $NP(President)$  and  $VP(meet)$ . Under this approach, the CKY parsing  
 5582 algorithm could be applied directly to the lexicalized production rules. However, the  
 5583 complexity would be cubic in the size of the vocabulary of terminal symbols, which would  
 5584 clearly be intractable.

Another approach is to augment the CKY table with an additional index, keeping track of the head of each constituent. The cell  $t[i, j, h, X]$  stores the score of the best derivation in which non-terminal  $X$  spans  $w_{i+1:j}$  with head word  $h$ , where  $i < h \leq j$ . To compute such a table recursively, we must consider the possibility that each phrase gets its head from either its left or right child. The scores of the best derivations in which the head comes from the left and right child are denoted  $t_\ell$  and  $t_r$  respectively, leading to the following recurrence:

$$t_\ell[i, j, h, X] = \max_{(X \rightarrow Y Z)} \max_{k > h} \max_{k < h' \leq j} t[i, k, h, Y] + t[k, j, h', Z] + \psi(X(h) \rightarrow Y(h)Z(h')) \quad [10.40]$$

$$t_r[i, j, h, X] = \max_{(X \rightarrow Y Z)} \max_{k < h} \max_{i < h' \leq k} t[i, k, h', Y] + t[k, j, h, Z] + (\psi(X(h) \rightarrow Y(h')Z(h))) \quad [10.41]$$

$$t[i, j, h, X] = \max(t_\ell[i, j, h, X], t_r[i, j, h, X]). \quad [10.42]$$

5585 To compute  $t_\ell$ , we maximize over all split points  $k > h$ , since the head word must be in  
 5586 the left child. We then maximize again over possible head words  $h'$  for the right child. An  
 5587 analogous computation is performed for  $t_r$ . The size of the table is now  $\mathcal{O}(M^3N)$ , where  
 5588  $M$  is the length of the input and  $N$  is the number of non-terminals. Furthermore, each  
 5589 cell is computed by performing  $\mathcal{O}(M^2)$  operations, since we maximize over both the split  
 5590 point  $k$  and the head  $h'$ . The time complexity of the algorithm is therefore  $\mathcal{O}(RM^5N)$ ,  
 5591 where  $R$  is the number of rules in the grammar. Fortunately, more efficient solutions are  
 5592 possible. In general, the complexity of parsing can be reduced to  $\mathcal{O}(M^4)$  in the length of

5593 the input; for a broad class of lexicalized CFGs, the complexity can be made cubic in the  
 5594 length of the input, just as in unlexicalized CFGs (Eisner, 2000).

5595 **10.5.2.3 Estimating lexicalized context-free grammars**

5596 The final problem for lexicalized parsing is how to estimate weights for lexicalized pro-  
 5597 ductions  $X(i) \rightarrow Y(j) Z(k)$ . These productions are said to be **bilexical**, because they  
 5598 involve scores over pairs of words: in the example *meet the President of Mexico*, we hope  
 5599 to choose the correct attachment point by modeling the bilexical affinities of (*meet, of*) and  
 5600 (*President, of*). The number of such word pairs is quadratic in the size of the vocabulary,  
 5601 making it difficult to estimate the weights of lexicalized production rules directly from  
 5602 data. This is especially true for probabilistic context-free grammars, in which the weights  
 5603 are obtained from smoothed relative frequency. In a treebank with a million tokens, a  
 5604 vanishingly small fraction of the possible lexicalized productions will be observed more  
 5605 than once.<sup>7</sup> The Charniak (1997) and Collins (1997) parsers therefore focus on approxi-  
 5606 mating the probabilities of lexicalized productions, using various smoothing techniques  
 5607 and independence assumptions.

In discriminatively-trained weighted context-free grammars, the scores for each production can be computed from a set of features, which can be made progressively more fine-grained (Finkel et al., 2008). For example, the score of the lexicalized production  $\text{NP}(\text{President}) \rightarrow \text{NP}(\text{President}) \text{ PP}(of)$  can be computed from the following features:

$$\begin{aligned} f(\text{NP}(\text{President}) \rightarrow \text{NP}(\text{President}) \text{ PP}(of)) = & \{\text{NP}(*) \rightarrow \text{NP}(*) \text{ PP}(*), \\ & \text{NP}(\text{President}) \rightarrow \text{NP}(\text{President}) \text{ PP}(*), \\ & \text{NP}(*) \rightarrow \text{NP}(*) \text{ PP}(of), \\ & \text{NP}(\text{President}) \rightarrow \text{NP}(\text{President}) \text{ PP}(of)\} \end{aligned}$$

5608 The first feature scores the unlexicalized production  $\text{NP} \rightarrow \text{NP PP}$ ; the next two features  
 5609 lexicalize only one element of the production, thereby scoring the appropriateness of  $\text{NP}$   
 5610 attachment for the individual words *President* and *of*; the final feature scores the specific  
 5611 bilexical affinity of *President* and *of*. For bilexical pairs that are encountered frequently in  
 5612 the treebank, this bilexical feature can play an important role in parsing; for pairs that are  
 5613 absent or rare, regularization will drive its weight to zero, forcing the parser to rely on the  
 5614 more coarse-grained features.

5615 In chapter 14, we will encounter techniques for clustering words based on their **distribu-**  
 5616 **tional** properties — the contexts in which they appear. Such a clustering would group  
 5617 rare and common words, such as *whale*, *shark*, *Leviathan*. Word clusters can be used

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<sup>7</sup>The real situation is even more difficult, because non-binary context-free grammars can involve **trilexical** or higher-order dependencies, between the head of the constituent and multiple of its children (Carreras et al., 2008).

5618 as features in discriminative lexicalized parsing, striking a middle ground between full  
 5619 lexicalization and non-terminals (Finkel et al., 2008). In this way, labeled examples con-  
 5620 taining relatively common words like *whale* can help to improve parsing for rare words  
 5621 like *beluga*, as long as those two words are clustered together.

### 5622 10.5.3 \*Refinement grammars

5623 Lexicalization improves on context-free parsing by adding detailed information in the  
 5624 form of lexical heads. However, estimating the scores of lexicalized productions is dif-  
 5625 ficult. Klein and Manning (2003) argue that the right level of linguistic detail is some-  
 5626 where between treebank categories and individual words. Some parts-of-speech and non-  
 5627 terminals are truly substitutable: for example, *cat*/N and *dog*/N. But others are not: for  
 5628 example, the preposition *of* exclusively attaches to nouns, while the preposition *as* is more  
 5629 likely to modify verb phrases. Klein and Manning (2003) obtained a 2% improvement in  
 5630 *F*-MEASURE on a parent-annotated PCFG parser by making a single change: splitting the  
 5631 preposition category into six subtypes. They propose a series of linguistically-motivated  
 5632 refinements to the Penn Treebank annotations, which in total yielded a 40% error reduc-  
 5633 tion.

5634 Non-terminal refinement process can be automated by treating the refined categories  
 5635 as latent variables. For example, we might split the noun phrase non-terminal into NP1, NP2, NP3, ...,  
 5636 without defining in advance what each refined non-terminal corresponds to. This can  
 5637 be treated as **partially supervised learning**, similar to the multi-component document  
 5638 classification model described in § 5.2.3. A latent variable PCFG can be estimated by  
 5639 expectation-maximization (Matsuzaki et al., 2005):

- 5640 • In the E-step, estimate a marginal distribution  $q$  over the refinement type of each  
 5641 non-terminal in each derivation. These marginals are constrained by the original  
 5642 annotation: an NP can be reannotated as NP4, but not as VP3. Marginal probabili-  
 5643 ties over refined productions can be computed from the **inside-outside algorithm**,  
 5644 as described in § 10.4.3, where the E-step enforces the constraints imposed by the  
 5645 original annotations.
- 5646 • In the M-step, recompute the parameters of the grammar, by summing over the  
 5647 probabilities of anchored productions that were computed in the E-step:

$$E[\text{count}(X \rightarrow Y Z)] = \sum_{i=0}^M \sum_{j=i}^M \sum_{k=i}^j p(X \rightarrow Y Z, (i, j, k) | \mathbf{w}). \quad [10.43]$$

5648 As usual, this process can be iterated to convergence. To determine the number of re-  
 5649 finement types for each tag, Petrov et al. (2006) apply a split-merge heuristic; Liang et al.  
 5650 (2007) and Finkel et al. (2007) apply **Bayesian nonparametrics** (Cohen, 2016).

Proper nouns			
NNP-14	<i>Oct.</i>	<i>Nov.</i>	<i>Sept.</i>
NNP-12	<i>John</i>	<i>Robert</i>	<i>James</i>
NNP-2	<i>J.</i>	<i>E.</i>	<i>L.</i>
NNP-1	<i>Bush</i>	<i>Noriega</i>	<i>Peters</i>
NNP-15	<i>New</i>	<i>San</i>	<i>Wall</i>
NNP-3	<i>York</i>	<i>Francisco</i>	<i>Street</i>
Personal Pronouns			
PRP-0	<i>It</i>	<i>He</i>	<i>I</i>
PRP-1	<i>it</i>	<i>he</i>	<i>they</i>
PRP-2	<i>it</i>	<i>them</i>	<i>him</i>

Table 10.4: Examples of automatically refined non-terminals and some of the words that they generate (Petrov et al., 2006).

5651 Some examples of refined non-terminals are shown in Table 10.4. The proper nouns  
 5652 differentiate months, first names, middle initials, last names, first names of places, and  
 5653 second names of places; each of these will tend to appear in different parts of grammatical  
 5654 productions. The personal pronouns differentiate grammatical role, with PRP-0 appear-  
 5655 ing in subject position at the beginning of the sentence (note the capitalization), PRP-1  
 5656 appearing in subject position but not at the beginning of the sentence, and PRP-2 appear-  
 5657 ing in object position.

## 5658 10.6 Beyond context-free parsing

5659 In the context-free setting, the score for a parse is a combination of the scores of individual  
 5660 productions. As we have seen, these models can be improved by using finer-grained non-  
 5661 terminals, via parent-annotation, lexicalization, and automated refinement. However, the  
 5662 inherent limitations to the expressiveness of context-free parsing motivate the consider-  
 5663 ation of other search strategies. These strategies abandon the optimality guaranteed by  
 5664 bottom-up parsing, in exchange for the freedom to consider arbitrary properties of the  
 5665 proposed parses.

### 5666 10.6.1 Reranking

5667 A simple way to relax the restrictions of context-free parsing is to perform a two-stage pro-  
 5668 cess, in which a context-free parser generates a  $k$ -best list of candidates, and a **reranker**  
 5669 then selects the best parse from this list (Charniak and Johnson, 2005; Collins and Koo,  
 5670 2005). The reranker can be trained from an objective that is similar to multi-class classi-  
 5671 fication: the goal is to learn weights that assign a high score to the reference parse, or to

5672 the parse on the  $k$ -best list that has the lowest error. In either case, the reranker need only  
 5673 evaluate the  $K$  best parses, and so no context-free assumptions are necessary. This opens  
 5674 the door to more expressive scoring functions:

- 5675 • It is possible to incorporate arbitrary non-local features, such as the structural par-  
 5676 allelism and right-branching orientation of the parse (Charniak and Johnson, 2005).  
 5677 • Reranking enables the use of **recursive neural networks**, in which each constituent  
 5678 span  $w_{i+1:j}$  receives a vector  $\mathbf{u}_{i,j}$  which is computed from the vector representa-  
 5679 tions of its children, using a composition function that is linked to the production  
 5680 rule (Socher et al., 2013), e.g.,

$$\mathbf{u}_{i,j} = f \left( \Theta_{X \rightarrow Y \ Z} \begin{bmatrix} \mathbf{u}_{i,k} \\ \mathbf{u}_{k,j} \end{bmatrix} \right) \quad [10.44]$$

5681 The overall score of the parse can then be computed from the final vector,  $\Psi(\tau) =$   
 5682  $\theta \mathbf{u}_{0,M}$ .

5683 Reranking can yield substantial improvements in accuracy. The main limitation is that it  
 5684 can only find the best parse among the  $K$ -best offered by the generator, so it is inherently  
 5685 limited by the ability of the bottom-up parser to find high-quality candidates.

### 5686 10.6.2 Transition-based parsing

5687 Structure prediction can be viewed as a form of search. An alternative to bottom-up pars-  
 5688 ing is to read the input from left-to-right, gradually building up a parse structure through  
 5689 a series of **transitions**. Transition-based parsing is described in more detail in the next  
 5690 chapter, in the context of dependency parsing. However, it can also be applied to CFG  
 5691 parsing, as briefly described here.

5692 For any context-free grammar, there is an equivalent **pushdown automaton**, a model  
 5693 of computation that accepts exactly those strings that can be derived from the grammar.  
 5694 This computational model consumes the input from left to right, while pushing and pop-  
 5695 ping elements on a stack. This architecture provides a natural transition-based parsing  
 5696 framework for context-free grammars, known as **shift-reduce parsing**.

5697 Shift-reduce parsing is a type of transition-based parsing, in which the parser can take  
 5698 the following actions:

- 5699 • *shift* the next terminal symbol onto the stack;  
 5700 • *unary-reduce* the top item on the stack, using a unary production rule in the gram-  
 5701 mar;  
 5702 • *binary-reduce* the top two items onto the stack, using a binary production rule in the  
 5703 grammar.

5704 The set of available actions is constrained by the situation: the parser can only shift if  
 5705 there are remaining terminal symbols in the input, and it can only reduce if an applicable  
 5706 production rule exists in the grammar. If the parser arrives at a state where the input  
 5707 has been completely consumed, and the stack contains only the element S, then the input  
 5708 is accepted. If the parser arrives at a non-accepting state where there are no possible  
 5709 actions, the input is rejected. A parse error occurs if there is some action sequence that  
 5710 would accept an input, but the parser does not find it.

5711 **Example** Consider the input *we eat sushi* and the grammar in Table 10.1. The input can  
 5712 be parsed through the following sequence of actions:

- 5713 1. **Shift** the first token *we* onto the stack.
- 5714 2. **Reduce** the top item on the stack to NP, using the production  $NP \rightarrow we$ .
- 5715 3. **Shift** the next token *eat* onto the stack, and **reduce** it to V with the production  $V \rightarrow$   
 5716 *eat*.
- 5717 4. **Shift** the final token *sushi* onto the stack, and **reduce** it to NP. The input has been  
 5718 completely consumed, and the stack contains [NP, V, NP].
- 5719 5. **Reduce** the top two items using the production  $VP \rightarrow V NP$ . The stack now con-  
 5720 tains [VP, NP].
- 5721 6. **Reduce** the top two items using the production  $S \rightarrow NP VP$ . The stack now contains  
 5722 [S]. Since the input is empty, this is an accepting state.

5723 One thing to notice from this example is that the number of shift actions is equal to the  
 5724 length of the input. The number of reduce actions is equal to the number of non-terminals  
 5725 in the analysis, which grows linearly in the length of the input. Thus, the overall time  
 5726 complexity of shift-reduce parsing is linear in the length of the input (assuming the com-  
 5727 plexity of each individual classification decision is constant in the length of the input).  
 5728 This is far better than the cubic time complexity required by CKY parsing.

5729 **Transition-based parsing as inference** In general, it is not possible to guarantee that  
 5730 a transition-based parser will find the optimal parse,  $\text{argmax}_\tau \Psi(\tau; \mathbf{w})$ , even under the  
 5731 usual CFG independence assumptions. We could assign a score to each anchored parsing  
 5732 action in each context, with  $\psi(a, c)$  indicating the score of performing action  $a$  in context  $c$ .  
 5733 One might imagine that transition-based parsing could efficiently find the derivation that  
 5734 maximizes the sum of such scores. But this too would require backtracking and searching  
 5735 over an exponentially large number of possible action sequences: if a bad decision is  
 5736 made at the beginning of the derivation, then it may be impossible to recover the optimal  
 5737 action sequence without backtracking to that early mistake. This is known as a **search**  
 5738 **error**. Transition-based parsers can incorporate arbitrary features, without the restrictive

5739 independence assumptions required by chart parsing; search errors are the price that must  
 5740 be paid for this flexibility.

5741 **Learning transition-based parsing** Transition-based parsing can be combined with ma-  
 5742 chine learning by training a classifier to select the correct action in each situation. This  
 5743 classifier is free to choose any feature of the input, the state of the parser, and the parse  
 5744 history. However, there is no optimality guarantee: the parser may choose a suboptimal  
 5745 parse, due to a mistake at the beginning of the analysis. Nonetheless, some of the strongest  
 5746 CFG parsers are based on the shift-reduce architecture, rather than CKY. A recent genera-  
 5747 tion of models links shift-reduce parsing with recurrent neural networks, updating a  
 5748 hidden state vector while consuming the input (e.g., Cross and Huang, 2016; Dyer et al.,  
 5749 2016). Learning algorithms for transition-based parsing are discussed in more detail in  
 5750 § 11.3.

## 5751 Exercises

5752 1. Design a grammar that handles English subject-verb agreement. Specifically, your  
 5753 grammar should handle the examples below correctly:

5754 (10.7) a. She sings.

5755 b. We sing.

5756 (10.8) a. \*She sing.

5757 b. \*We sings.

5758 2. Extend your grammar from the previous problem to include the auxiliary verb *can*,  
 5759 so that the following cases are handled:

5760 (10.9) a. She can sing.

5761 b. We can sing.

5762 (10.10) a. \*She can sings.

5763 b. \*We can sings.

5764 3. French requires subjects and verbs to agree in person and number, and it requires  
 5765 determiners and nouns to agree in gender and number. Verbs and their objects need  
 5766 not agree. Assuming that French has two genders (feminine and masculine), three  
 5767 persons (first [*me*], second [*you*], third [*her*]), and two numbers (singular and plural),  
 5768 how many productions are required to extend the following simple grammar to  
 5769 handle agreement?

---

5770	$S \rightarrow NP\ VP$ $VP \rightarrow V \mid V\ NP \mid V\ NP\ NP$ $NP \rightarrow DET\ NN$
------	--

---

5771 4. Consider the grammar:

---

5772	$S \rightarrow NP\ VP$ $VP \rightarrow V\ NP$ $NP \rightarrow JJ\ NP$ $NP \rightarrow fish\ (the\ animal)$ $V \rightarrow fish\ (the\ action\ of\ fishing)$ $JJ \rightarrow fish\ (a\ modifier,\ as\ in\ fish\ sauce\ or\ fish\ stew)$
------	---

---

5773 Apply the CKY algorithm and identify all possible parses for the sentence *fish fish fish fish*.

5774

5775 5. Choose one of the possible parses for the previous problem, and show how it can be  
5776 derived by a series of shift-reduce actions.

5777 6. To handle VP coordination, a grammar includes the production  $VP \rightarrow VP\ CC\ VP$ .  
5778 To handle adverbs, it also includes the production  $VP \rightarrow VP\ ADV$ . Assume all verbs  
5779 are generated from a sequence of unary productions, e.g.,  $VP \rightarrow V \rightarrow eat$ .

- 5780 a) Show how to binarize the production  $VP \rightarrow VP\ CC\ VP$ .
- 5781 b) Use your binarized grammar to parse the sentence *They eat and drink together*,  
5782 treating *together* as an adverb.
- 5783 c) Prove that a weighted CFG cannot distinguish the two possible derivations of  
5784 this sentence. Your explanation should focus on the productions in the original,  
5785 non-binary grammar.
- 5786 d) Explain what condition must hold for a parent-annotated WCFG to prefer the  
5787 derivation in which *together* modifies the coordination *eat and drink*.

7. Consider the following PCFG:

$$p(X \rightarrow X\ X) = \frac{1}{2} \quad [10.45]$$

$$p(X \rightarrow Y) = \frac{1}{2} \quad [10.46]$$

$$p(Y \rightarrow \sigma) = \frac{1}{|\Sigma|}, \forall \sigma \in \Sigma \quad [10.47]$$

5788 a) Compute the probability  $p(\hat{\tau})$  of the maximum probability parse for a string  
5789  $w \in \Sigma^M$ .

- 5790            b) Compute the conditional probability  $p(\hat{\tau} \mid \mathbf{w})$ .
- 5791        8. Context-free grammars can be used to parse the internal structure of words. Us-  
 5792        ing the weighted CKY algorithm and the following weighted context-free grammar,  
 5793        identify the best parse for the sequence of morphological segments *in+flame+able*.
- 
- |         |   |              |    |
|---------|---|--------------|----|
| S       | → | V            | 0  |
| S       | → | N            | 0  |
| S       | → | J            | 0  |
| V       | → | VPref N      | -1 |
| J       | → | N JSuff      | 1  |
| J       | → | V JSuff      | 0  |
| J       | → | NegPref J    | 1  |
| VPref   | → | <i>in+</i>   | 2  |
| NegPref | → | <i>in+</i>   | 1  |
| N       | → | <i>flame</i> | 0  |
| JSuff   | → | <i>+able</i> | 0  |
- 5794
- 5795        9. Use the inside and outside scores to compute the marginal probability  $p(X_{i:j} \rightarrow Y_{i:k-1} Z_{k:j} \mid \mathbf{w})$ ,  
 5796        indicating that  $Y$  spans  $\mathbf{w}_{i:k-1}$ ,  $Z$  spans  $\mathbf{w}_{k:j}$ , and  $X$  is the parent of  $Y$  and  $Z$ , span-  
 5797        ning  $\mathbf{w}_{i:j}$ .
- 5798        10. Suppose that the potentials  $\Psi(X \rightarrow \alpha)$  are log-probabilities, so that  $\sum_{\alpha} \exp \Psi(X \rightarrow \alpha) = 1$   
 5799        for all  $X$ . Verify that the semiring inside recurrence from Equation 10.26 generates  
 5800        the log-probability  $\log p(\mathbf{w}) = \log \sum_{\tau: \text{yield}(\tau)=\mathbf{w}} p(\tau)$ .

# 5801 Chapter 11

## 5802 Dependency parsing

5803 The previous chapter discussed algorithms for analyzing sentences in terms of nested con-  
5804 stituents, such as noun phrases and verb phrases. However, many of the key sources of  
5805 ambiguity in phrase-structure analysis relate to questions of **attachment**: where to attach a  
5806 prepositional phrase or complement clause, how to scope a coordinating conjunction, and  
5807 so on. These attachment decisions can be represented with a more lightweight structure:  
5808 a directed graph over the words in the sentence, known as a **dependency parse**. Syntac-  
5809 tic annotation has shifted its focus to such dependency structures: at the time of this  
5810 writing, the **Universal Dependencies** project offers more than 100 dependency treebanks  
5811 for more than 60 languages.<sup>1</sup> This chapter will describe the linguistic ideas underlying  
5812 dependency grammar, and then discuss exact and transition-based parsing algorithms.  
5813 The chapter will also discuss recent research on **learning to search** in transition-based  
5814 structure prediction.

### 5815 11.1 Dependency grammar

5816 While **dependency grammar** has a rich history of its own (Tesnière, 1966; Kübler et al.,  
5817 2009), it can be motivated by extension from the lexicalized context-free grammars that  
5818 we encountered in previous chapter (§ 10.5.2). Recall that lexicalization augments each  
5819 non-terminal with a **head word**. The head of a constituent is identified recursively, using  
5820 a set of **head rules**, as shown in Table 10.3. An example of a lexicalized context-free parse  
5821 is shown in Figure 11.1a. In this sentence, the head of the S constituent is the main verb,  
5822 *scratch*; this non-terminal then produces the noun phrase *the cats*, whose head word is  
5823 *cats*, and from which we finally derive the word *the*. Thus, the word *scratch* occupies the  
5824 central position for the sentence, with the word *cats* playing a supporting role. In turn, *cats*

---

<sup>1</sup>[universaldependencies.org](http://universaldependencies.org)

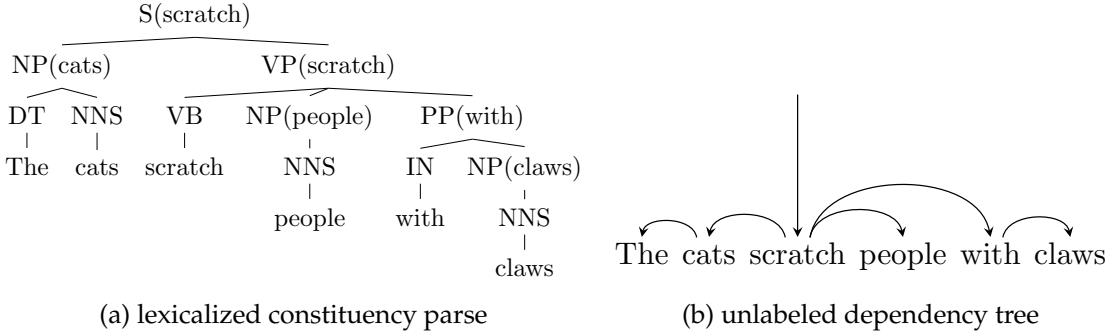


Figure 11.1: Dependency grammar is closely linked to lexicalized context free grammars: each lexical head has a dependency path to every other word in the constituent. (This example is based on the lexicalization rules from § 10.5.2, which make the preposition the head of a prepositional phrase. In the more contemporary Universal Dependencies annotations, the head of *with claws* would be *claws*, so there would be an edge *scratch* → *claws*.)

5825 occupies the central position for the noun phrase, with the word *the* playing a supporting  
5826 role.

5827 The relationships between words in a sentence can be formalized in a directed graph,  
5828 based on the lexicalized phrase-structure parse: create an edge  $(i, j)$  iff word  $i$  is the head  
5829 of a phrase whose child is a phrase headed by word  $j$ . Thus, in our example, we would  
5830 have *scratch* → *cats* and *cats* → *the*. We would not have the edge *scratch* → *the*, because  
5831 although  $S(\text{scratch})$  dominates  $\text{DET}(\text{the})$  in the phrase-structure parse tree, it is not its im-  
5832 mediate parent. These edges describe **syntactic dependencies**, a bilexical relationship  
5833 between a **head** and a **dependent**, which is at the heart of dependency grammar.

5834 Continuing to build out this **dependency graph**, we will eventually reach every word  
5835 in the sentence, as shown in Figure 11.1b. In this graph — and in all graphs constructed  
5836 in this way — every word has exactly one incoming edge, except for the root word, which  
5837 is indicated by a special incoming arrow from above. Furthermore, the graph is *weakly*  
5838 *connected*: if the directed edges were replaced with undirected edges, there would be a  
5839 path between all pairs of nodes. From these properties, it can be shown that there are no  
5840 cycles in the graph (or else at least one node would have to have more than one incoming  
5841 edge), and therefore, the graph is a tree. Because the graph includes all vertices, it is a  
5842 **spanning tree**.

### 5843 11.1.1 Heads and dependents

5844 A dependency edge implies an asymmetric syntactic relationship between the head and  
5845 dependent words, sometimes called **modifiers**. For a pair like *the cats* or *cats scratch*, how

5846 do we decide which is the head? Here are some possible criteria:

- 5847 • The head sets the syntactic category of the construction: for example, nouns are the  
5848 heads of noun phrases, and verbs are the heads of verb phrases.
- 5849 • The modifier may be optional while the head is mandatory: for example, in the  
5850 sentence *cats scratch people with claws*, the subtrees *cats scratch* and *cats scratch people*  
5851 are grammatical sentences, but *with claws* is not.
- 5852 • The head determines the morphological form of the modifier: for example, in lan-  
5853 guages that require gender agreement, the gender of the noun determines the gen-  
5854 der of the adjectives and determiners.
- 5855 • Edges should first connect content words, and then connect function words.

5856 As always, these guidelines sometimes conflict. The Universal Dependencies (UD)  
5857 project has attempted to identify a set of principles that can be applied to dozens of dif-  
5858 ferent languages (Nivre et al., 2016).<sup>2</sup> These guidelines are based on the universal part-  
5859 of-speech tags from chapter 8. They differ somewhat from the head rules described in  
5860 § 10.5.2: for example, on the principle that dependencies should relate content words, the  
5861 prepositional phrase *with claws* would be headed by *claws*, resulting in an edge *scratch* →  
5862 *claws*, and another edge *claws* → *with*.

5863 One objection to dependency grammar is that not all syntactic relations are asymmet-  
5864 ric. Coordination is one of the most obvious examples (Popel et al., 2013): in the sentence,  
5865 *Abigail and Max like kimchi* (Figure 11.2), which word is the head of the coordinated noun  
5866 phrase *Abigail and Max*? Choosing either *Abigail* or *Max* seems arbitrary; fairness argues  
5867 for making *and* the head, but this seems like the least important word in the noun phrase,  
5868 and selecting it would violate the principle of linking content words first. The Universal  
5869 Dependencies annotation system arbitrarily chooses the left-most item as the head — in  
5870 this case, *Abigail* — and includes edges from this head to both *Max* and the coordinating  
5871 conjunction *and*. These edges are distinguished by the labels CONJ (for the thing begin  
5872 conjoined) and CC (for the coordinating conjunction). The labeling system is discussed  
5873 next.

### 5874 11.1.2 Labeled dependencies

5875 Edges may be **labeled** to indicate the nature of the syntactic relation that holds between  
5876 the two elements. For example, in Figure 11.2, the label NSUBJ on the edge from *like* to  
5877 *Abigail* indicates that the subtree headed by *Abigail* is the noun subject of the verb *like*;  
5878 similarly, the label OBJ on the edge from *like* to *kimchi* indicates that the subtree headed by

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<sup>2</sup>The latest and most specific guidelines are available at [universaldependencies.org/guidelines.html](http://universaldependencies.org/guidelines.html)

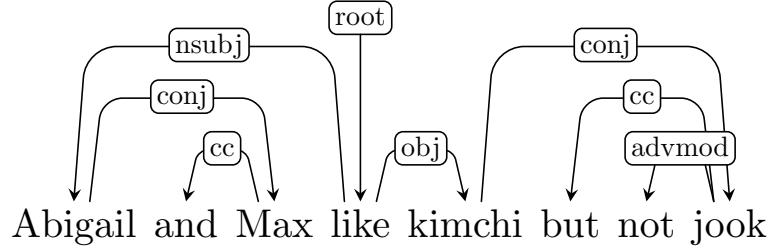


Figure 11.2: In the Universal Dependencies annotation system, the left-most item of a coordination is the head.

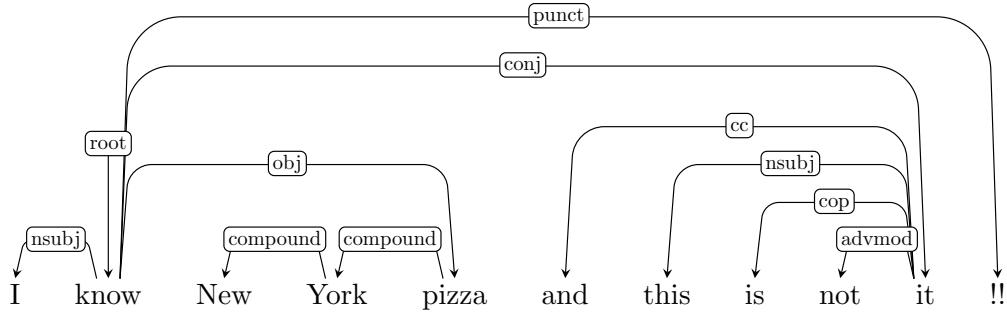


Figure 11.3: A labeled dependency parse from the English UD Treebank (reviews-361348-0006)

5879    *kimchi* is the object.<sup>3</sup> The negation *not* is treated as an adverbial modifier (ADVMOD) on  
5880    the noun *jook*.

5881    A slightly more complex example is shown in Figure 11.3. The multiword expression  
5882    *New York pizza* is treated as a “flat” unit of text, with the elements linked by the COM-  
5883    POUND relation. The sentence includes two clauses that are conjoined in the same way  
5884    that noun phrases are conjoined in Figure 11.2. The second clause contains a **copula** verb  
5885    (see § 8.1.1). For such clauses, we treat the “object” of the verb as the root — in this case,  
5886    *it* — and label the verb as a dependent, with the COP relation. This example also shows  
5887    how punctuation are treated, with label PUNCT.

### 5888    11.1.3 Dependency subtrees and constituents

5889    Dependency trees hide information that would be present in a CFG parse. Often what  
5890    is hidden is in fact irrelevant: for example, Figure 11.4 shows three different ways of

<sup>3</sup>Earlier work distinguished direct and indirect objects (De Marneffe and Manning, 2008), but this has been dropped in version 2.0 of the Universal Dependencies annotation system.

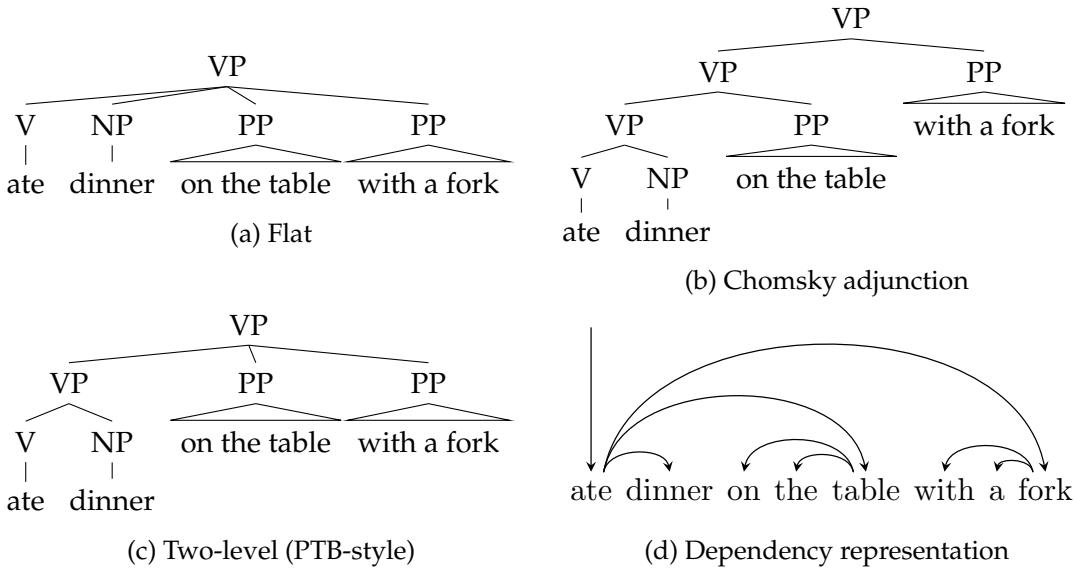


Figure 11.4: The three different CFG analyses of this verb phrase all correspond to a single dependency structure.

representing prepositional phrase adjuncts to the verb *ate*. Because there is apparently no meaningful difference between these analyses, the Penn Treebank decides by convention to use the two-level representation (see Johnson, 1998, for a discussion). As shown in Figure 11.4d, these three cases all look the same in a dependency parse.

But dependency grammar imposes its own set of annotation decisions, such as the identification of the head of a coordination (§ 11.1.1); without lexicalization, context-free grammar does not require either element in a coordination to be privileged in this way. Dependency parses can be disappointingly flat: for example, in the sentence *Yesterday, Abigail was reluctantly giving Max kimchi*, the root *giving* is the head of every dependency! The constituent parse arguably offers a more useful structural analysis for such cases.

**Projectivity** Thus far, we have defined dependency trees as spanning trees over a graph in which each word is a vertex. As we have seen, one way to construct such trees is by connecting the heads in a lexicalized constituent parse. However, there are spanning trees that cannot be constructed in this way. Syntactic constituents are *contiguous spans*. In a spanning tree constructed from a lexicalized constituent parse, the head  $h$  of any constituent that spans the nodes from  $i$  to  $j$  must have a path to every node in this span. This property is known as **projectivity**, and projective dependency parses are a restricted class of spanning trees. Informally, projectivity means that “crossing edges” are prohibited. The formal definition follows:

	% non-projective edges	% non-projective sentences
Czech	1.86%	22.42%
English	0.39%	7.63%
German	2.33%	28.19%

Table 11.1: Frequency of non-projective dependencies in three languages (Kuhlmann and Nivre, 2010)

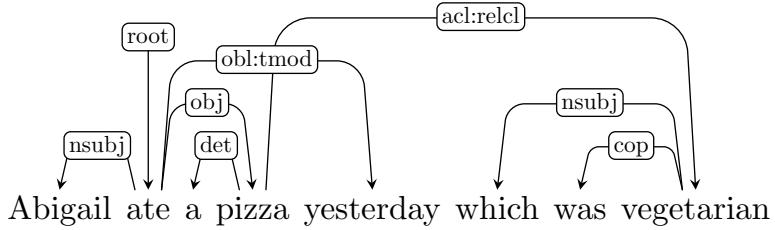


Figure 11.5: An example of a non-projective dependency parse. The “crossing edge” arises from the relative clause *which was vegetarian* and the oblique temporal modifier *yesterday*.

5910 **Definition 2** (Projectivity). *An edge from  $i$  to  $j$  is projective iff all  $k$  between  $i$  and  $j$  are descendants of  $i$ . A dependency parse is projective iff all its edges are projective.*

5912 Figure 11.5 gives an example of a non-projective dependency graph in English. This  
 5913 dependency graph does not correspond to any constituent parse. As shown in Table 11.1,  
 5914 non-projectivity is more common in languages such as Czech and German. Even though  
 5915 relatively few dependencies are non-projective in these languages, many sentences have  
 5916 at least one such dependency. As we will soon see, projectivity has important algorithmic  
 5917 consequences.

## 5918 11.2 Graph-based dependency parsing

5919 Let  $\mathbf{y} = \{i \xrightarrow{r} j\}$  represent a dependency graph, in which each edge is a relation  $r$  from  
 5920 head word  $i \in \{1, 2, \dots, M, \text{ROOT}\}$  to modifier  $j \in \{1, 2, \dots, M\}$ . The special node ROOT  
 5921 indicates the root of the graph, and  $M$  is the length of the input  $|\mathbf{w}|$ . Given a scoring  
 5922 function  $\Psi(\mathbf{y}, \mathbf{w}; \theta)$ , the optimal parse is,

$$\hat{\mathbf{y}} = \underset{\mathbf{y} \in \mathcal{Y}(\mathbf{w})}{\operatorname{argmax}} \Psi(\mathbf{y}, \mathbf{w}; \theta), \quad [11.1]$$

5923 where  $\mathcal{Y}(\mathbf{w})$  is the set of valid dependency parses on the input  $\mathbf{w}$ . As usual, the number  
 5924 of possible labels  $|\mathcal{Y}(\mathbf{w})|$  is exponential in the length of the input (Wu and Chao, 2004).

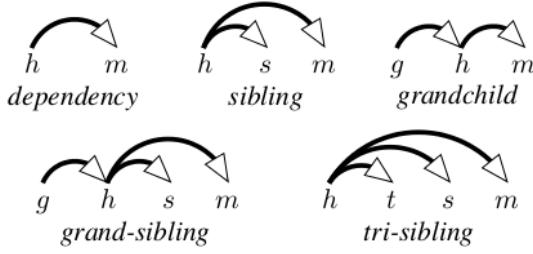


Figure 11.6: Feature templates for higher-order dependency parsing (Koo and Collins, 2010) [todo: permission]

5925 Algorithms that search over this space of possible graphs are known as **graph-based de-**  
5926 **pendency parsers.**

In sequence labeling and constituent parsing, it was possible to search efficiently over an exponential space by choosing a feature function that decomposes into a sum of local feature vectors. A similar approach is possible for dependency parsing, by requiring the scoring function to decompose across dependency arcs  $i \rightarrow j$ :

$$\Psi(\mathbf{y}, \mathbf{w}; \boldsymbol{\theta}) = \sum_{i \xrightarrow{r} j \in \mathbf{y}} \psi(i \xrightarrow{r} j, \mathbf{w}; \boldsymbol{\theta}). \quad [11.2]$$

5927 Dependency parsers that operate under this assumption are known as **arc-factored**, since  
5928 the overall score is a product of scores over all arcs.

**Higher-order dependency parsing** The arc-factored decomposition can be relaxed to allow higher-order dependencies. In **second-order dependency parsing**, the scoring function may include grandparents and siblings, as shown by the templates in Figure 11.6. The scoring function is,

$$\begin{aligned} \Psi(\mathbf{y}, \mathbf{w}; \boldsymbol{\theta}) &= \sum_{i \xrightarrow{r} j \in \mathbf{y}} \psi_{\text{parent}}(i \xrightarrow{r} j, \mathbf{w}; \boldsymbol{\theta}) \\ &\quad + \sum_{k \xrightarrow{r'} i \in \mathbf{y}} \psi_{\text{grandparent}}(i \xrightarrow{r} j, k, r', \mathbf{w}; \boldsymbol{\theta}) \end{aligned} \quad [11.3]$$

$$+ \sum_{\substack{i \xrightarrow{r'} s \in \mathbf{y} \\ s \neq j}} \psi_{\text{sibling}}(i \xrightarrow{r} j, s, r', \mathbf{w}; \boldsymbol{\theta}). \quad [11.4]$$

5929 The top line scores computes a scoring function that includes the grandparent *k*; the  
5930 bottom line computes a scoring function for each sibling *s*. For projective dependency

graphs, there are efficient algorithms for second-order and third-order dependency parsing (Eisner, 1996; McDonald and Pereira, 2006; Koo and Collins, 2010); for non-projective dependency graphs, second-order dependency parsing is NP-hard (McDonald and Pereira, 2006). The specific algorithms are discussed in the next section.

### 11.2.1 Graph-based parsing algorithms

The distinction between projective and non-projective dependency trees (§ 11.1.3) plays a key role in the choice of algorithms. Because projective dependency trees are closely related to (and can be derived from) lexicalized constituent trees, lexicalized parsing algorithms can be applied directly. For the more general problem of parsing to arbitrary spanning trees, a different class of algorithms is required. In both cases, arc-factored dependency parsing relies on precomputing the scores  $\psi(i \xrightarrow{r} j, w; \theta)$  for each potential edge. There are  $\mathcal{O}(M^2 R)$  such scores, where  $M$  is the length of the input and  $R$  is the number of dependency relation types, and this is a lower bound on the time and space complexity of any exact algorithm for arc-factored dependency parsing.

#### 11.2.1.1 Projective dependency parsing

Any lexicalized constituency tree can be converted into a projective dependency tree by creating arcs between the heads of constituents and their parents, so any algorithm for lexicalized constituent parsing can be converted into an algorithm for projective dependency parsing, by converting arc scores into scores for lexicalized productions. As noted in § 10.5.2, there are cubic time algorithms for lexicalized constituent parsing, which are extensions of the CKY algorithm. Therefore, arc-factored projective dependency parsing can be performed in cubic time in the length of the input.

Second-order projective dependency parsing can also be performed in cubic time, with minimal modifications to the lexicalized parsing algorithm (Eisner, 1996). It is possible to go even further, to **third-order dependency parsing**, in which the scoring function may consider great-grandparents, grand-siblings, and “tri-siblings”, as shown in Figure 11.6. Third-order dependency parsing can be performed in  $\mathcal{O}(M^4)$  time, which can be made practical through the use of pruning to eliminate unlikely edges (Koo and Collins, 2010).

#### 11.2.1.2 Non-projective dependency parsing

In non-projective dependency parsing, the goal is to identify the highest-scoring spanning tree over the words in the sentence. The arc-factored assumption ensures that the score for each spanning tree will be computed as a sum over scores for the edges, which are precomputed. Based on these scores, we build a weighted connected graph. Arc-factored non-projective dependency parsing is then equivalent to finding the spanning tree that achieves the maximum total score,  $\Psi(y, w) = \sum_{i \xrightarrow{r} j \in y} \psi(i \xrightarrow{r} j, w)$ . The **Chu-**

5966 **Liu-Edmonds algorithm** (Chu and Liu, 1965; Edmonds, 1967) computes this **maximum**  
 5967 **spanning tree** efficiently. It does this by first identifying the best incoming edge  $i \xrightarrow{r} j$  for  
 5968 each vertex  $j$ . If the resulting graph does not contain cycles, it is the maximum spanning  
 5969 tree. If there is a cycle, it is collapsed into a super-vertex, whose incoming and outgoing  
 5970 edges are based on the edges to the vertices in the cycle. The algorithm is then applied  
 5971 recursively to the resulting graph, and process repeats until a graph without cycles is  
 5972 obtained.

5973 The time complexity of identifying the best incoming edge for each vertex is  $\mathcal{O}(M^2R)$ ,  
 5974 where  $M$  is the length of the input and  $R$  is the number of relations; in the worst case, the  
 5975 number of cycles is  $\mathcal{O}(M)$ . Therefore, the complexity of the Chu-Liu-Edmonds algorithm  
 5976 is  $\mathcal{O}(M^3R)$ . This complexity can be reduced to  $\mathcal{O}(M^2N)$  by storing the edge scores in a  
 5977 Fibonacci heap (Gabow et al., 1986). For more detail on graph-based parsing algorithms,  
 5978 see Eisner (1997) and Kübler et al. (2009).

5979 **Higher-order non-projective dependency parsing** Given the tractability of higher-order  
 5980 projective dependency parsing, you may be surprised to learn that non-projective second-  
 5981 order dependency parsing is NP-Hard. This can be proved by reduction from the vertex  
 5982 cover problem (Neuhaus and Bröker, 1997). A heuristic solution is to do projective pars-  
 5983 ing first, and then post-process the projective dependency parse to add non-projective  
 5984 edges (Nivre and Nilsson, 2005). More recent work has applied techniques for approxi-  
 5985 mate inference in graphical models, including belief propagation (Smith and Eisner, 2008),  
 5986 integer linear programming (Martins et al., 2009), variational inference (Martins et al.,  
 5987 2010), and Markov Chain Monte Carlo (Zhang et al., 2014).

### 5988 11.2.2 Computing scores for dependency arcs

The arc-factored scoring function  $\psi(i \xrightarrow{r} j, \mathbf{w}; \boldsymbol{\theta})$  can be defined in several ways:

$$\text{Linear} \quad \psi(i \xrightarrow{r} j, \mathbf{w}; \boldsymbol{\theta}) = \boldsymbol{\theta} \cdot \mathbf{f}(i \xrightarrow{r} j, \mathbf{w}) \quad [11.5]$$

$$\text{Neural} \quad \psi(i \xrightarrow{r} j, \mathbf{w}; \boldsymbol{\theta}) = \text{Feedforward}([\mathbf{u}_{w_i}; \mathbf{u}_{w_j}]; \boldsymbol{\theta}) \quad [11.6]$$

$$\text{Generative} \quad \psi(i \xrightarrow{r} j, \mathbf{w}; \boldsymbol{\theta}) = \log p(w_j, r | w_i). \quad [11.7]$$

#### 5989 11.2.2.1 Linear feature-based arc scores

5990 Linear models for dependency parsing incorporate many of the same features used in  
 5991 sequence labeling and discriminative constituent parsing. These include:

- 5992 • the length and direction of the arc;
- 5993 • the words  $w_i$  and  $w_j$  linked by the dependency relation;
- 5994 • the prefixes, suffixes, and parts-of-speech of these words;

- 5995 • the neighbors of the dependency arc,  $w_{i-1}, w_{i+1}, w_{j-1}, w_{j+1}$ ;  
 5996 • the prefixes, suffixes, and part-of-speech of these neighbor words.

5997 Each of these features can be conjoined with the dependency edge label  $r$ . Note that  
 5998 features in an arc-factored parser can refer to words other than  $w_i$  and  $w_j$ . The restriction  
 5999 is that the features consider only a single arc.

**Bilexical features** (e.g., *sushi* → *chopsticks*) are powerful but rare, so it is useful to augment them with coarse-grained alternatives, by “backing off” to the part-of-speech or affix. For example, the following features are created by backing off to part-of-speech tags in an unlabeled dependency parser:

$$\begin{aligned} \mathbf{f}(3 \rightarrow 5, \text{we eat sushi with chopsticks}) = & \langle \text{sushi} \rightarrow \text{chopsticks}, \\ & \text{sushi} \rightarrow \text{NNS}, \\ & \text{NN} \rightarrow \text{chopsticks}, \\ & \text{NNS} \rightarrow \text{NN} \rangle. \end{aligned}$$

6000 Regularized discriminative learning algorithms can then trade off between features at  
 6001 varying levels of detail. McDonald et al. (2005) take this approach as far as *tetralexical*  
 6002 features (e.g.,  $(w_i, w_{i+1}, w_{j-1}, w_j)$ ). Such features help to avoid choosing arcs that are un-  
 6003 likely due to the intervening words: for example, there is unlikely to be an edge between  
 6004 two nouns if the intervening span contains a verb. A large list of first and second-order  
 6005 features is provided by Bohnet (2010), who uses a hashing function to store these features  
 6006 efficiently.

### 6007 11.2.2.2 Neural arc scores

Given vector representations  $\mathbf{x}_i$  for each word  $w_i$  in the input, a set of arc scores can be computed from a feedforward neural network:

$$\psi(i \xrightarrow{r} j, \mathbf{w}; \boldsymbol{\theta}) = \text{FeedForward}([\mathbf{x}_i; \mathbf{x}_j]; \boldsymbol{\theta}_r), \quad [11.8]$$

where unique weights  $\boldsymbol{\theta}_r$  are available for each arc type (Pei et al., 2015; Kiperwasser and Goldberg, 2016). Kiperwasser and Goldberg (2016) use a feedforward network with a single hidden layer,

$$\mathbf{z} = g(\boldsymbol{\Theta}_r[\mathbf{x}_i; \mathbf{x}_j] + \mathbf{b}_r^{(z)}) \quad [11.9]$$

$$\psi(i \xrightarrow{r} j) = \boldsymbol{\beta}_r \mathbf{z} + \mathbf{b}_r^{(y)}, \quad [11.10]$$

6008 where  $\boldsymbol{\Theta}_r$  is a matrix,  $\boldsymbol{\beta}_r$  is a vector, each  $b_r$  is a scalar, and the function  $g$  is an elementwise  
 6009 tanh activation function.

6010 The vector  $\mathbf{x}_i$  can be set equal to the word embedding, which may be pre-trained or  
 6011 learned by backpropagation (Pei et al., 2015). Alternatively, contextual information can  
 6012 be incorporated by applying a bidirectional recurrent neural network across the input, as  
 6013 described in § 7.6. The RNN hidden states at each word can be used as inputs to the arc  
 6014 scoring function (Kiperwasser and Goldberg, 2016).

6015 **11.2.2.3 Probabilistic arc scores**

If each arc score is equal to the log probability  $\log p(w_j, r \mid w_i)$ , then the sum of scores gives the log probability of the sentence and arc labels, by the chain rule. For example, consider the unlabeled parse of *we eat sushi with rice*,

$$\mathbf{y} = \{(ROOT, 2), (2, 1), (2, 3), (3, 5), (5, 4)\} \quad [11.11]$$

$$\log p(\mathbf{w} \mid \mathbf{y}) = \sum_{(i \rightarrow j) \in \mathbf{y}} \log p(w_j \mid w_i) \quad [11.12]$$

$$\begin{aligned} &= \log p(eat \mid ROOT) + \log p(we \mid eat) + \log p(sushi \mid eat) \\ &\quad + \log p(rice \mid sushi) + \log p(with \mid rice). \end{aligned} \quad [11.13]$$

6016 Probabilistic generative models are used in combination with expectation-maximization  
 6017 (chapter 5) for unsupervised dependency parsing (Klein and Manning, 2004).

6018 **11.2.3 Learning**

Having formulated graph-based dependency parsing as a structure prediction problem, we can apply similar learning algorithms to those used in sequence labeling. Given a loss function  $\ell(\boldsymbol{\theta}; \mathbf{w}^{(i)}, \mathbf{y}^{(i)})$ , we can compute gradient-based updates to the parameters. For a model with feature-based arc scores and a perceptron loss, we obtain the usual structured perceptron update,

$$\hat{\mathbf{y}} = \operatorname{argmax}_{\mathbf{y}' \in \mathcal{Y}(\mathbf{w})} \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{w}, \mathbf{y}') \quad [11.14]$$

$$\boldsymbol{\theta} = \boldsymbol{\theta} + \mathbf{f}(\mathbf{w}, \mathbf{y}) - \mathbf{f}(\mathbf{w}, \hat{\mathbf{y}}) \quad [11.15]$$

6019 In this case, the argmax requires a maximization over all dependency trees for the sen-  
 6020 tence, which can be computed using the algorithms described in § 11.2.1. We can apply  
 6021 all the usual tricks from § 2.2: weight averaging, a large margin objective, and regular-  
 6022 ization. McDonald et al. (2005) were the first to treat dependency parsing as a structure  
 6023 prediction problem, using MIRA, an online margin-based learning algorithm. Neural arc  
 6024 scores can be learned in the same way, backpropagating from a margin loss to updates on  
 6025 the feedforward network that computes the score for each edge.

A conditional random field for arc-factored dependency parsing is built on the probability model,

$$p(\mathbf{y} \mid \mathbf{w}) = \frac{\exp \sum_{i \xrightarrow{r} j \in \mathbf{y}} \psi(i \xrightarrow{r} j, \mathbf{w}; \boldsymbol{\theta})}{\sum_{\mathbf{y}' \in \mathcal{Y}(\mathbf{w})} \exp \sum_{i \xrightarrow{r} j \in \mathbf{y}'} \psi(i \xrightarrow{r} j, \mathbf{w}; \boldsymbol{\theta})} \quad [11.16]$$

Such a model is trained to minimize the negative log conditional-likelihood. Just as in CRF sequence models (§ 7.5.3) and the logistic regression classifier (§ 2.4), the gradients involve marginal probabilities  $p(i \xrightarrow{r} j \mid \mathbf{w}; \boldsymbol{\theta})$ , which in this case are probabilities over individual dependencies. In arc-factored models, these probabilities can be computed in polynomial time. For projective dependency trees, the marginal probabilities can be computed in cubic time, using a variant of the inside-outside algorithm (Lari and Young, 1990). For non-projective dependency parsing, marginals can also be computed in cubic time, using the **matrix-tree theorem** (Koo et al., 2007; McDonald et al., 2007; Smith and Smith, 2007). Details of these methods are described by Kübler et al. (2009).

### 11.3 Transition-based dependency parsing

Graph-based dependency parsing offers exact inference, meaning that it is possible to recover the best-scoring parse for any given model. But this comes at a price: the scoring function is required to decompose into local parts — in the case of non-projective parsing, these parts are restricted to individual arcs. These limitations are felt more keenly in dependency parsing than in sequence labeling, because second-order dependency features are critical to correctly identify some types of attachments. For example, prepositional phrase attachment depends on the attachment point, the object of the preposition, and the preposition itself; arc-factored scores cannot account for all three of these features simultaneously. Graph-based dependency parsing may also be criticized on the basis of intuitions about human language processing: people read and listen to sentences *sequentially*, incrementally building mental models of the sentence structure and meaning before getting to the end (Jurafsky, 1996). This seems hard to reconcile with graph-based algorithms, which perform bottom-up operations on the entire sentence, requiring the parser to keep every word in memory. Finally, from a practical perspective, graph-based dependency parsing is relatively slow, running in cubic time in the length of the input.

Transition-based algorithms address all three of these objections. They work by moving through the sentence sequentially, while performing actions that incrementally update a stored representation of what has been read thus far. As with the shift-reduce parser from § 10.6.2, this representation consists of a stack, onto which parsing substructures can be pushed and popped. In shift-reduce, these substructures were constituents; in the transition systems that follow, they will be projective dependency trees over partial

spans of the input.<sup>4</sup> Parsing is complete when the input is consumed and there is only a single structure on the stack. The sequence of actions that led to the parse is known as the **derivation**. One problem with transition-based systems is that there may be multiple derivations for a single parse structure — a phenomenon known as **spurious ambiguity**.

### 11.3.1 Transition systems for dependency parsing

A **transition system** consists of a representation for describing configurations of the parser, and a set of transition actions, which manipulate the configuration. There are two main transition systems for dependency parsing: **arc-standard**, which is closely related to shift-reduce, and **arc-eager**, which adds an additional action that can simplify derivations (Abney and Johnson, 1991). In both cases, transitions are between **configurations** that are represented as triples,  $C = (\sigma, \beta, A)$ , where  $\sigma$  is the stack,  $\beta$  is the input buffer, and  $A$  is the list of arcs that have been created (Nivre, 2008). In the initial configuration,

$$C_{\text{initial}} = ([\text{ROOT}], \mathbf{w}, \emptyset), \quad [11.17]$$

indicating that the stack contains only the special node ROOT, the entire input is on the buffer, and the set of arcs is empty. An accepting configuration is,

$$C_{\text{accept}} = ([\text{ROOT}], \emptyset, A), \quad [11.18]$$

where the stack contains only ROOT, the buffer is empty, and the arcs  $A$  define a spanning tree over the input. The arc-standard and arc-eager systems define a set of transitions between configurations, which are capable of transforming an initial configuration into an accepting configuration. In both of these systems, the number of actions required to parse an input grows linearly in the length of the input, making transition-based parsing considerably more efficient than graph-based methods.

#### 11.3.1.1 Arc-standard

The **arc-standard** transition system is closely related to shift-reduce, and to the LR algorithm that is used to parse programming languages (Aho et al., 2006). It includes the following classes of actions:

- SHIFT: move the first item from the input buffer on to the top of the stack,

$$(\sigma, i|\beta, A) \Rightarrow (\sigma|i, \beta, A), \quad [11.19]$$

where we write  $i|\beta$  to indicate that  $i$  is the leftmost item in the input buffer, and  $\sigma|i$  to indicate the result of pushing  $i$  on to stack  $\sigma$ .

---

<sup>4</sup>Transition systems also exist for non-projective dependency parsing (e.g., Nivre, 2008).

- 6084 • ARC-LEFT: create a new left-facing arc of type  $r$  between the item on the top of the  
 6085 stack and the first item in the input buffer. The head of this arc is  $j$ , which remains  
 6086 at the front of the input buffer. The arc  $j \xrightarrow{r} i$  is added to  $A$ . Formally,

$$(\sigma|i, j|\beta, A) \Rightarrow (\sigma, j|\beta, A \oplus j \xrightarrow{r} i), \quad [11.20]$$

6087 where  $r$  is the label of the dependency arc, and  $\oplus$  concatenates the new arc  $j \xrightarrow{r} i$  to  
 6088 the list  $A$ .

- 6089 • ARC-RIGHT: creates a new right-facing arc of type  $r$  between the item on the top of the  
 6090 stack and the first item in the input buffer. The head of this arc is  $i$ , which is  
 6091 “popped” from the stack and pushed to the front of the input buffer. The arc  $i \xrightarrow{r} j$   
 6092 is added to  $A$ . Formally,

$$(\sigma|i, j|\beta, A) \Rightarrow (\sigma, i|\beta, A \oplus i \xrightarrow{r} j), \quad [11.21]$$

6093 where again  $r$  is the label of the dependency arc.

6094 Each action has preconditions. The SHIFT action can be performed only when the buffer  
 6095 has at least one element. The ARC-LEFT action cannot be performed when the root node  
 6096 ROOT is on top of the stack, since this node must be the root of the entire tree. The ARC-  
 6097 LEFT and ARC-RIGHT remove the modifier words from the stack (in the case of ARC-LEFT)  
 6098 and from the buffer (in the case of ARC-RIGHT), so it is impossible for any word to have  
 6099 more than one parent. Furthermore, the end state can only be reached when every word is  
 6100 removed from the buffer and stack, so the set of arcs is guaranteed to constitute a spanning  
 6101 tree. An example arc-standard derivation is shown in Table 11.2.

### 6102 11.3.1.2 Arc-eager dependency parsing

6103 In the arc-standard transition system, a word is completely removed from the parse once  
 6104 it has been made the modifier in a dependency arc. At this time, any dependents of  
 6105 this word must have already been identified. Right-branching structures are common in  
 6106 English (and many other languages), with words often modified by units such as prepo-  
 6107 sitional phrases to their right. In the arc-standard system, this means that we must first  
 6108 shift all the units of the input onto the stack, and then work backwards, creating a series of  
 6109 arcs, as occurs in Table 11.2. Note that the decision to shift *bagels* onto the stack guarantees  
 6110 that the prepositional phrase *with lox* will attach to the noun phrase, and that this decision  
 6111 must be made before the prepositional phrase is itself parsed. This has been argued to be  
 6112 cognitively implausible (Abney and Johnson, 1991); from a computational perspective, it  
 6113 means that a parser may need to look several steps ahead to make the correct decision.

6114 **Arc-eager dependency parsing** changes the ARC-RIGHT action so that right depen-  
 6115 dents can be attached before all of their dependents have been found. Rather than re-  
 6116 moving the modifier from both the buffer and stack, the ARC-RIGHT action pushes the

$\sigma$	$\beta$	action	arc added to $\mathcal{A}$
1. [ROOT]	<i>they like bagels with lox</i>	SHIFT	
2. [ROOT, <i>they</i> ]	<i>like bagels with lox</i>	ARC-LEFT	( <i>they</i> $\leftarrow$ <i>like</i> )
3. [ROOT]	<i>like bagels with lox</i>	SHIFT	
4. [ROOT, <i>like</i> ]	<i>bagels with lox</i>	SHIFT	
5. [ROOT, <i>like</i> , <i>bagels</i> ]	<i>with lox</i>	SHIFT	
6. [ROOT, <i>like</i> , <i>bagels</i> , <i>with</i> ]	<i>lox</i>	ARC-LEFT	( <i>with</i> $\leftarrow$ <i>lox</i> )
7. [ROOT, <i>like</i> , <i>bagels</i> ]	<i>lox</i>	ARC-RIGHT	( <i>bagels</i> $\rightarrow$ <i>lox</i> )
8. [ROOT, <i>like</i> ]	<i>bagels</i>	ARC-RIGHT	( <i>like</i> $\rightarrow$ <i>bagels</i> )
9. [ROOT]	<i>like</i>	ARC-RIGHT	(ROOT $\rightarrow$ <i>like</i> )
10. [ROOT]	$\emptyset$	DONE	

Table 11.2: Arc-standard derivation of the unlabeled dependency parse for the input *they like bagels with lox*.

6117 modifier on to the stack, on top of the head. Because the stack can now contain elements  
 6118 that already have parents in the partial dependency graph, two additional changes are  
 6119 necessary:

- 6120 • A precondition is required to ensure that the ARC-LEFT action cannot be applied  
 6121 when the top element on the stack already has a parent in  $A$ .  
 6122 • A new REDUCE action is introduced, which can remove elements from the stack if  
 6123 they already have a parent in  $A$ :

$$(\sigma|i, \beta, A) \Rightarrow (\sigma, \beta, A). \quad [11.22]$$

6124 As a result of these changes, it is now possible to create the arc *like*  $\rightarrow$  *bagels* before parsing  
 6125 the prepositional phrase *with lox*. Furthermore, this action does not imply a decision about  
 6126 whether the prepositional phrase will attach to the noun or verb. Noun attachment is  
 6127 chosen in the parse in Table 11.3, but verb attachment could be achieved by applying the  
 6128 REDUCE action at step 5 or 7.

### 6129 11.3.1.3 Projectivity

6130 The arc-standard and arc-eager transition systems are guaranteed to produce projective  
 6131 dependency trees, because all arcs are between the word at the top of the stack and the  
 6132 left-most edge of the buffer (Nivre, 2008). Non-projective transition systems can be con-  
 6133 structed by adding actions that create arcs with words that are second or third in the  
 6134 stack (Attardi, 2006), or by adopting an alternative configuration structure, which main-  
 6135 tains a list of all words that do not yet have heads (Covington, 2001). In **pseudo-projective**

$\sigma$	$\beta$	action	arc added to $\mathcal{A}$
1. [ROOT]	<i>they like bagels with lox</i>	SHIFT	
2. [ROOT, <i>they</i> ]	<i>like bagels with lox</i>	ARC-LEFT	( <i>they</i> $\leftarrow$ <i>like</i> )
3. [ROOT]	<i>like bagels with lox</i>	ARC-RIGHT	(ROOT $\rightarrow$ <i>like</i> )
4. [ROOT, <i>like</i> ]	<i>bagels with lox</i>	ARC-RIGHT	( <i>like</i> $\rightarrow$ <i>bagels</i> )
5. [ROOT, <i>like</i> , <i>bagels</i> ]	<i>with lox</i>	SHIFT	
6. [ROOT, <i>like</i> , <i>bagels</i> , <i>with</i> ]	<i>lox</i>	ARC-LEFT	( <i>with</i> $\leftarrow$ <i>lox</i> )
7. [ROOT, <i>like</i> , <i>bagels</i> ]	<i>lox</i>	ARC-RIGHT	( <i>bagels</i> $\rightarrow$ <i>lox</i> )
8. [ROOT, <i>like</i> , <i>bagels</i> , <i>lox</i> ]	$\emptyset$	REDUCE	
9. [ROOT, <i>like</i> , <i>bagels</i> ]	$\emptyset$	REDUCE	
10. [ROOT, <i>like</i> ]	$\emptyset$	REDUCE	
11. [ROOT]	$\emptyset$	DONE	

Table 11.3: Arc-eager derivation of the unlabeled dependency parse for the input *they like bagels with lox*.

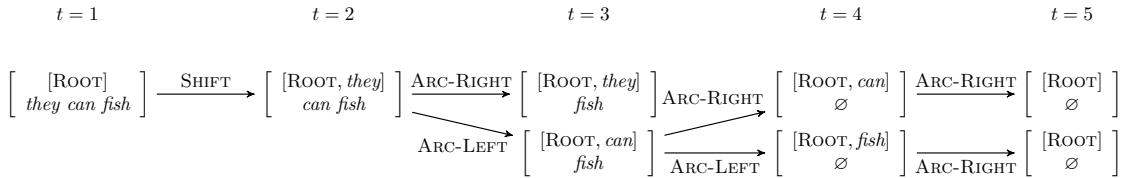


Figure 11.7: Beam search for unlabeled dependency parsing, with beam size  $K = 2$ . The arc lists for each configuration are not shown, but can be computed from the transitions.

6136 **dependency parsing**, a projective dependency parse is generated first, and then a set of  
 6137 graph transformation techniques are applied, producing non-projective edges (Nivre and  
 6138 Nilsson, 2005).

#### 6139 11.3.1.4 Beam search

6140 In “greedy” transition-based parsing, the parser tries to make the best decision at each  
 6141 configuration. This can lead to search errors, when an early decision locks the parser into  
 6142 a poor derivation. For example, in Table 11.2, if ARC-RIGHT were chosen at step 4, then  
 6143 the parser would later be forced to attach the prepositional phrase *with lox* to the verb  
 6144 *likes*. Note that the *likes*  $\rightarrow$  *bagels* arc is indeed part of the correct dependency parse, but  
 6145 the arc-standard transition system requires it to be created later in the derivation.

Beam search addresses this issue by maintaining a set of hypothetical derivations, called a beam. At step  $t$  of the derivation, there is a set of  $k$  hypotheses, each of which is a

tuple of a score and a sequence of actions,

$$h_t^{(k)} = (s_t^{(k)}, A_t^{(k)}) \quad [11.23]$$

Each hypothesis is then “expanded” by considering the set of all valid actions from the current configuration  $c_t^{(k)}$ , written  $\mathcal{A}(c_t^{(k)})$ . This yields a large set of new hypotheses. For each action  $a \in \mathcal{A}(c_t^{(k)})$ , we score the new hypothesis  $A_t^{(k)} \oplus a$ . The top  $k$  hypotheses by this scoring metric are kept, and parsing proceeds to the next step (Zhang and Clark, 2008). Note that beam search requires a scoring function for action *sequences*, rather than individual actions. This issue will be revisited in the next section.

An example of beam search is shown in Figure 11.7, with a beam size of  $K = 2$ . For the first transition, the only valid action is SHIFT, so there is only one possible configuration at  $t = 2$ . From this configuration, there are three possible actions. The top two are ARC-RIGHT and ARC-LEFT, and so the resulting hypotheses from these actions are on the beam at  $t = 3$ . From these configurations, there are three possible actions each, but the best two are expansions of the bottom hypothesis at  $t = 3$ . Parsing continues until  $t = 5$ , at which point both hypotheses reach an accepting state. The best-scoring hypothesis is then selected as the parse.

### 11.3.2 Scoring functions for transition-based parsers

Transition-based parsing requires selecting a series of actions. In greedy transition-based parsing, this can be done by training a classifier,

$$\hat{a} = \operatorname{argmax}_{a \in \mathcal{A}(c)} \Psi(a, c, \mathbf{w}; \boldsymbol{\theta}), \quad [11.24]$$

where  $\mathcal{A}(c)$  is the set of admissible actions in the current configuration  $c$ ,  $\mathbf{w}$  is the input, and  $\Psi$  is a scoring function with parameters  $\boldsymbol{\theta}$  (Yamada and Matsumoto, 2003).

A feature-based score can be computed,  $\Psi(a, c, \mathbf{w}) = \boldsymbol{\theta} \cdot \mathbf{f}(a, c, \mathbf{w})$ , using features that may consider any aspect of the current configuration and input sequence. Typical features for transition-based dependency parsing include: the word and part-of-speech of the top element on the stack; the word and part-of-speech of the first, second, and third elements on the input buffer; pairs and triples of words and parts-of-speech from the top of the stack and the front of the buffer; the distance (in tokens) between the element on the top of the stack and the element in the front of the input buffer; the number of modifiers of each of these elements; and higher-order dependency features as described above in the section on graph-based dependency parsing (see, e.g., Zhang and Nivre, 2011).

Parse actions can also be scored by neural networks. For example, Chen and Manning (2014) build a feedforward network in which the input layer consists of the concatenation of embeddings of several words and tags:

- 6175 • the top three words on the stack, and the first three words on the buffer;
- 6176 • the first and second leftmost and rightmost children (dependents) of the top two
- 6177       words on the stack;
- 6178 • the leftmost and right most grandchildren of the top two words on the stack;
- 6179 • embeddings of the part-of-speech tags of these words.

Let us call this base layer  $\mathbf{x}(c, \mathbf{w})$ , defined as,

$$c = (\sigma, \beta, A)$$

$$\mathbf{x}(c, \mathbf{w}) = [\mathbf{v}_{w_{\sigma_1}}, \mathbf{v}_{t_{\sigma_1}} \mathbf{v}_{w_{\sigma_2}}, \mathbf{v}_{t_{\sigma_2}}, \mathbf{v}_{w_{\sigma_3}}, \mathbf{v}_{t_{\sigma_3}}, \mathbf{v}_{w_{\beta_1}}, \mathbf{v}_{t_{\beta_1}}, \mathbf{v}_{w_{\beta_2}}, \mathbf{v}_{t_{\beta_2}}, \dots],$$

where  $\mathbf{v}_{w_{\sigma_1}}$  is the embedding of the first word on the stack,  $\mathbf{v}_{t_{\beta_2}}$  is the embedding of the part-of-speech tag of the second word on the buffer, and so on. Given this base encoding of the parser state, the score for the set of possible actions is computed through a feedforward network,

$$\mathbf{z} = g(\Theta^{(x \rightarrow z)} \mathbf{x}(c, \mathbf{w})) \quad [11.25]$$

$$\psi(a, c, \mathbf{w}; \boldsymbol{\theta}) = \Theta_a^{(z \rightarrow y)} \mathbf{z}, \quad [11.26]$$

6180 where the vector  $\mathbf{z}$  plays the same role as the features  $f(a, c, \mathbf{w})$ , but is a learned representation. Chen and Manning (2014) use a cubic elementwise activation function,  $g(x) = x^3$ ,  
 6181 so that the hidden layer models products across all triples of input features. The learning  
 6182 algorithm updates the embeddings as well as the parameters of the feedforward network.  
 6183

### 6184 11.3.3 Learning to parse

6185 Transition-based dependency parsing suffers from a mismatch between the supervision,  
 6186 which comes in the form of dependency trees, and the classifier's prediction space, which  
 6187 is a set of parsing actions. One solution is to create new training data by converting parse  
 6188 trees into action sequences; another is to derive supervision directly from the parser's  
 6189 performance.

#### 6190 11.3.3.1 Oracle-based training

6191 A transition system can be viewed as a function from action sequences (also called **deriva-**  
 6192 **tions**) to parse trees. The inverse of this function is a mapping from parse trees to deriva-  
 6193 tions, which is called an **oracle**. For the arc-standard and arc-eager parsing system, an  
 6194 oracle can be computed in linear time in the length of the derivation (Kübler et al., 2009,  
 6195 page 32). Both the arc-standard and arc-eager transition systems suffer from **spurious**  
 6196 **ambiguity**: there exist dependency parses for which multiple derivations are possible,

such as  $1 \leftarrow 2 \rightarrow 3$ . The oracle must choose between these different derivations. For example, the algorithm described by Kübler et al. (2009) would first create the left arc ( $1 \leftarrow 2$ ), and then create the right arc,  $(1 \leftarrow 2) \rightarrow 3$ ; another oracle might begin by shifting twice, resulting in the derivation  $1 \leftarrow (2 \rightarrow 3)$ .

Given such an oracle, a dependency treebank can be converted into a set of oracle action sequences  $\{A^{(i)}\}_{i=1}^N$ . The parser can be trained by stepping through the oracle action sequences, and optimizing on a classification-based objective that rewards selecting the oracle action. For transition-based dependency parsing, maximum conditional likelihood is a typical choice (Chen and Manning, 2014; Dyer et al., 2015):

$$p(a | c, \mathbf{w}) = \frac{\exp \Psi(a, c, \mathbf{w}; \boldsymbol{\theta})}{\sum_{a' \in \mathcal{A}(c)} \exp \Psi(a', c, \mathbf{w}; \boldsymbol{\theta})} \quad [11.27]$$

$$\hat{\boldsymbol{\theta}} = \underset{\boldsymbol{\theta}}{\operatorname{argmax}} \sum_{i=1}^N \sum_{t=1}^{|A^{(i)}|} \log p(a_t^{(i)} | c_t^{(i)}, \mathbf{w}), \quad [11.28]$$

where  $|A^{(i)}|$  is the length of the action sequence  $A^{(i)}$ .

Recall that beam search requires a scoring function for action sequences. Such a score can be obtained by adding the log-likelihoods (or hinge losses) across all actions in the sequence (Chen and Manning, 2014).

### 11.3.3.2 Global objectives

The objective in Equation 11.28 is **locally-normalized**: it is the product of normalized probabilities over individual actions. A similar characterization could be made of non-probabilistic algorithms in which hinge-loss objectives are summed over individual actions. In either case, training on individual actions can be sub-optimal with respect to global performance, due to the **label bias problem** (Lafferty et al., 2001; Andor et al., 2016).

As a stylized example, suppose that a given configuration appears 100 times in the training data, with action  $a_1$  as the oracle action in 51 cases, and  $a_2$  as the oracle action in the other 49 cases. However, in cases where  $a_2$  is correct, choosing  $a_1$  results in a cascade of subsequent errors, while in cases where  $a_1$  is correct, choosing  $a_2$  results in only a single error. A classifier that is trained on a local objective function will learn to always choose  $a_1$ , but choosing  $a_2$  would minimize the overall number of errors.

This observation motivates a global objective, such as the globally-normalized conditional likelihood,

$$p(A^{(i)} | \mathbf{w}; \boldsymbol{\theta}) = \frac{\exp \sum_{t=1}^{|A^{(i)}|} \Psi(a_t^{(i)}, c_t^{(i)}, \mathbf{w})}{\sum_{A' \in \mathbb{A}(\mathbf{w})} \exp \sum_{t=1}^{|A'|} \Psi(a'_t, c'_t, \mathbf{w})}, \quad [11.29]$$

where the denominator sums over the set of all possible action sequences,  $\mathbb{A}(\mathbf{w})$ .<sup>5</sup> In the conditional random field model for sequence labeling (§ 7.5.3), it was possible to compute this sum explicitly, using dynamic programming. In transition-based parsing, this is not possible. However, the sum can be approximated using beam search,

$$\sum_{A' \in \mathbb{A}(\mathbf{w})} \exp \sum_{t=1}^{|A'|} \Psi(a'_t, c'_t, \mathbf{w}) \approx \sum_{k=1}^K \exp \sum_{t=1}^{|A^{(k)}|} \Psi(a_t^{(k)}, c_t^{(k)}, \mathbf{w}), \quad [11.30]$$

where  $A^{(k)}$  is an action sequence on a beam of size  $K$ . This gives rise to the following loss function,

$$L(\boldsymbol{\theta}) = - \sum_{t=1}^{|A^{(i)}|} \Psi(a_t^{(i)}, c_t^{(i)}, \mathbf{w}) + \log \sum_{k=1}^K \exp \sum_{t=1}^{|A^{(k)}|} \Psi(a_t^{(k)}, c_t^{(k)}, \mathbf{w}). \quad [11.31]$$

6220 The derivatives of this loss involve expectations with respect to a probability distribution  
6221 over action sequences on the beam.

### 6222 11.3.3.3 \*Early update and the incremental perceptron

6223 When learning in the context of beam search, the goal is to learn a decision function so that  
6224 the gold dependency parse is always reachable from at least one of the partial derivations  
6225 on the beam. (The combination of a transition system (such as beam search) and a scoring  
6226 function for actions is known as a **policy**.) To achieve this, we can make an **early update**  
6227 as soon as the oracle action sequence “falls off” the beam, even before a complete analysis  
6228 is available (Collins and Roark, 2004; Daumé III and Marcu, 2005). The loss can be based  
6229 on the best-scoring hypothesis on the beam, or the sum of all hypotheses (Huang et al.,  
6230 2012).

6231 For example, consider the beam search in Figure 11.7. In the correct parse, *fish* is the  
6232 head of dependency arcs to both of the other two words. In the arc-standard system,  
6233 this can be achieved only by using SHIFT for the first two actions. At  $t = 3$ , the oracle  
6234 action sequence has fallen off the beam. The parser should therefore stop, and update the  
6235 parameters by the gradient  $\frac{\partial}{\partial \boldsymbol{\theta}} L(A_{1:3}^{(i)}, \{A_{1:3}^{(k)}\}; \boldsymbol{\theta})$ , where  $A_{1:3}^{(i)}$  is the first three actions of the  
6236 oracle sequence, and  $\{A_{1:3}^{(k)}\}$  is the beam.

6237 This integration of incremental search and learning was first developed in the **incremental**  
6238 **perceptron** (Collins and Roark, 2004). This method updates the parameters with  
6239 respect to a hinge loss, which compares the top-scoring hypothesis and the gold action

---

<sup>5</sup>Andor et al. (2016) prove that the set of globally-normalized conditional distributions is a strict superset of the set of locally-normalized conditional distributions, and that globally-normalized conditional models are therefore strictly more expressive.

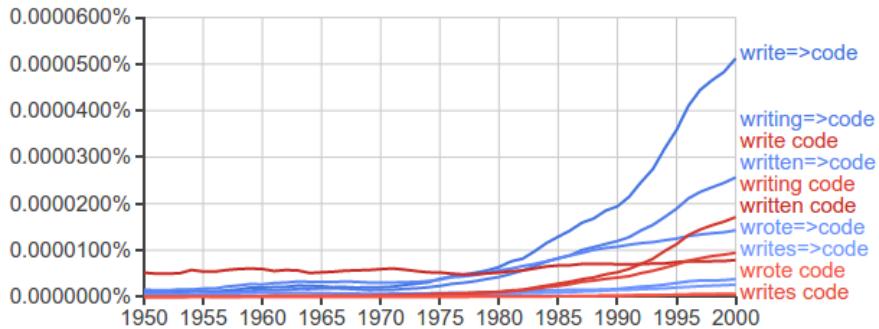


Figure 11.8: Google n-grams results for the bigram *write code* and the dependency arc *write => code* (and their morphological variants)

6240 sequence, up to the current point  $t$ . Several improvements to this basic protocol are pos-  
6241 sible:

- 6242 • As noted earlier, the gold dependency parse can be derived by multiple action se-  
6243 quences. Rather than checking for the presence of a single oracle action sequence on  
6244 the beam, we can check if the gold dependency parse is *reachable* from the current  
6245 beam, using a **dynamic oracle** (Goldberg and Nivre, 2012).
- 6246 • By maximizing the score of the gold action sequence, we are training a decision  
6247 function to find the correct action given the gold context. But in reality, the parser  
6248 will make errors, and the parser is not trained to find the best action given a context  
6249 that may not itself be optimal. This issue is addressed by various generalizations of  
6250 incremental perceptron, known as **learning to search** (Daumé III et al., 2009). Some  
6251 of these methods are discussed in chapter 15.

## 6252 11.4 Applications

6253 Dependency parsing is used in many real-world applications: any time you want to know  
6254 about pairs of words which might not be adjacent, you can use dependency arcs instead  
6255 of regular expression search patterns. For example, you may want to match strings like  
6256 *delicious pastries*, *delicious French pastries*, and *the pastries are delicious*.

6257 It is possible to search the Google *n*-gramscorpus by dependency edges, finding the  
6258 trend in how often a dependency edge appears over time. For example, we might be inter-  
6259 ested in knowing when people started talking about *writing code*, but we also want *write*  
6260 *some code*, *write good code*, *write all the code*, etc. The result of a search on the dependency  
6261 edge *write → code* is shown in Figure 11.8. This capability has been applied to research

6262 in digital humanities, such as the analysis of gender in Shakespeare Muralidharan and  
 6263 Hearst (2013).

A classic application of dependency parsing is **relation extraction**, which is described in chapter 17. The goal of relation extraction is to identify entity pairs, such as

(MELVILLE, MOBY-DICK)  
 (TOLSTOY, WAR AND PEACE)  
 (MARQUÉZ, 100 YEARS OF SOLITUDE)  
 (SHAKESPEARE, A MIDSUMMER NIGHT'S DREAM),

6264 which stand in some relation to each other (in this case, the relation is authorship). Such  
 6265 entity pairs are often referenced via consistent chains of dependency relations. Therefore,  
 6266 dependency paths are often a useful feature in supervised systems which learn to detect  
 6267 new instances of a relation, based on labeled examples of other instances of the same  
 6268 relation type (Culotta and Sorensen, 2004; Fundel et al., 2007; Mintz et al., 2009).

6269 Cui et al. (2005) show how dependency parsing can improve automated question an-  
 6270 swering. Suppose you receive the following query:

6271 (11.1) What percentage of the nation's cheese does Wisconsin produce?

6272 The corpus contains this sentence:

6273 (11.2) In Wisconsin, where farmers produce 28% of the nation's cheese, ...

6274 The location of *Wisconsin* in the surface form of this string makes it a poor match for the  
 6275 query. However, in the dependency graph, there is an edge from *produce* to *Wisconsin* in  
 6276 both the question and the potential answer, raising the likelihood that this span of text is  
 6277 relevant to the question.

6278 A final example comes from sentiment analysis. As discussed in chapter 4, the polarity  
 6279 of a sentence can be reversed by negation, e.g.

6280 (11.3) *There is no reason at all to believe the polluters will suddenly become reasonable.*

6281 By tracking the sentiment polarity through the dependency parse, we can better iden-  
 6282 tify the overall polarity of the sentence, determining when key sentiment words are re-  
 6283 versed (Wilson et al., 2005; Nakagawa et al., 2010).

## 6284 Additional resources

6285 More details on dependency grammar and parsing algorithms can be found in the manuscript  
 6286 by Kübler et al. (2009). For a comprehensive but whimsical overview of graph-based de-  
 6287 pendency parsing algorithms, see Eisner (1997). Jurafsky and Martin (2018) describe an

6288 **agenda-based** version of beam search, in which the beam contains hypotheses of varying  
 6289 lengths. New hypotheses are added to the beam only if their score is better than the worst  
 6290 item currently on the beam. Another search algorithm for transition-based parsing is  
 6291 **easy-first**, which abandons the left-to-right traversal order, and adds the highest-scoring  
 6292 edges first, regardless of where they appear (Goldberg and Elhadad, 2010). Goldberg et al.  
 6293 (2013) note that although transition-based methods can be implemented in linear time in  
 6294 the length of the input, naïve implementations of beam search will require quadratic time,  
 6295 due to the cost of copying each hypothesis when it is expanded on the beam. This issue  
 6296 can be addressed by using a more efficient data structure for the stack.

## 6297 Exercises

- 6298 1. The dependency structure  $1 \leftarrow 2 \rightarrow 3$ , with 2 as the root, can be obtained from more  
 6299 than one set of actions in arc-standard parsing. List both sets of actions that can  
 6300 obtain this parse.
- 6301 2. This problem develops the relationship between dependency parsing and lexical-  
 6302 ized context-free parsing. Suppose you have a set of unlabeled arc scores  $\{\psi(i \rightarrow$   
 6303  $j)\}_{i,j=1}^M \cup \{\psi(\text{ROOT} \rightarrow j)\}_{j=1}^M$ .
  - 6304 a) Assuming each word type occurs no more than once in the input ( $(i \neq j) \Rightarrow$   
   6305  $(w_i \neq w_j)$ ), how would you construct a weighted lexicalized context-free gram-  
   6306 mar so that the score of *any* projective dependency tree is equal to the score of  
   6307 some equivalent derivation in the lexicalized context-free grammar?
  - 6308 b) Verify that your method works for the example *They fish*.
  - 6309 c) Does your method require the restriction that each word type occur no more  
   6310 than once in the input? If so, why?
  - 6311 d) \*If your method required that each word type occur only once in the input,  
   6312 show how to generalize it.
- 6313 3. In arc-factored dependency parsing of an input of length  $M$ , the score of a parse  
 6314 is the sum of  $M$  scores, one for each arc. In second order dependency parsing, the  
 6315 total score is the sum over many more terms. How many terms are the score of the  
 6316 parse for Figure 11.2, using a second-order dependency parser with grandparent  
 6317 and sibling features? Assume that a child of ROOT has no grandparent score, and  
 6318 that a node with no siblings has no sibling scores.
- 6319 4. a) In the worst case, how many terms can be involved in the score of an input of  
 6320 length  $M$ , assuming second-order dependency parsing? Describe the structure  
 6321 of the worst-case parse. As in the previous problem, assume that there is only  
 6322 one child of ROOT, and that it does not have any grandparent scores.

- 6323            b) What about third-order dependency parsing?
- 6324        5. Provide the UD-style dependency parse for the sentence *Xi-Lan eats shoots and leaves*,  
 6325        assuming *leaves* is a verb. Provide arc-standard and arc-eager derivations for this  
 6326        dependency parse.
- 6327        6. Compute an upper bound on the number of successful derivations in arc-standard  
 6328        shift-reduce parsing for unlabeled dependencies, as a function of the length of the  
 6329        input,  $M$ . Hint: a lower bound is the number of projective decision trees,  $\frac{1}{M+1} \binom{3M-2}{M-1}$  (Zhang,  
 6330        2017), where  $\binom{a}{b} = \frac{a!}{(a-b)!b!}$ .
- 6331        7. In § 11.3.3.2, we encounter the **label bias** problem, in which a decision may be lo-  
 6332        cally correct, yet lead to a cascade of errors. Design a scenario in which this occurs.  
 6333        Specifically:
- 6334        • Assume an arc-standard dependency parser, whose action classifier considers  
 6335        only the words at the top of the stack and at the front of the input buffer.
  - 6336        • Design two examples, which both involve a decision with identical features:
    - 6337        – In one example, shift is the correct decision; in the other example, arc-left  
 6338        or arc-right is the correct decision.
    - 6339        – In one of the two examples, a mistake should lead to a cascade of attach-  
 6340        ment errors.
    - 6341        – In the other example, a mistake should lead only to a single attachment  
 6342        error.
- 6343        For the following exercises, run a dependency parser, such as Stanford’s CoreNLP  
 6344        parser, on a large corpus of text (at least  $10^5$  tokens), such as `nltk.corpus.webtext`.
- 6345        8. The dependency relation NMOD:POSS indicates possession. Compute the top ten  
 6346        words most frequently possessed by each of the following pronouns: *his*, *her*, *our*,  
 6347        *my*, *your*, and *their* (inspired by Muralidharan and Hearst, 2013).
- 6348        9. Count all pairs of words grouped by the CONJ relation. Select all pairs of words  $(i, j)$   
 6349        for which  $i$  and  $j$  each participate in CONJ relations at least five times. Compute and  
 sort by the **pointwise mutual information**, which is defined in § 14.3 as,

$$\text{PMI}(i, j) = \log \frac{\text{p}(i, j)}{\text{p}(i)\text{p}(j)}. \quad [11.32]$$

6348        Here,  $\text{p}(i)$  is the fraction of CONJ relations containing word  $i$  (in either position), and  
 6349         $\text{p}(i, j)$  is the fraction of such relations linking  $i$  and  $j$  (in any order).

- 6350    10. In § 4.2, we encountered lexical semantic relationships such as **synonymy** (same  
6351    meaning), **antonymy** (opposite meaning), and **hyponymy** (*i* is a special case of  
6352    *j*). Another relevant relation is **co-hyponymy**, which means that *i* and *j* share a  
6353    hyponym. Of the top 20 pairs identified by PMI in the previous problem, how  
6354    many participate in synsets that are linked by one of these four relations?



6355

## **Part III**

6356

# **Meaning**



6357 **Chapter 12**

6358 **Logical semantics**

6359 The previous few chapters have focused on building systems that reconstruct the **syntax**  
6360 of natural language — its structural organization — through tagging and parsing. But  
6361 some of the most exciting and promising potential applications of language technology  
6362 involve going beyond syntax to **semantics** — the underlying meaning of the text:

- 6363 • Answering questions, such as *where is the nearest coffeeshop?* or *what is the middle name*  
6364 *of the mother of the 44th President of the United States?*.
- 6365 • Building a robot that can follow natural language instructions to execute tasks.
- 6366 • Translating a sentence from one language into another, while preserving the under-  
6367 lying meaning.
- 6368 • Fact-checking an article by searching the web for contradictory evidence.
- 6369 • Logic-checking an argument by identifying contradictions, ambiguity, and unsup-  
6370 ported assertions.

6371 Semantic analysis involves converting natural language into a **meaning representa-**  
6372 **tion**. To be useful, a meaning representation must meet several criteria:

- 6373 • **c1**: it should be unambiguous: unlike natural language, there should be exactly one  
6374 meaning per statement;
- 6375 • **c2**: it should provide a way to link language to external knowledge, observations,  
6376 and actions;
- 6377 • **c3**: it should support computational **inference**, so that meanings can be combined  
6378 to derive additional knowledge;
- 6379 • **c4**: it should be expressive enough to cover the full range of things that people talk  
6380 about in natural language.

6381 Much more than this can be said about the question of how best to represent knowledge  
 6382 for computation (e.g., Sowa, 2000), but this chapter will focus on these four criteria.

## 6383 12.1 Meaning and denotation

6384 The first criterion for a meaning representation is that statements in the representation  
 6385 should be unambiguous — they should have only one possible interpretation. Natural  
 6386 language does not have this property: as we saw in chapter 10, sentences like *cats scratch*  
 6387 *people with claws* have multiple interpretations.

6388 But what does it mean for a statement to be unambiguous? Programming languages  
 6389 provide a useful example: the output of a program is completely specified by the rules of  
 6390 the language and the properties of the environment in which the program is run. For ex-  
 6391 ample, the python code  $5 + 3$  will have the output 8, as will the codes  $(4 * 4) - (3 * 3) + 1$   
 6392 and  $((8))$ . This output is known as the **denotation** of the program, and can be written  
 6393 as,

$$\llbracket 5+3 \rrbracket = \llbracket (4 * 4) - (3 * 3) + 1 \rrbracket = \llbracket ((8)) \rrbracket = 8. \quad [12.1]$$

6394 The denotations of these arithmetic expressions are determined by the meaning of the  
 6395 **constants** (e.g., 5, 3) and the **relations** (e.g.,  $+$ ,  $*$ ,  $(,)$ ). Now let's consider another snippet  
 6396 of python code, `double(4)`. The denotation of this code could be,  $\llbracket \text{double}(4) \rrbracket = 8$ , or  
 6397 it could be  $\llbracket \text{double}(4) \rrbracket = 44$  — it depends on the meaning of `double`. This meaning  
 6398 is defined in a **world model**  $\mathcal{M}$  as an infinite set of pairs. We write the denotation with  
 6399 respect to model  $\mathcal{M}$  as  $\llbracket \cdot \rrbracket_{\mathcal{M}}$ , e.g.,  $\llbracket \text{double} \rrbracket_{\mathcal{M}} = \{(0, 0), (1, 2), (2, 4), \dots\}$ . The world  
 6400 model would also define the (infinite) list of constants, e.g.,  $\{0, 1, 2, \dots\}$ . As long as the  
 6401 denotation of string  $\phi$  in model  $\mathcal{M}$  can be computed unambiguously, the language can be  
 6402 said to be unambiguous.

6403 This approach to meaning is known as **model-theoretic semantics**, and it addresses  
 6404 not only criterion *c1* (no ambiguity), but also *c2* (connecting language to external knowl-  
 6405 edge, observations, and actions). For example, we can connect a representation of the  
 6406 meaning of a statement like *the capital of Georgia* with a world model that includes knowl-  
 6407 edge base of geographical facts, obtaining the denotation `Atlanta`. We might populate  
 6408 a world model by applying an image analysis algorithm to Figure 12.1, and then use this  
 6409 world model to evaluate **propositions** like *a man is riding a moose*. Another desirable prop-  
 6410 erty of model-theoretic semantics is that when the facts change, the denotations change  
 6411 too: the meaning representation of *President of the USA* would have a different denotation  
 6412 in the model  $\mathcal{M}_{2014}$  as it would in  $\mathcal{M}_{2022}$ .



Figure 12.1: A (doctored) image, which could be the basis for a world model

## 6413 12.2 Logical representations of meaning

6414 Criterion *c3* requires that the meaning representation support inference — for example,  
 6415 automatically deducing new facts from known premises. While many representations  
 6416 have been proposed that meet these criteria, the most mature is the language of first-order  
 6417 logic.<sup>1</sup>

### 6418 12.2.1 Propositional logic

6419 The bare bones of logical meaning representation are Boolean operations on propositions:

6420 **Propositional symbols.** Greek symbols like  $\phi$  and  $\psi$  will be used to represent **proposi-**  
 6421 **tions**, which are statements that are either true or false. For example,  $\phi$  may corre-  
 6422 spond to the proposition, *bagels are delicious*.

6423 **Boolean operators.** We can build up more complex propositional formulas from Boolean  
 6424 operators. These include:

- 6425 • Negation  $\neg\phi$ , which is true if  $\phi$  is false.

---

<sup>1</sup>Alternatives include the “variable-free” representation used in semantic parsing of geographical queries (Zelle and Mooney, 1996) and robotic control (Ge and Mooney, 2005), and dependency-based compositional semantics (Liang et al., 2013).

- 6426 • Conjunction,  $\phi \wedge \psi$ , which is true if both  $\phi$  and  $\psi$  are true.
- 6427 • Disjunction,  $\phi \vee \psi$ , which is true if at least one of  $\phi$  and  $\psi$  is true
- 6428 • Implication,  $\phi \Rightarrow \psi$ , which is true unless  $\phi$  is true and  $\psi$  is false. Implication
- 6429 has identical truth conditions to  $\neg\phi \vee \psi$ .
- 6430 • Equivalence,  $\phi \Leftrightarrow \psi$ , which is true if  $\phi$  and  $\psi$  are both true or both false. Equiv-
- 6431 alence has identical truth conditions to  $(\phi \Rightarrow \psi) \wedge (\psi \Rightarrow \phi)$ .

6432 It is not strictly necessary to have all five Boolean operators: readers familiar with  
 6433 Boolean logic will know that it is possible to construct all other operators from either the  
 6434 NAND (not-and) or NOR (not-or) operators. Nonetheless, it is clearest to use all five  
 6435 operators. From the truth conditions for these operators, it is possible to define a number  
 6436 of “laws” for these Boolean operators, such as,

- 6437 • *Commutativity*:  $\phi \wedge \psi = \psi \wedge \phi$ ,  $\phi \vee \psi = \psi \vee \phi$
- 6438 • *Associativity*:  $\phi \wedge (\psi \wedge \chi) = (\phi \wedge \psi) \wedge \chi$ ,  $\phi \vee (\psi \vee \chi) = (\phi \vee \psi) \vee \chi$
- 6439 • *Complementation*:  $\phi \wedge \neg\phi = \perp$ ,  $\phi \vee \neg\phi = \top$ , where  $\top$  indicates a true proposition  
 6440 and  $\perp$  indicates a false proposition.

These laws can be combined to derive further equivalences, which can support logical inferences. For example, suppose  $\phi = \text{The music is loud}$  and  $\psi = \text{Max can't sleep}$ . Then if we are given,

$$\begin{aligned} \phi \Rightarrow \psi & \quad \text{If the music is loud, Max can't sleep.} \\ \phi & \quad \text{The music is loud.} \end{aligned}$$

6441 we can derive  $\psi$  (*Max can't sleep*) by application of **modus ponens**, which is one of a  
 6442 set of **inference rules** that can be derived from more basic laws and used to manipulate  
 6443 propositional formulas. **Automated theorem provers** are capable of applying inference  
 6444 rules to a set of premises to derive desired propositions (Loveland, 2016).

### 6445 12.2.2 First-order logic

6446 Propositional logic is so named because it treats propositions as its base units. However,  
 6447 the criterion *c4* states that our meaning representation should be sufficiently expressive.  
 6448 Now consider the sentence pair,

- 6449 (12.1) If anyone is making noise, then Max can't sleep.  
 6450 Abigail is making noise.

6451 People are capable of making inferences from this sentence pair, but such inferences re-  
 6452 quire formal tools that are beyond propositional logic. To understand the relationship

6453 between the statement *anyone is making noise* and the statement *Abigail is making noise*, our  
 6454 meaning representation requires the additional machinery of **first-order logic** (FOL).

6455 In FOL, logical propositions can be constructed from relationships between entities.  
 6456 Specifically, FOL extends propositional logic with the following classes of terms:

6457 **Constants.** These are elements that name individual entities in the model, such as MAX  
 6458 and ABIGAIL. The denotation of each constant in a model  $\mathcal{M}$  is an element in the  
 6459 model, e.g.,  $[\![\text{MAX}]\!] = m$  and  $[\![\text{ABIGAIL}]\!] = a$ .

6460 **Relations.** Relations can be thought of as sets of entities, or sets of tuples. For example,  
 6461 the relation CAN-SLEEP is defined as the set of entities who can sleep, and has the  
 6462 denotation  $[\![\text{CAN-SLEEP}]\!] = \{a, m, \dots\}$ . To test the truth value of the proposition  
 6463 CAN-SLEEP(MAX), we ask whether  $[\![\text{MAX}]\!] \in [\![\text{CAN-SLEEP}]\!]$ . Logical relations that are  
 6464 defined over sets of entities are sometimes called **properties**.

6465 Relations may also be ordered tuples of entities. For example BROTHER(MAX,ABIGAIL)  
 6466 expresses the proposition that MAX is the brother of ABIGAIL. The denotation of  
 6467 such relations is a set of tuples,  $[\![\text{BROTHER}]\!] = \{(m, a), (x, y), \dots\}$ . To test the  
 6468 truth value of the proposition BROTHER(MAX,ABIGAIL), we ask whether the tuple  
 6469  $([\![\text{MAX}]\!], [\![\text{ABIGAIL}]\!])$  is in the denotation  $[\![\text{BROTHER}]\!]$ .

Using constants and relations, it is possible to express statements like *Max can't sleep* and *Max is Abigail's brother*:

$$\neg \text{CAN-SLEEP}(\text{MAX}) \\ \text{BROTHER}(\text{MAX}, \text{ABIGAIL}).$$

These statements can also be combined using Boolean operators, such as,

$$(\text{BROTHER}(\text{MAX}, \text{ABIGAIL}) \vee \text{BROTHER}(\text{MAX}, \text{STEVE})) \Rightarrow \neg \text{CAN-SLEEP}(\text{MAX}).$$

6470 This fragment of first-order logic permits only statements about specific entities. To  
 6471 support inferences about statements like *If anyone is making noise, then Max can't sleep*,  
 6472 two more elements must be added to the meaning representation:

6473 **Variables.** Variables are mechanisms for referring to entities that are not locally specified.  
 6474 We can then write CAN-SLEEP( $x$ ) or BROTHER( $x$ , ABIGAIL). In these cases,  $x$  is a **free  
 6475 variable**, meaning that we have not committed to any particular assignment.

6476 **Quantifiers.** Variables are bound by quantifiers. There are two quantifiers in first-order  
 6477 logic.<sup>2</sup>

- 6478 • The **existential quantifier**  $\exists$ , which indicates that there must be at least one en-  
 6479 tity to which the variable can bind. For example, the statement  $\exists x \text{MAKES-NOISE}(x)$   
 6480 indicates that there is at least one entity for which MAKES-NOISE is true.  
 6481 • The **universal quantifier**  $\forall$ , which indicates that the variable must be able to  
 6482 bind to any entity in the model. For example, the statement,

$$\text{MAKES-NOISE(ABIGAIL)} \Rightarrow (\forall x \neg \text{CAN-SLEEP}(x)) \quad [12.3]$$

6483 asserts that if Abigail makes noise, no one can sleep.

6484 The expressions  $\exists x$  and  $\forall x$  make  $x$  into a **bound variable**. A formula that contains  
 6485 no free variables is a **sentence**.

6486 **Functions.** Functions map from entities to entities, e.g.,  $\llbracket \text{CAPITAL-OF(GEORGIA)} \rrbracket = \llbracket \text{ATLANTA} \rrbracket$ .  
 6487 With functions, it is convenient to add an equality operator, supporting statements  
 6488 like,

$$\forall x \exists y \text{MOTHER-OF}(x) = \text{DAUGHTER-OF}(y). \quad [12.4]$$

6489 Note that MOTHER-OF is a functional analogue of the relation MOTHER, so that  
 6490  $\text{MOTHER-OF}(x) = y$  if  $\text{MOTHER}(x, y)$ . Any logical formula that uses functions can be  
 6491 rewritten using only relations and quantification. For example,

$$\text{MAKES-NOISE}(\text{MOTHER-OF(ABIGAIL)}) \quad [12.5]$$

6492 can be rewritten as  $\exists x \text{MAKES-NOISE}(x) \wedge \text{MOTHER}(x, \text{ABIGAIL})$ .

An important property of quantifiers is that the order can matter. Unfortunately, natural language is rarely clear about this! The issue is demonstrated by examples like *everyone speaks a language*, which has the following interpretations:

$$\forall x \exists y \text{ SPEAKS}(x, y) \quad [12.6]$$

$$\exists y \forall x \text{ SPEAKS}(x, y). \quad [12.7]$$

6493 In the first case,  $y$  may refer to several different languages, while in the second case, there  
 6494 is a single  $y$  that is spoken by everyone.

---

<sup>2</sup>In first-order logic, it is possible to quantify only over entities. In **second-order logic**, it is possible to quantify over properties, supporting statements like *Butch has every property that a good boxer has* (example from Blackburn and Bos, 2005),

$$\forall P \forall x ((\text{GOOD-BOXER}(x) \Rightarrow P(x)) \Rightarrow P(\text{BUTCH})). \quad [12.2]$$

## 6495 12.2.2.1 Truth-conditional semantics

6496 One way to look at the meaning of an FOL sentence  $\phi$  is as a set of **truth conditions**,  
 6497 or models under which  $\phi$  is satisfied. But how to determine whether a sentence is true  
 6498 or false in a given model? We will approach this inductively, starting with a predicate  
 6499 applied to a tuple of constants. The truth of such a sentence depends on whether the  
 6500 tuple of denotations of the constants is in the denotation of the predicate. For example,  
 6501 CAPITAL(GEORGIA,ATLANTA) is true in model  $\mathcal{M}$  iff,

$$(\llbracket \text{GEORGIA} \rrbracket_{\mathcal{M}}, \llbracket \text{ATLANTA} \rrbracket_{\mathcal{M}}) \in \llbracket \text{CAPITAL} \rrbracket_{\mathcal{M}}. \quad [12.8]$$

6502 The Boolean operators  $\wedge, \vee, \dots$  provide ways to construct more complicated sentences,  
 6503 and the truth of such statements can be assessed based on the truth tables associated with  
 6504 these operators. The statement  $\exists x\phi$  is true if there is some assignment of the variable  $x$   
 6505 to an entity in the model such that  $\phi$  is true; the statement  $\forall x\phi$  is true if  $\phi$  is true under  
 6506 all possible assignments of  $x$ . More formally, we would say that  $\phi$  is **satisfied** under  $\mathcal{M}$ ,  
 6507 written as  $\mathcal{M} \models \phi$ .

6508 Truth conditional semantics allows us to define several other properties of sentences  
 6509 and pairs of sentences. Suppose that in every  $\mathcal{M}$  under which  $\phi$  is satisfied, another  
 6510 formula  $\psi$  is also satisfied; then  $\phi$  **entails**  $\psi$ , which is also written as  $\phi \models \psi$ . For example,

$$\text{CAPITAL(GEORGIA,ATLANTA)} \models \exists x \text{CAPITAL(GEORGIA, } x\text{)}. \quad [12.9]$$

6511 A statement that is satisfied under any model, such as  $\phi \vee \neg\phi$ , is **valid**, written  $\models (\phi \vee$   
 6512  $\neg\phi)$ . A statement that is not satisfied under any model, such as  $\phi \wedge \neg\phi$ , is **unsatisfiable**,  
 6513 or **inconsistent**. A **model checker** is a program that determines whether a sentence  $\phi$   
 6514 is satisfied in  $\mathcal{M}$ . A **model builder** is a program that constructs a model in which  $\phi$   
 6515 is satisfied. The problems of checking for consistency and validity in first-order logic  
 6516 are **undecidable**, meaning that there is no algorithm that can automatically determine  
 6517 whether an FOL formula is valid or inconsistent.

## 6518 12.2.2.2 Inference in first-order logic

6519 Our original goal was to support inferences that combine general statements *If anyone is*  
*making noise, then Max can't sleep* with specific statements like *Abigail is making noise*. We  
 6520 can now represent such statements in first-order logic, but how are we to perform the  
 6521 inference that *Max can't sleep*? One approach is to use “generalized” versions of proposi-  
 6522 tional inference rules like modus ponens, which can be applied to FOL formulas. By  
 6523 repeatedly applying such inference rules to a knowledge base of facts, it is possible to  
 6524 produce proofs of desired propositions. To find the right sequence of inferences to derive  
 6525 a desired theorem, classical artificial intelligence search algorithms like backward chain-  
 6526 ing can be applied. Such algorithms are implemented in interpreters for the `prolog` logic  
 6527 programming language (Pereira and Shieber, 2002).

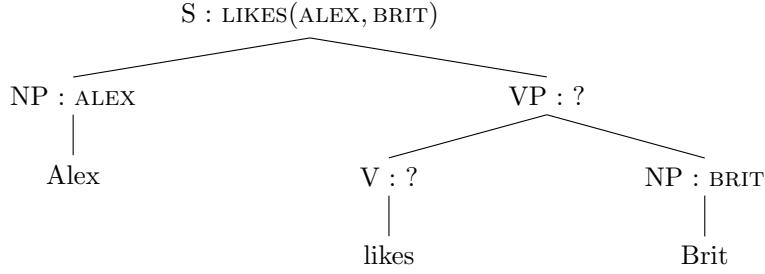


Figure 12.2: The principle of compositionality requires that we identify meanings for the constituents *likes* and *likes Brit* that will make it possible to compute the meaning for the entire sentence.

### 6529 12.3 Semantic parsing and the lambda calculus

6530 The previous section laid out a lot of formal machinery; the remainder of this chapter  
 6531 links these formalisms back to natural language. Given an English sentence like *Alex likes*  
 6532 *Brit*, how can we obtain the desired first-order logical representation,  $\text{LIKES}(\text{ALEX}, \text{BRIT})$ ?  
 6533 This is the task of **semantic parsing**. Just as a syntactic parser is a function from a natu-  
 6534 ral language sentence to a syntactic structure such as a phrase structure tree, a semantic  
 6535 parser is a function from natural language to logical formulas.

6536 As in syntactic analysis, semantic parsing is difficult because the space of inputs and  
 6537 outputs is very large, and their interaction is complex. Our best hope is that, like syntactic  
 6538 parsing, semantic parsing can somehow be decomposed into simpler sub-problems. This  
 6539 idea, usually attributed to the German philosopher Gottlob Frege, is called the **principle**  
 6540 **of compositionality**: the meaning of a complex expression is a function of the meanings of  
 6541 that expression's constituent parts. We will define these "constituent parts" as syntactic  
 6542 constituents: noun phrases and verb phrases. These constituents are combined using  
 6543 function application: if the syntactic parse contains the production  $x \rightarrow y z$ , then the  
 6544 semantics of  $x$ , written  $x.\text{sem}$ , will be computed as a function of the semantics of the  
 6545 constituents,  $y.\text{sem}$  and  $z.\text{sem}$ .<sup>3</sup> <sup>4</sup>

---

<sup>3</sup>§ 9.3.2 briefly discusses Combinatory Categorial Grammar (CCG) as an alternative to a phrase-structure analysis of syntax. CCG is argued to be particularly well-suited to semantic parsing (Hockenmaier and Steedman, 2007), and is used in much of the contemporary work on machine learning for semantic parsing, summarized in § 12.4.

<sup>4</sup>The approach of algorithmically building up meaning representations from a series of operations on the syntactic structure of a sentence is generally attributed to the philosopher Richard Montague, who published a series of influential papers on the topic in the early 1970s (e.g., Montague, 1973).

6546 **12.3.1 The lambda calculus**

6547 Let's see how this works for a simple sentence like *Alex likes Brit*, whose syntactic structure  
 6548 is shown in Figure 12.2. Our goal is the formula, LIKES(ALEX,BRIT), and it is clear that the  
 6549 meaning of the constituents *Alex* and *Brit* should be ALEX and BRIT. That leaves two more  
 6550 constituents: the verb *likes*, and the verb phrase *likes Brit*. The meanings of these units  
 6551 must be defined in a way that makes it possible to recover the desired meaning for the  
 6552 entire sentence by function application. If the meanings of *Alex* and *Brit* are constants,  
 6553 then the meanings of *likes* and *likes Brit* must be functional expressions, which can be  
 6554 applied to their siblings to produce the desired analyses.

6555 Modeling these partial analyses requires extending the first-order logic meaning rep-  
 6556 resentation. We do this by adding **lambda expressions**, which are descriptions of anony-  
 6557 mous functions,<sup>5</sup> e.g.,

$$\lambda x.\text{LIKES}(x, \text{BRIT}). \quad [12.10]$$

6558 This functional expression is the meaning of the verb phrase *likes Brit*; it takes a single  
 6559 argument, and returns the result of substituting that argument for  $x$  in the expression  
 6560  $\text{LIKES}(x, \text{BRIT})$ . We write this substitution as,

$$(\lambda x.\text{LIKES}(x, \text{BRIT}))@\text{ALEX} = \text{LIKES}(\text{ALEX}, \text{BRIT}), \quad [12.11]$$

6561 with the symbol "@" indicating function application. Function application in the lambda  
 6562 calculus is sometimes called  **$\beta$ -reduction** or  **$\beta$ -conversion**. The expression  $\phi@\psi$  indicates  
 6563 a function application to be performed by  $\beta$ -reduction, and  $\phi(\psi)$  indicates a function or  
 6564 predicate in the final logical form.

6565 Equation 12.11 shows how to obtain the desired semantics for the sentence *Alex likes*  
 6566 *Brit*: by applying the lambda expression  $\lambda x.\text{LIKES}(x, \text{BRIT})$  to the logical constant ALEX.  
 6567 This rule of composition can be specified in a **syntactic-semantic grammar**, in which  
 6568 syntactic productions are paired with semantic operations. For the syntactic production  
 6569  $S \rightarrow NP VP$ , we have the semantic rule  $VP.sem @ NP.sem$ .

The meaning of the transitive verb phrase *likes Brit* can also be obtained by function application on its syntactic constituents. For the syntactic production  $VP \rightarrow V NP$ , we apply the semantic rule,

$$VP.sem = (V.sem) @ NP.sem \quad [12.12]$$

$$= (\lambda y. \lambda x. \text{LIKES}(x, y)) @ (\text{BRIT}) \quad [12.13]$$

$$= \lambda x. \text{LIKES}(x, \text{BRIT}). \quad [12.14]$$

---

<sup>5</sup>Formally, all first-order logic formulas are lambda expressions; in addition, if  $\phi$  is a lambda expression, then  $\lambda x.\phi$  is also a lambda expression. Readers who are familiar with functional programming will recognize lambda expressions from their use in programming languages such as Lisp and Python.

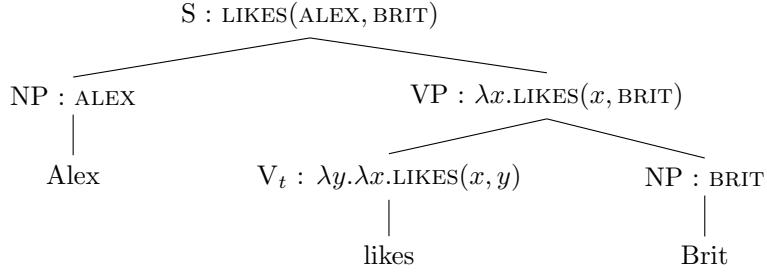


Figure 12.3: Derivation of the semantic representation for *Alex likes Brit* in the grammar  $G_1$ .

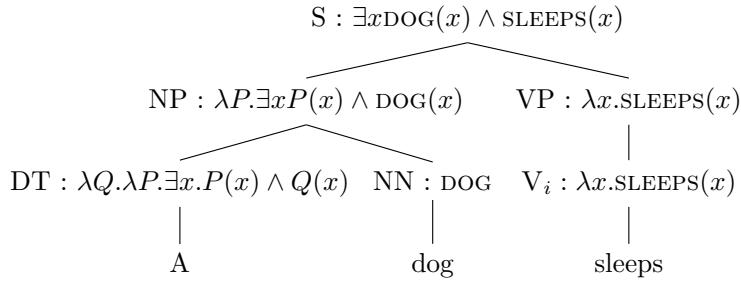
S	$\rightarrow$	NP VP	VP.sem@NP.sem
VP	$\rightarrow$	V <sub>t</sub> NP	V <sub>t</sub> .sem@NP.sem
VP	$\rightarrow$	V <sub>i</sub>	V <sub>i</sub> .sem
V <sub>t</sub>	$\rightarrow$	likes	$\lambda y. \lambda x. \text{LIKES}(x, y)$
V <sub>i</sub>	$\rightarrow$	sleeps	$\lambda x. \text{SLEEPS}(x)$
NP	$\rightarrow$	Alex	ALEX
NP	$\rightarrow$	Brit	BRIT

Table 12.1:  $G_1$ , a minimal syntactic-semantic context-free grammar

6570 Thus, the meaning of the transitive verb *likes* is a lambda expression whose output is  
 6571 *another* lambda expression: it takes  $y$  as an argument to fill in one of the slots in the LIKES  
 6572 relation, and returns a lambda expression that is ready to take an argument to fill in the  
 6573 other slot.<sup>6</sup>

6574 Table 12.1 shows a minimal syntactic-semantic grammar fragment,  $G_1$ . The complete  
 6575 **derivation** of *Alex likes Brit* in  $G_1$  is shown in Figure 12.3. In addition to the transitive  
 6576 verb *likes*, the grammar also includes the intransitive verb *sleeps*; it should be clear how  
 6577 to derive the meaning of sentences like *Alex sleeps*. For verbs that can be either transitive  
 6578 or intransitive, such as *eats*, we would have two terminal productions, one for each sense  
 6579 (terminal productions are also called the **lexical entries**). Indeed, most of the grammar is  
 6580 in the **lexicon** (the terminal productions), since these productions select the basic units of  
 6581 the semantic interpretation.

<sup>6</sup>This can be written in a few different ways. The notation  $\lambda y. x. \text{LIKES}(x, y)$  is a somewhat informal way to indicate a lambda expression that takes two arguments; this would be acceptable in functional programming. Logicians (e.g., Carpenter, 1997) often prefer the more formal notation  $\lambda y. \lambda x. \text{LIKES}(x)(y)$ , indicating that each lambda expression takes exactly one argument.

Figure 12.4: Derivation of the semantic representation for *A dog sleeps*, in grammar  $G_2$ 6582 **12.3.2 Quantification**

6583 Things get more complicated when we move from sentences about named entities to sen-  
 6584 tences that involve more general noun phrases. Let's consider the example, *A dog sleeps*,  
 6585 which has the meaning  $\exists x\text{DOG}(x) \wedge \text{SLEEPS}(x)$ . Clearly, the DOG relation will be intro-  
 6586 duced by the word *dog*, and the SLEEP relation will be introduced by the word *sleeps*.<sup>7</sup>  
 6587 The existential quantifier  $\exists$  must be introduced by the lexical entry for the determiner *a*.<sup>7</sup>  
 6588 However, this seems problematic for the compositional approach taken in the grammar  
 6589  $G_1$ : if the semantics of the noun phrase *a dog* is an existentially quantified expression, how  
 6590 can it be the argument to the semantics of the verb *sleeps*, which expects an entity? And  
 6591 where does the logical conjunction come from?

6592 There are a few different approaches to handling these issues.<sup>8</sup> We will begin by re-  
 6593 versing the semantic relationship between subject NPs and VPs, so that the production  
 6594  $S \rightarrow \text{NP VP}$  has the semantics  $\text{NP.sem}@\text{VP.sem}$ : the meaning of the sentence is now the  
 6595 semantics of the noun phrase applied to the verb phrase. The implications of this change  
 6596 are best illustrated by exploring the derivation of the example, shown in Figure 12.4. Let's  
 6597 start with the indefinite article *a*, to which we assign the rather intimidating semantics,

$$\lambda P. \lambda Q. \exists x P(x) \wedge Q(x). \quad [12.15]$$

This is a lambda expression that takes two **relations** as arguments,  $P$  and  $Q$ . The relation  $P$  is scoped to the outer lambda expression, so it will be provided by the immediately

---

<sup>7</sup>Conversely, the sentence *Every dog sleeps* would involve a universal quantifier,  $\forall x\text{DOG}(x) \Rightarrow \text{SLEEPS}(x)$ . The definite article *the* requires more consideration, since *the dog* must refer to some dog which is uniquely identifiable, perhaps from contextual information external to the sentence. Carpenter (1997, pp. 96-100) summarizes recent approaches to handling definite descriptions.

<sup>8</sup>Carpenter (1997) offers an alternative treatment based on combinatory categorial grammar.

adjacent noun, which in this case is DOG. Thus, the noun phrase *a dog* has the semantics,

$$\text{NP.sem} = \text{DET.sem} @ \text{NN.sem} \quad [12.16]$$

$$= (\lambda P. \lambda Q. \exists x P(x) \wedge Q(x)) @ (\text{DOG}) \quad [12.17]$$

$$= \lambda Q. \exists x \text{DOG}(x) \wedge Q(x). \quad [12.18]$$

6598 This is a lambda expression that is expecting another relation,  $Q$ , which will be provided  
 6599 by the verb phrase, SLEEPS. This gives the desired analysis,  $\exists x \text{DOG}(x) \wedge \text{SLEEPS}(x)$ .<sup>9</sup>

6600 If noun phrases like *a dog* are interpreted as lambda expressions, then proper nouns  
 6601 like *Alex* must be treated in the same way. This is achieved by **type-raising** from  
 6602 constants to lambda expressions,  $x \Rightarrow \lambda P. P(x)$ . After type-raising, the semantics of *Alex* is  
 6603  $\lambda P. P(\text{ALEX})$  — a lambda expression that expects a relation to tell us something about  
 6604 *ALEX*.<sup>10</sup> Again, make sure you see how the analysis in Figure 12.4 can be applied to the  
 6605 sentence *Alex sleeps*.

6606 Direct objects are handled by applying the same type-raising operation to transitive  
 6607 verbs: the meaning of verbs such as *likes* is raised to,

$$\lambda P. \lambda x. P(\lambda y. \text{LIKES}(x, y)) \quad [12.19]$$

As a result, we can keep the verb phrase production  $\text{VP.sem} = \text{V.sem} @ \text{NP.sem}$ , knowing  
 that the direct object will provide the function  $P$  in Equation 12.19. To see how this works,  
 let's analyze the verb phrase *likes a dog*. After uniquely relabeling each lambda variable,  
 we have,

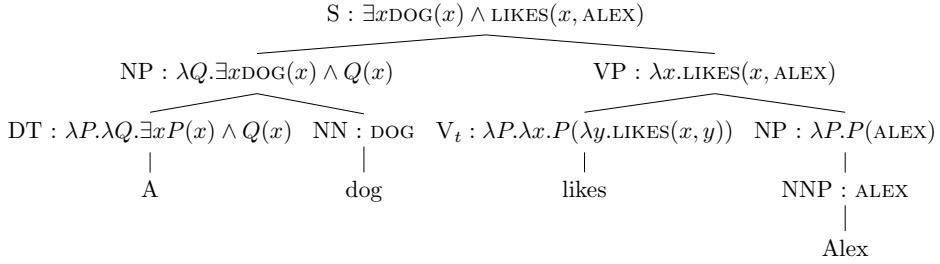
$$\begin{aligned} \text{VP.sem} &= \text{V.sem} @ \text{NP.sem} \\ &= (\lambda P. \lambda x. P(\lambda y. \text{LIKES}(x, y))) @ (\lambda Q. \exists z \text{DOG}(z) \wedge Q(z)) \\ &= \lambda x. (\lambda Q. \exists z \text{DOG}(z) \wedge Q(z)) @ (\lambda y. \text{LIKES}(x, y)) \\ &= \lambda x. \exists z \text{DOG}(z) \wedge (\lambda y. \text{LIKES}(x, y)) @ z \\ &= \lambda x. \exists z \text{DOG}(z) \wedge \text{LIKES}(x, z). \end{aligned}$$

6608 These changes are summarized in the revised grammar  $G_2$ , shown in Table 12.2. Fig-  
 6609 ure 12.5 shows a derivation that involves a transitive verb, an indefinite noun phrase, and  
 6610 a proper noun.

---

<sup>9</sup>When applying  $\beta$ -reduction to arguments that are themselves lambda expressions, be sure to use unique variable names to avoid confusion. For example, it is important to distinguish the  $x$  in the semantics for *a* from the  $x$  in the semantics for *likes*. Variable names are abstractions, and can always be changed — this is known as  **$\alpha$ -conversion**. For example,  $\lambda x. P(x)$  can be converted to  $\lambda y. P(y)$ , etc.

<sup>10</sup>Compositional semantic analysis is often supported by **type systems**, which make it possible to check whether a given function application is valid. The base types are entities  $e$  and truth values  $t$ . A property, such as DOG, is a function from entities to truth values, so its type is written  $\langle e, t \rangle$ . A transitive verb has type

Figure 12.5: Derivation of the semantic representation for *A dog likes Alex*.

S	$\rightarrow$ NP VP	NP.sem@VP.sem
VP	$\rightarrow$ V <sub>t</sub> NP	V <sub>t</sub> .sem@NP.sem
VP	$\rightarrow$ V <sub>i</sub>	V <sub>i</sub> .sem
NP	$\rightarrow$ DET NN	DET.sem@NN.sem
NP	$\rightarrow$ NNP	$\lambda P. P(\text{NNP.sem})$
DET	$\rightarrow a$	$\lambda P. \lambda Q. \exists x P(x) \wedge Q(x)$
DET	$\rightarrow$ every	$\lambda P. \lambda Q. \forall x (P(x) \Rightarrow Q(x))$
V <sub>t</sub>	$\rightarrow$ likes	$\lambda P. \lambda x. P(\lambda y. \text{LIKES}(x, y))$
V <sub>i</sub>	$\rightarrow$ sleeps	$\lambda x. \text{SLEEPS}(x)$
NN	$\rightarrow$ dog	DOG
NNP	$\rightarrow$ Alex	ALEX
NNP	$\rightarrow$ Brit	BRIT

Table 12.2:  $G_2$ , a syntactic-semantic context-free grammar fragment, which supports quantified noun phrases

## 6611 12.4 Learning semantic parsers

6612 As with syntactic parsing, any syntactic-semantic grammar with sufficient coverage risks  
 6613 producing many possible analyses for any given sentence. Machine learning is the dom-  
 6614 inant approach to selecting a single analysis. We will focus on algorithms that learn to  
 6615 score logical forms by attaching weights to features of their derivations (Zettlemoyer  
 6616 and Collins, 2005). Alternative approaches include transition-based parsing (Zelle and  
 6617 Mooney, 1996; Misra and Artzi, 2016) and methods inspired by machine translation (Wong  
 6618 and Mooney, 2006). Methods also differ in the form of supervision used for learning,

$\langle e, \langle e, t \rangle \rangle$ : after receiving the first entity (the direct object), it returns a function from entities to truth values, which will be applied to the subject of the sentence. The type-raising operation  $x \Rightarrow \lambda P. P(x)$  corresponds to a change in type from  $e$  to  $\langle \langle e, t \rangle, t \rangle$ : it expects a function from entities to truth values, and returns a truth value.

which can range from complete derivations to much more limited training signals. We will begin with the case of complete supervision, and then consider how learning is still possible even when seemingly key information is missing.

**Datasets** Early work on semantic parsing focused on natural language expressions of geographical database queries, such as *What states border Texas*. The GeoQuery dataset of Zelle and Mooney (1996) was originally coded in prolog, but has subsequently been expanded and converted into the SQL database query language by Popescu et al. (2003) and into first-order logic with lambda calculus by Zettlemoyer and Collins (2005), providing logical forms like  $\lambda x.\text{STATE}(x) \wedge \text{BORDERS}(x, \text{TEXAS})$ . Another early dataset consists of instructions for RoboCup robot soccer teams (Kate et al., 2005). More recent work has focused on broader domains, such as the Freebase database (Bollacker et al., 2008), for which queries have been annotated by Krishnamurthy and Mitchell (2012) and Cai and Yates (2013). Other recent datasets include child-directed speech (Kwiatkowski et al., 2012) and elementary school science exams (Krishnamurthy, 2016).

### 12.4.1 Learning from derivations

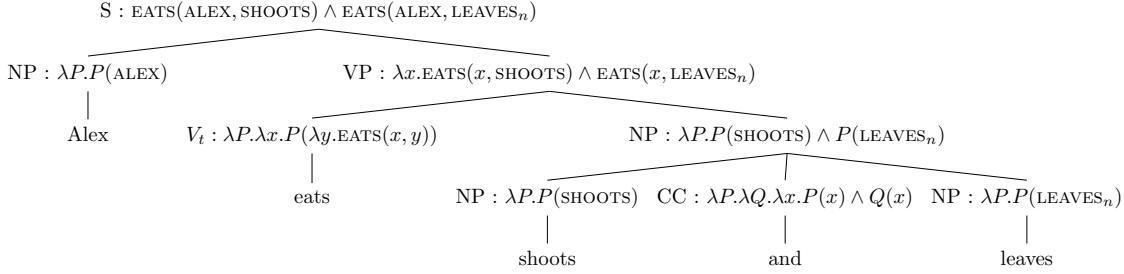
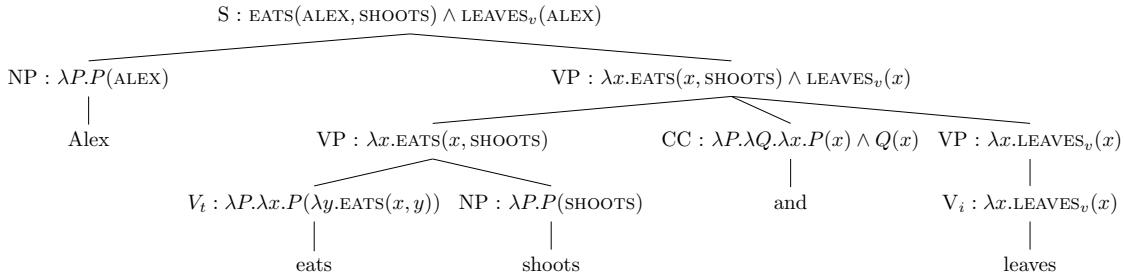
Let  $w^{(i)}$  indicate a sequence of text, and let  $y^{(i)}$  indicate the desired logical form. For example:

$$\begin{aligned} w^{(i)} &= \text{Alex eats shoots and leaves} \\ y^{(i)} &= \text{EATS(ALEX,SHOOTS)} \wedge \text{EATS(ALEX,LEAVES)} \end{aligned}$$

In the standard supervised learning paradigm that was introduced in § 2.2, we first define a feature function,  $f(w, y)$ , and then learn weights on these features, so that  $y^{(i)} = \operatorname{argmax}_y \theta \cdot f(w, y)$ . The weight vector  $\theta$  is learned by comparing the features of the true label  $f(w^{(i)}, y^{(i)})$  against either the features of the predicted label  $f(w^{(i)}, \hat{y})$  (perceptron, support vector machine) or the expected feature vector  $E_{y|w}[f(w^{(i)}, y)]$  (logistic regression).

While this basic framework seems similar to discriminative syntactic parsing, there is a crucial difference. In (context-free) syntactic parsing, the annotation  $y^{(i)}$  contains all of the syntactic productions; indeed, the task of identifying the correct set of productions is identical to the task of identifying the syntactic structure. In semantic parsing, this is not the case: the logical form  $\text{EATS(ALEX,SHOOTS)} \wedge \text{EATS(ALEX,LEAVES)}$  does not reveal the syntactic-semantic productions that were used to obtain it. Indeed, there may be **spurious ambiguity**, so that a single logical form can be reached by multiple derivations. (We previously encountered spurious ambiguity in transition-based dependency parsing, § 11.3.2.)

These ideas can be formalized by introducing an additional variable  $z$ , representing the **derivation** of the logical form  $y$  from the text  $w$ . Assume that the feature function de-

Figure 12.6: Derivation for gold semantic analysis of *Alex eats shoots and leaves*Figure 12.7: Derivation for incorrect semantic analysis of *Alex eats shoots and leaves*

6651 composes across the productions in the derivation,  $f(\mathbf{w}, \mathbf{z}, \mathbf{y}) = \sum_{t=1}^T f(\mathbf{w}, z_t, \mathbf{y})$ , where  
 6652  $z_t$  indicates a single syntactic-semantic production. For example, we might have a feature  
 6653 for the production  $S \rightarrow NP VP : NP.sem@VP.sem$ , as well as for terminal productions  
 6654 like  $NNP \rightarrow Alex : ALEX$ . Under this decomposition, it is possible to compute scores  
 6655 for each semantically-annotated subtree in the analysis of  $\mathbf{w}$ , so that bottom-up parsing  
 6656 algorithms like CKY (§ 10.1) can be applied to find the best-scoring semantic analysis.

6657 Figure 12.6 shows a derivation of the correct semantic analysis of the sentence *Alex*  
 6658 *eats shoots and leaves*, in a simplified grammar in which the plural noun phrases *shoots*  
 6659 and *leaves* are interpreted as logical constants *SHOOTS* and *LEAVES<sub>n</sub>*. Figure 12.7 shows a  
 6660 derivation of an incorrect analysis. Assuming one feature per production, the perceptron  
 6661 update is shown in Table 12.3. From this update, the parser would learn to prefer the  
 6662 noun interpretation of *leaves* over the verb interpretation. It would also learn to prefer  
 6663 noun phrase coordination over verb phrase coordination.

6664 While the update is explained in terms of the perceptron, it would be easy to replace  
 6665 the perceptron with a conditional random field. In this case, the online updates would be  
 6666 based on feature expectations, which can be computed using the inside-outside algorithm  
 6667 (§ 10.6).

$NP_1 \rightarrow NP_2 \ CC \ NP_3$	$(CC.sem @ (NP_2.sem)) @ (NP_3.sem)$	+1
$VP_1 \rightarrow VP_2 \ CC \ VP_3$	$(CC.sem @ (VP_2.sem)) @ (VP_3.sem)$	-1
$NP \rightarrow leaves$	$LEAVES_n$	+1
$VP \rightarrow V_i$	$V_i.sem$	-1
$V_i \rightarrow leaves$	$\lambda x.LEAVES_v$	-1

Table 12.3: Perceptron update for analysis in Figure 12.6 (gold) and Figure 12.7 (predicted)

#### 6668 12.4.2 Learning from logical forms

Complete derivations are expensive to annotate, and are rarely available.<sup>11</sup> One solution is to focus on learning from logical forms directly, while treating the derivations as **latent variables** (Zettlemoyer and Collins, 2005). In a conditional probabilistic model over logical forms  $y$  and derivations  $z$ , we have,

$$p(y, z | w) = \frac{\exp(\theta \cdot f(w, z, y))}{\sum_{y', z'} \exp(\theta \cdot f(w, z', y'))}, \quad [12.20]$$

6669 which is the standard log-linear model, applied to the logical form  $y$  and the derivation  
6670  $z$ .

Since the derivation  $z$  unambiguously determines the logical form  $y$ , it may seem silly to model the joint probability over  $y$  and  $z$ . However, since  $z$  is unknown, it can be marginalized out,

$$p(y | w) = \sum_z p(y, z | w). \quad [12.21]$$

The semantic parser can then select the logical form with the maximum log marginal probability,

$$\log \sum_z p(y, z | w) = \log \sum_z \frac{\exp(\theta \cdot f(w, z, y))}{\sum_{y', z'} \exp(\theta \cdot f(w, z', y'))} \quad [12.22]$$

$$\propto \log \sum_z \exp(\theta \cdot f(w, z', y')) \quad [12.23]$$

$$\geq \max_z \theta \cdot f(w, z, y). \quad [12.24]$$

6671 It is impossible to push the log term inside the sum over  $z$ , so our usual linear scoring  
6672 function does not apply. We can recover this scoring function only in approximation, by  
6673 taking the max (rather than the sum) over derivations  $z$ , which provides a lower bound.

---

<sup>11</sup>An exception is the work of Ge and Mooney (2005), who annotate the meaning of each syntactic constituents for several hundred sentences.

Learning can be performed by maximizing the log marginal likelihood,

$$\ell(\boldsymbol{\theta}) = \sum_{i=1}^N \log p(\mathbf{y}^{(i)} \mid \mathbf{w}^{(i)}; \boldsymbol{\theta}) \quad [12.25]$$

$$= \sum_{i=1}^N \log \sum_z p(\mathbf{y}^{(i)}, \mathbf{z}^{(i)} \mid \mathbf{w}^{(i)}; \boldsymbol{\theta}). \quad [12.26]$$

6674 This log-likelihood is not **convex** in  $\boldsymbol{\theta}$ , unlike the log-likelihood of a fully-observed conditional random field. This means that learning can give different results depending on the  
 6675 initialization.  
 6676

The derivative of Equation 12.26 is,

$$\frac{\partial \ell_i}{\partial \boldsymbol{\theta}} = \sum_z p(z \mid \mathbf{y}, \mathbf{w}; \boldsymbol{\theta}) \mathbf{f}(\mathbf{w}, z, \mathbf{y}) - \sum_{z'} p(z' \mid \mathbf{y}, \mathbf{w}; \boldsymbol{\theta}) \mathbf{f}(\mathbf{w}, z', \mathbf{y}) \quad [12.27]$$

$$= E_{z|\mathbf{y}, \mathbf{w}} \mathbf{f}(\mathbf{w}, z, \mathbf{y}) - E_{y, z|\mathbf{w}} \mathbf{f}(\mathbf{w}, z, \mathbf{y}) \quad [12.28]$$

6677 Both expectations can be computed via bottom-up algorithms like inside-outside. Alternatively, we can again maximize rather than marginalize over derivations for an approx-  
 6678imate solution. In either case, the first term of the gradient requires us to identify  
 6679 derivations  $z$  that are compatible with the logical form  $\mathbf{y}$ . This can be done in a bottom-  
 6680 up dynamic programming algorithm, by having each cell in the table  $t[i, j, X]$  include the  
 6681 set of all possible logical forms for  $X \rightsquigarrow \mathbf{w}_{i+1:j}$ . The resulting table may therefore be much  
 6682 larger than in syntactic parsing. This can be controlled by using pruning to eliminate inter-  
 6683 mediate analyses that are incompatible with the final logical form  $\mathbf{y}$  (Zettlemoyer and  
 6684 Collins, 2005), or by using beam search and restricting the size of each cell to some fixed  
 6685 constant (Liang et al., 2013).  
 6686

6687 If we replace each expectation in Equation 12.28 with argmax and then apply stochastic  
 6688 gradient descent to learn the weights, we obtain the **latent variable perceptron**, a simple  
 6689 and general algorithm for learning with missing data. The algorithm is shown in its most  
 6690 basic form in Algorithm 16, but the usual tricks such as averaging and margin loss can  
 6691 be applied (Yu and Joachims, 2009). Aside from semantic parsing, the latent variable  
 6692 perceptron has been used in tasks such as machine translation (Liang et al., 2006) and  
 6693 named entity recognition (Sun et al., 2009). In **latent conditional random fields**, we use  
 6694 the full expectations rather than maximizing over the hidden variable. This model has  
 6695 also been employed in a range of problems beyond semantic parsing, including parse  
 6696 reranking (Koo and Collins, 2005) and gesture recognition (Quattoni et al., 2007).

### 6697 12.4.3 Learning from denotations

Logical forms are easier to obtain than complete derivations, but the annotation of logical forms still requires considerable expertise. However, it is relatively easy to obtain deno-

**Algorithm 16** Latent variable perceptron

---

```

1: procedure LATENTVARIABLEPERCEPTRON( $\mathbf{w}^{(1:N)}, \mathbf{y}^{(1:N)}$ )
2:    $\theta \leftarrow 0$ 
3:   repeat
4:     Select an instance  $i$ 
5:      $\mathbf{z}^{(i)} \leftarrow \text{argmax}_{\mathbf{z}} \theta \cdot \mathbf{f}(\mathbf{w}^{(i)}, \mathbf{z}, \mathbf{y}^{(i)})$ 
6:      $\hat{\mathbf{y}}, \hat{\mathbf{z}} \leftarrow \text{argmax}_{\mathbf{y}', \mathbf{z}'} \theta \cdot \mathbf{f}(\mathbf{w}^{(i)}, \mathbf{z}', \mathbf{y}')$ 
7:      $\theta \leftarrow \theta + \mathbf{f}(\mathbf{w}^{(i)}, \mathbf{z}^{(i)}, \mathbf{y}^{(i)}) - \mathbf{f}(\mathbf{w}^{(i)}, \hat{\mathbf{z}}, \hat{\mathbf{y}})$ 
8:   until tired
9:   return  $\theta$ 

```

---

tations for many natural language sentences. For example, in the geography domain, the denotation of a question would be its answer (Clarke et al., 2010; Liang et al., 2013):

**Text** :*What states border Georgia?*  
**Logical form** : $\lambda x.\text{STATE}(x) \wedge \text{BORDER}(x, \text{GEORGIA})$   
**Denotation** :{Alabama, Florida, North Carolina,  
South Carolina, Tennessee}

6698 Similarly, in a robotic control setting, the denotation of a command would be an action or  
6699 sequence of actions (Artzi and Zettlemoyer, 2013). In both cases, the idea is to reward the  
6700 semantic parser for choosing an analysis whose denotation is correct: the right answer to  
6701 the question, or the right action.

Learning from logical forms was made possible by summing or maxing over derivations. This idea can be carried one step further, summing or maxing over all logical forms with the correct denotation. Let  $v_i(\mathbf{y}) \in \{0, 1\}$  be a **validation function**, which assigns a binary score indicating whether the denotation  $[\mathbf{y}]$  for the text  $\mathbf{w}^{(i)}$  is correct. We can then learn by maximizing a conditional-likelihood objective,

$$\ell^{(i)}(\boldsymbol{\theta}) = \log \sum_{\mathbf{y}} v_i(\mathbf{y}) \times p(\mathbf{y} \mid \mathbf{w}; \boldsymbol{\theta}) \quad [12.29]$$

$$= \log \sum_{\mathbf{y}} v_i(\mathbf{y}) \times \sum_{\mathbf{z}} p(\mathbf{y}, \mathbf{z} \mid \mathbf{w}; \boldsymbol{\theta}), \quad [12.30]$$

6702 which sums over all derivations  $\mathbf{z}$  of all valid logical forms,  $\{\mathbf{y} : v_i(\mathbf{y}) = 1\}$ . This cor-  
6703 responds to the log-probability that the semantic parser produces a logical form with a  
6704 valid denotation.

Differentiating with respect to  $\theta$ , we obtain,

$$\frac{\partial \ell^{(i)}}{\partial \theta} = \sum_{\mathbf{y}, \mathbf{z}: v_i(\mathbf{y})=1} p(\mathbf{y}, \mathbf{z} | \mathbf{w}) \mathbf{f}(\mathbf{w}, \mathbf{z}, \mathbf{y}) - \sum_{\mathbf{y}', \mathbf{z}'} p(\mathbf{y}', \mathbf{z}' | \mathbf{w}) \mathbf{f}(\mathbf{w}, \mathbf{z}', \mathbf{y}'), \quad [12.31]$$

which is the usual difference in feature expectations. The positive term computes the expected feature expectations conditioned on the denotation being valid, while the second term computes the expected feature expectations according to the current model, without regard to the ground truth. Large-margin learning formulations are also possible for this problem. For example, Artzi and Zettlemoyer (2013) generate a set of valid and invalid derivations, and then impose a constraint that all valid derivations should score higher than all invalid derivations. This constraint drives a perceptron-like learning rule.

## Additional resources

A key issue not considered here is how to handle **semantic underspecification**: cases in which there are multiple semantic interpretations for a single syntactic structure. Quantifier scope ambiguity is a classic example. Blackburn and Bos (2005) enumerate a number of approaches to this issue, and also provide links between natural language semantics and computational inference techniques. Much of the contemporary research on semantic parsing uses the framework of combinatory categorial grammar (CCG). Carpenter (1997) provides a comprehensive treatment of how CCG can support compositional semantic analysis. Another recent area of research is the semantics of multi-sentence texts. This can be handled with models of **dynamic semantics**, such as dynamic predicate logic (Groenendijk and Stokhof, 1991).

Alternative readings on formal semantics include an “informal” reading from Levy and Manning (2009), and a more involved introduction from Briscoe (2011). To learn more about ongoing research on data-driven semantic parsing, readers may consult the survey article by Liang and Potts (2015), tutorial slides and videos by Artzi and Zettlemoyer (2013),<sup>12</sup> and the source code by Yoav Artzi<sup>13</sup> and Percy Liang.<sup>14</sup>

## Exercises

- Derive the **modus ponens** inference rule, which states that if we know  $\phi \Rightarrow \psi$  and  $\phi$ , then  $\psi$  must be true. The derivation can be performed using the definition of the  $\Rightarrow$  operator and some of the laws provided in § 12.2.1, plus one additional identity:  $\perp \vee \phi = \phi$ .

---

<sup>12</sup>Videos are currently available at <http://yoavartzi.com/tutorial/>

<sup>13</sup><http://yoavartzi.com/spf>

<sup>14</sup><https://github.com/percyliang/sempre>

- 6733     2. Convert the following examples into first-order logic, using the relations CAN-SLEEP,  
 6734     MAKES-NOISE, and BROTHER.
- 6735       • If Abigail makes noise, no one can sleep.  
 6736       • If Abigail makes noise, someone cannot sleep.  
 6737       • None of Abigail's brothers can sleep.  
 6738       • If one of Abigail's brothers makes noise, Abigail cannot sleep.
- 6739     3. Extend the grammar fragment  $G_1$  to include the ditransitive verb *teaches* and the  
 6740     proper noun *Swahili*. Show how to derive the interpretation for the sentence *Alex*  
 6741     *teaches Brit Swahili*, which should be  $\text{TEACHES}(\text{ALEX}, \text{BRIT}, \text{SWAHILI})$ . The grammar  
 6742     need not be in Chomsky Normal Form. For the ditransitive verb, use  $\text{NP}_1$  and  $\text{NP}_2$   
 6743     to indicate the two direct objects.
- 6744     4. Derive the semantic interpretation for the sentence *Alex likes every dog*, using gram-  
 6745     mar fragment  $G_2$ .
- 6746     5. Extend the grammar fragment  $G_2$  to handle adjectives, so that the meaning of *an  
 6747     angry dog* is  $\lambda P. \exists x \text{DOG}(x) \wedge \text{ANGRY}(x) \wedge P(x)$ . Specifically, you should supply the  
 6748     lexical entry for the adjective *angry*, and you should specify the syntactic-semantic  
 6749     productions  $\text{NP} \rightarrow \text{DET } \text{NOM}$ ,  $\text{NOM} \rightarrow \text{JJ } \text{NOM}$ , and  $\text{NOM} \rightarrow \text{NN}$ .
- 6750     6. Extend your answer to the previous question to cover copula constructions with  
 6751     predicative adjectives, such as *Alex is angry*. The interpretation should be  $\text{ANGRY}(\text{ALEX})$ .  
 6752     You should add a verb phrase production  $\text{VP} \rightarrow \text{V}_{\text{cop}} \text{ JJ}$ , and a terminal production  
 6753      $\text{V}_{\text{cop}} \rightarrow \text{is}$ . Show why your grammar extensions result in the correct interpretation.
- 6754     7. In Figure 12.6 and Figure 12.7, we treat the plurals *shoots* and *leaves* as entities. Revise  
 6755      $G_2$  so that the interpretation of *Alex eats leaves* is  $\forall x. (\text{LEAF}(x) \Rightarrow \text{EATS}(\text{ALEX}, x))$ , and  
 6756     show the resulting perceptron update.
- 6757     8. Statements like *every student eats a pizza* have two possible interpretations, depend-  
 6758     ing on quantifier scope:

$$\forall x \exists y \text{PIZZA}(y) \wedge (\text{STUDENT}(x) \Rightarrow \text{EATS}(x, y)) \quad [12.32]$$

$$\exists y \forall x \text{PIZZA}(y) \wedge (\text{STUDENT}(x) \Rightarrow \text{EATS}(x, y)) \quad [12.33]$$

6757     Explain why these interpretations really are different, and modify the grammar  $G_2$   
 6758     so that it can produce both interpretations.

- 6759     9. Derive Equation 12.27.
- 6760     10. In the GeoQuery domain, give a natural language query that has multiple plausible  
 6761     semantic interpretations with the same denotation. List both interpretaions and the  
 6762     denotation.

6763      **Hint:** There are many ways to do this, but one approach involves using toponyms  
6764      (place names) that could plausibly map to several different entities in the model.



6765 

## Chapter 13

6766 

# Predicate-argument semantics

6767 This chapter considers more “lightweight” semantic representations, which discard some  
6768 aspects of first-order logic, but focus on predicate-argument structures. Let’s begin by  
6769 thinking about the semantics of events, with a simple example:

6770 (13.1) Asha gives Boyang a book.

6771 A first-order logical representation of this sentence is,

$$\exists x. \text{BOOK}(x) \wedge \text{GIVE}(\text{ASHA}, \text{BOYANG}, x) \quad [13.1]$$

6772 In this representation, we define variable  $x$  for the book, and we link the strings *Asha* and  
6773 *Boyang* to entities ASHA and BOYANG. Because the action of giving involves a giver, a  
6774 recipient, and a gift, the predicate GIVE must take three arguments.

6775 Now suppose we have additional information about the event:

6776 (13.2) Yesterday, Asha reluctantly gave Boyang a book.

6777 One possible solution is to extend the predicate GIVE to take additional arguments,

$$\exists x. \text{BOOK}(x) \wedge \text{GIVE}(\text{ASHA}, \text{BOYANG}, x, \text{YESTERDAY}, \text{RELUCTANTLY}) \quad [13.2]$$

But this is clearly unsatisfactory: *yesterday* and *reluctantly* are optional arguments, and we would need a different version of the GIVE predicate for every possible combination of arguments. **Event semantics** solves this problem by **reifying** the event as an existentially quantified variable  $e$ ,

$$\begin{aligned} \exists e, x. & \text{GIVE-EVENT}(e) \wedge \text{GIVER}(e, \text{ASHA}) \wedge \text{GIFT}(e, x) \wedge \text{BOOK}(e, x) \wedge \text{RECIPIENT}(e, \text{BOYANG}) \\ & \wedge \text{TIME}(e, \text{YESTERDAY}) \wedge \text{MANNER}(e, \text{RELUCTANTLY}) \end{aligned}$$

6778 In this way, each argument of the event — the giver, the recipient, the gift — can be rep-  
 6779 resented with a relation of its own, linking the argument to the event  $e$ . The expression  
 6780 GIVER( $e$ , ASHA) says that ASHA plays the **role** of GIVER in the event. This reformulation  
 6781 handles the problem of optional information such as the time or manner of the event,  
 6782 which are called **adjuncts**. Unlike arguments, adjuncts are not a mandatory part of the  
 6783 relation, but under this representation, they can be expressed with additional logical rela-  
 6784 tions that are conjoined to the semantic interpretation of the sentence.<sup>1</sup>

6785 The event semantic representation can be applied to nested clauses, e.g.,

6786 (13.3) Chris sees Asha pay Boyang.

This is done by using the event variable as an argument:

$$\begin{aligned} \exists e_1 \exists e_2 \text{SEE-EVENT}(e_1) \wedge \text{SEER}(e_1, \text{CHRIS}) \wedge \text{SIGHT}(e_1, e_2) \\ \wedge \text{PAY-EVENT}(e_2) \wedge \text{PAYER}(e_2, \text{ASHA}) \wedge \text{PAYEE}(e_2, \text{BOYANG}) \end{aligned} \quad [13.3]$$

6787 As with first-order logic, the goal of event semantics is to provide a representation that  
 6788 generalizes over many surface forms. Consider the following paraphrases of (13.1):

- 6789 (13.4) Asha gives a book to Boyang.
- 6790 (13.5) A book is given to Boyang by Asha.
- 6791 (13.6) A book is given by Asha to Boyang.
- 6792 (13.7) The gift of a book from Asha to Boyang ...

6793 All have the same event semantic meaning as Equation 13.1, but the ways in which the  
 6794 meaning can be expressed are diverse. The final example does not even include a verb:  
 6795 events are often introduced by verbs, but as shown by (13.7), the noun *gift* can introduce  
 6796 the same predicate, with the same accompanying arguments.

6797 **Semantic role labeling** (SRL) is a relaxed form of semantic parsing, in which each  
 6798 semantic role is filled by a set of tokens from the text itself. This is sometimes called  
 6799 “shallow semantics” because, unlike model-theoretic semantic parsing, role fillers need  
 6800 not be symbolic expressions with denotations in some world model. A semantic role  
 6801 labeling system is required to identify all predicates, and then specify the spans of text  
 6802 that fill each role. To give a sense of the task, here is a more complicated example:

- 6803 (13.8) Boyang wants Asha to give him a linguistics book.

---

<sup>1</sup>This representation is often called **Neo-Davidsonian event semantics**. The use of existentially-quantified event variables was proposed by Davidson (1967) to handle the issue of optional adjuncts. In Neo-Davidsonian semantics, this treatment of adjuncts is extended to mandatory arguments as well (e.g., Parsons, 1990).

6804 In this example, there are two predicates, expressed by the verbs *want* and *give*. Thus, a  
 6805 semantic role labeler might return the following output:

- 6806 • (PREDICATE : *wants*, WANTED : *Boyang*, DESIRE : *Asha to give him a linguistics book*)  
 6807 • (PREDICATE : *give*, GIVER : *Asha*, RECIPIENT : *him*, GIFT : *a linguistics book*)

6808 *Boyang* and *him* may refer to the same person, but the semantic role labeling is not re-  
 6809 quired to resolve this reference. Other predicate-argument representations, such as **Ab-**  
 6810 **stract Meaning Representation (AMR)**, do require reference resolution. We will return to  
 6811 AMR in § 13.3, but first, let us further consider the definition of semantic roles.

## 6812 13.1 Semantic roles

6813 In event semantics, it is necessary to specify a number of additional logical relations to  
 6814 link arguments to events: GIVER, RECIPIENT, SEER, SIGHT, etc. Indeed, every predicate re-  
 6815 quires a set of logical relations to express its own arguments. In contrast, adjuncts such as  
 6816 TIME and MANNER are shared across many types of events. A natural question is whether  
 6817 it is possible to treat mandatory arguments more like adjuncts, by identifying a set of  
 6818 generic argument types that are shared across many event predicates. This can be further  
 6819 motivated by examples involving related verbs:

- 6820 (13.9) Asha gave Boyang a book.  
 6821 (13.10) Asha loaned Boyang a book.  
 6822 (13.11) Asha taught Boyang a lesson.  
 6823 (13.12) Asha gave Boyang a lesson.

6824 The respective roles of Asha, Boyang, and the book are nearly identical across the first  
 6825 two examples. The third example is slightly different, but the fourth example shows that  
 6826 the roles of GIVER and TEACHER can be viewed as related.

6827 One way to think about the relationship between roles such as GIVER and TEACHER is  
 6828 by enumerating the set of properties that an entity typically possesses when it fulfills these  
 6829 roles: givers and teachers are usually **animate** (they are alive and sentient) and **volitional**  
 6830 (they choose to enter into the action).<sup>2</sup> In contrast, the thing that gets loaned or taught is  
 6831 usually not animate or volitional; furthermore, it is unchanged by the event.

6832 Building on these ideas, **thematic roles** generalize across predicates by leveraging the  
 6833 shared semantic properties of typical role fillers (Fillmore, 1968). For example, in exam-  
 6834 ples (13.9-13.12), Asha plays a similar role in all four sentences, which we will call the

<sup>2</sup>There are always exceptions. For example, in the sentence *The C programming language has taught me a lot about perseverance*, the “teacher” is the *The C programming language*, which is presumably not animate or volitional.

	<i>Asha</i>	<i>gave</i>	<i>Boyang</i>	<i>a book</i>
<b>VerbNet</b>	AGENT		RECIPIENT	THEME
<b>PropBank</b>	ARG0: giver		ARG2: entity given to	ARG1: thing given
<b>FrameNet</b>	DONOR		RECIPIENT	THEME
	<i>Asha</i>	<i>taught</i>	<i>Boyang</i>	<i>algebra</i>
<b>VerbNet</b>	AGENT		RECIPIENT	TOPIC
<b>PropBank</b>	ARG0: teacher		ARG2: student	ARG1: subject
<b>FrameNet</b>	TEACHER		STUDENT	SUBJECT

Figure 13.1: Example semantic annotations according to VerbNet, PropBank, and FrameNet

6835 **agent.** This reflects several shared semantic properties: she is the one who is actively and  
 6836 intentionally performing the action, while Boyang is a more passive participant; the book  
 6837 and the lesson would play a different role, as non-animate participants in the event.

6838 Example annotations from three well known systems are shown in Figure 13.1. We  
 6839 will now discuss these systems in more detail.

### 6840 13.1.1 VerbNet

6841 **VerbNet** (Kipper-Schuler, 2005) is a lexicon of verbs, and it includes thirty “core” thematic  
 6842 roles played by arguments to these verbs. Here are some example roles, accompanied by  
 6843 their definitions from the VerbNet Guidelines.<sup>3</sup>

- 6844 • AGENT: “ACTOR in an event who initiates and carries out the event intentionally or  
   6845 consciously, and who exists independently of the event.”
- 6846 • PATIENT: “UNDERGOER in an event that experiences a change of state, location or  
   6847 condition, that is causally involved or directly affected by other participants, and  
   6848 exists independently of the event.”
- 6849 • RECIPIENT: “DESTINATION that is animate”
- 6850 • THEME: “UNDERGOER that is central to an event or state that does not have control  
   6851 over the way the event occurs, is not structurally changed by the event, and/or is  
   6852 characterized as being in a certain position or condition throughout the state.”
- 6853 • TOPIC: “THEME characterized by information content transferred to another partic-  
   6854 ipant.”

<sup>3</sup>[http://verbs.colorado.edu/verb-index/VerbNet\\_Guidelines.pdf](http://verbs.colorado.edu/verb-index/VerbNet_Guidelines.pdf)

6855 VerbNet roles are organized in a hierarchy, so that a TOPIC is a type of THEME, which in  
 6856 turn is a type of UNDERGOER, which is a type of PARTICIPANT, the top-level category.

6857 In addition, VerbNet organizes verb senses into a class hierarchy, in which verb senses  
 6858 that have similar meanings are grouped together. Recall from § 4.2 that multiple meanings  
 6859 of the same word are called **senses**, and that WordNet identifies senses for many English  
 6860 words. VerbNet builds on WordNet, so that verb classes are identified by the WordNet  
 6861 senses of the verbs that they contain. For example, the verb class give-13.1 includes  
 6862 the first WordNet sense of *loan* and the second WordNet sense of *lend*.

6863 Each VerbNet class or subclass takes a set of thematic roles. For example, give-13.1  
 6864 takes arguments with the thematic roles of AGENT, THEME, and RECIPIENT;<sup>4</sup> the pred-  
 6865 icate TEACH takes arguments with the thematic roles AGENT, TOPIC, RECIPIENT, and  
 6866 SOURCE.<sup>5</sup> So according to VerbNet, *Asha* and *Boyang* play the roles of AGENT and RECIP-  
 6867 IENT in the sentences,

6868 (13.13) Asha gave Boyang a book.

6869 (13.14) Asha taught Boyang algebra.

6870 The *book* and *algebra* are both THEMES, but *algebra* is a subcategory of THEME — a TOPIC  
 6871 — because it consists of information content that is given to the receiver.

### 6872 13.1.2 Proto-roles and PropBank

6873 Detailed thematic role inventories of the sort used in VerbNet are not universally accepted.  
 6874 For example, Dowty (1991, pp. 547) notes that “Linguists have often found it hard to agree  
 6875 on, and to motivate, the location of the boundary between role types.” He argues that a  
 6876 solid distinction can be identified between just two **proto-roles**:

6877 **Proto-Agent.** Characterized by volitional involvement in the event or state; sentience  
 6878 and/or perception; causing an event or change of state in another participant; move-  
 6879 ment; exists independently of the event.

6880 **Proto-Patient.** Undergoes change of state; causally affected by another participant; sta-  
 6881 tionary relative to the movement of another participant; does not exist indepen-  
 6882 dently of the event.<sup>6</sup>

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<sup>4</sup><https://verbs.colorado.edu/verb-index/vn/give-13.1.php>

<sup>5</sup>[https://verbs.colorado.edu/verb-index/vn/transfer\\_mesg-37.1.1.php](https://verbs.colorado.edu/verb-index/vn/transfer_mesg-37.1.1.php)

<sup>6</sup>Reisinger et al. (2015) ask crowd workers to annotate these properties directly, finding that annotators tend to agree on the properties of each argument. They also find that in English, arguments having more proto-agent properties tend to appear in subject position, while arguments with more proto-patient properties appear in object position.

6883 In the examples in Figure 13.1, Asha has most of the proto-agent properties: in giving  
 6884 the book to Boyang, she is acting volitionally (as opposed to *Boyang got a book from Asha*, in  
 6885 which it is not clear whether Asha gave up the book willingly); she is sentient; she causes a  
 6886 change of state in Boyang; she exists independently of the event. Boyang has some proto-  
 6887 agent properties: he is sentient and exists independently of the event. But he also has  
 6888 some proto-patient properties: he is the one who is causally affected and who undergoes  
 6889 change of state. The book that Asha gives Boyang has even fewer of the proto-agent  
 6890 properties: it is not volitional or sentient, and it has no causal role. But it also lacks many  
 6891 of the proto-patient properties: it does not undergo change of state, exists independently  
 6892 of the event, and is not stationary.

6893 The **Proposition Bank**, or PropBank (Palmer et al., 2005), builds on this basic agent-  
 6894 patient distinction, as a middle ground between generic thematic roles and roles that are  
 6895 specific to each predicate. Each verb is linked to a list of numbered arguments, with ARG0  
 6896 as the proto-agent and ARG1 as the proto-patient. Additional numbered arguments are  
 6897 verb-specific. For example, for the predicate TEACH,<sup>7</sup> the arguments are:

- 6898 • ARG0: the teacher
- 6899 • ARG1: the subject
- 6900 • ARG2: the student(s)

6901 Verbs may have any number of arguments: for example, WANT and GET have five, while  
 6902 EAT has only ARG0 and ARG1. In addition to the semantic arguments found in the frame  
 6903 files, roughly a dozen general-purpose **adjuncts** may be used in combination with any  
 6904 verb. These are shown in Table 13.1.

6905 PropBank-style semantic role labeling is annotated over the entire Penn Treebank. This  
 6906 annotation includes the sense of each verbal predicate, as well as the argument spans.

### 6907 13.1.3 FrameNet

6908 Semantic **frames** are descriptions of situations or events. Frames may be *evoked* by one  
 6909 of their **lexical units** (often a verb, but not always), and they include some number of  
 6910 **frame elements**, which are like roles (Fillmore, 1976). For example, the act of teaching  
 6911 is a frame, and can be evoked by the verb *taught*; the associated frame elements include  
 6912 the teacher, the student(s), and the subject being taught. Frame semantics has played a  
 6913 significant role in the history of artificial intelligence, in the work of Minsky (1974) and  
 6914 Schank and Abelson (1977). In natural language processing, the theory of frame semantics  
 6915 has been implemented in **FrameNet** (Fillmore and Baker, 2009), which consists of a lexicon

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<sup>7</sup><http://verbs.colorado.edu/propbank/framesets-english-aliases/teach.html>

---

TMP	time	<i>Boyang ate a bagel</i> [AM-TMP <i>yesterday</i> ].
LOC	location	<i>Asha studies in</i> [AM-LOC <i>Stuttgart</i> ]
MOD	modal verb	<i>Asha</i> [AM-MOD <i>will</i> ] <i>study in Stuttgart</i>
ADV	general purpose	[AM-ADV <i>Luckily</i> ], <i>Asha knew algebra</i> .
MNR	manner	<i>Asha ate</i> [AM-MNR <i>aggressively</i> ].
DIS	discourse connective	[AM-DIS <i>However</i> ], <i>Asha prefers algebra</i> .
PRP	purpose	<i>Barry studied</i> [AM-PRP <i>to pass the bar</i> ].
DIR	direction	<i>Workers dumped burlap sacks</i> [AM-DIR <i>into a bin</i> ].
NEG	negation	<i>Asha does</i> [AM-NEG <i>not</i> ] <i>speak Albanian</i> .
EXT	extent	<i>Prices increased</i> [AM-EXT <i>4%</i> ].
CAU	cause	<i>Boyang returned the book</i> [AM-CAU <i>because it was overdue</i> ].

---

Table 13.1: PropBank adjuncts (Palmer et al., 2005), sorted by frequency in the corpus

6916 of roughly 1000 frames, and a corpus of more than 200,000 “exemplar sentences,” in which  
 6917 the frames and their elements are annotated.<sup>8</sup>

6918 Rather than seeking to link semantic roles such as TEACHER and GIVER into the-  
 6919 thematic roles such as AGENT, FrameNet aggressively groups verbs into frames, and links  
 6920 semantically-related roles across frames. For example, the following two sentences would  
 6921 be annotated identically in FrameNet:

6922 (13.15) Asha taught Boyang algebra.

6923 (13.16) Boyang learned algebra from Asha.

6924 This is because *teach* and *learn* are both lexical units in the EDUCATION-TEACHING frame.  
 6925 Furthermore, roles can be shared even when the frames are distinct, as in the following  
 6926 two examples:

6927 (13.17) Asha gave Boyang a book.

6928 (13.18) Boyang got a book from Asha.

6929 The GIVING and GETTING frames both have RECIPIENT and THEME elements, so Boyang  
 6930 and the book would play the same role. Asha’s role is different: she is the DONOR in the  
 6931 GIVING frame, and the SOURCE in the GETTING frame. FrameNet makes extensive use of  
 6932 multiple inheritance to share information across frames and frame elements: for example,  
 6933 the COMMERCE-SELL and LENDING frames inherit from GIVING frame.

<sup>8</sup>Current details and data can be found at <https://framenet.icsi.berkeley.edu/>

6934 **13.2 Semantic role labeling**

6935 The task of semantic role labeling is to identify the parts of the sentence comprising the  
 6936 semantic roles. In English, this task is typically performed on the PropBank corpus, with  
 6937 the goal of producing outputs in the following form:

6938 (13.19) [ARG0 Asha] [GIVE.01 gave] [ARG2 Boyang's mom] [ARG1 a book] [AM-TMP yesterday].

6939 Note that a single sentence may have multiple verbs, and therefore a given word may be  
 6940 part of multiple role-fillers:

6941 (13.20) [ARG0 Asha] [WANT.01 wanted]  
 Asha            wanted

6942            [ARG1 Boyang to give her the book].  
 [ARG0 Boyang] [GIVE.01 to give] [ARG2 her] [ARG1 the book].

6943 **13.2.1 Semantic role labeling as classification**

6944 PropBank is annotated on the Penn Treebank, and annotators used phrasal constituents  
 6945 ( $\S$  9.2.2) to fill the roles. PropBank semantic role labeling can be viewed as the task of as-  
 6946 signing to each phrase a label from the set  $\mathcal{R} = \{\emptyset, \text{PRED}, \text{ARG0}, \text{ARG1}, \text{ARG2}, \dots, \text{AM-LOC}, \text{AM-TMP}, \dots\}$ ,  
 6947 with respect to each predicate. If we treat semantic role labeling as a classification prob-  
 6948 lem, we obtain the following functional form:

$$\hat{y}_{(i,j)} = \underset{y}{\operatorname{argmax}} \psi(\mathbf{w}, y, i, j, \rho, \tau), \quad [13.4]$$

6949 where,

- 6950 •  $(i, j)$  indicates the span of a phrasal constituent  $(w_{i+1}, w_{i+2}, \dots, w_j)$ ;<sup>9</sup>
- 6951 •  $\mathbf{w}$  represents the sentence as a sequence of tokens;
- 6952 •  $\rho$  is the index of the predicate verb in  $\mathbf{w}$ ;
- 6953 •  $\tau$  is the structure of the phrasal constituent parse of  $\mathbf{w}$ .

6954 Early work on semantic role labeling focused on discriminative feature-based models,  
 6955 where  $\psi(\mathbf{w}, y, i, j, \rho, \tau) = \theta \cdot f(\mathbf{w}, y, i, j, \rho, \tau)$ . Table 13.2 shows the features used in a sem-  
 6956 inal paper on FrameNet semantic role labeling (Gildea and Jurafsky, 2002). By 2005 there

---

<sup>9</sup>PropBank roles can also be filled by **split constituents**, which are discontinuous spans of text. This situation most frequently in reported speech, e.g. [ARG1 *By addressing these problems*], *Mr. Maxwell said*, [ARG1 *the new funds have become extremely attractive.*] (example adapted from Palmer et al., 2005). This issue is typically addressed by defining “continuation arguments”, e.g. C-ARG1, which refers to the continuation of ARG1 after the split.

---

<b>Predicate lemma and POS tag</b>	The lemma of the predicate verb and its part-of-speech tag
<b>Voice</b>	Whether the predicate is in active or passive voice, as determined by a set of syntactic patterns for identifying passive voice constructions
<b>Phrase type</b>	The constituent phrase type for the proposed argument in the parse tree, e.g. NP, PP
<b>Headword and POS tag</b>	The head word of the proposed argument and its POS tag, identified using the Collins (1997) rules
<b>Position</b>	Whether the proposed argument comes before or after the predicate in the sentence
<b>Syntactic path</b>	The set of steps on the parse tree from the proposed argument to the predicate (described in detail in the text)
<b>Subcategorization</b>	The syntactic production from the first branching node above the predicate. For example, in Figure 13.2, the subcategorization feature around <i>taught</i> would be VP → VBD NP PP.

---

Table 13.2: Features used in semantic role labeling by Gildea and Jurafsky (2002).

6957 were several systems for PropBank semantic role labeling, and their approaches and fea-  
 6958 ture sets are summarized by Carreras and Márquez (2005). Typical features include: the  
 6959 phrase type, head word, part-of-speech, boundaries, and neighbors of the proposed argu-  
 6960 ment  $w_{i+1:j}$ ; the word, lemma, part-of-speech, and voice of the verb  $w_\rho$  (active or passive),  
 6961 as well as features relating to its frameset; the distance and path between the verb and  
 6962 the proposed argument. In this way, semantic role labeling systems are high-level “con-  
 6963 sumers” in the NLP stack, using features produced from lower-level components such as  
 6964 part-of-speech taggers and parsers. More comprehensive feature sets are enumerated by  
 6965 Das et al. (2014) and Täckström et al. (2015).

6966 A particularly powerful class of features relate to the **syntactic path** between the ar-  
 6967 gument and the predicate. These features capture the sequence of moves required to get  
 6968 from the argument to the verb by traversing the phrasal constituent parse of the sentence.  
 6969 The idea of these features is to capture syntactic regularities in how various arguments  
 6970 are realized. Syntactic path features are best illustrated by example, using the parse tree  
 6971 in Figure 13.2:

- 6972 • The path from *Asha* to the verb *taught* is NNP↑NP↑S↓VP↓VBD. The first part of  
 6973 the path, NNP↑NP↑S, means that we must travel up the parse tree from the NNP  
 6974 tag (proper noun) to the S (sentence) constituent. The second part of the path,  
 6975 S↓VP↓VBD, means that we reach the verb by producing a VP (verb phrase) from

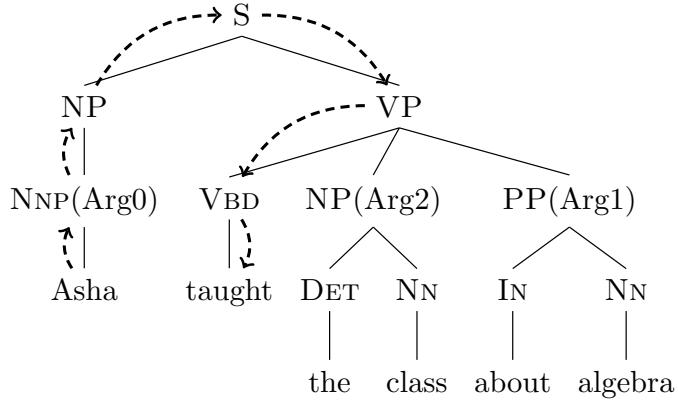


Figure 13.2: Semantic role labeling on the phrase-structure parse tree for a sentence. The dashed line indicates the syntactic path from *Asha* to the predicate verb *taught*.

6976 the S constituent, and then by producing a VBD (past tense verb). This feature is  
 6977 consistent with *Asha* being in subject position, since the path includes the sentence  
 6978 root S.

- 6979 • The path from *the class* to *taught* is NP↑VP↓VBD. This is consistent with *the class*  
 6980 being in object position, since the path passes through the VP node that dominates  
 6981 the verb *taught*.

6982 Because there are many possible path features, it can also be helpful to look at smaller  
 6983 parts: for example, the upward and downward parts can be treated as separate features;  
 6984 another feature might consider whether S appears anywhere in the path.

6985 Rather than using the constituent parse, it is also possible to build features from the  
 6986 **dependency path** between the head word of each argument and the verb (Pradhan et al.,  
 6987 2005). Using the Universal Dependency part-of-speech tagset and dependency relations (Nivre  
 6988 et al., 2016), the dependency path from *Asha* to *taught* is PROPN  $\xleftarrow[\text{NSUBJ}]{} \text{VERB}$ , because *taught*  
 6989 is the head of a relation of type  $\xleftarrow[\text{NSUBJ}]{} \text{VERB}$  with *Asha*. Similarly, the dependency path from *class*  
 6990 to *taught* is NOUN  $\xleftarrow[\text{DOBJ}]{} \text{VERB}$ , because *class* heads the noun phrase that is a direct object of  
 6991 *taught*. A more interesting example is *Asha wanted to teach the class*, where the path from  
 6992 *Asha* to *teach* is PROPN  $\xleftarrow[\text{NSUBJ}]{} \text{VERB} \rightarrow[\text{XCOMP}] \text{VERB}$ . The right-facing arrow in second relation  
 6993 indicates that *wanted* is the head of its XCOMP relation with *teach*.

6994 **13.2.2 Semantic role labeling as constrained optimization**

6995 A potential problem with treating SRL as a classification problem is that there are a num-  
 6996 ber of sentence-level **constraints**, which a classifier might violate.

- 6997 • For a given verb, there can be only one argument of each type (ARG0, ARG1, etc.)  
 6998 • Arguments cannot overlap. This problem arises when we are labeling the phrases  
 6999 in a constituent parse tree, as shown in Figure 13.2: if we label the PP *about algebra*  
 7000 as an argument or adjunct, then its children *about* and *algebra* must be labeled as  $\emptyset$ .  
 7001 The same constraint also applies to the syntactic ancestors of this phrase.

7002 These constraints introduce dependencies across labeling decisions. In structure pre-  
 7003 diction problems such as sequence labeling and parsing, such dependencies are usually  
 7004 handled by defining a scoring over the entire structure,  $\mathbf{y}$ . Efficient inference requires  
 7005 that the global score decomposes into local parts: for example, in sequence labeling, the  
 7006 scoring function decomposes into scores of pairs of adjacent tags, permitting the applica-  
 7007 tion of the Viterbi algorithm for inference. But the constraints that arise in semantic role  
 7008 labeling are less amenable to local decomposition.<sup>10</sup> We therefore consider **constrained**  
 7009 **optimization** as an alternative solution.

Let the set  $\mathcal{C}(\tau)$  refer to all labelings that obey the constraints introduced by the parse  $\tau$ . The semantic role labeling problem can be reformulated as a constrained optimization over  $\mathbf{y} \in \mathcal{C}(\tau)$ ,

$$\begin{aligned} \max_{\mathbf{y}} \quad & \sum_{(i,j) \in \tau} \psi(\mathbf{w}, y_{i,j}, i, j, \rho, \tau) \\ \text{s.t.} \quad & \mathbf{y} \in \mathcal{C}(\tau). \end{aligned} \quad [13.5]$$

7010 In this formulation, the objective (shown on the first line) is a separable function of each  
 7011 individual labeling decision, but the constraints (shown on the second line) apply to the  
 7012 overall labeling. The sum  $\sum_{(i,j) \in \tau}$  indicates that we are summing over all constituent  
 7013 spans in the parse  $\tau$ . The expression s.t. in the second line means that we maximize the  
 7014 objective *subject to* the constraint  $\mathbf{y} \in \mathcal{C}(\tau)$ .

7015 A number of practical algorithms exist for restricted forms of constrained optimiza-  
 7016 tion. One such restricted form is **integer linear programming**, in which the objective and  
 7017 constraints are linear functions of integer variables. To formulate SRL as an integer linear  
 7018 program, we begin by rewriting the labels as a set of binary variables  $\mathbf{z} = \{z_{i,j,r}\}$  (Pun-  
 7019 yakanok et al., 2008),

$$z_{i,j,r} = \begin{cases} 1, & y_{i,j} = r \\ 0, & \text{otherwise,} \end{cases} \quad [13.6]$$

---

<sup>10</sup>Dynamic programming solutions have been proposed by Tromble and Eisner (2006) and Täckström et al. (2015), but they involve creating a trellis structure whose size is exponential in the number of labels.

7020 where  $r \in \mathcal{R}$  is a label in the set  $\{\text{ARG0}, \text{ARG1}, \dots, \text{AM-LOC}, \dots, \emptyset\}$ . Thus, the variables  
 7021  $z$  are a binarized version of the semantic role labeling  $y$ .

The objective can then be formulated as a linear function of  $z$ .

$$\sum_{(i,j) \in \tau} \psi(\mathbf{w}, y_{i,j}, i, j, \rho, \tau) = \sum_{i,j,r} \psi(\mathbf{w}, r, i, j, \rho, \tau) \times z_{i,j,r}, \quad [13.7]$$

7022 which is the sum of the scores of all relations, as indicated by  $z_{i,j,r}$ .

**Constraints** Integer linear programming permits linear inequality constraints, of the general form  $\mathbf{A}z \leq \mathbf{b}$ , where the parameters  $\mathbf{A}$  and  $\mathbf{b}$  define the constraints. To make this more concrete, let's start with the constraint that each non-null role type can occur only once in a sentence. This constraint can be written,

$$\forall r \neq \emptyset, \quad \sum_{(i,j) \in \tau} z_{i,j,r} \leq 1. \quad [13.8]$$

7023 Recall that  $z_{i,j,r} = 1$  iff the span  $(i, j)$  has label  $r$ ; this constraint says that for each possible  
 7024 label  $r \neq \emptyset$ , there can be at most one  $(i, j)$  such that  $z_{i,j,r} = 1$ . Rewriting this constraint  
 7025 can be written in the form  $\mathbf{A}z \leq \mathbf{b}$ , as you will find if you complete the exercises at the  
 7026 end of the chapter.

Now consider the constraint that labels cannot overlap. Let's define the convenience function  $o((i, j), (i', j')) = 1$  iff  $(i, j)$  overlaps  $(i', j')$ , and zero otherwise. Thus,  $o$  will indicate if a constituent  $(i', j')$  is either an ancestor or descendant of  $(i, j)$ . The constraint is that if two constituents overlap, only one can have a non-null label:

$$\forall (i, j) \in \tau, \quad \sum_{(i', j') \in \tau} \sum_{r \neq \emptyset} o((i, j), (i', j')) \times z_{i',j',r} \leq 1, \quad [13.9]$$

7027 where  $o((i, j), (i, j)) = 1$ .

In summary, the semantic role labeling problem can thus be rewritten as the following integer linear program,

$$\max_{z \in \{0,1\}^{|\tau|}} \quad \sum_{(i,j) \in \tau} \sum_{r \in \mathcal{R}} z_{i,j,r} \psi_{i,j,r} \quad [13.10]$$

$$s.t. \quad \forall r \neq \emptyset, \quad \sum_{(i,j) \in \tau} z_{i,j,r} \leq 1. \quad [13.11]$$

$$\forall (i, j) \in \tau, \quad \sum_{(i', j') \in \tau} \sum_{r \neq \emptyset} o((i, j), (i', j')) \times z_{i',j',r} \leq 1. \quad [13.12]$$

7028 **Learning with constraints** Learning can be performed in the context of constrained op-  
 7029 timization using the usual perceptron or large-margin classification updates. Because  
 7030 constrained inference is generally more time-consuming, a key question is whether it is  
 7031 necessary to apply the constraints during learning. Chang et al. (2008) find that better per-  
 7032 formance can be obtained by learning *without* constraints, and then applying constraints  
 7033 only when using the trained model to predict semantic roles for unseen data.

7034 **How important are the constraints?** Das et al. (2014) find that an unconstrained, classification-  
 7035 based method performs nearly as well as constrained optimization for FrameNet parsing;  
 7036 while it commits many violations of the “no-overlap” constraint, the overall  $F_1$  score is  
 7037 less than one point worse than the score at the constrained optimum. Similar results  
 7038 were obtained for PropBank semantic role labeling by Punyakanok et al. (2008). He et al.  
 7039 (2017) find that constrained inference makes a bigger impact if the constraints are based  
 7040 on manually-labeled “gold” syntactic parses. This implies that errors from the syntac-  
 7041 tic parser may limit the effectiveness of the constraints. Punyakanok et al. (2008) hedge  
 7042 against parser error by including constituents from several different parsers; any con-  
 7043 stituent can be selected from any parse, and additional constraints ensure that overlap-  
 7044 ping constituents are not selected.

7045 **Implementation** Integer linear programming solvers such as `glpk`,<sup>11</sup> `cplex`,<sup>12</sup> and `Gurobi`<sup>13</sup>  
 7046 allow inequality constraints to be expressed directly in the problem definition, rather than  
 7047 in the matrix form  $\mathbf{A}z \leq b$ . The time complexity of integer linear programming is theoreti-  
 7048 cally exponential in the number of variables  $|z|$ , but in practice these off-the-shelf solvers  
 7049 obtain good solutions efficiently. Das et al. (2014) report that the `cplex` solver requires 43  
 7050 seconds to perform inference on the FrameNet test set, which contains 4,458 predicates.

7051 Recent work has shown that many constrained optimization problems in natural lan-  
 7052 guage processing can be solved in a highly parallelized fashion, using optimization tech-  
 7053 niques such as **dual decomposition**, which are capable of exploiting the underlying prob-  
 7054 lem structure (Rush et al., 2010). Das et al. (2014) apply this technique to FrameNet se-  
 7055 mantic role labeling, obtaining an order-of-magnitude speedup over `cplex`.

### 7056 13.2.3 Neural semantic role labeling

7057 Neural network approaches to SRL have tended to treat it as a sequence labeling task,  
 7058 using a labeling scheme such as the **BIO notation**, which we previously saw in named  
 7059 entity recognition (§ 8.3). In this notation, the first token in a span of type ARG1 is labeled

---

<sup>11</sup><https://www.gnu.org/software/glpk/>

<sup>12</sup><https://www-01.ibm.com/software/commerce/optimization/cplex-optimizer/>

<sup>13</sup><http://www.gurobi.com/>

7060 B-ARG1; all remaining tokens in the span are *inside*, and are therefore labeled I-ARG1.  
 7061 Tokens outside any argument are labeled O. For example:

- 7062 (13.21) *Asha taught Boyang 's mom about algebra*  
 B-ARG0 PRED B-ARG2 I-ARG2 I-ARG2 B-ARG1 I-ARG1

Recurrent neural networks are a natural approach to this tagging task. For example, Zhou and Xu (2015) apply a deep bidirectional multilayer LSTM (see § 7.6) to PropBank semantic role labeling. In this model, each bidirectional LSTM serves as input for another, higher-level bidirectional LSTM, allowing complex non-linear transformations of the original input embeddings,  $\mathbf{X} = [\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_M]$ . The hidden state of the final LSTM is  $\mathbf{Z}^{(K)} = [\mathbf{z}_1^{(K)}, \mathbf{z}_2^{(K)}, \dots, \mathbf{z}_M^{(K)}]$ . The “emission” score for each tag  $Y_m = y$  is equal to the inner product  $\theta_y \cdot \mathbf{z}_m^{(K)}$ , and there is also a transition score for each pair of adjacent tags. The complete model can be written,

$$\mathbf{Z}^{(1)} = \text{BiLSTM}(\mathbf{X}) \quad [13.13]$$

$$\mathbf{Z}^{(i)} = \text{BiLSTM}(\mathbf{Z}^{(i-1)}) \quad [13.14]$$

$$\hat{\mathbf{y}} = \underset{\mathbf{y}}{\operatorname{argmax}} \sum_{m=1}^M \Theta^{(y)} \mathbf{z}_m^{(K)} + \psi_{y_{m-1}, y_m}. \quad [13.15]$$

7063 Note that the final step maximizes over the entire labeling  $\mathbf{y}$ , and includes a score for  
 7064 each tag transition  $\psi_{y_{m-1}, y_m}$ . This combination of LSTM and pairwise potentials on tags  
 7065 is an example of an **LSTM-CRF**. The maximization over  $\mathbf{y}$  is performed by the Viterbi  
 7066 algorithm.

7067 This model strongly outperformed alternative approaches at the time, including con-  
 7068 strained decoding and convolutional neural networks.<sup>14</sup> More recent work has combined  
 7069 recurrent neural network models with constrained decoding, using the  $A^*$  search algo-  
 7070 rithm to search over labelings that are feasible with respect to the constraints (He et al.,  
 7071 2017). This yields small improvements over the method of Zhou and Xu (2015). He et al.  
 7072 (2017) obtain larger improvements by creating an **ensemble** of SRL systems, each trained  
 7073 on an 80% subsample of the corpus. The average prediction across this ensemble is more  
 7074 robust than any individual model.

### 7075 13.3 Abstract Meaning Representation

7076 Semantic role labeling transforms the task of semantic parsing to a labeling task. Consider  
 7077 the sentence,

---

<sup>14</sup>The successful application of convolutional neural networks to semantic role labeling by Collobert and Weston (2008) was an influential early result in the most recent wave of neural networks in natural language processing.

```
(w / want-01
  :ARG0 (b / boy)
  :ARG1 (g / go-02
    :ARG0 b))
```

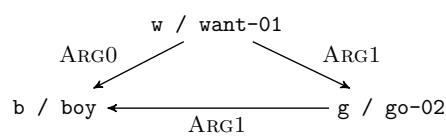


Figure 13.3: Two views of the AMR representation for the sentence *The boy wants to go.*

7078 (13.22) The boy wants to go.

7079 The PropBank semantic role labeling analysis is:

7080 • (PREDICATE : *wants*, ARG0 : *the boy*, ARG1 : *to go*)

7081 • (PREDICATE : *go*, ARG1 : *the boy*)

7082 The **Abstract Meaning Representation (AMR)** unifies this analysis into a graph structure, in which each node is a **variable**, and each edge indicates a **concept** (Banarescu et al., 2013). This can be written in two ways, as shown in Figure 13.3. On the left is the 7083 PENMAN notation (Matthiessen and Bateman, 1991), in which each set of parentheses 7084 introduces a variable. Each variable is an **instance** of a concept, which is indicated with 7085 the slash notation: for example, *w / want-01* indicates that the variable *w* is an instance 7086 of the concept *want-01*, which in turn refers to the PropBank frame for the first sense 7087 of the verb *want*. Relations are introduced with colons: for example, *:ARG0 (b / boy)* 7088 indicates a relation of type *ARG0* with the newly-introduced variable *b*. Variables can be 7089 reused, so that when the variable *b* appears again as an argument to *g*, it is understood to 7090 refer to the same boy in both cases. This arrangement is indicated compactly in the graph 7091 structure on the right, with edges indicating concepts. 7092

7093 One way in which AMR differs from PropBank-style semantic role labeling is that it 7094 reifies each entity as a variable: for example, *the boy* in (13.22) is reified in the variable 7095 *b*, which is reused as *ARG0* in its relationship with *w / want-01*, and as *ARG1* in its 7096 relationship with *g / go-02*. Reifying entities as variables also makes it possible to 7097 represent the substructure of noun phrases more explicitly. For example, *Asha borrowed* 7098 *the algebra book* would be represented as:

```
7100 (b / borrow-01
  :ARG0 (p / person
    :name (n / name
      :op1 "Asha"))
  :ARG1 (b2 / book
    :topic (a / algebra)))
```

7106 This indicates that the variable *p* is a person, whose name is the variable *n*; that name  
 7107 has one token, the string *Asha*. Similarly, the variable *b2* is a book, and the topic of *b2*  
 7108 is a variable *a* whose type is algebra. The relations name and topic are examples of  
 7109 **non-core roles**, which are similar to adjunct modifiers in PropBank. However, AMR’s  
 7110 inventory is more extensive, including more than 70 non-core roles, such as negation,  
 7111 time, manner, frequency, and location. Lists and sequences — such as the list of tokens in  
 7112 a name — are described using the roles *op1*, *op2*, etc.

7113 Another feature of AMR is that a semantic predicate can be introduced by any syntac-  
 7114 tic element, as in the following examples from Banarescu et al. (2013):

- 7115 (13.23) The boy destroyed the room.
- 7116 (13.24) the destruction of the room by the boy ...
- 7117 (13.25) the boy’s destruction of the room ...

7118 All these examples have the same semantics in AMR,

```
7119 (d / destroy-01
7120   :ARG0 (b / boy)
7121   :ARG1 (r / room))
```

7122 The noun *destruction* is linked to the verb *destroy*, which is captured by the PropBank  
 7123 frame *destroy-01*. This can happen with adjectives as well: in the phrase *the attractive*  
 7124 *spy*, the adjective *attractive* is linked to the PropBank frame *attract-01*:

```
7125 (s / spy
7126   :ARG0-of (a / attract-01))
```

7127 In this example, *ARG0-of* is an **inverse relation**, indicating that *s* is the *ARG0* of the  
 7128 predicate *a*. Inverse relations make it possible for all AMR parses to have a single root  
 7129 concept, which should be the **focus** of the utterance.

7130 While AMR goes farther than semantic role labeling, it does not link semantically-  
 7131 related frames such as *buy*/*sell* (as FrameNet does), does not handle quantification (as  
 7132 first-order predicate calculus does), and makes no attempt to handle noun number and  
 7133 verb tense (as PropBank does). A recent survey by Abend and Rappoport (2017) situ-  
 7134 ates AMR with respect to several other semantic representation schemes. Other linguistic  
 7135 features of AMR are summarized in the original paper (Banarescu et al., 2013) and the  
 7136 tutorial slides by Schneider et al. (2015).

### 7137 13.3.1 AMR Parsing

7138 Abstract Meaning Representation is not a labeling of the original text — unlike PropBank  
7139 semantic role labeling, and most of the other tagging and parsing tasks that we have  
7140 encountered thus far. The AMR for a given sentence may include multiple concepts for  
7141 single words in the sentence: as we have seen, the sentence *Asha likes algebra* contains both  
7142 person and name concepts for the word *Asha*. Conversely, words in the sentence may not  
7143 appear in the AMR: in *Boyang made a tour of campus*, the **light verb** *make* would not appear  
7144 in the AMR, which would instead be rooted on the predicate *tour*. As a result, AMR  
7145 is difficult to parse, and even evaluating AMR parsing involves considerable algorithmic  
7146 complexity (Cai and Yates, 2013).

7147 A further complexity is that AMR labeled datasets do not explicitly show the **alignment**  
7148 between the AMR annotation and the words in the sentence. For example, the link  
7149 between the word *wants* and the concept *want-01* is not annotated. To acquire training  
7150 data for learning-based parsers, it is therefore necessary to first perform an alignment  
7151 between the training sentences and their AMR parses. Flanigan et al. (2014) introduce a  
7152 rule-based parser, which links text to concepts through a series of increasingly high-recall  
7153 steps.

7154 **Graph-based parsing** One family of approaches to AMR parsing is similar to the graph-  
7155 based methods that we encountered in syntactic dependency parsing (chapter 11). For  
7156 these systems (Flanigan et al., 2014), parsing is a two-step process:

- 7157 1. **Concept identification** (Figure 13.4a). This involves constructing concept subgraphs  
7158 for individual words or spans of adjacent words. For example, in the sentence,  
7159 *Asha likes algebra*, we would hope to identify the minimal subtree including just the  
7160 concept *like-01* for the word *like*, and the subtree (*p / person :name (n /*  
7161 *name :op1 Asha)*) for the word *Asha*.
- 7162 2. **Relation identification** (Figure 13.4b). This involves building a directed graph over  
7163 the concepts, where the edges are labeled by the relation type. AMR imposes a  
7164 number of constraints on the graph: all concepts must be included, the graph must  
7165 be **connected** (there must be a path between every pair of nodes in the undirected  
7166 version of the graph), and every node must have at most one outgoing edge of each  
7167 type.

7168 Both of these problems are solved by structure prediction. Concept identification re-  
7169 quires simultaneously segmenting the text into spans, and labeling each span with a graph  
7170 fragment containing one or more concepts. This is done by computing a set of features  
7171 for each candidate span *s* and concept labeling *c*, and then returning the labeling with the  
7172 highest overall score.

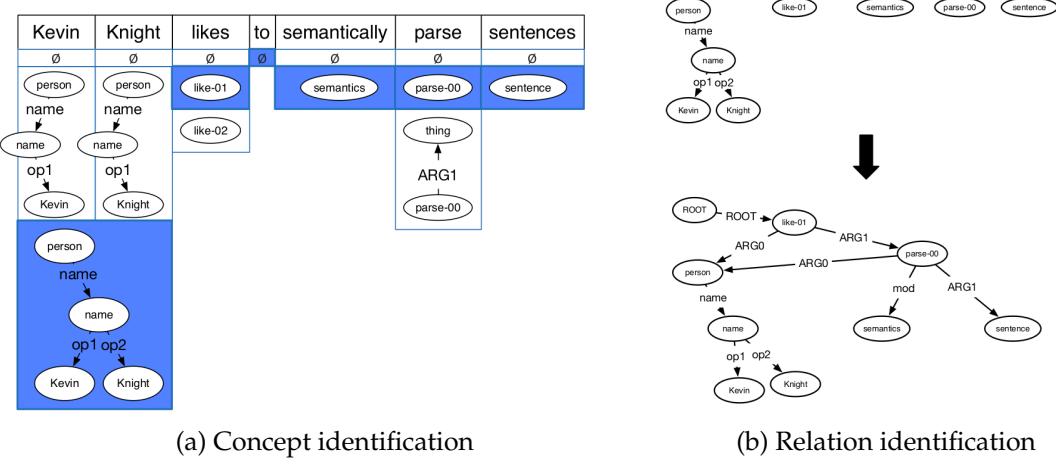


Figure 13.4: Subtasks for Abstract Meaning Representation parsing, from Schneider et al. (2015). [todo: permission]

7173     Relation identification can be formulated as search for the maximum spanning sub-  
 7174     graph, under a set of constraints. Each labeled edge has a score, which is computed  
 7175     from features of the concepts. We then search for the set of labeled edges that maximizes  
 7176     the sum of these scores, under the constraint that the resulting graph is a well-formed  
 7177     AMR (Flanigan et al., 2014). This constrained search can be performed by optimization  
 7178     techniques such as integer linear programming, as described in § 13.2.2.

7179     **Transition-based parsing** In many cases, AMR parses are structurally similar to syn-  
 7180     tactic dependency parses. Figure 13.5 shows one such example. This motivates an alter-  
 7181     native approach to AMR parsing: modify the syntactic dependency parse until it looks  
 7182     like a good AMR parse. Wang et al. (2015) propose a transition-based method, based on  
 7183     incremental modifications to the syntactic dependency tree (transition-based dependency  
 7184     parsing is discussed in § 11.3). At each step, the parser performs an action: for example,  
 7185     adding an AMR relation label to the current dependency edge, swapping the direction of  
 7186     a syntactic dependency edge, or cutting an edge and reattaching the orphaned subtree to  
 7187     a new parent. The overall system is trained as a classifier, learning to choose the action as  
 7188     would be given by an **oracle** that is capable of reproducing the ground-truth parse.

## 7189     13.4 Applications of Predicate-Argument Semantics

7190     **Question answering** Factoid questions have answers that are single words or phrases,  
 7191     such as *who discovered prions?*, *where was Barack Obama born?*, and *in what year did the Knicks*  
 7192     *last win the championship?* Semantic role labeling can be used to answer such questions,

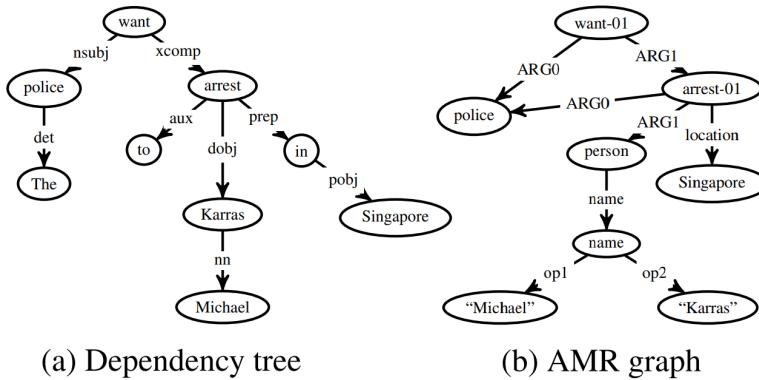


Figure 13.5: Syntactic dependency parse and AMR graph for the sentence *The police want to arrest Michael Karras in Singapore* (borrowed from Wang et al. (2015)) [todo: permission]

7193 by linking questions to sentences in a corpus of text. Shen and Lapata (2007) perform  
 7194 FrameNet semantic role labeling on the query, and then construct a weighted **bipartite**  
 7195 **graph**<sup>15</sup> between FrameNet semantic roles and the words and phrases in the sentence.  
 7196 This is done by first scoring all pairs of semantic roles and assignments, as shown in the  
 7197 top half of Figure 13.6. They then find the bipartite edge cover, which is the minimum  
 7198 weighted subset of edges such that each vertex has at least one edge, as shown in the  
 7199 bottom half of Figure 13.6. After analyzing the question in this manner, Shen and Lapata  
 7200 then find semantically-compatible sentences in the corpus, by performing graph matching  
 7201 on the bipartite graphs for the question and candidate answer sentences. Finally, the  
 7202 *expected answer phrase* in the question — typically the *wh*-word — is linked to a phrase in  
 7203 the candidate answer source, and that phrase is returned as the answer.

7204 **Relation extraction** The task of **relation extraction** involves identifying pairs of entities  
 7205 for which a given semantic relation holds (see § 17.2. For example, we might like to find  
 7206 all pairs  $(i, j)$  such that  $i$  is the INVENTOR-OF  $j$ . PropBank semantic role labeling can  
 7207 be applied to this task by identifying sentences whose verb signals the desired relation,  
 7208 and then extracting ARG1 and ARG2 as arguments. (To fully solve this task, these argu-  
 7209 ments must then be linked to entities, as described in chapter 17.) Christensen et al. (2010)  
 7210 compare a semantic role labeling system against a simpler approach based on surface pat-  
 7211 terns (Banko et al., 2007). They find that the SRL system is considerably more accurate,  
 7212 but that it is several orders of magnitude slower. Conversely, Barnickel et al. (2009) apply  
 7213 SENNA, a convolutional neural network SRL system (Collobert and Weston, 2008) to the  
 7214 task of identifying biomedical relations (e.g., which genes inhibit or activate each other).

<sup>15</sup>A bipartite graph is one in which the vertices can be divided into two disjoint sets, and every edge connects a vertex in one set to a vertex in the other.

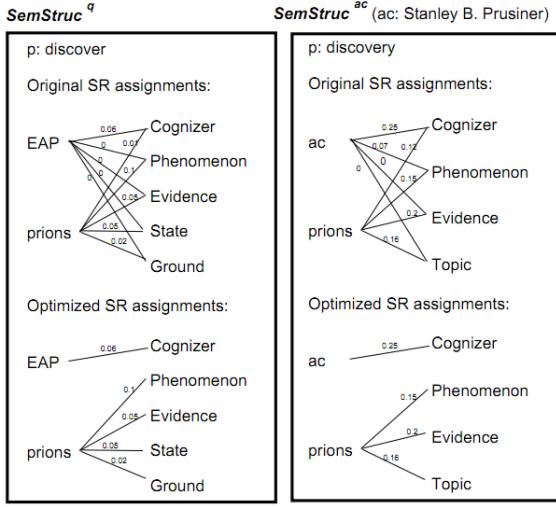


Figure 13.6: FrameNet semantic role labeling is used in factoid question answering, by aligning the semantic roles in the question (q) against those of sentences containing answer candidates (ac). “EAP” is the expected answer phrase, replacing the word *who* in the question. Figure reprinted from Shen and Lapata (2007) [todo: permission]

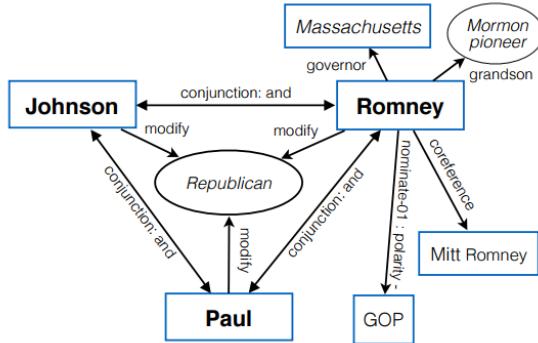


Figure 13.7: Fragment of AMR knowledge network for entity linking. Figure reprinted from Pan et al. (2015) [todo: permission]

7215 In comparison with a strong baseline that applies a set of rules to syntactic dependency  
 7216 structures (Fundel et al., 2007), the SRL system is faster but less accurate. One possible  
 7217 explanation for these divergent results is that Fundel et al. compare against a baseline  
 7218 which is carefully tuned for performance in a relatively narrow domain, while the system  
 7219 of Banko et al. is designed to analyze text across the entire web.

7220 **Entity linking** Another core task in information extraction is to link mentions of entities  
7221 (e.g., *Republican candidates like Romney, Paul, and Johnson* ...) to entities in a knowledge  
7222 base (e.g., LYNDON JOHNSON or GARY JOHNSON). This task, which is described in § 17.1,  
7223 is often performed by examining nearby “collaborator” mentions — in this case, *Romney*  
7224 and *Paul*. By jointly linking all such mentions, it is possible to arrive at a good overall  
7225 solution. Pan et al. (2015) apply AMR to this problem. For each entity, they construct a  
7226 knowledge network based on its semantic relations with other mentions within the same  
7227 sentence. They then rerank a set of candidate entities, based on the overlap between  
7228 the entity’s knowledge network and the semantic relations present in the sentence (Figure  
7229 13.7).

7230 **Exercises**

- 7231 1. Write out an event semantic representation for the following sentences. You may  
7232 make up your own predicates.
    - 7233 (13.26) *Abigail shares with Max.*
    - 7234 (13.27) *Abigail reluctantly shares a toy with Max.*
    - 7235 (13.28) *Abigail hates to share with Max.*
  - 7236 2. Find the PropBank framesets for *share* and *hate* at <http://verbs.colorado.edu/propbank/framesets-english-aliases/>, and rewrite your answers from the  
7237 previous question, using the thematic roles ARG0, ARG1, and ARG2.
  - 7239 3. Compute the syntactic path features for Abigail and Max in each of the example sentences (13.26) and (13.28) in Question 1, with respect to the verb *share*. If you’re not  
7240 sure about the parse, you can try an online parser such as <http://nlp.stanford.edu:8080/parser/>.  
7241
  - 7243 4. Compute the dependency path features for Abigail and Max in each of the example sentences (13.26) and (13.28) in Question 1, with respect to the verb *share*. Again, if  
7244 you’re not sure about the parse, you can try an online parser such as <http://nlp.stanford.edu:8080/parser/>. As a hint, the dependency relation between *share*  
7245 and *Max* is OBL according to the Universal Dependency treebank (version 2).  
7246
  - 7248 5. PropBank semantic role labeling includes **reference arguments**, such as,
- 7249 (13.29) [AM-LOC The bed] on [R-AM-LOC which] I slept broke.<sup>16</sup>

---

<sup>16</sup>Example from 2013 NAACL tutorial slides by Shumin Wu

7250       The label R-AM-LOC indicates that word *which* is a reference to *The bed*, which ex-  
 7251       presses the location of the event. Reference arguments must have referents: the tag  
 7252       R-AM-LOC can appear only when AM-LOC also appears in the sentence. Show how  
 7253       to express this as a linear constraint, specifically for the tag R-AM-LOC. Be sure to  
 7254       correctly handle the case in which neither AM-LOC nor R-AM-LOC appear in the  
 7255       sentence.

- 7256     6. Explain how to express the constraints on semantic role labeling in Equation 13.8  
 7257       and Equation 13.9 in the general form  $Az \geq b$ .
- 7258     7. Download the FrameNet sample data (<https://framenet.icsi.berkeley.edu/fndrupal/fulltextIndex>), and train a bag-of-words classifier to predict the  
 7259       frame that is evoked by each verb in each example. Your classifier should build  
 7260       a bag-of-words from the sentence in which the frame-evoking lexical unit appears.  
 7261       [**todo: Somehow limit to one or a few lexical units.**] [**todo: use NLTK if possible**]
- 7263     8. Download the PropBank sample data, using NLTK (<http://www.nltk.org/howto/propbank.html>). Use a deep learning toolkit such as PyTorch or DyNet to train an  
 7264       LSTM to predict tags. You will have to convert the downloaded instances to a BIO  
 7265       sequence labeling representation first.
- 7267     9. Produce the AMR annotations for the following examples:

- 7268       (13.30) The girl likes the boy.
- 7269       (13.31) The girl was liked by the boy.
- 7270       (13.32) Abigail likes Maxwell Aristotle.
- 7271       (13.33) The spy likes the attractive boy.
- 7272       (13.34) The girl doesn't like the boy.
- 7273       (13.35) The girl likes her dog.

7274       For (13.32), recall that multi-token names are created using op1, op2, etc. You will  
 7275       need to consult Banerjee et al. (2013) for (13.34), and Schneider et al. (2015) for  
 7276       (13.35). You may assume that *her* refers to *the girl* in this example.

- 7277     10. Using an off-the-shelf PropBank SRL system,<sup>17</sup> build a simplified question answer-  
 7278       ing system in the style of Shen and Lapata (2007). Specifically, your system should  
 7279       do the following:

---

<sup>17</sup>At the time of writing, the following systems are available: SENNA (<http://ronan.collobert.com/senna/>), Illinois Semantic Role Labeler ([https://cogcomp.cs.illinois.edu/page/software\\_view/SRL](https://cogcomp.cs.illinois.edu/page/software_view/SRL)), and mate-tools (<https://code.google.com/archive/p/mate-tools/>).

- 7280 • For each document in a collection, it should apply the semantic role labeler,  
7281 and should store the output as a tuple.
- 7282 • For a question, your system should again apply the semantic role labeler. If  
7283 any of the roles are filled by a *wh*-pronoun, you should mark that role as the  
7284 expected answer phrase (EAP).
- 7285 • To answer the question, search for a stored tuple which matches the question as  
7286 well as possible (same predicate, no incompatible semantic roles, and as many  
7287 matching roles as possible). Align the EAP against its role filler in the stored  
7288 tuple, and return this as the answer.

7289 To evaluate your system, download a set of three news articles on the same topic,  
7290 and write down five factoid questions that should be answerable from the arti-  
7291 cles. See if your system can answer these questions correctly. (If this problem is  
7292 assigned to an entire class, you can build a large-scale test set and compare various  
7293 approaches.)



## 7294 Chapter 14

# 7295 Distributional and distributed 7296 semantics

7297 A recurring theme in natural language processing is the complexity of the mapping from  
7298 words to meaning. In chapter 4, we saw that a single word form, like *bank*, can have mul-  
7299 tiple meanings; conversely, a single meaning may be created by multiple surface forms,  
7300 a lexical semantic relationship known as **synonymy**. Despite this complex mapping be-  
7301 tween words and meaning, natural language processing systems usually rely on words  
7302 as the basic unit of analysis. This is especially true in semantics: the logical and frame  
7303 semantic methods from the previous two chapters rely on hand-crafted lexicons that map  
7304 from words to semantic predicates. But how can we analyze texts that contain words  
7305 that we haven't seen before? This chapter describes methods that learn representations  
7306 of word meaning by analyzing unlabeled data, vastly improving the generalizability of  
7307 natural language processing systems. The theory that makes it possible to acquire mean-  
7308 ingful representations from unlabeled data is the **distributional hypothesis**.

### 7309 14.1 The distributional hypothesis

7310 Here's a word you may not know: *tezgüino* (the example is from Lin, 1998). If you do not  
7311 know the meaning of *tezgüino*, then you are in the same situation as a natural language  
7312 processing system when it encounters a word that did not appear in its training data.  
7313 Now suppose you see that *tezgüino* is used in the following contexts:

- 7314 (14.1) A bottle of \_\_\_\_\_ is on the table.
- 7315 (14.2) Everybody likes \_\_\_\_\_.
- 7316 (14.3) Don't have \_\_\_\_\_ before you drive.
- 7317 (14.4) We make \_\_\_\_\_ out of corn.

	(14.1)	(14.2)	(14.3)	(14.4)	...
<i>tezgüino</i>	1	1	1	1	
<i>loud</i>	0	0	0	0	
<i>motor oil</i>	1	0	0	1	
<i>tortillas</i>	0	1	0	1	
<i>choices</i>	0	1	0	0	
<i>wine</i>	1	1	1	0	

Table 14.1: Distributional statistics for *tezgüino* and five related terms

7318     What other words fit into these contexts? How about: *loud*, *motor oil*, *tortillas*, *choices*,  
 7319     *wine*? Each row of Table 14.1 is a vector that summarizes the contextual properties for  
 7320     each word, with a value of one for contexts in which the word can appear, and a value of  
 7321     zero for contexts in which it cannot. Based on these vectors, we can conclude: *wine* is very  
 7322     similar to *tezgüino*; *motor oil* and *tortillas* are fairly similar to *tezgüino*; *loud* is completely  
 7323     different.

7324     These vectors, which we will call **word representations**, describe the **distributional**  
 7325     properties of each word. Does vector similarity imply semantic similarity? This is the **dis-**  
 7326     **distributional hypothesis**, stated by Firth (1957) as: “You shall know a word by the company  
 7327     it keeps.” The distributional hypothesis has stood the test of time: distributional statistics  
 7328     are a core part of language technology today, because they make it possible to leverage  
 7329     large amounts of unlabeled data to learn about rare words that do not appear in labeled  
 7330     training data.

7331     Distributional statistics have a striking ability to capture lexical semantic relationships  
 7332     such as analogies. Figure 14.1 shows two examples, based on two-dimensional projections  
 7333     of distributional **word embeddings**, discussed later in this chapter. In each case, word-  
 7334     pair relationships correspond to regular linear patterns in this two dimensional space. No  
 7335     labeled data about the nature of these relationships was required to identify this underly-  
 7336     ing structure.

7337     **Distributional** semantics are computed from context statistics. **Distributed** seman-  
 7338     tics are a related but distinct idea: that meaning can be represented by numerical vectors  
 7339     rather than symbolic structures. Distributed representations are often estimated from dis-  
 7340     tributional statistics, as in latent semantic analysis and WORD2VEC, described later in this  
 7341     chapter. However, distributed representations can also be learned in a supervised fashion  
 7342     from labeled data, as in the neural classification models encountered in chapter 3.

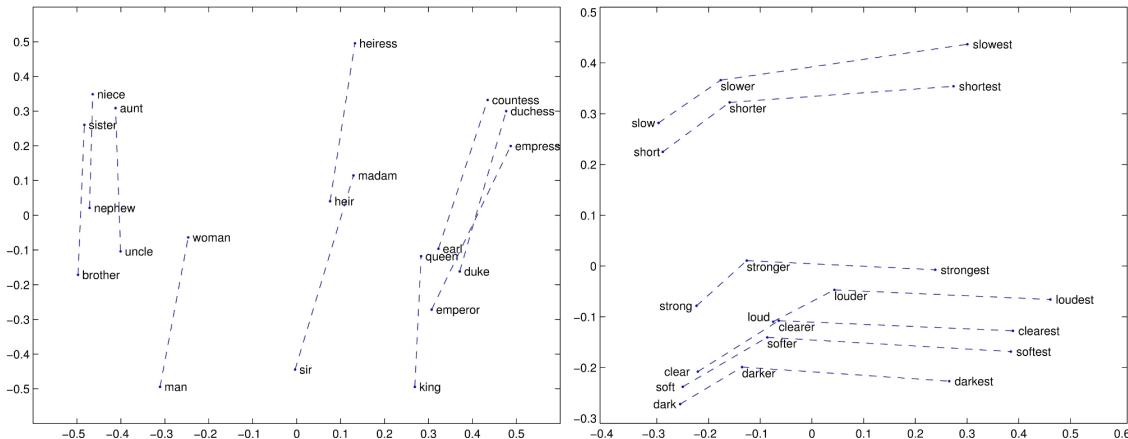


Figure 14.1: Lexical semantic relationships have regular linear structures in two dimensional projections of distributional statistics. From [http://nlp.stanford.edu/projects/glove/.\[todo: redo to make words bigger?\]](http://nlp.stanford.edu/projects/glove/.[todo: redo to make words bigger?])

## 7343 14.2 Design decisions for word representations

7344 There are many approaches for computing word representations, but most can be distin-  
 7345 guished on three main dimensions: the nature of the representation, the source of context-  
 7346 ual information, and the estimation procedure.

### 7347 14.2.1 Representation

7348 Today, the dominant word representations are  $k$ -dimensional vectors of real numbers,  
 7349 known as **word embeddings**. (The name is due to the fact that each discrete word is em-  
 7350 bedded in a continuous vector space.) This representation dates back at least to the late  
 7351 1980s (Deerwester et al., 1990), and is used in popular techniques such as WORD2VEC (Mikolov  
 7352 et al., 2013).

7353 Word embeddings are well suited for neural networks, where they can be plugged  
 7354 in as inputs. They can also be applied in linear classifiers and structure prediction mod-  
 7355 els (Turian et al., 2010), although it can be difficult to learn linear models that employ  
 7356 real-valued features (Kummerfeld et al., 2015). A popular alternative is bit-string rep-  
 7357 resentations, such as **Brown clusters** (§ 14.4), in which each word is represented by a  
 7358 variable-length sequence of zeros and ones (Brown et al., 1992).

7359 Another representational question is whether to estimate one embedding per surface  
 7360 form (e.g., *bank*), or to estimate distinct embeddings for each word sense or synset. In-  
 7361 tuitively, if word representations are to capture the meaning of individual words, then  
 7362 words with multiple meanings should have multiple embeddings. This can be achieved

---

*The moment one learns English, complications set in* (Alfau, 1999)

---

Brown Clusters (Brown et al., 1992)	{one}
WORD2VEC (Mikolov et al., 2013) ( $h = 2$ )	{moment, one, English, complications}
Structured WORD2VEC (Ling et al., 2015) ( $h = 2$ )	$\{(moment, -2), (one, -1), (English, +1), (complications, +2)\}$
Dependency contexts (Levy and Goldberg, 2014)	$\{(one, \text{NSUBJ}), (\text{English}, \text{DOBJ}), (moment, \text{ACL}^{-1})\}$

---

Table 14.2: Contexts for the word *learns*, according to various word representations. For dependency context, *(one, NSUBJ)* means that there is a relation of type NSUBJ (nominal subject) **to** the word *one*, and *(moment, ACL<sup>-1</sup>)* means that there is a relation of type ACL (adjectival clause) **from** the word *moment*.

7363 by integrating unsupervised clustering with word embedding estimation (Huang and  
 7364 Yates, 2012; Li and Jurafsky, 2015). However, Arora et al. (2016) argue that it is unnec-  
 7365 essary to model distinct word senses explicitly, because the embeddings for each surface  
 7366 form are a linear combination of the embeddings of the underlying senses.

### 7367 14.2.2 Context

7368 The distributional hypothesis says that word meaning is related to the “contexts” in which  
 7369 the word appears, but context can be defined in many ways. In the *tezgiiino* example, con-  
 7370 texts are entire sentences, but in practice there are far too many sentences. At the oppo-  
 7371 site extreme, the context could be defined as the immediately preceding word; this is the  
 7372 context considered in Brown clusters. WORD2VEC takes an intermediate approach, using  
 7373 local neighborhoods of words (e.g.,  $h = 5$ ) as contexts (Mikolov et al., 2013). Contexts  
 7374 can also be much larger: for example, in **latent semantic analysis**, each word’s context  
 7375 vector includes an entry per document, with a value of one if the word appears in the  
 7376 document (Deerwester et al., 1990); in **explicit semantic analysis**, these documents are  
 7377 Wikipedia pages (Gabrilovich and Markovitch, 2007).

7378 Words in context can be labeled by their position with respect to the target word  $w_m$   
 7379 (e.g., two words before, one word after), which makes the resulting word representations  
 7380 more sensitive to syntactic differences (Ling et al., 2015). Another way to incorporate  
 7381 syntax is to perform parsing as a preprocessing step, and then form context vectors from  
 7382 the dependency edges (Levy and Goldberg, 2014) or predicate-argument relations (Lin,  
 7383 1998). The resulting context vectors for several of these methods are shown in Table 14.2.

7384 The choice of context has a profound effect on the resulting representations, which

7385 can be viewed in terms of word similarity. Applying latent semantic analysis (§ 14.3) to  
 7386 contexts of size  $h = 2$  and  $h = 30$  yields the following nearest-neighbors for the word  
 7387 *dog*:<sup>1</sup>

- 7388 • ( $h = 2$ ): *cat, horse, fox, pet, rabbit, pig, animal, mongrel, sheep, pigeon*  
 7389 • ( $h = 30$ ): *kennel, puppy, pet, bitch, terrier, rottweiler, canine, cat, to bark, Alsatian*

7390 Which word list is better? Each word in the  $h = 2$  list is an animal, reflecting the fact that  
 7391 locally, the word *dog* tends to appear in the same contexts as other animal types (e.g., *pet*  
 7392 *the dog, feed the dog*). In the  $h = 30$  list, nearly everything is dog-related, including specific  
 7393 breeds such as *rottweiler* and *Alsatian*. The list also includes words that are not animals  
 7394 (*kennel*), and in one case (*to bark*), is not a noun at all. The 2-word context window is more  
 7395 sensitive to syntax, while the 30-word window is more sensitive to topic.

### 7396 14.2.3 Estimation

7397 Word embeddings are estimated by optimizing some objective: the likelihood of a set of  
 7398 unlabeled data (or a closely related quantity), or the reconstruction of a matrix of context  
 7399 counts, similar to Table 14.1.

7400 **Maximum likelihood estimation** Likelihood-based optimization is derived from the  
 7401 objective  $\log p(\mathbf{w}; \mathbf{U})$ , where  $\mathbf{U} \in \mathbb{R}^{K \times V}$  is matrix of word embeddings, and  $\mathbf{w} =$   
 7402  $\{\mathbf{w}_m\}_{m=1}^M$  is a corpus, represented as a list of  $M$  tokens. Recurrent neural network lan-  
 7403 guage models (§ 6.3) optimize this objective directly, backpropagating to the input word  
 7404 embeddings through the recurrent structure. However, state-of-the-art word embeddings  
 7405 employ huge corpora with hundreds of billions of tokens, and recurrent architectures are  
 7406 difficult to scale to such data. As a result, likelihood-based word embeddings are usually  
 7407 based on simplified likelihoods or heuristic approximations.

**Matrix factorization** The matrix  $\mathbf{C} = \{\text{count}(i, j)\}$  stores the co-occurrence counts of  
 word  $i$  and context  $j$ . Word representations can be obtained by approximately factoring  
 this matrix, so that  $\text{count}(i, j)$  is approximated by a function of a word embedding  $\mathbf{u}_i$  and  
 a context embedding  $\mathbf{v}_j$ . These embeddings can be obtained by minimizing the norm of  
 the reconstruction error,

$$\min_{\mathbf{u}, \mathbf{v}} \|\mathbf{C} - \tilde{\mathbf{C}}(\mathbf{u}, \mathbf{v})\|_F, \quad [14.1]$$

---

<sup>1</sup>The example is from lecture slides by Marco Baroni, Alessandro Lenci, and Stefan Evert, who applied latent semantic analysis to the British National Corpus. You can find an online demo here: <http://clic.cimec.unitn.it/infomap-query/>

7408 where  $\tilde{\mathbf{C}}(\mathbf{u}, \mathbf{v})$  is the approximate reconstruction resulting from the embeddings  $\mathbf{u}$  and  
 7409  $\mathbf{v}$ , and  $\|\mathbf{X}\|_F$  indicates the Frobenius norm,  $\sum_{i,j} x_{i,j}^2$ . Rather than factoring the matrix of  
 7410 word-context counts directly, it is often helpful to transform these counts using information-  
 7411 theoretic metrics such as **pointwise mutual information** (PMI), described in the next sec-  
 7412 tion.

### 7413 14.3 Latent semantic analysis

Latent semantic analysis (LSA) is one of the oldest approaches to distributed semantics (Deerwester et al., 1990). It induces continuous vector representations of words by factoring a matrix of word and context counts, using **truncated singular value decomposition** (SVD),

$$\min_{\mathbf{U} \in \mathbb{R}^{V \times K}, \mathbf{S} \in \mathbb{R}^{K \times K}, \mathbf{V} \in \mathbb{R}^{|\mathcal{C}| \times K}} \|\mathbf{C} - \mathbf{USV}^\top\|_F \quad [14.2]$$

$$\text{s.t. } \mathbf{U}^\top \mathbf{U} = \mathbb{I} \quad [14.3]$$

$$\mathbf{V}^\top \mathbf{V} = \mathbb{I} \quad [14.4]$$

$$\forall i \neq j, \mathbf{S}_{i,j} = 0, \quad [14.5]$$

7414 where  $V$  is the size of the vocabulary,  $|\mathcal{C}|$  is the number of contexts, and  $K$  is size of the  
 7415 resulting embeddings, which are set equal to the rows of the matrix  $\mathbf{U}$ . The matrix  $\mathbf{S}$  is  
 7416 constrained to be diagonal (these diagonal elements are called the singular values), and  
 7417 the columns of the product  $\mathbf{SV}^\top$  provide descriptions of the contexts. Each element  $c_{i,j}$  is  
 7418 then reconstructed as a **bilinear product**,

$$c_{i,j} \approx \sum_{k=1}^K u_{i,k} s_k v_{j,k}. \quad [14.6]$$

7419 The objective is to minimize the sum of squared approximation errors. The orthonormality  
 7420 constraints  $\mathbf{U}^\top \mathbf{U} = \mathbf{V}^\top \mathbf{V} = \mathbb{I}$  ensure that all pairs of dimensions in  $\mathbf{U}$  and  $\mathbf{V}$  are  
 7421 uncorrelated, so that each dimension conveys unique information. Efficient implemen-  
 7422 tations of truncated singular value decomposition are available in numerical computing  
 7423 packages such as `scipy` and `matlab`.<sup>2</sup>

Latent semantic analysis is most effective when the count matrix is transformed before the application of SVD. One such transformation is **pointwise mutual information** (PMI; Church and Hanks, 1990), which captures the degree of association between word  $i$  and

---

<sup>2</sup>An important implementation detail is to represent  $\mathbf{C}$  as a **sparse matrix**, so that the storage cost is equal to the number of non-zero entries, rather than the size  $V \times |\mathcal{C}|$ .

context  $j$ ,

$$\text{PMI}(i, j) = \log \frac{p(i, j)}{p(i)p(j)} = \log \frac{p(i | j)p(j)}{p(i)p(j)} = \log \frac{p(i | j)}{p(i)} \quad [14.7]$$

$$= \log \text{count}(i, j) - \log \sum_{i'=1}^V \text{count}(i', j) \quad [14.8]$$

$$- \log \sum_{j' \in \mathcal{C}} \text{count}(i, j') + \log \sum_{i'=1}^V \sum_{j' \in \mathcal{C}} \text{count}(i', j'). \quad [14.9]$$

7424 The pointwise mutual information can be viewed as the logarithm of the ratio of the con-  
 7425 ditional probability of word  $i$  in context  $j$  to the marginal probability of word  $i$  in all  
 7426 contexts. When word  $i$  is statistically associated with context  $j$ , the ratio will be greater  
 7427 than one, so  $\text{PMI}(i, j) > 0$ . The PMI transformation focuses latent semantic analysis on re-  
 7428 constructing strong word-context associations, rather than on reconstructing large counts.

7429 The PMI is negative when a word and context occur together less often than if they  
 7430 were independent, but such negative correlations are unreliable because counts of rare  
 7431 events have high variance. Furthermore, the PMI is undefined when  $\text{count}(i, j) = 0$ . One  
 7432 solution to these problems is to use the **Positive PMI** (PPMI),

$$\text{PPMI}(i, j) = \begin{cases} \text{PMI}(i, j), & p(i | j) > p(i) \\ 0, & \text{otherwise.} \end{cases} \quad [14.10]$$

7433 Bullinaria and Levy (2007) compare a range of matrix transformations for latent se-  
 7434 mantic analysis, using a battery of tasks related to word meaning and word similarity  
 7435 (for more on evaluation, see § 14.6). They find that PPMI-based latent semantic analysis  
 7436 yields strong performance on a battery of tasks related to word meaning: for example,  
 7437 PPMI-based LSA vectors can be used to solve multiple-choice word similarity questions  
 7438 from the Test of English as a Foreign Language (TOEFL), obtaining 85% accuracy.

## 7439 14.4 Brown clusters

7440 Learning algorithms like perceptron and conditional random fields often perform better  
 7441 with discrete feature vectors. A simple way to obtain discrete representations from distri-  
 7442 butional statistics is by clustering (§ 5.1.1), so that words in the same cluster have similar  
 7443 distributional statistics. This can help in downstream tasks, by sharing features between  
 7444 all words in the same cluster. However, there is an obvious tradeoff: if the number of clus-  
 7445 ters is too small, the words in each cluster will not have much in common; if the number  
 7446 of clusters is too large, then the learner will not see enough examples from each cluster to  
 7447 generalize.

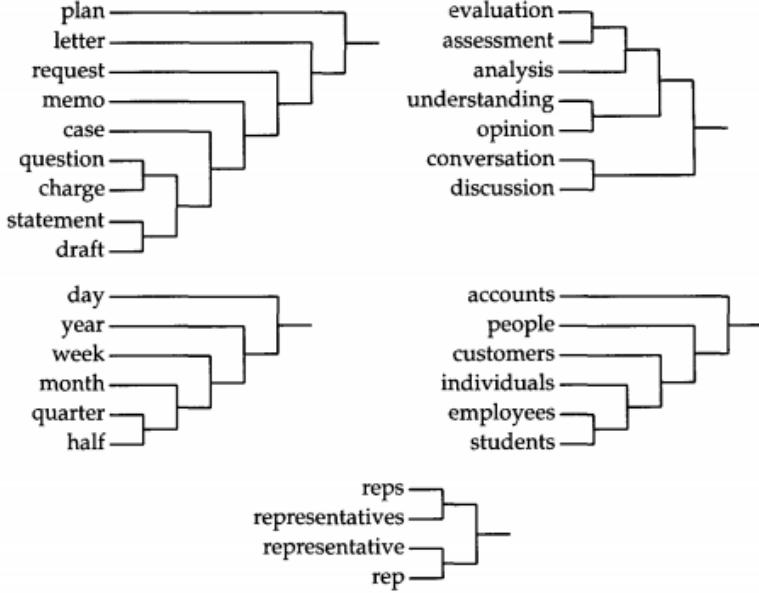


Figure 14.2: Some subtrees produced by bottom-up Brown clustering (Miller et al., 2004) on news text [todo: permission]

7448 A solution to this problem is **hierarchical clustering**: using the distributional statistics  
 7449 to induce a tree-structured representation. Fragments of **Brown cluster** trees are shown in  
 7450 Figure 14.2 and Table 14.3. Each word’s representation consists of a binary string describ-  
 7451 ing a path through the tree: 0 for taking the left branch, and 1 for taking the right branch.  
 7452 In the subtree in the upper right of the figure, the representation of the word *conversation*  
 7453 is 10; the representation of the word *assessment* is 0001. Bitstring prefixes capture simila-  
 7454 rity at varying levels of specificity, and it is common to use the first eight, twelve, sixteen,  
 7455 and twenty bits as features in tasks such as named entity recognition (Miller et al., 2004)  
 7456 and dependency parsing (Koo et al., 2008).

Hierarchical trees can be induced from a likelihood-based objective, using a discrete latent variable  $k_i \in \{1, 2, \dots, K\}$  to represent the cluster of word  $i$ :

$$\log p(\mathbf{w}; \mathbf{k}) \approx \sum_{m=1}^M \log p(w_m | w_{m-1}; \mathbf{k}) \quad [14.11]$$

$$\triangleq \sum_{m=1}^M \log p(w_m | k_{w_m}) + \log p(k_{w_m} | k_{w_{m-1}}). \quad [14.12]$$

7457 This is similar to a hidden Markov model, with the crucial difference that each word can

bitstring	ten most frequent words
01111010 <b>0111</b>	<i>excited thankful grateful stoked pumped anxious hyped psyched exited geeked</i>
01111010 <b>100</b>	<i>talking talkin complaining talkn bitching tlkn tlkin bragging rav- ing +k</i>
01111010 <b>1010</b>	<i>thinking thinkin dreaming worrying thinkn speakin reminiscing dreamin daydreaming fantasizing</i>
01111010 <b>1011</b>	<i>saying sayin suggesting stating sayn jokin talmbout implying insisting 5'2</i>
01111010 <b>1100</b>	<i>wonder dunno wondered duno donno dno doно wonda wounder dunnoe</i>
01111010 <b>1101</b>	<i>wondering wonders debating deciding pondering unsure won- derin debatin woundering wondern</i>
01111010 <b>1110</b>	<i>sure suree suuure suure sure- surre sures shuree</i>

Table 14.3: Fragment of a Brown clustering of Twitter data (Owoputi et al., 2013). Each row is a leaf in the tree, showing the ten most frequent words. This part of the tree emphasizes verbs of communicating and knowing, especially in the present participle. Each leaf node includes orthographic variants (*thinking*, *thinkin*, *thinkn*), semantically related terms (*excited*, *thankful*, *grateful*), and some outliers (*5'2*, *+k*). See [http://www.cs.cmu.edu/~ark/TweetNLP/cluster\\_viewer.html](http://www.cs.cmu.edu/~ark/TweetNLP/cluster_viewer.html) for more.

7458 be emitted from only a single cluster:  $\forall k \neq k_{w_m}, p(w_m | k) = 0$ .

Using the objective in Equation 14.12, the Brown clustering tree can be constructed from the bottom up: begin with each word in its own cluster, and incrementally merge clusters until only a single cluster remains. At each step, we merge the pair of clusters such that the objective in Equation 14.12 is maximized. Although the objective seems to involve a sum over the entire corpus, the score for each merger can be computed from the cluster-to-cluster co-occurrence counts. These counts can be updated incrementally as the clustering proceeds. The optimal merge at each step can be shown to maximize the **average mutual information**,

$$I(\mathbf{k}) = \sum_{k_1=1}^K \sum_{k_2=1}^K p(k_1, k_2) \times \text{PMI}(k_1, k_2) \quad [14.13]$$

$$p(k_1, k_2) = \frac{\text{count}(k_1, k_2)}{\sum_{k_{1'}=1}^K \sum_{k_{2'}=1}^K \text{count}(k_{1'}, k_{2'})},$$

7459 where  $p(k_1, k_2)$  is the joint probability of a bigram involving a word in cluster  $k_1$  followed  
7460 by a word in  $k_2$ . This probability and the PMI are both computed from the co-occurrence

---

**Algorithm 17** Exchange clustering algorithm. Assumes that words are sorted by frequency, and that MAXMI finds the cluster pair whose merger maximizes the mutual information, as defined in Equation 14.13.

---

```

procedure EXCHANGECLUSTERING({count( $\cdot, \cdot$ )},  $K$ )
    for  $i \in 1 \dots K$  do                                 $\triangleright$  Initialization
         $k_i \leftarrow i$ ,  $i = 1, 2, \dots, K$ 
        for  $j \in 1 \dots K$  do
             $c_{i,j} \leftarrow \text{count}(i, j)$ 
         $\tau \leftarrow \{(i)\}_{i=1}^K$ 
        for  $i \in \{K + 1, K + 2, \dots, V\}$  do       $\triangleright$  Iteratively add each word to the clustering
             $\tau \leftarrow \tau \cup (i)$ 
            for  $k \in \tau$  do
                 $c_{k,i} \leftarrow \text{count}(k, i)$ 
                 $c_{i,k} \leftarrow \text{count}(i, k)$ 
                 $\hat{i}, \hat{j} \leftarrow \text{MAXMI}(\mathbf{C})$ 
                 $\tau, \mathbf{C} \leftarrow \text{MERGE}(\hat{i}, \hat{j}, \mathbf{C}, \tau)$ 
        repeat                                          $\triangleright$  Merge the remaining clusters into a tree
             $\hat{i}, \hat{j} \leftarrow \text{MAXMI}(\mathbf{C}, \tau)$ 
             $\tau, \mathbf{C} \leftarrow \text{MERGE}(\hat{i}, \hat{j}, \mathbf{C}, \tau)$ 
        until  $|\tau| = 1$ 
        return  $\tau$ 
procedure MERGE( $i, j, \mathbf{C}, \tau$ )
     $\tau \leftarrow \tau \setminus i \setminus j \cup (i, j)$            $\triangleright$  Merge the clusters in the tree
    for  $k \in \tau$  do                                 $\triangleright$  Aggregate the counts across the merged clusters
         $c_{k,(i,j)} \leftarrow c_{k,i} + c_{k,j}$ 
         $c_{(i,j),k} \leftarrow c_{i,k} + c_{j,k}$ 
    return  $\tau, \mathbf{C}$ 

```

---

7461 counts between clusters. After each merger, the co-occurrence vectors for the merged  
 7462 clusters are simply added up, so that the next optimal merger can be found efficiently.

7463 This bottom-up procedure requires iterating over the entire vocabulary, and evaluating  
 7464  $K_t^2$  possible mergers at each step, where  $K_t$  is the current number of clusters at step  $t$   
 7465 of the algorithm. Furthermore, computing the score for each merger involves a sum over  
 7466  $K_t^2$  clusters. The maximum number of clusters is  $K_0 = V$ , which occurs when every word  
 7467 is in its own cluster at the beginning of the algorithm. The time complexity is thus  $\mathcal{O}(V^5)$ .

7468 To avoid this complexity, practical implementations use a heuristic approximation  
 7469 called **exchange clustering**. The  $K$  most common words are placed in clusters of their  
 7470 own at the beginning of the process. We then consider the next most common word, and

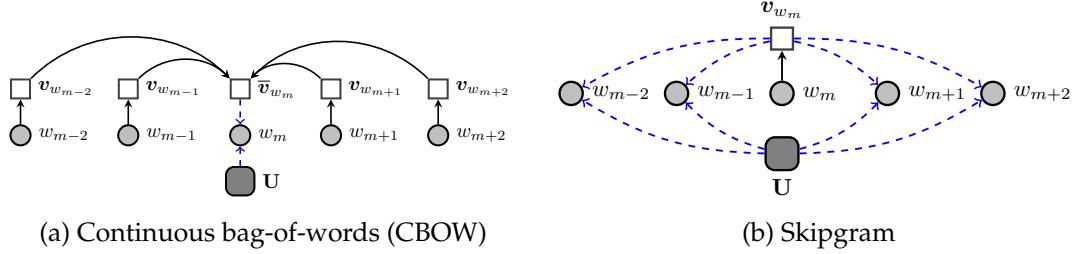


Figure 14.3: The CBOW and skipgram variants of WORD2VEC. The parameter  $\mathbf{U}$  is the matrix of word embeddings, and each  $\mathbf{v}_m$  is the context embedding for word  $w_m$ .

7471 merge it with one of the existing clusters. This continues until the entire vocabulary has  
 7472 been incorporated, at which point the  $K$  clusters are merged down to a single cluster,  
 7473 forming a tree. The algorithm never considers more than  $K + 1$  clusters at any step, and  
 7474 the complexity is  $\mathcal{O}(VK + V \log V)$ , with the second term representing the cost of sorting  
 7475 the words at the beginning of the algorithm.

## 7476 14.5 Neural word embeddings

7477 Neural word embeddings combine aspects of the previous two methods: like latent se-  
 7478 mantic analysis, they are a continuous vector representation; like Brown clusters, they are  
 7479 trained from a likelihood-based objective. Let the vector  $\mathbf{u}_i$  represent the  $K$ -dimensional  
 7480 **embedding** for word  $i$ , and let  $\mathbf{v}_j$  represent the  $K$ -dimensional embedding for context  
 7481  $j$ . The inner product  $\mathbf{u}_i \cdot \mathbf{v}_j$  represents the compatibility between word  $i$  and context  $j$ .  
 7482 By incorporating this inner product into an approximation to the log-likelihood of a cor-  
 7483 pus, it is possible to estimate both parameters by backpropagation. WORD2VEC (Mikolov  
 7484 et al., 2013) includes two such approximations: continuous bag-of-words (CBOW) and  
 7485 skipgrams.

### 7486 14.5.1 Continuous bag-of-words (CBOW)

7487 In recurrent neural network language models, each word  $w_m$  is conditioned on a recurrently-  
 7488 updated state vector, which is based on word representations going all the way back to the  
 7489 beginning of the text. The **continuous bag-of-words (CBOW)** model is a simplification:  
 7490 the local context is computed as an average of embeddings for words in the immediate  
 7491 neighborhood  $m - h, m - h + 1, \dots, m + h - 1, m + h$ ,

$$\bar{\mathbf{v}}_m = \frac{1}{2h} \sum_{n=1}^h \mathbf{v}_{w_{m+n}} + \mathbf{v}_{w_{m-n}}. \quad [14.14]$$

7492 Thus, CBOW is a bag-of-words model, because the order of the context words does not  
 7493 matter; it is continuous, because rather than conditioning on the words themselves, we  
 7494 condition on a continuous vector constructed from the word embeddings. The parameter  
 7495  $h$  determines the neighborhood size, which Mikolov et al. (2013) set to  $h = 4$ .

The CBOW model optimizes an approximation to the corpus log-likelihood,

$$\log p(\mathbf{w}) \approx \sum_{m=1}^M \log p(w_m | w_{m-h}, w_{m-h+1}, \dots, w_{m+h-1}, w_{m+h}) \quad [14.15]$$

$$= \sum_{m=1}^M \log \frac{\exp(\mathbf{u}_{w_m} \cdot \bar{\mathbf{v}}_m)}{\sum_{j=1}^V \exp(\mathbf{u}_j \cdot \bar{\mathbf{v}}_m)} \quad [14.16]$$

$$= \sum_{m=1}^M \mathbf{u}_{w_m} \cdot \bar{\mathbf{v}}_m - \log \sum_{j=1}^V \exp(\mathbf{u}_j \cdot \bar{\mathbf{v}}_m). \quad [14.17]$$

### 7496 14.5.2 Skipgrams

In the CBOW model, words are predicted from their context. In the **skipgram** model, the context is predicted from the word, yielding the objective:

$$\log p(\mathbf{w}) \approx \sum_{m=1}^M \sum_{n=1}^{h_m} \log p(w_{m-n} | w_m) + \log p(w_{m+n} | w_m) \quad [14.18]$$

$$= \sum_{m=1}^M \sum_{n=1}^{h_m} \log \frac{\exp(\mathbf{u}_{w_{m-n}} \cdot \mathbf{v}_{w_m})}{\sum_{j=1}^V \exp(\mathbf{u}_j \cdot \mathbf{v}_{w_m})} + \log \frac{\exp(\mathbf{u}_{w_{m+n}} \cdot \mathbf{v}_{w_m})}{\sum_{j=1}^V \exp(\mathbf{u}_j \cdot \mathbf{v}_{w_m})} \quad [14.19]$$

$$= \sum_{m=1}^M \sum_{n=1}^{h_m} \mathbf{u}_{w_{m-n}} \cdot \mathbf{v}_{w_m} + \mathbf{u}_{w_{m+n}} \cdot \mathbf{v}_{w_m} - 2 \log \sum_{j=1}^V \exp(\mathbf{u}_j \cdot \mathbf{v}_{w_m}). \quad [14.20]$$

7497 In the skipgram approximation, each word is generated multiple times; each time it is con-  
 7498 ditioned only on a single word. This makes it possible to avoid averaging the word vec-  
 7499 tors, as in the CBOW model. The local neighborhood size  $h_m$  is randomly sampled from  
 7500 a uniform categorical distribution over the range  $\{1, 2, \dots, h_{\max}\}$ ; Mikolov et al. (2013) set  
 7501  $h_{\max} = 10$ . Because the neighborhood grows outward with  $h$ , this approach has the effect  
 7502 of weighting near neighbors more than distant ones. Skipgram performs better on most  
 7503 evaluations than CBOW (see § 14.6 for details of how to evaluate word representations),  
 7504 but CBOW is faster to train (Mikolov et al., 2013).

### 7505 14.5.3 Computational complexity

7506 The WORD2VEC models can be viewed as an efficient alternative to recurrent neural net-  
 7507 work language models, which involve a recurrent state update whose time complexity

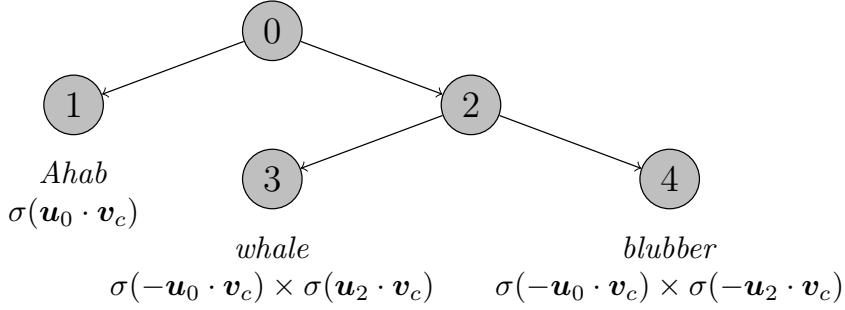


Figure 14.4: A fragment of a hierarchical softmax tree. The probability of each word is computed as a product of probabilities of local branching decisions in the tree.

is quadratic in the size of the recurrent state vector. CBOW and skipgram avoid this computation, and incur only a linear time complexity in the size of the word and context representations. However, all three models compute a normalized probability over word tokens; a naïve implementation of this probability requires summing over the entire vocabulary. The time complexity of this sum is  $\mathcal{O}(V \times K)$ , which dominates all other computational costs. There are two solutions: **hierarchical softmax**, a tree-based computation that reduces the cost to a logarithm of the size of the vocabulary; and **negative sampling**, an approximation that eliminates the dependence on vocabulary size. Both methods are also applicable to RNN language models.

#### 14.5.3.1 Hierarchical softmax

In Brown clustering, the vocabulary is organized into a binary tree. Mnih and Hinton (2008) show that the normalized probability over words in the vocabulary can be reparametrized as a probability over paths through such a tree. This **hierarchical softmax** probability is computed as a product of binary decisions over whether to move left or right through the tree, with each binary decision represented as a sigmoid function of the inner product between the context embedding  $\mathbf{v}_c$  and an output embedding associated with the node  $\mathbf{u}_n$ ,

$$\Pr(\text{left at } n \mid c) = \sigma(\mathbf{u}_n \cdot \mathbf{v}_c) \quad [14.21]$$

$$\Pr(\text{right at } n \mid c) = 1 - \sigma(\mathbf{u}_n \cdot \mathbf{v}_c) = \sigma(-\mathbf{u}_n \cdot \mathbf{v}_c), \quad [14.22]$$

where  $\sigma$  refers to the sigmoid function,  $\sigma(x) = \frac{1}{1+\exp(-x)}$ . The range of the sigmoid is the interval  $(0, 1)$ , and  $1 - \sigma(x) = \sigma(-x)$ .

As shown in Figure 14.4, the probability of generating each word is redefined as the product of the probabilities across its path. The sum of all such path probabilities is guaranteed to be one, for any context vector  $\mathbf{v}_c \in \mathbb{R}^K$ . In a balanced binary tree, the depth is

7523 logarithmic in the number of leaf nodes, and thus the number of multiplications is equal  
 7524 to  $\mathcal{O}(\log V)$ . The number of non-leaf nodes is equal to  $\mathcal{O}(2V - 1)$ , so the number of pa-  
 7525 rameters to be estimated increases by only a small multiple. The tree can be constructed  
 7526 using an incremental clustering procedure similar to hierarchical Brown clusters (Mnih  
 7527 and Hinton, 2008), or by using the Huffman (1952) encoding algorithm for lossless com-  
 7528 pression.

7529 **14.5.3.2 Negative sampling**

Likelihood-based methods are computationally intensive because each probability must be normalized over the vocabulary. These probabilities are based on scores for each word in each context, and it is possible to design an alternative objective that is based on these scores more directly: we seek word embeddings that maximize the score for the word that was really observed in each context, while minimizing the scores for a set of randomly selected **negative samples**:

$$\psi(i, j) = \log \sigma(\mathbf{u}_i \cdot \mathbf{v}_j) + \sum_{i' \in \mathcal{W}_{\text{neg}}} \log(1 - \sigma(\mathbf{u}_{i'} \cdot \mathbf{v}_j)), \quad [14.23]$$

7530 where  $\psi(i, j)$  is the score for word  $i$  in context  $j$ , and  $\mathcal{W}_{\text{neg}}$  is the set of negative samples.  
 7531 The objective is to maximize the sum over the corpus,  $\sum_{m=1}^M \psi(w_m, c_m)$ , where  $w_m$  is  
 7532 token  $m$  and  $c_m$  is the associated context.

7533 The set of negative samples  $\mathcal{W}_{\text{neg}}$  is obtained by sampling from a unigram language  
 7534 model. Mikolov et al. (2013) construct this unigram language model by exponentiating  
 7535 the empirical word probabilities, setting  $\hat{p}(i) \propto (\text{count}(i))^{\frac{3}{4}}$ . This has the effect of redi-  
 7536 tributing probability mass from common to rare words. The number of negative samples  
 7537 increases the time complexity of training by a constant factor. Mikolov et al. (2013) report  
 7538 that 5-20 negative samples works for small training sets, and that two to five samples  
 7539 suffice for larger corpora.

7540 **14.5.4 Word embeddings as matrix factorization**

7541 The negative sampling objective in Equation 14.23 can be justified as an efficient approx-  
 7542 imation to the log-likelihood, but it is also closely linked to the matrix factorization ob-  
 7543 jective employed in latent semantic analysis. For a matrix of word-context pairs in which  
 7544 all counts are non-zero, negative sampling is equivalent to factorization of the matrix  $M$ ,  
 7545 where  $M_{ij} = \text{PMI}(i, j) - \log k$ : each cell in the matrix is equal to the pointwise mutual  
 7546 information of the word and context, shifted by  $\log k$ , with  $k$  equal to the number of neg-  
 7547 ative samples (Levy and Goldberg, 2014). For word-context pairs that are not observed in  
 7548 the data, the pointwise mutual information is  $-\infty$ , but this can be addressed by consid-  
 7549 ering only PMI values that are greater than  $\log k$ , resulting in a matrix of **shifted positive**

7550 **pointwise mutual information,**

$$M_{ij} = \max(0, \text{PMI}(i, j) - \log k). \quad [14.24]$$

7551 Word embeddings are obtained by factoring this matrix with truncated singular value  
7552 decomposition.

GloVe (“global vectors”) are a closely related approach (Pennington et al., 2014), in which the matrix to be factored is constructed from log co-occurrence counts,  $M_{ij} = \log \text{count}(i, j)$ . The word embeddings are estimated by minimizing the sum of squares,

$$\begin{aligned} \min_{\mathbf{u}, \mathbf{v}, b, \tilde{b}} \quad & \sum_{j=1}^V \sum_{j \in C} f(M_{ij}) \left( \widehat{\log M_{ij}} - \log M_{ij} \right)^2 \\ \text{s.t.} \quad & \widehat{\log M_{ij}} = \mathbf{u}_i \cdot \mathbf{v}_j + b_i + \tilde{b}_j, \end{aligned} \quad [14.25]$$

7553 where  $b_i$  and  $\tilde{b}_j$  are offsets for word  $i$  and context  $j$ , which are estimated jointly with the  
7554 embeddings  $\mathbf{u}$  and  $\mathbf{v}$ . The weighting function  $f(M_{ij})$  is set to be zero at  $M_{ij} = 0$ , thus  
7555 avoiding the problem of taking the logarithm of zero counts; it saturates at  $M_{ij} = m_{\max}$ ,  
7556 thus avoiding the problem of overcounting common word-context pairs. This heuristic  
7557 turns out to be critical to the method’s performance.

7558 The time complexity of sparse matrix reconstruction is determined by the number of  
7559 non-zero word-context counts. Pennington et al. (2014) show that this number grows  
7560 sublinearly with the size of the dataset: roughly  $\mathcal{O}(N^{0.8})$  for typical English corpora. In  
7561 contrast, the time complexity of WORD2VEC is linear in the corpus size. Computing the co-  
7562 occurrence counts also requires linear time in the size of the corpus, but this operation can  
7563 easily be parallelized using MapReduce-style algorithms (Dean and Ghemawat, 2008).

## 7564 14.6 Evaluating word embeddings

7565 Distributed word representations can be evaluated in two main ways. **Intrinsic** evalua-  
7566 tions test whether the representations cohere with our intuitions about word meaning.  
7567 **Extrinsic** evaluations test whether they are useful for downstream tasks, such as sequence  
7568 labeling.

### 7569 14.6.1 Intrinsic evaluations

7570 A basic question for word embeddings is whether the similarity of words  $i$  and  $j$  is re-  
7571 flected in the similarity of the vectors  $\mathbf{u}_i$  and  $\mathbf{u}_j$ . **Cosine similarity** is typically used to  
7572 compare two word embeddings,

$$\cos(\mathbf{u}_i, \mathbf{u}_j) = \frac{\mathbf{u}_i \cdot \mathbf{u}_j}{\|\mathbf{u}_i\|_2 \times \|\mathbf{u}_j\|_2}. \quad [14.26]$$

word 1	word 2	similarity
<i>love</i>	<i>sex</i>	6.77
<i>stock</i>	<i>jaguar</i>	0.92
<i>money</i>	<i>cash</i>	9.15
<i>development</i>	<i>issue</i>	3.97
<i>lad</i>	<i>brother</i>	4.46

Table 14.4: Subset of the WS-353 (Finkelstein et al., 2002) dataset of word similarity ratings (examples from Faruqui et al. (2016)).

7573 For any embedding method, we can evaluate whether the cosine similarity of word em-  
 7574 beddings is correlated with human judgments of word similarity. The WS-353 dataset (Finkel-  
 7575 stein et al., 2002) includes similarity scores for 353 word pairs (Table 14.4). To test the  
 7576 accuracy of embeddings for rare and morphologically complex words, Luong et al. (2013)  
 7577 introduce a dataset of “rare words.” Outside of English, word similarity resources are  
 7578 limited, mainly consisting of translations of WS-353.

7579 Word analogies (e.g., *king:queen :: man:woman*) have also been used to evaluate word  
 7580 embeddings (Mikolov et al., 2013). In this evaluation, the system is provided with the first  
 7581 three parts of the analogy ( $i_1 : j_1 :: i_2 : ?$ ), and the final element is predicted by finding the  
 7582 word embedding most similar to  $\mathbf{u}_{i_1} - \mathbf{u}_{j_1} + \mathbf{u}_{i_2}$ . Another evaluation tests whether word  
 7583 embeddings are related to broad lexical semantic categories called **supersenses** (Caramita  
 7584 and Johnson, 2003): verbs of motion, nouns that describe animals, nouns that describe  
 7585 body parts, and so on. These supersenses are annotated for English synsets in Word-  
 7586 Net (Fellbaum, 2010). This evaluation is implemented in the `qvec` metric, which tests  
 7587 whether the matrix of supersenses can be reconstructed from the matrix of word embed-  
 7588 dings (Tsvetkov et al., 2015).

7589 Levy et al. (2015) compared several dense word representations for English — includ-  
 7590 ing latent semantic analysis, WORD2VEC, and GloVe — using six word similarity metrics  
 7591 and two analogy tasks. None of the embeddings outperformed the others on every task,  
 7592 but skipgrams were the most broadly competitive. Hyperparameter tuning played a key  
 7593 role: any method will perform badly if the wrong hyperparameters are used. Relevant  
 7594 hyperparameters include the embedding size, as well as algorithm-specific details such  
 7595 as the neighborhood size and the number of negative samples.

### 7596 14.6.2 Extrinsic evaluations

7597 Word representations contribute to downstream tasks like sequence labeling and docu-  
 7598 ment classification by enabling generalization across words. The use of distributed repre-  
 7599 sentations as features is a form of **semi-supervised learning**, in which performance on a

7600 supervised learning problem is augmented by learning distributed representations from  
 7601 unlabeled data (Miller et al., 2004; Koo et al., 2008; Turian et al., 2010). These **pre-trained**  
 7602 **word representations** can be used as features in a linear prediction model, or as the input  
 7603 layer in a neural network, such as a Bi-LSTM tagging model (§ 7.6). Word representations  
 7604 can be evaluated by the performance of the downstream systems that consume them:  
 7605 for example, GloVe embeddings are convincingly better than Latent Semantic Analysis  
 7606 as features in the downstream task of named entity recognition (Pennington et al., 2014).  
 7607 Unfortunately, extrinsic and intrinsic evaluations do not always point in the same direc-  
 7608 tion, and the best word representations for one downstream task may perform poorly on  
 7609 another task (Schnabel et al., 2015).

7610 When word representations are updated from labeled data in the downstream task,  
 7611 they are said to be **fine-tuned**. When labeled data is plentiful, pre-training may be un-  
 7612 necessary; when labeled data is scarce, fine-tuning may lead to overfitting. Various com-  
 7613 binations of pre-training and fine-tuning can be employed. Pre-trained embeddings can  
 7614 be used as initialization before fine-tuning, and this can substantially improve perfor-  
 7615 mance (Lample et al., 2016). Alternatively, both fine-tuned and pre-trained embeddings  
 7616 can be used as inputs in a single model (Kim, 2014).

7617 In semi-supervised scenarios, pretrained word embeddings can be replaced by “con-  
 7618 textualized” word representations (Peters et al., 2018). These contextualized represen-  
 7619 tations are set to the hidden states of a deep bi-directional LSTM, which is trained as a  
 7620 bi-directional language model, motivating the name **ELMo (embeddings from language**  
 7621 **models**). Given a supervised learning problem, the language model generates contextu-  
 7622 alized representations, which are then used as the base layer in a task-specific supervised  
 7623 neural network. This approach yields significant gains over pretrained word embeddings  
 7624 on several tasks, presumably because the contextualized embeddings use unlabeled data  
 7625 to learn how to integrate linguistic context into the base layer of the supervised neural  
 7626 network.

## 7627 14.7 Distributed representations beyond distributional statistics

7628 Distributional word representations can be estimated from huge unlabeled datasets, thereby  
 7629 covering many words that do not appear in labeled data: for example, GloVe embeddings  
 7630 are estimated from 800 billion tokens of web data,<sup>3</sup> while the largest labeled datasets for  
 7631 NLP tasks are on the order of millions of tokens. Nonetheless, even a dataset of hundreds  
 7632 of billions of tokens will not cover every word that may be encountered in the future.  
 7633 Furthermore, many words will appear only a few times, making their embeddings un-  
 7634 reliable. Many languages exceed English in morphological complexity, and thus have  
 7635 lower token-to-type ratios. When this problem is coupled with small training corpora, it

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<sup>3</sup><http://commoncrawl.org/>

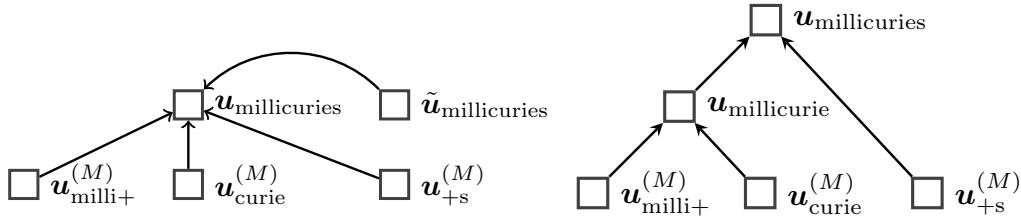


Figure 14.5: Two architectures for building word embeddings from subword units. On the left, morpheme embeddings  $u^{(m)}$  are combined by addition with the non-compositional word embedding  $\tilde{u}$  (Botha and Blunsom, 2014). On the right, morpheme embeddings are combined in a recursive neural network (Luong et al., 2013).

7636 becomes especially important to leverage other sources of information beyond distributional statistics.

#### 7638 14.7.1 Word-internal structure

7639 One solution is to incorporate word-internal structure into word embeddings. Purely  
7640 distributional approaches consider words as atomic units, but in fact, many words have  
7641 internal structure, so that their meaning can be **composed** from the representations of  
7642 sub-word units. Consider the following terms, all of which are missing from Google's  
7643 pre-trained WORD2VEC embeddings:<sup>4</sup>

7644 **millicuries** This word has **morphological** structure (see § 9.1.2 for more on morphology):  
7645 the prefix *milli-* indicates an amount, and the suffix *-s* indicates a plural. (A *millicurie*  
7646 is an unit of radioactivity.)

7647 **caesium** This word is a single morpheme, but the characters *-ium* are often associated  
7648 with chemical elements. (*Caesium* is the British spelling of a chemical element,  
7649 spelled *cesium* in American English.)

7650 **IAEA** This term is an acronym, as suggested by the use of capitalization. The prefix *I-* frequently  
7651 refers to international organizations, and the suffix *-A* often refers to agencies or associations. (*IAEA* is the International Atomic Energy Agency.)

7653 **Zhezhgan** This term is in title case, suggesting the name of a person or place, and the  
7654 character bigram *zh* indicates that it is likely a transliteration. (*Zhezhgan* is a mining  
7655 facility in Kazakhstan.)

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<sup>4</sup><https://code.google.com/archive/p/word2vec/>, accessed September 20, 2017

7656 How can word-internal structure be incorporated into word representations? One  
7657 approach is to construct word representations from embeddings of the characters or mor-  
7658 phemes. For example, if word  $i$  has morphological segments  $\mathcal{M}_i$ , then its embedding can  
7659 be constructed by addition (Botha and Blunsom, 2014),

$$\mathbf{u}_i = \tilde{\mathbf{u}}_i + \sum_{j \in \mathcal{M}_i} \mathbf{u}_j^{(M)}, \quad [14.27]$$

7660 where  $\mathbf{u}_m^{(M)}$  is a morpheme embedding and  $\tilde{\mathbf{u}}_i$  is a non-compositional embedding of the  
7661 whole word, which is an additional free parameter of the model (Figure 14.5, left side).  
7662 All embeddings are estimated from a **log-bilinear language model** (Mnih and Hinton,  
7663 2007), which is similar to the CBOW model (§ 14.5), but includes only contextual informa-  
7664 tion from preceding words. The morphological segments are obtained using an unsuper-  
7665 vised segmenter (Creutz and Lagus, 2007). For words that do not appear in the training  
7666 data, the embedding can be constructed directly from the morphemes, assuming that each  
7667 morpheme appears in some other word in the training data. The free parameter  $\tilde{\mathbf{u}}$  adds  
7668 flexibility: words with similar morphemes are encouraged to have similar embeddings,  
7669 but this parameter makes it possible for them to be different.

7670 Word-internal structure can be incorporated into word representations in various other  
7671 ways. Here are some of the main parameters.

7672 **Subword units.** Examples like *IAEA* and *Zhezghan* are not based on morphological com-  
7673 position, and a morphological segmenter is unlikely to identify meaningful sub-  
7674 word units for these terms. Rather than using morphemes for subword embeddings,  
7675 one can use characters (Santos and Zadrozny, 2014; Ling et al., 2015; Kim et al., 2016),  
7676 character  $n$ -grams (Wieting et al., 2016; Bojanowski et al., 2017), and **byte-pair en-**  
7677 **codings**, a compression technique which captures frequent substrings (Gage, 1994;  
7678 Sennrich et al., 2016).

7679 **Composition.** Combining the subword embeddings by addition does not differentiate  
7680 between orderings, nor does it identify any particular morpheme as the **root**. A  
7681 range of more flexible compositional models have been considered, including re-  
7682 currence (Ling et al., 2015), convolution (Santos and Zadrozny, 2014; Kim et al.,  
7683 2016), and **recursive neural networks** (Luong et al., 2013), in which representa-  
7684 tions of progressively larger units are constructed over a morphological parse, e.g.  
7685  $((milli+curie)+s)$ ,  $((in+flam)+able)$ ,  $(in+(vis+ible))$ . A recursive embedding model is  
7686 shown in the right panel of Figure 14.5.

7687 **Estimation.** Estimating subword embeddings from a full dataset is computationally ex-  
7688 pensive. An alternative approach is to train a subword model to match pre-trained  
7689 word embeddings (Cotterell et al., 2016; Pinter et al., 2017). To train such a model, it  
7690 is only necessary to iterate over the vocabulary, and the not the corpus.

7691 **14.7.2 Lexical semantic resources**

Resources such as WordNet provide another source of information about word meaning; if we know that *caesium* is a synonym of *cesium*, or that a *millicurie* is a type of *measurement unit*, then this should help to provide embeddings for the unknown words, and to smooth embeddings of rare words. One way to do this is to **retrofit** pre-trained word embeddings across a network of lexical semantic relationships (Faruqui et al., 2015) by minimizing the following objective,

$$\min_{\mathbf{U}} \sum_{j=1}^V \|\mathbf{u}_i - \hat{\mathbf{u}}_i\|_2 + \sum_{(i,j) \in \mathcal{L}} \beta_{ij} \|\mathbf{u}_i - \mathbf{u}_j\|_2, \quad [14.28]$$

7692 where  $\hat{\mathbf{u}}_i$  is the pretrained embedding of word  $i$ , and  $\mathcal{L} = \{(i,j)\}$  is a lexicon of word  
 7693 relations. The hyperparameter  $\beta_{ij}$  controls the importance of adjacent words having  
 7694 similar embeddings; Faruqui et al. (2015) set it to the inverse of the degree of word  $i$ ,  
 7695  $\beta_{ij} = |\{j : (i,j) \in \mathcal{L}\}|^{-1}$ . Retrofitting improves performance on a range of intrinsic evalua-  
 7696 tions, and gives small improvements on an extrinsic document classification task.

7697 **14.8 Distributed representations of multiword units**

7698 Can distributed representations extend to phrases, sentences, paragraphs, and beyond?  
 7699 Before exploring this possibility, recall the distinction between distributed and distri-  
 7700 butional representations. Neural embeddings such as WORD2VEC are both distributed  
 7701 (vector-based) and distributional (derived from counts of words in context). As we con-  
 7702 sider larger units of text, the counts decrease: in the limit, a multi-paragraph span of text  
 7703 would never appear twice, except by plagiarism. Thus, the meaning of a large span of  
 7704 text cannot be determined from distributional statistics alone; it must be computed com-  
 7705 positionally from smaller spans. But these considerations are orthogonal to the question  
 7706 of whether distributed representations — dense numerical vectors — are sufficiently ex-  
 7707 pressive to capture the meaning of phrases, sentences, and paragraphs.

7708 **14.8.1 Purely distributional methods**

7709 Some multiword phrases are non-compositional: the meaning of such phrases is not de-  
 7710 rived from the meaning of the individual words using typical compositional semantics.  
 7711 This includes proper nouns like *San Francisco* as well as idiomatic expressions like *kick*  
 7712 *the bucket* (Baldwin and Kim, 2010). For these cases, purely distributional approaches  
 7713 can work. A simple approach is to identify multiword units that appear together fre-  
 7714 quently, and then treat these units as words, learning embeddings using a technique such  
 7715 as WORD2VEC. The problem of identifying multiword units is sometimes called **colloca-**  
 7716 **tion extraction**, and can be approached using metrics such as pointwise mutual informa-  
 7717 tion: two-word units are extracted first, and then larger units are extracted. Mikolov et al.

7718 (2013) identify such units and then treat them as words when estimating skipgram em-  
7719 beddings, showing that the resulting embeddings perform reasonably on a task of solving  
7720 phrasal analogies, e.g. *New York : New York Times :: Baltimore : Baltimore Sun*.

### 7721 14.8.2 Distributional-compositional hybrids

7722 To move beyond short multiword phrases, composition is necessary. A simple but sur-  
7723 prisingly powerful approach is to represent a sentence with the average of its word em-  
7724 beddings (Mitchell and Lapata, 2010). This can be considered a hybrid of the distribu-  
7725 tional and compositional approaches to semantics: the word embeddings are computed  
7726 distributionally, and then the sentence representation is computed by composition.

7727 The WORD2VEC approach can be stretched considerably further, embedding entire  
7728 sentences using a model similar to skipgrams, in the “skip-thought” model of Kiros et al.  
7729 (2015). Each sentence is *encoded* into a vector using a recurrent neural network: the encod-  
7730 ing of sentence  $t$  is set to the RNN hidden state at its final token,  $h_{M_t}^{(t)}$ . This vector is then  
7731 a parameter in a *decoder* model that is used to generate the previous and subsequent sen-  
7732 tences: the decoder is another recurrent neural network, which takes the encoding of the  
7733 neighboring sentence as an additional parameter in its recurrent update. (This **encoder-**  
7734 **decoder model** is discussed at length in chapter 18.) The encoder and decoder are trained  
7735 simultaneously from a likelihood-based objective, and the trained encoder can be used to  
7736 compute a distributed representation of any sentence. Skip-thought can also be viewed  
7737 as a hybrid of distributional and compositional approaches: the vector representation of  
7738 each sentence is computed compositionally from the representations of the individual  
7739 words, but the training objective is distributional, based on sentence co-occurrence across  
7740 a corpus.

7741 **Autoencoders** are a variant of encoder-decoder models in which the decoder is trained  
7742 to produce the same text that was originally encoded, using only the distributed encod-  
7743 ing vector (Li et al., 2015). The encoding acts as a bottleneck, so that generalization is  
7744 necessary if the model is to successfully fit the training data. In **denoising autoencoders**,  
7745 the input is a corrupted version of the original sentence, and the auto-encoder must re-  
7746 construct the uncorrupted original (Vincent et al., 2010; Hill et al., 2016). By interpolating  
7747 between distributed representations of two sentences,  $\alpha \mathbf{u}_i + (1 - \alpha) \mathbf{u}_j$ , it is possible to gen-  
7748 erate sentences that combine aspects of the two inputs, as shown in Figure 14.6 (Bowman  
7749 et al., 2016).

7750 Autoencoders can also be applied to longer texts, such as paragraphs and documents.  
7751 This enables applications such as **question answering**, which can be performed by match-  
7752 ing the encoding of the question with encodings of candidate answers (Miao et al., 2016).

---

**this was the only way**  
 it was the only way  
 it was her turn to blink  
 it was hard to tell  
 it was time to move on  
 he had to do it again  
 they all looked at each other  
 they all turned to look back  
 they both turned to face him  
**they both turned and walked away**

---

Figure 14.6: By interpolating between the distributed representations of two sentences (in bold), it is possible to generate grammatical sentences that combine aspects of both (Bowman et al., 2016)

### 7753 14.8.3 Supervised compositional methods

7754 Given a supervision signal, such as a label describing the sentiment or meaning of a sen-  
 7755 tence, a wide range of compositional methods can be applied to compute a distributed  
 7756 representation that then predicts the label. The simplest is to average the embeddings  
 7757 of each word in the sentence, and pass this average through a feedforward neural net-  
 7758 work (Iyyer et al., 2015). Convolutional and recurrent neural networks go further, with  
 7759 the ability to effectively capturing multiword phenomena such as negation (Kalchbrenner  
 7760 et al., 2014; Kim, 2014; Li et al., 2015; Tang et al., 2015). Another approach is to incorpo-  
 7761 rate the syntactic structure of the sentence into a **recursive neural networks**, in which the  
 7762 representation for each syntactic constituent is computed from the representations of its  
 7763 children (Socher et al., 2012). However, in many cases, recurrent neural networks perform  
 7764 as well or better than recursive networks (Li et al., 2015).

7765 Whether convolutional, recurrent, or recursive, a key question is whether supervised  
 7766 sentence representations are task-specific, or whether a single supervised sentence repre-  
 7767 sentation model can yield useful performance on other tasks. Wieting et al. (2015) train a  
 7768 variety of sentence embedding models for the task of labeling pairs of sentences as **para-**  
 7769 **phrases**. They show that the resulting sentence embeddings give good performance for  
 7770 sentiment analysis. The **Stanford Natural Language Inference corpus** classifies sentence  
 7771 pairs as **entailments** (the truth of sentence  $i$  implies the truth of sentence  $j$ ), **contradictions**  
 7772 (the truth of sentence  $i$  implies the falsity of sentence  $j$ ), and neutral ( $i$  neither entails nor  
 7773 contradicts  $j$ ). Sentence embeddings trained on this dataset transfer to a wide range of  
 7774 classification tasks (Conneau et al., 2017).

#### 7775 14.8.4 Hybrid distributed-symbolic representations

7776 The power of distributed representations is in their generality: the distributed represen-  
7777 tation of a unit of text can serve as a summary of its meaning, and therefore as the input  
7778 for downstream tasks such as classification, matching, and retrieval. For example, dis-  
7779 tributed sentence representations can be used to recognize the paraphrase relationship  
7780 between closely related sentences like the following:

- 7781 (14.5) Donald thanked Vlad profusely.  
7782 (14.6) Donald conveyed to Vlad his profound appreciation.  
7783 (14.7) Vlad was showered with gratitude by Donald.

7784 Symbolic representations are relatively brittle to this sort of variation, but are better  
7785 suited to describe individual entities, the things that they do, and the things that are done  
7786 to them. In examples (14.5)-(14.7), we not only know that somebody thanked someone  
7787 else, but we can make a range of inferences about what has happened between the en-  
7788 tities named *Donald* and *Vlad*. Because distributed representations do not treat entities  
7789 symbolically, they lack the ability to reason about the roles played by entities across a sen-  
7790 tence or larger discourse.<sup>5</sup> A hybrid between distributed and symbolic representations  
7791 might give the best of both worlds: robustness to the many different ways of describing  
7792 the same event, plus the expressiveness to support inferences about entities and the roles  
7793 that they play.

7794 A “top-down” hybrid approach is to begin with logical semantics (of the sort de-  
7795 scribed in the previous two chapters), and but replace the predefined lexicon with a set  
7796 of distributional word clusters (Poon and Domingos, 2009; Lewis and Steedman, 2013). A  
7797 “bottom-up” approach is to add minimal symbolic structure to existing distributed repre-  
7798 sentations, such as vector representations for each entity (Ji and Eisenstein, 2015; Wiseman  
7799 et al., 2016). This has been shown to improve performance on two problems that we will  
7800 encounter in the following chapters: classification of **discourse relations** between adjac-  
7801 ent sentences (chapter 16; Ji and Eisenstein, 2015), and **coreference resolution** of entity  
7802 mentions (chapter 15; Wiseman et al., 2016; Ji et al., 2017). Research on hybrid seman-  
7803 tic representations is still in an early stage, and future representations may deviate more  
7804 boldly from existing symbolic and distributional approaches.

#### 7805 Additional resources

7806 Turney and Pantel (2010) survey a number of facets of vector word representations, fo-  
7807 cusing on matrix factorization methods. Schnabel et al. (2015) highlight problems with

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<sup>5</sup>At a 2014 workshop on semantic parsing, this critique of distributed representations was expressed by Ray Mooney — a leading researcher in computational semantics — in a now well-known quote, “you can’t cram the meaning of a whole sentence into a single vector!”

7808 similarity-based evaluations of word embeddings, and present a novel evaluation that  
 7809 controls for word frequency. Baroni et al. (2014) address linguistic issues that arise in  
 7810 attempts to combine distributed and compositional representations.

7811 In bilingual and multilingual distributed representations, embeddings are estimated  
 7812 for translation pairs or tuples, such as (*dog, perro, chien*). These embeddings can improve  
 7813 machine translation (Zou et al., 2013; Klementiev et al., 2012), transfer natural language  
 7814 processing models across languages (Täckström et al., 2012), and make monolingual word  
 7815 embeddings more accurate (Faruqui and Dyer, 2014). A typical approach is to learn a pro-  
 7816 jection that maximizes the correlation of the distributed representations of each element  
 7817 in a translation pair, which can be obtained from a bilingual dictionary. Distributed rep-  
 7818 resentations can also be linked to perceptual information, such as image features. Bruni  
 7819 et al. (2014) use textual descriptions of images to obtain visual contextual information for  
 7820 various words, which supplements traditional distributional context. Image features can  
 7821 also be inserted as contextual information in log bilinear language models (Kiros et al.,  
 7822 2014), making it possible to automatically generate text descriptions of images.

## 7823 Exercises

- 7824 1. Prove that the sum of probabilities of paths through a hierarchical softmax tree is  
 7825 equal to one.
- 7826 2. In skipgram word embeddings, the negative sampling objective can be written as,

$$\mathcal{L} = \sum_{i \in \mathcal{V}} \sum_{j \in \mathcal{C}} \text{count}(i, j) \psi(i, j), \quad [14.29]$$

7826 with  $\psi(i, j)$  is defined in Equation 14.23.

7827 Suppose we draw the negative samples from the empirical unigram distribution  
 7828  $\hat{p}(i) = p_{\text{unigram}}(i)$ . First, compute the expectation of  $\mathcal{L}$  with respect to this probability.

7829 Next, take the derivative of this expectation with respect to the score of a single word  
 7830 context pair  $\sigma(\mathbf{u}_i \cdot \mathbf{v}_j)$ , and solve for the pointwise mutual information  $\text{PMI}(i, j)$ . You  
 7831 should be able to show that at the optimum, the PMI is a simple function of  $\sigma(\mathbf{u}_i \cdot \mathbf{v}_j)$   
 7832 and the number of negative samples.

- 7833 3. \* In Brown clustering, prove that the cluster merge that maximizes the average mu-  
 7834 tual information (Equation 14.13) also maximizes the log-likelihood objective (Equa-  
 7835 tion 14.12).
- 7836 4. A simple way to compute a distributed phrase representation is to add up the dis-  
 7837 tributed representations of the words in the phrase. Consider a sentiment analysis  
 7838 model in which the predicted sentiment is,  $\psi(\mathbf{w}) = \boldsymbol{\theta} \cdot (\sum_{m=1}^M \mathbf{x}_m)$ , where  $\mathbf{x}_m$  is

the vector representation of word  $m$ . Prove that in such a model, the following two inequalities cannot both hold:

$$\psi(\text{good}) > \psi(\text{not good}) \quad [14.30]$$

$$\psi(\text{bad}) < \psi(\text{not bad}). \quad [14.31]$$

Then construct a similar example pair for the case in which phrase representations are the *average* of the word representations.

5. Now let's consider a slight modification to the prediction model in the previous problem:

$$\psi(\mathbf{w}) = \boldsymbol{\theta} \cdot \text{ReLU}\left(\sum_{m=1}^M \mathbf{x}_m\right) \quad [14.32]$$

Show that in this case, it *is* possible to achieve the inequalities above. Your solution should provide the weights  $\boldsymbol{\theta}$  and the embeddings  $\mathbf{x}_{\text{good}}$ ,  $\mathbf{x}_{\text{bad}}$ , and  $\mathbf{x}_{\text{not}}$ .

- For the next two problems, download a set of pre-trained word embeddings, such as the WORD2VEC or polyglot embeddings.

6. Use cosine similarity to find the most similar words to: *dog*, *whale*, *before*, *however*, *fabricate*.

7. Use vector addition and subtraction to compute target vectors for the analogies below. After computing each target vector, find the top three candidates by cosine similarity.

- *dog:puppy :: cat: ?*
- *speak:speaker :: sing: ?*
- *France:French :: England: ?*
- *France:wine :: England: ?*

- The remaining problems will require you to build a classifier and test its properties. Pick a multi-class text classification dataset, such as RCV1<sup>6</sup>). Divide your data into training (60%), development (20%), and test sets (20%), if no such division already exists.

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<sup>6</sup>[http://www.ai.mit.edu/projects/jmlr/papers/volume5/lewis04a/lyrl2004\\_rcv1v2\\_README.htm](http://www.ai.mit.edu/projects/jmlr/papers/volume5/lewis04a/lyrl2004_rcv1v2_README.htm)

- 7854     8. Train a convolutional neural network, with inputs set to pre-trained word embed-  
7855         dings from the previous problem. Use a special, fine-tuned embedding for out-of-  
7856         vocabulary words. Train until performance on the development set does not im-  
7857         prove. You can also use the development set to tune the model architecture, such  
7858         as the convolution width and depth. Report *F-MEASURE* and accuracy, as well as  
7859         training time.
- 7860     9. Now modify your model from the previous problem to fine-tune the word embed-  
7861         dings. Report *F-MEASURE*, accuracy, and training time.
- 7862     10. Try a simpler approach, in which word embeddings in the document are averaged,  
7863         and then this average is passed through a feed-forward neural network. Again, use  
7864         the development data to tune the model architecture. How close is the accuracy to  
7865         the convolutional networks from the previous problems?

7866 

## Chapter 15

7867 

# Reference Resolution

7868 References are one of the most noticeable forms of linguistic ambiguity, afflicting not just  
7869 automated natural language processing systems, but also fluent human readers. Warnings  
7870 to avoid “ambiguous pronouns” are ubiquitous in manuals and tutorials on writing  
7871 style. But referential ambiguity is not limited to pronouns, as shown in the text in Fig-  
7872 ure 15.1. Each of the bracketed substrings refers to an entity that is introduced earlier  
7873 in the passage. These references include the pronouns *he* and *his*, but also the shortened  
7874 name *Cook*, and **nominals** such as *the firm* and *the firm’s biggest growth market*.

7875 **Reference resolution** subsumes several subtasks. This chapter will focus on **corefer-  
7876 ence resolution**, which is the task of grouping spans of text that refer to a single underly-  
7877 ing entity, or, in some cases, a single event: for example, the spans *Tim Cook*, *he*, and *Cook*  
7878 are all **coreferent**. These individual spans are called **mentions**, because they mention an  
7879 entity; the entity is sometimes called the **referent**. Each mention has a set of **antecedents**,  
7880 which are preceding mentions that are coreferent; for the first mention of an entity, the an-  
7881 tecedent set is empty. The task of **pronominal anaphora resolution** requires identifying  
7882 only the antecedents of pronouns. In **entity linking**, references are resolved not to other  
7883 spans of text, but to entities in a knowledge base. This task is discussed in chapter 17.

7884 Coreference resolution is a challenging problem for several reasons. Resolving differ-  
7885 ent types of **referring expressions** requires different types of reasoning: the features and  
7886 methods that are useful for resolving pronouns are different from those that are useful  
7887 to resolve names and nominals. Coreference resolution involves not only linguistic rea-  
7888 soning, but also world knowledge and pragmatics: you may not have known that China  
7889 was Apple’s biggest growth market, but it is likely that you effortlessly resolved this ref-  
7890 erence while reading the passage in Figure 15.1.<sup>1</sup> A further challenge is that coreference

---

<sup>1</sup>This interpretation is based in part on the assumption that a **cooperative** author would not use the expression *the firm’s biggest growth market* to refer to an entity not yet mentioned in the article (Grice, 1975). **Pragmatics** is the discipline of linguistics concerned with the formalization of such assumptions (Huang,

- (15.1) *[[Apple Inc] Chief Executive Tim Cook] has jetted into [China] for talks with government officials as [he] seeks to clear up a pile of problems in [[the firm] 's biggest growth market] ... [Cook] is on [his] first trip to [the country] since taking over...*

Figure 15.1: Running example (Yee and Jones, 2012). Coreferring entity mentions are underlined and bracketed.

7891 resolution decisions are often entangled: each mention adds information about the entity,  
 7892 which affects other coreference decisions. This means that coreference resolution must  
 7893 be addressed as a structure prediction problem. But as we will see, there is no dynamic  
 7894 program that allows the space of coreference decisions to be searched efficiently.

## 7895 15.1 Forms of referring expressions

7896 There are three main forms of referring expressions — pronouns, names, and nominals.

### 7897 15.1.1 Pronouns

7898 Pronouns are a closed class of words that are used for references. A natural way to think  
 7899 about pronoun resolution is SMASH (Kehler, 2007):

- 7900 • Search for candidate antecedents;  
 7901 • Match against hard agreement constraints;  
 7902 • And Select using Heuristics, which are “soft” constraints such as recency, syntactic  
 7903 prominence, and parallelism.

#### 7904 15.1.1.1 Search

7905 In the search step, candidate antecedents are identified from the preceding text or speech.<sup>2</sup>  
 7906 Any noun phrase can be a candidate antecedent, and pronoun resolution usually requires

2015).

<sup>2</sup>Pronouns whose referents come later are known as **cataphora**, as in this example from Márquez (1970):

- (15.1) Many years later, as [he] faced the firing squad, [Colonel Aureliano Buendía] was to remember that distant afternoon when his father took him to discover ice.

7907 parsing the text to identify all such noun phrases.<sup>3</sup> Filtering heuristics can help to prune  
 7908 the search space to noun phrases that are likely to be coreferent (Lee et al., 2013; Durrett  
 7909 and Klein, 2013). In nested noun phrases, mentions are generally considered to be the  
 7910 largest unit with a given head word: thus, *Apple Inc. Chief Executive Tim Cook* would be  
 7911 included as a mention, but *Tim Cook* would not, since they share the same head word,  
 7912 *Cook*.

7913 **15.1.1.2 Matching constraints for pronouns**

7914 References and their antecedents must agree on semantic features such as number, person,  
 7915 gender, and animacy. Consider the pronoun *he* in this passage from the running example:

7916 (15.2) Tim Cook has jetted in for talks with officials as [he] seeks to clear up a pile of  
 7917 problems...

7918 The pronoun and possible antecedents have the following features:

- 7919 • *he*: singular, masculine, animate, third person
- 7920 • *officials*: plural, animate, third person
- 7921 • *talks*: plural, inanimate, third person
- 7922 • *Tim Cook*: singular, masculine, animate, third person

7923 The SMASH method searches backwards from *he*, discarding *officials* and *talks* because they  
 7924 do not satisfy the agreements constraints.

7925 Another source of constraints comes from syntax — specifically, from the phrase struc-  
 7926 ture trees discussed in chapter 10. Consider a parse tree in which both *x* and *y* are phrasal  
 7927 constituents. The constituent *x* **c-commands** the constituent *y* iff the first branching node  
 7928 above *x* also dominates *y*. For example, in Figure 15.2a, *Abigail* c-commands *her*, because  
 7929 the first branching node above *Abigail*, *S*, also dominates *her*. Now, if *x* c-commands *y*,  
 7930 **government and binding theory** (Chomsky, 1982) states that *y* can refer to *x* only if it is  
 7931 a **reflexive pronoun** (e.g., *herself*). Furthermore, if *y* is a reflexive pronoun, then its an-  
 7932 tecedent must c-command it. Thus, in Figure 15.2a, *her* cannot refer to *Abigail*; conversely,  
 7933 if we replace *her* with *herself*, then the reflexive pronoun *must* refer to *Abigail*, since this is  
 7934 the only candidate antecedent that c-commands it.

7935 Now consider the example shown in Figure 15.2b. Here, *Abigail* does not c-command  
 7936 *her*, but *Abigail's mom* does. Thus, *her* can refer to *Abigail* — and we cannot use reflexive

---

<sup>3</sup>In the OntoNotes coreference annotations, verbs can also be antecedents, if they are later referenced by nominals (Pradhan et al., 2011):

(15.1) Sales of passenger cars [grew] 22%. [The strong growth] followed year-to-year increases.

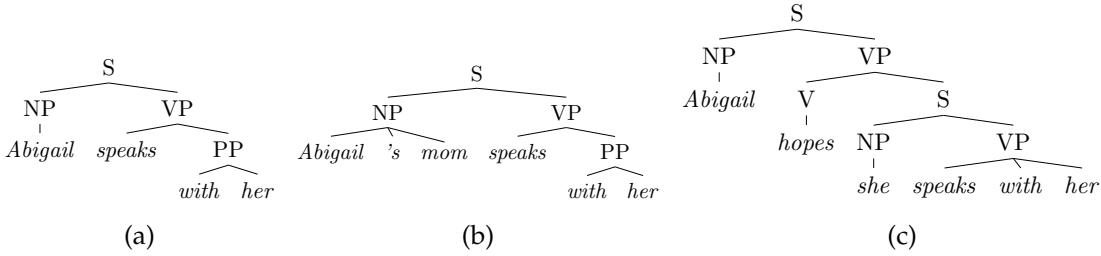


Figure 15.2: In (a), *Abigail* c-commands *her*; in (b), *Abigail* does not c-command *her*, but *Abigail's mom* does; in (c), the scope of *Abigail* is limited by the S non-terminal, so that *she* or *her* can bind to *Abigail*, but not both.

7937 *herself* in this context, unless we are talking about *Abigail*'s mom. However, *her* does not  
 7938 have to refer to *Abigail*. Finally, Figure 15.2c shows how these constraints are limited.  
 7939 In this case, the pronoun *she* can refer to *Abigail*, because the S non-terminal puts *Abigail*  
 7940 outside the domain of *she*. Similarly, *her* can also refer to *Abigail*. But *she* and *her* cannot be  
 7941 coreferent, because *she* c-commands *her*.

#### 7942 15.1.1.3 Heuristics

7943 After applying constraints, heuristics are applied to select among the remaining candidates.  
 7944 Recency is a particularly strong heuristic. All things equal, readers will prefer  
 7945 the more recent referent for a given pronoun, particularly when comparing referents that  
 7946 occur in different sentences. Jurafsky and Martin (2009) offer the following example:

- 7947 (15.3) The doctor found an old map in the captain's chest. Jim found an even older map  
 7948 hidden on the shelf. [It] described an island.

7949 Readers are expected to prefer the older map as the referent for the pronoun *it*.

7950 However, subjects are often preferred over objects, and this can contradict the preference  
 7951 for recency when two candidate referents are in the same sentence. For example,

- 7952 (15.4) Asha loaned Mei a book on Spanish. [She] is always trying to help people.

7953 Here, we may prefer to link *she* to *Asha* rather than *Mei*, because of *Asha*'s position in the  
 7954 subject role of the preceding sentence. (Arguably, this preference would not be strong  
 7955 enough to select *Asha* if the second sentence were *She is visiting Valencia next month*.)

7956 A third heuristic is parallelism:

- 7957 (15.5) Asha loaned Mei a book on Spanish. Olya loaned [her] a book on Portuguese.

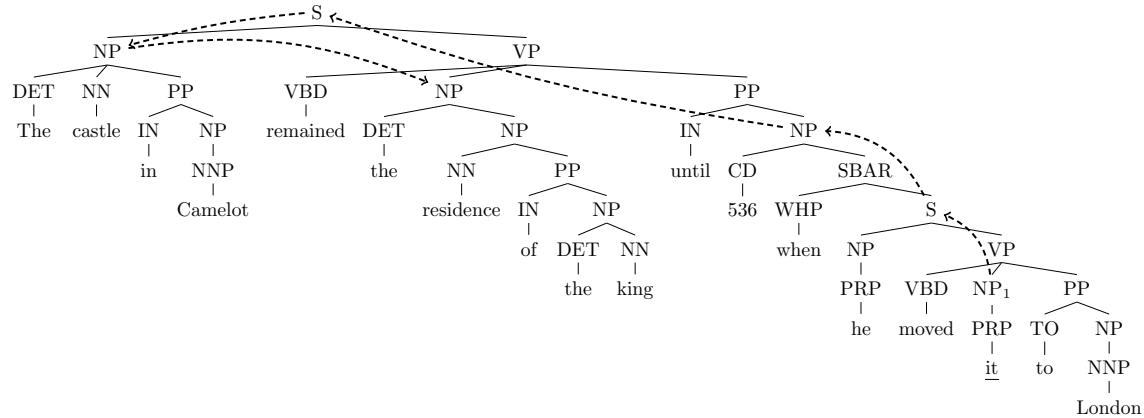


Figure 15.3: Left-to-right breadth-first tree traversal (Hobbs, 1978), indicating that the search for an antecedent for *it* ( $NP_1$ ) would proceed in the following order: 536; *the castle in Camelot*; *the residence of the king*; *Camelot*; *the king*. Hobbs (1978) proposes semantic constraints to eliminate 536 and *the castle in Camelot* as candidates, since they are unlikely to be the direct object of the verb *move*.

7958 Here *Mei* is preferred as the referent for *her*, contradicting the preference for the subject  
 7959 *Asha* in the preceding sentence.

7960 The recency and subject role heuristics can be unified by traversing the document in  
 7961 a syntax-driven fashion (Hobbs, 1978): each preceding sentence is traversed breadth-first,  
 7962 left-to-right (Figure 15.3). This heuristic successfully handles (15.4): *Asha* is preferred as  
 7963 the referent for *she* because the subject NP is visited first. It also handles (15.3): the older  
 7964 map is preferred as the referent for *it* because the more recent sentence is visited first. (An  
 7965 alternative unification of recency and syntax is proposed by **centering theory** (Grosz et al.,  
 7966 1995), which is discussed in detail in chapter 16.)

7967 In early work on reference resolution, the number of heuristics was small enough that  
 7968 a set of numerical weights could be set by hand (Lappin and Leass, 1994). More recent  
 7969 work uses machine learning to quantify the importance of each of these factors. However,  
 7970 pronoun resolution cannot be completely solved by constraints and heuristics alone. This  
 7971 is shown by the classic example pair (Winograd, 1972):

7972 (15.6) The [city council] denied [the protesters] a permit because [they] advocated / feared  
 7973 violence.

7974 Without reasoning about the motivations of the city council and protesters, it is unlikely  
 7975 that any system could correctly resolve both versions of this example.

7976 **15.1.1.4 Non-referential pronouns**

7977 While pronouns are generally used for reference, they need not refer to entities. The fol-  
 7978 lowing examples show how pronouns can refer to propositions, events, and speech acts.

- 7979 (15.7) They told me that I was too ugly for show business, but I didn't believe [it].  
 7980 (15.8) Asha saw Babak get angry, and I saw [it] too.  
 7981 (15.9) Asha said she worked in security. I suppose [that]'s one way to put it.

7982 These forms of reference are generally not annotated in large-scale coreference resolution  
 7983 datasets such as OntoNotes (Pradhan et al., 2011).

7984 Pronouns may also have **generic referents**:

- 7985 (15.10) A poor carpenter blames [her] tools.  
 7986 (15.11) On the moon, [you] have to carry [your] own oxygen.  
 7987 (15.12) Every farmer who owns a donkey beats [it]. (Geach, 1962)

7988 In the OntoNotes dataset, coreference is not annotated for generic referents, even in cases  
 7989 like these examples, in which the same generic entity is mentioned multiple times.

7990 Some pronouns do not refer to anything at all:

- 7991 (15.13) *[It]'s raining.*  
 [Il] pleut. (Fr)  
 7992 (15.14) [It] 's money that she's really after.  
 7993 (15.15) [It] is too bad that we have to work so hard.

7994 How can we automatically distinguish these usages of *it* from referential pronouns?  
 7995 Consider the the difference between the following two examples (Bergsma et al., 2008):

- 7996 (15.16) You can make [it] in advance.  
 7997 (15.17) You can make [it] in showbiz.

7998 In the second example, the pronoun *it* is non-referential. One way to see this is by substi-  
 7999 tuting another pronoun, like *them*, into these examples:

- 8000 (15.18) You can make [them] in advance.  
 8001 (15.19) ? You can make [them] in showbiz.

8002 The questionable grammaticality of the second example suggests that *it* is not referential.  
 8003 Bergsma et al. (2008) operationalize this idea by comparing distributional statistics for the

8004 *n*-grams around the word *it*, testing how often other pronouns or nouns appear in the  
8005 same context. In cases where nouns and other pronouns are infrequent, the *it* is unlikely  
8006 to be referential.

8007 **15.1.2 Proper Nouns**

8008 If a proper noun is used as a referring expression, it often corefers with another proper  
8009 noun, so that the coreference problem is simply to determine whether the two names  
8010 match. Subsequent proper noun references often use a shortened form, as in the running  
8011 example (Figure 15.1):

8012 (15.20) Apple Inc Chief Executive [Tim Cook] has jetted into China ... [Cook] is on his  
8013 first business trip to the country ...

8014 A typical solution for proper noun coreference is to match the syntactic **head words**  
8015 of the reference with the referent. In § 10.5.2, we saw that the head word of a phrase can  
8016 be identified by applying head percolation rules to the phrasal parse tree; alternatively,  
8017 the head can be identified as the root of the dependency subtree covering the name. For  
8018 sequences of proper nouns, the head word will be the final token.

8019 There are a number of caveats to the practice of matching head words of proper nouns.

- 8020 • In the European tradition, family names tend to be more specific than given names,  
8021 and family names usually come last. However, other traditions have other practices:  
8022 for example, in Chinese names, the family name typically comes first; in Japanese,  
8023 honorifics come after the name, as in *Nobu-San* (*Mr. Nobu*).
- 8024 • In organization names, the head word is often not the most informative, as in *Georgia*  
8025 *Tech* and *Virginia Tech*. Similarly, *Lebanon* does not refer to the same entity as *Southern Lebanon*, necessitating special rules for the specific case of geographical modi-  
8026 fiers (Lee et al., 2011).
- 8027 • Proper nouns can be nested, as in [*the CEO of [Microsoft]*], resulting in head word  
8028 match without coreference.

8030 Despite these difficulties, proper nouns are the easiest category of references to re-  
8031 solve (Stoyanov et al., 2009). In machine learning systems, one solution is to include a  
8032 range of matching features, including exact match, head match, and string inclusion. In  
8033 addition to matching features, competitive systems (e.g., Bengtson and Roth, 2008) in-  
8034 clude large lists, or **gazetteers**, of acronyms (e.g., *the National Basketball Association/NBA*),  
8035 demonyms (e.g., *the Israelis/Israel*), and other aliases (e.g., *the Georgia Institute of Technol-*  
8036 *ogy/Georgia Tech*).

8037 **15.1.3 Nominals**

8038 In coreference resolution, noun phrases that are neither pronouns nor proper nouns are  
 8039 referred to as **nominals**. In the running example (Figure 15.1), nominal references include:  
 8040 *the firm (Apple Inc); the firm's biggest growth market (China); and the country (China)*.

8041 Nominals are especially difficult to resolve (Denis and Baldridge, 2007; Durrett and  
 8042 Klein, 2013), and the examples above suggest why this may be the case: world knowledge  
 8043 is required to identify *Apple Inc* as a *firm*, and *China* as a *growth market*. Other difficult  
 8044 examples include the use of colloquial expressions, such as coreference between *Clinton*  
 8045 *campaign officials* and *the Clinton camp* (Soon et al., 2001).

8046 **15.2 Algorithms for coreference resolution**

The ground truth training data for coreference resolution is a set of mention sets, where all mentions within each set refer to a single entity.<sup>4</sup> In the running example from Figure 15.1, the ground truth coreference annotation is:

$$c_1 = \{ \text{Apple Inc}_{1:2}, \text{the firm}_{27:28} \} \quad [15.1]$$

$$c_2 = \{ \text{Apple Inc Chief Executive Tim Cook}_{1:6}, \text{he}_{17}, \text{Cook}_{33}, \text{his}_{36} \} \quad [15.2]$$

$$c_3 = \{ \text{China}_{10}, \text{the firm's biggest growth market}_{27:32}, \text{the country}_{40:41} \} \quad [15.3]$$

8047 Each row specifies the token spans that mention an entity. (“Singleton” entities, which are  
 8048 mentioned only once (e.g., *talks, government officials*), are excluded from the annotations.)  
 8049 Equivalently, if given a set of  $M$  mentions,  $\{m_i\}_{i=1}^M$ , each mention  $i$  can be assigned to a  
 8050 cluster  $z_i$ , where  $z_i = z_j$  if  $i$  and  $j$  are coreferent. The cluster assignments  $z$  are invariant  
 8051 under permutation. The unique clustering associated with the assignment  $z$  is written  
 8052  $c(z)$ .

8053 Coreference resolution can thus be viewed as a structure prediction problem, involving  
 8054 two subtasks: identifying which spans of text mention entities, and then clustering  
 8055 those spans.

8056 **Mention identification** The task of identifying mention spans for coreference resolution  
 8057 is often performed by applying a set of heuristics to the phrase structure parse of each  
 8058 sentence. A typical approach is to start with all noun phrases and named entities, and  
 8059 then apply filtering rules to remove nested noun phrases with the same head (e.g., [*Apple*  
 8060 *CEO [Tim Cook]*]), numeric entities (e.g., [*100 miles*], [*97%*]), non-referential *it*, etc (Lee

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<sup>4</sup>In many annotations, the term **markable** is used to refer to spans of text that can *potentially* mention an entity. The set of markables includes non-referential pronouns, which does not mention any entity. Part of the job of the coreference system is to avoid incorrectly linking these non-referential markables to any mention chains.

et al., 2013; Durrett and Klein, 2013). In general, these deterministic approaches err in favor of recall, since the mention clustering component can choose to ignore false positive mentions, but cannot recover from false negatives. An alternative is to consider all spans (up to some finite length) as candidate mentions, performing mention identification and clustering jointly (Daumé III and Marcu, 2005; Lee et al., 2017).

**Mention clustering** The subtask of mention clustering will be the focus of the remainder of this chapter. There are two main classes of models. In *mention-based models*, the scoring function for a coreference clustering decomposes over pairs of mentions. These pairwise decisions are then aggregated, using a clustering heuristic. Mention-based coreference clustering can be treated as a fairly direct application of supervised classification or ranking. However, the mention-pair locality assumption can result in incoherent clusters, like  $\{\text{Hillary Clinton} \leftarrow \text{Clinton} \leftarrow \text{Mr Clinton}\}$ , in which the pairwise links score well, but the overall result is unsatisfactory. *Entity-based models* address this issue by scoring entities holistically. This can make inference more difficult, since the number of possible entity groupings is exponential in the number of mentions.

### 15.2.1 Mention-pair models

In the **mention-pair model**, a binary label  $y_{i,j} \in \{0, 1\}$  is assigned to each pair of mentions  $(i, j)$ , where  $i < j$ . If  $i$  and  $j$  corefer ( $z_i = z_j$ ), then  $y_{i,j} = 1$ ; otherwise,  $y_{i,j} = 0$ . The mention *he* in Figure 15.1 is preceded by five other mentions: (1) *Apple Inc*; (2) *Apple Inc Chief Executive Tim Cook*; (3) *China*; (4) *talks*; (5) *government officials*. The correct mention pair labeling is  $y_{2,6} = 1$  and  $y_{i \neq 2,6} = 0$  for all other  $i$ . If a mention  $j$  introduces a new entity, such as mention 3 in the example, then  $y_{i,j} = 0$  for all  $i$ . The same is true for “mentions” that do not refer to any entity, such as non-referential pronouns. If mention  $j$  refers to an entity that has been mentioned more than once, then  $y_{i,j} = 1$  for all  $i < j$  that mention the referent.

By transforming coreference into a set of binary labeling problems, the mention-pair model makes it possible to apply an off-the-shelf binary classifier (Soon et al., 2001). This classifier is applied to each mention  $j$  independently, searching backwards from  $j$  until finding an antecedent  $i$  which corefers with  $j$  with high confidence. After identifying a single **antecedent**, the remaining mention pair labels can be computed by transitivity: if  $y_{i,j} = 1$  and  $y_{j,k} = 1$ , then  $y_{i,k} = 1$ .

Since the ground truth annotations give entity chains  $c$  but not individual mention-pair labels  $y$ , an additional heuristic must be employed to convert the labeled data into training examples for classification. A typical approach is to generate at most one positive labeled instance  $y_{a_j,j} = 1$  for mention  $j$ , where  $a_j$  is the index of the most recent antecedent,  $a_j = \max\{i : i < j \wedge z_i = z_j\}$ . Negative labeled instances are generated for all for all  $i \in \{a_j + 1, \dots, j\}$ . In the running example, the most recent antecedent of the

8098 pronoun *he* is  $a_6 = 2$ , so the training data would be  $y_{2,6} = 1$  and  $y_{3,6} = y_{4,6} = y_{5,6} = 0$ .  
 8099 The variable  $y_{1,6}$  is not part of the training data, because the first mention appears before  
 8100 the true antecedent  $a_6 = 2$ .

8101 **15.2.2 Mention-ranking models**

In **mention ranking** (Denis and Baldridge, 2007), the classifier learns to identify a single antecedent  $a_i \in \{\epsilon, 1, 2, \dots, i-1\}$  for each referring expression  $i$ ,

$$\hat{a}_i = \operatorname{argmax}_{a \in \{\epsilon, 1, 2, \dots, i-1\}} \psi_M(a, i), \quad [15.4]$$

8102 where  $\psi_M(a, i)$  is a score for the mention pair  $(a, i)$ . If  $a = \epsilon$ , then mention  $i$  does not refer  
 8103 to any previously-introduced entity — it is not **anaphoric**. Mention-ranking is similar to  
 8104 the mention-pair model, but all candidates are considered simultaneously, and at most  
 8105 a single antecedent is selected. The mention-ranking model explicitly accounts for the  
 8106 possibility that mention  $i$  is not anaphoric, through the score  $\psi_M(\epsilon, i)$ . The determination  
 8107 of anaphoricity can be made by a special classifier in a preprocessing step, so that non- $\epsilon$   
 8108 antecedents are identified only for spans that are determined to be anaphoric (Denis and  
 8109 Baldridge, 2008).

8110 As a learning problem, ranking can be trained using the same objectives as in dis-  
 8111 criminative classification. For each mention  $i$ , we can define a gold antecedent  $a_i^*$ , and an  
 8112 associated loss, such as the hinge loss,  $\ell_i = (1 - \psi_M(a_i^*, i) + \psi_M(\hat{a}, i))_+$  or the negative  
 8113 log-likelihood,  $\ell_i = -\log p(a_i^* | i; \theta)$ . (For more on learning to rank, see § 17.1.1.) But as  
 8114 with the mention-pair model, there is a mismatch between the labeled data, which comes  
 8115 in the form of mention sets, and the desired supervision, which would indicate the spe-  
 8116 cific antecedent of each mention. The antecedent variables  $\{a_i\}_{i=1}^M$  relate to the mention  
 8117 sets in a many-to-one mapping: each set of antecedents induces a single clustering, but a  
 8118 clustering can correspond to many different settings of antecedent variables.

A heuristic solution is to set  $a_i^* = \max\{j : j < i \wedge z_j = z_i\}$ , the most recent mention in  
 the same cluster as  $i$ . But the most recent mention may not be the most informative: in the  
 running example, the most recent antecedent of the mention *Cook* is the pronoun *he*, but  
 a more useful antecedent is the earlier mention *Apple Inc Chief Executive Tim Cook*. Rather  
 than selecting a specific antecedent to train on, the antecedent can be treated as a latent  
 variable, in the manner of the **latent variable perceptron** from § 12.4.2 (Fernandes et al.,

2014):

$$\hat{\mathbf{a}} = \operatorname{argmax}_{\mathbf{a}} \sum_{i=1}^M \psi_M(a_i, i) \quad [15.5]$$

$$\mathbf{a}^* = \operatorname{argmax}_{\mathbf{a} \in \mathcal{A}(c)} \sum_{i=1}^M \psi_M(a_i, i) \quad [15.6]$$

$$\boldsymbol{\theta} \leftarrow \boldsymbol{\theta} + \sum_{i=1}^M \frac{\partial L}{\partial \boldsymbol{\theta}} \psi_M(a_i^*, i) - \sum_{i=1}^M \frac{\partial L}{\partial \boldsymbol{\theta}} \psi_M(\hat{a}_i, i) \quad [15.7]$$

where  $\mathcal{A}(c)$  is the set of antecedent structures that is compatible with the ground truth coreference clustering  $c$ . Another alternative is to sum over all the conditional probabilities of antecedent structures that are compatible with the ground truth clustering (Durrett and Klein, 2013; Lee et al., 2017). For the set of mention  $\mathbf{m}$ , we compute the following probabilities:

$$p(c | \mathbf{m}) = \sum_{\mathbf{a} \in \mathcal{A}(c)} p(\mathbf{a} | \mathbf{m}) = \sum_{\mathbf{a} \in \mathcal{A}(c)} \prod_{i=1}^M p(a_i | i, \mathbf{m}) \quad [15.8]$$

$$p(a_i | i, \mathbf{m}) = \frac{\exp(\psi_M(a_i, i))}{\sum_{a' \in \{\epsilon, 1, 2, \dots, i-1\}} \exp(\psi_M(a', i))}. \quad [15.9]$$

8119 This objective rewards models that assign high scores for all valid antecedent structures.  
 8120 In the running example, this would correspond to summing the probabilities of the two  
 8121 valid antecedents for *Cook, he* and *Apple Inc Chief Executive Tim Cook*. In one of the exer-  
 8122 cises, you will compute the number of valid antecedent structures for a given clustering.

### 8123 15.2.3 Transitive closure in mention-based models

A problem for mention-based models is that individual mention-level decisions may be incoherent. Consider the following mentions:

$$m_1 = \text{Hillary Clinton} \quad [15.10]$$

$$m_2 = \text{Clinton} \quad [15.11]$$

$$m_3 = \text{Bill Clinton} \quad [15.12]$$

8124 A mention-pair system might predict  $\hat{y}_{1,2} = 1, \hat{y}_{2,3} = 1, \hat{y}_{1,3} = 0$ . Similarly, a mention-  
 8125 ranking system might choose  $\hat{a}_2 = 1$  and  $\hat{a}_3 = 2$ . Logically, if mentions 1 and 3 are both  
 8126 coreferent with mention 2, then all three mentions must refer to the same entity. This  
 8127 constraint is known as **transitive closure**.

8128 Transitive closure can be applied *post hoc*, revising the independent mention-pair or  
 8129 mention-ranking decisions. However, there are many possible ways to enforce transitive  
 8130 closure: in the example above, we could set  $\hat{y}_{1,3} = 1$ , or  $\hat{y}_{1,2} = 0$ , or  $\hat{y}_{2,3} = 0$ . For docu-  
 8131 ments with many mentions, there may be many violations of transitive closure, and many  
 8132 possible fixes. Transitive closure can be enforced by always adding edges, so that  $\hat{y}_{1,3} = 1$   
 8133 is preferred (e.g., Soon et al., 2001), but this can result in overclustering, with too many  
 8134 mentions grouped into too few entities.

Mention-pair coreference resolution can be viewed as a constrained optimization prob-  
 lem,

$$\max_{\mathbf{y} \in \{0,1\}^M} \sum_{j=1}^M \sum_{i=1}^j \psi_M(i, j) \times y_{i,j}$$

s.t.  $y_{i,j} + y_{j,k} - 1 \leq y_{i,k}, \quad \forall i < j < k,$

8135 with the constraint enforcing transitive closure. This constrained optimization problem  
 8136 is equivalent to graph partitioning with positive and negative edge weights: construct a  
 8137 graph where the nodes are mentions, and the edges are the pairwise scores  $\psi_M(i, j)$ ; the  
 8138 goal is to partition the graph so as to maximize the sum of the edge weights between all  
 8139 nodes within the same partition (McCallum and Wellner, 2004). This problem is NP-hard,  
 8140 motivating approximations such as correlation clustering (Bansal et al., 2004) and **integer**  
 8141 **linear programming** (Klenner, 2007; Finkel and Manning, 2008, also see § 13.2.2).

#### 8142 15.2.4 Entity-based models

A weakness of mention-based models is that they treat coreference resolution as a classifi-  
 cation or ranking problem, when it is really a clustering problem: the goal is to group the  
 mentions together into clusters that correspond to the underlying entities. Entity-based  
 approaches attempt to identify these clusters directly. Such methods require a scoring  
 function at the entity level, measuring whether each set of mentions is internally consis-  
 tent. Coreference resolution can then be viewed as the following optimization,

$$\max_{\mathbf{z}} \sum_{e=1} \psi_E(\{i : z_i = e\}), \tag{15.13}$$

8143 where  $z_i$  indicates the entity referenced by mention  $i$ , and  $\psi_E(\{i : z_i = e\})$  is a scoring  
 8144 function applied to all mentions  $i$  that are assigned to entity  $e$ .

Entity-based coreference resolution is conceptually similar to the unsupervised clus-  
 tering problems encountered in chapter 5: the goal is to obtain clusters of mentions that  
 are internally coherent. The number of possible clusterings of  $n$  items is the **Bell number**,

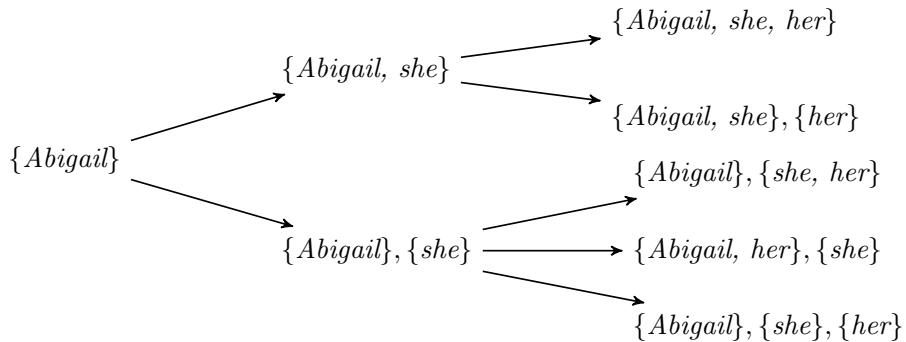


Figure 15.4: The Bell Tree for the sentence *Abigail hopes she speaks with her*. Which paths are excluded by the syntactic constraints mentioned in § 15.1.1?

which is defined by the following recurrence (Bell, 1934; Luo et al., 2004),

$$B_n = \sum_{k=0}^{n-1} B_k \binom{n-1}{k} B_0 = \quad B_1 = 1. \quad [15.14]$$

8145 This recurrence is illustrated by the Bell tree, which is applied to a short coreference prob-  
 8146 lem in Figure 15.4. The Bell number  $B_n$  grows exponentially with  $n$ , making exhaustive  
 8147 search of the space of clusterings impossible. For this reason, entity-based coreference  
 8148 resolution typically involves incremental search, in which clustering decisions are based  
 8149 on local evidence, in the hope of approximately optimizing the full objective in Equa-  
 8150 tion 15.13. This approach is sometimes called **cluster ranking**, in contrast to mention  
 8151 ranking.

8152 **\*Generative models of coreference** Entity-based coreference can be approached through  
 8153 probabilistic **generative models**, in which the mentions in the document are conditioned  
 8154 on a set of latent entities (Haghghi and Klein, 2007, 2010). An advantage of these meth-  
 8155 ods is that they can be learned from unlabeled data (Poon and Domingos, 2008, e.g.); a  
 8156 disadvantage is that probabilistic inference is required not just for learning, but also for  
 8157 prediction. Furthermore, generative models require independence assumptions that are  
 8158 difficult to apply in coreference resolution, where the diverse and heterogeneous features  
 8159 do not admit an easy decomposition into mutually independent subsets.

#### 8160 15.2.4.1 Incremental cluster ranking

8161 The SMASH method (§ 15.1.1) can be extended to entity-based coreference resolution by  
 8162 building up coreference clusters while moving through the document (Cardie and Wagstaff,  
 8163 1999). At each mention, the algorithm iterates backwards through possible antecedent

8164 clusters; but unlike SMASH, a cluster is selected only if *all* members of its cluster are compatible  
 8165 with the current mention. As mentions are added to a cluster, so are their features  
 8166 (e.g., gender, number, animacy). In this way, incoherent chains like *{Hillary Clinton, Clinton, Bill Clinton}*  
 8167 can be avoided. However, an incorrect assignment early in the document — a **search error**  
 8168 — might lead to a cascade of errors later on.

8169 More sophisticated search strategies can help to ameliorate the risk of search errors.  
 8170 One approach is **beam search** (§ 11.3), in which a set of hypotheses is maintained through-  
 8171 out search. Each hypothesis represents a path through the Bell tree (Figure 15.4). Hy-  
 8172 potheses are “expanded” either by adding the next mention to an existing cluster, or by  
 8173 starting a new cluster. Each expansion receives a score, based on Equation 15.13, and the  
 8174 top  $K$  hypotheses are kept on the beam as the algorithm moves to the next step.

8175 Incremental cluster ranking can be made more accurate by performing multiple passes  
 8176 over the document, applying rules (or “sieves”) with increasing recall and decreasing  
 8177 precision at each pass (Lee et al., 2013). In the early passes, coreference links are pro-  
 8178 posed only between mentions that are highly likely to corefer (e.g., exact string match  
 8179 for full names and nominals). Information can then be shared among these mentions,  
 8180 so that when more permissive matching rules are applied later, agreement is preserved  
 8181 across the entire cluster. For example, in the case of *{Hillary Clinton, Clinton, she}*, the  
 8182 name-matching sieve would link *Clinton* and *Hillary Clinton*, and the pronoun-matching  
 8183 sieve would then link *she* to the combined cluster. A deterministic multi-pass system  
 8184 won nearly every track of the 2011 CoNLL shared task on coreference resolution (Prad-  
 8185 han et al., 2011). Given the dominance of machine learning in virtually all other areas  
 8186 of natural language processing — and more than fifteen years of prior work on machine  
 8187 learning for coreference — this was a surprising result, even if learning-based methods  
 8188 have subsequently regained the upper hand (e.g., Lee et al., 2017, the state-of-the-art at  
 8189 the time of this writing).

#### 8190 15.2.4.2 Incremental perceptron

Incremental coreference resolution can be learned with the **incremental perceptron**, as described in § 11.3.2. At mention  $i$ , each hypothesis on the beam corresponds to a clustering of mentions  $1 \dots i - 1$ , or equivalently, a path through the Bell tree up to position  $i - 1$ . As soon as none of the hypotheses on the beam are compatible with the gold coreference clustering, a perceptron update is made (Daumé III and Marcu, 2005). For concreteness, consider a linear cluster ranking model,

$$\psi_E(\{i : z_i = e\}) = \sum_{i:z_i=e} \theta \cdot f(i, \{j : j < i \wedge z_j = e\}), \quad [15.15]$$

8191 where the score for each cluster is computed as the sum of scores of all mentions that are  
 8192 linked into the cluster, and  $f(i, \emptyset)$  is a set of features for the non-anaphoric mention that  
 8193 initiates the cluster.

8194 Using Figure 15.4 as an example, suppose that the ground truth is,

$$\mathbf{c}^* = \{\text{Abigail}, \text{her}\}, \{\text{she}\}, \quad [15.16]$$

8195 but that with a beam of size one, the learner reaches the hypothesis,

$$\hat{\mathbf{c}} = \{\text{Abigail}, \text{she}\}. \quad [15.17]$$

This hypothesis is incompatible with  $\mathbf{c}^*$ , so an update is needed:

$$\boldsymbol{\theta} \leftarrow \boldsymbol{\theta} + \mathbf{f}(\mathbf{c}^*) - \mathbf{f}(\hat{\mathbf{c}}) \quad [15.18]$$

$$= \boldsymbol{\theta} + (\mathbf{f}(\text{Abigail}, \emptyset) + \mathbf{f}(\text{she}, \emptyset)) - (\mathbf{f}(\text{Abigail}, \emptyset) + \mathbf{f}(\text{she}, \{\text{Abigail}\})) \quad [15.19]$$

$$= \boldsymbol{\theta} + \mathbf{f}(\text{she}, \emptyset) - \mathbf{f}(\text{she}, \{\text{Abigail}\}). \quad [15.20]$$

8196 This style of incremental update can also be applied to a margin loss between the gold  
 8197 clustering and the top clustering on the beam. By backpropagating from this loss, it is also  
 8198 possible to train a more complicated scoring function, such as a neural network in which  
 8199 the score for each entity is a function of embeddings for the entity mentions (Wiseman  
 8200 et al., 2015).

#### 8201 15.2.4.3 Reinforcement learning

8202 **Reinforcement learning** is a topic worthy of a textbook of its own (Sutton and Barto,  
 8203 1998),<sup>5</sup> so this section will provide only a very brief overview, in the context of coreference  
 8204 resolution. A stochastic **policy** assigns a probability to each possible **action**, conditional  
 8205 on the context. The goal is to learn a policy that achieves a high expected reward, or  
 8206 equivalently, a low expected cost.

8207 In incremental cluster ranking, a complete clustering on  $M$  mentions can be produced  
 8208 by a sequence of  $M$  actions, in which the action  $z_i$  either merges mention  $i$  with an existing  
 8209 cluster or begins a new cluster. We can therefore create a stochastic policy using the cluster  
 8210 scores (Clark and Manning, 2016),

$$\Pr(z_i = e; \boldsymbol{\theta}) = \frac{\exp \psi_E(i \cup \{j : z_j = e\}; \boldsymbol{\theta})}{\sum_{e'} \exp \psi_E(i \cup \{j : z_j = e'\}; \boldsymbol{\theta})}, \quad [15.21]$$

8211 where  $\psi_E(i \cup \{j : z_j = e\}; \boldsymbol{\theta})$  is the score under parameters  $\boldsymbol{\theta}$  for assigning mention  $i$  to  
 8212 cluster  $e$ . This score can be an arbitrary function of the mention  $i$ , the cluster  $e$  and its  
 8213 (possibly empty) set of mentions; it can also include the history of actions taken thus far.

---

<sup>5</sup>A draft of the second edition can be found here: <http://incompleteideas.net/book/the-book-2nd.html>. Reinforcement learning has been used in spoken dialogue systems (Walker, 2000) and text-based game playing (Branavan et al., 2009), and was applied to coreference resolution by Clark and Manning (2015).

8214 If a policy assigns probability  $p(c; \theta)$  to clustering  $c$ , then its expected loss is,

$$L(\theta) = \sum_{c \in \mathcal{C}(m)} p_\theta(c) \times \ell(c), \quad [15.22]$$

8215 where  $\mathcal{C}(m)$  is the set of possible clusterings for mentions  $m$ . The loss  $\ell(c)$  can be based on  
 8216 any arbitrary scoring function, including the complex evaluation metrics used in corefer-  
 8217 ence resolution (see § 15.4). This is an advantage of reinforcement learning, which can be  
 8218 trained directly on the evaluation metric — unlike traditional supervised learning, which  
 8219 requires a loss function that is differentiable and decomposable across individual deci-  
 8220 sions.

Rather than summing over the exponentially many possible clusterings, we can approximate the expectation by sampling trajectories of actions,  $z = (z_1, z_2, \dots, z_M)$ , from the current policy. Each action  $z_i$  corresponds to a step in the Bell tree: adding mention  $m_i$  to an existing cluster, or forming a new cluster. Each trajectory  $z$  corresponds to a single clustering  $c$ , and so we can write the loss of an action sequence as  $\ell(c(z))$ . The **policy gradient** algorithm computes the gradient of the expected loss as an expectation over trajectories (Sutton et al., 2000),

$$\frac{\partial}{\partial \theta} L(\theta) = E_{z \sim \mathcal{Z}(m)} \ell(c(z)) \sum_{i=1}^M \frac{\partial}{\partial \theta} \log p(z_i | z_{1:i-1}, m) \quad [15.23]$$

$$\approx \frac{1}{K} \sum_{k=1}^K \ell(c(z^{(k)})) \sum_{i=1}^M \frac{\partial}{\partial \theta} \log p(z_i^{(k)} | z_{1:i-1}^{(k)}, m), \quad [15.24]$$

8221 where each action sequence  $z^{(k)}$  is sampled from the current policy. Unlike the incremen-  
 8222 tal perceptron, an update is not made until the complete action sequence is available.

#### 8223 15.2.4.4 Learning to search

8224 Policy gradient can suffer from high variance: while the average loss over  $K$  samples is  
 8225 asymptotically equal to the expected reward of a given policy, this estimate may not be  
 8226 accurate unless  $K$  is very large. This can make it difficult to allocate credit and blame to  
 8227 individual actions. In **learning to search**, this problem is addressed through the addition  
 8228 of an **oracle** policy, which is known to receive zero or small loss. The oracle policy can be  
 8229 used in two ways:

- 8230 • The oracle can be used to generate partial hypotheses that are likely to score well,  
 8231 by generating  $i$  actions from the initial state. These partial hypotheses are then used  
 8232 as starting points for the learned policy. This is known as **roll-in**.

**Algorithm 18** Learning to search for entity-based coreference resolution

---

```

1: procedure COMPUTE-GRADIENT(mentions  $m$ , loss function  $\ell$ , parameters  $\theta$ )
2:    $L(\theta) \leftarrow 0$ 
3:    $z \sim p(z | m; \theta)$                                  $\triangleright$  Sample a trajectory from the current policy
4:   for  $i \in \{1, 2, \dots, M\}$  do
5:     for action  $z \in \mathcal{Z}(z_{1:i-1}, m)$  do           $\triangleright$  All possible actions after history  $z_{1:i-1}$ 
6:        $h \leftarrow z_{1:i-1} \oplus z$                        $\triangleright$  Concatenate history  $z_{1:i-1}$  with action  $z$ 
7:       for  $j \in \{i+1, i+2, \dots, M\}$  do            $\triangleright$  Roll-out
8:          $h_j \leftarrow \operatorname{argmin}_h \ell(h_{1:j-1} \oplus h)$      $\triangleright$  Oracle selects action with minimum loss
9:        $L(\theta) \leftarrow L(\theta) + p(z | z_{1:i-1}, m; \theta) \times \ell(h)$        $\triangleright$  Update expected loss
10:      return  $\frac{\partial}{\partial \theta} L(\theta)$ 

```

---

- 8233 • The oracle can be used to compute the minimum possible loss from a given state, by  
 8234 generating  $M - i$  actions from the current state until completion. This is known as  
 8235 **roll-out**.

8236 The oracle can be combined with the existing policy during both roll-in and roll-out, sam-  
 8237 pling actions from each policy (Daumé III et al., 2009). One approach is to gradually  
 8238 decrease the number of actions drawn from the oracle over the course of learning (Ross  
 8239 et al., 2011).

8240 In the context of entity-based coreference resolution, Clark and Manning (2016) use  
 8241 the learned policy for roll-in and the oracle policy for roll-out. Algorithm 18 shows how  
 8242 the gradients on the policy weights are computed in this case. In this application, the  
 8243 oracle is “noisy”, because it selects the action that minimizes only the *local* loss — the  
 8244 accuracy of the coreference clustering up to mention  $i$  — rather than identifying the action  
 8245 sequence that will lead to the best final coreference clustering on the entire document.  
 8246 When learning from noisy oracles, it can be helpful to mix in actions from the current  
 8247 policy with the oracle during roll-out (Chang et al., 2015).

8248 **15.3 Representations for coreference resolution**

8249 Historically, coreference resolution has employed an array of hand-engineered features  
 8250 to capture the linguistic constraints and preferences described in § 15.1 (Soon et al., 2001).  
 8251 Later work has documented the utility of lexical and bilexical features on mention pairs (Björkelund  
 8252 and Nugues, 2011; Durrett and Klein, 2013). The most recent and successful methods re-  
 8253 place many (but not all) of these features with distributed representations of mentions  
 8254 and entities (Wiseman et al., 2015; Clark and Manning, 2016; Lee et al., 2017).

8255 **15.3.1 Features**

8256 Coreference features generally rely on a preprocessing pipeline to provide part-of-speech  
 8257 tags and phrase structure parses. This pipeline makes it possible to design features that  
 8258 capture many of the phenomena from § 15.1, and is also necessary for typical approaches  
 8259 to mention identification. However, the pipeline may introduce errors that propagate  
 8260 to the downstream coreference clustering system. Furthermore, the existence of such  
 8261 a pipeline presupposes resources such as treebanks, which do not exist for many lan-  
 8262 guages.<sup>6</sup>

8263 **15.3.1.1 Mention features**

8264 Features of individual mentions can help to predict anaphoricity. In systems where men-  
 8265 tion detection is performed jointly with coreference resolution, these features can also  
 8266 predict whether a span of text is likely to be a mention. For mention  $i$ , typical features  
 8267 include:

8268 **Mention type.** Each span can be identified as a pronoun, name, or nominal, using the  
 8269 part-of-speech of the head word of the mention: both the Penn Treebank and Uni-  
 8270 versal Dependencies tagsets (§ 8.1.1) include tags for pronouns and proper nouns,  
 8271 and all other heads can be marked as nominals (Haghghi and Klein, 2009).

8272 **Mention width.** The number of tokens in a mention is a rough predictor of its anaphor-  
 8273 icity, with longer mentions being less likely to refer back to previously-defined enti-  
 8274 ties.

8275 **Lexical features.** The first, last, and head words can help to predict anaphoricity; they are  
 8276 also useful in conjunction with features such as mention type and part-of-speech,  
 8277 providing a rough measure of agreement (Björkelund and Nugues, 2011). The num-  
 8278 ber of lexical features can be very large, so it can be helpful to select only frequently-  
 8279 occurring features (Durrett and Klein, 2013).

8280 **Morphosyntactic features.** These features include the part-of-speech, number, gender,  
 8281 and dependency ancestors.

8282 The features for mention  $i$  and candidate antecedent  $a$  can be conjoined, producing  
 8283 joint features that can help to assess the compatibility of the two mentions. For example,  
 8284 Durrett and Klein (2013) conjoin each feature with the mention types of the anaphora  
 8285 and the antecedent. Coreference resolution corpora such as ACE and OntoNotes contain

---

<sup>6</sup>The Universal Dependencies project has produced dependency treebanks for more than sixty languages. However, coreference features and mention detection are generally based on phrase structure trees, which exist for roughly two dozen languages. A list is available here: <https://en.wikipedia.org/wiki/Treebank>

8286 documents from various genres. By conjoining the genre with other features, it is possible  
8287 to learn genre-specific feature weights.

8288 **15.3.1.2 Mention-pair features**

8289 For any pair of mentions  $i$  and  $j$ , typical features include:

8290 **Distance.** The number of intervening tokens, mentions, and sentences between  $i$  and  $j$   
8291 can all be used as distance features. These distances can be computed on the surface  
8292 text, or on a transformed representation reflecting the breadth-first tree traversal  
8293 (Figure 15.3). Rather than using the distances directly, they are typically binned,  
8294 creating binary features.

8295 **String match.** A variety of string match features can be employed: exact match, suffix  
8296 match, head match, and more complex matching rules that disregard irrelevant  
8297 modifiers (Soon et al., 2001).

8298 **Compatibility.** Building on the model, features can measure the anaphor and antecedent  
8299 agree with respect to morphosyntactic attributes such as gender, number, and ani-  
8300 macy.

8301 **Nesting.** If one mention is nested inside another (e.g., *[The President of [France]]*), they  
8302 generally cannot corefer.

8303 **Same speaker.** For documents with quotations, such as news articles, personal pronouns  
8304 can be resolved only by determining the speaker for each mention (Lee et al., 2013).  
8305 Coreference is also more likely between mentions from the same speaker.

8306 **Gazetteers.** These features indicate that the anaphor and candidate antecedent appear in  
8307 a gazetteer of acronyms (e.g., *USA/United States*, *GATech/Georgia Tech*), demonymns  
8308 (e.g., *Israel/Israeli*), or other aliases (e.g., *Knickerbockers/New York Knicks*).

8309 **Lexical semantics.** These features use a lexical resource such as WordNet to determine  
8310 whether the head words of the mentions are related through synonymy, antonymy,  
8311 and hypernymy (§ 4.2).

8312 **Dependency paths.** The dependency path between the anaphor and candidate antecedent  
8313 can help to determine whether the pair can corefer, under the government and bind-  
8314 ing constraints described in § 15.1.1.

8315 Comprehensive lists of mention-pair features are offered by Bengtson and Roth (2008) and  
8316 Rahman and Ng (2011). Neural network approaches use far fewer mention-pair features:  
8317 for example, Lee et al. (2017) include only speaker, genre, distance, and mention width  
8318 features.

8319 **Semantics** In many cases, coreference seems to require knowledge and semantic in-  
 8320 ferences, as in the running example, where we link *China* with a *country* and a *growth*  
 8321 *market*. Some of this information can be gleaned from WordNet, which defines a graph  
 8322 over **synsets** (see § 4.2). For example, one of the synsets of *China* is an instance of an  
 8323 *Asian\_nation#1*, which in turn is a hyponym of *country#2*, a synset that includes  
 8324 *country*.<sup>7</sup> Such paths can be used to measure the similarity between concepts (Pedersen  
 8325 et al., 2004), and this similarity can be incorporated into coreference resolution as a fea-  
 8326 ture (Ponzetto and Strube, 2006). Similar ideas can be applied to knowledge graphs in-  
 8327 duced from Wikipedia (Ponzetto and Strube, 2007). But while such approaches improve  
 8328 relatively simple classification-based systems, they have proven less useful when added  
 8329 to the current generation of techniques.<sup>8</sup> For example, Durrett and Klein (2013) employ  
 8330 a range of semantics-based features — WordNet synonymy and hypernymy relations on  
 8331 head words, named entity types (e.g., person, organization), and unsupervised clustering  
 8332 over nominal heads — but find that these features give minimal improvement over a  
 8333 baseline system using surface features.

### 8334 15.3.1.3 Entity features

8335 Many of the features for entity-mention coreference are generated by aggregating mention-  
 8336 pair features over all mentions in the candidate entity (Culotta et al., 2007; Rahman and  
 8337 Ng, 2011). Specifically, for each binary mention-pair feature  $f(i, j)$ , we compute the fol-  
 8338 lowing entity-mention features for mention  $i$  and entity  $e = \{j : j < i \wedge z_j = e\}$ .

- 8339 • ALL-TRUE: Feature  $f(i, j)$  holds for all mentions  $j \in e$ .
- 8340 • MOST-TRUE: Feature  $f(i, j)$  holds for at least half and fewer than all mentions  $j \in e$ .
- 8341 • MOST-FALSE: Feature  $f(i, j)$  holds for at least one and fewer than half of all men-  
 8342 tions  $j \in e$ .
- 8343 • NONE: Feature  $f(i, j)$  does not hold for any mention  $j \in e$ .

8344 For scalar mention-pair features (e.g., distance features), aggregation can be performed by  
 8345 computing the minimum, maximum, and median values across all mentions in the cluster.  
 8346 Additional entity-mention features include the number of mentions currently clustered in  
 8347 the entity, and ALL-X and MOST-X features for each mention type.

### 8348 15.3.2 Distributed representations of mentions and entities

8349 Recent work has emphasized distributed representations of both mentions and entities.  
 8350 One potential advantage is that pre-trained embeddings could help to capture the se-

---

<sup>7</sup>teletype font is used to indicate wordnet synsets, and *italics* is used to indicate strings.

<sup>8</sup>This point was made by Michael Strube at a 2015 workshop, noting that as the quality of the machine learning models in coreference has improved, the benefit of including semantics has become negligible.

8351 mantic compatibility underlying nominal coreference, helping with difficult cases like  
 8352 (*Apple, the firm*) and (*China, the firm's biggest growth market*). Furthermore, a distributed  
 8353 representation of entities can be trained to capture semantic features that are added by  
 8354 each mention.

8355 **15.3.2.1 Mention embeddings**

8356 Entity mentions can be embedded into a vector space, providing the base layer for neural  
 8357 networks that score coreference decisions (Wiseman et al., 2015).

8358 **Constructing the mention embedding** Various approaches for embedding multiword  
 8359 units can be applied (see § 14.8). Figure 15.5 shows a recurrent neural network approach,  
 8360 which begins by running a bidirectional LSTM over the entire text, obtaining hidden states  
 8361 from the left-to-right and right-to-left passes,  $\mathbf{h}_m = [\overleftarrow{\mathbf{h}}_m; \overrightarrow{\mathbf{h}}_m]$ . Each candidate mention  
 8362 span  $(s, t)$  is then represented by the vertical concatenation of four vectors:

$$\mathbf{u}^{(s,t)} = [\mathbf{u}_{\text{first}}^{(s,t)}; \mathbf{u}_{\text{last}}^{(s,t)}; \mathbf{u}_{\text{head}}^{(s,t)}; \phi^{(s,t)}], \quad [15.25]$$

8363 where  $\mathbf{u}_{\text{first}}^{(s,t)} = \mathbf{h}_{s+1}$  is the embedding of the first word in the span,  $\mathbf{u}_{\text{last}}^{(s,t)} = \mathbf{h}_t$  is the  
 8364 embedding of the last word,  $\mathbf{u}_{\text{head}}^{(s,t)}$  is the embedding of the “head” word, and  $\phi^{(s,t)}$  is a  
 8365 vector of surface features, such as the length of the span (Lee et al., 2017).

**Attention over head words** Rather than identifying the head word from the output of a parser, it can be computed from a neural **attention mechanism**:

$$\tilde{\alpha}_m = \theta_\alpha \cdot \mathbf{h}_m \quad [15.26]$$

$$\mathbf{a}^{(s,t)} = \text{SoftMax}([\tilde{\alpha}_{s+1}, \tilde{\alpha}_{s+2}, \dots, \tilde{\alpha}_t]) \quad [15.27]$$

$$\mathbf{u}_{\text{head}}^{(s,t)} = \sum_{m=s+1}^t a_m^{(s,t)} \mathbf{h}_m. \quad [15.28]$$

8366 Each token  $m$  gets a scalar score  $\tilde{\alpha}_m = \theta_\alpha \cdot \mathbf{h}_m$ , which is the dot product of the LSTM  
 8367 hidden state  $\mathbf{h}_m$  and a vector of weights  $\theta_\alpha$ . The vector of scores for tokens in the span  
 8368  $m \in \{s + 1, s + 2, \dots, t\}$  is then passed through a softmax layer, yielding a vector  $\mathbf{a}^{(s,t)}$   
 8369 that allocates one unit of attention across the span. This eliminates the need for syntactic  
 8370 parsing to recover the head word; instead, the model learns to identify the most important  
 8371 words in each span. Attention mechanisms were introduced in neural machine transla-  
 8372 tion (Bahdanau et al., 2014), and are described in more detail in § 18.3.1.

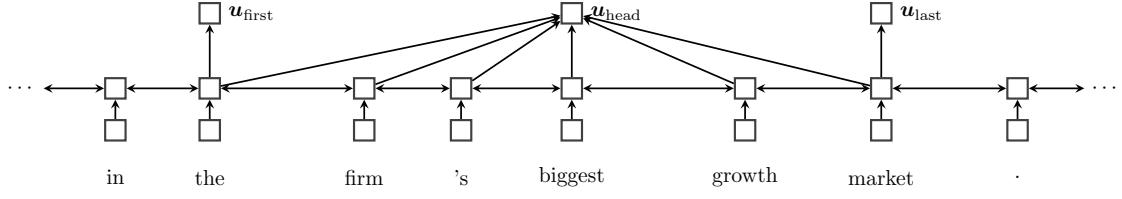


Figure 15.5: A bidirectional recurrent model of mention embeddings. The mention is represented by its first word, its last word, and an estimate of its head word, which is computed from a weighted average (Lee et al., 2017).

**Using mention embeddings** Given a set of mention embeddings, each mention  $i$  and candidate antecedent  $a$  is scored as,

$$\psi(a, i) = \psi_S(a) + \psi_S(i) + \psi_M(a, i) \quad [15.29]$$

$$\psi_S(a) = \text{FeedForward}_S(\mathbf{u}^{(a)}) \quad [15.30]$$

$$\psi_S(i) = \text{FeedForward}_S(\mathbf{u}^{(i)}) \quad [15.31]$$

$$\psi_M(a, i) = \text{FeedForward}_M([\mathbf{u}^{(a)}; \mathbf{u}^{(i)}; \mathbf{u}^{(a)} \odot \mathbf{u}^{(i)}; \mathbf{f}(a, i, \mathbf{w})]), \quad [15.32]$$

8373 where  $\mathbf{u}^{(a)}$  and  $\mathbf{u}^{(i)}$  are the embeddings for spans  $a$  and  $i$  respectively, as defined in Equa-  
8374 tion 15.25.

- 8375 • The scores  $\psi_S(a)$  quantify whether span  $a$  is likely to be a coreferring mention, inde-  
8376 pendent of what it corefers with. This allows the model to learn identify mentions  
8377 directly, rather than identifying mentions with a preprocessing step.  
8378 • The score  $\psi_M(a, i)$  computes the compatibility of spans  $a$  and  $i$ . Its base layer is a  
8379 vector that includes the embeddings of spans  $a$  and  $i$ , their elementwise product  
8380  $\mathbf{u}^{(a)} \odot \mathbf{u}^{(i)}$ , and a vector of surface features  $\mathbf{f}(a, i, \mathbf{w})$ , including distance, speaker,  
8381 and genre information.

8382 Lee et al. (2017) provide an error analysis that shows how this method can correctly link  
8383 a *blaze* and a *fire*, while incorrectly linking *pilots* and *fight attendants*. In each case, the  
8384 coreference decision is based on similarities in the word embeddings.

8385 Rather than embedding individual mentions, Clark and Manning (2016) embed men-  
8386 tion pairs. At the base layer, their network takes embeddings of the words in and around  
8387 each mention, as well as **one-hot** vectors representing a few surface features, such as the  
8388 distance and string matching features. This base layer is then passed through a multilayer  
8389 feedforward network with ReLU nonlinearities, resulting in a representation of the men-  
8390 tion pair. The output of the mention pair encoder  $\mathbf{u}_{i,j}$  is used in the scoring function of  
8391 a mention-ranking model,  $\psi_M(i, j) = \theta \cdot \mathbf{u}_{i,j}$ . A similar approach is used to score cluster

8392 pairs, constructing a cluster-pair encoding by **pooling** over the mention-pair encodings  
8393 for all pairs of mentions within the two clusters.

8394 **15.3.2.2 Entity embeddings**

8395 In entity-based coreference resolution, each entity should be represented by properties of  
8396 its mentions. In a distributed setting, we maintain a set of vector entity embeddings,  $v_e$ .  
8397 Each candidate mention receives an embedding  $u_i$ ; Wiseman et al. (2016) compute this  
8398 embedding by a single-layer neural network, applied to a vector of surface features. The  
8399 decision of whether to merge mention  $i$  with entity  $e$  can then be driven by a feedforward  
8400 network,  $\psi_E(i, e) = \text{Feedforward}([v_e; u_i])$ . If  $i$  is added to entity  $e$ , then its representa-  
8401 tion is updated recurrently,  $v_e \leftarrow f(v_e, u_i)$ , using a recurrent neural network such as a  
8402 long short-term memory (LSTM; chapter 6). Alternatively, we can apply a **pooling** oper-  
8403 ation, such as max-pooling or average-pooling (chapter 3), setting  $v_e \leftarrow \text{Pool}(v_e, u_i)$ . In  
8404 either case, the update to the representation of entity  $e$  can be thought of as adding new  
8405 information about the entity from mention  $i$ .

8406 **15.4 Evaluating coreference resolution**

8407 The state of coreference evaluation is aggravatingly complex. Early attempts at sim-  
8408 ple evaluation metrics were found to be susceptible to trivial baselines, such as placing  
8409 each mention in its own cluster, or grouping all mentions into a single cluster. Follow-  
8410 ing Denis and Baldridge (2009), the CoNLL 2011 shared task on coreference (Pradhan  
8411 et al., 2011) formalized the practice of averaging across three different metrics: MUC (Vi-  
8412 lain et al., 1995), B-CUBED (Bagga and Baldwin, 1998a), and CEAf (Luo, 2005). Refer-  
8413 ence implementations of these metrics are available from Pradhan et al. (2014) at <https://github.com/conll/reference-coreference-scorers>.  
8414

8415 **Additional resources**

8416 Ng (2010) surveys coreference resolution through 2010. Early work focused exclusively  
8417 on pronoun resolution, with rule-based (Lappin and Leass, 1994) and probabilistic meth-  
8418 ods (Ge et al., 1998). The full coreference resolution problem was popularized in a shared  
8419 task associated with the sixth Message Understanding Conference, which included coref-  
8420 erence annotations for training and test sets of thirty documents each (Grishman and  
8421 Sundheim, 1996). An influential early paper was the decision tree approach of Soon et al.  
8422 (2001), who introduced mention ranking. A comprehensive list of surface features for  
8423 coreference resolution is offered by Bengtson and Roth (2008). Durrett and Klein (2013)  
8424 improved on prior work by introducing a large lexicalized feature set; subsequent work  
8425 has emphasized neural representations of entities and mentions (Wiseman et al., 2015).

8426 **Exercises**

- 8427 1. Select an article from today's news, and annotate coreference for the first twenty  
8428 noun phrases that appear in the article (include nested noun phrases). That is,  
8429 group the noun phrases into entities, where each entity corresponds to a set of noun  
8430 phrases. Then specify the mention-pair training data that would result from the first  
8431 five noun phrases.
  - 8432 2. Using your annotations from the preceding problem, compute the following statistics:  
8433
    - 8434 • The number of times new entities are introduced by each of the three types of  
8435 referring expressions: pronouns, proper nouns, and nominals. Include "single-  
8436 ton" entities that are mentioned only once.
    - 8437 • For each type of referring expression, compute the fraction of mentions that are  
8438 anaphoric.
  - 8439 3. Apply a simple heuristic to all pronouns in the article from the previous exercise.  
8440 Specifically, link each pronoun to the closest preceding noun phrase that agrees in  
8441 gender, number, animacy, and person. Compute the following evaluation:  
8442
    - 8443 • True positive: a pronoun that is linked to a noun phrase with which it is coref-  
erent, or is correctly labeled as the first mention of an entity.
    - 8444 • False positive: a pronoun that is linked to a noun phrase with which it is not  
8445 coreferent. (This includes mistakenly linking singleton or non-referential pro-  
8446 nouns.)
    - 8447 • False negative: a pronoun that is not linked to a noun phrase with which it is  
8448 coreferent.
- 8449 Compute the *F*-MEASURE for your method, and for a trivial baseline in which ev-  
8450 ery mention is its own entity. Are there any additional heuristics that would have  
8451 improved the performance of this method?
- 8452 4. Durrett and Klein (2013) compute the probability of the gold coreference clustering  
8453 by summing over all antecedent structures that are compatible with the clustering.  
8454 For example, if there are three mentions of a single entity,  $m_1, m_2, m_3$ , there are two  
8455 possible antecedent structures:  $a_2 = 1, a_3 = 1$  and  $a_2 = 1, a_3 = 2$ . Compute the  
8456 number of antecedent structures for a single entity with  $K$  mentions.
  - 8457 5. Suppose that all mentions can be unambiguously divided into  $C$  classes, for exam-  
8458 ple by gender and number. Further suppose that mentions from different classes  
8459 can never corefer. In a document with  $M$  mentions, give upper and lower bounds  
8460 on the total number of possible coreference clusterings, in terms of the Bell numbers

and the parameters  $M$  and  $C$ . Compute numerical upper and lower bounds for the case  $M = 4, C = 2$ .

6. Lee et al. (2017) propose a model that considers all contiguous spans in a document as possible mentions.

- a) In a document of length  $M$ , how many mention pairs must be evaluated? (All answers can be given in asymptotic, big-O notation.)
- b) To make inference more efficient, Lee et al. (2017) restrict consideration to spans of maximum length  $L \ll M$ . Under this restriction, how many mention pairs must be evaluated?
- c) To further improve inference, one might evaluate coreference only between pairs of mentions whose endpoints are separated by a maximum of  $D$  tokens. Under this additional restriction, how many mention pairs must be evaluated?

7. In Spanish, the subject can be omitted when it is clear from context, e.g.,

(15.21) *Las ballenas no son peces. Son mamíferos.*

The whales no are fish. Are mammals.

Whales are not fish. They are mammals.

Resolution of such **null subjects** is facilitated by the Spanish system of verb morphology, which includes distinctive suffixes for most combinations of person and number. For example, the verb form *son* ('are') agrees with the third-person plural pronouns *ellos* (masculine) and *ellas* (feminine), as well as the second-person plural *ustedes*.

Suppose that you are given the following components:

- A system that automatically identifies verbs with null subjects.
- A function  $c(j, p) \in \{0, 1\}$  that indicates whether pronoun  $p$  is compatible with null subject  $j$ , according to the verb morphology.
- A trained mention-pair model, which computes scores  $\psi(w_i, w_j, i - j) \in \mathbb{R}$  for all pairs of mentions  $i$  and  $j$ , scoring the pair by the antecedent mention  $w_i$ , the anaphor  $w_j$ , and the distance  $i - j$ .

Describe an integer linear program that simultaneously performs two tasks: resolving coreference among all entity mentions, and identifying suitable pronouns for all null subjects. In the example above, your program should link the null subject with *las ballenas* ('whales'), and identify *ellas* as the correct pronoun. For simplicity, you may assume that null subjects cannot be antecedents, and you need not worry about the transitivity constraint described in § 15.2.3.

- 8494     8. Use the policy gradient algorithm to compute the gradient for the following sce-  
 8495       nario, based on the Bell tree in Figure 15.4:

- 8496       • The gold clustering  $c^*$  is  $\{Abigail, her\}, \{she\}$ .  
 8497       • Drawing a single sequence of actions ( $K = 1$ ) from the current policy, you  
 8498        obtain the following incremental clusterings:

$$\begin{aligned}c(a_1) &= \{Abigail\} \\c(\mathbf{a}_{1:2}) &= \{Abigail, she\} \\c(\mathbf{a}_{1:3}) &= \{Abigail, she\}, \{her\}.\end{aligned}$$

- 8497       • At each mention  $t$ , the action space  $\mathcal{A}_t$  is to merge the mention with each exist-  
 8498        ing cluster, or the empty cluster, with probability,

$$\Pr(\text{Merge}(m_t, c(\mathbf{a}_{1:t-1}))) \propto \exp \psi_E(m_t \cup c(\mathbf{a}_{1:t-1})), \quad [15.33]$$

8499       where the cluster score  $\psi_E(m_t \cup c)$  is defined in Equation 15.15.

8500       Compute the gradient  $\frac{\partial}{\partial \theta} L(\theta)$  in terms of the loss  $\ell(c(\mathbf{a}))$  and the features of each  
 8501       (potential) cluster. Explain the differences between the gradient-based update  $\theta \leftarrow \theta - \frac{\partial}{\partial \theta} L(\theta)$   
 8502       and the incremental perceptron update from this same example.

- 8503     9. As discussed in § 15.1.1.4, some pronouns are not referential. In English, this occurs  
 8504       frequently with the word *it*. Download the text of *Alice in Wonderland* from nltk,  
 8505       and examine the first ten appearances of *it*. For each occurrence:

- 8506       • First, examine a five-token window around the word. In the first example, this  
 8507        window is,

8508       , but it had no

8509       Is there another pronoun that could be substituted for *it*? Consider *she*, *they*,  
 8510       and *them*. In this case, both *she* and *they* yield grammatical substitutions. What  
 8511       about the other ten cases?

- 8512       • Now, view an fifteen-word window for each example. Based on this window,  
 8513       mark whether you think the word *it* is referential.

8514       How often does the substitution test predict whether *it* is referential?

- 8515     10. Now try to automate the test, using the Google  $n$ -grams corpus (BRANTS and Franz,  
 8516       2006). Specifically, find the count of each 5-gram containing *it*, and then compute the  
 8517       counts of 5-grams in which *it* is replaced with other third-person pronouns: *he*, *she*,  
 8518       *they*, *her*, *him*, *them*, *herself*, *himself*. There are various ways to get these counts.

8519 One approach is to download the raw data and search it; another is to construct web  
8520 queries to <https://books.google.com/ngrams>.

8521 Compare the ratio of the counts of the original 5-gram to the summed counts of  
8522 the 5-grams created by substitution. Is this ratio a good predictor of whether *it* is  
8523 referential?



8524 **Chapter 16**

8525 **Discourse**

8526 Applications of natural language processing often concern multi-sentence documents:  
8527 from paragraph-long restaurant reviews, to 500-word newspaper articles, to 500-page  
8528 novels. Yet most of the methods that we have discussed thus far are concerned with  
8529 individual sentences. This chapter discusses theories and methods for handling multi-  
8530 sentence linguistic phenomena, known collectively as **discourse**. There are diverse char-  
8531 acterizations of discourse structure, and no single structure is ideal for every computa-  
8532 tional application. This chapter covers some of the most well studied discourse repre-  
8533 sentations, while highlighting computational models for identifying and exploiting these  
8534 structures.

8535 **16.1 Segments**

8536 A document or conversation can be viewed as a sequence of **segments**, each of which is  
8537 **cohesive** in its content and/or function. In Wikipedia biographies, these segments often  
8538 pertain to various aspects to the subject's life: early years, major events, impact on others,  
8539 and so on. This segmentation is organized around **topics**. Alternatively, scientific research  
8540 articles are often organized by **functional themes**: the introduction, a survey of previous  
8541 research, experimental setup, and results.

8542 Written texts often mark segments with section headers and related formatting de-  
8543 vices. However, such formatting may be too coarse-grained to support applications such  
8544 as the retrieval of specific passages of text that are relevant to a query (Hearst, 1997).  
8545 Unformatted speech transcripts, such as meetings and lectures, are also an application  
8546 scenario for segmentation (Carletta, 2007; Glass et al., 2007; Janin et al., 2003).

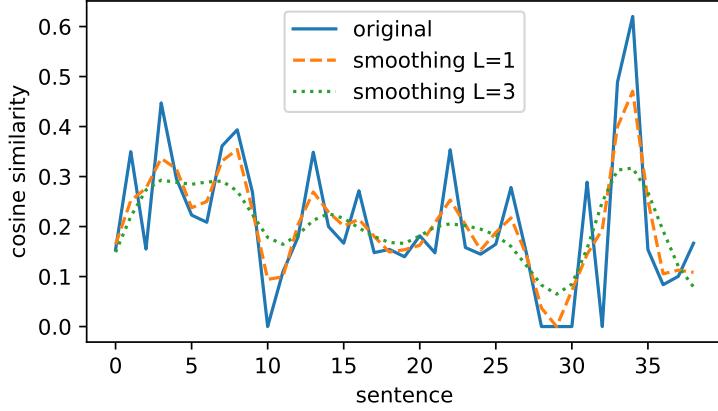


Figure 16.1: Smoothed cosine similarity among adjacent sentences in a news article. Local minima at  $m = 10$  and  $m = 29$  indicate likely segmentation points.

### 8547 16.1.1 Topic segmentation

A cohesive topic segment forms a unified whole, using various linguistic devices: repeated references to an entity or event; the use of conjunctions to link related ideas; and the repetition of meaning through lexical choices (Halliday and Hasan, 1976). Each of these cohesive devices can be measured, and then used as features for topic segmentation. A classical example is the use of lexical cohesion in the `TextTiling` method for topic segmentation (Hearst, 1997). The basic idea is to compute the textual similarity between each pair of adjacent blocks of text (sentences or fixed-length units), using a formula such as the smoothed **cosine similarity** of their bag-of-words vectors,

$$s_m = \frac{\mathbf{x}_m \cdot \mathbf{x}_{m+1}}{\|\mathbf{x}_m\|_2 \times \|\mathbf{x}_{m+1}\|_2} \quad [16.1]$$

$$\bar{s}_m = \sum_{\ell=0}^L k_\ell (s_{m+\ell} + s_{m-\ell}), \quad [16.2]$$

8548 with  $k_\ell$  representing the value of a smoothing kernel of size  $L$ , e.g.  $\mathbf{k} = [1, 0.5, 0.25]^\top$ .  
 8549 Segmentation points are then identified at local minima in the smoothed similarities  $\bar{s}$ ,  
 8550 since these points indicate changes in the overall distribution of words in the text. An  
 8551 example is shown in Figure 16.1.

8552 Text segmentation can also be formulated as a probabilistic model, in which each seg-  
 8553 ment has a unique language model that defines the probability over the text in the seg-  
 8554 ment (Utiyama and Isahara, 2001; Eisenstein and Barzilay, 2008; Du et al., 2013).<sup>1</sup> A good

---

<sup>1</sup>There is a rich literature on how latent variable models (such as **latent Dirichlet allocation**) can track

segmentation achieves high likelihood by grouping segments with similar word distributions. This probabilistic approach can be extended to **hierarchical topic segmentation**, in which each topic segment is divided into subsegments (Eisenstein, 2009). All of these approaches are unsupervised. While labeled data can be obtained from well-formatted texts such as textbooks, such annotations may not generalize to speech transcripts in alternative domains. Supervised methods have been tried in cases where in-domain labeled data is available, substantially improving performance by learning weights on multiple types of features (Galley et al., 2003).

### 16.1.2 Functional segmentation

In some genres, there is a canonical set of communicative *functions*: for example, in scientific research articles, one such function is to communicate the general background for the article, another is to introduce a new contribution, or to describe the aim of the research (Teufel et al., 1999). A **functional segmentation** divides the document into contiguous segments, sometimes called **rhetorical zones**, in which each sentence has the same function. Teufel and Moens (2002) train a supervised classifier to identify the functional of each sentence in a set of scientific research articles, using features that describe the sentence's position in the text, its similarity to the rest of the article and title, tense and voice of the main verb, and the functional role of the previous sentence. Functional segmentation can also be performed without supervision. Noting that some types of Wikipedia articles have very consistent functional segmentations (e.g., articles about cities or chemical elements), Chen et al. (2009) introduce an unsupervised model for functional segmentation, which learns both the language model associated with each function and the typical patterning of functional segments across the article.

## 16.2 Entities and reference

Another dimension of discourse relates to which entities are mentioned throughout the text, and how. Consider the examples in Figure 16.2: Grosz et al. (1995) argue that the first discourse is more coherent. Do you agree? The examples differ in their choice of **referring expressions** for the protagonist *John*, and in the syntactic constructions in sentences (b) and (d). The examples demonstrate the need for theoretical models to explain how referring expressions are chosen, and where they are placed within sentences. Such models can then be used to help interpret the overall structure of the discourse, to measure discourse coherence, and to generate discourses in which referring expressions are used coherently.

---

topics across documents (Blei et al., 2003; Blei, 2012).

- |  |   |
|--|---|
| (16.1) a. John went to his favorite music store to buy a piano.<br>b. He had frequented the store for many years.<br>c. He was excited that he could finally buy a piano.<br>d. He arrived just as the store was closing for the day | (16.2) a. John went to his favorite music store to buy a piano.<br>b. It was a store John had frequented for many years.<br>c. He was excited that he could finally buy a piano.<br>d. It was closing just as John arrived. |
|--|---|

Figure 16.2: Two tellings of the same story (Grosz et al., 1995). The discourse on the left uses referring expressions coherently, while the one on the right does not.

### 8588 16.2.1 Centering theory

8589 The relationship between discourse and entity reference is most elaborated in **centering**  
 8590 **theory** (Grosz et al., 1995). According to the theory, every utterance in the discourse is  
 8591 characterized by a set of entities, known as *centers*.

- 8592 • The **forward-looking centers** in utterance  $m$  are all the entities that are mentioned  
 8593 in the utterance,  $c_f(w_m) = \{e_1, e_2, \dots\}$ . The forward-looking centers are partially  
 8594 ordered by their syntactic prominence, favoring subjects over other positions.
- 8595 • The **backward-looking center**  $c_b(w_m)$  is the highest-ranked element in the set of  
 8596 forward-looking centers from the previous utterance  $c_f(w_{m-1})$  that is also men-  
 8597 tioned in  $w_m$ .

8598 Given these two definitions, centering theory makes the following predictions about  
 8599 the form and position of referring expressions:

- 8600 1. If a pronoun appears in the utterance  $w_m$ , then the backward-looking center  $c_b(w_m)$   
 8601 must also be realized as a pronoun. This rule argues against the use of *it* to refer  
 8602 to the piano store in Example (16.2d), since JOHN is the backward looking center of  
 8603 (16.2d), and he is mentioned by name and not by a pronoun.
- 8604 2. Sequences of utterances should retain the same backward-looking center if possible,  
 8605 and ideally, the backward-looking center should also be the top-ranked element in  
 8606 the list of forward-looking centers. This rule argues in favor of the preservation of  
 8607 JOHN as the backward-looking center throughout Example (16.1).

8608 Centering theory unifies aspects of syntax, discourse, and anaphora resolution. However,  
 8609 it can be difficult to clarify exactly how to rank the elements of each utterance, or even  
 8610 how to partition a text or dialog into utterances (Poesio et al., 2004).

	SKYLER	WALTER	DANGER	A GUY	THE DOOR
<i>You don't know who you're talking to,</i>	S	-	-	-	-
<i>so let me clue you in.</i>	O	O	-	-	-
<i>I am not in danger, Skyler.</i>	X	S	X	-	-
<i>I am the danger.</i>	-	S	O	-	-
<i>A guy opens his door and gets shot,</i>	-	-	-	S	O
<i>and you think that of me?</i>	S	X	-	-	-
<i>No. I am the one who knocks!</i>	-	S	-	-	-

Figure 16.3: The entity grid representation for a dialogue from the television show *Breaking Bad*.

### 16.2.2 The entity grid

One way to formalize the ideas of centering theory is to arrange the entities in a text or conversation in an **entity grid**. This is a data structure with one row per sentence, and one column per entity (Barzilay and Lapata, 2008). Each cell  $c(m, i)$  can take the following values:

$$c(m, i) = \begin{cases} S, & \text{entity } i \text{ is in subject position in sentence } m \\ O, & \text{entity } i \text{ is in object position in sentence } m \\ X, & \text{entity } i \text{ appears in sentence } m, \text{ in neither subject nor object position} \\ -, & \text{entity } i \text{ does not appear in sentence } m. \end{cases} \quad [16.3]$$

To populate the entity grid, syntactic parsing is applied to identify subject and object positions, and coreference resolution is applied to link multiple mentions of a single entity. An example is shown in Figure 16.3.

After the grid is constructed, the coherence of a document can be measured by the transitions between adjacent cells in each column. For example, the transition  $(S \rightarrow S)$  keeps an entity in subject position across adjacent sentences; the transition  $(O \rightarrow S)$  promotes an entity from object position to subject position; the transition  $(S \rightarrow -)$  drops the subject of one sentence from the next sentence. The probabilities of each transition can be estimated from labeled data, and an entity grid can then be scored by the sum of the log-probabilities across all columns and all transitions,  $\sum_{i=1}^{N_e} \sum_{m=1}^M \log p(c(m, i) | c(m-1, i))$ . The resulting probability can be used as a proxy for the coherence of a text. This has been shown to be useful for a range of tasks: determining which of a pair of articles is more readable (Schwartz and Ostendorf, 2005), correctly ordering the sentences in a scrambled

8629 text (Lapata, 2003), and disentangling multiple conversational threads in an online multi-  
 8630 party chat (Elsner and Charniak, 2010).

8631 **16.2.3 \*Formal semantics beyond the sentence level**

8632 An alternative view of the role of entities in discourse focuses on formal semantics, and the  
 8633 construction of meaning representations for multi-sentence units. Consider the following  
 8634 two sentences (from Bird et al., 2009):

- 8635 (16.3) a. Angus owns a dog.  
 8636 b. It bit Irene.

8637 We would like to recover the formal semantic representation,

$$\exists x. \text{DOG}(x) \wedge \text{OWN}(\text{ANGUS}, x) \wedge \text{BITE}(x, \text{IRENE}). \quad [16.4]$$

However, the semantic representations of each individual sentence are:

$$\exists x. \text{DOG}(x) \wedge \text{OWN}(\text{ANGUS}, x) \quad [16.5]$$

$$\text{BITE}(y, \text{IRENE}). \quad [16.6]$$

8638 Unifying these two representations into the form of Equation 16.4 requires linking the  
 8639 unbound variable  $y$  from [16.6] with the quantified variable  $x$  in [16.5]. Discourse under-  
 8640 standing therefore requires the reader to update a set of assignments, from variables  
 8641 to entities. This update would (presumably) link the *dog* in the first sentence of [16.3]  
 8642 with the unbound variable  $y$  in the second sentence, thereby licensing the conjunction in  
 8643 [16.4].<sup>2</sup> This basic idea is at the root of **dynamic semantics** (Groenendijk and Stokhof,  
 8644 1991). **Segmented discourse representation theory** links dynamic semantics with a set  
 8645 of **discourse relations**, which explain how adjacent units of text are rhetorically or con-  
 8646 ceptually related (Lascarides and Asher, 2007). The next section explores the theory of  
 8647 discourse relations in more detail.

8648 **16.3 Relations**

8649 In dependency grammar, sentences are characterized by a graph (usually a tree) of syntac-  
 8650 tic relations between words, such as NSUBJ and DET. A similar idea can be applied at the  
 8651 document level, identifying relations between discourse units, such as clauses, sentences,  
 8652 or paragraphs. The task of **discourse parsing** involves identifying discourse units and  
 8653 the relations that hold between them. These relations can then be applied to tasks such as  
 8654 document classification and summarization, as discussed in § 16.3.4.

---

<sup>2</sup>This linking task is similar to coreference resolution (see chapter 15), but here the connections are between semantic variables, rather than spans of text.

- TEMPORAL
  - Asynchronous
  - Synchronous: precedence, succession
- CONTINGENCY
  - Cause: result, reason
  - Pragmatic cause: justification
  - Condition: hypothetical, general, unreal present, unreal past, real present, real past
  - Pragmatic condition: relevance, implicit assertion
- COMPARISON
  - Contrast: juxtaposition, opposition
  - Pragmatic contrast
  - Concession: expectation, contra-expectation
  - Pragmatic concession
- EXPANSION
  - Conjunction
  - Instantiation
  - Restatement: specification, equivalence, generalization
  - Alternative: conjunctive, disjunctive, chosen alternative
  - Exception
  - List

Table 16.1: The hierarchy of discourse relation in the Penn Discourse Treebank annotations (Prasad et al., 2008). For example, PRECEDENCE is a subtype of SYNCHRONOUS, which is a type of TEMPORAL relation.

### 8655 16.3.1 Shallow discourse relations

8656 The existence of discourse relations is hinted by **discourse connectives**, such as *however*,  
 8657 *moreover*, *meanwhile*, and *if ... then*. These connectives explicitly specify the relationship  
 8658 between adjacent units of text: *however* signals a contrastive relationship, *moreover* signals  
 8659 that the subsequent text elaborates or strengthens the point that was made immediately  
 8660 beforehand, *meanwhile* indicates that two events are contemporaneous, and *if ... then* sets  
 8661 up a conditional relationship. Discourse connectives can therefore be viewed as a starting  
 8662 point for the analysis of discourse relations.

8663 In **lexicalized tree-adjoining grammar for discourse (D-LTAG)**, each connective an-  
 8664 chors a relationship between two units of text (Webber, 2004). This model provides the  
 8665 theoretical basis for the **Penn Discourse Treebank (PDTB)**, the largest corpus of discourse  
 8666 relations in English (Prasad et al., 2008). It includes a hierarchical inventory of discourse  
 8667 relations (shown in Table 16.1), which is created by abstracting the meanings implied by  
 8668 the discourse connectives that appear in real texts (Knott, 1996). These relations are then  
 8669 annotated on the same corpus of news text used in the Penn Treebank (see § 9.2.2), adding  
 8670 the following information:

- 8671     • Each connective is annotated for the discourse relation or relations that it expresses,  
   8672        if any — many discourse connectives have senses in which they do not signal a  
   8673        discourse relation (Pitler and Nenkova, 2009).
- 8674     • For each discourse relation, the two arguments of the relation are specified as ARG1  
   8675        and ARG2, where ARG2 is constrained to be adjacent to the connective. These argu-  
   8676        ments may be sentences, but they may also smaller or larger units of text.
- 8677     • Adjacent sentences are annotated for **implicit discourse relations**, which are not  
   8678        marked by any connective. When a connective could be inserted between a pair  
   8679        of sentence, the annotator supplies it, and also labels its sense (e.g., example 16.5).  
   8680        In some cases, there is no relationship at all between a pair of adjacent sentences;  
   8681        in other cases, the only relation is that the adjacent sentences mention one or more  
   8682        shared entity. These phenomena are annotated as NOREL and ENTRREL (entity rela-  
   8683        tion), respectively.

8684     Examples of Penn Discourse Treebank annotations are shown in (16.4). In (16.4), the  
   8685        word *therefore* acts as an explicit discourse connective, linking the two adjacent units of  
   8686        text. The Treebank annotations also specify the “sense” of each relation, linking the con-  
   8687        nective to a relation in the sense inventory shown in Table 16.1: in (16.4), the relation is  
   8688        PRAGMATIC CAUSE:JUSTIFICATION because it relates to the author’s communicative in-  
   8689        tentions. The word *therefore* can also signal causes in the external world (e.g., *He was*  
   8690        *therefore forced to relinquish his plan*). In **discourse sense classification**, the goal is to de-  
   8691        termine which discourse relation, if any, is expressed by each connective. A related task  
   8692        is the classification of implicit discourse relations, as in (16.5). In this example, the re-  
   8693        lationship between the adjacent sentences could be expressed by the connective *because*,  
   8694        indicating a CAUSE:REASON relationship.

### 8695     16.3.1.1 Classifying explicit discourse relations and their arguments

8696     As suggested by the examples above, many connectives can be used to invoke multiple  
   8697        types of discourse relations. Similarly, some connectives have senses that are unrelated  
   8698        to discourse: for example, *and* functions as a discourse connective when it links propo-  
   8699        sitions, but not when it links noun phrases (Lin et al., 2014). Nonetheless, the senses of  
   8700        explicitly-marked discourse relations in the Penn Treebank are relatively easy to classify,  
   8701        at least at the coarse-grained level. When classifying the four top-level PDTB relations,  
   8702        90% accuracy can be obtained simply by selecting the most common relation for each  
   8703        connective (Pitler and Nenkova, 2009). At the more fine-grained levels of the discourse  
   8704        relation hierarchy, connectives are more ambiguous. This fact is reflected both in the ac-  
   8705        curacy of automatic sense classification (Versley, 2011) and in interannotator agreement,  
   8706        which falls to 80% for level-3 discourse relations (Prasad et al., 2008).

- (16.4) *...as this business of whaling has somehow come to be regarded among landsmen as a rather unpoetical and disreputable pursuit; therefore, I am all anxiety to convince ye, ye landsmen, of the injustice hereby done to us hunters of whales.*
- (16.5) But a few funds have taken other defensive steps. *Some have raised their cash positions to record levels. Implicit = BECAUSE High cash positions help buffer a fund when the market falls.*
- (16.6) Michelle lives in a hotel room, and although **she drives a canary-colored Porsche**, *she hasn't time to clean or repair it.*
- (16.7) *Most oil companies, when they set exploration and production budgets for this year, forecast revenue of \$15 for each barrel of crude produced.*

Figure 16.4: Example annotations of discourse relations. In the style of the Penn Discourse Treebank, the discourse connective is underlined, the first argument is shown in italics, and the second argument is shown in bold. Examples (16.5-16.7) are quoted from Prasad et al. (2008).

8707 A more challenging task for explicitly-marked discourse relations is to identify the  
 8708 scope of the arguments. Discourse connectives need not be adjacent to ARG1, as shown  
 8709 in item 16.6, where ARG1 follows ARG2; furthermore, the arguments need not be contigu-  
 8710 ous, as shown in (16.7). For these reasons, recovering the arguments of each discourse  
 8711 connective is a challenging subtask. Because intra-sentential arguments are often syn-  
 8712 tactic constituents (see chapter 10), many approaches train a classifier to predict whether  
 8713 each constituent is an appropriate argument for each explicit discourse connective (Well-  
 8714 ner and Pustejovsky, 2007; Lin et al., 2014, e.g.,).

#### 8715 16.3.1.2 Classifying implicit discourse relations

Implicit discourse relations are considerably more difficult to classify and to annotate.<sup>3</sup> Most approaches are based on an encoding of each argument, which is then used as input to a non-linear classifier:

$$\mathbf{z}^{(i)} = \text{Encode}(\mathbf{w}^{(i)}) \quad [16.7]$$

$$\mathbf{z}^{(i+1)} = \text{Encode}(\mathbf{w}^{(i+1)}) \quad [16.8]$$

$$\hat{y}_i = \underset{y}{\operatorname{argmax}} \Psi(y, \mathbf{z}^{(i)}, \mathbf{z}^{(i+1)}). \quad [16.9]$$

---

<sup>3</sup>In the dataset for the 2015 shared task on shallow discourse parsing, the interannotator agreement was 91% for explicit discourse relations and 81% for non-explicit relations, across all levels of detail (Xue et al., 2015).

8716 This basic framework can be instantiated in several ways, including both feature-based  
 8717 and neural encoders. Several recent approaches are compared in the 2015 and 2016 shared  
 8718 tasks at the Conference on Natural Language Learning (Xue et al., 2015, 2016).

8719 **Feature-based approaches** Each argument can be encoded into a vector of surface fea-  
 8720 tures. The encoding typically includes lexical features (all words, or all content words, or  
 8721 a subset of words such as the first three and the main verb), Brown clusters of individ-  
 8722 ual words (§ 14.4), and syntactic features such as terminal productions and dependency  
 8723 arcs (Pitler et al., 2009; Lin et al., 2009; Rutherford and Xue, 2014). The classification func-  
 8724 tion then has two parts. First, it creates a joint feature vector by combining the encodings  
 8725 of each argument, typically by computing the cross-product of all features in each encod-  
 8726 ing:

$$\mathbf{f}(y, \mathbf{z}^{(i)}, \mathbf{z}^{(i+1)}) = \{(a \times b \times y) : (\mathbf{z}_a^{(i)} \mathbf{z}_b^{(i+1)})\} \quad [16.10]$$

8727 The size of this feature set grows with the square of the size of the vocabulary, so it can be  
 8728 helpful to select a subset of features that are especially useful on the training data (Park  
 8729 and Cardie, 2012). After  $\mathbf{f}$  is computed, any classifier can be trained to compute the final  
 8730 score,  $\Psi(y, \mathbf{z}^{(i)}, \mathbf{z}^{(i+1)}) = \boldsymbol{\theta} \cdot \mathbf{f}(y, \mathbf{z}^{(i)}, \mathbf{z}^{(i+1)})$ .

8731 **Neural network approaches** In neural network architectures, the encoder is learned  
 8732 jointly with the classifier as an end-to-end model. Each argument can be encoded using  
 8733 a variety of neural architectures (surveyed in § 14.8): recursive (§ 10.6.1; Ji and Eisenstein,  
 8734 2015), recurrent (§ 6.3; Ji et al., 2016), and convolutional (§ 3.4; Qin et al., 2017). The clas-  
 8735 sification function can then be implemented as a feedforward neural network on the two  
 8736 encodings (chapter 3; for examples, see Rutherford et al., 2017; Qin et al., 2017), or as a  
 8737 simple bilinear product,  $\Psi(y, \mathbf{z}^{(i)}, \mathbf{z}^{(i+1)}) = (\mathbf{z}^{(i)})^\top \boldsymbol{\Theta}_y \mathbf{z}^{(i+1)}$  (Ji and Eisenstein, 2015). The  
 8738 encoding model can be trained by backpropagation from the classification objective, such  
 8739 as the margin loss. Rutherford et al. (2017) show that neural architectures outperform  
 8740 feature-based approaches in most settings. While neural approaches require engineering  
 8741 the network architecture (e.g., embedding size, number of hidden units in the classifier),  
 8742 feature-based approaches also require significant engineering to incorporate linguistic re-  
 8743 sources such as Brown clusters and parse trees, and to select a subset of relevant features.

### 8744 16.3.2 Hierarchical discourse relations

8745 In sentence parsing, adjacent phrases combine into larger constituents, ultimately pro-  
 8746 ducing a single constituent for the entire sentence. The resulting tree structure enables  
 8747 structured analysis of the sentence, with subtrees that represent syntactically coherent  
 8748 chunks of meaning. **Rhetorical Structure Theory (RST)** extends this style of hierarchical  
 8749 analysis to the discourse level (Mann and Thompson, 1988).

8750        The basic element of RST is the **discourse unit**, which refers to a contiguous span of  
 8751        text. **Elementary discourse units** (EDUs) are the atomic elements in this framework, and  
 8752        are typically (but not always) clauses.<sup>4</sup> Each discourse relation combines two or more  
 8753        adjacent discourse units into a larger, composite discourse unit; this process ultimately  
 8754        unites the entire text into a tree-like structure.<sup>5</sup>

8755        **Nuclearity** In many discourse relations, one argument is primary. For example:

8756        (16.8) [LaShawn loves animals]<sub>N</sub>  
 8757                [She has nine dogs and one pig]<sub>S</sub>

8758        In this example, the second sentence provides EVIDENCE for the point made in the first  
 8759        sentence. The first sentence is thus the **nucleus** of the discourse relation, and the second  
 8760        sentence is the **satellite**. The notion of **nuclearity** is analogous to the head-modifier struc-  
 8761        ture of dependency parsing (see § 11.1.1). However, in RST, some relations have multiple  
 8762        nuclei. For example, the arguments of the CONTRAST relation are equally important:

8763        (16.9) [The clash of ideologies survives this treatment]<sub>N</sub>  
 8764                [but the nuance and richness of Gorky's individual characters have vanished in the scuffle]<sub>N</sub><sup>6</sup>

8765        Relations that have multiple nuclei are called **coordinating**; relations with a single nu-  
 8766        cleus are called **subordinating**. Subordinating relations are constrained to have only two  
 8767        arguments, while coordinating relations (such as CONJUNCTION) may have more than  
 8768        two.

8769        **RST Relations** Rhetorical structure theory features a large inventory of discourse rela-  
 8770        tions, which are divided into two high-level groups: subject matter relations, and presen-  
 8771        tational relations. Presentational relations are organized around the intended beliefs of  
 8772        the reader. For example, in (16.8), the second discourse unit provides evidence intended  
 8773        to increase the reader's belief in the proposition expressed by the first discourse unit, that  
 8774        *LaShawn loves animals*. In contrast, subject-matter relations are meant to communicate ad-  
 8775        ditional facts about the propositions contained in the discourse units that they relate:

---

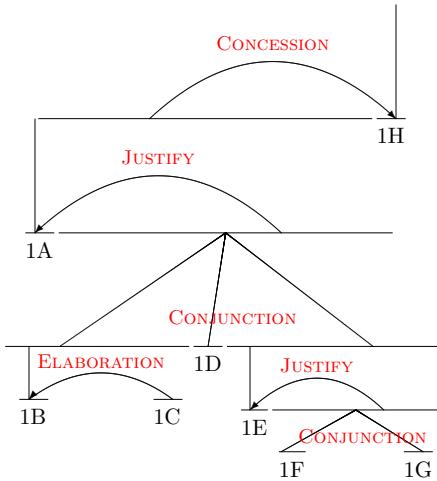
<sup>4</sup>Details of discourse segmentation can be found in the RST annotation manual (Carlson and Marcu, 2001).

<sup>5</sup>While RST analyses are typically trees, this should be taken as a strong theoretical commitment to the principle that all coherent discourses have a tree structure. Taboada and Mann (2006) write:

It is simply the case that trees are convenient, easy to represent, and easy to understand. There is, on the other hand, no theoretical reason to assume that trees are the only possible representation of discourse structure and of coherence relations.

The appropriateness of tree structures to discourse has been challenged, e.g., by Wolf and Gibson (2005), who propose a more general graph-structured representation.

<sup>6</sup>from the RST Treebank (Carlson et al., 2002)



[It could have been a great movie]<sup>1A</sup> [It does have beautiful scenery,]<sup>1B</sup> [some of the best since Lord of the Rings.]<sup>1C</sup> [The acting is well done,]<sup>1D</sup> [and I really liked the son of the leader of the Samurai.]<sup>1E</sup> [He was a likable chap,]<sup>1F</sup> [and I hated to see him die.]<sup>1G</sup> [But, other than all that, this movie is nothing more than hidden rip-offs.]<sup>1H</sup>

Figure 16.5: A rhetorical structure theory analysis of a short movie review, adapted from Voll and Taboada (2007). Positive and negative sentiment words are underlined, indicating RST’s potential utility in document-level sentiment analysis.

8776 (16.10) [the debt plan was rushed to completion]<sub>N</sub>  
 8777 [in order to be announced at the meeting]<sub>S</sub><sup>7</sup>

8778 In this example, the satellite describes a world state that is realized by the action described  
 8779 in the nucleus. This relationship is about the world, and not about the author’s commu-  
 8780 nicative intentions.

8781 **Example** Figure 16.5 depicts an RST analysis of a paragraph from a movie review. Asym-  
 8782 metric (subordinating) relations are depicted with an arrow from the satellite to the nu-  
 8783 cleus; symmetric (coordinating) relations are depicted with lines. The elementary dis-  
 8784 course units 1F and 1G are combined into a larger discourse unit with the symmetric  
 8785 CONJUNCTION relation. The resulting discourse unit is then the satellite in a JUSTIFY  
 8786 relation with 1E.

<sup>7</sup>from the RST Treebank (Carlson et al., 2002)

8787 **16.3.2.1 Hierarchical discourse parsing**

8788 The goal of discourse parsing is to recover a hierarchical structural analysis from a doc-  
 8789 ument text, such as the analysis in Figure 16.5. For now, let's assume a segmentation  
 8790 of the document into elementary discourse units (EDUs); segmentation algorithms are  
 8791 discussed below. After segmentation, discourse parsing can be viewed as a combination  
 8792 of two components: the discourse relation classification techniques discussed in § 16.3.1.2,  
 8793 and algorithms for phrase-structure parsing, such as chart parsing and shift-reduce, which  
 8794 were discussed in chapter 10.

8795 Both chart parsing and shift-reduce require encoding composite discourse units, ei-  
 8796 ther in a discrete feature vector or a dense neural representation.<sup>8</sup> Some discourse parsers  
 8797 rely on the **strong compositionality criterion** (Marcu, 1996), which states the assumption  
 8798 that a composite discourse unit can be represented by its nucleus. This criterion is used in  
 8799 feature-based discourse parsing to determine the feature vector for a composite discourse  
 8800 unit (Hernault et al., 2010); it is used in neural approaches to setting the vector encod-  
 8801 ing for a composite discourse unit equal to the encoding of its nucleus (Ji and Eisenstein,  
 8802 2014). An alternative neural approach is to learn a composition function over the compo-  
 8803 nents of a composite discourse unit (Li et al., 2014), using a recursive neural network (see  
 8804 § 14.8.3).

8805 **Bottom-up discourse parsing** Assume a segmentation of the text into  $N$  elementary  
 8806 discourse units with base representations  $\{z^{(i)}\}_{i=1}^N$ , and assume a composition function  
 8807 COMPOSE  $(z^{(i)}, z^{(j)}, \ell)$ , which maps two encodings and a discourse relation  $\ell$  into a new  
 8808 encoding. The composition function can follow the strong compositionality criterion and  
 8809 simply select the encoding of the nucleus, or it can do something more complex. We  
 8810 also need a scoring function  $\Psi(z^{(i,k)}, z^{(k,j)}, \ell)$ , which computes a scalar score for the (bi-  
 8811 narized) discourse relation  $\ell$  with left child covering the span  $i + 1 : k$ , and the right  
 8812 child covering the span  $k + 1 : j$ . Given these components, we can construct vector rep-  
 8813 resentations for each span, and this is the basic idea underlying **compositional vector**  
 8814 **grammars** (Socher et al., 2013).

8815 These same components can also be used in bottom-up parsing, in a manner that is  
 8816 similar to the CKY algorithm for weighted context-free grammars (see § 10.1): compute  
 8817 the score and best analysis for each possible span of increasing lengths, while storing  
 8818 back-pointers that make it possible to recover the optimal parse of the entire input. How-  
 8819 ever, there is an important distinction from CKY parsing: for each labeled span  $(i, j, \ell)$ , we  
 8820 must use the composition function to construct a representation  $z^{(i,j,\ell)}$ . This representa-  
 8821 tion is then used to combine the discourse unit spanning  $i + 1 : j$  in higher-level discourse  
 8822 relations. The representation  $z^{(i,j,\ell)}$  depends on the entire substructure of the unit span-

---

<sup>8</sup>To use these algorithms, is also necessary to binarize all discourse relations during parsing, and then to “unbinarize” them to reconstruct the desired structure (e.g., Hernault et al., 2010).

8823 ning  $i + 1 : j$ , and this violates the locality assumption that underlie CKY’s optimality  
 8824 guarantee. Bottom-up parsing with recursively constructed span representations is gen-  
 8825 erally not guaranteed to find the best-scoring discourse parse. This problem is explored  
 8826 in an exercise at the end of the chapter.

8827 **Transition-based discourse parsing** One drawback of bottom-up parsing is its cubic  
 8828 time complexity in the length of the input. For long documents, transition-based parsing  
 8829 is an appealing alternative. The shift-reduce algorithm can be applied to discourse parsing  
 8830 fairly directly (Sagae, 2009): the stack stores a set of discourse units and their repres-  
 8831 entations, and each action is chosen by a function of these representations. This function  
 8832 could be a linear product of weights and features, or it could be a neural network ap-  
 8833 plied to encodings of the discourse units. The REDUCE action then performs composition  
 8834 on the two discourse units at the top of the stack, yielding a larger composite discourse  
 8835 unit, which goes on top of the stack. All of the techniques for integrating learning and  
 8836 transition-based parsing, described in § 11.3, are applicable to discourse parsing.

### 8837 16.3.2.2 Segmenting discourse units

8838 In rhetorical structure theory, elementary discourse units do not cross the sentence bound-  
 8839 ary, so discourse segmentation can be performed within sentences, assuming the sentence  
 8840 segmentation is given. The segmentation of sentences into elementary discourse units is  
 8841 typically performed using features of the syntactic analysis (Braud et al., 2017). One ap-  
 8842 proach is to train a classifier to determine whether each syntactic constituent is an EDU,  
 8843 using features such as the production, tree structure, and head words (Soricut and Marcu,  
 8844 2003; Hernault et al., 2010). Another approach is to train a sequence labeling model, such  
 8845 as a conditional random field (Sporleder and Lapata, 2005; Xuan Bach et al., 2012; Feng  
 8846 et al., 2014). This is done using the BIO formalism for segmentation by sequence labeling,  
 8847 described in § 8.3.

### 8848 16.3.3 Argumentation

8849 An alternative view of text-level relational structure focuses on **argumentation** (Stab and  
 8850 Gurevych, 2014b). Each segment (typically a sentence or clause) may support or rebut  
 8851 another segment, creating a graph structure over the text. In the following example (from  
 8852 Peldszus and Stede, 2013), segment  $S_2$  provides argumentative support for the proposi-  
 8853 tion in the segment  $S_1$ :

8854 (16.11) [We should tear the building down] $_{S1}$   
 8855 [because it is full of asbestos] $_{S2}$ .

8856 Assertions may also support or rebut proposed links between two other assertions, cre-  
 8857 ating a **hypergraph**, which is a generalization of a graph to the case in which edges can

8858 join any number of vertices. This can be seen by introducing another sentence into the  
8859 example:

8860 (16.12) [In principle it is possible to clean it up.]<sub>S3</sub>  
8861 [but according to the mayor that is too expensive.]<sub>S4</sub>

8862 S3 acknowledges the validity of *S2*, but **undercuts** its support of *S1*. This can be repre-  
8863 sented by introducing a hyperedge,  $(S3, S2, S1)_{\text{undercut}}$ , indicating that *S3* undercuts the  
8864 proposed relationship between *S2* and *S1*. *S4* then undercuts the relevance of *S3*.

8865 **Argumentation mining** is the task of recovering such structures from raw texts. At  
8866 present, annotations of argumentation structure are relatively small: Stab and Gurevych  
8867 (2014a) have annotated a collection of 90 persuasive essays, and Peldszus and Stede (2015)  
8868 have solicited and annotated a set of 112 paragraph-length “microtexts” in German.

#### 8869 16.3.4 Applications of discourse relations

8870 The predominant application of discourse parsing is to select content within a document.  
8871 In rhetorical structure theory, the nucleus is considered the more important element of  
8872 the relation, and is more likely to be part of a summary of the document; it may also  
8873 be more informative for document classification. The D-LTAG theory that underlies the  
8874 Penn Discourse Treebank lacks this notion of nuclearity, but arguments may have varying  
8875 importance, depending on the relation type. For example, the span of text constituting  
8876 ARG1 of an expansion relation is more likely to appear in a summary, while the sentence  
8877 constituting ARG2 of an implicit relation is less likely (Louis et al., 2010). Discourse rela-  
8878 tions may also signal segmentation points in the document structure. Explicit discourse  
8879 markers have been shown to correlate with changes in subjectivity, and identifying such  
8880 change points can improve document-level sentiment classification, by helping the clas-  
8881 sifier to focus on the subjective parts of the text (Trivedi and Eisenstein, 2013; Yang and  
8882 Cardie, 2014).

##### 8883 16.3.4.1 Extractive Summarization

8884 Text **summarization** is the problem of converting a longer text into a shorter one, while  
8885 still conveying the key facts, events, ideas, and sentiments from the original. In **extractive**  
8886 **summarization**, the summary is a subset of the original text; in **abstractive summariza-**  
8887 **tion**, the summary is produced *de novo*, by paraphrasing the original, or by first encoding  
8888 it into a semantic representation (see § 19.2). The main strategy for extractive summa-  
8889 rization is to maximize **coverage**, choosing a subset of the document that best covers the  
8890 concepts mentioned in the document as a whole; typically, coverage is approximated by  
8891 bag-of-words overlap (Nenkova and McKeown, 2012). Coverage-based objectives can be  
8892 supplemented by hierarchical discourse relations, using the principle of nuclearity: in any  
8893 subordinating discourse relation, the nucleus is more critical to the overall meaning of the

8894 text, and is therefore more important to include in an extractive summary (Marcu, 1997a).<sup>9</sup>  
 8895 This insight can be generalized from individual relations using the concept of **discourse**  
 8896 **depth** (Hirao et al., 2013): for each elementary discourse unit  $e$ , the discourse depth  $d_e$  is  
 8897 the number of relations in which a discourse unit containing  $e$  is the satellite.

8898 Both discourse depth and nuclearity can be incorporated into extractive summarization  
 8899 using constrained optimization. Let  $\mathbf{x}_n$  be a bag-of-words vector representation of  
 8900 elementary discourse unit  $n$ , let  $y_n \in \{0, 1\}$  indicate whether  $n$  is included in the summary,  
 8901 and let  $d_n$  be the depth of unit  $n$ . Furthermore, let each discourse unit have a “head”  $h$ ,  
 8902 which is defined recursively:

- 8903 • if a discourse unit is produced by a subordinating relation, then its head is the head  
 8904 of the (unique) nucleus;
- 8905 • if a discourse unit is produced by a coordinating relation, then its head is the head  
 8906 of the left-most nucleus;
- 8907 • for each elementary discourse unit, its parent  $\pi(n) \in \{\emptyset, 1, 2, \dots, N\}$  is the head of  
 8908 the smallest discourse unit containing  $n$  whose head is not  $n$ ;
- 8909 • if  $n$  is the head of the discourse unit spanning the whole document, then  $\pi(n) = \emptyset$ .

With these definitions in place, discourse-driven extractive summarization can be formalized as (Hirao et al., 2013),

$$\begin{aligned} & \max_{\mathbf{y}=\{0,1\}^N} \sum_{n=1}^N y_n \frac{\Psi(\mathbf{x}_n, \{\mathbf{x}_{1:N}\})}{d_n} \\ & \text{s.t. } \sum_{n=1}^N y_n \left( \sum_{j=1}^V x_{n,j} \right) \leq L \\ & \quad y_{\pi(n)} \geq y_n, \quad \forall n \text{ s.t. } \pi(n) \neq \emptyset \end{aligned} \tag{16.11}$$

8910 where  $\Psi(\mathbf{x}_n, \{\mathbf{x}_{1:N}\})$  measures the coverage of elementary discourse unit  $n$  with respect  
 8911 to the rest of the document, and  $\sum_{j=1}^V x_{n,j}$  is the number of tokens in  $\mathbf{x}_n$ . The first con-  
 8912 straint ensures that the number of tokens in the summary has an upper bound  $L$ . The  
 8913 second constraint ensures that no elementary discourse unit is included unless its parent  
 8914 is also included. In this way, the discourse structure is used twice: to downweight the  
 8915 contributions of elementary discourse units that are not central to the discourse, and to  
 8916 ensure that the resulting structure is a subtree of the original discourse parse. The opti-

---

<sup>9</sup>Conversely, the arguments of a multi-nuclear relation should either both be included in the summary, or both excluded (Durrett et al., 2016).

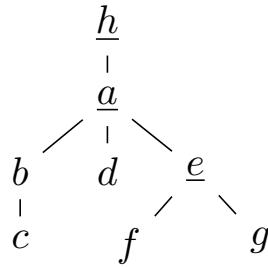


Figure 16.6: A **discourse depth tree** (Hirao et al., 2013) for the discourse parse from Figure 16.5, in which each elementary discourse unit is connected to its parent. The discourse units in one valid summary are underlined.

8917 mization problem in 16.11 can be solved with **integer linear programming**, described in  
 8918 § 13.2.2.<sup>10</sup>

8919 Figure 16.6 shows a **discourse depth tree** for the RST analysis from Figure 16.5, in  
 8920 which each elementary discourse is connected to (and below) its parent. The underlined  
 8921 discourse units in the figure constitute the following summary:

8922 (16.13) It could have been a great movie, and I really liked the son of the leader of the  
 8923 Samurai. But, other than all that, this movie is nothing more than hidden rip-offs.

#### 8924 16.3.4.2 Document classification

8925 Hierarchical discourse structures lend themselves naturally to text classification: in a sub-  
 8926 ordinating discourse relation, the nucleus should play a stronger role in the classification  
 8927 decision than the satellite. Various implementations of this idea have been proposed.

- 8928 • Focusing on within-sentence discourse relations and lexicon-based classification (see  
 8929 § 4.1.2), Voll and Taboada (2007) simply ignore the text in the satellites of each dis-  
 8930 course relation.
- 8931 • At the document level, elements of each discourse relation argument can be reweighted,  
 8932 favoring words in the nucleus, and disfavoring words in the satellite (Heerschop  
 8933 et al., 2011; Bhatia et al., 2015). This approach can be applied recursively, computing  
 8934 weights across the entire document. The weights can be relation-specific, so that the  
 8935 features from the satellites of contrastive relations are discounted or even reversed.
- 8936 • Alternatively, the hierarchical discourse structure can define the structure of a **re-  
 8937 cursive neural network** (see § 10.6.1). In this network, the representation of each

---

<sup>10</sup>Formally, 16.11 is a special case of the **knapsack problem**, in which the goal is to find a subset of items with maximum value, constrained by some maximum weight (Cormen et al., 2009).

8938 discourse unit is computed from its arguments and from a parameter corresponding  
 8939 to the discourse relation (Ji and Smith, 2017).

8940 Shallow, non-hierarchical discourse relations have also been applied to document clas-  
 8941 sification. One approach is to impose a set of constraints on the analyses of individual  
 8942 discourse units, so that adjacent units have the same polarity when they are connected  
 8943 by a discourse relation indicating agreement, and opposite polarity when connected by a  
 8944 contrastive discourse relation, indicating disagreement (Somasundaran et al., 2009; Zirn  
 8945 et al., 2011). Yang and Cardie (2014) apply explicitly-marked relations from the Penn  
 8946 Discourse Treebank to the problem of sentence-level sentiment polarity classification (see  
 8947 § 4.1). They impose the following soft constraints:

- 8948 • When a CONTRAST relation appears at the beginning of a sentence, the sentence  
 8949 should have the opposite sentiment polarity as its predecessor.
- 8950 • When an EXPANSION or CONTINGENCY appears at the beginning of a sentence, it  
 8951 should have the same polarity as its predecessor.
- 8952 • When a CONTRAST relation appears *within* a sentence, the sentence should have  
 8953 neutral polarity, since it is likely to express both sentiments.

8954 These discourse-driven constraints are shown to improve performance on two datasets of  
 8955 product reviews.

#### 8956 16.3.4.3 Coherence

8957 Just as **grammaticality** is the property shared by well-structured sentences, **coherence** is  
 8958 the property shared by well-structured discourses. One application of discourse process-  
 8959 ing is to measure (and maximize) the coherence of computer-generated texts like transla-  
 8960 tions and summaries (Kibble and Power, 2004). Coherence assessment is also used to eval-  
 8961 uate human-generated texts, such as student essays (e.g., Miltsakaki and Kukich, 2004;  
 8962 Burstein et al., 2013).

8963 Coherence subsumes a range of phenomena, many of which have been highlighted  
 8964 earlier in this chapter: e.g., that adjacent sentences should be lexically cohesive (Foltz  
 8965 et al., 1998; Ji et al., 2015; Li and Jurafsky, 2017), and that entity references should follow  
 8966 the principles of centering theory (Barzilay and Lapata, 2008; Nguyen and Joty, 2017).  
 8967 Discourse relations also bear on the coherence of a text in a variety of ways:

- 8968 • Hierarchical discourse relations tend to have a “canonical ordering” of the nucleus  
 8969 and satellite (Mann and Thompson, 1988): for example, in the ELABORATION rela-  
 8970 tion from rhetorical structure theory, the nucleus always comes first, while in the  
 8971 JUSTIFICATION relation, the satellite tends to be first (Marcu, 1997b).

- Discourse relations should be signaled by connectives that are appropriate to the semantic or functional relationship between the arguments: for example, a coherent text would be more likely to use *however* to signal a COMPARISON relation than a *temporal* relation (Kibble and Power, 2004).
- Discourse relations tend to appear in predictable sequences: for example, COMPARISON relations tend to immediately precede CONTINGENCY relations (Pitler et al., 2008). This observation can be formalized by generalizing the entity grid model (§ 16.2.2), so that each cell  $(i, j)$  provides information about the role of the discourse argument containing a mention of entity  $j$  in sentence  $i$  (Lin et al., 2011). For example, if the first sentence is ARG1 of a comparison relation, then any entity mentions in the sentence would be labeled COMP.ARG1. This approach can also be applied to RST discourse relations (Feng et al., 2014).

**Datasets** One difficulty with evaluating metrics of discourse coherence is that human-generated texts usually meet some minimal threshold of coherence. For this reason, much of the research on measuring coherence has focused on synthetic data. A typical setting is to permute the sentences of a human-written text, and then determine whether the original sentence ordering scores higher according to the proposed coherence measure (Barzilay and Lapata, 2008). There are also small datasets of human evaluations of the coherence of machine summaries: for example, human judgments of the summaries from the participating systems in the 2003 Document Understanding Conference are available online.<sup>11</sup> Researchers from the Educational Testing Service (an organization which administers several national exams in the United States) have studied the relationship between discourse coherence and student essay quality (Burstein et al., 2003, 2010). A public dataset of essays from second-language learners, with quality annotations, has been made available by researchers at Cambridge University (Yannakoudakis et al., 2011). At the other extreme, Louis and Nenkova (2013) analyze the structure of professionally written scientific essays, finding that discourse relation transitions help to distinguish prize-winning essays from other articles in the same genre.

## Additional resources

For a manuscript-length discussion of discourse processing, see Stede (2011). Article-length surveys are offered by Webber et al. (2012) and Webber and Joshi (2012).

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<sup>11</sup><http://homepages.inf.ed.ac.uk/mlap/coherence/>

## 9003 Exercises

- 9004 1. One way to formulate text segmentation as a probabilistic model is through the use  
 9005 of the Dirichlet compound Multinomial (DCM) distribution, which computes the probability  
 9006 of a bag-of-words,  $\text{DCM}(\mathbf{x}; \boldsymbol{\alpha})$ , where  $\boldsymbol{\alpha}$  is a parameter,  $\boldsymbol{\alpha} \in \mathbb{R}_+^V$ . This  
 9007 distribution can be configured to assign high likelihood to bag-of-words vectors that  
 9008 are internally coherent, such that individual words appear repeatedly: for example,  
 9009 this behavior can be observed for simple parameterizations, such as  $\boldsymbol{\alpha} = \{\alpha_i\}_{i=1}^V$ .  
 Let  $\psi_\alpha(i, j)$  represent the log-probability of a segment  $w_{i+1:j}$  under a DCM distribution  
 with parameter  $\boldsymbol{\alpha}$ . Give a dynamic program for segmenting a text into a total of  $K$  segments  
 maximizing the sum of log-probabilities  $\sum_{k=1}^K \psi_\alpha(s_{k-1}, s_k)$ , where  $s_k$  indexes the last token of segment  $k$ , and  $s_0 = 0$ . The time complexity of your  
 dynamic program should not be worse than quadratic in the length of the input and  
 linear in the number of segments.
- 9016 2. Building on the previous problem, you will now adapt the CKY algorithm to per-  
 9017 form hierarchical segmentation. Define a hierarchical segmentation as a set of seg-  
 9018 mentations  $\{\{s_k^{(\ell)}\}_{k=1}^{K^{(\ell)}}\}_{\ell=1}^L$ , where  $L$  is the segmentation depth. To ensure that the  
 9019 segmentation is hierarchically valid, we require that each segmentation point  $s_k^{(\ell)}$   
 9020 at level  $\ell$  is also a segmentation point at level  $\ell - 1$ , where  $\ell > 1$ . We will focus  
 9021 on binary hierarchical segmentation, so that each segment at level  $\ell > 1$  has ex-  
 9022 actly 2 subsegments. Define the score of a hierarchical segmentation as the sum of  
 9023 the scores of all segments (at all levels), using the the DCM log-probabilities from  
 9024 the previous problem as the segment scores. Give a CKY-like recurrence such that  
 9025 the optimal “parse” of the text is the maximum log-probability binary segmentation  
 9026 with exactly  $L$  levels.
- 9027 3. In this exercise, you will produce a figure similar to Figure 16.1.
  - 9028 a) Implement the smoothed cosine similarity metric from Equation 16.2, using the  
   9029 smoothing kernel  $\mathbf{k} = [.5, .3, .15, .05]$ .
  - 9030 b) Download the text of a news article with at least ten paragraphs.
  - 9031 c) Compute and plot the smoothed similarity  $\bar{s}$  over the length of the article.
  - 9032 d) Identify *local minima* in  $\bar{s}$  as follows: first find all sentences  $m$  such that  $\bar{s}_m <$   
   9033  $\bar{s}_{m \pm 1}$ . Then search among these points to find the five sentences with the lowest  
   9034  $\bar{s}_m$ .
  - 9035 e) How often do the five local minima correspond to paragraph boundaries?
    - 9036 • The fraction of local minima that are paragraph boundaries is the **precision-**  
   9037 **at- $k$** , where in this case,  $k = 5$ .

- 9038     • The fraction of paragraph boundaries which are local minima is the **recall-**  
9039       **at- $k$ .**  
9040     • Compute precision-at- $k$  and recall-at- $k$  for  $k = 3$  and  $k = 10$ .

- 9041     4. This exercise is to be done in pairs. Each participant selects an article from to-  
9042       day's news, and replaces all mentions of individual people with special tokens like  
9043       PERSON1, PERSON2, and so on. The other participant should then use the rules  
9044       of centering theory to guess each type of referring expression: full name (*Captain*  
9045       *Ahab*), partial name (e.g., *Ahab*), nominal (e.g., *the ship's captain*), or pronoun. Check  
9046       whether the predictions match the original text, and whether the text conforms to  
9047       the rules of centering theory.
- 9048     5. The entity grid representation of centering theory can be used to compute a score for  
9049       adjacent sentences, as described in § 16.2.2. Given a set of sentences, these scores can  
9050       be used to compute an optimal ordering. Show that finding the ordering with the  
9051       maximum log probability is NP-complete, by reduction from a well-known prob-  
9052       lem.
- 9053     6. Some discourse connectives tend to occur between their arguments; others can pre-  
9054       cede both arguments, and a few can follow both arguments. Indicate whether the  
9055       following connectives can occur between, before, and after their arguments: *how-  
9056       ever*, *but*, *while* (contrastive, not temporal), *although*, *therefore*, *nonetheless*.
- 9057     7. In § 16.3.2.1, it is noted that bottom-up parsing with compositional vector represen-  
9058       tations of each span is not guaranteed to be optimal. In this exercise, you will con-  
9059       struct a minimal example proving this point. Consider a discourse with four units,  
9060       with base representations  $\{z^{(i)}\}_{i=1}^4$ . Construct a scenario in which the parse selected  
9061       by bottom-up parsing is not optimal, and give the precise mathematical conditions  
9062       under which this suboptimal parse is selected. You may ignore the relation labels  $\ell$   
9063       for the purpose of this example.
- 9064     8. As noted in § 16.3.3, arguments can described by hypergraphs, in which a segment  
9065       may **undercut** a proposed edge between two other segments. Extend the model of  
9066       extractive summarization described in § 16.3.4.1 to arguments, adding the follwoing  
9067       constraint: if segment  $i$  undercuts an argumentative relationship between  $j$  and  $k$ ,  
9068       then  $i$  cannot be included in the summary unless both  $j$  and  $k$  are included. Your sol-  
9069       ution should take the form of a set of *linear* constraints on an integer linear program  
9070       — that is, each constraint can only involve addition and subtraction of variables.

9071     In the next two exercises, you will explore the use of discourse connectives in a real corpus.  
9072     Using `nltk`, acquire the Brown corpus, and identify sentences that begin with any of the  
9073     following connectives: *however*, *nevertheless*, *moreover*, *furthermore*, *thus*.

9074     9. Both lexical consistency and discourse connectives contribute to the **cohesion** of a  
9075       text. We might therefore expect adjacent sentences that are joined by explicit dis-  
9076       course connectives to also have higher word overlap. Using the Brown corpus, test  
9077       this theory by computing the average cosine similarity between adjacent sentences  
9078       that are connected by one of the connectives mentioned above. Compare this to the  
9079       average cosine similarity of all other adjacent sentences. If you know how, perform  
9080       a two-sample t-test to determine whether the observed difference is statistically sig-  
9081       nificant.

9082     10. Group the above connectives into the following three discourse relations:

- 9083       • Expansion: *moreover, furthermore*  
9084       • Comparison: *however, nevertheless*  
9085       • Contingency: *thus*

9086     Focusing on pairs of sentences which are joined by one of these five connectives,  
9087       build a classifier to predict the discourse relation from the text of the two adjacent  
9088       sentences — taking care to ignore the connective itself. Use the first 30000 sentences  
9089       of the Brown corpus as the training set, and the remaining sentences as the test  
9090       set. Compare the performance of your classifier against simply choosing the most  
9091       common class. Using a bag-of-words classifier, it is hard to do much better than this  
9092       baseline, so consider alternatives!

9093

## **Part IV**

9094

# **Applications**



## 9095 Chapter 17

# 9096 Information extraction

9097 Computers offer powerful capabilities for searching and reasoning about structured records  
9098 and relational data. Some even argue that the most important limitation of artificial intel-  
9099 ligence is not inference or learning, but simply having too little knowledge (Lenat et al.,  
9100 1990). Natural language processing provides an appealing solution: automatically con-  
9101 struct a structured **knowledge base** by reading natural language text.

9102 For example, many Wikipedia pages have an “infobox” that provides structured in-  
9103 formation about an entity or event. An example is shown in Figure 17.1a: each row rep-  
9104 resents one or more properties of the entity IN THE AEROPLANE OVER THE SEA, a record  
9105 album. The set of properties is determined by a predefined **schema**, which applies to all  
9106 record albums in Wikipedia. As shown in Figure 17.1b, the values for many of these fields  
9107 are indicated directly in the first few sentences of text on the same Wikipedia page.

9108 The task of automatically constructing (or “populating”) an infobox from text is an  
9109 example of **information extraction**. Much of information extraction can be described in  
9110 terms of **entities**, **relations**, and **events**.

- 9111 • **Entities** are uniquely specified objects in the world, such as people (JEFF MANGUM),  
9112 places (ATHENS, GEORGIA), organizations (MERGE RECORDS), and times (FEBRUARY  
9113 10, 1998). Chapter 8 described the task of **named entity recognition**, which labels  
9114 tokens as parts of entity spans. Now we will see how to go further, **linking** each  
9115 entity **mention** to an element in a **knowledge base**.
- 9116 • **Relations** include a **predicate** and two **arguments**: for example, CAPITAL(GEORGIA, ATLANTA).
- **Events** involve multiple typed arguments. For example, the production and release

Studio album by Neutral Milk Hotel	
<b>Released</b>	February 10, 1998
<b>Recorded</b>	July–September 1997
<b>Studio</b>	Pet Sounds Studio, Denver, Colorado
<b>Genre</b>	Indie rock • psychedelic folk • lo-fi
<b>Length</b>	39:55
<b>Label</b>	Merge • Domino
<b>Producer</b>	Robert Schneider

(a) A Wikipedia infobox

- (17.1) In the Aeroplane Over the Sea is the second and final studio album by the American indie rock band Neutral Milk Hotel.
- (17.2) It was released in the United States on February 10, 1998 on Merge Records and May 1998 on Blue Rose Records in the United Kingdom.
- (17.3) Jeff Mangum moved from Athens, Georgia to Denver, Colorado to prepare the bulk of the album's material with producer Robert Schneider, this time at Schneider's newly created Pet Sounds Studio at the home of Jim McIntyre.

- (b) The first few sentences of text. Strings that match fields or field names in the infobox are underlined; strings that mention other entities are wavy underlined.

Figure 17.1: From the Wikipedia page for the album “In the Aeroplane Over the Sea”, retrieved October 26, 2017.

of the album described in Figure 17.1 is described by the event,

```
<TITLE : IN THE AEROPLANE OVER THE SEA,
ARTIST : NEUTRAL MILK HOTEL,
RELEASE-DATE : 1998-FEB-10,...>
```

9117     The set of arguments for an event type is defined by a **schema**. Events often refer to  
 9118     time-delimited occurrences: weddings, protests, purchases, terrorist attacks.

9119     Information extraction is similar to semantic role labeling (chapter 13): we may think  
 9120     of predicates as corresponding to events, and the arguments as defining slots in the event  
 9121     representation. However, the goals of information extraction are different. Rather than  
 9122     accurately parsing every sentence, information extraction systems often focus on recog-  
 9123     nizing a few key relation or event types, or on the task of identifying all properties of a  
 9124     given entity. Information extraction is often evaluated by the correctness of the resulting  
 9125     knowledge base, and not by how many sentences were accurately parsed. The goal is  
 9126     sometimes described as **macro-reading**, as opposed to **micro-reading**, in which each sen-  
 9127     tence must be analyzed correctly. Macro-reading systems are not penalized for ignoring  
 9128     difficult sentences, as long as they can recover the same information from other, easier-  
 9129     to-read sources. However, macro-reading systems must resolve apparent inconsistencies

9130 (was the album released on MERGE RECORDS or BLUE ROSE RECORDS?), requiring reasoning across the entire dataset.

9132 In addition to the basic tasks of recognizing entities, relations, and events, information  
9133 extraction systems must handle negation, and must be able to distinguish statements of  
9134 fact from hopes, fears, hunches, and hypotheticals. Finally, information extraction is often paired with the problem of **question answering**, which requires accurately parsing a  
9135 query, and then selecting or generating a textual answer. Question answering systems can  
9136 be built on knowledge bases that are extracted from large text corpora, or may attempt to  
9137 identify answers directly from the source texts.

## 9139 17.1 Entities

9140 The starting point for information extraction is to identify mentions of entities in text.  
9141 Consider the following example:

9142 (17.4) *The United States Army captured a hill overlooking Atlanta on May 14, 1864.*

9143 For this sentence, there are two goals:

- 9144 1. *Identify* the spans *United States Army*, *Atlanta*, and *May 14, 1864* as entity mentions.  
9145 (The hill is not uniquely identified, so it is not a *named* entity.) We may also want to  
9146 recognize the **named entity types**: organization, location, and date. This is **named**  
9147 **entity recognition**, and is described in chapter 8.
- 9148 2. *Link* these spans to entities in a knowledge base: U.S. ARMY, ATLANTA, and 1864-  
9149 MAY-14. This task is known as **entity linking**.

9150 The strings to be linked to entities are **mentions** — similar to the use of this term in  
9151 coreference resolution. In some formulations of the entity linking task, only named entities  
9152 are candidates for linking. This is sometimes called **named entity linking** (Ling et al.,  
9153 2015). In other formulations, such as **Wikification** (Milne and Witten, 2008), any string  
9154 can be a mention. The set of target entities often corresponds to Wikipedia pages, and  
9155 Wikipedia is the basis for more comprehensive knowledge bases such as YAGO (Suchanek  
9156 et al., 2007), DBPedia (Auer et al., 2007), and Freebase (Bollacker et al., 2008). Entity link-  
9157 ing may also be performed in more “closed” settings, where a much smaller list of targets  
9158 is provided in advance. The system must also determine if a mention does not refer to  
9159 any entity in the knowledge base, sometimes called a **NIL entity** (McNamee and Dang,  
9160 2009).

9161 Returning to (17.4), the three entity mentions may seem unambiguous. But the Wikipedia  
9162 disambiguation page for the string *Atlanta* says otherwise:<sup>1</sup> there are more than twenty

<sup>1</sup>[https://en.wikipedia.org/wiki/Atlanta\\_\(disambiguation\)](https://en.wikipedia.org/wiki/Atlanta_(disambiguation)), retrieved November 1, 2017.

9163 different towns and cities, five United States Navy vessels, a magazine, a television show,  
 9164 a band, and a singer — each prominent enough to have its own Wikipedia page. We now  
 9165 consider how to choose among these dozens of possibilities. In this chapter we will focus  
 9166 on supervised approaches. Unsupervised entity linking is closely related to the problem  
 9167 of **cross-document coreference resolution**, where the task is to identify pairs of mentions  
 9168 that corefer, across document boundaries (Bagga and Baldwin, 1998b; Singh et al., 2011).

### 9169 17.1.1 Entity linking by learning to rank

9170 Entity linking is often formulated as a **ranking** problem,

$$\hat{y} = \operatorname{argmax}_{y \in \mathcal{Y}(x)} \Psi(y, x, c), \quad [17.1]$$

9171 where  $y$  is a target entity,  $x$  is a description of the mention,  $\mathcal{Y}(x)$  is a set of candidate  
 9172 entities, and  $c$  is a description of the context — such as the other text in the document,  
 9173 or its metadata. The function  $\Psi$  is a scoring function, which could be a linear model,  
 9174  $\Psi(y, x, c) = \theta \cdot f(y, x, c)$ , or a more complex function such as a neural network. In either  
 9175 case, the scoring function can be learned by minimizing a margin-based **ranking loss**,

$$\ell(\hat{y}, y^{(i)}, x^{(i)}, c^{(i)}) = (\Psi(\hat{y}, x^{(i)}, c^{(i)}) - \Psi(y^{(i)}, x^{(i)}, c^{(i)}) + 1)_+, \quad [17.2]$$

9176 where  $y^{(i)}$  is the ground truth and  $\hat{y} \neq y^{(i)}$  is the predicted target for mention  $x^{(i)}$  in  
 9177 context  $c^{(i)}$  (Joachims, 2002; Dredze et al., 2010).

9178 **Candidate identification** For computational tractability, it is helpful to restrict the set of  
 9179 candidates,  $\mathcal{Y}(x)$ . One approach is to use a **name dictionary**, which maps from strings  
 9180 to the entities that they might mention. This mapping is many-to-many: a string such as  
 9181 *Atlanta* can refer to multiple entities, and conversely, an entity such as ATLANTA can be  
 9182 referenced by multiple strings. A name dictionary can be extracted from Wikipedia, with  
 9183 links between each Wikipedia entity page and the anchor text of all hyperlinks that point  
 9184 to the page (Bunescu and Pasca, 2006; Ratinov et al., 2011). To improve recall, the name  
 9185 dictionary can be augmented by partial and approximate matching (Dredze et al., 2010),  
 9186 but as the set of candidates grows, the risk of false positives increases. For example, the  
 9187 string *Atlanta* is a partial match to *the Atlanta Fed* (a name for the FEDERAL RESERVE BANK  
 9188 OF ATLANTA), and a noisy match (edit distance of one) from *Atalanta* (a heroine in Greek  
 9189 mythology and an Italian soccer team).

9190 **Features** Feature-based approaches to entity ranking rely on three main types of local  
 9191 information (Dredze et al., 2010):

- The similarity of the mention string to the canonical entity name, as quantified by string similarity. This feature would elevate the city ATLANTA over the basketball team ATLANTA HAWKS for the string *Atlanta*.
- The popularity of the entity, which can be measured by Wikipedia page views or PageRank in the Wikipedia link graph. This feature would elevate ATLANTA, GEORGIA over the unincorporated community of ATLANTA, OHIO.
- The entity type, as output by the named entity recognition system. This feature would elevate the city of ATLANTA over the magazine ATLANTA in contexts where the mention is tagged as a location.

In addition to these local features, the document context can also help. If *Jamaica* is mentioned in a document about the Caribbean, it is likely to refer to the island nation; in the context of New York, it is likely to refer to the neighborhood in Queens; in the context of a menu, it might refer to a hibiscus tea beverage. Such hints can be formalized by computing the similarity between the Wikipedia page describing each candidate entity and the mention context  $c^{(i)}$ , which may include the bag-of-words representing the document (Dredze et al., 2010; Hoffart et al., 2011) or a smaller window of text around the mention (Ratinov et al., 2011). For example, we can compute the cosine similarity between bag-of-words vectors for the context and entity description, typically weighted using **inverse document frequency** to emphasize rare words.<sup>2</sup>

**Neural entity linking** An alternative approach is to compute the score for each entity candidate using distributed vector representations of the entities, mentions, and context. For example, for the task of entity linking in Twitter, Yang et al. (2016) employ the bilinear scoring function,

$$\Psi(y, x, c) = v_y^\top \Theta^{(y,x)} x + v_y^\top \Theta^{(y,c)} c, \quad [17.3]$$

with  $v_y \in \mathbb{R}^{K_y}$  as the vector embedding of entity  $y$ ,  $x \in \mathbb{R}^{K_x}$  as the embedding of the mention,  $c \in \mathbb{R}^{K_c}$  as the embedding of the context, and the matrices  $\Theta^{(y,x)}$  and  $\Theta^{(y,c)}$  as parameters that score the compatibility of each entity with respect to the mention and context. Each of the vector embeddings can be learned from an end-to-end objective, or pre-trained on unlabeled data.

- Pretrained **entity embeddings** can be obtained from an existing knowledge base (Bordes et al., 2011, 2013), or by running a word embedding algorithm such as WORD2VEC

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<sup>2</sup>The **document frequency** of word  $j$  is  $DF(j) = \frac{1}{N} \sum_{i=1}^N \delta(x_j^{(i)} > 0)$ , equal to the number of documents in which the word appears. The contribution of each word to the cosine similarity of two bag-of-words vectors can be weighted by the **inverse document frequency**  $\frac{1}{DF(j)}$  or  $\log \frac{1}{DF(j)}$ , to emphasize rare words (Spärck Jones, 1972).

- 9222       on the text of Wikipedia, with hyperlinks substituted for the anchor text.<sup>3</sup>
- 9223     • The embedding of the mention  $x$  can be computed by averaging the embeddings  
 9224       of the words in the mention (Yang et al., 2016), or by the compositional techniques  
 9225       described in § 14.8.
- 9226     • The embedding of the context  $c$  can also be computed from the embeddings of the  
 9227       words in the context. A **denoising autoencoder** learns a function from raw text to  
 9228       dense  $K$ -dimensional vector encodings by minimizing a reconstruction loss (Vin-  
 9229       cent et al., 2010),

$$\min_{\theta_g, \theta_h} \sum_{i=1}^N \|\mathbf{x}^{(i)} - g(h(\tilde{\mathbf{x}}^{(i)}; \theta_h); \theta_g)\|^2, \quad [17.4]$$

9230       where  $\tilde{\mathbf{x}}^{(i)}$  is a noisy version of the bag-of-words counts  $\mathbf{x}^{(i)}$ , which is produced by  
 9231       randomly setting some counts to zero;  $h : \mathbb{R}^V \rightarrow \mathbb{R}^K$  is an encoder with parameters  
 9232        $\theta_h$ ; and  $g : \mathbb{R}^K \rightarrow \mathbb{R}^V$ , with parameters  $\theta_g$ . The encoder and decoder functions  
 9233       are typically implemented as feedforward neural networks. To apply this model to  
 9234       entity linking, each entity and context are initially represented by the encoding of  
 9235       their bag-of-words vectors,  $h(e)$  and  $g(c)$ , and these encodings are then fine-tuned  
 9236       from labeled data (He et al., 2013). The context vector  $c$  can also be obtained by  
 9237       convolution on the embeddings of words in the document (Sun et al., 2015), or by  
 9238       examining metadata such as the author’s social network (Yang et al., 2016).

9239       The remaining parameters  $\Theta^{(y,x)}$  and  $\Theta^{(y,c)}$  can be trained by backpropagation from the  
 9240       margin loss in Equation 17.2.

### 9241     17.1.2 Collective entity linking

9242       Entity linking can be more accurate when it is performed jointly across a document. To  
 9243       see why, consider the following lists:

- 9244       (17.5) California, Oregon, Washington  
 9245       (17.6) Baltimore, Washington, Philadelphia  
 9246       (17.7) Washington, Adams, Jefferson

9247       In each case, the term *Washington* refers to a different entity, and this reference is strongly  
 9248       suggested by the other entries on the list. In the last list, all three names are highly am-  
 9249       biguous — there are dozens of other *Adams* and *Jefferson* entities in Wikipedia. But a

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<sup>3</sup>Pre-trained entity embeddings can be downloaded from <https://code.google.com/archive/p/word2vec/>.

9246 preference for coherence motivates **collectively** linking these references to the first three  
 9247 U.S. presidents.

9248 A general approach to collective entity linking is to introduce a compatibility score  
 9249  $\psi_c(\mathbf{y})$ . Collective entity linking is then performed by optimizing the global objective,

$$\hat{\mathbf{y}} = \underset{\mathbf{y} \in \mathbb{Y}(\mathbf{x})}{\operatorname{argmax}} \Psi_c(\mathbf{y}) + \sum_{i=1}^N \Psi_\ell(y^{(i)}, \mathbf{x}^{(i)}, \mathbf{c}^{(i)}), \quad [17.5]$$

9250 where  $\mathbb{Y}(\mathbf{x})$  is the set of all possible collective entity assignments for the mentions in  $\mathbf{x}$ ,  
 9251 and  $\psi_\ell$  is the local scoring function for each entity  $i$ . The compatibility function is typically  
 9252 decomposed into a sum of pairwise scores,  $\Psi_c(\mathbf{y}) = \sum_{i=1}^N \sum_{j \neq i}^N \Psi_c(y^{(i)}, y^{(j)})$ . These scores  
 9253 can be computed in a number of different ways:

- 9254 • Wikipedia defines high-level categories for entities (e.g., *living people*, *Presidents of*  
 9255 *the United States*, *States of the United States*), and  $\Psi_c$  can reward entity pairs for the  
 9256 number of categories that they have in common (Cucerzan, 2007).
- 9257 • Compatibility can be measured by the number of incoming hyperlinks shared by  
 9258 the Wikipedia pages for the two entities (Milne and Witten, 2008).
- 9259 • In a neural architecture, the compatibility of two entities can be set equal to the inner  
 9260 product of their embeddings,  $\Psi_c(y^{(i)}, y^{(j)}) = \mathbf{v}_{y^{(i)}} \cdot \mathbf{v}_{y^{(j)}}$ .
- 9261 • A non-pairwise compatibility score can be defined using a type of latent variable  
 9262 model known as a **probabilistic topic model** (Blei et al., 2003; Blei, 2012). In this  
 9263 framework, each latent topic is a probability distribution over entities, and each  
 9264 document has a probability distribution over topics. Each entity helps to determine  
 9265 the document's distribution over topics, and in turn these topics help to resolve am-  
 9266 biguous entity mentions (Newman et al., 2006). Inference can be performed using  
 9267 the sampling techniques described in chapter 5.

9268 Unfortunately, collective entity linking is **NP-hard** even for pairwise compatibility func-  
 9269 tions, so exact optimization is almost certainly intractable. Various approximate inference  
 9270 techniques have been proposed, including **integer linear programming** (Cheng and Roth,  
 9271 2013), **Gibbs sampling** (Han and Sun, 2012), and graph-based algorithms (Hoffart et al.,  
 9272 2011; Han et al., 2011).

### 9273 17.1.3 \*Pairwise ranking loss functions

9274 The loss function defined in Equation 17.2 considers only the highest-scoring prediction  
 9275  $\hat{y}$ , but in fact, the true entity  $y^{(i)}$  should outscore *all* other entities. A loss function based on  
 9276 this idea would give a gradient against the features or representations of several entities,

**Algorithm 19** WARP approximate ranking loss

---

```

1: procedure WARP( $y^{(i)}$ ,  $\mathbf{x}^{(i)}$ )
2:    $N \leftarrow 0$ 
3:   repeat
4:     Randomly sample  $y \sim \mathcal{Y}(\mathbf{x}^{(i)})$ 
5:      $N \leftarrow N + 1$ 
6:     if  $\psi(y, \mathbf{x}^{(i)}) + 1 > \psi(y^{(i)}, \mathbf{x}^{(i)})$  then            $\triangleright$  check for margin violation
7:        $r \leftarrow \lfloor |\mathcal{Y}(\mathbf{x}^{(i)})|/N \rfloor$                           $\triangleright$  compute approximate rank
8:       return  $L_{\text{rank}}(r) \times (\psi(y, \mathbf{x}^{(i)}) + 1 - \psi(y^{(i)}, \mathbf{x}^{(i)}))$ 
9:     until  $N \geq |\mathcal{Y}(\mathbf{x}^{(i)})| - 1$                             $\triangleright$  no violation found
10:    return 0                                          $\triangleright$  return zero loss

```

---

not just the top-scoring prediction. Usunier et al. (2009) define a general ranking error function,

$$L_{\text{rank}}(k) = \sum_{j=1}^k \alpha_j, \quad \text{with } \alpha_1 \geq \alpha_2 \geq \dots \geq 0, \quad [17.6]$$

where  $k$  is equal to the number of labels ranked higher than the correct label  $y^{(i)}$ . This function defines a class of ranking errors: if  $\alpha_j = 1$  for all  $j$ , then the ranking error is equal to the rank of the correct entity; if  $\alpha_1 = 1$  and  $\alpha_{j>1} = 0$ , then the ranking error is one whenever the correct entity is not ranked first; if  $\alpha_j$  decreases smoothly with  $j$ , as in  $\alpha_j = \frac{1}{j}$ , then the error is between these two extremes.

This ranking error can be integrated into a margin objective. Remember that large margin classification requires not only the correct label, but also that the correct label outscores other labels by a substantial margin. A similar principle applies to ranking: we want a high rank for the correct entity, and we want it to be separated from other entities by a substantial margin. We therefore define the margin-augmented rank,

$$r(y^{(i)}, \mathbf{x}^{(i)}) \triangleq \sum_{y \in \mathcal{Y}(\mathbf{x}^{(i)}) \setminus y^{(i)}} \delta \left( 1 + \psi(y, \mathbf{x}^{(i)}) \geq \psi(y^{(i)}, \mathbf{x}^{(i)}) \right), \quad [17.7]$$

where  $\delta(\cdot)$  is a delta function, and  $\mathcal{Y}(\mathbf{x}^{(i)}) \setminus y^{(i)}$  is the set of all entity candidates minus the true entity  $y^{(i)}$ . The margin-augmented rank is the rank of the true entity, after augmenting every other candidate with a margin of one, under the current scoring function  $\psi$ . (The context  $c$  is omitted for clarity, and can be considered part of  $x$ .)

For each instance, a hinge loss is computed from the ranking error associated with this

margin-augmented rank, and the violation of the margin constraint,

$$\ell(y^{(i)}, \mathbf{x}^{(i)}) = \frac{L_{\text{rank}}(r(y^{(i)}, \mathbf{x}^{(i)}))}{r(y^{(i)}, \mathbf{x}^{(i)})} \sum_{y \in \mathcal{Y}(\mathbf{x}) \setminus y^{(i)}} \left( \psi(y, \mathbf{x}^{(i)}) - \psi(y^{(i)}, \mathbf{x}^{(i)}) + 1 \right)_+, \quad [17.8]$$

The sum in Equation 17.8 includes non-zero values for every label that is ranked at least as high as the true entity, after applying the margin augmentation. Dividing by the margin-augmented rank of the true entity thus gives the average violation.

The objective in Equation 17.8 is expensive to optimize when the label space is large, as is usually the case for entity linking against large knowledge bases. This motivates a randomized approximation called **WARP** (Weston et al., 2011), shown in Algorithm 19. In this procedure, we sample random entities until one violates the pairwise margin constraint,  $\psi(y, \mathbf{x}^{(i)}) + 1 \geq \psi(y^{(i)}, \mathbf{x}^{(i)})$ . The number of samples  $N$  required to find such a violation yields an approximation of the margin-augmented rank of the true entity,  $r(y^{(i)}, \mathbf{x}^{(i)}) \approx \left\lceil \frac{|\mathcal{Y}(\mathbf{x})|}{N} \right\rceil$ . If a violation is found immediately,  $N = 1$ , the correct entity probably ranks below many others,  $r \approx |\mathcal{Y}(\mathbf{x})|$ . If many samples are required before a violation is found,  $N \rightarrow |\mathcal{Y}(\mathbf{x})|$ , then the correct entity is probably highly ranked,  $r \rightarrow 1$ . A computational advantage of WARP is that it is not necessary to find the highest-scoring label, which can impose a non-trivial computational cost when  $\mathcal{Y}(\mathbf{x}^{(i)})$  is large. The objective is conceptually similar to the **negative sampling** objective in WORD2VEC (chapter 14), which compares the observed word against randomly sampled alternatives.

## 17.2 Relations

After identifying the entities that are mentioned in a text, the next step is to determine how they are related. Consider the following example:

(17.8) George Bush traveled to France on Thursday for a summit.

This sentence introduces a relation between the entities referenced by *George Bush* and *France*. In the Automatic Content Extraction (ACE) ontology (Linguistic Data Consortium, 2005), the type of this relation is PHYSICAL, and the subtype is LOCATED. This relation would be written,

PHYSICAL.LOCATED(GEORGE BUSH, FRANCE). [17.9]

Relations take exactly two arguments, and the order of the arguments matters.

In the ACE datasets, relations are annotated between entity mentions, as in the example above. Relations can also hold between nominals, as in the following example from the SemEval-2010 shared task (Hendrickx et al., 2009):

CAUSE-EFFECT	<i>those cancers were caused by radiation exposures</i>
INSTRUMENT-AGENCY	<i>phone operator</i>
PRODUCT-PRODUCER	<i>a factory manufactures suits</i>
CONTENT-CONTAINER	<i>a bottle of honey was weighed</i>
ENTITY-ORIGIN	<i>letters from foreign countries</i>
ENTITY-DESTINATION	<i>the boy went to bed</i>
COMPONENT-WHOLE	<i>my apartment has a large kitchen</i>
MEMBER-COLLECTION	<i>there are many trees in the forest</i>
COMMUNICATION-TOPIC	<i>the lecture was about semantics</i>

Table 17.1: Relations and example sentences from the SemEval-2010 dataset (Hendrickx et al., 2009)

9316 (17.9) The cup contained tea from dried ginseng.

9317 This sentence describes a relation of type ENTITY-ORIGIN between *tea* and *ginseng*. Nominal  
 9318 relation extraction is closely related to **semantic role labeling** (chapter 13). The main  
 9319 difference is that relation extraction is restricted to a relatively small number of relation  
 9320 types; for example, Table 17.1 shows the ten relation types from SemEval-2010.

### 9321 17.2.1 Pattern-based relation extraction

9322 Early work on relation extraction focused on hand-crafted patterns (Hearst, 1992). For  
 9323 example, the appositive *Starbuck, a native of Nantucket* signals the relation ENTITY-ORIGIN  
 9324 between *Starbuck* and *Nantucket*. This pattern can be written as,

$$\text{PERSON , } a \text{ native of LOCATION} \Rightarrow \text{ENTITY-ORIGIN(PERSON, LOCATION)}. \quad [17.10]$$

9325 This pattern will be “triggered” whenever the literal string *, a native of* occurs between an  
 9326 entity of type PERSON and an entity of type LOCATION. Such patterns can be generalized  
 9327 beyond literal matches using techniques such as lemmatization, which would enable the  
 9328 words (*buy, buys, buying*) to trigger the same patterns (see § 4.3.1.2). A more aggressive  
 9329 strategy would be to group all words in a WordNet synset (§ 4.2), so that, e.g., *buy* and  
 9330 *purchase* trigger the same patterns.

9331 Relation extraction patterns can be implemented in finite-state automata (§ 9.1). If the  
 9332 named entity recognizer is also a finite-state machine, then the systems can be combined  
 9333 by finite-state transduction (Hobbs et al., 1997). This makes it possible to propagate uncer-  
 9334 tainty through the finite-state cascade, and disambiguate from higher-level context. For  
 9335 example, suppose the entity recognizer cannot decide whether *Starbuck* refers to either a  
 9336 PERSON or a LOCATION; in the composed transducer, the relation extractor would be free  
 9337 to select the PERSON annotation when it appears in the context of an appropriate pattern.

9338 **17.2.2 Relation extraction as a classification task**

9339 Relation extraction can be formulated as a classification problem,

$$\hat{r}_{(i,j),(m,n)} = \operatorname{argmax}_{r \in \mathcal{R}} \Psi(r, (i, j), (m, n), \mathbf{w}), \quad [17.11]$$

9340 where  $r \in \mathcal{R}$  is a relation type (possibly NIL),  $\mathbf{w}_{i+1:j}$  is the span of the first argument, and  
 9341  $\mathbf{w}_{m+1:n}$  is the span of the second argument. The argument  $\mathbf{w}_{m+1:n}$  may appear before  
 9342 or after  $\mathbf{w}_{i+1:j}$  in the text, or they may overlap; we stipulate only that  $\mathbf{w}_{i+1:j}$  is the first  
 9343 argument of the relation. We now consider three alternatives for computing the scoring  
 9344 function.

9345 **17.2.2.1 Feature-based classification**

9346 In a feature-based classifier, the scoring function is defined as,

$$\Psi(r, (i, j), (m, n), \mathbf{w}) = \boldsymbol{\theta} \cdot \mathbf{f}(r, (i, j), (m, n), \mathbf{w}), \quad [17.12]$$

9347 with  $\boldsymbol{\theta}$  representing a vector of weights, and  $\mathbf{f}(\cdot)$  a vector of features. The pattern-based  
 9348 methods described in § 17.2.1 suggest several features:

- 9349 • Local features of  $\mathbf{w}_{i+1:j}$  and  $\mathbf{w}_{m+1:n}$ , including: the strings themselves; whether they  
 9350 are recognized as entities, and if so, which type; whether the strings are present in a  
 9351 **gazetteer** of entity names; each string's syntactic **head** (§ 9.2.2).
- 9352 • Features of the span between the two arguments,  $\mathbf{w}_{j+1:m}$  or  $\mathbf{w}_{n+1:i}$  (depending on  
 9353 which argument appears first): the length of the span; the specific words that appear  
 9354 in the span, either as a literal sequence or a bag-of-words; the wordnet synsets (§ 4.2)  
 9355 that appear in the span between the arguments.
- 9356 • Features of the syntactic relationship between the two arguments, typically the **de-**  
 9357 **pendency path** between the arguments (§ 13.2.1). Example dependency paths are  
 9358 shown in Table 17.2.

9359 **17.2.2.2 Kernels**

9360 Suppose that the first line of Table 17.2 is a labeled example, and the remaining lines are  
 9361 instances to be classified. A feature-based approach would have to decompose the depen-  
 9362 dency paths into features that capture individual edges, with or without their labels, and  
 9363 then learn weights for each of these features: for example, the second line contains identi-  
 9364 cal dependencies, but different arguments; the third line contains a different inflection of  
 9365 the word *travel*; the fourth and fifth lines each contain an additional edge on the depen-  
 9366 dency path; and the sixth example uses an entirely different path. Rather than attempting  
 9367 to create local features that capture all of the ways in which these dependencies paths

1. <i>George Bush traveled to France</i>	<i>George Bush</i> $\leftarrow$ traveled $\rightarrow$ France NSUBJ OBL
2. <i>Ahab traveled to Nantucket</i>	<i>Ahab</i> $\leftarrow$ traveled $\rightarrow$ Nantucket NSUBJ OBL
3. <i>George Bush will travel to France</i>	<i>George Bush</i> $\leftarrow$ travel $\rightarrow$ France NSUBJ OBL
4. <i>George Bush wants to travel to France</i>	<i>George Bush</i> $\leftarrow$ wants $\rightarrow$ travel $\rightarrow$ France NSUBJ XCOMP OBL
5. <i>Ahab traveled to a city in France</i>	<i>Ahab</i> $\leftarrow$ traveled $\rightarrow$ city $\rightarrow$ France NSUBJ OBL NMOD
6. <i>We await Ahab's visit to France</i>	<i>Ahab</i> $\leftarrow$ visit $\rightarrow$ France NMOD:POSS NMOD

Table 17.2: Candidates instances for the PHYSICAL.LOCATED relation, and their dependency paths

9368 are similar and different, we can instead define a similarity function  $\kappa$ , which computes a  
 9369 score for any pair of instances,  $\kappa : \mathcal{X} \times \mathcal{X} \mapsto \mathbb{R}_+$ . The score for any pair of instances  $(i, j)$   
 9370 is  $\kappa(\mathbf{x}^{(i)}, \mathbf{x}^{(j)}) \geq 0$ , with  $\kappa(i, j)$  being large when instances  $\mathbf{x}^{(i)}$  and  $\mathbf{x}^{(j)}$  are similar. If the  
 9371 function  $\kappa$  obeys a few key properties it is a valid **kernel function**.<sup>4</sup>

Given a valid kernel function, we can build a non-linear classifier without explicitly defining a feature vector or neural network architecture. For a binary classification problem  $y \in \{-1, 1\}$ , we have the decision function,

$$\hat{y} = \text{Sign}(b + \sum_{i=1}^N y^{(i)} \alpha^{(i)} \kappa(\mathbf{x}^{(i)}, \mathbf{x})) \quad [17.13]$$

9372 where  $b$  and  $\{\alpha^{(i)}\}_{i=1}^N$  are parameters that must be learned from the training set, under  
 9373 the constraint  $\forall_i, \alpha^{(i)} \geq 0$ . Intuitively, each  $\alpha_i$  specifies the importance of the instance  $\mathbf{x}^{(i)}$   
 9374 towards the classification rule. Kernel-based classification can be viewed as a weighted  
 9375 form of the **nearest-neighbor** classifier (Hastie et al., 2009), in which test instances are  
 9376 assigned the most common label among their near neighbors in the training set. This  
 9377 results in a non-linear classification boundary. The parameters are typically learned from  
 9378 a margin-based objective (see § 2.3), leading to the **kernel support vector machine**. To  
 9379 generalize to multi-class classification, we can train separate binary classifiers for each  
 9380 label (sometimes called **one-versus-all**), or train binary classifiers for each pair of possible  
 9381 labels (**one-versus-one**).

9382 Dependency kernels are particularly effective for relation extraction, due to their ability  
 9383 to capture syntactic properties of the path between the two candidate arguments. One  
 9384 class of dependency tree kernels is defined recursively, with the score for a pair of trees

<sup>4</sup>The **Gram matrix**  $\mathbf{K}$  arises from computing the kernel function between all pairs in a set of instances. For a valid kernel, the Gram matrix must be symmetric ( $\mathbf{K} = \mathbf{K}^\top$ ) and positive semi-definite ( $\forall \mathbf{a}, \mathbf{a}^\top \mathbf{K} \mathbf{a} \geq 0$ ). For more on kernel-based classification, see chapter 14 of Murphy (2012).

equal to the similarity of the root nodes and the sum of similarities of matched pairs of child subtrees (Zelenko et al., 2003; Culotta and Sorensen, 2004). Alternatively, Bunescu and Mooney (2005) define a kernel function over sequences of unlabeled dependency edges, in which the score is computed as a product of scores for each pair of words in the sequence: identical words receive a high score, words that share a synset or part-of-speech receive a small non-zero score (e.g., *travel* / *visit*), and unrelated words receive a score of zero.

### 17.2.2.3 Neural relation extraction

**Convolutional neural networks** were an early neural architecture for relation extraction (Zeng et al., 2014; dos Santos et al., 2015). For the sentence  $(w_1, w_2, \dots, w_M)$ , obtain a matrix of word embeddings  $\mathbf{X}$ , where  $x_m \in \mathbb{R}^K$  is the embedding of  $w_m$ . Now, suppose the candidate arguments appear at positions  $a_1$  and  $a_2$ ; then for each word in the sentence, its position with respect to each argument is  $m - a_1$  and  $m - a_2$ . (Following Zeng et al. (2014), this is a restricted version of the relation extraction task in which the arguments are single tokens.) To capture any information conveyed by these positions, the word embeddings are concatenated with embeddings of the positional offsets,  $x_{m-a_1}^{(p)}$  and  $x_{m-a_2}^{(p)}$ . The complete base representation of the sentence is,

$$\mathbf{X}(a_1, a_2) = \begin{pmatrix} \mathbf{x}_1 & \mathbf{x}_2 & \cdots & \mathbf{x}_M \\ \mathbf{x}_{1-a_1}^{(p)} & \mathbf{x}_{2-a_1}^{(p)} & \cdots & \mathbf{x}_{M-a_1}^{(p)} \\ \mathbf{x}_{1-a_2}^{(p)} & \mathbf{x}_{2-a_2}^{(p)} & \cdots & \mathbf{x}_{M-a_2}^{(p)} \end{pmatrix}, \quad [17.14]$$

where each column is a vertical concatenation of a word embedding, represented by the column vector  $\mathbf{x}_m$ , and two positional embeddings, specifying the position with respect to  $a_1$  and  $a_2$ . The matrix  $\mathbf{X}(a_1, a_2)$  is then taken as input to a convolutional layer (see § 3.4), and max-pooling is applied to obtain a vector. The final scoring function is then,

$$\Psi(r, i, j, \mathbf{X}) = \theta_r \cdot \text{MaxPool}(\text{ConvNet}(\mathbf{X}(i, j); \phi)), \quad [17.15]$$

where  $\phi$  defines the parameters of the convolutional operator, and the  $\theta_r$  defines a set of weights for relation  $r$ . The model can be trained using a margin objective,

$$\hat{r} = \underset{r}{\operatorname{argmax}} \Psi(r, i, j, \mathbf{X}) \quad [17.16]$$

$$\ell = (1 + \psi(\hat{r}, i, j, \mathbf{X}) - \psi(r, i, j, \mathbf{X}))_+. \quad [17.17]$$

**Recurrent neural networks** have also been applied to relation extraction, using a network such as an bidirectional LSTM to encode the words or dependency path between the two arguments. Xu et al. (2015) segment each dependency path into left and right subpaths: the path  $George \xleftarrow{\text{NSUBJ}} Bush \xrightarrow{\text{XCOMP}} wants \xrightarrow{\text{OBL}} travel \rightarrow France$  is segmented into the subpaths,

9411 (17.10) *George Bush*  $\xleftarrow{\text{NSUBJ}}$  *wants*

9412 (17.11) *wants*  $\xrightarrow{\text{XCOMP}}$  *travel*  $\xrightarrow{\text{OBL}}$  *France*.

Xu et al. (2015) then run recurrent networks from the arguments to the root word (in this case, *wants*), obtaining the final representation by max pooling across all the recurrent states along each path. This process can be applied across separate “channels”, in which the inputs consist of embeddings for the words, parts-of-speech, dependency relations, and WordNet hypernyms. To define the model formally, let  $s(m)$  define the successor of word  $m$  in either the left or right subpath (in a dependency path, each word can have a successor in at most one subpath). Let  $\mathbf{x}_m^{(c)}$  indicate the embedding of word (or relation)  $m$  in channel  $c$ , and let  $\overleftarrow{\mathbf{h}}_m^{(c)}$  and  $\overrightarrow{\mathbf{h}}_m^{(c)}$  indicate the associated recurrent states in the left and right subtrees respectively. Then the complete model is specified as follows,

$$\mathbf{h}_{s(m)}^{(c)} = \text{RNN}(\mathbf{x}_{s(m)}^{(c)}, \mathbf{h}_m^{(c)}) \quad [17.18]$$

$$\mathbf{z}^{(c)} = \text{MaxPool}(\overleftarrow{\mathbf{h}}_i^{(c)}, \overleftarrow{\mathbf{h}}_{s(i)}^{(c)}, \dots, \overleftarrow{\mathbf{h}}_{\text{root}}^{(c)}, \overrightarrow{\mathbf{h}}_j^{(c)}, \overrightarrow{\mathbf{h}}_{s(j)}^{(c)}, \dots, \overrightarrow{\mathbf{h}}_{\text{root}}^{(c)}) \quad [17.19]$$

$$\Psi(r, i, j) = \theta \cdot [\mathbf{z}^{(\text{word})}; \mathbf{z}^{(\text{POS})}; \mathbf{z}^{(\text{dependency})}; \mathbf{z}^{(\text{hypernym})}] \quad [17.20]$$

9413 Note that  $\mathbf{z}$  is computed by applying max-pooling to the *matrix* of horizontally concate-  
 9414 nated vectors  $\mathbf{h}$ , while  $\Psi$  is computed from the *vector* of vertically concatenated vectors  
 9415  $\mathbf{z}$ . Xu et al. (2015) pass the score  $\Psi$  through a **softmax** layer to obtain a probability  
 9416  $p(r | i, j, w)$ , and train the model by regularized **cross-entropy**. Miwa and Bansal (2016)  
 9417 show that a related model can solve the more challenging “end-to-end” relation extrac-  
 9418 tion task, in which the model must simultaneously detect entities and then extract their  
 9419 relations.

### 9420 17.2.3 Knowledge base population

9421 In many applications, what matters is not what fraction of sentences are analyzed cor-  
 9422 rectly, but how much accurate knowledge can be extracted. **Knowledge base population**  
 9423 (**KBP**) refers to the task of filling in Wikipedia-style infoboxes, as shown in Figure 17.1a.  
 9424 Knowledge base population can be decomposed into two subtasks: **entity linking** (de-  
 9425 scribed in § 17.1), and **slot filling** (Ji and Grishman, 2011). Slot filling has two key dif-  
 9426 ferences from the formulation of relation extraction presented above: the relations hold  
 9427 between entities rather than spans of text, and the performance is evaluated at the *type*  
 9428 *level* (on entity pairs), rather than on the *token level* (on individual sentences).

9429 From a practical standpoint, there are three other important differences between slot  
 9430 filling and per-sentence relation extraction.

- KBP tasks are often formulated from the perspective of identifying attributes of a few “query” entities. As a result, these systems often start with an **information retrieval** phase, in which relevant passages of text are obtained by search.
- For many entity pairs, there will be multiple passages of text that provide evidence. Slot filling systems must aggregate this evidence to predict a single relation type (or set of relations).
- Labeled data is usually available in the form of pairs of related entities, rather than annotated passages of text. Training from such type-level annotations is a challenge: two entities may be linked by several relations, or they may appear together in a passage of text that nonetheless does not describe their relation to each other.

Information retrieval is beyond the scope of this text (see Manning et al., 2008). The remainder of this section describes approaches to information fusion and learning from type-level annotations.

#### 17.2.3.1 Information fusion

In knowledge base population, there will often be multiple pieces of evidence for (and sometimes against) a single relation. For example, a search for the entity MAYNARD JACKSON, JR. may return several passages that reference the entity ATLANTA:<sup>5</sup>

- (17.12) Elected mayor of Atlanta in 1973, **Maynard Jackson** was the first African American to serve as mayor of a major southern city.
- (17.13) **Atlanta's** airport will be renamed to honor **Maynard Jackson**, the city's first Black mayor.
- (17.14) Born in Dallas, Texas in 1938, **Maynard Holbrook Jackson, Jr.** moved to Atlanta when he was 8.
- (17.15) **Maynard Jackson** has gone from one of the worst high schools in **Atlanta** to one of the best.

The first and second examples provide evidence for the relation **MAYOR** holding between the entities **ATLANTA** and **MAYNARD JACKSON, JR.**. The third example provides evidence for a different relation between these same entities, **LIVED-IN**. The fourth example poses an entity linking problem, referring to **MAYNARD JACKSON HIGH SCHOOL**. Knowledge base population requires aggregating this sort of textual evidence, and predicting the relations that are most likely to hold.

---

<sup>5</sup>First three examples from: <http://www.georgiaencyclopedia.org/articles/government-politics/maynard-jackson-1938-2003>; JET magazine, November 10, 2003; [www.todayingeorgiahistory.org/content/maynard-jackson-elected](http://www.todayingeorgiahistory.org/content/maynard-jackson-elected)

9462 One approach is to run a single-document relation extraction system (using the tech-  
 9463 niques described in § 17.2.2), and then aggregate the results (Li et al., 2011). Relations  
 9464 that are detected with high confidence in multiple documents are more likely to be valid,  
 9465 motivating the heuristic,

$$\psi(r, e_1, e_2) = \sum_{i=1}^N (\text{p}(r(e_1, e_2) | \mathbf{w}^{(i)}))^\alpha, \quad [17.21]$$

9466 where  $\text{p}(r(e_1, e_2) | \mathbf{w}^{(i)})$  is the probability of relation  $r$  between entities  $e_1$  and  $e_2$  condi-  
 9467 tioned on the text  $\mathbf{w}^{(i)}$ , and  $\alpha \gg 1$  is a tunable hyperparameter. Using this heuristic, it is  
 9468 possible to rank all candidate relations, and trace out a **precision-recall curve** as more rel-  
 9469 relations are extracted.<sup>6</sup> Alternatively, features can be aggregated across multiple passages  
 9470 of text, feeding a single type-level relation extraction system (Wolfe et al., 2017).

9471 Precision can be improved by introducing constraints across multiple relations. For  
 9472 example, if we are certain of the relation  $\text{PARENT}(e_1, e_2)$ , then it cannot also be the case  
 9473 that  $\text{PARENT}(e_2, e_1)$ . Integer linear programming makes it possible to incorporate such  
 9474 constraints into a global optimization (Li et al., 2011). Other pairs of relations have pos-  
 9475 itive correlations, such  $\text{MAYOR}(e_1, e_2)$  and  $\text{LIVED-IN}(e_1, e_2)$ . Compatibility across relation  
 9476 types can be incorporated into probabilistic graphical models (e.g., Riedel et al., 2010).

### 9477 17.2.3.2 Distant supervision

9478 Relation extraction is “annotation hungry,” because each relation requires its own la-  
 9479 beled data. Rather than relying on annotations of individual documents, it would be  
 9480 preferable to use existing knowledge resources — such as the many facts that are al-  
 9481 ready captured in knowledge bases like DBpedia. However such annotations raise the  
 9482 inverse of the information fusion problem considered above: the existence of the relation  
 9483  $\text{MAYOR}(\text{MAYNARD JACKSON JR., ATLANTA})$  provides only **distant supervision** for the  
 9484 example texts in which this entity pair is mentioned.

9485 One approach is to treat the entity pair as the instance, rather than the text itself (Mintz  
 9486 et al., 2009). Features are then aggregated across all sentences in which both entities are  
 9487 mentioned, and labels correspond to the relation (if any) between the entities in a knowl-  
 9488 edge base, such as FreeBase. Negative instances are constructed from entity pairs that are  
 9489 not related in the knowledge base. In some cases, two entities are related, but the knowl-  
 9490 edge base is missing the relation; however, because the number of possible entity pairs is  
 9491 huge, these missing relations are presumed to be relatively rare. This approach is shown  
 9492 in Figure 17.2.

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<sup>6</sup>The precision-recall curve is similar to the ROC curve shown in Figure 4.4, but it includes the precision  $\frac{\text{TP}}{\text{TP} + \text{FP}}$  rather than the false positive rate  $\frac{\text{FP}}{\text{FP} + \text{TN}}$ .

- **Label** : MAYOR(ATLANTA, MAYNARD JACKSON)
  - Elected mayor of **Atlanta** in 1973, **Maynard Jackson** ...
  - **Atlanta**'s airport will be renamed to honor **Maynard Jackson**, the city's first Black mayor
  - Born in Dallas, Texas in 1938, **Maynard Holbrook Jackson, Jr.** moved to **Atlanta** when he was 8.
- **Label** : MAYOR(NEW YORK, FIORELLO LA GUARDIA)
  - **Fiorello La Guardia** was Mayor of **New York** for three terms ...
  - **Fiorello La Guardia**, then serving on the **New York** City Board of Aldermen...
- **Label** : BORN-IN(DALLAS, MAYNARD JACKSON)
  - Born in **Dallas**, Texas in 1938, **Maynard Holbrook Jackson, Jr.** moved to Atlanta when he was 8.
  - **Maynard Jackson** was raised in **Dallas** ...
- **Label** : NIL(NEW YORK, MAYNARD JACKSON)
  - **Jackson** married Valerie Richardson, whom he had met in **New York**...
  - **Jackson** was a member of the Georgia and **New York** bars ...

Figure 17.2: Four training instances for relation classification using **distant supervision** Mintz et al. (2009). The first two instances are positive for the MAYOR relation, and the third instance is positive for the BORN-IN relation. The fourth instance is a negative example, constructed from a pair of entities (NEW YORK, MAYNARD JACKSON) that do not appear in any Freebase relation. Each instance's features are computed by aggregating across all sentences in which the two entities are mentioned.

9493        In **multiple instance learning**, labels are assigned to *sets* of instances, of which only  
 9494        an unknown subset are actually relevant (Dietterich et al., 1997; Maron and Lozano-Pérez,  
 9495        1998). This formalizes the framework of distant supervision: the relation  $\text{REL}(A, B)$  acts  
 9496        as a label for the entire set of sentences mentioning entities A and B, even when only a  
 9497        subset of these sentences actually describes the relation. One approach to multi-instance  
 9498        learning is to introduce a binary **latent variable** for each sentence, indicating whether the  
 9499        sentence expresses the labeled relation (Riedel et al., 2010). A variety of inference tech-  
 9500        niques have been employed for this probabilistic model of relation extraction: Surdeanu  
 9501        et al. (2012) use expectation maximization, Riedel et al. (2010) use sampling, and Hoff-  
 9502        mann et al. (2011) use a custom graph-based algorithm. Expectation maximization and  
 9503        sampling are surveyed in chapter 5, and are covered in more detail by Murphy (2012);  
 9504        graph-based methods are surveyed by Mihalcea and Radev (2011).

Task	Relation ontology	Supervision
PropBank semantic role labeling	VerbNet	sentence
FrameNet semantic role labeling	FrameNet	sentence
Relation extraction	ACE, TAC, SemEval, etc	sentence
Slot filling	ACE, TAC, SemEval, etc	relation
Open Information Extraction	open	seed relations or patterns

Table 17.3: Various relation extraction tasks and their properties. VerbNet and FrameNet are described in chapter 13. ACE (Linguistic Data Consortium, 2005), TAC (McNamee and Dang, 2009), and SemEval (Hendrickx et al., 2009) refer to shared tasks, each of which involves an ontology of relation types.

#### 9505 17.2.4 Open information extraction

9506 In classical relation extraction, the set of relations is defined in advance, using a **schema**.  
 9507 The relation for any pair of entities can then be predicted using multi-class classification.  
 9508 In **open information extraction** (OpenIE), a relation can be any triple of text. The example  
 9509 sentence (17.12) instantiates several “relations” of this sort, e.g.,

- 9510 • (*mayor of, Maynard Jackson, Atlanta*),
- 9511 • (*elected, Maynard Jackson, mayor of Atlanta*),
- 9512 • (*elected in, Maynard Jackson, 1973*).

9513 Extracting such tuples can be viewed as a lightweight version of **semantic role labeling**  
 9514 (chapter 13), with only two argument types: first slot and second slot. The task is gen-  
 9515 erally evaluated on the relation level, rather than on the level of sentences: precision is  
 9516 measured by the number of extracted relations that are accurate, and recall is measured  
 9517 by the number of true relations that were successfully extracted. OpenIE systems are  
 9518 trained from distant supervision or bootstrapping, rather than from labeled sentences.

9519 An early example is the `TextRunner` system (Banko et al., 2007), which identifies re-  
 9520 lations with a set of handcrafted syntactic rules. The examples that are acquired from the  
 9521 handcrafted rules are then used to train a classification model that uses part-of-speech pat-  
 9522 terns as features. Finally, the relations that are extracted by the classifier are aggregated,  
 9523 removing redundant relations and computing the number of times that each relation is  
 9524 mentioned in the corpus. `TextRunner` was the first in a series of systems that performed  
 9525 increasingly accurate open relation extraction by incorporating more precise linguistic fea-  
 9526 tures (Etzioni et al., 2011), distant supervision from Wikipedia infoboxes (Wu and Weld,  
 9527 2010), and better learning algorithms (Zhu et al., 2009).

## 9528 17.3 Events

9529 Relations link pairs of entities, but many real-world situations involve more than two en-  
9530 tities. Consider again the example sentence (17.12), which describes the **event** of an elec-  
9531 tion, with four properties: the office (MAYOR), the district (ATLANTA), the date (1973), and  
9532 the person elected (MAYNARD JACKSON, JR.). In **event detection**, a schema is provided  
9533 for each event type (e.g., an election, a terrorist attack, or a chemical reaction), indicating  
9534 all the possible properties of the event. The system is then required to fill in as many of  
9535 these properties as possible (Doddington et al., 2004).

9536 Event detection systems generally involve a retrieval component (finding relevant  
9537 documents and passages of text) and an extraction component (determining the proper-  
9538 ties of the event based on the retrieved texts). Early approaches focused on finite-state pat-  
9539 terns for identify event properties (Hobbs et al., 1997); such patterns can be automatically  
9540 induced by searching for patterns that are especially likely to appear in documents that  
9541 match the event query (Riloff, 1996). Contemporary approaches employ techniques that  
9542 are similar to FrameNet semantic role labeling (§ 13.2), such as structured prediction over  
9543 local and global features (Li et al., 2013) and bidirectional recurrent neural networks (Feng  
9544 et al., 2016). These methods detect whether an event is described in a sentence, and if so,  
9545 what are its properties.

9546 **Event coreference** Because multiple sentences may describe unique properties of a sin-  
9547 gle event, **event coreference** is required to link event mentions across a single passage  
9548 of text, or between passages (Humphreys et al., 1997). Bejan and Harabagiu (2014) de-  
9549 fine event coreference as the task of identifying event mentions that share the same event  
9550 participants (i.e., the slot-filling entities) and the same event properties (e.g., the time and  
9551 location), within or across documents. Event coreference resolution can be performed us-  
9552 ing supervised learning techniques in a similar way to entity coreference, as described  
9553 in chapter 15: move left-to-right through the document, and use a classifier to decide  
9554 whether to link each event reference to an existing cluster of coreferent events, or to cre-  
9555 ate a new cluster (Ahn, 2006). Each clustering decision is based on the compatibility of  
9556 features describing the participants and properties of the event. Due to the difficulty of  
9557 annotating large amounts of data for entity coreference, unsupervised approaches are es-  
9558 pecially desirable (Chen and Ji, 2009; Bejan and Harabagiu, 2014).

9559 **Relations between events** Just as entities are related to other entities, events may be  
9560 related to other events: for example, the event of winning an election both *precedes* and  
9561 *causes* the event of serving as mayor; moving to Atlanta *precedes* and *enables* the event of  
9562 becoming mayor of Atlanta; moving from Dallas to Atlanta *prevents* the event of later be-  
9563 coming mayor of Dallas. As these examples show, events may be related both temporally  
9564 and causally. The **TimeML** annotation scheme specifies a set of six temporal relations

	Positive (+)	Negative (-)	Underspecified (u)
Certain (CT)	Fact: CT+	Counterfact: CT-	Certain, but unknown: CTU
Probable (PR)	Probable: PR+	Not probable: PR-	(NA)
Possible (PS)	Possible: PS+	Not possible: PS-	(NA)
Underspecified (U)	(NA)	(NA)	Unknown or uncommitted: UU

Table 17.4: Table of factuality values from the FactBank corpus (Saurí and Pustejovsky, 2009). The entry (NA) indicates that this combination is not annotated.

9565 between events (Pustejovsky et al., 2005), derived in part from **interval algebra** (Allen,  
9566 1984). The TimeBank corpus provides TimeML annotations for 186 documents (Pustejovsky  
9567 et al., 2003). Methods for detecting these temporal relations combine supervised  
9568 machine learning with temporal constraints, such as transitivity (e.g. Mani et al., 2006;  
9569 Chambers and Jurafsky, 2008).

9570 More recent annotation schemes and datasets combine temporal and causal relations (Mirza  
9571 et al., 2014; Dunietz et al., 2017): for example, the CaTeRS dataset includes annotations of  
9572 320 five-sentence short stories (Mostafazadeh et al., 2016). Abstracting still further, **processes**  
9573 are networks of causal relations between multiple events. A small dataset of biological  
9574 processes is annotated in the ProcessBank dataset (Berant et al., 2014), with the  
9575 goal of supporting automatic question answering on scientific textbooks.

## 9576 17.4 Hedges, denials, and hypotheticals

9577 The methods described thus far apply to **propositions** about the way things are in the  
9578 real world. But natural language can also describe events and relations that are likely or  
9579 unlikely, possible or impossible, desired or feared. The following examples hint at the  
9580 scope of the problem (Prabhakaran et al., 2010):

- 9581 (17.16) GM will lay off workers.
- 9582 (17.17) A spokesman for GM said GM will lay off workers.
- 9583 (17.18) GM may lay off workers.
- 9584 (17.19) The politician claimed that GM will lay off workers.
- 9585 (17.20) Some wish GM would lay off workers.
- 9586 (17.21) Will GM lay off workers?
- 9587 (17.22) Many wonder whether GM will lay off workers.

9588 Accurate information extraction requires handling these **extra-propositional** aspects  
9589 of meaning, which are sometimes summarized under the terms **modality** and **negation**.<sup>7</sup>  
9590 Modality refers to expressions of the speaker's attitude towards her own statements, in-  
9591 cluding "degree of certainty, reliability, subjectivity, sources of information, and perspec-  
9592 tive" (Morante and Sporleder, 2012). Various systematizations of modality have been  
9593 proposed (e.g., Palmer, 2001), including categories such as future, interrogative, imper-  
9594 ative, conditional, and subjective. Information extraction is particularly concerned with  
9595 negation and certainty. For example, Saurí and Pustejovsky (2009) link negation with  
9596 a modal calculus of certainty, likelihood, and possibility, creating the two-dimensional  
9597 schema shown in Table 17.4. This is the basis for the FactBank corpus, with annotations  
9598 of the **factuality** of all sentences in 208 documents of news text.

9599 A related concept is **hedging**, in which speakers limit their commitment to a proposi-  
9600 tion (Lakoff, 1973):

- 9601 (17.23) These results **suggest** that expression of c-jun, jun B and jun D genes **might** be in-  
9602 volved in terminal granulocyte differentiation... (Morante and Daelemans, 2009)  
9603 (17.24) A whale is **technically** a mammal (Lakoff, 1973)

9604 In the first example, the hedges *suggest* and *might* communicate uncertainty; in the second  
9605 example, there is no uncertainty, but the hedge *technically* indicates that the evidence for  
9606 the proposition will not fully meet the reader's expectations. Hedging has been studied  
9607 extensively in scientific texts (Medlock and Briscoe, 2007; Morante and Daelemans, 2009),  
9608 where the goal of large-scale extraction of scientific facts is obstructed by hedges and spec-  
9609 ulation. Still another related aspect of modality is **evidentiality**, in which speakers mark  
9610 the source of their information. In many languages, it is obligatory to mark evidentiality  
9611 through affixes or particles (Aikhenvald, 2004); while evidentiality is not grammaticalized  
9612 in English, authors are expected to express this information in contexts such as journal-  
9613 ism (Kovach and Rosenstiel, 2014) and Wikipedia.<sup>8</sup>

9614 Methods for handling negation and modality generally include two phases:

- 9615 1. detecting negated or uncertain events;  
9616 2. identifying the scope and focus of the negation or modal operator.

<sup>7</sup>The classification of negation as extra-propositional is controversial: Packard et al. (2014) argue that negation is a "core part of compositionally constructed logical-form representations." Negation is an element of the semantic parsing tasks discussed in chapter 12 and chapter 13 — for example, negation markers are treated as adjuncts in PropBank semantic role labeling. However, many of the relation extraction methods mentioned in this chapter do not handle negation directly. A further consideration is that negation interacts closely with aspects of modality that are generally not considered in propositional semantics, such as certainty and subjectivity.

<sup>8</sup><https://en.wikipedia.org/wiki/Wikipedia:Verifiability>

9617 A considerable body of work on negation has employed rule-based techniques such as  
 9618 regular expressions (Chapman et al., 2001) to detect negated events. Such techniques  
 9619 match lexical cues (e.g., *Norwood was not elected Mayor*), while avoiding “double nega-  
 9620 tives” (e.g., *surely all this is not without meaning*). More recent approaches employ classi-  
 9621 fiers over lexical and syntactic features (Uzuner et al., 2009) and sequence labeling (Prab-  
 9622 hakaran et al., 2010).

9623 The tasks of scope and focus resolution are more fine grained, as shown in the example  
 9624 from Morante and Sporleder (2012):

- 9625 (17.25) [ After his habit he said ] **nothing**, and after mine I asked no questions.  
 9626       After his habit he said nothing, and [ after mine I asked ] **no** [ questions ].

9627 In this sentence, there are two negation cues (*nothing* and *no*). Each negates an event,  
 9628 indicated by the underlined verbs *said* and *asked* (this is the focus of negation), and each  
 9629 occurs within a scope: *after his habit he said* and *after mine I asked* \_\_\_\_ *questions*. These tasks  
 9630 are typically formalized as sequence labeling problems, with each word token labeled  
 9631 as beginning, inside, or outside of a cue, focus, or scope span (see § 8.3). Conventional  
 9632 sequence labeling approaches can then be applied, using surface features as well as syn-  
 9633 tax (Velldal et al., 2012) and semantic analysis (Packard et al., 2014). Labeled datasets  
 9634 include the BioScope corpus of biomedical texts (Vincze et al., 2008) and a shared task  
 9635 dataset of detective stories by Arthur Conan Doyle (Morante and Blanco, 2012).

## 9636 17.5 Question answering and machine reading

9637 The victory of the Watson question-answering system against three top human players on  
 9638 the game show *Jeopardy!* was a landmark moment for natural language processing (Fer-  
 9639 rucci et al., 2010). Game show questions are usually answered by **factoids**: entity names  
 9640 and short phrases.<sup>9</sup> The task of factoid question answering is therefore closely related to  
 9641 information extraction, with the additional problem of accurately parsing the question.

### 9642 17.5.1 Formal semantics

9643 Semantic parsing is an effective method for question-answering in restricted domains  
 9644 such as questions about geography and airline reservations (Zettlemoyer and Collins,  
 9645 2005), and has also been applied in “open-domain” settings such as question answering  
 9646 on Freebase (Berant et al., 2013) and biomedical research abstracts (Poon and Domingos,  
 9647 2009). One approach is to convert the question into a lambda calculus expression that

---

<sup>9</sup>The broader landscape of question answering includes “why” questions (*Why did Ahab continue to pursue the white whale?*), “how questions” (*How did Queequeg die?*), and requests for summaries (*What was Ishmael’s attitude towards organized religion?*). For more, see Hirschman and Gaizauskas (2001).

9648 returns a boolean value: for example, the question *who is the mayor of the capital of Georgia?*  
 9649 would be converted to,

$$\lambda x. \exists y \text{ CAPITAL(GEORGIA, } y) \wedge \text{MAYOR}(y, x). \quad [17.22]$$

9650 This lambda expression can then be used to query an existing knowledge base, returning  
 9651 “true” for all entities that satisfy it.

### 9652 17.5.2 Machine reading

9653 Recent work has focused on answering questions about specific textual passages, similar  
 9654 to the reading comprehension examinations for young students (Hirschman et al., 1999).  
 9655 This task has come to be known as **machine reading**.

#### 9656 17.5.2.1 Datasets

9657 The machine reading problem can be formulated in a number of different ways. The most  
 9658 important distinction is what form the answer should take.

- 9659 • **Multiple-choice question answering**, as in the MCTest dataset of stories (Richardson et al., 2013) and the New York Regents Science Exams (Clark, 2015). In MCTest,  
 9660 the answer is deducible from the text alone, while in the science exams, the system  
 9661 must make inferences using an existing model of the underlying scientific phenomena.  
 9662 Here is an example from MCTest:

9664 (17.26) James the turtle was always getting into trouble. Sometimes he'd reach into  
 9665 the freezer and empty out all the food ...

9666 Q: What is the name of the trouble making turtle?  
 9667 (a) Fries  
 9668 (b) Pudding  
 9669 (c) James  
 9670 (d) Jane

- 9671 • **Cloze-style “fill in the blank”** questions, as in the CNN/Daily Mail comprehension  
 9672 task (Hermann et al., 2015), the Children’s Book Test (Hill et al., 2016), and the Who-  
 9673 did-What dataset (Onishi et al., 2016). In these tasks, the system must guess which  
 9674 word or entity completes a sentence, based on reading a passage of text. Here is an  
 9675 example from Who-did-What:

9676 (17.27) Q: Tottenham manager Juande Ramos has hinted he will allow \_\_\_\_ to leave  
 9677 if the Bulgaria striker makes it clear he is unhappy. (Onishi et al., 2016)

9678     The query sentence may be selected either from the story itself, or from an external  
 9679     summary. In either case, datasets can be created automatically by processing large  
 9680     quantities existing documents. An additional constraint is that that missing element  
 9681     from the cloze must appear in the main passage of text: for example, in Who-did-  
 9682     What, the candidates include all entities mentioned in the main passage. In the  
 9683     CNN/Daily Mail dataset, each entity name is replaced by a unique identifier, e.g.,  
 9684     ENTITY37. This ensures that correct answers can only be obtained by accurately  
 9685     reading the text, and not from external knowledge about the entities.

- 9686     • **Extractive** question answering, in which the answer is drawn from the original text.  
 9687     In WikiQA, answers are sentences (Yang et al., 2015). In the Stanford Question An-  
 9688     swering Dataset (SQuAD), answers are words or short phrases (Rajpurkar et al.,  
 9689     2016):

9690       (17.28) In metereology, precipitation is any product of the condensation of atmo-  
 9691        spheric water vapor that falls under gravity.  
 9692        Q: What causes precipitation to fall? A: gravity

9693       In both WikiQA and SQuAD, the original texts are Wikipedia articles, and the ques-  
 9694       tions are generated by crowdworkers.

### 9695     17.5.2.2 Methods

9696       A baseline method is to search the text for sentences or short passages that overlap with  
 9697       both the query and the candidate answer (Richardson et al., 2013). In example (17.26), this  
 9698       baseline would select the correct answer, since *James* appears in a sentence that includes  
 9699       the query terms *trouble* and *turtle*.

This baseline can be implemented as a neural architecture, using an **attention mechanism** (see § 18.3.1), which scores the similarity of the query to each part of the source text (Chen et al., 2016). The first step is to encode the passage  $w^{(p)}$  and the query  $w^{(q)}$ , using two bidirectional LSTMs (§ 7.6).

$$\mathbf{h}^{(q)} = \text{BiLSTM}(\mathbf{w}^{(q)}; \Theta^{(q)}) \quad [17.23]$$

$$\mathbf{h}^{(p)} = \text{BiLSTM}(\mathbf{w}^{(p)}; \Theta^{(p)}). \quad [17.24]$$

The query is represented by vertically concatenating the final states of the left-to-right and right-to-left passes:

$$\mathbf{u} = [\overrightarrow{\mathbf{h}}^{(q)}_{M_q}; \overleftarrow{\mathbf{h}}^{(q)}_0]. \quad [17.25]$$

The attention vector is computed as a softmax over a vector of bilinear products, and the expected representation is computed by summing over attention values,

$$\tilde{\alpha}_m = (\mathbf{u}^{(q)})^\top \mathbf{W}_a \mathbf{h}_m^{(p)} \quad [17.26]$$

$$\boldsymbol{\alpha} = \text{SoftMax}(\tilde{\boldsymbol{\alpha}}) \quad [17.27]$$

$$\mathbf{o} = \sum_{m=1}^M \alpha_m \mathbf{h}_m^{(p)}. \quad [17.28]$$

Each candidate answer  $c$  is represented by a vector  $\mathbf{x}_c$ . Assuming the candidate answers are spans from the original text, these vectors can be set equal to the corresponding element in  $\mathbf{h}^{(p)}$ . The score for each candidate answer  $a$  is computed by the inner product,

$$\hat{c} = \underset{c}{\operatorname{argmax}} \mathbf{o} \cdot \mathbf{x}_c. \quad [17.29]$$

9700 This architecture can be trained end-to-end from a loss based on the log-likelihood of the  
 9701 correct answer. A number of related architectures have been proposed (e.g., Hermann  
 9702 et al., 2015; Kadlec et al., 2016; Dhingra et al., 2017; Cui et al., 2017), and these methods are  
 9703 surveyed by Wang et al. (2017).

## 9704 Additional resources

9705 The field of information extraction is surveyed in course notes by Grishman (2012), and  
 9706 more recently in a short survey paper (Grishman, 2015). Shen et al. (2015) survey the task  
 9707 of entity linking, and Ji and Grishman (2011) survey work on knowledge base popula-  
 9708 tion. This chapter's discussion of non-propositional meaning was strongly influenced by  
 9709 Morante and Sporleder (2012), who introduced a special issue of the journal *Computational  
 9710 Linguistics* dedicated to recent work on modality and negation.

## 9711 Exercises

- 9712 1. Go to the Wikipedia page for your favorite movie. For each record in the info box  
 9713 (e.g., *Screenplay by: Stanley Kubrick*), report whether there is a sentence in the ar-  
 9714 ticle containing both the field and value (e.g., *The screenplay was written by Stanley  
 9715 Kubrick*). If not, is there a sentence in the article containing just the value? (For  
 9716 records with more than one value, just use the first value.)
- 9717 2. Building on your answer in the previous question, report the dependency path be-  
 9718 tween the head words of the field and value for at least three records.
- 9719 3. Consider the following heuristic for entity linking:

- 9720     • Among all entities that have the same type as the mention (e.g., LOC, PER),  
 9721       choose the one whose name has the lowest edit distance from the mention.  
 9722     • If more than one entity has the right type and the lowest edit distance from the  
 9723       mention, choose the most popular one.  
 9724     • If no candidate entity has the right type, choose NIL.

Now suppose you have the following feature function:

$$f(y, \mathbf{x}) = [\text{edit-dist}(\text{name}(y), \mathbf{x}), \text{same-type}(y, \mathbf{x}), \text{popularity}(y), \delta(y = \text{NIL})]$$

9725     Design a set of ranking weights  $\theta$  that match the heuristic. You may assume that  
 9726       edit distance and popularity are always in the range [0, 100], and that the NIL entity  
 9727       has values of zero for all features except  $\delta(y = \text{NIL})$ .

9728     4. Now consider another heuristic:

- 9729     • Among all candidate entities that have edit distance zero from the mention and  
 9730       the right type, choose the most popular one.  
 9731     • If no entity has edit distance zero from the mention, choose the one with the  
 9732       right type that is most popular, regardless of edit distance.  
 9733     • If no entity has the right type, choose NIL.

9734     Using the same features and assumptions from the previous problem, prove that  
 9735       there is no set of weights that could implement this heuristic. Then show that the  
 9736       heuristic can be implemented by adding a single feature. Your new feature should  
 9737       consider only the edit distance.

9738     5. \* Consider the following formulation for collective entity linking, which rewards  
 9739       sets of entities that are all of the same type, where “types” can be elements of any  
 9740       set:

$$\psi_c(\mathbf{y}) = \begin{cases} \alpha & \text{all entities in } \mathbf{y} \text{ have the same type} \\ \beta & \text{more than half of the entities in } \mathbf{y} \text{ have the same type} \\ 0 & \text{otherwise.} \end{cases} \quad [17.30]$$

9741     Show how to implement this model of collective entity linking in an **integer linear**  
 9742       **program**. You may want to review § 13.2.2.

To get started, here is an integer linear program for entity linking, without including the collective term  $\psi_c$ :

$$\begin{aligned} \max_{z_{i,y} \in \{0,1\}} \quad & \sum_{i=1}^N \sum_{y \in \mathcal{Y}(\mathbf{x}^{(i)})} s_{i,y} z_{i,y} \\ \text{s.t.} \quad & \sum_{y \in \mathcal{Y}(\mathbf{x}^{(i)})} z_{i,y} \leq 1 \quad \forall i \in \{1, 2, \dots, N\} \end{aligned}$$

where  $z_{i,y} = 1$  if entity  $y$  is linked to mention  $i$ , and  $s_{i,y}$  is a parameter that scores the quality of this individual ranking decision, e.g.,  $s_{i,y} = \theta \cdot \mathbf{f}(y, \mathbf{x}^{(i)}, \mathbf{c}^{(i)})$ .

To incorporate the collective linking score, you may assume parameters  $r$ ,

$$r_{y,\tau} = \begin{cases} 1, & \text{entity } y \text{ has type } \tau \\ 0, & \text{otherwise.} \end{cases} \quad [17.31]$$

**Hint:** You will need to define several auxiliary variables to optimize over.

6. Run `nltk.corpus.download('reuters')` to download the Reuters corpus in NLTK, and run from `nltk.corpus import reuters` to import it. The command `reuters.words()` returns an iterator over the tokens in the corpus.
  - a) Apply the pattern *\_\_\_\_\_, such as \_\_\_\_\_* to this corpus, obtaining candidates for the IS-A relation, e.g. IS-A(ROMANIA, COUNTRY). What are three pairs that this method identifies correctly? What are three different pairs that it gets wrong?
  - b) Design a pattern for the PRESIDENT relation, e.g. PRESIDENT(PHILIPPINES, CORAZON AQUINO). In this case, you may want to augment your pattern matcher with the ability to match multiple token wildcards, perhaps using case information to detect proper names. Again, list three correct
  - c) Preprocess the Reuters data by running a named entity recognizer, replacing tokens with named entity spans when applicable. Apply your PRESIDENT matcher to this new data. Does the accuracy improve? Compare 20 randomly-selected pairs from this pattern and the one you designed in the previous part.
7. Represent the dependency path  $\mathbf{x}^{(i)}$  as a sequence of words and dependency arcs of length  $M_i$ , ignoring the endpoints of the path. In example 1 of Table 17.2, the dependency path is,

$$\mathbf{x}^{(1)} = (\xleftarrow[\text{NSUBJ}]{} \text{traveled}, \xrightarrow[\text{OBL}]{} ) \quad [17.32]$$

If  $x_m^{(i)}$  is a word, then let  $\text{pos}(x_m^{(i)})$  be its part-of-speech, using the tagset defined in chapter 8.

We can define the following kernel function over pairs of dependency paths (Bunescu and Mooney, 2005):

$$\kappa(\mathbf{x}^{(i)}, \mathbf{x}^{(j)}) = \begin{cases} 0, & M_i \neq M_j \\ \prod_{m=1}^{M_i} c(x_m^{(i)}, x_m^{(j)}), & M_i = M_j \end{cases}$$

$$c(x_m^{(i)}, x_m^{(j)}) = \begin{cases} 2, & x_m^{(i)} = x_m^{(j)} \\ 1, & x_m^{(i)} \text{ and } x_m^{(j)} \text{ are words and } \text{pos}(x_m^{(i)}) = \text{pos}(x_m^{(j)}) \\ 0, & \text{otherwise.} \end{cases}$$

Using this kernel function, compute the kernel similarities of example 1 from Table 17.2 with the other five examples.

- 9766        8. Continuing from the previous problem, suppose that the instances have the follow-  
 9767        ing labels:

$$y_2 = 1, y_3 = -1, y_4 = -1, y_5 = 1, y_6 = 1 \quad [17.33]$$

9768        Identify the conditions for  $\alpha$  and  $b$  under which  $\hat{y}_1 = 1$ . Remember the constraint  
 9769        that  $\alpha_i \geq 0$  for all  $i$ .

9770        9. Using the `reuters` corpus in `nltk`, apply distant supervision to build a training  
 9771        set for detecting the relation between nations and their capitals. Start with the fol-  
 9772        lowing known relations: (JAPAN, TOKYO), (FRANCE, PARIS), (ITALY, ROME). How  
 9773        many positive and negative examples are you able to extract?

9774        10. Identify the focus and scope of negation in the following examples:

- 9775        (17.29)    a. As no better man advances to take this matter in hand, I hereupon offer  
 9776                my own poor endeavors.  
 9777                b. That's no way to convert sinners, cook!  
 9778                c. And concerning all these, is not Possession the whole of the law?  
 9779                d. And had Flask helped himself, the chances were Ahab had never so  
 9780                much as noticed it.

9781        11. Consider the neural QA system described in § 17.5.2.2, but restrict the set of can-  
 9782        didate answers to words in the passage, and set each candidate answer embed-  
 9783        ding  $\mathbf{x}$  equal to the vector  $\mathbf{h}_m^{(p)}$ , representing token  $m$  in the passage, so that  $\hat{m} = \arg\max_m \mathbf{o} \cdot \mathbf{h}_m^{(p)}$ . Suppose the system selects answer  $\hat{m}$ , but the correct answer is  $m^*$ .  
 9784        Consider the gradient of the margin loss with respect to the attention:  
 9785

- 9786        a) Prove that  $\frac{\partial \ell}{\partial \alpha_{\hat{m}}} \geq \frac{\partial \ell}{\partial \alpha_{m^*}}$ .

- 9787        b) Assuming that  $\|\mathbf{h}_{\hat{m}}\| = \|\mathbf{h}_{m^*}\|$ , prove that  $\frac{\partial \ell}{\partial \alpha_{\hat{m}}} \geq 0$  and  $\frac{\partial \ell}{\partial \alpha_{m^*}} \leq 0$ . Explain in  
9788        words what this means about how the attention is expected to change after a  
9789        gradient-based update.



9790 

# Chapter 18

9791 

## Machine translation

9792 Machine translation (MT) is one of the “holy grail” problems in artificial intelligence,  
9793 with the potential to transform society by facilitating communication between people  
9794 anywhere in the world. As a result, MT has received significant attention and funding  
9795 since the early 1950s. However, it has proved remarkably challenging, and while there  
9796 has been substantial progress towards usable MT systems — especially for high-resource  
9797 language pairs like English-French — we are still far from translation systems that match  
9798 the nuance and depth of human translations.

9799 

### 18.1 Machine translation as a task

9800 Machine translation can be formulated as an optimization problem:

$$\hat{\mathbf{w}}^{(t)} = \underset{\mathbf{w}^{(t)}}{\operatorname{argmax}} \Psi(\mathbf{w}^{(s)}, \mathbf{w}^{(t)}), \quad [18.1]$$

9801 where  $\mathbf{w}^{(s)}$  is a sentence in a **source** language,  $\mathbf{w}^{(t)}$  is a sentence in the **target language**,  
9802 and  $\Psi$  is a scoring function. As usual, this formalism requires two components: a decod-  
9803 ing algorithm for computing  $\hat{\mathbf{w}}^{(t)}$ , and a learning algorithm for estimating the parameters  
9804 of the scoring function  $\Psi$ .

9805 Decoding is difficult for machine translation because of the huge space of possible  
9806 translations. We have faced large label spaces before: for example, in sequence labeling,  
9807 the set of possible label sequences is exponential in the length of the input. In these cases,  
9808 it was possible to search the space quickly by introducing locality assumptions: for ex-  
9809 ample, that each tag depends only on its predecessor, or that each production depends  
9810 only on its parent. In machine translation, no such locality assumptions seem possible:  
9811 human translators reword, reorder, and rearrange words; they replace single words with  
9812 multi-word phrases, and vice versa. This flexibility means that in even relatively simple

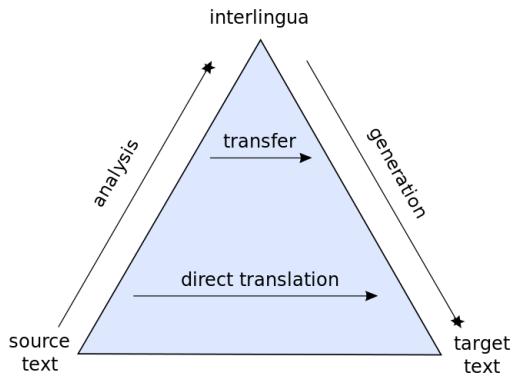


Figure 18.1: The Vauquois Pyramid [http://commons.wikimedia.org/wiki/File:Direct\\_translation\\_and\\_transfer\\_translation\\_pyramind.svg](http://commons.wikimedia.org/wiki/File:Direct_translation_and_transfer_translation_pyramind.svg)

9813 translation models, decoding is NP-hard (Knight, 1999). Approaches for dealing with this  
 9814 complexity are described in § 18.4.

Estimating translation models is difficult as well. Labeled translation data usually comes in the form parallel sentences, e.g.,

$$\begin{aligned} w^{(s)} &= A \text{ Vinay le gusta las manzanas.} \\ w^{(t)} &= \text{Vinay likes apples.} \end{aligned}$$

9815 A useful feature function would note the translation pairs (*gusta, likes*), (*manzanas, apples*),  
 9816 and even (*Vinay, Vinay*). But this word-to-word **alignment** is not given in the data. One  
 9817 solution is to treat this alignment as a **latent variable**; this is the approach taken by clas-  
 9818 sical **statistical machine translation** (SMT) systems, described in § 18.2. Another solution  
 9819 is to model the relationship between  $w^{(t)}$  and  $w^{(s)}$  through a more complex and expres-  
 9820 sive function; this is the approach taken by **neural machine translation** (NMT) systems,  
 9821 described in § 18.3.

9822 The **Vauquois Pyramid** is a theory of how translation should be done. At the lowest  
 9823 level, the translation system operates on individual words, but the horizontal distance  
 9824 at this level is large, because languages express ideas differently. If we can move up the  
 9825 triangle to syntactic structure, the distance for translation is reduced; we then need only  
 9826 produce target-language text from the syntactic representation, which can be as simple  
 9827 as reading off a tree. Further up the triangle lies semantics; translating between semantic  
 9828 representations should be easier still, but mapping between semantics and surface text is a  
 9829 difficult, unsolved problem. At the top of the triangle is **interlingua**, a semantic represen-  
 9830 tation that is so generic that it is identical across all human languages. Philosophers de-  
 9831 bate whether such a thing as interlingua is really possible (e.g., Derrida, 1985). While the

	Adequate?	Fluent?
<i>To Vinay it like Python</i>	yes	no
<i>Vinay debugs memory leaks</i>	no	yes
<i>Vinay likes Python</i>	yes	yes

Table 18.1: Adequacy and fluency for translations of the Spanish sentence *A Vinay le gusta Python*.

first-order logic representations discussed in chapter 12 might be thought to be language independent, they are built on an inventory of predicates that are suspiciously similar to English words (Nirenburg and Wilks, 2001). Nonetheless, the idea of linking translation and semantic understanding may still be a promising path, if the resulting translations better preserve the meaning of the original text.

### 18.1.1 Evaluating translations

There are two main criteria for a translation, summarized in Table 18.1.

- **Adequacy:** The translation  $w^{(t)}$  should adequately reflect the linguistic content of  $w^{(s)}$ . For example, if  $w^{(s)} = A Vinay le gusta Python$ , the gloss<sup>1</sup>  $w^{(t)} = To Vinay it like Python$  is considered adequate becomes it contains all the relevant content. The output  $w^{(t)} = Vinay debugs memory leaks$  is not adequate.
- **Fluency:** The translation  $w^{(t)}$  should read like fluent text in the target language. By this criterion, the gloss  $w^{(t)} = To Vinay it like Python$  will score poorly, and  $w^{(t)} = Vinay debugs memory leaks$  will be preferred.

Automated evaluations of machine translations typically merge both of these criteria, by comparing the system translation with one or more **reference translations**, produced by professional human translators. The most popular quantitative metric is **BLEU** (bilingual evaluation understudy; Papineni et al., 2002), which is based on  $n$ -gram precision: what fraction of  $n$ -grams in the system translation appear in the reference? Specifically, for each  $n$ -gram length, the precision is defined as,

$$p_n = \frac{\text{number of } n\text{-grams appearing in both reference and hypothesis translations}}{\text{number of } n\text{-grams appearing in the hypothesis translation}}. \quad [18.2]$$

The  $n$ -gram precisions for three hypothesis translations are shown in Figure 18.2.

The BLEU score is then based on the average,  $\exp \frac{1}{N} \sum_{n=1}^N \log p_n$ . Two modifications of Equation 18.2 are necessary: (1) to avoid computing  $\log 0$ , all precisions are smoothed

<sup>1</sup>A gloss is a word-for-word translation.

	<b>Translation</b>	$p_1$	$p_2$	$p_3$	$p_4$	BP	BLEU
<i>Reference</i>	<i>Vinay likes programming in Python</i>						
<i>Sys1</i>	<i>To Vinay it like to program Python</i>	$\frac{2}{7}$	0	0	0	1	.21
<i>Sys2</i>	<i>Vinay likes Python</i>	$\frac{3}{3}$	$\frac{1}{2}$	0	0	.51	.33
<i>Sys3</i>	<i>Vinay likes programming in his pajamas</i>	$\frac{4}{6}$	$\frac{3}{5}$	$\frac{2}{4}$	$\frac{1}{3}$	1	.76

Figure 18.2: A reference translation and three system outputs. For each output,  $p_n$  indicates the precision at each  $n$ -gram, and BP indicates the brevity penalty.

to ensure that they are positive; (2) each  $n$ -gram in the reference can be used at most once, so that *to to to to to* does not achieve  $p_1 = 1$  against the reference *to be or not to be*. Furthermore, precision-based metrics are biased in favor of short translations, which can achieve high scores by minimizing the denominator in [18.2]. To avoid this issue, a **brevity penalty** is applied to translations that are shorter than the reference. This penalty is indicated as “BP” in Figure 18.2.

Automated metrics like BLEU have been validated by correlation with human judgments of translation quality. Nonetheless, it is not difficult to construct examples in which the BLEU score is high, yet the translation is disfluent or carries a completely different meaning from the original. To give just one example, consider the problem of translating pronouns. Because pronouns refer to specific entities, a single incorrect pronoun can obliterate the semantics of the original sentence. Existing state-of-the-art systems generally do not attempt the reasoning necessary to correctly resolve pronominal anaphora (Hartmeier, 2012). Despite the importance of pronouns for semantics, they have a marginal impact on BLEU, which may help to explain why existing systems do not make a greater effort to translate them correctly.

**Fairness and bias** The problem of pronoun translation intersects with issues of fairness and bias. In many languages, such as Turkish, the third person singular pronoun is gender neutral. Today’s state-of-the-art systems produce the following Turkish-English translations (Caliskan et al., 2017):

- 9875 (18.1) *O bir doktor.*  
He is a doctor.
- 9876 (18.2) *O bir hemşire.*  
She is a nurse.

The same problem arises for other professions that have stereotypical genders, such as engineers, soldiers, and teachers, and for other languages that have gender-neutral pro-

nouns. This bias was not directly programmed into the translation model; it arises from statistical tendencies in existing datasets. This highlights a general problem with data-driven approaches, which can perpetuate biases that negatively impact disadvantaged groups. Worse, machine learning can *amplify* biases in data (Bolukbasi et al., 2016): if a dataset has even a slight tendency towards men as doctors, the resulting translation model may produce translations in which doctors are always *he*, and nurses are always *she*.

**Other metrics** A range of other automated metrics have been proposed for machine translation. One potential weakness of BLEU is that it only measures precision; METEOR is a weighted *F*-MEASURE, which is a combination of recall and precision (see § 4.4.1). **Translation Error Rate (TER)** computes the string **edit distance** (see § 9.1.4.1) between the reference and the hypothesis (Snover et al., 2006). For language pairs like English and Japanese, there are substantial differences in word order, and word order errors are not sufficiently captured by *n*-gram based metrics. The **RIBES** metric applies rank correlation to measure the similarity in word order between the system and reference translations (Isozaki et al., 2010).

### 18.1.2 Data

Data-driven approaches to machine translation rely primarily on **parallel corpora**: sentence-level translations. Early work focused on government records, in which fine-grained official translations are often required. For example, the IBM translation systems were based on the proceedings of the Canadian Parliament, called **Hansards**, which are recorded in English and French (Brown et al., 1990). The growth of the European Union led to the development of the **EuroParl corpus**, which spans 21 European languages (Koehn, 2005). While these datasets helped to launch the field of machine translation, they are restricted to narrow domains and a formal speaking style, limiting their applicability to other types of text. As more resources are committed to machine translation, new translation datasets have been commissioned. This has broadened the scope of available data to news,<sup>2</sup> movie subtitles,<sup>3</sup> social media (Ling et al., 2013), dialogues (Fordyce, 2007), TED talks (Paul et al., 2010), and scientific research articles (Nakazawa et al., 2016).

Despite this growing set of resources, the main bottleneck in machine translation data is the need for parallel corpora that are aligned at the sentence level. Many languages have sizable parallel corpora with some high-resource language, but not with each other. The high-resource language can then be used as a “pivot” or “bridge” (Boitet, 1988; Utiyama and Isahara, 2007): for example, De Gispert and Marino (2006) use Spanish as a bridge for translation between Catalan and English. For most of the 6000 languages spoken today,

<sup>2</sup>[https://catalog.ldc.upenn.edu/LDC2010T10\\_translation-task.html](https://catalog.ldc.upenn.edu/LDC2010T10_translation-task.html) <http://www.statmt.org/wmt15/>

<sup>3</sup><http://opus.nlpl.eu/>

the only source of translation data remains the Judeo-Christian Bible (Resnik et al., 1999). While relatively small, at less than a million tokens, the Bible has been translated into more than 2000 languages, far outpacing any other corpus. Some research has explored the possibility of automatically identifying parallel sentence pairs from unaligned parallel texts, such as web pages and Wikipedia articles (Kilgarriff and Grefenstette, 2003; Resnik and Smith, 2003; Adafre and De Rijke, 2006). Another approach is to create large parallel corpora through crowdsourcing (Zaidan and Callison-Burch, 2011).

## 18.2 Statistical machine translation

The previous section introduced adequacy and fluency as the two main criteria for machine translation. A natural modeling approach is to represent them with separate scores,

$$\Psi(\mathbf{w}^{(s)}, \mathbf{w}^{(t)}) = \Psi_A(\mathbf{w}^{(s)}, \mathbf{w}^{(t)}) + \Psi_F(\mathbf{w}^{(t)}). \quad [18.3]$$

The fluency score  $\Psi_F$  need not even consider the source sentence; it only judges  $\mathbf{w}^{(t)}$  on whether it is fluent in the target language. This decomposition is advantageous because it makes it possible to estimate the two scoring functions on separate data. While the adequacy model must be estimated from aligned sentences — which are relatively expensive and rare — the fluency model can be estimated from monolingual text in the target language. Large monolingual corpora are now available in many languages, thanks to resources such as Wikipedia.

An elegant justification of the decomposition in Equation 18.3 is provided by the **noisy channel model**, in which each scoring function is a log probability:

$$\Psi_A(\mathbf{w}^{(s)}, \mathbf{w}^{(t)}) \triangleq \log p_{S|T}(\mathbf{w}^{(s)} | \mathbf{w}^{(t)}) \quad [18.4]$$

$$\Psi_F(\mathbf{w}^{(t)}) \triangleq \log p_T(\mathbf{w}^{(t)}) \quad [18.5]$$

$$\Psi(\mathbf{w}^{(s)}, \mathbf{w}^{(t)}) = \log p_{S|T}(\mathbf{w}^{(s)} | \mathbf{w}^{(t)}) + \log p_T(\mathbf{w}^{(t)}) = \log p_{S,T}(\mathbf{w}^{(s)}, \mathbf{w}^{(t)}). \quad [18.6]$$

By setting the scoring functions equal to the logarithms of the prior and likelihood, their sum is equal to  $\log p_{S,T}$ , which is the logarithm of the joint probability of the source and target. The sentence  $\hat{\mathbf{w}}^{(t)}$  that maximizes this joint probability is also the maximizer of the conditional probability  $p_{T|S}$ , making it the most likely target language sentence, conditioned on the source.

The noisy channel model can be justified by a generative story. The target text is originally generated from a probability model  $p_T$ . It is then encoded in a “noisy channel”  $p_{S|T}$ , which converts it to a string in the source language. In decoding, we apply Bayes’ rule to recover the string  $\mathbf{w}^{(t)}$  that is maximally likely under the conditional probability  $p_{T|S}$ . Under this interpretation, the target probability  $p_T$  is just a language model, and can be estimated using any of the techniques from chapter 6. The only remaining learning problem is to estimate the translation model  $p_{S|T}$ .

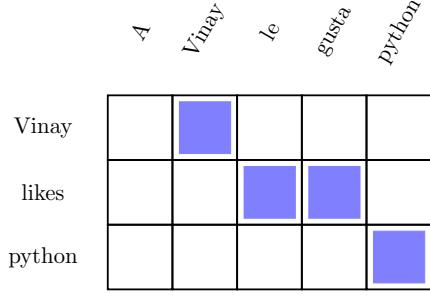


Figure 18.3: An example word-to-word alignment

### 18.2.1 Statistical translation modeling

The simplest decomposition of the translation model is word-to-word: each word in the source should be aligned to a word in the translation. This approach presupposes an alignment  $\mathcal{A}(\mathbf{w}^{(s)}, \mathbf{w}^{(t)})$ , which contains a list of pairs of source and target tokens. For example, given  $\mathbf{w}^{(s)} = A\ Vinay\ le\ gusta\ Python$  and  $\mathbf{w}^{(t)} = Vinay\ likes\ Python$ , one possible word-to-word alignment is,

$$\mathcal{A}(\mathbf{w}^{(s)}, \mathbf{w}^{(t)}) = \{(A, \emptyset), (Vinay, Vinay), (le, likes), (gusta, likes), (Python, Python)\}. \quad [18.7]$$

This alignment is shown in Figure 18.3. Another, less promising, alignment is:

$$\mathcal{A}(\mathbf{w}^{(s)}, \mathbf{w}^{(t)}) = \{(A, Vinay), (Vinay, likes), (le, Python), (gusta, \emptyset), (Python, \emptyset)\}. \quad [18.8]$$

Each alignment contains exactly one tuple for each word in the *source*, which serves to explain how the source word could be translated from the target, as required by the translation probability  $p_{S|T}$ . If no appropriate word in the target can be identified for a source word, it is aligned to  $\emptyset$  — as is the case for the Spanish function word *a* in the example, which glosses to the English word *to*. Words in the target can align with multiple words in the source, so that the target word *likes* can align to both *le* and *gusta* in the source.

The joint probability of the alignment and the translation can be defined conveniently as,

$$p(\mathbf{w}^{(s)}, \mathcal{A} | \mathbf{w}^{(t)}) = \prod_{m=1}^{M^{(s)}} p(w_m^{(s)}, a_m | w_{a_m}^{(t)}, m, M^{(s)}, M^{(t)}) \quad [18.9]$$

$$= \prod_{m=1}^{M^{(s)}} p(a_m | m, M^{(s)}, M^{(t)}) \times p(w_m^{(s)} | w_{a_m}^{(t)}). \quad [18.10]$$

This probability model makes two key assumptions:

- 9956 • The alignment probability factors across tokens,

$$p(\mathcal{A} \mid \mathbf{w}^{(s)}, \mathbf{w}^{(t)}) = \prod_{m=1}^{M^{(s)}} p(a_m \mid m, M^{(s)}, M^{(t)}). \quad [18.11]$$

9957 This means that each alignment decision is independent of the others, and depends  
 9958 only on the index  $m$ , and the sentence lengths  $M^{(s)}$  and  $M^{(t)}$ .

- 9959 • The translation probability also factors across tokens,

$$p(\mathbf{w}^{(s)} \mid \mathbf{w}^{(t)}, \mathcal{A}) = \prod_{m=1}^{M^{(s)}} p(w_m^{(s)} \mid w_{a_m}^{(t)}), \quad [18.12]$$

9960 so that each word in  $\mathbf{w}^{(s)}$  depends only on its aligned word in  $\mathbf{w}^{(t)}$ . This means that  
 9961 translation is word-to-word, ignoring context. The hope is that the target language  
 9962 model  $p(\mathbf{w}^{(t)})$  will correct any disfluencies that arise from word-to-word translation.

To translate with such a model, we could sum or max over all possible alignments,

$$p(\mathbf{w}^{(s)}, \mathbf{w}^{(t)}) = \sum_{\mathcal{A}} p(\mathbf{w}^{(s)}, \mathbf{w}^{(t)}, \mathcal{A}) \quad [18.13]$$

$$= p(\mathbf{w}^{(t)}) \sum_{\mathcal{A}} p(\mathcal{A}) \times p(\mathbf{w}^{(s)} \mid \mathbf{w}^{(t)}, \mathcal{A}) \quad [18.14]$$

$$\geq p(\mathbf{w}^{(t)}) \max_{\mathcal{A}} p(\mathcal{A}) \times p(\mathbf{w}^{(s)} \mid \mathbf{w}^{(t)}, \mathcal{A}). \quad [18.15]$$

The term  $p(\mathcal{A})$  defines the prior probability over alignments. A series of alignment models with increasingly relaxed independence assumptions was developed by researchers at IBM in the 1980s and 1990s, known as IBM Models 1-6 (Och and Ney, 2003). IBM Model 1 makes the strongest independence assumption:

$$p(a_m \mid m, M^{(s)}, M^{(t)}) = \frac{1}{M^{(t)}}. \quad [18.16]$$

9963 In this model, every alignment is equally likely. This is almost surely wrong, but it re-  
 9964 sults in a convex learning objective, yielding a good initialization for the more complex  
 9965 alignment models (Brown et al., 1993; Koehn, 2009).

### 9966 18.2.2 Estimation

9967 Let us define the parameter  $\theta_{u \rightarrow v}$  as the probability of translating target word  $u$  to source  
 9968 word  $v$ . If word-to-word alignments were annotated, these probabilities could be com-  
 9969 puted from relative frequencies,

$$\hat{\theta}_{u \rightarrow v} = \frac{\text{count}(u, v)}{\text{count}(u)}, \quad [18.17]$$

9970 where  $\text{count}(u, v)$  is the count of instances in which word  $v$  was aligned to word  $u$  in  
 9971 the training set, and  $\text{count}(u)$  is the total count of the target word  $u$ . The smoothing  
 9972 techniques mentioned in chapter 6 can help to reduce the variance of these probability  
 9973 estimates.

9974 Conversely, if we had an accurate translation model, we could estimate the likelihood  
 9975 of each alignment decision,

$$q_m(a_m \mid \mathbf{w}^{(s)}, \mathbf{w}^{(t)}) \propto p(a_m \mid m, M^{(s)}, M^{(t)}) \times p(w_m^{(s)} \mid w_{a_m}^{(t)}), \quad [18.18]$$

where  $q_m(a_m \mid \mathbf{w}^{(s)}, \mathbf{w}^{(t)})$  is a measure of our confidence in aligning source word  $w_m^{(s)}$   
 to target word  $w_{a_m}^{(t)}$ . The relative frequencies could then be computed from the *expected  
 counts*,

$$\hat{\theta}_{u \rightarrow v} = \frac{E_q [\text{count}(u, v)]}{\text{count}(u)} \quad [18.19]$$

$$E_q [\text{count}(u, v)] = \sum_m q_m(a_m \mid \mathbf{w}^{(s)}, \mathbf{w}^{(t)}) \times \delta(w_m^{(s)} = v) \times \delta(w_{a_m}^{(t)} = u). \quad [18.20]$$

9976 The **expectation-maximization** (EM) algorithm proceeds by iteratively updating  $q_m$   
 9977 and  $\hat{\Theta}$ . The algorithm is described in general form in chapter 5. For statistical machine  
 9978 translation, the steps of the algorithm are:

- 9979 1. **E-step:** Update beliefs about word alignment using Equation 18.18.  
 9980 2. **M-step:** Update the translation model using Equations 18.19 and 18.20.

9981 As discussed in chapter 5, the expectation maximization algorithm is guaranteed to con-  
 9982 verge, but not to a global optimum. However, for IBM Model 1, it can be shown that EM  
 9983 optimizes a convex objective, and global optimality is guaranteed. For this reason, IBM  
 9984 Model 1 is often used as an initialization for more complex alignment models. For more  
 9985 detail, see Koehn (2009).

### 9986 18.2.3 Phrase-based translation

9987 Real translations are not word-to-word substitutions. One reason is that many multiword  
 9988 expressions are not translated literally, as shown in this example from French:

- 9989 (18.3) *Nous allons prendre un verre*  
 We will take a glass  
 9990 We'll have a drink

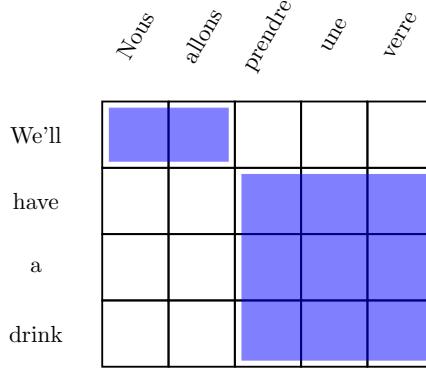


Figure 18.4: A phrase-based alignment between French and English, corresponding to example (18.3)

9991 The line *we will take a glass* is the word-for-word gloss of the French sentence; the transla-  
 9992 tion *we'll have a drink* is shown on the third line. Such examples are difficult for word-to-  
 9993 word translation models, since they require translating *prendre* to *have* and *verre* to *drink*.  
 9994 These translations are only correct in the context of these specific phrases.

Phrase-based translation generalizes on word-based models by building translation tables and alignments between multiword spans. (These “phrases” are not necessarily syntactic constituents like the noun phrases and verb phrases described in chapters 9 and 10.) The generalization from word-based translation is surprisingly straightforward: the translation tables can now condition on multi-word units, and can assign probabilities to multi-word units; alignments are mappings from spans to spans,  $((i, j), (k, \ell))$ , so that

$$p(\mathbf{w}^{(s)} | \mathbf{w}^{(t)}, \mathcal{A}) = \prod_{((i, j), (k, \ell)) \in \mathcal{A}} p_{w^{(s)}|w^{(t)}}(\{w_{i+1}^{(s)}, w_{i+2}^{(s)}, \dots, w_j^{(s)}\} | \{w_{k+1}^{(t)}, w_{k+2}^{(t)}, \dots, w_\ell^{(t)}\}). \quad [18.21]$$

9995 The phrase alignment  $((i, j), (k, \ell))$  indicates that the span  $\mathbf{w}_{i+1:j}^{(s)}$  is the translation of the  
 9996 span  $\mathbf{w}_{k+1:\ell}^{(t)}$ . An example phrasal alignment is shown in Figure 18.4. Note that the align-  
 9997 ment set  $\mathcal{A}$  is required to cover all of the tokens in the source, just as in word-based trans-  
 9998 lation. The probability model  $p_{w^{(s)}|w^{(t)}}$  must now include translations for all phrase pairs,  
 9999 which can be learned from expectation-maximization just as in word-based statistical ma-  
 10000 chine translation.

10001 **18.2.4 \*Syntax-based translation**

10002 The Vauquois Pyramid (Figure 18.1) suggests that translation might be easier if we take a  
 10003 higher-level view. One possibility is to incorporate the syntactic structure of the source,  
 10004 the target, or both. This is particularly promising for language pairs that consistent syn-  
 10005 tactic differences. For example, English adjectives almost always precede the nouns that  
 10006 they modify, while in Romance languages such as French and Spanish, the adjective often  
 10007 follows the noun: thus, *angry fish* would translate to *pez (fish) enojado (angry)* in Spanish.  
 10008 In word-to-word translation, these reorderings cause the alignment model to be overly  
 10009 permissive. It is not that the order of *any* pair of English words can be reversed when  
 10010 translating into Spanish, but only adjectives and nouns within a noun phrase. Similar  
 10011 issues arise when translating between verb-final languages such as Japanese (in which  
 10012 verbs usually follow the subject and object), verb-initial languages like Tagalog and clas-  
 10013 sical Arabic, and verb-medial languages such as English.

10014 An elegant solution is to link parsing and translation in a **synchronous context-free**  
 10015 **grammar** (SCFG; Chiang, 2007).<sup>4</sup> An SCFG is a set of productions of the form  $X \rightarrow (\alpha, \beta, \sim)$ ,  
 10016 where  $X$  is a non-terminal,  $\alpha$  and  $\beta$  are sequences of terminals or non-terminals, and  $\sim$   
 10017 is a one-to-one alignment of items in  $\alpha$  with items in  $\beta$ . To handle the English-Spanish  
 10018 adjective-noun ordering, an SCFG would include productions such as,

$$\text{NP} \rightarrow (\text{DET}_1 \text{NN}_2 \text{JJ}_3, \quad \text{DET}_1 \text{JJ}_3 \text{NN}_2), \quad [18.22]$$

10019 with subscripts indicating the alignment between the Spanish (left) and English (right)  
 10020 parts of the right-hand side. Terminal productions yield translation pairs,

$$\text{JJ} \rightarrow (enojado_1, angry_1). \quad [18.23]$$

10021 A synchronous derivation begins with the start symbol  $S$ , and derives a pair of sequences  
 10022 of terminal symbols.

10023 Given an SCFG in which each production yields at most two symbols in each language  
 10024 (Chomsky Normal Form; see § 9.2.1.2), a sentence can be parsed using only the CKY  
 10025 algorithm (chapter 10). The resulting derivation also includes productions in the other  
 10026 language, all the way down to the surface form. Therefore, SCFGs make translation very  
 10027 similar to parsing. In a weighted SCFG, the log probability  $\log p_{S|T}$  can be computed from  
 10028 the sum of the log-probabilities of the productions. However, combining SCFGs with a  
 10029 target language model is computationally expensive, necessitating approximate search  
 10030 algorithms (Huang and Chiang, 2007).

10031 Synchronous context-free grammars are an example of **tree-to-tree translation**, be-  
 10032 cause they model the syntactic structure of both the target and source language. In **string-**  
 10033 **to-tree translation**, string elements are translated into constituent tree fragments, which

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<sup>4</sup>Key earlier work includes syntax-driven transduction (Lewis II and Stearns, 1968) and stochastic inver-  
 sion transduction grammars (Wu, 1997).

10034 are then assembled into a translation (Yamada and Knight, 2001; Galley et al., 2004); in  
 10035 **tree-to-string translation**, the source side is parsed, and then transformed into a string on  
 10036 the target side (Liu et al., 2006). A key question for syntax-based translation is the extent  
 10037 to which we phrasal constituents align across translations (Fox, 2002), because this gov-  
 10038 erns the extent to which we can rely on monolingual parsers and treebanks. For more on  
 10039 syntax-based machine translation, see the monograph by Williams et al. (2016).

### 10040 18.3 Neural machine translation

Neural network models for machine translation are based on the **encoder-decoder** architecture (Cho et al., 2014). The encoder network converts the source language sentence into a vector or matrix representation; the decoder network then converts the encoding into a sentence in the target language.

$$\mathbf{z} = \text{ENCODE}(\mathbf{w}^{(s)}) \quad [18.24]$$

$$\mathbf{w}^{(t)} \mid \mathbf{w}^{(s)} \sim \text{DECODE}(\mathbf{z}), \quad [18.25]$$

10041 where the second line means that the function  $\text{DECODE}(\mathbf{z})$  defines the conditional proba-  
 10042 bility  $p(\mathbf{w}^{(t)} \mid \mathbf{w}^{(s)})$ .

The decoder is typically a recurrent neural network, which generates the target language sentence one word at a time, while recurrently updating a hidden state. The encoder and decoder networks are trained end-to-end from parallel sentences. If the output layer of the decoder is a logistic function, then the entire architecture can be trained to maximize the conditional log-likelihood,

$$\log p(\mathbf{w}^{(t)} \mid \mathbf{w}^{(s)}) = \sum_{m=1}^{M^{(t)}} p(w_m^{(t)} \mid \mathbf{w}_{1:m-1}^{(t)}, \mathbf{z}) \quad [18.26]$$

$$p(w_m^{(t)} \mid \mathbf{w}_{1:m-1}^{(t)}, \mathbf{w}^{(s)}) \propto \exp \left( \boldsymbol{\beta}_{w_m^{(t)}} \cdot \mathbf{h}_{m-1}^{(t)} \right) \quad [18.27]$$

where the hidden state  $\mathbf{h}_{m-1}^{(t)}$  is a recurrent function of the previously generated text  $\mathbf{w}_{1:m-1}^{(t)}$  and the encoding  $\mathbf{z}$ . The second line is equivalent to writing,

$$w_m^{(t)} \mid \mathbf{w}_{1:m-1}^{(t)}, \mathbf{w}^{(s)} \sim \text{SoftMax} \left( \boldsymbol{\beta} \cdot \mathbf{h}_{m-1}^{(t)} \right), \quad [18.28]$$

10043 where  $\boldsymbol{\beta} \in \mathbb{R}^{(V^{(t)} \times K)}$  is the matrix of output word vectors for the  $V^{(t)}$  words in the target  
 10044 language vocabulary.

The simplest encoder-decoder architecture is the **sequence-to-sequence** model (Sutskever et al., 2014). In this model, the encoder is set to the final hidden state of a **long short-term**

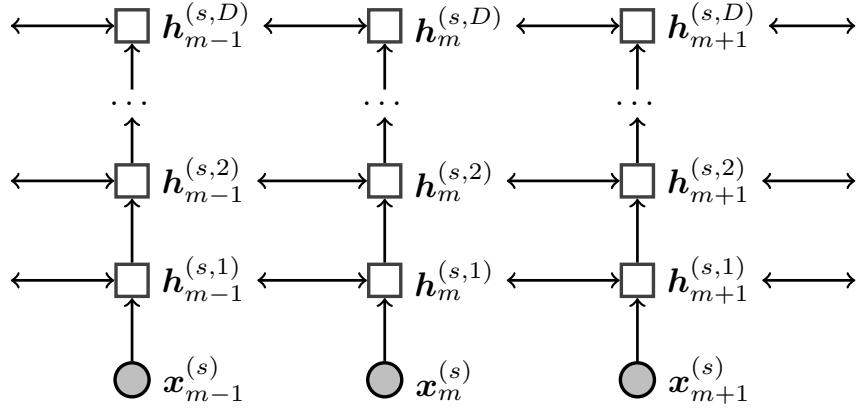


Figure 18.5: A deep bidirectional LSTM encoder

**memory (LSTM)** (see § 6.3.3) on the source sentence:

$$\mathbf{h}_m^{(s)} = \text{LSTM}(\mathbf{x}_m^{(s)}, \mathbf{h}_{m-1}^{(s)}) \quad [18.29]$$

$$\mathbf{z} \triangleq \mathbf{h}_{M^{(s)}}^{(s)}, \quad [18.30]$$

where  $\mathbf{x}_m^{(s)}$  is the embedding of source language word  $w_m^{(s)}$ . The encoding then provides the initial hidden state for the decoder LSTM:

$$\mathbf{h}_0^{(t)} = \mathbf{z} \quad [18.31]$$

$$\mathbf{h}_m^{(t)} = \text{LSTM}(\mathbf{x}_m^{(t)}, \mathbf{h}_{m-1}^{(t)}), \quad [18.32]$$

10045 where  $\mathbf{x}_m^{(t)}$  is the embedding of the target language word  $w_m^{(t)}$ .

10046 Sequence-to-sequence translation is nothing more than wiring together two LSTMs:  
 10047 one to read the source, and another to generate the target. To make the model work well,  
 10048 some additional tweaks are needed:

- 10049 • Most notably, the model works much better if the source sentence is reversed, reading  
 10050 from the end of the sentence back to the beginning. In this way, the words at the  
 10051 beginning of the source have the greatest impact on the encoding  $\mathbf{z}$ , and therefore  
 10052 impact the words at the beginning of the target sentence. Later work on more advanced  
 10053 encoding models, such as **neural attention** (see § 18.3.1), has eliminated the  
 10054 need for reversing the source sentence.
- The encoder and decoder can be implemented as **deep LSTMs**, with multiple layers of hidden states. As shown in Figure 18.5, each hidden state  $\mathbf{h}_m^{(s,i)}$  at layer  $i$  is treated

as the input to an LSTM at layer  $i + 1$ :

$$\mathbf{h}_m^{(s,1)} = \text{LSTM}(\mathbf{x}_m^{(s)}, \mathbf{h}_{m-1}^{(s)}) \quad [18.33]$$

$$\mathbf{h}_m^{(s,i+1)} = \text{LSTM}(\mathbf{h}_m^{(s,i)}, \mathbf{h}_{m-1}^{(s,i+1)}), \quad \forall i \geq 1. \quad [18.34]$$

10055 The original work on sequence-to-sequence translation used four layers; in 2016,  
 10056 Google's commercial machine translation system used eight layers (Wu et al., 2016).<sup>5</sup>

- 10057 • Significant improvements can be obtained by creating an **ensemble** of translation  
 10058 models, each trained from a different random initialization. For an ensemble of size  
 10059  $N$ , the per-token decoding probability is set equal to,

$$p(w^{(t)} | z, \mathbf{w}_{1:m-1}^{(t)}) = \frac{1}{N} \sum_{i=1}^N p_i(w^{(t)} | z, \mathbf{w}_{1:m-1}^{(t)}), \quad [18.35]$$

10060 where  $p_i$  is the decoding probability for model  $i$ . Each translation model in the  
 10061 ensemble includes its own encoder and decoder networks.

- 10062 • The original sequence-to-sequence model used a fairly standard training setup: stochastic  
 10063 gradient descent with an exponentially decreasing learning rate after the first five  
 10064 epochs; mini-batches of 128 sentences, chosen to have similar length so that each  
 10065 sentence on the batch will take roughly the same amount of time to process; gradient  
 10066 clipping (see § 3.3.4) to ensure that the norm of the gradient never exceeds some  
 10067 predefined value.

### 10068 18.3.1 Neural attention

10069 The sequence-to-sequence model discussed in the previous section was a radical departure  
 10070 from statistical machine translation, in which each word or phrase in the target lan-  
 10071 guage is conditioned on a single word or phrase in the source language. Both approaches  
 10072 have advantages. Statistical translation leverages the idea of compositionality — transla-  
 10073 tions of large units should be based on the translations of their component parts — and  
 10074 this seems crucial if we are to scale translation to longer units of text. But the translation  
 10075 of each word or phrase often depends on the larger context, and encoder-decoder models  
 10076 capture this context at the sentence level.

10077 Is it possible for translation to be both contextualized and compositional? One ap-  
 10078 proach is to augment neural translation with an **attention mechanism**. The idea of neural  
 10079 attention was described in § 17.5, but its application to translation bears further discus-  
 10080 sion. In general, attention can be thought of as using a query to select from a memory  
 10081 of key-value pairs. However, the query, keys, and values are all vectors, and the entire

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<sup>5</sup>Google reports that this system took six days to train for English-French translation, using 96 NVIDIA K80 GPUs, which would have cost roughly half a million dollars at the time.

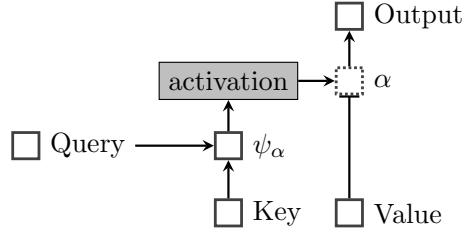


Figure 18.6: A general view of neural attention. The dotted box indicates that each  $\alpha_{m \rightarrow n}$  can be viewed as a **gate** on value  $n$ .

operation is differentiable. For each key  $n$  in the memory, we compute a score  $\psi_\alpha(m, n)$  with respect to the query  $m$ . That score is a function of the compatibility of the key and the query, and can be computed using a small feedforward neural network. The vector of scores is passed through an activation function, such as softmax. The output of this activation function is a vector of non-negative numbers  $[\alpha_{m \rightarrow 1}, \alpha_{m \rightarrow 2}, \dots, \alpha_{m \rightarrow N}]^\top$ , with length  $N$  equal to the size of the memory. Each value in the memory  $v_n$  is multiplied by the attention  $\alpha_{m \rightarrow n}$ ; the sum of these scaled values is the output. This process is shown in Figure 18.6. In the extreme case that  $\alpha_{m \rightarrow n} = 1$  and  $\alpha_{m \rightarrow n'} = 0$  for all other  $n'$ , then the attention mechanism simply selects the value  $v_n$  from the memory.

Neural attention makes it possible to integrate alignment into the encoder-decoder architecture. Rather than encoding the entire source sentence into a fixed length vector  $z$ , it can be encoded into a matrix  $Z \in \mathbb{R}^{K \times M^{(S)}}$ , where  $K$  is the dimension of the hidden state, and  $M^{(S)}$  is the number of tokens in the source input. Each column of  $Z$  represents the state of a recurrent neural network over the source sentence. These vectors are constructed from a **bidirectional LSTM** (see § 7.6), which can be a deep network as shown in Figure 18.5. These columns are both the keys and the values in the attention mechanism.

At each step  $m$  in decoding, the attentional state is computed by executing a query, which is equal to the state of the decoder,  $h_m^{(t)}$ . The resulting compatibility scores are,

$$\psi_\alpha(m, n) = v_\alpha \cdot \tanh(\Theta_\alpha[h_m^{(t)}; h_n^{(s)}]). \quad [18.36]$$

The function  $\psi$  is thus a two layer feedforward neural network, with weights  $v_\alpha$  on the output layer, and weights  $\Theta_\alpha$  on the input layer. To convert these scores into attention weights, we apply an activation function, which can be vector-wise softmax or an element-wise sigmoid:

### Softmax attention

$$\alpha_{m \rightarrow n} = \frac{\exp \psi_\alpha(m, n)}{\sum_{n'=1}^{M^{(s)}} \exp \psi_\alpha(m, n')} \quad [18.37]$$

### Sigmoid attention

$$\alpha_{m \rightarrow n} = \sigma(\psi_\alpha(m, n)) \quad [18.38]$$

The attention  $\alpha$  is then used to compute an **context vector**  $c_m$  by taking a weighted average over the columns of  $\mathbf{Z}$ ,

$$\mathbf{c}_m = \sum_{n=1}^{M^{(s)}} \alpha_{m \rightarrow n} \mathbf{z}_n, \quad [18.39]$$

where  $\alpha_{m \rightarrow n} \in [0, 1]$  is the amount of attention from word  $m$  of the target to word  $n$  of the source. The context vector can be incorporated into the decoder’s word output probability model, by adding another layer to the decoder (Luong et al., 2015):

$$\tilde{\mathbf{h}}_m^{(t)} = \tanh(\Theta_c[\mathbf{h}_m^{(t)}; \mathbf{c}_m]) \quad [18.40]$$

$$p(w_{m+1}^{(t)} | \mathbf{w}_{1:m}^{(t)}, \mathbf{w}^{(s)}) \propto \exp\left(\beta_{w_{m+1}^{(t)}} \cdot \tilde{\mathbf{h}}_m^{(t)}\right). \quad [18.41]$$

10102 Here the decoder state  $\mathbf{h}_m^{(t)}$  is concatenated with the context vector, forming the input  
 10103 to compute a final output vector  $\tilde{\mathbf{h}}_m^{(t)}$ . The context vector can be incorporated into the  
 10104 decoder recurrence in a similar manner (Bahdanau et al., 2014).

10105 **18.3.2 \*Neural machine translation without recurrence**

In the encoder-decoder model, attention’s “keys and values” are the hidden state representations in the encoder network,  $\mathbf{z}$ , and the “queries” are state representations in the decoder network  $\mathbf{h}^{(t)}$ . It is also possible to completely eliminate recurrence from neural translation, by applying **self-attention** (Lin et al., 2017; Kim et al., 2017) within the encoder and decoder, as in the **transformer architecture** (Vaswani et al., 2017). For level  $i$ , the basic equations of the encoder side of the transformer are:

$$\mathbf{z}_m^{(i)} = \sum_{n=1}^{M^{(s)}} \alpha_{m \rightarrow n}^{(i)} (\Theta_v \mathbf{h}_n^{(i-1)}) \quad [18.42]$$

$$\mathbf{h}_m^{(i)} = \Theta_2 \text{ReLU}\left(\Theta_1 \mathbf{z}_m^{(i)} + \mathbf{b}_1\right) + \mathbf{b}_2. \quad [18.43]$$

10106 For each token  $m$  at level  $i$ , we compute self-attention over the entire source sentence:  
 10107 the keys, values, and queries are all projections of the vector  $\mathbf{h}^{(i-1)}$ . The attention scores  
 10108  $\alpha_{m \rightarrow n}^{(i)}$  are computed using a scaled form of softmax attention,

$$\alpha_{m \rightarrow n} \propto \exp(\psi_\alpha(m, n)/M), \quad [18.44]$$

10109 where  $M$  is the length of the input. This encourages the attention to be more evenly  
 10110 dispersed across the input. Self-attention is applied across multiple “heads”, each using  
 10111 different projections of  $\mathbf{h}^{(i-1)}$  to form the keys, values, and queries.

The output of the self-attentional layer is the representation  $\mathbf{z}_m^{(i)}$ , which is then passed through a two-layer feed-forward network, yielding the input to the next layer,  $\mathbf{h}^{(i)}$ . To ensure that information about word order in the source is integrated into the model, the encoder includes **positional encodings** of the index of each word in the source. These encodings are vectors for each position  $m \in \{1, 2, \dots, M\}$ . The transformer sets these encodings equal to a set of sinusoidal functions of  $m$ ,

$$e_{2i-1}(m) = \sin(m/(10000^{\frac{2i}{K_e}})) \quad [18.45]$$

$$e_{2i}(m) = \cos(m/(10000^{\frac{2i}{K_e}})), \quad \forall i \in \{1, 2, \dots, K_e/2\} \quad [18.46]$$

10112 where  $e_{2i}(m)$  is the value at position  $2i$  of the encoding for position  $m$ . As we progress  
 10113 through the dimensions of the encoding, we encounter sinusoidal functions of progres-  
 10114 sively wider bandwidth. This enables the model to learn to attend by relative positions of  
 10115 words. The positional encodings are concatenated with the word embeddings  $\mathbf{x}_m$  at the  
 10116 base layer of the model.<sup>6</sup>

10117 Convolutional neural networks (see § 3.4) have also been applied as encoders in neu-  
 10118 ral machine translation. For each word  $w_m^{(s)}$ , a convolutional network computes a rep-  
 10119 resentation  $\mathbf{h}_m^{(s)}$  from the embeddings of the word and its neighbors. This procedure is  
 10120 applied several times, creating a deep convolutional network. The recurrent decoder then  
 10121 computes a set of attention weights over these convolutional representations, using the  
 10122 decoder’s hidden state  $\mathbf{h}^{(t)}$  as the queries. This attention vector is used to compute a  
 10123 weighted average over the outputs of *another* convolutional neural network of the source,  
 10124 yielding an averaged representation  $\mathbf{c}_m$ , which is then fed into the decoder. As with the  
 10125 transformer, speed is the main advantage over recurrent encoding models; another sim-  
 10126 ilarity is that word order information is approximated through the use of positional en-  
 10127 codings.<sup>7</sup>

### 10128 18.3.3 Out-of-vocabulary words

10129 Thus far, we have treated translation as a problem at the level of words or phrases. For  
 10130 words that do not appear in the training data, all such models will struggle. There are  
 10131 two main reasons for the presence of out-of-vocabulary (OOV) words:

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<sup>6</sup>The transformer architecture relies on several additional tricks, including **layer normalization** (see § 3.3.4) and residual connections around the nonlinear activations (see § 3.2.2).

<sup>7</sup>A recent evaluation found that best performance was obtained by using a recurrent network for the decoder, and a transformer for the encoder (Chen et al., 2018). The transformer was also found to significantly outperform a convolutional neural network.

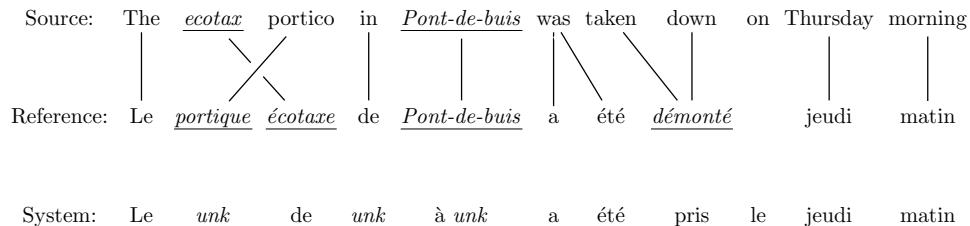


Figure 18.7: Translation with *unknown words*. The system outputs *unk* to indicate words that are outside its vocabulary. Figure adapted from Luong et al. (2015).

- New proper nouns, such as family names or organizations, are constantly arising — particularly in the news domain. The same is true, to a lesser extent, for technical terminology. This issue is shown in Figure 18.7.
- In many languages, words have complex internal structure, known as **morphology**. An example is German, which uses compounding to form nouns like *Abwasserbehandlungsanlage* (*sewage water treatment plant*; example from Sennrich et al. (2016)). While compounds could in principle be addressed by better tokenization (see § 8.4), other morphological processes involve more complex transformations of subword units.

Names and technical terms can be handled in a postprocessing step: after first identifying alignments between unknown words in the source and target, we can look up each aligned source word in a dictionary, and choose a replacement (Luong et al., 2015). If the word does not appear in the dictionary, it is likely to be a proper noun, and can be copied directly from the source to the target. This approach can also be integrated directly into the translation model, rather than applying it as a postprocessing step (Jean et al., 2015).

Words with complex internal structure can be handled by translating subword units rather than entire words. A popular technique for identifying subword units is **byte-pair encoding** (BPE; Gage, 1994; Sennrich et al., 2016). The initial vocabulary is defined as the set of characters used in the text. The most common character bigram is then merged into a new symbol, the vocabulary is updated, and the merging operation is applied again. For example, given the dictionary *{fish, fished, want, wanted, bike, biked}*, we would first form the subword unit *ed*, since this character bigram appears in three of the six words. Next, there are several bigrams that each appear in a pair of words: *fi, is, sh, wa, an*, etc. These can be merged in any order. By iterating this process, we eventually reach the segmentation, *{fish, fish+ed, want, want+ed, bik+e, bik+ed}*. At this point, there are no bigrams that appear more than once. In real data, merging is performed until the number of subword units reaches some predefined threshold, such as  $10^4$ .

10159     Each subword unit is treated as a token for translation, in both the encoder (source  
 10160    side) and decoder (target side). BPE can be applied jointly to the union of the source and  
 10161    target vocabularies, identifying subword units that appear in both languages. For lan-  
 10162    guages that have different scripts, such as English and Russian, **transliteration** between  
 10163    the scripts should be applied first.<sup>8</sup>

10164 **18.4 Decoding**

Given a trained translation model, the decoding task is:

$$\hat{\mathbf{w}}^{(t)} = \underset{\mathbf{w} \in \mathcal{V}^*}{\operatorname{argmax}} \Psi(\mathbf{w}, \mathbf{w}^{(s)}), \quad [18.47]$$

10165 where  $\mathbf{w}^{(t)}$  is a sequence of tokens from the target vocabulary  $\mathcal{V}$ . It is not possible to  
 10166 efficiently obtain exact solutions to the decoding problem, for even minimally effective  
 10167 models in either statistical or neural machine translation. Today's state-of-the-art transla-  
 10168 tion systems use **beam search** (see § 11.3.1.4), which is an incremental decoding algorithm  
 10169 that maintains a small constant number of competitive hypotheses. Such greedy approxi-  
 10170 mations are reasonably effective in practice, and this may be in part because the decoding  
 10171 objective is only loosely correlated with measures of translation quality, so that exact op-  
 10172 timization of [18.47] may not greatly improve the resulting translations.

Decoding in neural machine translation is simpler than in phrase-based statistical ma-  
 chine translation.<sup>9</sup> The scoring function  $\Psi$  is defined,

$$\Psi(\mathbf{w}^{(t)}, \mathbf{w}^{(s)}) = \sum_{m=1}^{M^{(t)}} \psi(w_m^{(t)}; \mathbf{w}_{1:m-1}^{(t)}, \mathbf{z}) \quad [18.48]$$

$$\psi(w^{(t)}; \mathbf{w}_{1:m-1}^{(t)}, \mathbf{z}) = \beta_{w_m^{(t)}} \cdot \mathbf{h}_m^{(t)} - \log \sum_{w \in \mathcal{V}} \exp(\beta_w \cdot \mathbf{h}_m^{(t)}), \quad [18.49]$$

10173 where  $\mathbf{z}$  is the encoding of the source sentence  $\mathbf{w}^{(s)}$ , and  $\mathbf{h}_m^{(t)}$  is a function of the encoding  
 10174  $\mathbf{z}$  and the decoding history  $\mathbf{w}_{1:m-1}^{(t)}$ . This formulation subsumes the attentional translation  
 10175 model, where  $\mathbf{z}$  is a matrix encoding of the source.

Now consider the incremental decoding algorithm,

$$\hat{w}_m^{(t)} = \underset{w \in \mathcal{V}}{\operatorname{argmax}} \psi(w; \hat{\mathbf{w}}_{1:m-1}^{(t)}, \mathbf{z}), \quad m = 1, 2, \dots \quad [18.50]$$

---

<sup>8</sup>Transliteration is crucial for converting names and other foreign words between languages that do not share a single script, such as English and Japanese. It is typically approached using the finite-state methods discussed in chapter 9 (Knight and Graehl, 1998).

<sup>9</sup>For more on decoding in phrase-based statistical models, see Koehn (2009).

10176 This algorithm selects the best target language word at position  $m$ , assuming that it has  
 10177 already generated the sequence  $\hat{w}_{1:m-1}^{(t)}$ . (Termination can be handled by augmenting  
 10178 the vocabulary  $\mathcal{V}$  with a special end-of-sequence token, ■.) The incremental algorithm  
 10179 is likely to produce a suboptimal solution to the optimization problem defined in Equa-  
 10180 tion 18.47, because selecting the highest-scoring word at position  $m$  can set the decoder  
 10181 on a “garden path,” in which there are no good choices at some later position  $n > m$ . We  
 10182 might hope for some dynamic programming solution, as in sequence labeling (§ 7.3). But  
 10183 the Viterbi algorithm and its relatives rely on a Markov decomposition of the objective  
 10184 function into a sum of local scores: for example, scores can consider locally adjacent tags  
 10185 ( $y_m, y_{m-1}$ ), but not the entire tagging history  $y_{1:m}$ . This decomposition is not applicable  
 10186 to recurrent neural networks, because the hidden state  $h_m^{(t)}$  is impacted by the entire his-  
 10187 tory  $w_{1:m}^{(t)}$ ; this sensitivity to long-range context is precisely what makes recurrent neural  
 10188 networks so effective.<sup>10</sup> In fact, it can be shown that decoding from any recurrent neural  
 10189 network is NP-complete (Siegelmann and Sontag, 1995; Chen et al., 2018).

10190 **Beam search** Beam search is a general technique for avoiding search errors when ex-  
 10191 haustive search is impossible; it was first discussed in § 11.3.1.4. Beam search can be  
 10192 seen as a variant of the incremental decoding algorithm sketched in Equation 18.50, but  
 10193 at each step  $m$ , a set of  $K$  different hypotheses are kept on the beam. For each hypothesis  
 10194  $k \in \{1, 2, \dots, K\}$ , we compute both the current score  $\sum_{m=1}^{M^{(t)}} \psi(w_{k,m}^{(t)}; w_{k,1:m-1}^{(t)}, z)$  as well as  
 10195 the current hidden state  $h_k^{(t)}$ . At each step in the beam search, the  $K$  top-scoring children  
 10196 of each hypothesis currently on the beam are “expanded”, and the beam is updated. For  
 10197 a detailed description of beam search for RNN decoding, see Graves (2012).

10198 **Learning and search** Conventionally, the learning algorithm is trained to predict the  
 10199 right token in the translation, conditioned on the translation history being correct. But  
 10200 if decoding must be approximate, then we might do better by modifying the learning  
 10201 algorithm to be robust to errors in the translation history. **Scheduled sampling** does this  
 10202 by training on histories that sometimes come from the ground truth, and sometimes come  
 10203 from the model’s own output (Bengio et al., 2015).<sup>11</sup> As training proceeds, the training  
 10204 wheels come off: we increase the fraction of tokens that come from the model rather than  
 10205 the ground truth. Another approach is to train on an objective that relates directly to beam  
 10206 search performance (Wiseman et al., 2016). **Reinforcement learning** has also been applied  
 10207 to decoding of RNN-based translation models, making it possible to directly optimize  
 10208 translation metrics such as BLEU (Ranzato et al., 2016).

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<sup>10</sup>Note that this problem does not impact RNN-based sequence labeling models (see § 7.6). This is because the tags produced by these models do not affect the recurrent state.

<sup>11</sup>Scheduled sampling builds on earlier work on learning to search (Daumé III et al., 2009; Ross et al., 2011), which are also described in § 15.2.4.

## 10209 18.5 Training towards the evaluation metric

10210 In likelihood-based training, the objective is to maximize the probability of a parallel  
 10211 corpus. However, translations are not evaluated in terms of likelihood: metrics like BLEU  
 10212 consider only the correctness of a single output translation, and not the range of prob-  
 10213 abilities that the model assigns. It might therefore be better to train translation models  
 10214 to achieve the highest BLEU score possible — to the extent that we believe BLEU mea-  
 10215 sures translation quality. Unfortunately, BLEU and related metrics are not friendly for  
 10216 optimization: they are discontinuous, non-differentiable functions of the parameters of  
 10217 the translation model.

Consider an error function  $\Delta(\hat{\mathbf{w}}^{(t)}, \mathbf{w}^{(t)})$ , which measures the discrepancy between the system translation  $\hat{\mathbf{w}}^{(t)}$  and the reference translation  $\mathbf{w}^{(t)}$ ; this function could be based on BLEU or any other metric on translation quality. One possible criterion would be to select the parameters  $\theta$  that minimize the error of the system's preferred translation,

$$\hat{\mathbf{w}}^{(t)} = \operatorname{argmax}_{\mathbf{w}^{(t)}} \Psi(\mathbf{w}^{(t)}, \mathbf{w}^{(s)}; \theta) \quad [18.51]$$

$$\hat{\theta} = \operatorname{argmin}_{\theta} \Delta(\hat{\mathbf{w}}^{(t)}, \mathbf{w}^{(s)}) \quad [18.52]$$

10218 However, identifying the top-scoring translation  $\hat{\mathbf{w}}^{(t)}$  is usually intractable, as described  
 10219 in the previous section. In **minimum error-rate training (MERT)**,  $\hat{\mathbf{w}}^{(t)}$  is selected from a  
 10220 set of candidate translations  $\mathcal{Y}(\mathbf{w}^{(s)})$ ; this is typically a strict subset of all possible transla-  
 10221 tions, so that it is only possible to optimize an approximation to the true error rate (Och  
 10222 and Ney, 2003).

A further issue is that the objective function in Equation 18.52 is discontinuous and non-differentiable, due to the argmax over translations: an infinitesimal change in the parameters  $\theta$  could cause another translation to be selected, with a completely different error. To address this issue, we can instead minimize the **risk**, which is defined as the expected error rate,

$$R(\theta) = E_{\hat{\mathbf{w}}^{(t)} | \mathbf{w}^{(s)}; \theta} [\Delta(\hat{\mathbf{w}}^{(t)}, \mathbf{w}^{(t)})] \quad [18.53]$$

$$= \sum_{\hat{\mathbf{w}}^{(t)} \in \mathcal{Y}(\mathbf{w}^{(s)})} p(\hat{\mathbf{w}}^{(t)} | \mathbf{w}^{(s)}) \times \Delta(\hat{\mathbf{w}}^{(t)}, \mathbf{w}^{(t)}). \quad [18.54]$$

10223 **Minimum risk training** minimizes the sum of  $R(\theta)$  across all instances in the training set.

The risk can be generalized by exponentiating the translation probabilities,

$$\tilde{p}(\mathbf{w}^{(t)}; \theta, \alpha) \propto \left( p(\mathbf{w}^{(t)} | \mathbf{w}^{(s)}; \theta) \right)^\alpha \quad [18.55]$$

$$\tilde{R}(\theta) = \sum_{\hat{\mathbf{w}}^{(t)} \in \mathcal{Y}(\mathbf{w}^{(s)})} \tilde{p}(\hat{\mathbf{w}}^{(t)} | \mathbf{w}^{(s)}; \alpha, \theta) \times \Delta(\hat{\mathbf{w}}^{(t)}, \mathbf{w}^{(t)}) \quad [18.56]$$

10224 where  $\mathcal{Y}(\mathbf{w}^{(s)})$  is now the set of *all* possible translations for  $\mathbf{w}^{(s)}$ . Exponentiating the prob-  
 10225 abilities in this way is known as **annealing** (Smith and Eisner, 2006). When  $\alpha = 1$ , then  
 10226  $\tilde{R}(\boldsymbol{\theta}) = R(\boldsymbol{\theta})$ ; when  $\alpha = \infty$ , then  $\tilde{R}(\boldsymbol{\theta})$  is equivalent to the sum of the errors of the maxi-  
 10227 mum probability translations for each sentence in the dataset.

Clearly the set of candidate translations  $\mathcal{Y}(\mathbf{w}^{(s)})$  is too large to explicitly sum over. Because the error function  $\Delta$  generally does not decompose into smaller parts, there is no efficient dynamic programming solution to sum over this set. We can approximate the sum  $\sum_{\mathbf{w}^{(t)} \in \mathcal{Y}(\mathbf{w}^{(s)})}$  with a sum over a finite number of samples,  $\{\mathbf{w}_1^{(t)}, \mathbf{w}_2^{(t)}, \dots, \mathbf{w}_K^{(t)}\}$ . If these samples were drawn uniformly at random, then the (annealed) risk would be approximated as (Shen et al., 2016),

$$\tilde{R}(\boldsymbol{\theta}) \approx \frac{1}{Z} \sum_{k=1}^K \tilde{p}(\mathbf{w}_k^{(t)} | \mathbf{w}^{(s)}; \boldsymbol{\theta}, \alpha) \times \Delta(\mathbf{w}_k^{(t)}, \mathbf{w}^{(t)}) \quad [18.57]$$

$$Z = \sum_{k=1}^K \tilde{p}(\mathbf{w}_k^{(t)} | \mathbf{w}^{(s)}; \boldsymbol{\theta}, \alpha). \quad [18.58]$$

10228 Shen et al. (2016) report that performance plateaus at  $K = 100$  for minimum risk training  
 10229 of neural machine translation.

Uniform sampling over the set of all possible translations is undesirable, because most translations have very low probability. A solution from Monte Carlo estimation is **importance sampling**, in which we draw samples from a **proposal distribution**  $q(\mathbf{w}^{(s)})$ . This distribution can be set equal to the current translation model  $p(\mathbf{w}^{(t)} | \mathbf{w}^{(s)}; \boldsymbol{\theta})$ . Each sample is then weighted by an **importance score**,  $\omega_k = \frac{\tilde{p}(\mathbf{w}_k^{(t)} | \mathbf{w}^{(s)})}{q(\mathbf{w}_k^{(t)}; \mathbf{w}^{(s)})}$ . The effect of this weighting is to correct for any mismatch between the proposal distribution  $q$  and the true distribution  $\tilde{p}$ . The risk can then be approximated as,

$$\mathbf{w}_k^{(t)} \sim q(\mathbf{w}^{(s)}) \quad [18.59]$$

$$\omega_k = \frac{\tilde{p}(\mathbf{w}_k^{(t)} | \mathbf{w}^{(s)})}{q(\mathbf{w}_k^{(t)}; \mathbf{w}^{(s)})} \quad [18.60]$$

$$\tilde{R}(\boldsymbol{\theta}) \approx \frac{1}{\sum_{k=1}^K \omega_k} \sum_{k=1}^K \omega_k \times \Delta(\mathbf{w}_k^{(t)}, \mathbf{w}^{(t)}). \quad [18.61]$$

10230 Importance sampling will generally give a more accurate approximation than uniform  
 10231 sampling. The only formal requirement is that the proposal assigns non-zero probability  
 10232 to every  $\mathbf{w}^{(t)} \in \mathcal{Y}(\mathbf{w}^{(s)})$ . For more on importance sampling and related methods, see  
 10233 Robert and Casella (2013).

**10234 Additional resources**

10235 A complete textbook on machine translation is available from Koehn (2009). While this  
10236 book precedes recent work on neural translation, a more recent draft chapter on neural  
10237 translation models is also available (Koehn, 2017). Neubig (2017) provides a comprehen-  
10238 sive tutorial on neural machine translation, starting from first principles. The course notes  
10239 from Cho (2015) are also useful. Several neural machine translation systems are avail-  
10240 able: `lamt ram` is an implementation of neural machine translation in the `dynet` (Neubig  
10241 et al., 2017); `OpenNMT` (Klein et al., 2017) and `FairSeq` are an implementation primar-  
10242 ily in `Torch`; `tensor2tensor` is an implementation of several of the Google translation  
10243 models in `tensorflow` (Abadi et al., 2016).

10244 Literary translation is especially challenging, even for expert human translators. Mes-  
10245 sud (2014) describes some of these issues in her review of an English translation of *L'étranger*,  
10246 the 1942 French novel by Albert Camus.<sup>12</sup> She compares the new translation by Sandra  
10247 Smith against earlier translations by Stuart Gilbert and Matthew Ward, focusing on the  
10248 difficulties presented by a single word in the first sentence:

10249 Then, too, Smith has reconsidered the book's famous opening. Camus's  
10250 original is deceptively simple: "*Aujourd'hui, maman est morte.*" Gilbert influ-  
10251 enced generations by offering us "Mother died today"—inscribing in Meur-  
10252 sault [the narrator] from the outset a formality that could be construed as  
10253 heartlessness. But *maman*, after all, is intimate and affectionate, a child's name  
10254 for his mother. Matthew Ward concluded that it was essentially untranslatable  
10255 ("mom" or "mummy" being not quite apt), and left it in the original French:  
10256 "Maman died today." There is a clear logic in this choice; but as Smith has  
10257 explained, in an interview in *The Guardian*, *maman* "didn't really tell the reader  
10258 anything about the connotation." She, instead, has translated the sentence as  
10259 "My mother died today."

10260 I chose "My mother" because I thought about how someone would  
10261 tell another person that his mother had died. Meursault is speaking  
10262 to the reader directly. "My mother died today" seemed to me the  
10263 way it would work, and also implied the closeness of "maman" you  
10264 get in the French.

10265 Elsewhere in the book, she has translated *maman* as "mama"—again, striving  
10266 to come as close as possible to an actual, colloquial word that will carry the  
10267 same connotations as *maman* does in French.

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<sup>12</sup>The book review is currently available online at <http://www.nybooks.com/articles/2014/06/05/camus-new-letranger/>.

10268     The passage is a useful reminder that while the quality of machine translation has  
 10269     improved dramatically in recent years, expert human translations draw on considerations  
 10270     that are beyond the ken of any known computational approach.

10271   **Exercises**

10272   1. Using Google translate or another online service, translate the following example  
 10273     into two different languages of your choice:

10274       (18.4) It is not down on any map; true places never are.

10275       Then translate each result back into English. Which is closer to the original? Can  
 10276     you explain the differences?

10277   2. Compute the unsmoothed  $n$ -gram precisions  $p_1 \dots p_4$  for the two back-translations  
 10278     in the previous problem. Your  $n$ -gramsshould include punctuation, and should seg-  
 10279     ment conjunctions like *it's* into two tokens.

10280   3. You are given the following dataset of translations from “simple” to “difficult” En-  
 10281     glish:

10282       (18.5) a. *Kids like cats.*  
                   Children adore felines.

10283       b. *Cats hats.*  
                   Felines fedoras.

10284       Estimate a word-to-word statistical translation model from simple English (source)  
 10285     to difficult English (target), using the expectation-maximization as described in § 18.2.2.  
 10286       Compute two iterations of the algorithm by hand, starting from a uniform transla-  
 10287       tion model, and using the simple alignment model  $p(a_m \mid m, M^{(s)}, M^{(t)}) = \frac{1}{M^{(t)}}$ .  
 10288       Hint: in the final M-step, you will want to switch from fractions to decimals.

10289   4. Building on the previous problem, what will be the converged translation proba-  
 10290     bility table? Can you state a general condition about the data, under which this  
 10291     translation model will fail in the way that it fails here?

10292   5. Propose a simple alignment model that would make it possible to recover the correct  
 10293     translation probabilities from the toy dataset in the previous two problems.

10294   6. Give a synchronized derivation (§ 18.2.4) for the Spanish-English translation,

- 10295 (18.6) *El pez enojado atacado.*  
 The fish angry attacked.  
 10296 The angry fish attacked.

10297 As above, the second line shows a word-for-word gloss, and the third line shows  
 10298 the desired translation. Use the synchronized production rule in [18.22], and design  
 10299 the other production rules necessary to derive this sentence pair. You may derive  
 10300 (*atacado*, *attacked*) directly from VP.

- 10301 7. Let  $\ell_{m+1}^{(t)}$  represent the loss at word  $m+1$  of the target, and let  $\mathbf{h}_n^{(s)}$  represent the hid-  
 10302 den state at word  $n$  of the source. Write the expression for the derivative  $\frac{\partial \ell_{m+1}^{(t)}}{\partial \mathbf{h}_n^{(s)}}$  in the  
 10303 sequence-to-sequence translation model expressed in Equations [18.29-18.32]. You  
 10304 may assume that both the encoder and decoder are one-layer LSTMs. In general,  
 10305 how many terms are on the shortest path from  $\ell_{m+1}^{(t)}$  to  $\mathbf{h}_n^{(s)}$ ?
- 10306 8. Now consider the neural attentional model from § 18.3.1, with sigmoid attention.  
 10307 The derivative  $\frac{\partial \ell_{m+1}^{(t)}}{\partial \mathbf{z}_n}$  is the sum of many paths through the computation graph;  
 10308 identify the shortest such path. You may assume that the initial state of the decoder  
 10309 recurrence  $\mathbf{h}_0^{(t)}$  is *not* tied to the final state of the encoder recurrence  $\mathbf{h}_{M^{(s)}}$ .
- 10310 9. Apply byte-pair encoding for the vocabulary *it*, *unit*, *unite*, until no bigram appears  
 10311 more than once.
- 10312 10. Hand-design an attentional recurrent translation model that simply copies the input  
 10313 from the source to the target. You may assume an arbitrarily large hidden state, and  
 10314 you may assume that there is a finite maximum input length  $M$ . Specify all the  
 10315 weights such that the maximum probability translation of any source is the source  
 10316 itself. Hint: it is simplest to use a simple Elman-recurrence  $\mathbf{h}_m = f(\Theta \mathbf{h}_{m-1} + \mathbf{x}_m)$   
 10317 rather than an LSTM.
- 10318 11. This problem relates to the complexity of machine translation. Suppose you have  
 10319 an oracle that returns the list of words to include in the translation, so that your  
 10320 only task is to order the words. Furthermore, suppose that the scoring function  
 10321 over orderings is a sum over bigrams,  $\sum_{m=1}^M \psi(\mathbf{w}_m^{(t)}, \mathbf{w}_{m-1}^{(t)})$ . Show that the problem  
 10322 of finding the optimal translation is NP-complete, by reduction from a well-known  
 10323 problem.



10324

# Chapter 19

10325

## Text generation

10326 In many of the most interesting problems in natural language processing, language is  
10327 the output. The previous chapter described the specific case of machine translation, but  
10328 there are many other applications, from summarization of research articles, to automated  
10329 journalism, to dialogue systems. This chapter emphasizes three main scenarios: data-to-  
10330 text, in which text is generated to explain or describe a structured record or unstructured  
10331 perceptual input; text-to-text, which typically involves fusing information from multiple  
10332 linguistic sources into a single coherent summary; and dialogue, in which text is generated  
10333 as part of an interactive conversation with one or more human participants.

10334

### 19.1 Data-to-text generation

10335 In data-to-text generation, the input ranges from structured records, such as the descrip-  
10336 tion of an weather forecast (as shown in Figure 19.1), to unstructured perceptual data,  
10337 such as a raw image or video; the output may be a single sentence, such as an image cap-  
10338 tion, or a multi-paragraph argument. Despite this diversity of conditions, all data-to-text  
10339 systems share some of the same challenges (Reiter and Dale, 2000):

- 10340 • determining what parts of the data to describe;
- 10341 • planning a presentation of this information;
- 10342 • **lexicalizing** the data into words and phrases;
- 10343 • organizing words and phrases into well-formed sentences and paragraphs.

10344 The earlier stages of this process are sometimes called **content selection** and **text plan-**  
10345 **ning**; the later stages are often called **surface realization**.

10346 Early systems for data-to-text generation were modular, with separate software com-  
10347 ponents for each task. Artificial intelligence **planning** algorithms can be applied to both

<b>Temperature</b>				<b>Cloud sky cover</b>	
<i>time</i>	<i>min</i>	<i>mean</i>	<i>max</i>	<i>time</i>	<i>percent (%)</i>
06:00-21:00	9	15	21	06:00-09:00	25-50
<b>Wind speed</b>				<b>Wind direction</b>	
<i>time</i>	<i>min</i>	<i>mean</i>	<i>max</i>	<i>time</i>	<i>mode</i>
06:00-21:00	15	20	30	06:00-21:00	S

*Cloudy, with temperatures between 10 and 20 degrees. South wind around 20 mph.*

Figure 19.1: An example input-output pair for the task of generating text descriptions of weather forecasts (adapted from Konstas and Lapata, 2013).

10348 the high-level information structure and the organization of individual sentences, ensur-  
 10349 ing that communicative goals are met (McKeown, 1992; Moore and Paris, 1993). Surface  
 10350 realization can be performed by grammars or templates, which link specific types of data  
 10351 to candidate words and phrases. A simple example template is offered by Wiseman et al.  
 10352 (2017), for generating descriptions of basketball games:

10353 (19.1) The <team1>(<wins1>-<losses1>) defeated the <team2>(<wins2>-<losses2>),  
 10354 <pts1>-<pts2>.   
 10355 The New York Knicks (45-5) defeated the Boston Celtics (11-38), 115-79.

10356 For more complex cases, it may be necessary to apply morphological inflections such as  
 10357 pluralization and tense marking — even in the simple example above, languages such  
 10358 as Russian would require case marking suffixes for the team names. Such inflections can  
 10359 be applied as a postprocessing step. Another difficult challenge for surface realization is  
 10360 the generation of varied **referring expressions** (e.g., *The Knicks, New York, they*), which is  
 10361 critical to avoid repetition. As discussed in § 16.2.1, the form of referring expressions is  
 10362 constrained by the discourse and information structure.

10363 An example at the intersection of rule-based and statistical techniques is the Nitrogen  
 10364 system (Langkilde and Knight, 1998). The input to Nitrogen is an abstract meaning rep-  
 10365 resentation (AMR; see § 13.3) of semantic content to be expressed in a single sentence. In  
 10366 data-to-text scenarios, the abstract meaning representation is the output of a higher-level  
 10367 text planning stage. A set of rules then converts the abstract meaning representation into  
 10368 various sentence plans, which may differ in both the high-level structure (e.g., active ver-  
 10369 sus passive voice) as well as the low-level details (e.g., word and phrase choice). Some  
 10370 examples are shown in Figure 19.2. To control the combinatorial explosion in the number  
 10371 of possible realizations for any given meaning, the sentence plans are unified into a single  
 10372 finite-state acceptor, in which word tokens are represented by arcs (see § 9.1.1). A bigram

```
(a / admire-01
 :ARG0 (v / visitor
       :ARG1-of (c / arrive-01
                  :ARG4 (j / Japan)))
       :ARG1 (m / "Mount Fuji"))
```

- Visitors who came to Japan admire Mount Fuji.
- Visitors who came in Japan admire Mount Fuji.
- Mount Fuji is admired by the visitor who came in Japan.

Figure 19.2: Abstract meaning representation and candidate surface realizations from the Nitrogen system. Example adapted from Langkilde and Knight (1998).

language model is then used to compute weights on the arcs, so that the shortest path is also the surface realization with the highest bigram language model probability.

More recent systems are unified models that are trained end-to-end using backpropagation. Data-to-text generation shares many properties with machine translation, including a problem of **alignment**: labeled examples provide the data and the text, but they do not specify which parts of the text correspond to which parts of the data. For example, to learn from Figure 19.1, the system must align the word *cloudy* to records in CLOUD SKY COVER, the phrases *10* and *20 degrees* to the MIN and MAX fields in TEMPERATURE, and so on. As in machine translation, both latent variables and neural attention have been proposed as solutions.

### 19.1.1 Latent data-to-text alignment

Given a dataset of texts and associated records  $\{(\mathbf{w}^{(i)}, \mathbf{y}^{(i)})\}_{i=1}^N$ , our goal is to learn a model  $\Psi$ , so that

$$\hat{\mathbf{w}} = \underset{\mathbf{w} \in \mathcal{V}^*}{\operatorname{argmax}} \Psi(\mathbf{w}, \mathbf{y}; \theta), \quad [19.1]$$

where  $\mathcal{V}^*$  is the set of strings over a discrete vocabulary, and  $\theta$  is a vector of parameters. The relationship between  $\mathbf{w}$  and  $\mathbf{y}$  is complex: the data  $\mathbf{y}$  may contain dozens of records, and  $\mathbf{w}$  may extend to several sentences. To facilitate learning and inference, it would be helpful to decompose the scoring function  $\Psi$  into subcomponents. This would be possible if given an **alignment**, specifying which element of  $\mathbf{y}$  is expressed in each part of  $\mathbf{w}$ . Specifically, let  $z_m$  indicates the record aligned to word  $m$ . For example, in Figure 19.1,  $z_1$  might specify that the word *cloudy* is aligned to the record *cloud-sky-cover:percent*. The score for this alignment would then be given by the weight on features such as

$$(\textit{cloudy}, \textit{cloud-sky-cover:percent}). \quad [19.2]$$

In general, given an observed set of alignments, the score for a generation can be

10395 written as sum of local scores (Angeli et al., 2010):

$$\Psi(\mathbf{w}, \mathbf{y}; \theta) = \sum_{m=1}^M \psi_{w,y}(\mathbf{w}_m, \mathbf{y}_{z_m}) + \psi_w(w_m, w_{m-1}) + \psi_z(z_m, z_{m-1}), \quad [19.3]$$

10396 where  $\psi_w$  can represent a bigram language model, and  $\psi_z$  can be tuned to reward coherence,  
 10397 such as the use of related records in nearby words.<sup>1</sup> The parameters of this model  
 10398 could be learned from labeled data  $\{(\mathbf{w}^{(i)}, \mathbf{y}^{(i)}, \mathbf{z}^{(i)})\}_{i=1}^N$ . However, while several datasets  
 10399 include structured records and natural language text (Barzilay and McKeown, 2005; Chen  
 10400 and Mooney, 2008; Liang and Klein, 2009), the alignments between text and records are  
 10401 usually not available.<sup>2</sup> One solution is to model the problem probabilistically, treating the  
 10402 alignment as a latent variable (Liang et al., 2009; Konstas and Lapata, 2013). The model  
 10403 can then be estimated using expectation maximization or sampling (see chapter 5).

### 10404 19.1.2 Neural data-to-text generation

10405 The **encoder-decoder model** and **neural attention** were introduced in § 18.3 as methods  
 10406 for neural machine translation. They can also be applied to data-to-text generation, with  
 10407 the data acting as the source language (Mei et al., 2016). In neural machine translation,  
 10408 the attention mechanism linked words in the source to words in the target; in data-to-  
 10409 text generation, the attention mechanism can link each part of the generated text back  
 10410 to a record in the data. The biggest departure from translation is in the encoder, which  
 10411 depends on the form of the data.

#### 10412 19.1.2.1 Data encoders

10413 In some types of structured records, all values are drawn from discrete sets. For example,  
 10414 the birthplace of an individual is drawn from a discrete set of possible locations; the diag-  
 10415 nosis and treatment of a patient are drawn from an exhaustive list of clinical codes (John-  
 10416 son et al., 2016). In such cases, vector embeddings can be estimated for each field and  
 10417 possible value: for example, a vector embedding for the field BIRTHPLACE, and another  
 10418 embedding for the value BERKELEY\_CALIFORNIA (Bordes et al., 2011). The table of such  
 10419 embeddings serves as the encoding of a structured record (He et al., 2017). It is also possi-  
 10420 ble to compress the entire table into a single vector representation, by **pooling** across the  
 10421 embeddings of each field and value (Lebret et al., 2016).

---

<sup>1</sup>More expressive decompositions of  $\Psi$  are possible. For example, Wong and Mooney (2007) use a synchronous context-free grammar (see § 18.2.4) to “translate” between a meaning representation and natural language text.

<sup>2</sup>An exception is a dataset of records and summaries from American football games, containing annotations of alignments between sentences and records (Snyder and Barzilay, 2007).

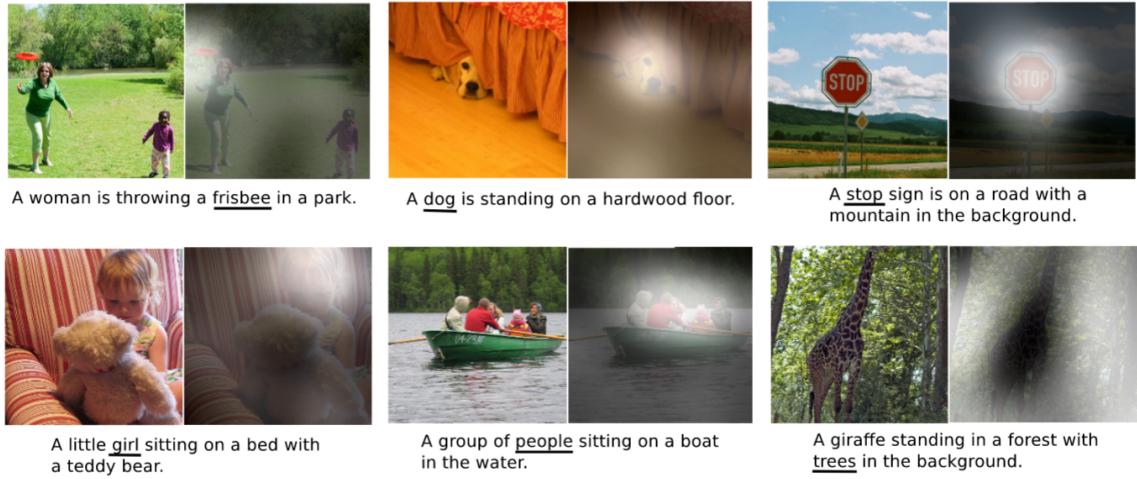


Figure 19.3: Examples of the image captioning task, with attention masks shown for each of the underlined words. From Xu et al. (2015). [todo: permission]

**Sequences** Some types of structured records have a natural ordering, such as events in a game (Chen and Mooney, 2008) and steps in a recipe (Tutin and Kittredge, 1992). For example, the following records describe a sequence of events in a robot soccer match (Mei et al., 2016):

```
PASS(arg1 = PURPLE6, arg2 = PURPLE3)
KICK(arg1 = PURPLE3)
BADPASS(arg1 = PURPLE3, arg2 = PINK9).
```

10422 Each event is a single record, and can be encoded by a concatenation of vector representations for the event type (e.g., PASS), the field (e.g., arg1), and the values (e.g., PURPLE3),  
10423 e.g.,  
10424

$$\mathbf{X} = [\mathbf{u}_{\text{PASS}}, \mathbf{u}_{\text{arg1}}, \mathbf{u}_{\text{PURPLE6}}, \mathbf{u}_{\text{arg2}}, \mathbf{u}_{\text{PURPLE3}}]. \quad [19.4]$$

10425 This encoding can then act as the input layer for a recurrent neural network, yielding a  
10426 sequence of vector representations  $\{\mathbf{z}_r\}_{r=1}^R$ , where  $r$  indexes over records. Interestingly,  
10427 this sequence-based approach can work even in cases where there is no natural ordering  
10428 over the records, such as the weather data in Figure 19.1 (Mei et al., 2016).

10429 **Images** Another flavor of data-to-text generation is the generation of text captions for  
10430 images. Examples from this task are shown in Figure 19.3. Images are naturally represented  
10431 as tensors: a color image of  $320 \times 240$  pixels would be stored as a tensor with  
10432  $320 \times 240 \times 3$  intensity values. The dominant approach to image classification is to encode  
10433 images as vectors using a combination of convolution and pooling (Krizhevsky et al.,

10434 2012). Chapter 3 explains how to use convolutional networks for text; for images, convolution  
 10435 is applied across the vertical, horizontal, and color dimensions. By pooling the re-  
 10436 sults of successive convolutions, the image is converted to a vector representation, which  
 10437 can then be fed directly into the decoder as the initial state (Vinyals et al., 2015), just as  
 10438 in the sequence-to-sequence translation model (see § 18.3). Alternatively, one can apply  
 10439 a set of convolutional networks, yielding vector representations for different parts of the  
 10440 image, which can then be combined using neural attention (Xu et al., 2015).

10441 **19.1.2.2 Attention**

Given a set of embeddings of the data  $\{z_r\}_{r=1}^R$  and a decoder state  $h_m$ , an attention vector over the data can be computed using the same techniques as in machine translation (see § 18.3.1). When generating word  $m$  of the output, attention is computed over the records,

$$\psi_\alpha(m, r) = \beta_\alpha \cdot f(\Theta_\alpha[h_m; z_r]) \quad [19.5]$$

$$\alpha_m = g([\psi_\alpha(m, 1), \psi_\alpha(m, 2), \dots, \psi_\alpha(m, R)]) \quad [19.6]$$

$$c_m = \sum_{r=1}^R \alpha_{m \rightarrow r} z_r, \quad [19.7]$$

10442 where  $f$  is an elementwise nonlinearity such as tanh or ReLU, and  $g$  is either softmax or  
 10443 elementwise sigmoid. The weighted sum  $c_m$  can then be included in the recurrent update  
 10444 to the decoder state, or in the emission probabilities, as described in § 18.3.1. Figure 19.4  
 10445 shows the attention to components of a weather record, while generating the text shown  
 10446 on the  $x$ -axis.

10447 Adapting this architecture to image captioning is straightforward. A convolutional  
 10448 neural networks is applied to a set of image locations, and the output at each location  $\ell$  is  
 10449 represented with a vector  $z_\ell$ . Attention can then be computed over the image locations,  
 10450 as shown in the right panels of each pair of images in Figure 19.3.

10451 Various modifications to this basic mechanism have been proposed. In **coarse-to-fine**  
 10452 **attention** (Mei et al., 2016), each record receives a global attention  $a_r \in [0, 1]$ , which is in-  
 10453 dependent of the decoder state. This global attention, which represents the overall impor-  
 10454 tance of the record, is multiplied with the decoder-based attention scores, before comput-  
 10455 ing the final normalized attentions. In **structured attention**, the attention vector  $\alpha_{m \rightarrow \cdot}$  can  
 10456 include structural biases, which can favor assigning higher attention values to contiguous  
 10457 segments or to dependency subtrees (Kim et al., 2017). Structured attention vectors can  
 10458 be computed by running the forward-backward algorithm to obtain marginal attention  
 10459 probabilities (see § 7.5.3.3). Because each step in the forward-backward algorithm is dif-  
 10460 ferentiable, it can be encoded in a computation graph, and end-to-end learning can be  
 10461 performed by backpropagation.

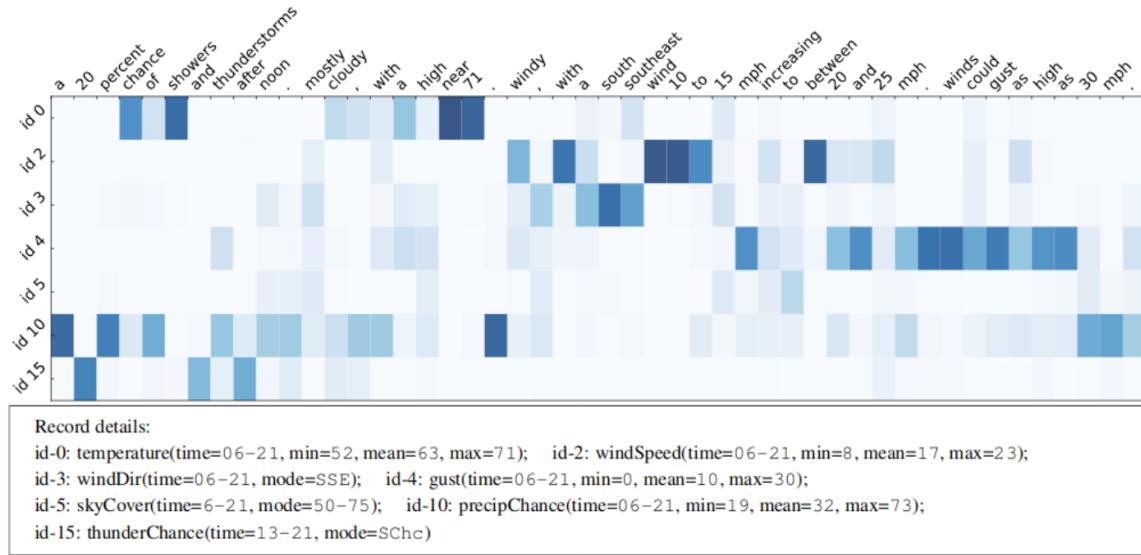


Figure 19.4: Neural attention in text generation. Figure from Mei et al. (2016).[todo: permission]

### 19.1.2.3 Decoder

Given the encoding, the decoder can function just as in neural machine translation (see § 18.3.1), using the attention-weighted encoder representation in the decoder recurrence and/or output computation. As in machine translation, beam search can help to avoid search errors (Lebret et al., 2016).

Many applications require generating words that do not appear in the training vocabulary. For example, a weather record may contain a previously unseen city name; a sports record may contain a previously unseen player name. Such tokens can be generated in the text by copying them over from the input (e.g., Gulcehre et al., 2016).<sup>3</sup> First introduce an additional variable  $s_m \in \{\text{gen}, \text{copy}\}$ , indicating whether token  $w_m^{(t)}$  should be generated or copied. The decoder probability is then,

$$p(w^{(t)} | w_{1:m-1}^{(t)}, \mathbf{Z}, s_m) = \begin{cases} \text{SoftMax}(\beta_{w^{(t)}} \cdot h_{m-1}^{(t)}), & s_m = \text{gen} \\ \sum_{r=1}^R \delta(w_r^{(s)} = w^{(t)}) \times \alpha_{m \rightarrow r}, & s_m = \text{copy}, \end{cases} \quad [19.8]$$

where  $\delta(w_r^{(s)} = w^{(t)})$  is an indicator function, taking the value 1 iff the text of the record  $w_r^{(s)}$  is identical to the target word  $w^{(t)}$ . The probability of copying record  $r$  from the source

<sup>3</sup>A number of variants of this strategy have been proposed (e.g., Gu et al., 2016; Merity et al., 2017). See Wiseman et al. (2017) for an overview.

10469 is  $\delta(s_m = \text{copy}) \times \alpha_{m \rightarrow r}$ , the product of the copy probability by the local attention. Note  
 10470 that in this model, the attention weights  $\alpha_m$  are computed from the *previous* decoder state  
 10471  $\mathbf{h}_{m-1}$ . The computation graph therefore remains a feedforward network, with recurrent  
 10472 paths such as  $\mathbf{h}_{m-1}^{(t)} \rightarrow \alpha_m \rightarrow w_m^{(t)} \rightarrow \mathbf{h}_m^{(t)}$ .

10473 To facilitate end-to-end training, the switching variable  $s_m$  can be represented by a  
 10474 gate  $\pi_m$ , which is computed from a two-layer feedforward network, whose input consists  
 10475 of the concatenation of the decoder state  $\mathbf{h}_{m-1}^{(t)}$  and the attention-weighted representation  
 10476 of the data,  $\mathbf{c}_m = \sum_{r=1}^R \alpha_{m \rightarrow r} \mathbf{z}_r$ ,

$$\pi_m = \sigma(\Theta^{(2)} f(\Theta^{(1)}[\mathbf{h}_{m-1}^{(t)}; \mathbf{c}_m])). \quad [19.9]$$

The full generative probability at token  $m$  is then,

$$p(w^{(t)} | \mathbf{w}_{1:m}^{(t)}, \mathbf{Z}) = \pi_m \times \underbrace{\frac{\exp \beta_{w^{(t)}} \cdot \mathbf{h}_{m-1}^{(t)}}{\sum_{j=1}^V \exp \beta_j \cdot \mathbf{h}_{m-1}^{(t)}}}_{\text{generate}} + (1 - \pi_m) \times \underbrace{\sum_{r=1}^R \delta(w_r^{(s)} = w^{(t)}) \times \alpha_{m \rightarrow r}}_{\text{copy}}. \quad [19.10]$$

## 10477 19.2 Text-to-text generation

10478 Text-to-text generation includes problems of summarization and simplification:

- 10479 • reading a novel and outputting a paragraph-long summary of the plot;<sup>4</sup>
- 10480 • reading a set of blog posts about politics, and outputting a bullet list of the various  
 10481 issues and perspectives;
- 10482 • reading a technical research article about the long-term health consequences of drink-  
 10483 ing kombucha, and outputting a summary of the article in language that non-experts  
 10484 can understand.

10485 These problems can be approached in two ways: through the encoder-decoder architec-  
 10486 ture discussed in the previous section, or by operating directly on the input text.

### 10487 19.2.1 Neural abstractive summarization

10488 **Sentence summarization** is the task of shortening a sentence while preserving its mean-  
 10489 ing, as in the following examples (Knight and Marcu, 2000; Rush et al., 2015):

---

<sup>4</sup>In § 16.3.4.1, we encountered a special case of single-document summarization, which involved extracting the most important sentences or discourse units. We now consider the more challenging problem of **abstractive summarization**, in which the summary can include words that do not appear in the original text.

- 10490 (19.2) The documentation is typical of Epson quality: excellent.  
 10491 Documentation is excellent.  
 10492
- 10493 (19.3) Russian defense minister Ivanov called sunday for the creation of a joint front for  
 10494 combating global terrorism.  
 10495 Russia calls for joint front against terrorism.  
 10496

10497 Sentence summarization is closely related to **sentence compression**, in which the sum-  
 10498 mary is produced by deleting words or phrases from the original (Clarke and Lapata,  
 10499 2008). But as shown in (19.3), a sentence summary can also introduce new words, such as  
 10500 *against*, which replaces the phrase *for combatting*.

10501 Sentence summarization can be treated as a machine translation problem, using the at-  
 10502 tentional encoder-decoder translation model discussed in § 18.3.1 (Rush et al., 2015). The  
 10503 longer sentence is encoded into a sequence of vectors, one for each token. The decoder  
 10504 then computes attention over these vectors when updating its own recurrent state. As  
 10505 with data-to-text generation, it can be useful to augment the encoder-decoder model with  
 10506 the ability to copy words directly from the source. Rush et al. (2015) train this model by  
 10507 building four million sentence pairs from news articles. In each pair, the longer sentence is  
 10508 the first sentence of the article, and the summary is the article headline. Sentence summa-  
 10509 rization can also be trained in a semi-supervised fashion, using a probabilistic formulation  
 10510 of the encoder-decoder model called a **variational autoencoder** (Miao and Blunsom, 2016,  
 10511 also see § 14.8.2).

When summarizing longer documents, an additional concern is that the summary not be repetitive: each part of the summary should cover new ground. This can be addressed by maintaining a vector of the sum total of all attention values thus far,  $t_m = \sum_{n=1}^m \alpha_n$ . This total can be used as an additional input to the computation of the attention weights,

$$\alpha_{m \rightarrow n} \propto \exp \left( \mathbf{v}_\alpha \cdot \tanh(\Theta_\alpha[\mathbf{h}_m^{(t)}; \mathbf{h}_n^{(s)}; \mathbf{t}_m]) \right), \quad [19.11]$$

which enables the model to learn to prefer parts of the source which have not been attended to yet (Tu et al., 2016). To further encourage diversity in the generated summary, See et al. (2017) introduce a **coverage loss** to the objective function,

$$\ell_m = \sum_{n=1}^{M^{(s)}} \min(\alpha_{m \rightarrow n}, t_{m \rightarrow n}). \quad [19.12]$$

10512 This loss will be low if  $\alpha_m$  assigns little attention to words that already have large values in  
 10513  $t_m$ . Coverage loss is similar to the concept of **marginal relevance**, in which the reward for  
 10514 adding new content is proportional to the extent to which it increases the overall amount  
 10515 of information conveyed by the summary (Carbonell and Goldstein, 1998).

10516 **19.2.2 Sentence fusion for multi-document summarization**

10517 In **multi-document summarization**, the goal is to produce a summary that covers the  
 10518 content of several documents (McKeown et al., 2002). One approach to this challenging  
 10519 problem is to identify sentences across multiple documents that relate to a single theme,  
 10520 and then to fuse them into a single sentence (Barzilay and McKeown, 2005). As an exam-  
 10521 ple, consider the following two sentences (McKeown et al., 2010):

- 10522 (19.4) Palin actually turned against the bridge project only after it became a national  
 10523 symbol of wasteful spending.  
 10524 (19.5) Ms. Palin supported the bridge project while running for governor, and aban-  
 10525 doned it after it became a national scandal.

10526 An *intersection* preserves only the content that is present in both sentences:

- 10527 (19.6) Palin turned against the bridge project after it became a national scandal.

10528 A *union* includes information from both sentences:

- 10529 (19.7) Ms. Palin supported the bridge project while running for governor, but turned  
 10530 against it when it became a national scandal and a symbol of wasteful spending.

Dependency parsing is often used as a technique for sentence fusion. After parsing each sentence, the resulting dependency trees can be aggregated into a lattice (Barzilay and McKeown, 2005) or a graph structure (Filippova and Strube, 2008), in which identical or closely related words (e.g., *Palin*, *bridge*, *national*) are fused into a single node. The resulting graph can then be pruned back to a tree by solving an **integer linear program** (see § 13.2.2),

$$\max_{\mathbf{y}} \sum_{i,j,r} \psi(i \xrightarrow{r} j, \mathbf{w}; \boldsymbol{\theta}) \times y_{i,j,r} \quad [19.13]$$

$$\text{s.t. } \mathbf{y} \in \mathcal{C}, \quad [19.14]$$

10531 where the variable  $y_{i,j,r} \in \{0, 1\}$  indicates whether there is an edge from  $i$  to  $j$  of type  $r$ ,  
 10532 the score of this edge is  $\psi(i \xrightarrow{r} j, \mathbf{w}; \boldsymbol{\theta})$ , and  $\mathcal{C}$  is a set of constraints, which ensures that  $\mathbf{y}$   
 10533 forms a valid dependency graph. As usual,  $\mathbf{w}$  is the list of words in the graph, and  $\boldsymbol{\theta}$  is a  
 10534 vector of parameters. The score  $\psi(i \xrightarrow{r} j, \mathbf{w}; \boldsymbol{\theta})$  reflects the “importance” of the modifier  
 10535  $j$  to the overall meaning: in intersective fusion, this score indicates the extent to which  
 10536 the content in this edge is expressed in all sentences; in union fusion, the score indicates  
 10537 whether the content in the edge is expressed in any sentence. The constraint set  $\mathcal{C}$  can  
 10538 impose additional linguistic constraints: for example, ensuring that coordinated nouns  
 10539 are sufficiently similar. The resulting tree must then be **linearized** into a sentence. Lin-  
 10540 earization is like the inverse of dependency parsing: instead of parsing from a sequence

10541 of tokens into a tree, we must convert the tree back into a sequence of tokens. This is  
 10542 typically done by generating a set of candidate linearizations, and choosing the one with  
 10543 the highest score under a language model (Langkilde and Knight, 1998; Song et al., 2016).

10544 **19.3 Dialogue**

10545 **Dialogue systems** are capable of conversing with a human interlocutor, often to per-  
 10546 form some task (Grosz, 1979), but sometimes just to chat (Weizenbaum, 1966). While re-  
 10547 search on dialogue systems goes back several decades (Carbonell, 1970; Winograd, 1972),  
 10548 commercial systems such as Alexa and Siri have recently brought this technology into  
 10549 widespread use. Nonetheless, there is a significant gap between research and practice:  
 10550 many practical dialogue systems remain scripted and inflexible, while research systems  
 10551 emphasize abstractive text generation, “on-the-fly” decision making, and probabilistic  
 10552 reasoning about the user’s intentions.

10553 **19.3.1 Finite-state and agenda-based dialogue systems**

10554 Finite-state automata were introduced in chapter 9 as a formal model of computation,  
 10555 in which string inputs and outputs are linked to transitions between a finite number of  
 10556 discrete states. This model naturally fits simple task-oriented dialogues, such as the one  
 10557 shown in the left panel of Figure 19.5. This (somewhat frustrating) dialogue can be repre-  
 10558 sented with a finite-state transducer, as shown in the right panel of the figure. The accept-  
 10559 ing state is reached only when the two needed pieces of information are provided, and the  
 10560 human user confirms that the order is correct. In this simple scenario, the TOPPING and  
 10561 ADDRESS are the two **slots** associated with the activity of ordering a pizza, which is called  
 10562 a **frame**. Frame representations can be hierarchical: for example, an ADDRESS could have  
 10563 slots of its own, such as STREET and CITY.

10564 In the example dialogue in Figure 19.5, the user provides the precise inputs that are  
 10565 needed in each turn (e.g., *anchovies*; *the College of Computing building*). Some users may  
 10566 prefer to communicate more naturally, with phrases like *I’d, uh, like some anchovies please*.  
 10567 One approach to handling such utterances is to design a custom grammar, with non-  
 10568 terminals for slots such as TOPPING and LOCATION. However, context-free parsing of  
 10569 unconstrained speech input is challenging. A more lightweight alternative is BIO-style  
 10570 sequence labeling (see § 8.3), e.g.:

10571 (19.9) *I’d like anchovies , and please bring it to the College of Computing*  
 10572 *Building .*  
 O O B-TOPPING O O O O O O B-ADDR I-ADDR I-ADDR I-ADDR I-ADDR  
 I-ADDR O

- (19.8) A: I want to order a pizza.  
 B: What toppings?  
 A: Anchovies.  
 B: Ok, what address?  
 A: The College of Computing building.  
 B: Please confirm: one pizza with artichokes, to be delivered to the College of Computing building.  
 A: No.  
 B: What toppings?  
 ...

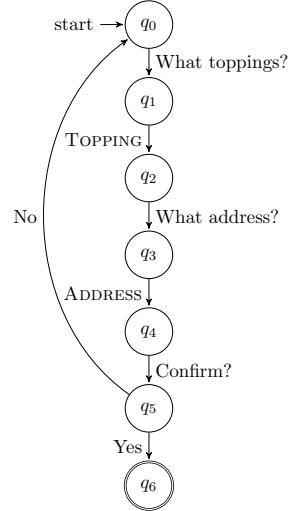


Figure 19.5: An example dialogue and the associated finite-state model. In the finite-state model, SMALL CAPS indicates that the user must provide information of this type in their answer.

10573 The tagger can be driven by a bi-directional recurrent neural network, similar to recurrent  
 10574 approaches to semantic role labeling described in § 13.2.3.

10575 The input in (19.9) could not be handled by the finite-state system from Figure 19.5,  
 10576 which forces the user to provide the topping first, and then the location. In this sense,  
 10577 the **initiative** is driven completely by the system. **Agenda-based dialogue systems** ex-  
 10578 tend finite-state architectures by attempting to recognize all slots that are filled by the  
 10579 user’s reply, thereby handling these more complex examples. Agenda-based systems dy-  
 10580 namically pose additional questions until the frame is complete (Bobrow et al., 1977; Allen  
 10581 et al., 1995; Rudnicky and Xu, 1999). Such systems are said to be **mixed-initiative**, because  
 10582 both the user and the system can drive the direction of the dialogue.

### 10583 19.3.2 Markov decision processes

10584 The task of dynamically selecting the next move in a conversation is known as **dialogue**  
 10585 **management**. This problem can be framed as a **Markov decision process**, which is a  
 10586 theoretical model that includes a discrete set of states, a discrete set of actions, a function  
 10587 that computes the probability of transitions between states, and a function that computes  
 10588 the cost or reward of action-state pairs. Let’s see how each of these elements pertains to  
 10589 the pizza ordering dialogue system.

- 10590 • Each state is a tuple of information about whether the topping and address are

10591 known, and whether the order has been confirmed. For example,

(KNOWN TOPPING, UNKNOWN ADDRESS, NOT CONFIRMED) [19.15]

10592 is a possible state. Any state in which the pizza order is confirmed is a terminal  
10593 state, and the Markov decision process stops after entering such a state.

- 10594 • The set of actions includes querying for the topping, querying for the address, and  
10595 requesting confirmation. Each action induces a probability distribution over states,  
10596  $p(s_t | a_t, s_{t-1})$ . For example, requesting confirmation of the order is not likely to  
10597 result in a transition to the terminal state if the topping is not yet known. This  
10598 probability distribution over state transitions may be learned from data, or it may  
10599 be specified in advance.
- 10600 • Each state-action-state tuple earns a reward,  $r_a(s_t, s_{t+1})$ . In the context of the pizza  
10601 ordering system, a simple reward function would be,

$$r_a(s_t, s_{t-1}) = \begin{cases} 0, & a = \text{CONFIRM}, s_t = (*, *, \text{CONFIRMED}) \\ -10, & a = \text{CONFIRM}, s_t = (*, *, \text{NOT CONFIRMED}) \\ -1, & a \neq \text{CONFIRM} \end{cases} \quad [19.16]$$

10602 This function assigns zero reward for successful transitions to the terminal state, a  
10603 large negative reward to a rejected request for confirmation, and a small negative re-  
10604 ward for every other type of action. The system is therefore rewarded for reaching  
10605 the terminal state in few steps, and penalized for prematurely requesting confirma-  
10606 tion.

10607 In a Markov decision process, a **policy** is a function  $\pi : \mathcal{S} \rightarrow \mathcal{A}$  that maps from states to  
10608 actions (see § 15.2.4.3). The value of a policy is the expected sum of discounted rewards,  
10609  $E_\pi[\sum_{t=1}^T \gamma^t r_{a_t}(s_t, s_{t+1})]$ , where  $\gamma$  is the discount factor,  $\gamma \in [0, 1)$ . Discounting has the  
10610 effect of emphasizing rewards that can be obtained immediately over less certain rewards  
10611 in the distant future.

10612 An optimal policy can be obtained by dynamic programming, by iteratively updating  
10613 the **value function**  $V(s)$ , which is the expectation of the cumulative reward from  $s$  under  
10614 the optimal action  $a$ ,

$$V(s) \leftarrow \max_{a \in \mathcal{A}} \sum_{s' \in \mathcal{S}} p(s' | s, a)[r_a(s, s') + \gamma V(s')]. \quad [19.17]$$

10615 The value function  $V(s)$  is computed in terms of  $V(s')$  for all states  $s' \in \mathcal{S}$ . A series  
10616 of iterative updates to the value function will eventually converge to a stationary point.  
10617 This algorithm is known as **value iteration**. Given the converged value function  $V(s)$ , the

10618 optimal action at each state is the argmax,

$$\pi(s) = \operatorname{argmax}_{a \in \mathcal{A}} \sum_{s' \in \mathcal{S}} p(s' | s, a)[r_a(s, s') + \gamma V(s')]. \quad [19.18]$$

10619 Value iteration and related algorithms are described in detail by Sutton and Barto (1998).  
 10620 For applications to dialogue systems, see Levin et al. (1998) and Walker (2000).

10621 The Markov decision process framework assumes that the current state of the dialogue  
 10622 is known. In reality, the system may misinterpret the user’s statements — for example,  
 10623 believing that a specification of the delivery location (PEACHTREE) is in fact a specification  
 10624 of the topping (PEACHES). In a **partially observable Markov decision process (POMDP)**,  
 10625 the system receives an *observation*  $o$ , which is probabilistically conditioned on the state,  
 10626  $p(o | s)$ . It must therefore maintain a distribution of beliefs about which state it is in, with  
 10627  $q_t(s)$  indicating the degree of belief that the dialogue is in state  $s$  at time  $t$ . The POMDP  
 10628 formulation can help to make dialogue systems more robust to errors, particularly in the  
 10629 context of spoken language dialogues, where the speech itself may be misrecognized (Roy  
 10630 et al., 2000; Williams and Young, 2007). However, finding the optimal policy in a POMDP  
 10631 is computationally intractable, requiring additional approximations.

### 10632 19.3.3 Neural chatbots

10633 Chatting is a lot easier when you don’t need to get anything done. **Chatbots** are systems  
 10634 that parry the user’s input with a response that keeps the conversation going. They can be  
 10635 built from the encoder-decoder architecture discussed in § 18.3 and § 19.1.2: the encoder  
 10636 converts the user’s input into a vector, and the decoder produces a sequence of words as a  
 10637 response. For example, Shang et al. (2015) apply the attentional encoder-decoder transla-  
 10638 tion model, training on a dataset of posts and responses from the Chinese microblogging  
 10639 platform Sina Weibo.<sup>5</sup> This approach is capable of generating replies that relate themati-  
 10640 cally to the input, as shown in the following examples:<sup>6</sup>

10641 (19.10) A: High fever attacks me every New Year’s day.  
 10642 B: Get well soon and stay healthy!

10643 (19.11) A: I gain one more year. Grateful to my group, so happy.  
 10644 B: Getting old now. Time has no mercy.

10645 While encoder-decoder models can generate responses that make sense in the con-  
 10646 text of the immediately preceding turn, they struggle to maintain coherence over longer

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<sup>5</sup>Twitter is also frequently used for construction of dialogue datasets (Ritter et al., 2011; Sordoni et al., 2015). Another source is technical support chat logs from the Ubuntu linux distribution (Uthus and Aha, 2013; Lowe et al., 2015).

<sup>6</sup>All examples are translated from Chinese by Shang et al. (2015).

conversations. One solution is to model the dialogue context recurrently. This creates a **hierarchical recurrent network**, including both word-level and turn-level recurrences. The turn-level hidden state is then used as additional context in the decoder (Serban et al., 2016).

An open question is how to integrate the encoder-decoder architecture into task-oriented dialogue systems. Neural chatbots can be trained end-to-end: the user’s turn is analyzed by the encoder, and the system output is generated by the decoder. This architecture can be trained by log-likelihood using backpropagation (e.g., Sordoni et al., 2015; Serban et al., 2016), or by more elaborate objectives, using reinforcement learning (Li et al., 2016). In contrast, the task-oriented dialogue systems described in § 19.3.1 typically involve a set of specialized modules: one for recognizing the user input, another for deciding what action to take, and a third for arranging the text of the system output.

Recurrent neural network decoders can be integrated into Markov Decision Process dialogue systems, by conditioning the decoder on a representation of the information that is to be expressed in each turn (Wen et al., 2015). Specifically, the long short-term memory (LSTM; § 6.3) architecture is augmented so that the memory cell at turn  $m$  takes an additional input  $d_m$ , which is a representation of the slots and values to be expressed in the next turn. However, this approach still relies on additional modules to recognize the user’s utterance and to plan the overall arc of the dialogue.

Another promising direction is to create embeddings for the elements in the domain: for example, the slots in a record and the entities that can fill them. The encoder then encodes not only the words of the user’s input, but the embeddings of the elements that the user mentions. Similarly, the decoder is endowed with the ability to refer to specific elements in the knowledge base. He et al. (2017) show that such a method can learn to play a collaborative dialogue game, in which both players are given a list of entities and their properties, and the goal is to find an entity that is on both players’ lists.

## 10673 Further reading

10674 Gatt and Krahmer (2018) provide a comprehensive recent survey on text generation. For  
10675 a book-length treatment of earlier work, see Reiter and Dale (2000). For a survey on image  
10676 captioning, see Bernardi et al. (2016); for a survey of pre-neural approaches to dialogue  
10677 systems, see Rieser and Lemon (2011). **Dialogue acts** were introduced in § 8.6 as a label-  
10678 ing scheme for human-human dialogues; they also play a critical role in task-based dialogue  
10679 systems (e.g., Allen et al., 1996). The incorporation of theoretical models of dialogue into  
10680 computational systems is reviewed by Jurafsky and Martin (2009, chapter 24).

10681 While this chapter has focused on the informative dimension of text generation, an-  
10682 other line of research aims to generate text with configurable stylistic properties (Walker  
10683 et al., 1997; Mairesse and Walker, 2011; Ficler and Goldberg, 2017; Hu et al., 2017). This

10684 chapter also does not address the generation of creative text such as narratives (Riedl and  
10685 Young, 2010), jokes (Ritchie, 2001), poems (Colton et al., 2012), and song lyrics (Gonçalo Oliveira  
10686 et al., 2007).

## 10687 Exercises

- 10688 1. Find an article about a professional basketball game, with an associated “box score”  
10689 of statistics. Which are the first three elements in the box score that are expressed  
10690 in the article? Can you identify template-based patterns that express these elements  
10691 of the record? Now find a second article about a different basketball game. Does it  
10692 mention the same first three elements of the box score? Do your templates capture  
10693 how these elements are expressed in the text?
- 10694 2. This exercise is to be done by a pair of students. One student should choose an article  
10695 from the news or from Wikipedia, and manually perform semantic role labeling  
10696 (SRL) on three short sentences or clauses. (See chapter 13 for a review of SRL.)  
10697 Identify the main the semantic relation and its arguments and adjuncts. Pass this  
10698 structured record — but not the original sentence — to the other student, whose  
10699 job is to generate a sentence expressing the semantics. Then reverse roles, and try  
10700 to regenerate three sentences from another article, based on the predicate-argument  
10701 semantics.
- 10702 3. Compute the BLEU scores (see § 18.1.1) for the generated sentences in the previous  
10703 problem, using the original article text as the reference.
- 10704 4. Align each token in the text of Figure 19.1 to a specific single record in the database,  
10705 or to the null record  $\emptyset$ . For example, the tokens *south wind* would align to the record  
10706 *wind direction: 06:00-21:00: mode=S*. How often is each token aligned  
10707 to the same record as the previous token? How many transitions are there? How  
10708 might a system learn to output *10 degrees* for the record *min=9*?
- 10709 5. In sentence compression and fusion, we may wish to preserve contiguous sequences  
10710 of tokens (*n*-grams) and/or dependency edges. Find five short news articles with  
10711 headlines. For each headline, compute the fraction of bigrams that appear in the  
10712 main text of the article. Then do a manual dependency parse of the headline. For  
10713 each dependency edge, count how often it appears as a dependency edge in the  
10714 main text. You may use an automatic dependency parser to assist with this exercise,  
10715 but check the output, and focus on UD 2.0 dependency grammar, as described in  
10716 chapter 11.
- 10717 6. § 19.2.2 presents the idea of generating text from dependency trees, which requires  
10718 **linearization**. Sometimes there are multiple ways that a dependency tree can be  
10719 linearized. For example:

10720 (19.12) The sick kids stayed at home in bed.

10721 (19.13) The sick kids stayed in bed at home.

10722 Both sentences have an identical dependency parse: both *home* and *bed* are (oblique)  
10723 dependents of *stayed*.

10724 Identify two more English dependency trees that can each be linearized in more than  
10725 one way, and try to use a different pattern of variation in each tree. As usual, specify  
10726 your trees in the Universal Dependencies 2 style, which is described in chapter 11.

7. In § 19.3.2, we considered a pizza delivery service. Let's simplify the problem to take-out, where it is only necessary to determine the topping and confirm the order. The state is a tuple in which the first element is *T* if the topping is specified and ? otherwise, and the second element is either YES or NO, depending on whether the order has been confirmed. The actions are TOPPING? (request information about the topping) and CONFIRM? (request confirmation). The state transition function is:

$$p(s_t | s_{t-1} = (?, \text{NO}), a = \text{TOPPING?}) = \begin{cases} 0.9, & s_t = (\text{T}, \text{NO}) \\ 0.1, & s_t = (?, \text{NO}). \end{cases} \quad [19.19]$$

$$p(s_t | s_{t-1} = (?, \text{NO}), a = \text{CONFIRM?}) = \begin{cases} 1, & s_t = (?, \text{NO}). \end{cases} \quad [19.20]$$

$$p(s_t | s_{t-1} = (\text{T}, \text{NO}), a = \text{TOPPING?}) = \begin{cases} 1, & s_t = (\text{T}, \text{NO}). \end{cases} \quad [19.21]$$

$$p(s_t | s_{t-1} = (\text{T}, \text{NO}), a = \text{CONFIRM?}) = \begin{cases} 0.9, & s_t = (\text{T}, \text{YES}) \\ 0.1, & s_t = (\text{T}, \text{NO}). \end{cases} \quad [19.22]$$

10727 Using the reward function defined in Equation 19.16, the discount  $\gamma = 0.9$ , and the  
10728 initialization  $V(s) = 0$ , execute three iterations of Equation 19.17. After these three  
10729 iterations, compute the optimal action in each state. You can assume that for the  
10730 terminal states,  $V(*, \text{YES}) = 0$ , so you only need to compute the values for non-  
10731 terminal states,  $V(?, \text{NO})$  and  $V(\text{T}, \text{NO})$ .

- 10732 8. There are several toolkits that allow you to train encoder-decoder translation models  
10733 "out of the box", such as FairSeq (Gehring et al., 2017), xnmt (Neubig et al., 2018),  
10734 tensor2tensor (Vaswani et al., 2018), and OpenNMT (Klein et al., 2017).<sup>7</sup> Use one  
10735 of these toolkits to train a chatbot dialogue system, using either the NPS dialogue  
10736 corpus that comes with nltk (Forsyth and Martell, 2007), or, if you are feeling more  
10737 ambitious, the Ubuntu dialogue corpus (Lowe et al., 2015).

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<sup>7</sup><https://github.com/facebookresearch/fairseq>; <https://github.com/neulab/xnmt>;  
<https://github.com/tensorflow/tensor2tensor>; <http://opennmt.net/>



10738 **Appendix A**

10739 **Probability**

10740 Probability theory provides a way to reason about random events. The sorts of random  
10741 events that are typically used to explain probability theory include coin flips, card draws,  
10742 and the weather. It may seem odd to think about the choice of a word as akin to the flip of  
10743 a coin, particularly if you are the type of person to choose words carefully. But random or  
10744 not, language has proven to be extremely difficult to model deterministically. Probability  
10745 offers a powerful tool for modeling and manipulating linguistic data.

10746 Probability can be thought of in terms of **random outcomes**: for example, a single coin  
10747 flip has two possible outcomes, heads or tails. The set of possible outcomes is the **sample**  
10748 **space**, and a subset of the **sample space** is an **event**. For a sequence of two coin flips,  
10749 there are four possible outcomes,  $\{HH, HT, TH, TT\}$ , representing the ordered sequences  
10750 heads-head, heads-tails, tails-heads, and tails-tails. The event of getting exactly one head  
10751 includes two outcomes:  $\{HT, TH\}$ .

10752 Formally, a probability is a function from events to the interval between zero and one:  
10753  $\Pr : \mathcal{F} \rightarrow [0, 1]$ , where  $\mathcal{F}$  is the set of possible events. An event that is certain has proba-  
10754 bility one; an event that is impossible has probability zero. For example, the probability  
10755 of getting fewer than three heads on two coin flips is one. Each outcome is also an event  
10756 (a set with exactly one element), and for two flips of a fair coin, the probability of each  
10757 outcome is,

$$\Pr(\{HH\}) = \Pr(\{HT\}) = \Pr(\{TH\}) = \Pr(\{TT\}) = \frac{1}{4}. \quad [\text{A.1}]$$

10758 **A.1 Probabilities of event combinations**

10759 Because events are sets of outcomes, we can use set-theoretic operations such as comple-  
10760 ment, intersection, and union to reason about the probabilities of events and their combi-  
10761 nations.

10762 For any event  $A$ , there is a **complement**  $\neg A$ , such that:

- 10763 • The probability of the union  $A \cup \neg A$  is  $\Pr(A \cup \neg A) = 1$ ;  
 10764 • The intersection  $A \cap \neg A = \emptyset$  is the empty set, and  $\Pr(A \cap \neg A) = 0$ .

10765 In the coin flip example, the event of obtaining a single head on two flips corresponds to  
 10766 the set of outcomes  $\{HT, TH\}$ ; the complement event includes the other two outcomes,  
 10767  $\{TT, HH\}$ .

### 10768 A.1.1 Probabilities of disjoint events

10769 When two events have an empty intersection,  $A \cap B = \emptyset$ , they are **disjoint**. The probabili-  
 10770 ty of the union of two disjoint events is equal to the sum of their probabilities,

$$A \cap B = \emptyset \Rightarrow \Pr(A \cup B) = \Pr(A) + \Pr(B). \quad [A.2]$$

10771 This is the **third axiom of probability**, and it can be generalized to any countable sequence  
 10772 of disjoint events.

In the coin flip example, this axiom can derive the probability of the event of getting a single head on two flips. This event is the set of outcomes  $\{HT, TH\}$ , which is the union of two simpler events,  $\{HT, TH\} = \{HT\} \cup \{TH\}$ . The events  $\{HT\}$  and  $\{TH\}$  are disjoint. Therefore,

$$\Pr(\{HT, TH\}) = \Pr(\{HT\} \cup \{TH\}) = \Pr(\{HT\}) + \Pr(\{TH\}) \quad [A.3]$$

$$= \frac{1}{4} + \frac{1}{4} = \frac{1}{2}. \quad [A.4]$$

10773 In the general, the probability of the union of two events is,

$$\Pr(A \cup B) = \Pr(A) + \Pr(B) - \Pr(A \cap B). \quad [A.5]$$

This can be seen visually in Figure A.1, and it can be derived from the third axiom of probability. Consider an event that includes all outcomes in  $B$  that are not in  $A$ , denoted as  $B - (A \cap B)$ . By construction, this event is disjoint from  $A$ . We can therefore apply the additive rule,

$$\Pr(A \cup B) = \Pr(A) + \Pr(B - (A \cap B)). \quad [A.6]$$

Furthermore, the event  $B$  is the union of two disjoint events:  $A \cap B$  and  $B - (A \cap B)$ .

$$\Pr(B) = \Pr(B - (A \cap B)) + \Pr(A \cap B). \quad [A.7]$$

Reorganizing and substituting into Equation A.6 gives the desired result:

$$\Pr(B - (A \cap B)) = \Pr(B) - \Pr(A \cap B) \quad [A.8]$$

$$\Pr(A \cup B) = \Pr(A) + \Pr(B) - \Pr(A \cap B). \quad [A.9]$$

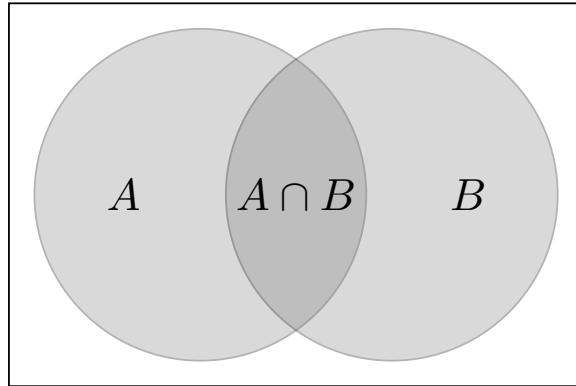


Figure A.1: A visualization of the probability of non-disjoint events  $A$  and  $B$ .

### 10774 A.1.2 Law of total probability

10775 A set of events  $\mathcal{B} = \{B_1, B_2, \dots, B_N\}$  is a **partition** of the sample space iff each pair of  
 10776 events is disjoint ( $B_i \cap B_j = \emptyset$ ), and the union of the events is the entire sample space.  
 10777 The law of total probability states that we can **marginalize** over these events as follows,

$$\Pr(A) = \sum_{B_n \in \mathcal{B}} \Pr(A \cap B_n). \quad [\text{A.10}]$$

10778 For any event  $B$ , the union  $B \cup \neg B$  is a partition of the sample space. Therefore, a special  
 10779 case of the law of total probability is,

$$\Pr(A) = \Pr(A \cap B) + \Pr(A \cap \neg B). \quad [\text{A.11}]$$

## 10780 A.2 Conditional probability and Bayes' rule

A **conditional probability** is an expression like  $\Pr(A \mid B)$ , which is the probability of the event  $A$ , assuming that event  $B$  happens too. For example, we may be interested in the probability of a randomly selected person answering the phone by saying *hello*, conditioned on that person being a speaker of English. Conditional probability is defined as the ratio,

$$\Pr(A \mid B) = \frac{\Pr(A \cap B)}{\Pr(B)}. \quad [\text{A.12}]$$

The **chain rule of probability** states that  $\Pr(A \cap B) = \Pr(A \mid B) \times \Pr(B)$ , which is just

a rearrangement of terms from Equation A.12. The chain rule can be applied repeatedly:

$$\begin{aligned}\Pr(A \cap B \cap C) &= \Pr(A | B \cap C) \times \Pr(B \cap C) \\ &= \Pr(A | B \cap C) \times \Pr(B | C) \times \Pr(C).\end{aligned}$$

**Bayes' rule** (sometimes called Bayes' law or Bayes' theorem) gives us a way to convert between  $\Pr(A | B)$  and  $\Pr(B | A)$ . It follows from the definition of conditional probability and the chain rule:

$$\Pr(A | B) = \frac{\Pr(A \cap B)}{\Pr(B)} = \frac{\Pr(B | A) \times \Pr(A)}{\Pr(B)} \quad [\text{A.13}]$$

10781 Each term in Bayes rule has a name, which we will occasionally use:

- 10782 • Pr( $A$ ) is the **prior**, since it is the probability of event  $A$  without knowledge about  
10783 whether  $B$  happens or not.
- 10784 • Pr( $B | A$ ) is the **likelihood**, the probability of event  $B$  given that event  $A$  has oc-  
10785 curred.
- 10786 • Pr( $A | B$ ) is the **posterior**, the probability of event  $A$  with knowledge that  $B$  has  
10787 occurred.

10788 **Example** The classic examples for Bayes' rule involve tests for rare diseases, but Man-  
10789 ning and Schütze (1999) reframe this example in a linguistic setting. Suppose that you are  
10790 interested in a rare syntactic construction, such as *parasitic gaps*, which occur on average  
10791 once in 100,000 sentences. Here is an example of a parasitic gap:

10792 (A.1) *Which class did you attend ... without registering for ...?*

10793 Lana Linguist has developed a complicated pattern matcher that attempts to identify  
10794 sentences with parasitic gaps. It's pretty good, but it's not perfect:

- 10795 • If a sentence has a parasitic gap, the pattern matcher will find it with probability  
10796 0.95. (This is the **recall**, which is one minus the **false positive rate**.)
- 10797 • If the sentence doesn't have a parasitic gap, the pattern matcher will wrongly say it  
10798 does with probability 0.005. (This is the **false positive rate**, which is one minus the  
10799 **precision**.)

10800 Suppose that Lana's pattern matcher says that a sentence contains a parasitic gap. What  
10801 is the probability that this is true?

Let  $G$  be the event of a sentence having a parasitic gap, and  $T$  be the event of the test being positive. We are interested in the probability of a sentence having a parasitic gap given that the test is positive. This is the conditional probability  $\Pr(G | T)$ , and it can be computed by Bayes' rule:

$$\Pr(G | T) = \frac{\Pr(T | G) \times \Pr(G)}{\Pr(T)}. \quad [\text{A.14}]$$

10802 We already know both terms in the numerator:  $\Pr(T | G)$  is the recall, which is 0.95;  $\Pr(G)$   
10803 is the prior, which is  $10^{-5}$ .

10804 We are not given the denominator, but it can be computed using tools developed earlier  
10805 in this section. First apply the law of total probability, using the partition  $\{G, \neg G\}$ :

$$\Pr(T) = \Pr(T \cap G) + \Pr(T \cap \neg G). \quad [\text{A.15}]$$

This says that the probability of the test being positive is the sum of the probability of a **true positive** ( $T \cap G$ ) and the probability of a **false positive** ( $T \cap \neg G$ ). The probability of each of these events can be computed using the chain rule:

$$\Pr(T \cap G) = \Pr(T | G) \times \Pr(G) = 0.95 \times 10^{-5} \quad [\text{A.16}]$$

$$\Pr(T \cap \neg G) = \Pr(T | \neg G) \times \Pr(\neg G) = 0.005 \times (1 - 10^{-5}) \approx 0.005 \quad [\text{A.17}]$$

$$\Pr(T) = \Pr(T \cap G) + \Pr(T \cap \neg G) \quad [\text{A.18}]$$

$$= 0.95 \times 10^{-5} + 0.005. \quad [\text{A.19}]$$

Plugging these terms into Bayes' rule gives the desired posterior probability,

$$\Pr(G | T) = \frac{\Pr(T | G) \Pr(G)}{\Pr(T)} \quad [\text{A.20}]$$

$$= \frac{0.95 \times 10^{-5}}{0.95 \times 10^{-5} + 0.005 \times (1 - 10^{-5})} \quad [\text{A.21}]$$

$$\approx 0.002. \quad [\text{A.22}]$$

10806 Lana's pattern matcher seems accurate, with false positive and false negative rates  
10807 below 5%. Yet the extreme rarity of the phenomenon means that a positive result from the  
10808 detector is most likely to be wrong.

### 10809 A.3 Independence

Two events are independent if the probability of their intersection is equal to the product of their probabilities:  $\Pr(A \cap B) = \Pr(A) \times \Pr(B)$ . For example, for two flips of a fair

coin, the probability of getting heads on the first flip is independent of the probability of getting heads on the second flip:

$$\Pr(\{HT, HH\}) = \Pr(HT) + \Pr(HH) = \frac{1}{4} + \frac{1}{4} = \frac{1}{2} \quad [A.23]$$

$$\Pr(\{HH, TH\}) = \Pr(HH) + \Pr(TH) = \frac{1}{4} + \frac{1}{4} = \frac{1}{2} \quad [A.24]$$

$$\Pr(\{HT, HH\}) \times \Pr(\{HH, TH\}) = \frac{1}{2} \times \frac{1}{2} = \frac{1}{4} \quad [A.25]$$

$$\Pr(\{HT, HH\} \cap \{HH, TH\}) = \Pr(HH) = \frac{1}{4} \quad [A.26]$$

$$= \Pr(\{HT, HH\}) \times \Pr(\{HH, TH\}). \quad [A.27]$$

If  $\Pr(A \cap B \mid C) = \Pr(A \mid C) \times \Pr(B \mid C)$ , then the events  $A$  and  $B$  are **conditionally independent**, written  $A \perp B \mid C$ . Conditional independence plays a important role in probabilistic models such as Naïve Bayes chapter 2.

## A.4 Random variables

Random variables are functions from events to  $\mathbb{R}^n$ , where  $\mathbb{R}$  is the set of real numbers. This subsumes several useful special cases:

- An **indicator random variable** is a function from events to the set  $\{0, 1\}$ . In the coin flip example, we can define  $Y$  as an indicator random variable, taking the value 1 when the coin has come up heads on at least one flip. This would include the outcomes  $\{HH, HT, TH\}$ . The probability  $\Pr(Y = 1)$  is the sum of the probabilities of these outcomes,  $\Pr(Y = 1) = \frac{1}{4} + \frac{1}{4} + \frac{1}{4} = \frac{3}{4}$ .
- A **discrete random variable** is a function from events to a discrete subset of  $\mathbb{R}$ . Consider the coin flip example: the number of heads on two flips,  $X$ , can be viewed as a discrete random variable,  $X \in \{0, 1, 2\}$ . The event probability  $\Pr(X = 1)$  can again be computed as the sum of the probabilities of the events in which there is one head,  $\{HT, TH\}$ , giving  $\Pr(X = 1) = \frac{1}{4} + \frac{1}{4} = \frac{1}{2}$ .

Each possible value of a random variable is associated with a subset of the sample space. In the coin flip example,  $X = 0$  is associated with the event  $\{TT\}$ ,  $X = 1$  is associated with the event  $\{HT, TH\}$ , and  $X = 2$  is associated with the event  $\{HH\}$ . Assuming a fair coin, the probabilities of these events are, respectively,  $1/4$ ,  $1/2$ , and  $1/4$ . This list of numbers represents the **probability distribution** over  $X$ , written  $p_X$ , which maps from the possible values of  $X$  to the non-negative reals. For a specific value  $x$ , we write  $p_X(x)$ , which is equal to the event probability  $\Pr(X = x)$ .<sup>1</sup> The function  $p_X$  is called

<sup>1</sup>In general, capital letters (e.g.,  $X$ ) refer to random variables, and lower-case letters (e.g.,  $x$ ) refer to specific values. When the distribution is clear from context, I will simply write  $p(x)$ .

a probability **mass** function (pmf) if  $X$  is discrete; it is called a probability **density** function (pdf) if  $X$  is continuous. In either case, the function must sum to one, and all values must be non-negative:

$$\int_x p_X(x)dx = 1 \quad [A.28]$$

$$\forall x, p_X(x) \geq 0. \quad [A.29]$$

Probabilities over multiple random variables can written as **joint probabilities**, e.g.,  $p_{A,B}(a,b) = \Pr(A = a \cap B = b)$ . Several properties of event probabilities carry over to probability distributions over random variables:

- The **marginal probability distribution** is  $p_A(a) = \sum_b p_{A,B}(a,b)$ .
- The **conditional probability distribution** is  $p_{A|B}(a | b) = \frac{p_{A,B}(a,b)}{p_B(b)}$ .
- Random variables  $A$  and  $B$  are independent iff  $p_{A,B}(a,b) = p_A(a) \times p_B(b)$ .

## A.5 Expectations

Sometimes we want the **expectation** of a function, such as  $E[g(x)] = \sum_{x \in \mathcal{X}} g(x)p(x)$ . Expectations are easiest to think about in terms of probability distributions over discrete events:

- If it is sunny, Lucia will eat three ice creams.
- If it is rainy, she will eat only one ice cream.
- There's a 80% chance it will be sunny.
- The expected number of ice creams she will eat is  $0.8 \times 3 + 0.2 \times 1 = 2.6$ .

If the random variable  $X$  is continuous, the expectation is an integral:

$$E[g(x)] = \int_{\mathcal{X}} g(x)p(x)dx \quad [A.30]$$

For example, a fast food restaurant in Quebec has a special offer for cold days: they give a 1% discount on poutine for every degree below zero. Assuming a thermometer with infinite precision, the expected price would be an integral over all possible temperatures,

$$E[\text{price}(x)] = \int_{\mathcal{X}} \min(1, 1+x) \times \text{original-price} \times p(x)dx. \quad [A.31]$$

10844 **A.6 Modeling and estimation**

10845 **Probabilistic models** provide a principled way to reason about random events and ran-  
10846 dom variables. Let's consider the coin toss example. Each toss can be modeled as a ran-  
10847 dom event, with probability  $\theta$  of the event  $H$ , and probability  $1 - \theta$  of the complementary  
10848 event  $T$ . If we write a random variable  $X$  as the total number of heads on three coin  
10849 flips, then the distribution of  $X$  depends on  $\theta$ . In this case,  $X$  is distributed as a **binomial**  
10850 **random variable**, meaning that it is drawn from a binomial distribution, with **parameters**  
10851  $(\theta, N = 3)$ . This is written,

$$X \sim \text{Binomial}(\theta, N = 3). \quad [\text{A.32}]$$

10852 The properties of the binomial distribution enable us to make statements about the  $X$ ,  
10853 such as its expected value and the likelihood that its value will fall within some interval.

Now suppose that  $\theta$  is unknown, but we have run an experiment, in which we ex-  
 ecuted  $N$  trials, and obtained  $x$  heads. We can **estimate**  $\theta$  by the principle of **maximum**  
**likelihood**:

$$\hat{\theta} = \operatorname{argmax}_{\theta} p_X(x; \theta, N). \quad [\text{A.33}]$$

This says that the estimate  $\hat{\theta}$  should be the value that maximizes the likelihood of the  
 data. The semicolon indicates that  $\theta$  and  $N$  are parameters of the probability function.  
 The likelihood  $p_X(x; \theta, N)$  can be computed from the binomial distribution,

$$p_X(x; \theta, N) = \frac{N!}{x!(N-x)!} \theta^x (1-\theta)^{N-x}. \quad [\text{A.34}]$$

10854 This likelihood is proportional to the product of the probability of individual out-  
10855 comes: for example, the sequence  $T, H, H, T, H$  would have probability  $\theta^3(1-\theta)^2$ . The  
10856 term  $\frac{N!}{x!(N-x)!}$  arises from the many possible orderings by which we could obtain  $x$  heads  
10857 on  $N$  trials. This term does not depend on  $\theta$ , so it can be ignored during estimation.

In practice, we maximize the log-likelihood, which is a monotonic function of the like-  
 lihood. Under the binomial distribution, the log-likelihood is a **convex** function of  $\theta$  (see

§ 2.3), so it can be maximized by taking the derivative and setting it equal to zero.

$$\ell(\theta) = x \log \theta + (N - x) \log(1 - \theta) \quad [\text{A.35}]$$

$$\frac{\partial \ell(\theta)}{\partial \theta} = \frac{x}{\theta} - \frac{N - x}{1 - \theta} \quad [\text{A.36}]$$

$$\frac{N - x}{1 - \theta} = \frac{x}{\theta} \quad [\text{A.37}]$$

$$\frac{N - x}{x} = \frac{1 - \theta}{\theta} \quad [\text{A.38}]$$

$$\frac{N}{x} - 1 = \frac{1}{\theta} - 1 \quad [\text{A.39}]$$

$$\hat{\theta} = \frac{x}{N}. \quad [\text{A.40}]$$

10858 In this case, the maximum likelihood estimate is equal to  $\frac{x}{N}$ , the fraction of trials that  
 10859 came up heads. This intuitive solution is also known as the **relative frequency estimate**,  
 10860 since it is equal to the relative frequency of the outcome.

Is maximum likelihood estimation always the right choice? Suppose you conduct one trial, and get heads. Would you conclude that  $\theta = 1$ , meaning that the coin is guaranteed to come up heads? If not, then you must have some **prior expectation** about  $\theta$ . To incorporate this prior information, we can treat  $\theta$  as a random variable, and use Bayes' rule:

$$p(\theta | x; N) = \frac{p(x | \theta) \times p(\theta)}{p(x)} \quad [\text{A.41}]$$

$$\propto p(x | \theta) \times p(\theta) \quad [\text{A.42}]$$

$$\hat{\theta} = \operatorname{argmax}_{\theta} p(x | \theta) \times p(\theta). \quad [\text{A.43}]$$

10861 This is the **maximum a posteriori** (MAP) estimate. Given a form for  $p(\theta)$ , you can de-  
 10862 rive the MAP estimate using the same approach that was used to derive the maximum  
 10863 likelihood estimate.

## 10864 Additional resources

10865 A good introduction to probability theory is offered by Manning and Schütze (1999),  
 10866 which helped to motivate this section. For more detail, Sharon Goldwater provides an-  
 10867 other useful reference, <http://homepages.inf.ed.ac.uk/sgwater/teaching/general/probability.pdf>. A historical and philosophical perspective on probability is offered  
 10868 by Diaconis and Skyrms (2017).



10870 **Appendix B**

10871 **Numerical optimization**

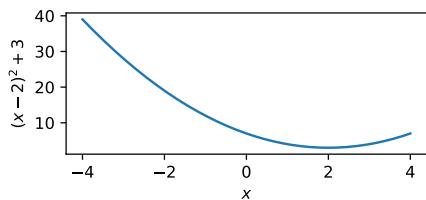
10872 Unconstrained numerical optimization involves solving problems of the form,

$$\min_{\mathbf{x} \in \mathbb{R}^D} f(\mathbf{x}), \quad [\text{B.1}]$$

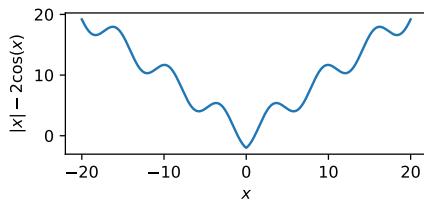
10873 where  $\mathbf{x} \in \mathbb{R}^D$  is a vector of  $D$  real numbers.

10874 Differentiation is fundamental to continuous optimization. Suppose that at some  $\mathbf{x}^*$ ,  
10875 every partial derivative is equal to 0: formally,  $\frac{\partial f}{\partial x_i}\Big|_{\mathbf{x}^*} = 0$ . Then  $\mathbf{x}^*$  is said to be a **critical**  
10876 **point** of  $f$ . For a **convex** function  $f$  (defined in § 2.3),  $f(\mathbf{x}^*)$  is equal to the global minimum  
10877 of  $f$  iff  $\mathbf{x}^*$  is a critical point of  $f$ .

As an example, consider the convex function  $f(x) = (x - 2)^2 + 3$ , shown in Figure B.1a. The derivative is  $\frac{\partial f}{\partial x} = 2x - 4$ . A unique minimum can be obtained by setting the derivative equal to zero and solving for  $x$ , obtaining  $x^* = 2$ . Now consider the multivariate convex function  $f(\mathbf{x}) = \frac{1}{2}\|\mathbf{x} - [2, 1]^\top\|^2$ , where  $\|\mathbf{x}\|^2$  is the squared Euclidean norm. The partial



(a) The function  $f(x) = (x - 2)^2 + 3$



(b) The function  $f(x) = |x| - 2\cos(x)$

Figure B.1: Two functions with unique global minima

derivatives are,

$$\frac{\partial d}{\partial x_1} = x_1 - 2 \quad [B.2]$$

$$\frac{\partial d}{\partial x_2} = x_2 - 1 \quad [B.3]$$

10878 The unique minimum is  $\mathbf{x}^* = [2, 1]^\top$ .

10879 For non-convex functions, critical points are not necessarily global minima. A **local**  
 10880 **minimum**  $\mathbf{x}^*$  is a point at which the function takes a smaller value than at all nearby  
 10881 neighbors: formally,  $\mathbf{x}^*$  is a local minimum if there is some positive  $\epsilon$  such that  $f(\mathbf{x}^*) \leq$   
 10882  $f(\mathbf{x})$  for all  $\mathbf{x}$  within distance  $\epsilon$  of  $\mathbf{x}^*$ . Figure B.1b shows the function  $f(x) = |x| - 2 \cos(x)$ ,  
 10883 which has many local minima, as well as a unique global minimum at  $x = 0$ . A critical  
 10884 point may also be the local or global maximum of the function; it may be a **saddle point**,  
 10885 which is a minimum with respect to at least one coordinate, and a maximum with respect  
 10886 to at least one other coordinate; it may be an **inflection point**, which is neither a minimum  
 10887 nor maximum. When available, the second derivative of  $f$  can help to distinguish these  
 10888 cases.

## 10889 B.1 Gradient descent

For many convex functions, it is not possible to solve for  $\mathbf{x}^*$  in closed form. In gradient descent, we compute a series of solutions,  $\mathbf{x}^{(0)}, \mathbf{x}^{(1)}, \dots$  by taking steps along the local gradient  $\nabla_{\mathbf{x}^{(t)}} f$ , which is the vector of partial derivatives of the function  $f$ , evaluated at the point  $\mathbf{x}^{(t)}$ . Each solution  $\mathbf{x}^{(t+1)}$  is computed,

$$\mathbf{x}^{(t+1)} \leftarrow \mathbf{x}^{(t)} - \eta^{(t)} \nabla_{\mathbf{x}^{(t)}} f. \quad [B.4]$$

10890 where  $\eta^{(t)} > 0$  is a **step size**. If the step size is chosen appropriately, this procedure will  
 10891 find the global minimum of a differentiable convex function. For non-convex functions,  
 10892 gradient descent will find a local minimum. The extension to non-differentiable convex  
 10893 functions is discussed in § 2.3.

## 10894 B.2 Constrained optimization

Optimization must often be performed under constraints: for example, when optimizing the parameters of a probability distribution, the probabilities of all events must sum to one. Constrained optimization problems can be written,

$$\min_{\mathbf{x}} f(\mathbf{x}) \quad [B.5]$$

$$\text{s.t. } g_c(\mathbf{x}) \leq 0, \quad \forall c = 1, 2, \dots, C \quad [B.6]$$

where each  $g_i(\mathbf{x})$  is a scalar function of  $\mathbf{x}$ . For example, suppose that  $\mathbf{x}$  must be non-negative, and that its sum cannot exceed a budget  $b$ . Then there are  $D + 1$  inequality constraints,

$$g_i(\mathbf{x}) = -x_i, \quad \forall i = 1, 2, \dots, D \quad [\text{B.7}]$$

$$g_{D+1}(\mathbf{x}) = -b + \sum_{i=1}^D x_i. \quad [\text{B.8}]$$

Inequality constraints can be combined with the original objective function  $f$  by forming a **Lagrangian**,

$$L(\mathbf{x}, \boldsymbol{\lambda}) = f(\mathbf{x}) + \sum_{c=1}^C \lambda_c g_c(\mathbf{x}), \quad [\text{B.9}]$$

where  $\lambda_c$  is a **Lagrange multiplier**. For any Lagrangian, there is a corresponding **dual form**, which is a function of  $\boldsymbol{\lambda}$ :

$$D(\boldsymbol{\lambda}) = \min_{\mathbf{x}} L(\mathbf{x}, \boldsymbol{\lambda}). \quad [\text{B.10}]$$

The Lagrangian  $L$  can be referred to as the **primal form**.

### B.3 Example: Passive-aggressive online learning

Sometimes it is possible to solve a constrained optimization problem by manipulating the Lagrangian. One example is maximum-likelihood estimation of a Naïve Bayes probability model, as described in § 2.1.3. In that case, it is unnecessary to explicitly compute the Lagrange multiplier. Another example is illustrated by the **passive-aggressive** algorithm for online learning (Crammer et al., 2006). This algorithm is similar to the perceptron, but the goal at each step is to make the most conservative update that gives zero margin loss on the current example.<sup>1</sup> Each update can be formulated as a constrained optimization over the weights  $\boldsymbol{\theta}$ :

$$\min_{\boldsymbol{\theta}} \frac{1}{2} \|\boldsymbol{\theta} - \boldsymbol{\theta}^{(i-1)}\|^2 \quad [\text{B.11}]$$

$$\text{s.t. } \ell^{(i)}(\boldsymbol{\theta}) = 0 \quad [\text{B.12}]$$

where  $\boldsymbol{\theta}^{(i-1)}$  is the previous set of weights, and  $\ell^{(i)}(\boldsymbol{\theta})$  is the margin loss on instance  $i$ . As in § 2.3.1, this loss is defined as,

$$\ell^{(i)}(\boldsymbol{\theta}) = 1 - \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y^{(i)}) + \max_{y \neq y^{(i)}} \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}^{(i)}, y). \quad [\text{B.13}]$$

---

<sup>1</sup>This is the basis for the name of the algorithm: it is passive when the loss is zero, but it aggressively moves to make the loss zero when necessary.

When the margin loss is zero for  $\theta^{(i-1)}$ , the optimal solution is simply to set  $\theta^* = \theta^{(i-1)}$ , so we will focus on the case where  $\ell^{(i)}(\theta^{(i-1)}) > 0$ . The Lagrangian for this problem is,

$$L(\theta, \lambda) = \frac{1}{2} \|\theta - \theta^{(i-1)}\|^2 + \lambda \ell^{(i)}(\theta), \quad [\text{B.14}]$$

Holding  $\lambda$  constant, we can solve for  $\theta$  by differentiating,

$$\nabla_{\theta} L = \theta - \theta^{(i-1)} + \lambda \frac{\partial}{\partial \theta} \ell^{(i)}(\theta) \quad [\text{B.15}]$$

$$\theta^* = \theta^{(i-1)} + \lambda \delta, \quad [\text{B.16}]$$

where  $\delta = f(x^{(i)}, y^{(i)}) - f(x^{(i)}, \hat{y})$  and  $\hat{y} = \operatorname{argmax}_{y \neq y^{(i)}} \theta \cdot f(x^{(i)}, y)$ .

The Lagrange multiplier  $\lambda$  acts as the learning rate in a perceptron-style update to  $\theta$ . We can solve for  $\lambda$  by plugging  $\theta^*$  back into the Lagrangian, obtaining the dual function,

$$D(\lambda) = \frac{1}{2} \|\theta^{(i-1)} + \lambda \delta - \theta^{(i-1)}\|^2 + \lambda(1 - (\theta^{(i-1)} + \lambda \delta) \cdot \delta) \quad [\text{B.17}]$$

$$= \frac{\lambda^2}{2} \|\delta\|^2 - \lambda^2 \|\delta\|^2 + \lambda(1 - \theta^{(i-1)} \cdot \delta) \quad [\text{B.18}]$$

$$= -\frac{\lambda^2}{2} \|\delta\|^2 + \lambda \ell^{(i)}(\theta^{(i-1)}). \quad [\text{B.19}]$$

Differentiating and solving for  $\lambda$ ,

$$\frac{\partial D}{\partial \lambda} = -\lambda \|\delta\|^2 + \ell^{(i)}(\theta^{(i-1)}) \quad [\text{B.20}]$$

$$\lambda^* = \frac{\ell^{(i)}(\theta^{(i-1)})}{\|\delta\|^2}. \quad [\text{B.21}]$$

The complete update equation is therefore:

$$\theta^* = \theta^{(i-1)} + \frac{\ell^{(i)}(\theta^{(i-1)})}{\|f(x^{(i)}, y^{(i)}) - f(x^{(i)}, \hat{y})\|^2} (f(x^{(i)}, y^{(i)}) - f(x^{(i)}, \hat{y})). \quad [\text{B.22}]$$

This update has strong intuitive support. The numerator of the learning rate grows with the loss. The denominator grows with the norm of the difference between the feature vectors associated with the correct and predicted label. If this norm is large, then the step with respect to each feature should be small, and vice versa.

10912 

# Bibliography

- 10913 Abadi, M., A. Agarwal, P. Barham, E. Brevdo, Z. Chen, C. Citro, G. S. Corrado, A. Davis,  
10914 J. Dean, M. Devin, S. Ghemawat, I. J. Goodfellow, A. Harp, G. Irving, M. Isard, Y. Jia,  
10915 R. Józefowicz, L. Kaiser, M. Kudlur, J. Levenberg, D. Mané, R. Monga, S. Moore,  
10916 D. G. Murray, C. Olah, M. Schuster, J. Shlens, B. Steiner, I. Sutskever, K. Talwar, P. A.  
10917 Tucker, V. Vanhoucke, V. Vasudevan, F. B. Viégas, O. Vinyals, P. Warden, M. Watten-  
10918 berg, M. Wicke, Y. Yu, and X. Zheng (2016). Tensorflow: Large-scale machine learning  
10919 on heterogeneous distributed systems. *CoRR abs/1603.04467*.
- 10920 Abend, O. and A. Rappoport (2017). The state of the art in semantic representation. In  
10921 *Proceedings of the Association for Computational Linguistics (ACL)*.
- 10922 Abney, S., R. E. Schapire, and Y. Singer (1999). Boosting applied to tagging and PP attach-  
10923 ment. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp.  
10924 132–134.
- 10925 Abney, S. P. (1987). *The English noun phrase in its sentential aspect*. Ph. D. thesis, Mas-  
10926 sachusetts Institute of Technology.
- 10927 Abney, S. P. and M. Johnson (1991). Memory requirements and local ambiguities of pars-  
10928 ing strategies. *Journal of Psycholinguistic Research* 20(3), 233–250.
- 10929 Adafre, S. F. and M. De Rijke (2006). Finding similar sentences across multiple languages  
10930 in wikipedia. In *Proceedings of the Workshop on NEW TEXT Wikis and blogs and other*  
10931 *dynamic text sources*.
- 10932 Ahn, D. (2006). The stages of event extraction. In *Proceedings of the Workshop on Annotating*  
10933 *and Reasoning about Time and Events*, pp. 1–8. Association for Computational Linguistics.
- 10934 Aho, A. V., M. S. Lam, R. Sethi, and J. D. Ullman (2006). Compilers: Principles, techniques,  
10935 & tools.
- 10936 Aikhenvald, A. Y. (2004). *Evidentiality*. Oxford University Press.

- 10937 Akaike, H. (1974). A new look at the statistical model identification. *IEEE Transactions on  
10938 Automatic Control* 19(6), 716–723.
- 10939 Akmajian, A., R. A. Demers, A. K. Farmer, and R. M. Harnish (2010). *Linguistics: An  
10940 introduction to language and communication* (Sixth ed.). Cambridge, MA: MIT press.
- 10941 Alfau, F. (1999). *Chromos*. Dalkey Archive Press.
- 10942 Allauzen, C., M. Riley, J. Schalkwyk, W. Skut, and M. Mohri (2007). OpenFst: A gen-  
10943 eral and efficient weighted finite-state transducer library. In *International Conference on  
10944 Implementation and Application of Automata*, pp. 11–23. Springer.
- 10945 Allen, J. F. (1984). Towards a general theory of action and time. *Artificial intelligence* 23(2),  
10946 123–154.
- 10947 Allen, J. F., B. W. Miller, E. K. Ringger, and T. Sikorski (1996). A robust system for natural  
10948 spoken dialogue. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp.  
10949 62–70.
- 10950 Allen, J. F., L. K. Schubert, G. Ferguson, P. Heeman, C. H. Hwang, T. Kato, M. Light,  
10951 N. Martin, B. Miller, M. Poesio, and D. Traum (1995). The TRAINS project: A case  
10952 study in building a conversational planning agent. *Journal of Experimental & Theoretical  
10953 Artificial Intelligence* 7(1), 7–48.
- 10954 Alm, C. O., D. Roth, and R. Sproat (2005). Emotions from text: machine learning for  
10955 text-based emotion prediction. In *Proceedings of Empirical Methods for Natural Language  
10956 Processing (EMNLP)*, pp. 579–586.
- 10957 Aluísio, S., J. Pelizzoni, A. Marchi, L. de Oliveira, R. Manenti, and V. Marquiafável (2003).  
10958 An account of the challenge of tagging a reference corpus for Brazilian Portuguese.  
10959 *Computational Processing of the Portuguese Language*, 194–194.
- 10960 Anand, P., M. Walker, R. Abbott, J. E. Fox Tree, R. Bowman, and M. Minor (2011). Cats rule  
10961 and dogs drool!: Classifying stance in online debate. In *Proceedings of the 2nd Workshop  
10962 on Computational Approaches to Subjectivity and Sentiment Analysis*, Portland, Oregon, pp.  
10963 1–9. Association for Computational Linguistics.
- 10964 Anandkumar, A. and R. Ge (2016). Efficient approaches for escaping higher order saddle  
10965 points in non-convex optimization. In *Proceedings of the Conference On Learning Theory  
10966 (COLT)*, pp. 81–102.
- 10967 Anandkumar, A., R. Ge, D. Hsu, S. M. Kakade, and M. Telgarsky (2014). Tensor decompo-  
10968 sitions for learning latent variable models. *The Journal of Machine Learning Research* 15(1),  
10969 2773–2832.

- 10970 Ando, R. K. and T. Zhang (2005). A framework for learning predictive structures from  
10971 multiple tasks and unlabeled data. *The Journal of Machine Learning Research* 6, 1817–  
10972 1853.
- 10973 Andor, D., C. Alberti, D. Weiss, A. Severyn, A. Presta, K. Ganchev, S. Petrov, and  
10974 M. Collins (2016). Globally normalized transition-based neural networks. In *Proceedings*  
10975 of the Association for Computational Linguistics (ACL), pp. 2442–2452.
- 10976 Angeli, G., P. Liang, and D. Klein (2010). A simple domain-independent probabilistic ap-  
10977 proach to generation. In *Proceedings of Empirical Methods for Natural Language Processing*  
10978 (EMNLP), pp. 502–512.
- 10979 Antol, S., A. Agrawal, J. Lu, M. Mitchell, D. Batra, C. Lawrence Zitnick, and D. Parikh  
10980 (2015). Vqa: Visual question answering. In *Proceedings of the International Conference on*  
10981 *Computer Vision (ICCV)*, pp. 2425–2433.
- 10982 Aronoff, M. (1976). *Word formation in generative grammar*. MIT Press.
- 10983 Arora, S. and B. Barak (2009). *Computational complexity: a modern approach*. Cambridge  
10984 University Press.
- 10985 Arora, S., R. Ge, Y. Halpern, D. Mimmo, A. Moitra, D. Sontag, Y. Wu, and M. Zhu (2013).  
10986 A practical algorithm for topic modeling with provable guarantees. In *Proceedings of the*  
10987 *International Conference on Machine Learning (ICML)*, pp. 280–288.
- 10988 Arora, S., Y. Li, Y. Liang, T. Ma, and A. Risteski (2016). Linear algebraic structure of word  
10989 senses, with applications to polysemy. *arXiv preprint arXiv:1601.03764*.
- 10990 Artstein, R. and M. Poesio (2008). Inter-coder agreement for computational linguistics.  
10991 *Computational Linguistics* 34(4), 555–596.
- 10992 Artzi, Y. and L. Zettlemoyer (2013). Weakly supervised learning of semantic parsers for  
10993 mapping instructions to actions. *Transactions of the Association for Computational Linguis-*  
10994 *tics* 1, 49–62.
- 10995 Attardi, G. (2006). Experiments with a multilanguage non-projective dependency parser.  
10996 In *Proceedings of the Conference on Natural Language Learning (CoNLL)*, pp. 166–170.
- 10997 Auer, P. (2013). *Code-switching in conversation: Language, interaction and identity*. Routledge.
- 10998 Auer, S., C. Bizer, G. Kobilarov, J. Lehmann, R. Cyganiak, and Z. Ives (2007). Dbpedia: A  
10999 nucleus for a web of open data. *The semantic web*, 722–735.
- 11000 Austin, J. L. (1962). *How to do things with words*. Oxford University Press.

- 11001 Aw, A., M. Zhang, J. Xiao, and J. Su (2006). A phrase-based statistical model for SMS text  
 11002 normalization. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp.  
 11003 33–40.
- 11004 Ba, J. L., J. R. Kiros, and G. E. Hinton (2016). Layer normalization. *arXiv preprint arXiv:1607.06450*.
- 11006 Bagga, A. and B. Baldwin (1998a). Algorithms for scoring coreference chains. In *Proceedings of the Language Resources and Evaluation Conference*, pp. 563–566.
- 11008 Bagga, A. and B. Baldwin (1998b). Entity-based cross-document coreferencing using the  
 11009 vector space model. In *Proceedings of the International Conference on Computational Lin-  
 11010 guistics (COLING)*, pp. 79–85.
- 11011 Bahdanau, D., K. Cho, and Y. Bengio (2014). Neural machine translation by jointly learn-  
 11012 ing to align and translate. In *Neural Information Processing Systems (NIPS)*.
- 11013 Baldwin, T. and S. N. Kim (2010). Multiword expressions. In *Handbook of natural language  
 11014 processing*, Volume 2, pp. 267–292. Boca Raton, USA: CRC Press.
- 11015 Balle, B., A. Quattoni, and X. Carreras (2011). A spectral learning algorithm for finite state  
 11016 transducers. In *Proceedings of the European Conference on Machine Learning and Principles  
 11017 and Practice of Knowledge Discovery in Databases (ECML)*, pp. 156–171.
- 11018 Banarescu, L., C. Bonial, S. Cai, M. Georgescu, K. Griffitt, U. Hermjakob, K. Knight,  
 11019 P. Koehn, M. Palmer, and N. Schneider (2013, August). Abstract meaning represen-  
 11020 tation for sembanking. In *Proceedings of the 7th Linguistic Annotation Workshop and Interoperability  
 11021 with Discourse*, Sofia, Bulgaria, pp. 178–186. Association for Computational  
 11022 Linguistics.
- 11023 Banko, M., M. J. Cafarella, S. Soderland, M. Broadhead, and O. Etzioni (2007). Open  
 11024 information extraction from the web. In *Proceedings of the International Joint Conference  
 11025 on Artificial Intelligence (IJCAI)*, pp. 2670–2676.
- 11026 Bansal, N., A. Blum, and S. Chawla (2004). Correlation clustering. *Machine Learning* 56(1–  
 11027 3), 89–113.
- 11028 Barber, D. (2012). *Bayesian reasoning and machine learning*. Cambridge University Press.
- 11029 Barman, U., A. Das, J. Wagner, and J. Foster (2014, October). Code mixing: A challenge for  
 11030 language identification in the language of social media. In *Proceedings of the First Work-  
 11031 shop on Computational Approaches to Code Switching*, Doha, Qatar, pp. 13–23. Association  
 11032 for Computational Linguistics.

- 11033 Barnickel, T., J. Weston, R. Collobert, H.-W. Mewes, and V. Stümpflen (2009). Large scale  
11034 application of neural network based semantic role labeling for automated relation ex-  
11035 traction from biomedical texts. *PLoS One* 4(7), e6393.
- 11036 Baron, A. and P. Rayson (2008). Vard2: A tool for dealing with spelling variation in his-  
11037 torical corpora. In *Postgraduate conference in corpus linguistics*.
- 11038 Baroni, M., R. Bernardi, and R. Zamparelli (2014). Frege in space: A program for compo-  
11039 sitional distributional semantics. *Linguistic Issues in Language Technologies*.
- 11040 Barzilay, R. and M. Lapata (2008, mar). Modeling local coherence: An Entity-Based ap-  
11041 proach. *Computational Linguistics* 34(1), 1–34.
- 11042 Barzilay, R. and K. R. McKeown (2005). Sentence fusion for multidocument news summa-  
11043 rization. *Computational Linguistics* 31(3), 297–328.
- 11044 Beesley, K. R. and L. Karttunen (2003). *Finite-state morphology*. Stanford, CA: Center for  
11045 the Study of Language and Information.
- 11046 Bejan, C. A. and S. Harabagiu (2014). Unsupervised event coreference resolution. *Compu-*  
11047 *tational Linguistics* 40(2), 311–347.
- 11048 Bell, E. T. (1934). Exponential numbers. *The American Mathematical Monthly* 41(7), 411–419.
- 11049 Bender, E. M. (2013, jun). *Linguistic Fundamentals for Natural Language Processing: 100*  
11050 *Essentials from Morphology and Syntax*, Volume 6 of *Synthesis Lectures on Human Language*  
11051 *Technologies*. Morgan & Claypool Publishers.
- 11052 Bengio, S., O. Vinyals, N. Jaitly, and N. Shazeer (2015). Scheduled sampling for sequence  
11053 prediction with recurrent neural networks. In *Neural Information Processing Systems*  
11054 (*NIPS*), pp. 1171–1179.
- 11055 Bengio, Y., R. Ducharme, P. Vincent, and C. Janvin (2003). A neural probabilistic language  
11056 model. *The Journal of Machine Learning Research* 3, 1137–1155.
- 11057 Bengio, Y., P. Simard, and P. Frasconi (1994). Learning long-term dependencies with gra-  
11058 dient descent is difficult. *IEEE Transactions on Neural Networks* 5(2), 157–166.
- 11059 Bengtsson, E. and D. Roth (2008). Understanding the value of features for coreference  
11060 resolution. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*,  
11061 pp. 294–303.
- 11062 Benjamini, Y. and Y. Hochberg (1995). Controlling the false discovery rate: a practical and  
11063 powerful approach to multiple testing. *Journal of the Royal Statistical Society. Series B*  
11064 (*Methodological*), 289–300.

- 11065 Berant, J., A. Chou, R. Frostig, and P. Liang (2013). Semantic parsing on freebase from  
11066 question-answer pairs. In *Proceedings of Empirical Methods for Natural Language Processing*  
11067 (*EMNLP*), pp. 1533–1544.
- 11068 Berant, J., V. Srikumar, P.-C. Chen, A. Vander Linden, B. Harding, B. Huang, P. Clark, and  
11069 C. D. Manning (2014). Modeling biological processes for reading comprehension. In  
11070 *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*.
- 11071 Berg-Kirkpatrick, T., A. Bouchard-Côté, J. DeNero, and D. Klein (2010). Painless unsuper-  
11072 vised learning with features. In *Proceedings of the North American Chapter of the Associa-*  
11073 *tion for Computational Linguistics (NAACL)*, pp. 582–590.
- 11074 Berg-Kirkpatrick, T., D. Burkett, and D. Klein (2012). An empirical investigation of sta-  
11075 tistical significance in NLP. In *Proceedings of Empirical Methods for Natural Language*  
11076 *Processing (EMNLP)*, pp. 995–1005.
- 11077 Berger, A. L., V. J. D. Pietra, and S. A. D. Pietra (1996). A maximum entropy approach to  
11078 natural language processing. *Computational linguistics* 22(1), 39–71.
- 11079 Bergsma, S., D. Lin, and R. Goebel (2008). Distributional identification of non-referential  
11080 pronouns. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 10–18.
- 11081 Bernardi, R., R. Cakici, D. Elliott, A. Erdem, E. Erdem, N. Ikizler-Cinbis, F. Keller, A. Mus-  
11082 cat, and B. Plank (2016). Automatic description generation from images: A survey of  
11083 models, datasets, and evaluation measures. *Journal of Artificial Intelligence Research* 55,  
11084 409–442.
- 11085 Bertsekas, D. P. (2012). Incremental gradient, subgradient, and proximal methods for  
11086 convex optimization: A survey. See Sra et al. (2012).
- 11087 Bhatia, P., R. Guthrie, and J. Eisenstein (2016). Morphological priors for probabilistic neu-  
11088 ral word embeddings. In *Proceedings of Empirical Methods for Natural Language Processing*  
11089 (*EMNLP*).
- 11090 Bhatia, P., Y. Ji, and J. Eisenstein (2015). Better document-level sentiment analysis from  
11091 rst discourse parsing. In *Proceedings of Empirical Methods for Natural Language Processing*  
11092 (*EMNLP*).
- 11093 Biber, D. (1991). *Variation across speech and writing*. Cambridge University Press.
- 11094 Bird, S., E. Klein, and E. Loper (2009). *Natural language processing with Python*. California:  
11095 O'Reilly Media.
- 11096 Bishop, C. M. (2006). *Pattern recognition and machine learning*. Springer.

- 11097 Björkelund, A. and P. Nugues (2011). Exploring lexicalized features for coreference reso-  
11098 lution. In *Proceedings of the Conference on Natural Language Learning (CoNLL)*, pp. 45–50.
- 11099 Blackburn, P. and J. Bos (2005). *Representation and inference for natural language: A first*  
11100 *course in computational semantics*. CSLI.
- 11101 Blei, D. M. (2012). Probabilistic topic models. *Communications of the ACM* 55(4), 77–84.
- 11102 Blei, D. M. (2014). Build, compute, critique, repeat: Data analysis with latent variable  
11103 models. *Annual Review of Statistics and Its Application* 1, 203–232.
- 11104 Blei, D. M., A. Y. Ng, and M. I. Jordan (2003). Latent dirichlet allocation. *the Journal of*  
11105 *machine Learning research* 3, 993–1022.
- 11106 Blitzer, J., M. Dredze, and F. Pereira (2007). Biographies, bollywood, boom-boxes and  
11107 blenders: Domain adaptation for sentiment classification. In *Proceedings of the Associa-*  
11108 *tion for Computational Linguistics (ACL)*, pp. 440–447.
- 11109 Blum, A. and T. Mitchell (1998). Combining labeled and unlabeled data with co-training.  
11110 In *Proceedings of the Conference On Learning Theory (COLT)*, pp. 92–100.
- 11111 Bobrow, D. G., R. M. Kaplan, M. Kay, D. A. Norman, H. Thompson, and T. Winograd  
11112 (1977). Gus, a frame-driven dialog system. *Artificial intelligence* 8(2), 155–173.
- 11113 Bochnet, B. (2010). Very high accuracy and fast dependency parsing is not a contradiction.  
11114 In *Proceedings of the International Conference on Computational Linguistics (COLING)*, pp.  
11115 89–97.
- 11116 Boitet, C. (1988). Pros and cons of the pivot and transfer approaches in multilingual ma-  
11117 chine translation. *Readings in machine translation*, 273–279.
- 11118 Bojanowski, P., E. Grave, A. Joulin, and T. Mikolov (2017). Enriching word vectors with  
11119 subword information. *Transactions of the Association for Computational Linguistics* 5, 135–  
11120 146.
- 11121 Bollacker, K., C. Evans, P. Paritosh, T. Sturge, and J. Taylor (2008). Freebase: a collabora-  
11122 tively created graph database for structuring human knowledge. In *Proceedings of the*  
11123 *ACM International Conference on Management of Data (SIGMOD)*, pp. 1247–1250. AcM.
- 11124 Bolukbasi, T., K.-W. Chang, J. Y. Zou, V. Saligrama, and A. T. Kalai (2016). Man is to  
11125 computer programmer as woman is to homemaker? debiasing word embeddings. In *Neural Information Processing Systems (NIPS)*, pp. 4349–4357.
- 11127 Bordes, A., N. Usunier, A. Garcia-Duran, J. Weston, and O. Yakhnenko (2013). Translating  
11128 embeddings for modeling multi-relational data. In *Neural Information Processing Systems*  
11129 (*NIPS*), pp. 2787–2795.

- 11130 Bordes, A., J. Weston, R. Collobert, Y. Bengio, et al. (2011). Learning structured embed-  
 11131       dings of knowledge bases. In *Proceedings of the National Conference on Artificial Intelligence*  
 11132       (AAAI), pp. 301–306.
- 11133 Borges, J. L. (1993). *Other Inquisitions 1937–1952*. University of Texas Press. Translated by  
 11134       Ruth L. C. Simms.
- 11135 Botha, J. A. and P. Blunsom (2014). Compositional morphology for word representations  
 11136       and language modelling. In *Proceedings of the International Conference on Machine Learn-*  
 11137       *ing (ICML)*.
- 11138 Bottou, L. (2012). Stochastic gradient descent tricks. In *Neural networks: Tricks of the trade*,  
 11139       pp. 421–436. Springer.
- 11140 Bottou, L., F. E. Curtis, and J. Nocedal (2016). Optimization methods for large-scale ma-  
 11141       chine learning. *arXiv preprint arXiv:1606.04838*.
- 11142 Bowman, S. R., L. Vilnis, O. Vinyals, A. Dai, R. Jozefowicz, and S. Bengio (2016). Gen-  
 11143       erating sentences from a continuous space. In *Proceedings of the Conference on Natural*  
 11144       *Language Learning (CoNLL)*, pp. 10–21.
- 11145 boyd, d. and K. Crawford (2012). Critical questions for big data. *Information, Communica-*  
 11146       *tion & Society* 15(5), 662–679.
- 11147 Boyd, S. and L. Vandenberghe (2004). *Convex Optimization*. New York: Cambridge Uni-  
 11148       versity Press.
- 11149 Branavan, S., H. Chen, J. Eisenstein, and R. Barzilay (2009). Learning document-level  
 11150       semantic properties from free-text annotations. *Journal of Artificial Intelligence Re-*  
 11151       *search* 34(2), 569–603.
- 11152 Branavan, S. R., H. Chen, L. S. Zettlemoyer, and R. Barzilay (2009). Reinforcement learning  
 11153       for mapping instructions to actions. In *Proceedings of the Association for Computational*  
 11154       *Linguistics (ACL)*, pp. 82–90.
- 11155 BRANTS, T. and A. Franz (2006). The google 1t 5-gram corpus. LDC2006T13.
- 11156 Braud, C., O. Lacroix, and A. Søgaard (2017). Does syntax help discourse segmenta-  
 11157       tion? not so much. In *Proceedings of Empirical Methods for Natural Language Processing*  
 11158       (*EMNLP*), pp. 2432–2442.
- 11159 Briscoe, T. (2011). Introduction to formal semantics for natural language.
- 11160 Brown, P. F., J. Cocke, S. A. D. Pietra, V. J. D. Pietra, F. Jelinek, J. D. Lafferty, R. L. Mercer,  
 11161       and P. S. Roossin (1990). A statistical approach to machine translation. *Computational*  
 11162       *linguistics* 16(2), 79–85.

- 11163 Brown, P. F., P. V. Desouza, R. L. Mercer, V. J. D. Pietra, and J. C. Lai (1992). Class-based  
11164 n-gram models of natural language. *Computational linguistics* 18(4), 467–479.
- 11165 Brown, P. F., V. J. D. Pietra, S. A. D. Pietra, and R. L. Mercer (1993). The mathematics  
11166 of statistical machine translation: Parameter estimation. *Computational linguistics* 19(2),  
11167 263–311.
- 11168 Brun, C. and C. Roux (2014). Décomposition des “hash tags” pour l’amélioration de la  
11169 classification en polarité des “tweets”. *Proceedings of Traitement Automatique des Langues  
11170 Naturelles*, 473–478.
- 11171 Bruni, E., N.-K. Tran, and M. Baroni (2014). Multimodal distributional semantics. *Journal  
11172 of Artificial Intelligence Research* 49(2014), 1–47.
- 11173 Bullinaria, J. A. and J. P. Levy (2007). Extracting semantic representations from word co-  
11174 occurrence statistics: A computational study. *Behavior research methods* 39(3), 510–526.
- 11175 Bunescu, R. C. and R. J. Mooney (2005). A shortest path dependency kernel for relation  
11176 extraction. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*,  
11177 pp. 724–731.
- 11178 Bunescu, R. C. and M. Pasca (2006). Using encyclopedic knowledge for named entity  
11179 disambiguation. In *Proceedings of the European Chapter of the Association for Computational  
11180 Linguistics (EACL)*, pp. 9–16.
- 11181 Burstein, J., D. Marcu, and K. Knight (2003). Finding the WRITE stuff: Automatic identi-  
11182 fication of discourse structure in student essays. *IEEE Intelligent Systems* 18(1), 32–39.
- 11183 Burstein, J., J. Tetreault, and S. Andreyev (2010). Using entity-based features to model  
11184 coherence in student essays. In *Human language technologies: The 2010 annual conference  
11185 of the North American chapter of the Association for Computational Linguistics*, pp. 681–684.  
11186 Association for Computational Linguistics.
- 11187 Burstein, J., J. Tetreault, and M. Chodorow (2013). Holistic discourse coherence annotation  
11188 for noisy essay writing. *Dialogue & Discourse* 4(2), 34–52.
- 11189 Cai, Q. and A. Yates (2013). Large-scale semantic parsing via schema matching and lexicon  
11190 extension. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 423–  
11191 433.
- 11192 Caliskan, A., J. J. Bryson, and A. Narayanan (2017). Semantics derived automatically from  
11193 language corpora contain human-like biases. *Science* 356(6334), 183–186.
- 11194 Canny, J. (1987). A computational approach to edge detection. In *Readings in Computer  
11195 Vision*, pp. 184–203. Elsevier.

- 11196 Cappé, O. and E. Moulines (2009). On-line expectation–maximization algorithm for latent  
11197 data models. *Journal of the Royal Statistical Society: Series B (Statistical Methodology)* 71(3),  
11198 593–613.
- 11199 Carbonell, J. and J. Goldstein (1998). The use of mmr, diversity-based reranking for re-  
11200 ordering documents and producing summaries. In *Proceedings of ACM SIGIR conference*  
11201 on Research and development in information retrieval, pp. 335–336.
- 11202 Carbonell, J. R. (1970). Mixed-initiative man-computer instructional dialogues. Technical  
11203 report, BOLT BERANEK AND NEWMAN INC CAMBRIDGE MASS.
- 11204 Cardie, C. and K. Wagstaff (1999). Noun phrase coreference as clustering. In *Proceedings*  
11205 of *Empirical Methods for Natural Language Processing (EMNLP)*, pp. 82–89.
- 11206 Carletta, J. (1996). Assessing agreement on classification tasks: the kappa statistic. *Com-  
11207 putational linguistics* 22(2), 249–254.
- 11208 Carletta, J. (2007). Unleashing the killer corpus: experiences in creating the multi-  
11209 everything ami meeting corpus. *Language Resources and Evaluation* 41(2), 181–190.
- 11210 Carlson, L. and D. Marcu (2001). Discourse tagging reference manual. Technical Report  
11211 ISI-TR-545, Information Sciences Institute.
- 11212 Carlson, L., M. E. Okurowski, and D. Marcu (2002). RST discourse treebank. Linguistic  
11213 Data Consortium, University of Pennsylvania.
- 11214 Carpenter, B. (1997). *Type-logical semantics*. Cambridge, MA: MIT Press.
- 11215 Carreras, X., M. Collins, and T. Koo (2008). Tag, dynamic programming, and the percep-  
11216 tron for efficient, feature-rich parsing. In *Proceedings of the Conference on Natural Language*  
11217 *Learning (CoNLL)*, pp. 9–16.
- 11218 Carreras, X. and L. Màrquez (2005). Introduction to the conll-2005 shared task: Semantic  
11219 role labeling. In *Proceedings of the Ninth Conference on Computational Natural Language*  
11220 *Learning*, pp. 152–164. Association for Computational Linguistics.
- 11221 Carroll, L. (1865). *Alice's Adventures in Wonderland*. London: Macmillan.
- 11222 Carroll, L. (1917). *Through the looking glass: And what Alice found there*. Chicago: Rand,  
11223 McNally.
- 11224 Chambers, N. and D. Jurafsky (2008). Jointly combining implicit constraints improves  
11225 temporal ordering. In *Proceedings of Empirical Methods for Natural Language Processing*  
11226 (*EMNLP*), pp. 698–706.

- 11227 Chang, K.-W., A. Krishnamurthy, A. Agarwal, H. Daume III, and J. Langford (2015).  
11228 Learning to search better than your teacher. In *Proceedings of the International Conference on Machine Learning (ICML)*.  
11229
- 11230 Chang, M.-W., L. Ratinov, and D. Roth (2007). Guiding semi-supervision with constraint-  
11231 driven learning. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp.  
11232 280–287.
- 11233 Chang, M.-W., L.-A. Ratinov, N. Rizzolo, and D. Roth (2008). Learning and inference with  
11234 constraints. In *Proceedings of the National Conference on Artificial Intelligence (AAAI)*, pp.  
11235 1513–1518.
- 11236 Chapman, W. W., W. Bridewell, P. Hanbury, G. F. Cooper, and B. G. Buchanan (2001). A  
11237 simple algorithm for identifying negated findings and diseases in discharge summaries.  
11238 *Journal of biomedical informatics* 34(5), 301–310.
- 11239 Charniak, E. (1997). Statistical techniques for natural language parsing. *AI magazine* 18(4),  
11240 33–43.
- 11241 Charniak, E. and M. Johnson (2005). Coarse-to-fine n-best parsing and maxent discriminative  
11242 reranking. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp.  
11243 173–180.
- 11244 Chelba, C. and A. Acero (2006). Adaptation of maximum entropy capitalizer: Little data  
11245 can help a lot. *Computer Speech & Language* 20(4), 382–399.
- 11246 Chelba, C., T. Mikolov, M. Schuster, Q. Ge, T. Brants, P. Koehn, and T. Robinson (2013).  
11247 One billion word benchmark for measuring progress in statistical language modeling.  
11248 *arXiv preprint arXiv:1312.3005*.
- 11249 Chen, D., J. Bolton, and C. D. Manning (2016). A thorough examination of the CNN/Daily  
11250 Mail reading comprehension task. In *Proceedings of the Association for Computational  
11251 Linguistics (ACL)*.
- 11252 Chen, D. and C. D. Manning (2014). A fast and accurate dependency parser using neural  
11253 networks. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*,  
11254 pp. 740–750.
- 11255 Chen, D. L. and R. J. Mooney (2008). Learning to sportscast: a test of grounded language  
11256 acquisition. In *Proceedings of the International Conference on Machine Learning (ICML)*, pp.  
11257 128–135.
- 11258 Chen, H., S. Branavan, R. Barzilay, and D. R. Karger (2009). Content modeling using latent  
11259 permutations. *Journal of Artificial Intelligence Research* 36(1), 129–163.

- 11260 Chen, M., Z. Xu, K. Weinberger, and F. Sha (2012). Marginalized denoising autoencoders  
11261 for domain adaptation. In *Proceedings of the International Conference on Machine Learning*  
11262 (*ICML*).
- 11263 Chen, M. X., O. Firat, A. Bapna, M. Johnson, W. Macherey, G. Foster, L. Jones, N. Parmar,  
11264 M. Schuster, Z. Chen, Y. Wu, and M. Hughes (2018). The best of both worlds: Combin-  
11265 ing recent advances in neural machine translation. In *Proceedings of the Association for*  
11266 *Computational Linguistics (ACL)*.
- 11267 Chen, S. F. and J. Goodman (1999). An empirical study of smoothing techniques for lan-  
11268 guage modeling. *Computer Speech & Language* 13(4), 359–393.
- 11269 Chen, T. and C. Guestrin (2016). Xgboost: A scalable tree boosting system. In *Proceedings*  
11270 *of Knowledge Discovery and Data Mining (KDD)*, pp. 785–794.
- 11271 Chen, X., X. Qiu, C. Zhu, P. Liu, and X. Huang (2015). Long short-term memory neural  
11272 networks for chinese word segmentation. In *Proceedings of Empirical Methods for Natural*  
11273 *Language Processing (EMNLP)*, pp. 1197–1206.
- 11274 Chen, Y., S. Gilroy, A. Malletti, K. Knight, and J. May (2018). Recurrent neural networks  
11275 as weighted language recognizers. In *Proceedings of the North American Chapter of the*  
11276 *Association for Computational Linguistics (NAACL)*.
- 11277 Chen, Z. and H. Ji (2009). Graph-based event coreference resolution. In *Proceedings of*  
11278 *the 2009 Workshop on Graph-based Methods for Natural Language Processing*, pp. 54–57.  
11279 Association for Computational Linguistics.
- 11280 Cheng, X. and D. Roth (2013). Relational inference for wikification. In *Proceedings of*  
11281 *Empirical Methods for Natural Language Processing (EMNLP)*, pp. 1787–1796.
- 11282 Chiang, D. (2007). Hierarchical phrase-based translation. *Computational Linguistics* 33(2),  
11283 201–228.
- 11284 Chiang, D., J. Graehl, K. Knight, A. Pauls, and S. Ravi (2010). Bayesian inference for  
11285 finite-state transducers. In *Proceedings of the North American Chapter of the Association for*  
11286 *Computational Linguistics (NAACL)*, pp. 447–455.
- 11287 Chinchor, N. and P. Robinson (1997). Muc-7 named entity task definition. In *Proceedings*  
11288 *of the 7th Conference on Message Understanding*, Volume 29.
- 11289 Cho, K. (2015). Natural language understanding with distributed representation.  
11290 *CoRR abs/1511.07916*.

- 11291 Cho, K., B. Van Merriënboer, C. Gulcehre, D. Bahdanau, F. Bougares, H. Schwenk, and  
11292 Y. Bengio (2014). Learning phrase representations using rnn encoder-decoder for sta-  
11293 tistical machine translation. In *Proceedings of Empirical Methods for Natural Language*  
11294 *Processing (EMNLP)*.
- 11295 Chomsky, N. (1957). *Syntactic structures*. The Hague: Mouton & Co.
- 11296 Chomsky, N. (1982). *Some concepts and consequences of the theory of government and binding*,  
11297 Volume 6. MIT press.
- 11298 Choromanska, A., M. Henaff, M. Mathieu, G. B. Arous, and Y. LeCun (2015). The loss  
11299 surfaces of multilayer networks. In *Proceedings of Artificial Intelligence and Statistics (AIS-*  
11300 *TATS*), pp. 192–204.
- 11301 Christensen, J., S. Soderland, O. Etzioni, et al. (2010). Semantic role labeling for open  
11302 information extraction. In *Proceedings of the Workshop on Formalisms and Methodology for*  
11303 *Learning by Reading*, pp. 52–60. Association for Computational Linguistics.
- 11304 Christodoulopoulos, C., S. Goldwater, and M. Steedman (2010). Two decades of unsuper-  
11305 vised pos induction: How far have we come? In *Proceedings of Empirical Methods for*  
11306 *Natural Language Processing (EMNLP)*, pp. 575–584.
- 11307 Chu, Y.-J. and T.-H. Liu (1965). On shortest arborescence of a directed graph. *Scientia*  
11308 *Sinica* 14(10), 1396–1400.
- 11309 Chung, C. and J. W. Pennebaker (2007). The psychological functions of function words.  
11310 In K. Fiedler (Ed.), *Social communication*, pp. 343–359. New York and Hove: Psychology  
11311 Press.
- 11312 Church, K. (2011). A pendulum swung too far. *Linguistic Issues in Language Technology* 6(5),  
11313 1–27.
- 11314 Church, K. W. (2000). Empirical estimates of adaptation: the chance of two Noriega-  
11315 s is closer to  $p/2$  than  $p^2$ . In *Proceedings of the International Conference on Computational*  
11316 *Linguistics (COLING)*, pp. 180–186.
- 11317 Church, K. W. and P. Hanks (1990). Word association norms, mutual information, and  
11318 lexicography. *Computational linguistics* 16(1), 22–29.
- 11319 Ciaramita, M. and M. Johnson (2003). Supersense tagging of unknown nouns in wordnet.  
11320 In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 168–  
11321 175.
- 11322 Clark, K. and C. D. Manning (2015). Entity-centric coreference resolution with model  
11323 stacking. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 1405–  
11324 1415.

- 11325 Clark, K. and C. D. Manning (2016). Improving coreference resolution by learning entity-  
 11326 level distributed representations. In *Proceedings of the Association for Computational Lin-*  
 11327 *guistics (ACL)*.
- 11328 Clark, P. (2015). Elementary school science and math tests as a driver for ai: take the aristo  
 11329 challenge! In *Proceedings of the National Conference on Artificial Intelligence (AAAI)*, pp.  
 11330 4019–4021.
- 11331 Clarke, J., D. Goldwasser, M.-W. Chang, and D. Roth (2010). Driving semantic parsing  
 11332 from the world’s response. In *Proceedings of the Conference on Natural Language Learning*  
 11333 (*CoNLL*), pp. 18–27.
- 11334 Clarke, J. and M. Lapata (2008). Global inference for sentence compression: An integer  
 11335 linear programming approach. *Journal of Artificial Intelligence Research* 31, 399–429.
- 11336 Cohen, J. (1960). A coefficient of agreement for nominal scales. *Educational and psychologi-*  
 11337 *cal measurement* 20(1), 37–46.
- 11338 Cohen, S. (2016). *Bayesian analysis in natural language processing*. Synthesis Lectures on  
 11339 Human Language Technologies. San Rafael, CA: Morgan & Claypool Publishers.
- 11340 Collier, N., C. Nobata, and J.-i. Tsujii (2000). Extracting the names of genes and gene  
 11341 products with a hidden markov model. In *Proceedings of the International Conference on*  
 11342 *Computational Linguistics (COLING)*, pp. 201–207.
- 11343 Collins, M. (1997). Three generative, lexicalised models for statistical parsing. In *Proceed-*  
 11344 *ings of the Association for Computational Linguistics (ACL)*, pp. 16–23.
- 11345 Collins, M. (2002). Discriminative training methods for hidden markov models: theory  
 11346 and experiments with perceptron algorithms. In *Proceedings of Empirical Methods for*  
 11347 *Natural Language Processing (EMNLP)*, pp. 1–8.
- 11348 Collins, M. (2013). Notes on natural language processing. <http://www.cs.columbia.edu/~mcollins/notes-spring2013.html>.
- 11350 Collins, M. and T. Koo (2005). Discriminative reranking for natural language parsing.  
 11351 *Computational Linguistics* 31(1), 25–70.
- 11352 Collins, M. and B. Roark (2004). Incremental parsing with the perceptron algorithm. In  
 11353 *Proceedings of the 42nd Annual Meeting on Association for Computational Linguistics*, pp.  
 11354 111. Association for Computational Linguistics.
- 11355 Collobert, R., K. Kavukcuoglu, and C. Farabet (2011). Torch7: A matlab-like environment  
 11356 for machine learning. Technical Report EPFL-CONF-192376, EPFL.

- 11357 Collobert, R. and J. Weston (2008). A unified architecture for natural language processing:  
11358 Deep neural networks with multitask learning. In *Proceedings of the International  
11359 Conference on Machine Learning (ICML)*, pp. 160–167.
- 11360 Collobert, R., J. Weston, L. Bottou, M. Karlen, K. Kavukcuoglu, and P. Kuksa (2011). Natural  
11361 language processing (almost) from scratch. *Journal of Machine Learning Research* 12,  
11362 2493–2537.
- 11363 Colton, S., J. Goodwin, and T. Veale (2012). Full-face poetry generation. In *Proceedings of  
11364 the International Conference on Computational Creativity*, pp. 95–102.
- 11365 Conneau, A., D. Kiela, H. Schwenk, L. Barrault, and A. Bordes (2017). Supervised learning  
11366 of universal sentence representations from natural language inference data. In *Proceed-  
11367 ings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 681–691.
- 11368 Cormen, T. H., C. E. Leiserson, R. L. Rivest, and C. Stein (2009). *Introduction to algorithms*  
11369 (third ed.). MIT press.
- 11370 Cotterell, R., H. Schütze, and J. Eisner (2016). Morphological smoothing and extrapolation  
11371 of word embeddings. In *Proceedings of the Association for Computational Linguistics (ACL)*,  
11372 pp. 1651–1660.
- 11373 Covello, L., Y. Sohn, A. D. Kramer, C. Marlow, M. Franceschetti, N. A. Christakis, and  
11374 J. H. Fowler (2014). Detecting emotional contagion in massive social networks. *PLoS  
11375 one* 9(3), e90315.
- 11376 Covington, M. A. (2001). A fundamental algorithm for dependency parsing. In *Proceedings  
11377 of the 39th annual ACM southeast conference*, pp. 95–102.
- 11378 Crammer, K., O. Dekel, J. Keshet, S. Shalev-Shwartz, and Y. Singer (2006, December).  
11379 Online passive-aggressive algorithms. *The Journal of Machine Learning Research* 7, 551–  
11380 585.
- 11381 Crammer, K. and Y. Singer (2001). Pranking with ranking. In *Neural Information Processing  
11382 Systems (NIPS)*, pp. 641–647.
- 11383 Creutz, M. and K. Lagus (2007). Unsupervised models for morpheme segmentation and  
11384 morphology learning. *ACM Transactions on Speech and Language Processing (TSLP)* 4(1),  
11385 3.
- 11386 Cross, J. and L. Huang (2016). Span-based constituency parsing with a structure-label  
11387 system and provably optimal dynamic oracles. In *Proceedings of Empirical Methods for  
11388 Natural Language Processing (EMNLP)*, pp. 1–11.

- 11389 Cucerzan, S. (2007). Large-scale named entity disambiguation based on wikipedia data.  
 11390 In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*.
- 11391 Cui, H., R. Sun, K. Li, M.-Y. Kan, and T.-S. Chua (2005). Question answering passage  
 11392 retrieval using dependency relations. In *Proceedings of the 28th annual international ACM*  
 11393 *SIGIR conference on Research and development in information retrieval*, pp. 400–407. ACM.
- 11394 Cui, Y., Z. Chen, S. Wei, S. Wang, T. Liu, and G. Hu (2017). Attention-over-attention neural  
 11395 networks for reading comprehension. In *Proceedings of the Association for Computational*  
 11396 *Linguistics (ACL)*.
- 11397 Culotta, A. and J. Sorensen (2004). Dependency tree kernels for relation extraction. In  
 11398 *Proceedings of the Association for Computational Linguistics (ACL)*.
- 11399 Culotta, A., M. Wick, and A. McCallum (2007). First-order probabilistic models for coref-  
 11400 erence resolution. In *Proceedings of the North American Chapter of the Association for Com-*  
 11401 *putational Linguistics (NAACL)*, pp. 81–88.
- 11402 Curry, H. B. and R. Feys (1958). *Combinatory Logic*, Volume I. Amsterdam: North Holland.
- 11403 Danescu-Niculescu-Mizil, C., M. Sudhof, D. Jurafsky, J. Leskovec, and C. Potts (2013). A  
 11404 computational approach to politeness with application to social factors. In *Proceedings*  
 11405 *of the Association for Computational Linguistics (ACL)*, pp. 250–259.
- 11406 Das, D., D. Chen, A. F. Martins, N. Schneider, and N. A. Smith (2014). Frame-semantic  
 11407 parsing. *Computational Linguistics* 40(1), 9–56.
- 11408 Daumé III, H. (2007). Frustratingly easy domain adaptation. In *Proceedings of the Associa-*  
 11409 *tion for Computational Linguistics (ACL)*.
- 11410 Daumé III, H., J. Langford, and D. Marcu (2009). Search-based structured prediction.  
 11411 *Machine learning* 75(3), 297–325.
- 11412 Daumé III, H. and D. Marcu (2005). A large-scale exploration of effective global features  
 11413 for a joint entity detection and tracking model. In *Proceedings of Empirical Methods for*  
 11414 *Natural Language Processing (EMNLP)*, pp. 97–104.
- 11415 Dauphin, Y. N., R. Pascanu, C. Gulcehre, K. Cho, S. Ganguli, and Y. Bengio (2014). Iden-  
 11416 tifying and attacking the saddle point problem in high-dimensional non-convex opti-  
 11417 mization. In *Neural Information Processing Systems (NIPS)*, pp. 2933–2941.
- 11418 Davidson, D. (1967). The logical form of action sentences. In N. Rescher (Ed.), *The Logic of*  
 11419 *Decision and Action*. Pittsburgh: University of Pittsburgh Press.

- 11420 De Gispert, A. and J. B. Marino (2006). Catalan-english statistical machine translation  
11421 without parallel corpus: bridging through spanish. In *Proc. of 5th International Conference*  
11422 *on Language Resources and Evaluation (LREC)*, pp. 65–68. Citeseer.
- 11423 De Marneffe, M.-C. and C. D. Manning (2008). The stanford typed dependencies represen-  
11424 tation. In *Coling 2008: Proceedings of the workshop on Cross-Framework and Cross-Domain*  
11425 *Parser Evaluation*, pp. 1–8. Association for Computational Linguistics.
- 11426 Dean, J. and S. Ghemawat (2008). Mapreduce: simplified data processing on large clusters.  
11427 *Communications of the ACM* 51(1), 107–113.
- 11428 Deerwester, S. C., S. T. Dumais, T. K. Landauer, G. W. Furnas, and R. A. Harshman (1990).  
11429 Indexing by latent semantic analysis. *JASIS* 41(6), 391–407.
- 11430 Dehdari, J. (2014). *A Neurophysiologically-Inspired Statistical Language Model*. Ph. D. thesis,  
11431 The Ohio State University.
- 11432 Deisenroth, M. P., A. A. Faisal, and C. S. Ong (2018). *Mathematics For Machine Learning*.  
11433 Cambridge UP.
- 11434 Dempster, A. P., N. M. Laird, and D. B. Rubin (1977). Maximum likelihood from incom-  
11435 plete data via the em algorithm. *Journal of the Royal Statistical Society. Series B (Methodo-*  
11436 *logical)*, 1–38.
- 11437 Denis, P. and J. Baldridge (2007). A ranking approach to pronoun resolution. In *IJCAI*.
- 11438 Denis, P. and J. Baldridge (2008). Specialized models and ranking for coreference resolu-  
11439 tion. In *Proceedings of the Conference on Empirical Methods in Natural Language Processing*,  
11440 EMNLP '08, Stroudsburg, PA, USA, pp. 660–669. Association for Computational Lin-  
11441 guistics.
- 11442 Denis, P. and J. Baldridge (2009). Global joint models for coreference resolution and named  
11443 entity classification. *Procesamiento del Lenguaje Natural* 42.
- 11444 Derrida, J. (1985). Des tours de babel. In J. Graham (Ed.), *Difference in translation*. Ithaca,  
11445 NY: Cornell University Press.
- 11446 Dhingra, B., H. Liu, Z. Yang, W. W. Cohen, and R. Salakhutdinov (2017). Gated-attention  
11447 readers for text comprehension. In *Proceedings of the Association for Computational Lin-*  
11448 *guistics (ACL)*.
- 11449 Diaconis, P. and B. Skyrms (2017). *Ten Great Ideas About Chance*. Princeton University  
11450 Press.
- 11451 Dietterich, T. G. (1998). Approximate statistical tests for comparing supervised classifica-  
11452 tion learning algorithms. *Neural computation* 10(7), 1895–1923.

- 11453 Dietterich, T. G., R. H. Lathrop, and T. Lozano-Pérez (1997). Solving the multiple instance  
11454 problem with axis-parallel rectangles. *Artificial intelligence* 89(1), 31–71.
- 11455 Dimitrova, L., N. Ide, V. Petkevic, T. Erjavec, H. J. Kaalep, and D. Tufis (1998). Multext-  
11456 east: Parallel and comparable corpora and lexicons for six central and eastern european  
11457 languages. In *Proceedings of the 17th international conference on Computational linguistics-*  
11458 *Volume 1*, pp. 315–319. Association for Computational Linguistics.
- 11459 Doddington, G. R., A. Mitchell, M. A. Przybocki, L. A. Ramshaw, S. Strassel, and R. M.  
11460 Weischedel (2004). The automatic content extraction (ace) program-tasks, data, and  
11461 evaluation. In *Proceedings of the Language Resources and Evaluation Conference*, pp. 837–  
11462 840.
- 11463 dos Santos, C., B. Xiang, and B. Zhou (2015). Classifying relations by ranking with con-  
11464 volutional neural networks. In *Proceedings of the Association for Computational Linguistics*  
11465 (*ACL*), pp. 626–634.
- 11466 Dowty, D. (1991). Thematic proto-roles and argument selection. *Language*, 547–619.
- 11467 Dredze, M., P. McNamee, D. Rao, A. Gerber, and T. Finin (2010). Entity disambiguation  
11468 for knowledge base population. In *Proceedings of the 23rd International Conference on*  
11469 *Computational Linguistics*, pp. 277–285. Association for Computational Linguistics.
- 11470 Dredze, M., M. J. Paul, S. Bergsma, and H. Tran (2013). Carmen: A Twitter geolocation  
11471 system with applications to public health. In *AAAI workshop on expanding the boundaries*  
11472 *of health informatics using AI (HIAI)*, pp. 20–24.
- 11473 Dreyfus, H. L. (1992). *What computers still can't do: a critique of artificial reason*. MIT press.
- 11474 Du, L., W. Buntine, and M. Johnson (2013). Topic segmentation with a structured topic  
11475 model. In *Proceedings of the North American Chapter of the Association for Computational*  
11476 *Linguistics (NAACL)*, pp. 190–200.
- 11477 Duchi, J., E. Hazan, and Y. Singer (2011). Adaptive subgradient methods for online learn-  
11478 ing and stochastic optimization. *The Journal of Machine Learning Research* 12, 2121–2159.
- 11479 Dunietz, J., L. Levin, and J. Carbonell (2017). The because corpus 2.0: Annotating causality  
11480 and overlapping relations. In *Proceedings of the Linguistic Annotation Workshop*.
- 11481 Durrett, G., T. Berg-Kirkpatrick, and D. Klein (2016). Learning-based single-document  
11482 summarization with compression and anaphoricity constraints. In *Proceedings of the*  
11483 *Association for Computational Linguistics (ACL)*, pp. 1998–2008.
- 11484 Durrett, G. and D. Klein (2013). Easy victories and uphill battles in coreference resolution.  
11485 In *Proceedings of the Conference on Empirical Methods in Natural Language Processing*.

- 11486 Durrett, G. and D. Klein (2015). Neural crf parsing. In *Proceedings of the Association for  
11487 Computational Linguistics (ACL)*.
- 11488 Dyer, C., M. Ballesteros, W. Ling, A. Matthews, and N. A. Smith (2015). Transition-based  
11489 dependency parsing with stack long short-term memory. In *Proceedings of the Association  
11490 for Computational Linguistics (ACL)*, pp. 334–343.
- 11491 Dyer, C., A. Kuncoro, M. Ballesteros, and N. A. Smith (2016). Recurrent neural network  
11492 grammars. In *Proceedings of the North American Chapter of the Association for Computational  
11493 Linguistics (NAACL)*, pp. 199–209.
- 11494 Edmonds, J. (1967). Optimum branchings. *Journal of Research of the National Bureau of  
11495 Standards B* 71(4), 233–240.
- 11496 Efron, B. and R. J. Tibshirani (1993). An introduction to the bootstrap: Monographs on  
11497 statistics and applied probability, vol. 57. *New York and London: Chapman and Hall/CRC*.
- 11498 Eisenstein, J. (2009). Hierarchical text segmentation from multi-scale lexical cohesion. In  
11499 *Proceedings of the North American Chapter of the Association for Computational Linguistics  
11500 (NAACL)*.
- 11501 Eisenstein, J. and R. Barzilay (2008). Bayesian unsupervised topic segmentation. In *Pro-  
11502 ceedings of Empirical Methods for Natural Language Processing (EMNLP)*.
- 11503 Eisner, J. (1997). State-of-the-art algorithms for minimum spanning trees: A tutorial dis-  
11504 cussion.
- 11505 Eisner, J. (2000). Bilexical grammars and their cubic-time parsing algorithms. In *Advances  
11506 in probabilistic and other parsing technologies*, pp. 29–61. Springer.
- 11507 Eisner, J. (2002). Parameter estimation for probabilistic finite-state transducers. In *Proceed-  
11508 ings of the Association for Computational Linguistics (ACL)*, pp. 1–8.
- 11509 Eisner, J. (2016). Inside-outside and forward-backward algorithms are just backprop. In  
11510 *Proceedings of the Workshop on Structured Prediction for NLP*, pp. 1–17.
- 11511 Eisner, J. M. (1996). Three new probabilistic models for dependency parsing: An explo-  
11512 ration. In *Proceedings of the International Conference on Computational Linguistics (COL-  
11513 ING)*, pp. 340–345.
- 11514 Ekman, P. (1992). Are there basic emotions? *Psychological Review* 99(3), 550–553.
- 11515 Elman, J. L. (1990). Finding structure in time. *Cognitive science* 14(2), 179–211.

- 11516 Elman, J. L., E. A. Bates, M. H. Johnson, A. Karmiloff-Smith, D. Parisi, and K. Plunkett  
11517 (1998). *Rethinking innateness: A connectionist perspective on development*, Volume 10. MIT  
11518 press.
- 11519 Elsner, M. and E. Charniak (2010). Disentangling chat. *Computational Linguistics* 36(3),  
11520 389–409.
- 11521 Esuli, A. and F. Sebastiani (2006). Sentiwordnet: A publicly available lexical resource for  
11522 opinion mining. In *LREC*, Volume 6, pp. 417–422. Citeseer.
- 11523 Etzioni, O., A. Fader, J. Christensen, S. Soderland, and M. Mausam (2011). Open informa-  
11524 tion extraction: The second generation. In *Proceedings of the International Joint Conference*  
11525 on *Artificial Intelligence (IJCAI)*, pp. 3–10.
- 11526 Faruqui, M., J. Dodge, S. K. Jauhar, C. Dyer, E. Hovy, and N. A. Smith (2015). Retrofitting  
11527 word vectors to semantic lexicons. In *Proceedings of the North American Chapter of the*  
11528 *Association for Computational Linguistics (NAACL)*.
- 11529 Faruqui, M. and C. Dyer (2014). Improving vector space word representations using mul-  
11530 tilingual correlation. In *Proceedings of the European Chapter of the Association for Compu-*  
11531 *tational Linguistics (EACL)*, pp. 462–471.
- 11532 Faruqui, M., R. McDonald, and R. Soricut (2016). Morpho-syntactic lexicon generation  
11533 using graph-based semi-supervised learning. *Transactions of the Association for Compu-*  
11534 *tational Linguistics* 4, 1–16.
- 11535 Faruqui, M., Y. Tsvetkov, P. Rastogi, and C. Dyer (2016, August). Problems with evaluation  
11536 of word embeddings using word similarity tasks. In *Proceedings of the 1st Workshop on*  
11537 *Evaluating Vector-Space Representations for NLP*, Berlin, Germany, pp. 30–35. Association  
11538 for Computational Linguistics.
- 11539 Fellbaum, C. (2010). *WordNet*. Springer.
- 11540 Feng, V. W., Z. Lin, and G. Hirst (2014). The impact of deep hierarchical discourse struc-  
11541 tures in the evaluation of text coherence. In *Proceedings of the International Conference on*  
11542 *Computational Linguistics (COLING)*, pp. 940–949.
- 11543 Feng, X., L. Huang, D. Tang, H. Ji, B. Qin, and T. Liu (2016). A language-independent  
11544 neural network for event detection. In *Proceedings of the Association for Computational*  
11545 *Linguistics (ACL)*, pp. 66–71.
- 11546 Fernandes, E. R., C. N. dos Santos, and R. L. Milidiú (2014). Latent trees for coreference  
11547 resolution. *Computational Linguistics*.

- 11548 Ferrucci, D., E. Brown, J. Chu-Carroll, J. Fan, D. Gondek, A. A. Kalyanpur, A. Lally, J. W.  
11549 Murdock, E. Nyberg, J. Prager, et al. (2010). Building Watson: An overview of the  
11550 DeepQA project. *AI magazine* 31(3), 59–79.
- 11551 Ficler, J. and Y. Goldberg (2017, September). Controlling linguistic style aspects in neural  
11552 language generation. In *Proceedings of the Workshop on Stylistic Variation*, Copenhagen,  
11553 Denmark, pp. 94–104. Association for Computational Linguistics.
- 11554 Filippova, K. and M. Strube (2008). Sentence fusion via dependency graph compression.  
11555 In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 177–  
11556 185.
- 11557 Fillmore, C. J. (1968). The case for case. In E. Bach and R. Harms (Eds.), *Universals in  
11558 linguistic theory*. Holt, Rinehart, and Winston.
- 11559 Fillmore, C. J. (1976). Frame semantics and the nature of language. *Annals of the New York  
11560 Academy of Sciences* 280(1), 20–32.
- 11561 Fillmore, C. J. and C. Baker (2009). A frames approach to semantic analysis. In *The Oxford  
11562 Handbook of Linguistic Analysis*. Oxford University Press.
- 11563 Finkel, J. R., T. Grenager, and C. Manning (2005). Incorporating non-local information  
11564 into information extraction systems by gibbs sampling. In *Proceedings of the Association  
11565 for Computational Linguistics (ACL)*, pp. 363–370.
- 11566 Finkel, J. R., T. Grenager, and C. D. Manning (2007). The infinite tree. In *Proceedings of the  
11567 Association for Computational Linguistics (ACL)*, pp. 272–279.
- 11568 Finkel, J. R., A. Kleeman, and C. D. Manning (2008). Efficient, feature-based, conditional  
11569 random field parsing. In *Proceedings of the Association for Computational Linguistics (ACL)*,  
11570 pp. 959–967.
- 11571 Finkel, J. R. and C. Manning (2009). Hierarchical bayesian domain adaptation. In *Proceed-  
11572 ings of the North American Chapter of the Association for Computational Linguistics (NAACL)*,  
11573 pp. 602–610.
- 11574 Finkel, J. R. and C. D. Manning (2008). Enforcing transitivity in coreference resolution.  
11575 In *Proceedings of the 46th Annual Meeting of the Association for Computational Linguistics  
11576 on Human Language Technologies: Short Papers*, pp. 45–48. Association for Computational  
11577 Linguistics.
- 11578 Finkelstein, L., E. Gabrilovich, Y. Matias, E. Rivlin, Z. Solan, G. Wolfman, and E. Ruppin  
11579 (2002). Placing search in context: The concept revisited. *ACM Transactions on Information  
11580 Systems* 20(1), 116–131.

- 11581 Firth, J. R. (1957). *Papers in Linguistics 1934-1951*. Oxford University Press.
- 11582 Flanigan, J., S. Thomson, J. Carbonell, C. Dyer, and N. A. Smith (2014). A discriminative graph-based parser for the abstract meaning representation. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 1426–1436.
- 11585 Foltz, P. W., W. Kintsch, and T. K. Landauer (1998). The measurement of textual coherence with latent semantic analysis. *Discourse processes* 25(2-3), 285–307.
- 11586
- 11587 Fordyce, C. S. (2007). Overview of the iwslt 2007 evaluation campaign. In *International Workshop on Spoken Language Translation (IWSLT) 2007*.
- 11588
- 11589 Forsyth, E. N. and C. H. Martell (2007). Lexical and discourse analysis of online chat dialog. In *International Conference on Semantic Computing*, pp. 19–26. IEEE.
- 11590
- 11591 Fox, H. (2002). Phrasal cohesion and statistical machine translation. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 304–3111.
- 11592
- 11593 Francis, W. and H. Kucera (1982). *Frequency analysis of English usage*. Houghton Mifflin Company.
- 11594
- 11595 Francis, W. N. (1964). A standard sample of present-day English for use with digital computers. Report to the U.S Office of Education on Cooperative Research Project No. E-007.
- 11596
- 11597
- 11598 Freund, Y. and R. E. Schapire (1999). Large margin classification using the perceptron algorithm. *Machine learning* 37(3), 277–296.
- 11599
- 11600 Fromkin, V., R. Rodman, and N. Hyams (2013). *An introduction to language*. Cengage Learning.
- 11601
- 11602 Fundel, K., R. Küffner, and R. Zimmer (2007). Relex – relation extraction using dependency parse trees. *Bioinformatics* 23(3), 365–371.
- 11603
- 11604 Gabow, H. N., Z. Galil, T. Spencer, and R. E. Tarjan (1986). Efficient algorithms for finding minimum spanning trees in undirected and directed graphs. *Combinatorica* 6(2), 109–122.
- 11605
- 11606
- 11607 Gabrilovich, E. and S. Markovitch (2007). Computing semantic relatedness using wikipedia-based explicit semantic analysis. In *Proceedings of the International Joint Conference on Artificial Intelligence (IJCAI)*, Volume 7, pp. 1606–1611.
- 11608
- 11609
- 11610 Gage, P. (1994). A new algorithm for data compression. *The C Users Journal* 12(2), 23–38.

- 11611 Gale, W. A., K. W. Church, and D. Yarowsky (1992). One sense per discourse. In *Proceedings of the workshop on Speech and Natural Language*, pp. 233–237. Association for  
11612 Computational Linguistics.
- 11613
- 11614 Galley, M., M. Hopkins, K. Knight, and D. Marcu (2004). What's in a translation rule? In *Proceedings of the North American Chapter of the Association for Computational Linguistics*  
11615 (NAACL), pp. 273–280.
- 11616
- 11617 Galley, M., K. R. McKeown, E. Fosler-Lussier, and H. Jing (2003). Discourse segmentation  
11618 of multi-party conversation. In *Proceedings of the Association for Computational Linguistics*  
11619 (ACL).
- 11620 Ganchev, K. and M. Dredze (2008). Small statistical models by random feature mixing. In  
11621 *Proceedings of the ACL08 HLT Workshop on Mobile Language Processing*, pp. 19–20.
- 11622 Ganchev, K., J. Graça, J. Gillenwater, and B. Taskar (2010). Posterior regularization for  
11623 structured latent variable models. *The Journal of Machine Learning Research* 11, 2001–  
11624 2049.
- 11625 Ganin, Y., E. Ustinova, H. Ajakan, P. Germain, H. Larochelle, F. Laviolette, M. Marchand,  
11626 and V. Lempitsky (2016). Domain-adversarial training of neural networks. *Journal of*  
11627 *Machine Learning Research* 17(59), 1–35.
- 11628 Gao, J., G. Andrew, M. Johnson, and K. Toutanova (2007). A comparative study of param-  
11629 eter estimation methods for statistical natural language processing. In *Proceedings of the*  
11630 *Association for Computational Linguistics (ACL)*, pp. 824–831.
- 11631 Gatt, A. and E. Krahmer (2018). Survey of the state of the art in natural language genera-  
11632 tion: Core tasks, applications and evaluation. *Journal of Artificial Intelligence Research* 61,  
11633 65–170.
- 11634 Ge, D., X. Jiang, and Y. Ye (2011). A note on the complexity of  $l_1$  p minimization. *Mathem-  
11635 atical programming* 129(2), 285–299.
- 11636 Ge, N., J. Hale, and E. Charniak (1998). A statistical approach to anaphora resolution. In  
11637 *Proceedings of the sixth workshop on very large corpora*, Volume 71, pp. 76.
- 11638 Ge, R., F. Huang, C. Jin, and Y. Yuan (2015). Escaping from saddle points — online stochas-  
11639 tic gradient for tensor decomposition. In P. Grünwald, E. Hazan, and S. Kale (Eds.),  
11640 *Proceedings of the Conference On Learning Theory (COLT)*.
- 11641 Ge, R. and R. J. Mooney (2005). A statistical semantic parser that integrates syntax and  
11642 semantics. In *Proceedings of the Conference on Natural Language Learning (CoNLL)*, pp.  
11643 9–16.

- 11644 Geach, P. T. (1962). *Reference and generality: An examination of some medieval and modern theories*. Cornell University Press.
- 11645 Gehring, J., M. Auli, D. Grangier, D. Yarats, and Y. N. Dauphin (2017, May). Convolutional sequence to sequence learning. *ArXiv e-prints*.
- 11646 Gildea, D. and D. Jurafsky (2002). Automatic labeling of semantic roles. *Computational linguistics* 28(3), 245–288.
- 11647 Gimpel, K., N. Schneider, B. O'Connor, D. Das, D. Mills, J. Eisenstein, M. Heilman, D. Yogoatama, J. Flanigan, and N. A. Smith (2011). Part-of-speech tagging for Twitter: annotation, features, and experiments. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 42–47.
- 11648 Glass, J., T. J. Hazen, S. Cyphers, I. Malioutov, D. Huynh, and R. Barzilay (2007). Recent progress in the mit spoken lecture processing project. In *Eighth Annual Conference of the International Speech Communication Association*.
- 11649 Glorot, X. and Y. Bengio (2010). Understanding the difficulty of training deep feedforward neural networks. In *Proceedings of Artificial Intelligence and Statistics (AISTATS)*, pp. 249–256.
- 11650 Glorot, X., A. Bordes, and Y. Bengio (2011). Deep sparse rectifier networks. In *Proceedings of the 14th International Conference on Artificial Intelligence and Statistics. JMLR W&CP Volume*, Volume 15, pp. 315–323.
- 11651 Godfrey, J. J., E. C. Holliman, and J. McDaniel (1992). Switchboard: Telephone speech corpus for research and development. In *Proceedings of the International Conference on Acoustics, Speech, and Signal Processing (ICASSP)*, pp. 517–520. IEEE.
- 11652 Goldberg, Y. (2017a, June). An adversarial review of “adversarial generation of natural language”. <https://medium.com/@yoav.goldberg/an-adversarial-review-of-adversarial-generation-of-natural-language-409ac3378bd7>.
- 11653 Goldberg, Y. (2017b). *Neural Network Methods for Natural Language Processing*. Synthesis Lectures on Human Language Technologies. Morgan & Claypool Publishers.
- 11654 Goldberg, Y. and M. Elhadad (2010). An efficient algorithm for easy-first non-directional dependency parsing. In *Proceedings of the North American Chapter of the Association for Computational Linguistics (NAACL)*, pp. 742–750.
- 11655 Goldberg, Y. and J. Nivre (2012). A dynamic oracle for arc-eager dependency parsing. In *Proceedings of the International Conference on Computational Linguistics (COLING)*, pp. 959–976.

- 11677 Goldberg, Y., K. Zhao, and L. Huang (2013). Efficient implementation of beam-search  
11678 incremental parsers. In *ACL* (2), pp. 628–633.
- 11679 Goldwater, S. and T. Griffiths (2007). A fully bayesian approach to unsupervised part-of-  
11680 speech tagging. In *Annual meeting-association for computational linguistics*, Volume 45.
- 11681 Gonçalo Oliveira, H. R., F. A. Cardoso, and F. C. Pereira (2007). Tra-la-lyrics: An approach  
11682 to generate text based on rhythm. In *Proceedings of the 4th. International Joint Workshop*  
11683 on *Computational Creativity*. A. Cardoso and G. Wiggins.
- 11684 Goodfellow, I., Y. Bengio, and A. Courville (2016). *Deep learning*. MIT Press.
- 11685 Goodman, J. T. (2001). A bit of progress in language modeling. *Computer Speech & Lan-*  
11686 *guage* 15(4), 403–434.
- 11687 Gouws, S., D. Metzler, C. Cai, and E. Hovy (2011). Contextual bearing on linguistic varia-  
11688 tion in social media. In *LASM*.
- 11689 Goyal, A., H. Daume III, and S. Venkatasubramanian (2009). Streaming for large scale  
11690 nlp: Language modeling. In *Proceedings of the North American Chapter of the Association*  
11691 for *Computational Linguistics* (NAACL), pp. 512–520.
- 11692 Graves, A. (2012). Sequence transduction with recurrent neural networks. In *Proceedings*  
11693 of the *International Conference on Machine Learning* (ICML).
- 11694 Graves, A. and N. Jaitly (2014). Towards end-to-end speech recognition with recur-  
11695 rent neural networks. In *Proceedings of the International Conference on Machine Learning*  
11696 (ICML), pp. 1764–1772.
- 11697 Graves, A. and J. Schmidhuber (2005). Framewise phoneme classification with bidirec-  
11698 tional lstm and other neural network architectures. *Neural Networks* 18(5), 602–610.
- 11699 Grice, H. P. (1975). Logic and conversation. In P. Cole and J. L. Morgan (Eds.), *Syntax and*  
11700 *Semantics Volume 3: Speech Acts*, pp. 41–58. Academic Press.
- 11701 Grishman, R. (2012). Information extraction: Capabilities and challenges. Notes prepared  
11702 for the 2012 International Winter School in Language and Speech Technologies, Rovira  
11703 i Virgili University, Tarragona, Spain.
- 11704 Grishman, R. (2015). Information extraction. *IEEE Intelligent Systems* 30(5), 8–15.
- 11705 Grishman, R., C. Macleod, and J. Sterling (1992). Evaluating parsing strategies using  
11706 standardized parse files. In *Proceedings of the third conference on Applied natural language*  
11707 *processing*, pp. 156–161. Association for Computational Linguistics.

- 11708 Grishman, R. and B. Sundheim (1996). Message understanding conference-6: A brief history.  
 11709 In *Proceedings of the International Conference on Computational Linguistics (COLING)*,  
 11710 pp. 466–471.
- 11711 Groenendijk, J. and M. Stokhof (1991). Dynamic predicate logic. *Linguistics and philosophy* 14(1), 39–100.
- 11713 Grosz, B. J. (1979). Focusing and description in natural language dialogues. Technical  
 11714 report, SRI INTERNATIONAL MENLO PARK CA.
- 11715 Grosz, B. J., S. Weinstein, and A. K. Joshi (1995). Centering: A framework for modeling  
 11716 the local coherence of discourse. *Computational linguistics* 21(2), 203–225.
- 11717 Gu, J., Z. Lu, H. Li, and V. O. Li (2016). Incorporating copying mechanism in sequence-to-  
 11718 sequence learning. In *Proceedings of the Association for Computational Linguistics (ACL)*,  
 11719 pp. 1631–1640.
- 11720 Gulcehre, C., S. Ahn, R. Nallapati, B. Zhou, and Y. Bengio (2016). Pointing the unknown  
 11721 words. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 140–149.
- 11722 Gutmann, M. U. and A. Hyvärinen (2012). Noise-contrastive estimation of unnormalized  
 11723 statistical models, with applications to natural image statistics. *The Journal of Machine  
 11724 Learning Research* 13(1), 307–361.
- 11725 Haghghi, A. and D. Klein (2007). Unsupervised coreference resolution in a nonparametric  
 11726 bayesian model. In *Proceedings of the Association for Computational Linguistics (ACL)*.
- 11727 Haghghi, A. and D. Klein (2009). Simple coreference resolution with rich syntactic and  
 11728 semantic features. In *Proceedings of Empirical Methods for Natural Language Processing  
 11729 (EMNLP)*, pp. 1152–1161.
- 11730 Haghghi, A. and D. Klein (2010). Coreference resolution in a modular, entity-centered  
 11731 model. In *Proceedings of the North American Chapter of the Association for Computational  
 11732 Linguistics (NAACL)*, pp. 385–393.
- 11733 Hajič, J. and B. Hladká (1998). Tagging inflective languages: Prediction of morphological  
 11734 categories for a rich, structured tagset. In *Proceedings of the Association for Computational  
 11735 Linguistics (ACL)*, pp. 483–490.
- 11736 Halliday, M. and R. Hasan (1976). *Cohesion in English*. London: Longman.
- 11737 Hammerton, J. (2003). Named entity recognition with long short-term memory. In *Pro-  
 11738 ceedings of the Conference on Natural Language Learning (CoNLL)*, pp. 172–175.
- 11739 Han, X. and L. Sun (2012). An entity-topic model for entity linking. In *Proceedings of  
 11740 Empirical Methods for Natural Language Processing (EMNLP)*, pp. 105–115.

- 11741 Han, X., L. Sun, and J. Zhao (2011). Collective entity linking in web text: a graph-based  
11742 method. In *Proceedings of ACM SIGIR conference on Research and development in informa-*  
11743 *tion retrieval*, pp. 765–774.
- 11744 Hannak, A., E. Anderson, L. F. Barrett, S. Lehmann, A. Mislove, and M. Riedewald (2012).  
11745 Tweetin’ in the rain: Exploring societal-scale effects of weather on mood. In *Proceedings*  
11746 *of the International Conference on Web and Social Media (ICWSM)*.
- 11747 Hardmeier, C. (2012). Discourse in statistical machine translation. a survey and a case  
11748 study. *Discours. Revue de linguistique, psycholinguistique et informatique. A journal of lin-*  
11749 *guistics, psycholinguistics and computational linguistics* (11).
- 11750 Haspelmath, M. and A. Sims (2013). *Understanding morphology*. Routledge.
- 11751 Hastie, T., R. Tibshirani, and J. Friedman (2009). *The elements of statistical learning* (Second  
11752 ed.). New York: Springer.
- 11753 Hatzivassiloglou, V. and K. R. McKeown (1997). Predicting the semantic orientation of  
11754 adjectives. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 174–  
11755 181.
- 11756 Hayes, A. F. and K. Krippendorff (2007). Answering the call for a standard reliability  
11757 measure for coding data. *Communication methods and measures* 1(1), 77–89.
- 11758 He, H., A. Balakrishnan, M. Eric, and P. Liang (2017). Learning symmetric collaborative  
11759 dialogue agents with dynamic knowledge graph embeddings. In *Proceedings of the As-*  
11760 *sociation for Computational Linguistics (ACL)*, pp. 1766–1776.
- 11761 He, K., X. Zhang, S. Ren, and J. Sun (2015). Delving deep into rectifiers: Surpassing  
11762 human-level performance on imagenet classification. In *Proceedings of the International*  
11763 *Conference on Computer Vision (ICCV)*, pp. 1026–1034.
- 11764 He, K., X. Zhang, S. Ren, and J. Sun (2016). Deep residual learning for image recognition.  
11765 In *Proceedings of the International Conference on Computer Vision (ICCV)*, pp. 770–778.
- 11766 He, L., K. Lee, M. Lewis, and L. Zettlemoyer (2017). Deep semantic role labeling: What  
11767 works and what’s next. In *Proceedings of the Association for Computational Linguistics*  
11768 *(ACL)*.
- 11769 He, Z., S. Liu, M. Li, M. Zhou, L. Zhang, and H. Wang (2013). Learning entity repre-  
11770 *sentation for entity disambiguation*. In *Proceedings of the Association for Computational*  
11771 *Linguistics (ACL)*, pp. 30–34.
- 11772 Hearst, M. A. (1992). Automatic acquisition of hyponyms from large text corpora. In  
11773 *Proceedings of the International Conference on Computational Linguistics (COLING)*, pp. 539–  
11774 545. Association for Computational Linguistics.

- 11775 Hearst, M. A. (1997). Texttiling: Segmenting text into multi-paragraph subtopic passages.  
11776 *Computational linguistics* 23(1), 33–64.
- 11777 Heerschap, B., F. Goossen, A. Hogenboom, F. Frasincar, U. Kaymak, and F. de Jong (2011).  
11778 Polarity analysis of texts using discourse structure. In *Proceedings of the 20th ACM inter-*  
11779 *national conference on Information and knowledge management*, pp. 1061–1070. ACM.
- 11780 Henderson, J. (2004). Discriminative training of a neural network statistical parser. In  
11781 *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 95–102.
- 11782 Hendrickx, I., S. N. Kim, Z. Kozareva, P. Nakov, D. Ó Séaghdha, S. Padó, M. Pennacchiotti,  
11783 L. Romano, and S. Szpakowicz (2009). Semeval-2010 task 8: Multi-way classification of  
11784 semantic relations between pairs of nominals. In *Proceedings of the Workshop on Semantic*  
11785 *Evaluations: Recent Achievements and Future Directions*, pp. 94–99. Association for Com-  
11786 putational Linguistics.
- 11787 Hermann, K. M., T. Kočiský, E. Grefenstette, L. Espeholt, W. Kay, M. Suleyman, and  
11788 P. Blunsom (2015). Teaching machines to read and comprehend. In *Advances in Neu-*  
11789 *ral Information Processing Systems*, pp. 1693–1701.
- 11790 Hernault, H., H. Prendinger, D. A. duVerle, and M. Ishizuka (2010). HILDA: A discourse  
11791 parser using support vector machine classification. *Dialogue and Discourse* 1(3), 1–33.
- 11792 Hill, F., A. Bordes, S. Chopra, and J. Weston (2016). The goldilocks principle: Reading  
11793 children’s books with explicit memory representations. In *Proceedings of the International*  
11794 *Conference on Learning Representations (ICLR)*.
- 11795 Hill, F., K. Cho, and A. Korhonen (2016). Learning distributed representations of sentences  
11796 from unlabelled data. In *Proceedings of the North American Chapter of the Association for*  
11797 *Computational Linguistics (NAACL)*.
- 11798 Hindle, D. and M. Rooth (1993). Structural ambiguity and lexical relations. *Computational*  
11799 *linguistics* 19(1), 103–120.
- 11800 Hirao, T., Y. Yoshida, M. Nishino, N. Yasuda, and M. Nagata (2013). Single-document  
11801 summarization as a tree knapsack problem. In *Proceedings of Empirical Methods for Nat-*  
11802 *ural Language Processing (EMNLP)*, pp. 1515–1520.
- 11803 Hirschman, L. and R. Gaizauskas (2001). Natural language question answering: the view  
11804 from here. *natural language engineering* 7(4), 275–300.
- 11805 Hirschman, L., M. Light, E. Breck, and J. D. Burger (1999). Deep read: A reading compre-  
11806 hension system. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp.  
11807 325–332.

- 11808 Hobbs, J. R. (1978). Resolving pronoun references. *Lingua* 44(4), 311–338.
- 11809 Hobbs, J. R., D. Appelt, J. Bear, D. Israel, M. Kameyama, M. Stickel, and M. Tyson (1997).
- 11810 Fastus: A cascaded finite-state transducer for extracting information from natural-
- 11811 language text. *Finite-state language processing*, 383–406.
- 11812 Hochreiter, S. and J. Schmidhuber (1997). Long short-term memory. *Neural computa-*
- 11813 *tion* 9(8), 1735–1780.
- 11814 Hockenmaier, J. and M. Steedman (2007). Ccgbank: a corpus of ccg derivations and de-
- 11815 pendency structures extracted from the penn treebank. *Computational Linguistics* 33(3),
- 11816 355–396.
- 11817 Hoffart, J., M. A. Yosef, I. Bordino, H. Fürstenau, M. Pinkal, M. Spaniol, B. Taneva,
- 11818 S. Thater, and G. Weikum (2011). Robust disambiguation of named entities in text. In
- 11819 *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 782–792.
- 11820 Hoffmann, R., C. Zhang, X. Ling, L. Zettlemoyer, and D. S. Weld (2011). Knowledge-based
- 11821 weak supervision for information extraction of overlapping relations. In *Proceedings of*
- 11822 *the Association for Computational Linguistics (ACL)*, pp. 541–550.
- 11823 Holmstrom, L. and P. Koistinen (1992). Using additive noise in back-propagation training.
- 11824 *IEEE Transactions on Neural Networks* 3(1), 24–38.
- 11825 Hovy, E. and J. Lavid (2010). Towards a ‘science’ of corpus annotation: a new methodo-
- 11826 logical challenge for corpus linguistics. *International journal of translation* 22(1), 13–36.
- 11827 Hsu, D., S. M. Kakade, and T. Zhang (2012). A spectral algorithm for learning hidden
- 11828 markov models. *Journal of Computer and System Sciences* 78(5), 1460–1480.
- 11829 Hu, M. and B. Liu (2004). Mining and summarizing customer reviews. In *Proceedings of*
- 11830 *Knowledge Discovery and Data Mining (KDD)*, pp. 168–177.
- 11831 Hu, Z., Z. Yang, X. Liang, R. Salakhutdinov, and E. P. Xing (2017). Toward controlled
- 11832 generation of text. In *International Conference on Machine Learning*, pp. 1587–1596.
- 11833 Huang, F. and A. Yates (2012). Biased representation learning for domain adaptation. In
- 11834 *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 1313–1323.
- 11835 Huang, L. and D. Chiang (2007). Forest rescoring: Faster decoding with integrated lan-
- 11836 guage models. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp.
- 11837 144–151.
- 11838 Huang, L., S. Fayong, and Y. Guo (2012). Structured perceptron with inexact search. In
- 11839 *Proceedings of the North American Chapter of the Association for Computational Linguistics*
- 11840 (*NAACL*), pp. 142–151.

- 11841 Huang, Y. (2015). *Pragmatics* (Second ed.). Oxford Textbooks in Linguistics. Oxford University Press.
- 11843 Huang, Z., W. Xu, and K. Yu (2015). Bidirectional lstm-crf models for sequence tagging.  
11844 *arXiv preprint arXiv:1508.01991*.
- 11845 Huffman, D. A. (1952). A method for the construction of minimum-redundancy codes.  
11846 *Proceedings of the IRE* 40(9), 1098–1101.
- 11847 Humphreys, K., R. Gaizauskas, and S. Azzam (1997). Event coreference for information  
11848 extraction. In *Proceedings of a Workshop on Operational Factors in Practical, Robust Anaphora*  
11849 *Resolution for Unrestricted Texts*, pp. 75–81. Association for Computational Linguistics.
- 11850 Ide, N. and Y. Wilks (2006). Making sense about sense. In *Word sense disambiguation*, pp.  
11851 47–73. Springer.
- 11852 Ioffe, S. and C. Szegedy (2015). Batch normalization: Accelerating deep network training-  
11853 ing by reducing internal covariate shift. In *Proceedings of the International Conference on*  
11854 *Machine Learning (ICML)*, pp. 448–456.
- 11855 Isozaki, H., T. Hirao, K. Duh, K. Sudoh, and H. Tsukada (2010). Automatic evaluation  
11856 of translation quality for distant language pairs. In *Proceedings of Empirical Methods for*  
11857 *Natural Language Processing (EMNLP)*, pp. 944–952.
- 11858 Iyyer, M., V. Manjunatha, J. Boyd-Graber, and H. Daumé III (2015). Deep unordered com-  
11859 position rivals syntactic methods for text classification. In *Proceedings of the Association*  
11860 *for Computational Linguistics (ACL)*, pp. 1681–1691.
- 11861 James, G., D. Witten, T. Hastie, and R. Tibshirani (2013). *An introduction to statistical learn-  
11862 ing*, Volume 112. Springer.
- 11863 Janin, A., D. Baron, J. Edwards, D. Ellis, D. Gelbart, N. Morgan, B. Peskin, T. Pfau,  
11864 E. Shriberg, A. Stolcke, et al. (2003). The ICSI meeting corpus. In *Acoustics, Speech,*  
11865 *and Signal Processing, 2003. Proceedings.(ICASSP'03). 2003 IEEE International Conference*  
11866 *on*, Volume 1, pp. I–I. IEEE.
- 11867 Jean, S., K. Cho, R. Memisevic, and Y. Bengio (2015). On using very large target vocab-  
11868 uary for neural machine translation. In *Proceedings of the Association for Computational*  
11869 *Linguistics (ACL)*, pp. 1–10.
- 11870 Jeong, M., C.-Y. Lin, and G. G. Lee (2009). Semi-supervised speech act recognition in  
11871 emails and forums. In *Proceedings of Empirical Methods for Natural Language Processing*  
11872 *(EMNLP)*, pp. 1250–1259.

- 11873 Ji, H. and R. Grishman (2011). Knowledge base population: Successful approaches and  
11874 challenges. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 1148–  
11875 1158.
- 11876 Ji, Y., T. Cohn, L. Kong, C. Dyer, and J. Eisenstein (2015). Document context language  
11877 models. In *International Conference on Learning Representations, Workshop Track*, Volume  
11878 abs/1511.03962.
- 11879 Ji, Y. and J. Eisenstein (2014). Representation learning for text-level discourse parsing. In  
11880 *Proceedings of the Association for Computational Linguistics (ACL)*.
- 11881 Ji, Y. and J. Eisenstein (2015, June). One vector is not enough: Entity-augmented distribu-  
11882 tional semantics for discourse relations. *Transactions of the Association for Computational  
11883 Linguistics (TACL)*.
- 11884 Ji, Y., G. Haffari, and J. Eisenstein (2016). A latent variable recurrent neural network for  
11885 discourse relation language models. In *Proceedings of the North American Chapter of the  
11886 Association for Computational Linguistics (NAACL)*.
- 11887 Ji, Y. and N. A. Smith (2017). Neural discourse structure for text categorization. In *Pro-  
11888 ceedings of the Association for Computational Linguistics (ACL)*, pp. 996–1005.
- 11889 Ji, Y., C. Tan, S. Martschat, Y. Choi, and N. A. Smith (2017). Dynamic entity representations  
11890 in neural language models. In *Proceedings of Empirical Methods for Natural Language  
11891 Processing (EMNLP)*, pp. 1831–1840.
- 11892 Jiang, L., M. Yu, M. Zhou, X. Liu, and T. Zhao (2011). Target-dependent twitter sentiment  
11893 classification. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp.  
11894 151–160.
- 11895 Jing, H. (2000). Sentence reduction for automatic text summarization. In *Proceedings of  
11896 the sixth conference on Applied natural language processing*, pp. 310–315. Association for  
11897 Computational Linguistics.
- 11898 Joachims, T. (2002). Optimizing search engines using clickthrough data. In *Proceedings of  
11899 Knowledge Discovery and Data Mining (KDD)*, pp. 133–142.
- 11900 Jockers, M. L. (2015). Szuzhet? <http://bla.bla.com>.
- 11901 Johnson, A. E., T. J. Pollard, L. Shen, H. L. Li-wei, M. Feng, M. Ghassemi, B. Moody,  
11902 P. Szolovits, L. A. Celi, and R. G. Mark (2016). Mimic-iii, a freely accessible critical care  
11903 database. *Scientific data* 3, 160035.
- 11904 Johnson, M. (1998). Pcfg models of linguistic tree representations. *Computational Linguis-  
11905 tics* 24(4), 613–632.

- 11906 Johnson, R. and T. Zhang (2017). Deep pyramid convolutional neural networks for text  
 11907 categorization. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp.  
 11908 562–570.
- 11909 Joshi, A. K. (1985). How much context-sensitivity is required to provide reasonable struc-  
 11910 tural descriptions? – tree adjoining grammars. In *Natural Language Processing – Theoret-  
 11911 ical, Computational and Psychological Perspective*. New York, NY: Cambridge University  
 11912 Press.
- 11913 Joshi, A. K. and Y. Schabes (1997). Tree-adjoining grammars. In *Handbook of formal lan-  
 11914 guages*, pp. 69–123. Springer.
- 11915 Joshi, A. K., K. V. Shanker, and D. Weir (1991). The convergence of mildly context-sensitive  
 11916 grammar formalisms. In *Foundational Issues in Natural Language Processing*. Cambridge  
 11917 MA: MIT Press.
- 11918 Jozefowicz, R., O. Vinyals, M. Schuster, N. Shazeer, and Y. Wu (2016). Exploring the limits  
 11919 of language modeling. *arXiv preprint arXiv:1602.02410*.
- 11920 Jozefowicz, R., W. Zaremba, and I. Sutskever (2015). An empirical exploration of recurrent  
 11921 network architectures. In *Proceedings of the International Conference on Machine Learning  
 (ICML)*, pp. 2342–2350.
- 11923 Jurafsky, D. (1996). A probabilistic model of lexical and syntactic access and disambigua-  
 11924 tion. *Cognitive Science* 20(2), 137–194.
- 11925 Jurafsky, D. and J. H. Martin (2009). *Speech and Language Processing* (Second ed.). Prentice  
 11926 Hall.
- 11927 Jurafsky, D. and J. H. Martin (2018). *Speech and Language Processing* (Third ed.). Prentice  
 11928 Hall.
- 11929 Kadlec, R., M. Schmid, O. Bajgar, and J. Kleindienst (2016). Text understanding with  
 11930 the attention sum reader network. In *Proceedings of the Association for Computational  
 11931 Linguistics (ACL)*, pp. 908–918.
- 11932 Kalchbrenner, N. and P. Blunsom (2013, August). Recurrent convolutional neural net-  
 11933 works for discourse compositionality. In *Proceedings of the Workshop on Continuous Vec-  
 11934 tor Space Models and their Compositionality*, Sofia, Bulgaria, pp. 119–126. Association for  
 11935 Computational Linguistics.
- 11936 Kalchbrenner, N., E. Grefenstette, and P. Blunsom (2014). A convolutional neural network  
 11937 for modelling sentences. In *Proceedings of the Association for Computational Linguistics  
 11938 (ACL)*, pp. 655–665.

- 11939 Karlsson, F. (2007). Constraints on multiple center-embedding of clauses. *Journal of Lin-*  
11940 *guistics* 43(02), 365–392.
- 11941 Kate, R. J., Y. W. Wong, and R. J. Mooney (2005). Learning to transform natural to formal  
11942 languages. In *Proceedings of the National Conference on Artificial Intelligence (AAAI)*.
- 11943 Kehler, A. (2007). Rethinking the SMASH approach to pronoun interpretation. In *Interdis-*  
11944 *ciplinary perspectives on reference processing*, New Directions in Cognitive Science Series,  
11945 pp. 95–122. Oxford University Press.
- 11946 Kibble, R. and R. Power (2004). Optimizing referential coherence in text generation. *Com-*  
11947 *putational Linguistics* 30(4), 401–416.
- 11948 Kilgarriff, A. (1997). I don't believe in word senses. *Computers and the Humanities* 31(2),  
11949 91–113.
- 11950 Kilgarriff, A. and G. Grefenstette (2003). Introduction to the special issue on the web as  
11951 corpus. *Computational linguistics* 29(3), 333–347.
- 11952 Kim, M.-J. (2002). Does korean have adjectives? *MIT Working Papers in Linguistics* 43,  
11953 71–89.
- 11954 Kim, S.-M. and E. Hovy (2006, July). Extracting opinions, opinion holders, and topics  
11955 expressed in online news media text. In *Proceedings of the Workshop on Sentiment and*  
11956 *Subjectivity in Text*, Sydney, Australia, pp. 1–8. Association for Computational Linguis-  
11957 tics.
- 11958 Kim, Y. (2014). Convolutional neural networks for sentence classification. In *Proceedings*  
11959 *of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 1746–1751.
- 11960 Kim, Y., C. Denton, L. Hoang, and A. M. Rush (2017). Structured attention networks. In  
11961 *Proceedings of the International Conference on Learning Representations (ICLR)*.
- 11962 Kim, Y., Y. Jernite, D. Sontag, and A. M. Rush (2016). Character-aware neural language  
11963 models. In *Proceedings of the National Conference on Artificial Intelligence (AAAI)*.
- 11964 Kingma, D. and J. Ba (2014). Adam: A method for stochastic optimization. *arXiv preprint*  
11965 *arXiv:1412.6980*.
- 11966 Kiperwasser, E. and Y. Goldberg (2016). Simple and accurate dependency parsing using  
11967 bidirectional lstm feature representations. *Transactions of the Association for Compu-*  
11968 *tational Linguistics* 4, 313–327.
- 11969 Kipper-Schuler, K. (2005). *VerbNet: A broad-coverage, comprehensive verb lexicon*. Ph. D.  
11970 thesis, Computer and Information Science, University of Pennsylvania.

- 11971 Kiros, R., R. Salakhutdinov, and R. Zemel (2014). Multimodal neural language models. In  
 11972 *Proceedings of the International Conference on Machine Learning (ICML)*, pp. 595–603.
- 11973 Kiros, R., Y. Zhu, R. Salakhutdinov, R. S. Zemel, A. Torralba, R. Urtasun, and S. Fidler  
 11974 (2015). Skip-thought vectors. In *Neural Information Processing Systems (NIPS)*.
- 11975 Klein, D. and C. D. Manning (2003). Accurate unlexicalized parsing. In *Proceedings of the*  
 11976 *Association for Computational Linguistics (ACL)*, pp. 423–430.
- 11977 Klein, D. and C. D. Manning (2004). Corpus-based induction of syntactic structure: Mod-  
 11978 els of dependency and constituency. In *Proceedings of the Association for Computational*  
 11979 *Linguistics (ACL)*.
- 11980 Klein, G., Y. Kim, Y. Deng, J. Senellart, and A. M. Rush (2017). Opennmt: Open-source  
 11981 toolkit for neural machine translation. *arXiv preprint arXiv:1701.02810*.
- 11982 Klementiev, A., I. Titov, and B. Bhattacharyya (2012). Inducing crosslingual distributed repre-  
 11983 sentations of words. In *Proceedings of the International Conference on Computational Lin-*  
 11984 *guistics (COLING)*, pp. 1459–1474.
- 11985 Klenner, M. (2007). Enforcing consistency on coreference sets. In *Recent Advances in Natu-*  
 11986 *ral Language Processing (RANLP)*, pp. 323–328.
- 11987 Knight, K. (1999). Decoding complexity in word-replacement translation models. *Computa-*  
 11988 *tional Linguistics* 25(4), 607–615.
- 11989 Knight, K. and J. Graehl (1998). Machine transliteration. *Computational Linguistics* 24(4),  
 11990 599–612.
- 11991 Knight, K. and D. Marcu (2000). Statistics-based summarization-step one: Sentence com-  
 11992 pression. In *Proceedings of the National Conference on Artificial Intelligence (AAAI)*, pp.  
 11993 703–710.
- 11994 Knight, K. and J. May (2009). Applications of weighted automata in natural language  
 11995 processing. In *Handbook of Weighted Automata*, pp. 571–596. Springer.
- 11996 Knott, A. (1996). *A data-driven methodology for motivating a set of coherence relations*. Ph. D.  
 11997 thesis, The University of Edinburgh.
- 11998 Koehn, P. (2005). Europarl: A parallel corpus for statistical machine translation. In *MT*  
 11999 *summit*, Volume 5, pp. 79–86.
- 12000 Koehn, P. (2009). *Statistical machine translation*. Cambridge University Press.
- 12001 Koehn, P. (2017). Neural machine translation. *arXiv preprint arXiv:1709.07809*.

- 12002 Konstas, I. and M. Lapata (2013). A global model for concept-to-text generation. *Journal  
12003 of Artificial Intelligence Research* 48, 305–346.
- 12004 Koo, T., X. Carreras, and M. Collins (2008, jun). Simple semi-supervised dependency  
12005 parsing. In *Proceedings of ACL-08: HLT*, Columbus, Ohio, pp. 595–603. Association for  
12006 Computational Linguistics.
- 12007 Koo, T. and M. Collins (2005). Hidden-variable models for discriminative reranking. In  
12008 *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 507–514.
- 12009 Koo, T. and M. Collins (2010). Efficient third-order dependency parsers. In *Proceedings of  
12010 the Association for Computational Linguistics (ACL)*.
- 12011 Koo, T., A. Globerson, X. Carreras, and M. Collins (2007). Structured prediction models  
12012 via the matrix-tree theorem. In *Proceedings of Empirical Methods for Natural Language  
12013 Processing (EMNLP)*, pp. 141–150.
- 12014 Kovach, B. and T. Rosenstiel (2014). *The elements of journalism: What newpeople should know  
12015 and the public should expect*. Three Rivers Press.
- 12016 Krishnamurthy, J. (2016). Probabilistic models for learning a semantic parser lexicon. In  
12017 *Proceedings of the North American Chapter of the Association for Computational Linguistics  
12018 (NAACL)*, pp. 606–616.
- 12019 Krishnamurthy, J. and T. M. Mitchell (2012). Weakly supervised training of semantic  
12020 parsers. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*,  
12021 pp. 754–765.
- 12022 Krizhevsky, A., I. Sutskever, and G. E. Hinton (2012). Imagenet classification with deep  
12023 convolutional neural networks. In *Neural Information Processing Systems (NIPS)*, pp.  
12024 1097–1105.
- 12025 Kübler, S., R. McDonald, and J. Nivre (2009). Dependency parsing. *Synthesis Lectures on  
12026 Human Language Technologies* 1(1), 1–127.
- 12027 Kuhlmann, M. and J. Nivre (2010). Transition-based techniques for non-projective depen-  
12028 dency parsing. *Northern European Journal of Language Technology (NEJLT)* 2(1), 1–19.
- 12029 Kummerfeld, J. K., T. Berg-Kirkpatrick, and D. Klein (2015). An empirical analysis of op-  
12030 timization for max-margin NLP. In *Proceedings of Empirical Methods for Natural Language  
12031 Processing (EMNLP)*.
- 12032 Kwiatkowski, T., S. Goldwater, L. Zettlemoyer, and M. Steedman (2012). A probabilistic  
12033 model of syntactic and semantic acquisition from child-directed utterances and their  
12034 meanings. In *Proceedings of the European Chapter of the Association for Computational Lin-  
12035 guistics (EACL)*, pp. 234–244.

- 12036 Lafferty, J., A. McCallum, and F. Pereira (2001). Conditional random fields: Probabilistic  
12037 models for segmenting and labeling sequence data. In *icml*.
- 12038 Lakoff, G. (1973). Hedges: A study in meaning criteria and the logic of fuzzy concepts.  
12039 *Journal of philosophical logic* 2(4), 458–508.
- 12040 Lample, G., M. Ballesteros, S. Subramanian, K. Kawakami, and C. Dyer (2016). Neural  
12041 architectures for named entity recognition. In *Proceedings of the North American Chapter*  
12042 of the Association for Computational Linguistics (NAACL), pp. 260–270.
- 12043 Langkilde, I. and K. Knight (1998). Generation that exploits corpus-based statistical  
12044 knowledge. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 704–  
12045 710.
- 12046 Lapata, M. (2003). Probabilistic text structuring: Experiments with sentence ordering. In  
12047 *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 545–552.
- 12048 Lappin, S. and H. J. Leass (1994). An algorithm for pronominal anaphora resolution.  
12049 *Computational linguistics* 20(4), 535–561.
- 12050 Lari, K. and S. J. Young (1990). The estimation of stochastic context-free grammars using  
12051 the inside-outside algorithm. *Computer speech & language* 4(1), 35–56.
- 12052 Lascarides, A. and N. Asher (2007). Segmented discourse representation theory: Dynamic  
12053 semantics with discourse structure. In *Computing meaning*, pp. 87–124. Springer.
- 12054 Law, E. and L. v. Ahn (2011). Human computation. *Synthesis Lectures on Artificial Intelli-*  
12055 *gence and Machine Learning* 5(3), 1–121.
- 12056 Lebret, R., D. Grangier, and M. Auli (2016). Neural text generation from structured data  
12057 with application to the biography domain. In *Proceedings of Empirical Methods for Natural*  
12058 *Language Processing (EMNLP)*, pp. 1203–1213.
- 12059 LeCun, Y. and Y. Bengio (1995). Convolutional networks for images, speech, and time  
12060 series. *The handbook of brain theory and neural networks* 3361.
- 12061 LeCun, Y., L. Bottou, G. B. Orr, and K.-R. Müller (1998). Efficient backprop. In *Neural*  
12062 *networks: Tricks of the trade*, pp. 9–50. Springer.
- 12063 Lee, C. M. and S. S. Narayanan (2005). Toward detecting emotions in spoken dialogs.  
12064 *IEEE transactions on speech and audio processing* 13(2), 293–303.
- 12065 Lee, H., A. Chang, Y. Peirsman, N. Chambers, M. Surdeanu, and D. Jurafsky (2013). De-  
12066 terministic coreference resolution based on entity-centric, precision-ranked rules. *Com-*  
12067 *putational Linguistics* 39(4), 885–916.

- 12068 Lee, H., Y. Peirsman, A. Chang, N. Chambers, M. Surdeanu, and D. Jurafsky (2011). Stan-  
12069 ford's multi-pass sieve coreference resolution system at the conll-2011 shared task. In  
12070 *Proceedings of the Conference on Natural Language Learning (CoNLL)*, pp. 28–34. Associa-  
12071 tion for Computational Linguistics.
- 12072 Lee, K., L. He, M. Lewis, and L. Zettlemoyer (2017). End-to-end neural coreference reso-  
12073 lution. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*.
- 12074 Lenat, D. B., R. V. Guha, K. Pittman, D. Pratt, and M. Shepherd (1990). Cyc: toward  
12075 programs with common sense. *Communications of the ACM* 33(8), 30–49.
- 12076 Lesk, M. (1986). Automatic sense disambiguation using machine readable dictionaries:  
12077 how to tell a pine cone from an ice cream cone. In *Proceedings of the 5th annual interna-*  
12078 *tional conference on Systems documentation*, pp. 24–26. ACM.
- 12079 Levesque, H. J., E. Davis, and L. Morgenstern (2011). The winograd schema challenge.  
12080 In *Aaaai spring symposium: Logical formalizations of commonsense reasoning*, Volume 46, pp.  
12081 47.
- 12082 Levin, E., R. Pieraccini, and W. Eckert (1998). Using markov decision process for learning  
12083 dialogue strategies. In *Acoustics, Speech and Signal Processing, 1998. Proceedings of the*  
12084 *1998 IEEE International Conference on*, Volume 1, pp. 201–204. IEEE.
- 12085 Levy, O. and Y. Goldberg (2014). Dependency-based word embeddings. In *Proceedings of*  
12086 *the Association for Computational Linguistics (ACL)*, pp. 302–308.
- 12087 Levy, O., Y. Goldberg, and I. Dagan (2015). Improving distributional similarity with  
12088 lessons learned from word embeddings. *Transactions of the Association for Computational*  
12089 *Linguistics* 3, 211–225.
- 12090 Levy, R. and C. Manning (2009). An informal introduction to computational semantics.
- 12091 Lewis, M. and M. Steedman (2013). Combined distributional and logical semantics. *Trans-*  
12092 *actions of the Association for Computational Linguistics* 1, 179–192.
- 12093 Lewis II, P. M. and R. E. Stearns (1968). Syntax-directed transduction. *Journal of the ACM*  
12094 (*JACM*) 15(3), 465–488.
- 12095 Li, J. and D. Jurafsky (2015). Do multi-sense embeddings improve natural language  
12096 understanding? In *Proceedings of Empirical Methods for Natural Language Processing*  
12097 (*EMNLP*), pp. 1722–1732.
- 12098 Li, J. and D. Jurafsky (2017). Neural net models of open-domain discourse coherence. In  
12099 *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 198–209.

- 12100 Li, J., R. Li, and E. Hovy (2014). Recursive deep models for discourse parsing. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*.
- 12102 Li, J., M.-T. Luong, and D. Jurafsky (2015). A hierarchical neural autoencoder for para-  
12103 graphs and documents. In *Proceedings of Empirical Methods for Natural Language Process-  
12104 ing (EMNLP)*.
- 12105 Li, J., T. Luong, D. Jurafsky, and E. Hovy (2015). When are tree structures necessary  
12106 for deep learning of representations? In *Proceedings of Empirical Methods for Natural  
12107 Language Processing (EMNLP)*, pp. 2304–2314.
- 12108 Li, J., W. Monroe, A. Ritter, D. Jurafsky, M. Galley, and J. Gao (2016, November). Deep  
12109 reinforcement learning for dialogue generation. In *Proceedings of the 2016 Conference on  
12110 Empirical Methods in Natural Language Processing*, Austin, Texas, pp. 1192–1202. Associa-  
12111 tion for Computational Linguistics.
- 12112 Li, Q., S. Anzaroot, W.-P. Lin, X. Li, and H. Ji (2011). Joint inference for cross-document  
12113 information extraction. In *Proceedings of the International Conference on Information and  
12114 Knowledge Management (CIKM)*, pp. 2225–2228.
- 12115 Li, Q., H. Ji, and L. Huang (2013). Joint event extraction via structured prediction with  
12116 global features. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp.  
12117 73–82.
- 12118 Liang, P., A. Bouchard-Côté, D. Klein, and B. Taskar (2006). An end-to-end discriminative  
12119 approach to machine translation. In *Proceedings of the Association for Computational  
12120 Linguistics (ACL)*, pp. 761–768.
- 12121 Liang, P., M. Jordan, and D. Klein (2009). Learning semantic correspondences with less  
12122 supervision. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 91–  
12123 99.
- 12124 Liang, P., M. I. Jordan, and D. Klein (2013). Learning dependency-based compositional  
12125 semantics. *Computational Linguistics* 39(2), 389–446.
- 12126 Liang, P. and D. Klein (2009). Online em for unsupervised models. In *Proceedings of the  
12127 North American Chapter of the Association for Computational Linguistics (NAACL)*, pp. 611–  
12128 619.
- 12129 Liang, P., S. Petrov, M. I. Jordan, and D. Klein (2007). The infinite pcfg using hierarchical  
12130 dirichlet processes. In *Proceedings of Empirical Methods for Natural Language Processing  
12131 (EMNLP)*, pp. 688–697.
- 12132 Liang, P. and C. Potts (2015). Bringing machine learning and compositional semantics  
12133 together. *Annual Review of Linguistics* 1(1), 355–376.

- 12134 Lieber, R. (2015). *Introducing morphology*. Cambridge University Press.
- 12135 Lin, D. (1998). Automatic retrieval and clustering of similar words. In *Proceedings of the 17th international conference on Computational linguistics-Volume 2*, pp. 768–774. Association for Computational Linguistics.
- 12138 Lin, J. and C. Dyer (2010). Data-intensive text processing with mapreduce. *Synthesis Lectures on Human Language Technologies* 3(1), 1–177.
- 12140 Lin, Z., M. Feng, C. N. d. Santos, M. Yu, B. Xiang, B. Zhou, and Y. Bengio (2017). A structured self-attentive sentence embedding. *arXiv preprint arXiv:1703.03130*.
- 12142 Lin, Z., M.-Y. Kan, and H. T. Ng (2009). Recognizing implicit discourse relations in the penn discourse treebank. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 343–351.
- 12145 Lin, Z., H. T. Ng, and M.-Y. Kan (2011). Automatically evaluating text coherence using discourse relations. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 997–1006.
- 12148 Lin, Z., H. T. Ng, and M. Y. Kan (2014, nov). A PDTB-styled end-to-end discourse parser. *Natural Language Engineering FirstView*, 1–34.
- 12150 Ling, W., C. Dyer, A. Black, and I. Trancoso (2015). Two/too simple adaptations of word2vec for syntax problems. In *Proceedings of the North American Chapter of the Association for Computational Linguistics (NAACL)*.
- 12153 Ling, W., T. Luís, L. Marujo, R. F. Astudillo, S. Amir, C. Dyer, A. W. Black, and I. Trancoso (2015). Finding function in form: Compositional character models for open vocabulary word representation. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*.
- 12157 Ling, W., G. Xiang, C. Dyer, A. Black, and I. Trancoso (2013). Microblogs as parallel corpora. In *Proceedings of the Association for Computational Linguistics (ACL)*.
- 12159 Ling, X., S. Singh, and D. S. Weld (2015). Design challenges for entity linking. *Transactions of the Association for Computational Linguistics* 3, 315–328.
- 12161 Linguistic Data Consortium (2005, July). ACE (automatic content extraction) English annotation guidelines for relations. Technical Report Version 5.8.3, Linguistic Data Consortium.
- 12164 Liu, B. (2015). *Sentiment Analysis: Mining Opinions, Sentiments, and Emotions*. Cambridge University Press.

- 12166 Liu, D. C. and J. Nocedal (1989). On the limited memory BFGS method for large scale  
12167 optimization. *Mathematical programming* 45(1-3), 503–528.
- 12168 Liu, Y., Q. Liu, and S. Lin (2006). Tree-to-string alignment template for statistical machine  
12169 translation. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 609–  
12170 616.
- 12171 Loper, E. and S. Bird (2002). NLTK: The natural language toolkit. In *Proceedings of the ACL-*  
12172 *02 Workshop on Effective tools and methodologies for teaching natural language processing and*  
12173 *computational linguistics-Volume 1*, pp. 63–70. Association for Computational Linguistics.
- 12174 Louis, A., A. Joshi, and A. Nenkova (2010). Discourse indicators for content selection in  
12175 summarization. In *Proceedings of the 11th Annual Meeting of the Special Interest Group on*  
12176 *Discourse and Dialogue*, pp. 147–156. Association for Computational Linguistics.
- 12177 Louis, A. and A. Nenkova (2013). What makes writing great? first experiments on article  
12178 quality prediction in the science journalism domain. *Transactions of the Association for*  
12179 *Computational Linguistics* 1, 341–352.
- 12180 Loveland, D. W. (2016). *Automated Theorem Proving: a logical basis*. Elsevier.
- 12181 Lowe, R., N. Pow, I. V. Serban, and J. Pineau (2015). The ubuntu dialogue corpus: A large  
12182 dataset for research in unstructured multi-turn dialogue systems. In *Proceedings of the*  
12183 *Special Interest Group on Discourse and Dialogue (SIGDIAL)*.
- 12184 Luo, X. (2005). On coreference resolution performance metrics. In *Proceedings of Empirical*  
12185 *Methods for Natural Language Processing (EMNLP)*, pp. 25–32.
- 12186 Luo, X., A. Ittycheriah, H. Jing, N. Kambhatla, and S. Roukos (2004). A mention-  
12187 synchronous coreference resolution algorithm based on the bell tree. In *Proceedings*  
12188 *of the Association for Computational Linguistics (ACL)*.
- 12189 Luong, M.-T., R. Socher, and C. D. Manning (2013). Better word representations with  
12190 recursive neural networks for morphology. *CoNLL-2013* 104.
- 12191 Luong, T., H. Pham, and C. D. Manning (2015). Effective approaches to attention-based  
12192 neural machine translation. In *Proceedings of Empirical Methods for Natural Language*  
12193 *Processing (EMNLP)*, pp. 1412–1421.
- 12194 Luong, T., I. Sutskever, Q. Le, O. Vinyals, and W. Zaremba (2015). Addressing the rare  
12195 word problem in neural machine translation. In *Proceedings of the Association for Compu-*  
12196 *tational Linguistics (ACL)*, pp. 11–19.
- 12197 Maas, A. L., A. Y. Hannun, and A. Y. Ng (2013). Rectifier nonlinearities improve neu-  
12198 ral network acoustic models. In *Proceedings of the International Conference on Machine*  
12199 *Learning (ICML)*.

- 12200 Mairesse, F. and M. A. Walker (2011). Controlling user perceptions of linguistic style:  
12201 Trainable generation of personality traits. *Computational Linguistics* 37(3), 455–488.
- 12202 Mani, I., M. Verhagen, B. Wellner, C. M. Lee, and J. Pustejovsky (2006). Machine learning  
12203 of temporal relations. In *Proceedings of the Association for Computational Linguistics (ACL)*,  
12204 pp. 753–760.
- 12205 Mann, W. C. and S. A. Thompson (1988). Rhetorical structure theory: Toward a functional  
12206 theory of text organization. *Text* 8(3), 243–281.
- 12207 Manning, C. D. (2015). Computational linguistics and deep learning. *Computational Lin-*  
12208 *guistics* 41(4), 701–707.
- 12209 Manning, C. D. (2016). Computational linguistics and deep learning. *Computational Lin-*  
12210 *guistics* 41(4).
- 12211 Manning, C. D., P. Raghavan, H. Schütze, et al. (2008). *Introduction to information retrieval*,  
12212 Volume 1. Cambridge university press.
- 12213 Manning, C. D. and H. Schütze (1999). *Foundations of Statistical Natural Language Process-*  
12214 *ing*. Cambridge, Massachusetts: MIT press.
- 12215 Marcu, D. (1996). Building up rhetorical structure trees. In *Proceedings of the National*  
12216 *Conference on Artificial Intelligence*, pp. 1069–1074.
- 12217 Marcu, D. (1997a). From discourse structures to text summaries. In *Proceedings of the*  
12218 *workshop on Intelligent Scalable Text Summarization*.
- 12219 Marcu, D. (1997b). From local to global coherence: A bottom-up approach to text plan-  
12220 ning. In *Proceedings of the National Conference on Artificial Intelligence (AAAI)*, pp. 629–635.
- 12221 Marcus, M. P., M. A. Marcinkiewicz, and B. Santorini (1993). Building a large annotated  
12222 corpus of English: The Penn Treebank. *Computational Linguistics* 19(2), 313–330.
- 12223 Maron, O. and T. Lozano-Pérez (1998). A framework for multiple-instance learning. In  
12224 *Neural Information Processing Systems (NIPS)*, pp. 570–576.
- 12225 Márquez, G. G. (1970). *One Hundred Years of Solitude*. Harper & Row. English translation  
12226 by Gregory Rabassa.
- 12227 Martins, A. F. T., N. A. Smith, and E. P. Xing (2009). Concise integer linear programming  
12228 formulations for dependency parsing. In *Proceedings of the Association for Computational*  
12229 *Linguistics (ACL)*, pp. 342–350.

- 12230 Martins, A. F. T., N. A. Smith, E. P. Xing, P. M. Q. Aguiar, and M. A. T. Figueiredo (2010).  
 12231 Turbo parsers: Dependency parsing by approximate variational inference. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 34–44.  
 12232
- 12233 Matsuzaki, T., Y. Miyao, and J. Tsujii (2005). Probabilistic cfg with latent annotations. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 75–82.  
 12234
- 12235 Matthiessen, C. and J. A. Bateman (1991). *Text generation and systemic-functional linguistics: experiences from English and Japanese*. Pinter Publishers.  
 12236
- 12237 McCallum, A. and W. Li (2003). Early results for named entity recognition with conditional random fields, feature induction and web-enhanced lexicons. In *Proceedings of the North American Chapter of the Association for Computational Linguistics (NAACL)*, pp. 188–191.  
 12238  
 12239  
 12240
- 12241 McCallum, A. and B. Wellner (2004). Conditional models of identity uncertainty with application to noun coreference. In *NIPS*, pp. 905–912.  
 12242
- 12243 McDonald, R., K. Crammer, and F. Pereira (2005). Online large-margin training of dependency parsers. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 91–98.  
 12244  
 12245
- 12246 McDonald, R., K. Hannan, T. Neylon, M. Wells, and J. Reynar (2007). Structured models for fine-to-coarse sentiment analysis. In *Proceedings of ACL*.  
 12247
- 12248 McDonald, R. and F. Pereira (2006). Online learning of approximate dependency parsing algorithms. In *Proceedings of the European Chapter of the Association for Computational Linguistics (EACL)*.  
 12249  
 12250
- 12251 McKeown, K. (1992). *Text generation*. Cambridge University Press.  
 12252
- 12253 McKeown, K., S. Rosenthal, K. Thadani, and C. Moore (2010). Time-efficient creation of an accurate sentence fusion corpus. In *Proceedings of the North American Chapter of the Association for Computational Linguistics (NAACL)*, pp. 317–320.  
 12254
- 12255 McKeown, K. R., R. Barzilay, D. Evans, V. Hatzivassiloglou, J. L. Klavans, A. Nenkova, C. Sable, B. Schiffman, and S. Sigelman (2002). Tracking and summarizing news on a daily basis with columbia’s newsblaster. In *Proceedings of the second international conference on Human Language Technology Research*, pp. 280–285.  
 12256  
 12257  
 12258
- 12259 McNamee, P. and H. T. Dang (2009). Overview of the tac 2009 knowledge base population track. In *Text Analysis Conference (TAC)*, Volume 17, pp. 111–113.  
 12260
- 12261 Medlock, B. and T. Briscoe (2007). Weakly supervised learning for hedge classification in scientific literature. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 992–999.  
 12262  
 12263

- 12264 Mei, H., M. Bansal, and M. R. Walter (2016). What to talk about and how? selective gen-  
12265 eration using lstms with coarse-to-fine alignment. In *Proceedings of the North American*  
12266 *Chapter of the Association for Computational Linguistics (NAACL)*, pp. 720–730.
- 12267 Merity, S., N. S. Keskar, and R. Socher (2018). Regularizing and optimizing lstm language  
12268 models. In *Proceedings of the International Conference on Learning Representations (ICLR)*.
- 12269 Merity, S., C. Xiong, J. Bradbury, and R. Socher (2017). Pointer sentinel mixture models.  
12270 In *Proceedings of the International Conference on Learning Representations (ICLR)*.
- 12271 Messud, C. (2014, June). A new ‘l'étranger’. *New York Review of Books*.
- 12272 Miao, Y. and P. Blunsom (2016). Language as a latent variable: Discrete generative mod-  
12273 els for sentence compression. In *Proceedings of Empirical Methods for Natural Language*  
12274 *Processing (EMNLP)*, pp. 319–328.
- 12275 Miao, Y., L. Yu, and P. Blunsom (2016). Neural variational inference for text processing. In  
12276 *Proceedings of the International Conference on Machine Learning (ICML)*.
- 12277 Mihalcea, R., T. A. Chklovski, and A. Kilgarriff (2004, July). The senseval-3 english lexical  
12278 sample task. In *Proceedings of SENSEVAL-3*, Barcelona, Spain, pp. 25–28. Association for  
12279 Computational Linguistics.
- 12280 Mihalcea, R. and D. Radev (2011). *Graph-based natural language processing and information*  
12281 *retrieval*. Cambridge University Press.
- 12282 Mikolov, T., K. Chen, G. Corrado, and J. Dean (2013). Efficient estimation of word repre-  
12283 sentations in vector space. In *Proceedings of International Conference on Learning Represen-*  
12284 *tations*.
- 12285 Mikolov, T., A. Deoras, D. Povey, L. Burget, and J. Cernocky (2011). Strategies for train-  
12286 ing large scale neural network language models. In *Automatic Speech Recognition and*  
12287 *Understanding (ASRU), 2011 IEEE Workshop on*, pp. 196–201. IEEE.
- 12288 Mikolov, T., M. Karafiát, L. Burget, J. Cernocký, and S. Khudanpur (2010). Recurrent  
12289 neural network based language model. In *INTERSPEECH*, pp. 1045–1048.
- 12290 Mikolov, T., I. Sutskever, K. Chen, G. S. Corrado, and J. Dean (2013). Distributed rep-  
12291 resentations of words and phrases and their compositionality. In *Advances in Neural*  
12292 *Information Processing Systems*, pp. 3111–3119.
- 12293 Mikolov, T., W.-t. Yih, and G. Zweig (2013). Linguistic regularities in continuous space  
12294 word representations. In *Proceedings of the North American Chapter of the Association for*  
12295 *Computational Linguistics (NAACL)*, pp. 746–751.

- 12296 Mikolov, T. and G. Zweig. Context dependent recurrent neural network language model.  
 12297 In *Proceedings of Spoken Language Technology (SLT)*, pp. 234–239.
- 12298 Miller, G. A., G. A. Heise, and W. Lichten (1951). The intelligibility of speech as a function  
 12299 of the context of the test materials. *Journal of experimental psychology* 41(5), 329.
- 12300 Miller, M., C. Sathi, D. Wiesenthal, J. Leskovec, and C. Potts (2011). Sentiment flow  
 12301 through hyperlink networks. In *Proceedings of the International Conference on Web and*  
 12302 *Social Media (ICWSM)*.
- 12303 Miller, S., J. Guinness, and A. Zamanian (2004). Name tagging with word clusters and  
 12304 discriminative training. In *Proceedings of the North American Chapter of the Association for*  
 12305 *Computational Linguistics (NAACL)*, pp. 337–342.
- 12306 Milne, D. and I. H. Witten (2008). Learning to link with wikipedia. In *Proceedings of the*  
 12307 *International Conference on Information and Knowledge Management (CIKM)*, pp. 509–518.  
 12308 ACM.
- 12309 Miltsakaki, E. and K. Kukich (2004). Evaluation of text coherence for electronic essay  
 12310 scoring systems. *Natural Language Engineering* 10(1), 25–55.
- 12311 Minka, T. P. (1999). From hidden markov models to linear dynamical systems. Tech. Rep.  
 12312 531, Vision and Modeling Group of Media Lab, MIT.
- 12313 Minsky, M. (1974). A framework for representing knowledge. Technical Report 306, MIT  
 12314 AI Laboratory.
- 12315 Minsky, M. and S. Papert (1969). *Perceptrons*. MIT press.
- 12316 Mintz, M., S. Bills, R. Snow, and D. Jurafsky (2009). Distant supervision for relation extrac-  
 12317 tion without labeled data. In *Proceedings of the Association for Computational Linguistics*  
 12318 (*ACL*), pp. 1003–1011.
- 12319 Mirza, P., R. Sprugnoli, S. Tonelli, and M. Speranza (2014). Annotating causality in the  
 12320 tempeval-3 corpus. In *Proceedings of the EACL 2014 Workshop on Computational Ap-*  
 12321 *proaches to Causality in Language (CAtoCL)*, pp. 10–19.
- 12322 Misra, D. K. and Y. Artzi (2016). Neural shift-reduce ccg semantic parsing. In *Proceedings*  
 12323 *of Empirical Methods for Natural Language Processing (EMNLP)*.
- 12324 Mitchell, J. and M. Lapata (2010). Composition in distributional models of semantics.  
 12325 *Cognitive Science* 34(8), 1388–1429.
- 12326 Miwa, M. and M. Bansal (2016). End-to-end relation extraction using lstms on sequences  
 12327 and tree structures. In *Proceedings of the Association for Computational Linguistics (ACL)*,  
 12328 pp. 1105–1116.

- 12329 Mnih, A. and G. Hinton (2007). Three new graphical models for statistical language mod-  
12330 eling. In *Proceedings of the 24th international conference on Machine learning*, ICML '07,  
12331 New York, NY, USA, pp. 641–648. ACM.
- 12332 Mnih, A. and G. E. Hinton (2008). A scalable hierarchical distributed language model. In  
12333 *Neural Information Processing Systems (NIPS)*, pp. 1081–1088.
- 12334 Mnih, A. and Y. W. Teh (2012). A fast and simple algorithm for training neural probabilis-  
12335 tic language models. In *Proceedings of the International Conference on Machine Learning*  
12336 (ICML).
- 12337 Mohammad, S. M. and P. D. Turney (2013). Crowdsourcing a word–emotion association  
12338 lexicon. *Computational Intelligence* 29(3), 436–465.
- 12339 Mohri, M., F. Pereira, and M. Riley (2002). Weighted finite-state transducers in speech  
12340 recognition. *Computer Speech & Language* 16(1), 69–88.
- 12341 Mohri, M., A. Rostamizadeh, and A. Talwalkar (2012). *Foundations of machine learning*.  
12342 MIT press.
- 12343 Montague, R. (1973). The proper treatment of quantification in ordinary english. In *Ap-  
12344 proaches to natural language*, pp. 221–242. Springer.
- 12345 Moore, J. D. and C. L. Paris (1993, dec). Planning text for advisory dialogues: Capturing  
12346 intentional and rhetorical information. *Comput. Linguist.* 19(4), 651–694.
- 12347 Morante, R. and E. Blanco (2012). \*sem 2012 shared task: Resolving the scope and fo-  
12348 cus of negation. In *Proceedings of the First Joint Conference on Lexical and Computational  
12349 Semantics-Volume 1: Proceedings of the main conference and the shared task, and Volume 2:  
12350 Proceedings of the Sixth International Workshop on Semantic Evaluation*, pp. 265–274. Asso-  
12351 ciation for Computational Linguistics.
- 12352 Morante, R. and W. Daelemans (2009). Learning the scope of hedge cues in biomedical  
12353 texts. In *Proceedings of the Workshop on Current Trends in Biomedical Natural Language  
12354 Processing*, pp. 28–36. Association for Computational Linguistics.
- 12355 Morante, R. and C. Sporleder (2012). Modality and negation: An introduction to the  
12356 special issue. *Computational linguistics* 38(2), 223–260.
- 12357 Mostafazadeh, N., A. Grelish, N. Chambers, J. Allen, and L. Vanderwende (2016, June).  
12358 Caters: Causal and temporal relation scheme for semantic annotation of event struc-  
12359 tures. In *Proceedings of the Fourth Workshop on Events*, San Diego, California, pp. 51–61.  
12360 Association for Computational Linguistics.

- 12361 Mueller, T., H. Schmid, and H. Schütze (2013). Efficient higher-order CRFs for morpholog-  
 12362 ical tagging. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*,  
 12363 pp. 322–332.
- 12364 Müller, C. and M. Strube (2006). Multi-level annotation of linguistic data with mmax2.  
 12365 *Corpus technology and language pedagogy: New resources, new tools, new methods 3*, 197–  
 12366 214.
- 12367 Muralidharan, A. and M. A. Hearst (2013). Supporting exploratory text analysis in litera-  
 12368 ture study. *Literary and linguistic computing* 28(2), 283–295.
- 12369 Murphy, K. P. (2012). *Machine Learning: A Probabilistic Perspective*. The MIT Press.
- 12370 Nakagawa, T., K. Inui, and S. Kurohashi (2010). Dependency tree-based sentiment classi-  
 12371 fication using crfs with hidden variables. In *Proceedings of the North American Chapter of  
 12372 the Association for Computational Linguistics (NAACL)*, pp. 786–794.
- 12373 Nakazawa, T., M. Yaguchi, K. Uchimoto, M. Utiyama, E. Sumita, S. Kurohashi, and H. Isa-  
 12374 hara (2016). ASPEC: Asian scientific paper excerpt corpus. In *Proceedings of the Language  
 12375 Resources and Evaluation Conference*, pp. 2204–2208.
- 12376 Navigli, R. (2009). Word sense disambiguation: A survey. *ACM Computing Surveys  
 (CSUR)* 41(2), 10.
- 12378 Neal, R. M. and G. E. Hinton (1998). A view of the em algorithm that justifies incremental,  
 12379 sparse, and other variants. In *Learning in graphical models*, pp. 355–368. Springer.
- 12380 Nenkova, A. and K. McKeown (2012). A survey of text summarization techniques. In  
 12381 *Mining text data*, pp. 43–76. Springer.
- 12382 Neubig, G. (2017). Neural machine translation and sequence-to-sequence models: A tu-  
 12383 torial. *arXiv preprint arXiv:1703.01619*.
- 12384 Neubig, G., C. Dyer, Y. Goldberg, A. Matthews, W. Ammar, A. Anastasopoulos, M. Balles-  
 12385 teros, D. Chiang, D. Clothiaux, T. Cohn, K. Duh, M. Faruqui, C. Gan, D. Garrette,  
 12386 Y. Ji, L. Kong, A. Kuncoro, G. Kumar, C. Malaviya, P. Michel, Y. Oda, M. Richardson,  
 12387 N. Saphra, S. Swayamdipta, and P. Yin (2017). Dynet: The dynamic neural network  
 12388 toolkit.
- 12389 Neubig, G., Y. Goldberg, and C. Dyer (2017). On-the-fly operation batching in dynamic  
 12390 computation graphs. In *Neural Information Processing Systems (NIPS)*.
- 12391 Neubig, G., M. Sperber, X. Wang, M. Felix, A. Matthews, S. Padmanabhan, Y. Qi, D. S.  
 12392 Sachan, P. Arthur, P. Godard, J. Hewitt, R. Riad, and L. Wang (2018, March). XNMT:  
 12393 The extensible neural machine translation toolkit. In *Conference of the Association for  
 12394 Machine Translation in the Americas (AMTA) Open Source Software Showcase*, Boston.

- 12395 Neuhaus, P. and N. Bröker (1997). The complexity of recognition of linguistically adequate  
12396 dependency grammars. In *eacl*, pp. 337–343.
- 12397 Newman, D., C. Chemudugunta, and P. Smyth (2006). Statistical entity-topic models. In  
12398 *Proceedings of Knowledge Discovery and Data Mining (KDD)*, pp. 680–686.
- 12399 Ng, V. (2010). Supervised noun phrase coreference research: The first fifteen years. In  
12400 *Proceedings of the 48th annual meeting of the association for computational linguistics*, pp.  
12401 1396–1411. Association for Computational Linguistics.
- 12402 Nguyen, D. and A. S. Dogruöz (2013). Word level language identification in online multi-  
12403 lingual communication. In *Proceedings of Empirical Methods for Natural Language Process-  
12404 ing (EMNLP)*.
- 12405 Nguyen, D. T. and S. Joty (2017). A neural local coherence model. In *Proceedings of the  
12406 Association for Computational Linguistics (ACL)*, pp. 1320–1330.
- 12407 Nigam, K., A. K. McCallum, S. Thrun, and T. Mitchell (2000). Text classification from  
12408 labeled and unlabeled documents using em. *Machine learning* 39(2-3), 103–134.
- 12409 Nirenburg, S. and Y. Wilks (2001). What's in a symbol: ontology, representation and lan-  
12410 guage. *Journal of Experimental & Theoretical Artificial Intelligence* 13(1), 9–23.
- 12411 Nivre, J. (2008). Algorithms for deterministic incremental dependency parsing. *Compu-  
12412 tational Linguistics* 34(4), 513–553.
- 12413 Nivre, J., M.-C. de Marneffe, F. Ginter, Y. Goldberg, J. Hajič, C. D. Manning, R. McDonald,  
12414 S. Petrov, S. Pyysalo, N. Silveira, R. Tsarfaty, and D. Zeman (2016, may). Universal de-  
12415 pendencies v1: A multilingual treebank collection. In N. C. C. Chair), K. Choukri, T. De-  
12416 clerck, S. Goggi, M. Grobelnik, B. Maegaard, J. Mariani, H. Mazo, A. Moreno, J. Odijk,  
12417 and S. Piperidis (Eds.), *Proceedings of the Tenth International Conference on Language Re-  
12418 sources and Evaluation (LREC 2016)*, Paris, France. European Language Resources Asso-  
12419 ciation (ELRA).
- 12420 Nivre, J. and J. Nilsson (2005). Pseudo-projective dependency parsing. In *Proceedings of the  
12421 43rd Annual Meeting on Association for Computational Linguistics*, pp. 99–106. Association  
12422 for Computational Linguistics.
- 12423 Novikoff, A. B. (1962). On convergence proofs on perceptrons. In *Proceedings of the Sym-  
12424 posium on the Mathematical Theory of Automata*, Volume 12, pp. 615—622.
- 12425 Och, F. J. and H. Ney (2003). A systematic comparison of various statistical alignment  
12426 models. *Computational linguistics* 29(1), 19–51.

- 12427 O'Connor, B., M. Krieger, and D. Ahn (2010). Tweetmotif: Exploratory search and topic  
12428 summarization for twitter. In *Proceedings of the International Conference on Web and Social  
12429 Media (ICWSM)*, pp. 384–385.
- 12430 Oflazer, K. and İ. Kuruöz (1994). Tagging and morphological disambiguation of turkish  
12431 text. In *Proceedings of the fourth conference on Applied natural language processing*, pp. 144–  
12432 149. Association for Computational Linguistics.
- 12433 Ohta, T., Y. Tateisi, and J.-D. Kim (2002). The genia corpus: An annotated research abstract  
12434 corpus in molecular biology domain. In *Proceedings of the second international conference  
12435 on Human Language Technology Research*, pp. 82–86. Morgan Kaufmann Publishers Inc.
- 12436 Onishi, T., H. Wang, M. Bansal, K. Gimpel, and D. McAllester (2016). Who did what: A  
12437 large-scale person-centered cloze dataset. In *Proceedings of Empirical Methods for Natural  
12438 Language Processing (EMNLP)*, pp. 2230–2235.
- 12439 Owoputi, O., B. O'Connor, C. Dyer, K. Gimpel, N. Schneider, and N. A. Smith (2013).  
12440 Improved part-of-speech tagging for online conversational text with word clusters. In  
12441 *Proceedings of the North American Chapter of the Association for Computational Linguistics  
(NAACL)*, pp. 380–390.
- 12443 Packard, W., E. M. Bender, J. Read, S. Oepen, and R. Dridan (2014). Simple negation  
12444 scope resolution through deep parsing: A semantic solution to a semantic problem. In  
12445 *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 69–78.
- 12446 Paice, C. D. (1990). Another stemmer. In *ACM SIGIR Forum*, Volume 24, pp. 56–61.
- 12447 Pak, A. and P. Paroubek (2010). Twitter as a corpus for sentiment analysis and opinion  
12448 mining. In *LREC*, Volume 10, pp. 1320–1326.
- 12449 Palmer, F. R. (2001). *Mood and modality*. Cambridge University Press.
- 12450 Palmer, M., D. Gildea, and P. Kingsbury (2005). The proposition bank: An annotated  
12451 corpus of semantic roles. *Computational linguistics* 31(1), 71–106.
- 12452 Pan, S. J. and Q. Yang (2010). A survey on transfer learning. *IEEE Transactions on knowledge  
12453 and data engineering* 22(10), 1345–1359.
- 12454 Pan, X., T. Cassidy, U. Hermjakob, H. Ji, and K. Knight (2015). Unsupervised entity linking  
12455 with abstract meaning representation. In *Proceedings of the North American Chapter of the  
12456 Association for Computational Linguistics (NAACL)*, pp. 1130–1139.
- 12457 Pang, B. and L. Lee (2004). A sentimental education: Sentiment analysis using subjectivity  
12458 summarization based on minimum cuts. In *Proceedings of the Association for Compu-  
12459 tational Linguistics (ACL)*, pp. 271–278.

- 12460 Pang, B. and L. Lee (2005). Seeing stars: Exploiting class relationships for sentiment categorization with respect to rating scales. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 115–124.
- 12463 Pang, B. and L. Lee (2008). Opinion mining and sentiment analysis. *Foundations and trends in information retrieval* 2(1-2), 1–135.
- 12465 Pang, B., L. Lee, and S. Vaithyanathan (2002). Thumbs up?: sentiment classification using machine learning techniques. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 79–86.
- 12468 Papineni, K., S. Roukos, T. Ward, and W.-J. Zhu (2002). Bleu: a method for automatic evaluation of machine translation. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 311–318.
- 12471 Park, J. and C. Cardie (2012). Improving implicit discourse relation recognition through feature set optimization. In *Proceedings of the Special Interest Group on Discourse and Dialogue (SIGDIAL)*, pp. 108–112.
- 12474 Parsons, T. (1990). *Events in the Semantics of English*, Volume 5. MIT Press.
- 12475 Pascanu, R., T. Mikolov, and Y. Bengio (2013). On the difficulty of training recurrent neural networks. In *Proceedings of the International Conference on Machine Learning (ICML)*, pp. 1310–1318.
- 12478 Paul, M., M. Federico, and S. Stüker (2010). Overview of the iwslt 2010 evaluation campaign. In *International Workshop on Spoken Language Translation (IWSLT) 2010*.
- 12480 Pedersen, T., S. Patwardhan, and J. Michelizzi (2004). Wordnet::similarity - measuring the relatedness of concepts. In *Proceedings of the North American Chapter of the Association for Computational Linguistics (NAACL)*, pp. 38–41.
- 12483 Pedregosa, F., G. Varoquaux, A. Gramfort, V. Michel, B. Thirion, O. Grisel, M. Blondel, P. Prettenhofer, R. Weiss, V. Dubourg, J. Vanderplas, A. Passos, D. Cournapeau, M. Brucher, M. Perrot, and E. Duchesnay (2011). Scikit-learn: Machine learning in Python. *Journal of Machine Learning Research* 12, 2825–2830.
- 12487 Pei, W., T. Ge, and B. Chang (2015). An effective neural network model for graph-based dependency parsing. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 313–322.
- 12490 Peldszus, A. and M. Stede (2013). From argument diagrams to argumentation mining in texts: A survey. *International Journal of Cognitive Informatics and Natural Intelligence (IJCINI)* 7(1), 1–31.

- 12493 Peldszus, A. and M. Stede (2015). An annotated corpus of argumentative microtexts. In  
 12494 *Proceedings of the First Conference on Argumentation*.
- 12495 Peng, F., F. Feng, and A. McCallum (2004). Chinese segmentation and new word detec-  
 12496 tion using conditional random fields. In *Proceedings of the International Conference on*  
 12497 *Computational Linguistics (COLING)*, pp. 562.
- 12498 Pennington, J., R. Socher, and C. Manning (2014). Glove: Global vectors for word repre-  
 12499 sentation. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*,  
 12500 pp. 1532–1543.
- 12501 Pereira, F. and Y. Schabes (1992). Inside-outside reestimation from partially bracketed  
 12502 corpora. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 128–  
 12503 135.
- 12504 Pereira, F. C. N. and S. M. Shieber (2002). *Prolog and natural-language analysis*. Microtome  
 12505 Publishing.
- 12506 Peters, M. E., M. Neumann, M. Iyyer, M. Gardner, C. Clark, K. Lee, and L. Zettlemoyer  
 12507 (2018). Deep contextualized word representations. In *Proceedings of the North American*  
 12508 *Chapter of the Association for Computational Linguistics (NAACL)*.
- 12509 Peterson, W. W., T. G. Birdsall, and W. C. Fox (1954). The theory of signal detectability.  
 12510 *Transactions of the IRE professional group on information theory* 4(4), 171–212.
- 12511 Petrov, S., L. Barrett, R. Thibaux, and D. Klein (2006). Learning accurate, compact, and in-  
 12512 terpretable tree annotation. In *Proceedings of the Association for Computational Linguistics*  
 12513 (*ACL*).
- 12514 Petrov, S., D. Das, and R. McDonald (2012, May). A universal part-of-speech tagset. In  
 12515 *Proceedings of LREC*.
- 12516 Petrov, S. and R. McDonald (2012). Overview of the 2012 shared task on parsing the web.  
 12517 In *Notes of the First Workshop on Syntactic Analysis of Non-Canonical Language (SANCL)*,  
 12518 Volume 59.
- 12519 Pinker, S. (2003). *The language instinct: How the mind creates language*. Penguin UK.
- 12520 Pinter, Y., R. Guthrie, and J. Eisenstein (2017). Mimicking word embeddings using  
 12521 subword RNNs. In *Proceedings of Empirical Methods for Natural Language Processing*  
 12522 (*EMNLP*).
- 12523 Pitler, E., A. Louis, and A. Nenkova (2009). Automatic sense prediction for implicit dis-  
 12524 course relations in text. In *Proceedings of the Association for Computational Linguistics*  
 12525 (*ACL*).

- 12526 Pitler, E. and A. Nenkova (2009). Using syntax to disambiguate explicit discourse con-  
12527 nectives in text. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp.  
12528 13–16.
- 12529 Pitler, E., M. Raghupathy, H. Mehta, A. Nenkova, A. Lee, and A. Joshi (2008). Easily iden-  
12530 tifiable discourse relations. In *Proceedings of the International Conference on Computational  
12531 Linguistics (COLING)*, pp. 87–90.
- 12532 Plank, B., A. Søgaard, and Y. Goldberg (2016). Multilingual part-of-speech tagging with  
12533 bidirectional long short-term memory models and auxiliary loss. In *Proceedings of the  
12534 Association for Computational Linguistics (ACL)*.
- 12535 Poesio, M., R. Stevenson, B. Di Eugenio, and J. Hitzeman (2004). Centering: A parametric  
12536 theory and its instantiations. *Computational linguistics* 30(3), 309–363.
- 12537 Polanyi, L. and A. Zaenen (2006). Contextual valence shifters. In *Computing attitude and  
12538 affect in text: Theory and applications*. Springer.
- 12539 Ponzetto, S. P. and M. Strube (2006). Exploiting semantic role labeling, wordnet and  
12540 wikipedia for coreference resolution. In *Proceedings of the North American Chapter of  
12541 the Association for Computational Linguistics (NAACL)*, pp. 192–199.
- 12542 Ponzetto, S. P. and M. Strube (2007). Knowledge derived from wikipedia for computing  
12543 semantic relatedness. *Journal of Artificial Intelligence Research* 30, 181–212.
- 12544 Poon, H. and P. Domingos (2008). Joint unsupervised coreference resolution with markov  
12545 logic. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp.  
12546 650–659.
- 12547 Poon, H. and P. Domingos (2009). Unsupervised semantic parsing. In *Proceedings of Em-  
12548 pirical Methods for Natural Language Processing (EMNLP)*, pp. 1–10.
- 12549 Popel, M., D. Marecek, J. Stepánek, D. Zeman, and Z. Zabokrtský (2013). Coordination  
12550 structures in dependency treebanks. In *Proceedings of the Association for Computational  
12551 Linguistics (ACL)*, pp. 517–527.
- 12552 Popescu, A.-M., O. Etzioni, and H. Kautz (2003). Towards a theory of natural language  
12553 interfaces to databases. In *Proceedings of Intelligent User Interfaces (IUI)*, pp. 149–157.
- 12554 Poplack, S. (1980). Sometimes i'll start a sentence in spanish y termino en español: toward  
12555 a typology of code-switching1. *Linguistics* 18(7-8), 581–618.
- 12556 Porter, M. F. (1980). An algorithm for suffix stripping. *Program* 14(3), 130–137.

- 12557 Prabhakaran, V., O. Rambow, and M. Diab (2010). Automatic committed belief tagging.  
 12558 In *Proceedings of the International Conference on Computational Linguistics (COLING)*, pp.  
 12559 1014–1022.
- 12560 Pradhan, S., X. Luo, M. Recasens, E. Hovy, V. Ng, and M. Strube (2014). Scoring corefer-  
 12561 ence partitions of predicted mentions: A reference implementation. In *Proceedings of the*  
 12562 *Association for Computational Linguistics (ACL)*, pp. 30–35.
- 12563 Pradhan, S., L. Ramshaw, M. Marcus, M. Palmer, R. Weischedel, and N. Xue (2011).  
 12564 CoNLL-2011 shared task: Modeling unrestricted coreference in OntoNotes. In *Proceed-  
 12565 ings of the Fifteenth Conference on Computational Natural Language Learning: Shared Task*,  
 12566 pp. 1–27. Association for Computational Linguistics.
- 12567 Pradhan, S., W. Ward, K. Hacioglu, J. H. Martin, and D. Jurafsky (2005). Semantic role  
 12568 labeling using different syntactic views. In *Proceedings of the Association for Computational  
 12569 Linguistics (ACL)*, pp. 581–588.
- 12570 Prasad, R., N. Dinesh, A. Lee, E. Miltsakaki, L. Robaldo, A. Joshi, and B. Webber (2008).  
 12571 The Penn Discourse Treebank 2.0. In *Proceedings of LREC*.
- 12572 Punyakanok, V., D. Roth, and W.-t. Yih (2008). The importance of syntactic parsing and  
 12573 inference in semantic role labeling. *Computational Linguistics* 34(2), 257–287.
- 12574 Pustejovsky, J., P. Hanks, R. Sauri, A. See, R. Gaizauskas, A. Setzer, D. Radev, B. Sundheim,  
 12575 D. Day, L. Ferro, et al. (2003). The timebank corpus. In *Corpus linguistics*, Volume 2003,  
 12576 pp. 40. Lancaster, UK.
- 12577 Pustejovsky, J., B. Ingria, R. Sauri, J. Castano, J. Littman, R. Gaizauskas, A. Setzer, G. Katz,  
 12578 and I. Mani (2005). The specification language timeml. In *The language of time: A reader*,  
 12579 pp. 545–557. Oxford University Press.
- 12580 Qin, L., Z. Zhang, H. Zhao, Z. Hu, and E. Xing (2017). Adversarial connective-exploiting  
 12581 networks for implicit discourse relation classification. In *Proceedings of the Association  
 12582 for Computational Linguistics (ACL)*, pp. 1006–1017.
- 12583 Qiu, G., B. Liu, J. Bu, and C. Chen (2011). Opinion word expansion and target extraction  
 12584 through double propagation. *Computational linguistics* 37(1), 9–27.
- 12585 Quattoni, A., S. Wang, L.-P. Morency, M. Collins, and T. Darrell (2007). Hidden conditional  
 12586 random fields. *IEEE transactions on pattern analysis and machine intelligence* 29(10).
- 12587 Rahman, A. and V. Ng (2011). Narrowing the modeling gap: a cluster-ranking approach  
 12588 to coreference resolution. *Journal of Artificial Intelligence Research* 40, 469–521.

- 12589 Rajpurkar, P., J. Zhang, K. Lopyrev, and P. Liang (2016). Squad: 100,000+ questions for  
12590 machine comprehension of text. In *Proceedings of Empirical Methods for Natural Language*  
12591 *Processing (EMNLP)*, pp. 2383–2392.
- 12592 Ranzato, M., S. Chopra, M. Auli, and W. Zaremba (2016). Sequence level training with  
12593 recurrent neural networks. In *Proceedings of the International Conference on Learning Rep-*  
12594 *resentations (ICLR)*.
- 12595 Rao, D., D. Yarowsky, A. Shreevats, and M. Gupta (2010). Classifying latent user attributes  
12596 in twitter. In *Proceedings of Workshop on Search and mining user-generated contents*.
- 12597 Ratinov, L. and D. Roth (2009). Design challenges and misconceptions in named entity  
12598 recognition. In *Proceedings of the Thirteenth Conference on Computational Natural Language*  
12599 *Learning*, pp. 147–155. Association for Computational Linguistics.
- 12600 Ratinov, L., D. Roth, D. Downey, and M. Anderson (2011). Local and global algorithms  
12601 for disambiguation to wikipedia. In *Proceedings of the Association for Computational Lin-*  
12602 *guistics (ACL)*, pp. 1375–1384.
- 12603 Ratliff, N. D., J. A. Bagnell, and M. Zinkevich (2007). (approximate) subgradient methods  
12604 for structured prediction. In *Proceedings of Artificial Intelligence and Statistics (AISTATS)*,  
12605 pp. 380–387.
- 12606 Ratnaparkhi, A. (1996). A maximum entropy model for part-of-speech tagging. In *emnlp*,  
12607 pp. 133–142.
- 12608 Ratnaparkhi, A., J. Reynar, and S. Roukos (1994). A maximum entropy model for preposi-  
12609 tional phrase attachment. In *Proceedings of the workshop on Human Language Technology*,  
12610 pp. 250–255. Association for Computational Linguistics.
- 12611 Read, J. (2005). Using emoticons to reduce dependency in machine learning techniques for  
12612 sentiment classification. In *Proceedings of the ACL student research workshop*, pp. 43–48.  
12613 Association for Computational Linguistics.
- 12614 Reisinger, D., R. Rudinger, F. Ferraro, C. Harman, K. Rawlins, and B. V. Durme (2015).  
12615 Semantic proto-roles. *Transactions of the Association for Computational Linguistics* 3, 475–  
12616 488.
- 12617 Reisinger, J. and R. J. Mooney (2010). Multi-prototype vector-space models of word mean-  
12618 ing. In *Proceedings of the North American Chapter of the Association for Computational Lin-*  
12619 *guistics (NAACL)*, pp. 109–117.
- 12620 Reiter, E. and R. Dale (2000). *Building natural language generation systems*. Cambridge  
12621 university press.

- 12622 Resnik, P., M. B. Olsen, and M. Diab (1999). The bible as a parallel corpus: Annotating the  
12623 'book of 2000 tongues'. *Computers and the Humanities* 33(1-2), 129–153.
- 12624 Resnik, P. and N. A. Smith (2003). The web as a parallel corpus. *Computational Linguistics*  
12625 29(3), 349–380.
- 12626 Ribeiro, F. N., M. Araújo, P. Gonçalves, M. A. Gonçalves, and F. Benevenuto (2016).  
12627 Sentibench-a benchmark comparison of state-of-the-practice sentiment analysis meth-  
12628 ods. *EPJ Data Science* 5(1), 1–29.
- 12629 Richardson, M., C. J. Burges, and E. Renshaw (2013). MCTest: A challenge dataset for  
12630 the open-domain machine comprehension of text. In *Proceedings of Empirical Methods for*  
12631 *Natural Language Processing (EMNLP)*, pp. 193–203.
- 12632 Riedel, S., L. Yao, and A. McCallum (2010). Modeling relations and their mentions without  
12633 labeled text. In *Proceedings of the European Conference on Machine Learning and Principles*  
12634 *and Practice of Knowledge Discovery in Databases (ECML)*, pp. 148–163.
- 12635 Riedl, M. O. and R. M. Young (2010). Narrative planning: Balancing plot and character.  
12636 *Journal of Artificial Intelligence Research* 39, 217–268.
- 12637 Rieser, V. and O. Lemon (2011). *Reinforcement learning for adaptive dialogue systems: a data-  
12638 driven methodology for dialogue management and natural language generation*. Springer Sci-  
12639 ence & Business Media.
- 12640 Riloff, E. (1996). Automatically generating extraction patterns from untagged text. In  
12641 *Proceedings of the national conference on artificial intelligence*, pp. 1044–1049.
- 12642 Riloff, E. and J. Wiebe (2003). Learning extraction patterns for subjective expressions. In  
12643 *Proceedings of the 2003 conference on Empirical methods in natural language processing*, pp.  
12644 105–112. Association for Computational Linguistics.
- 12645 Ritchie, G. (2001). Current directions in computational humour. *Artificial Intelligence Re-  
12646 view* 16(2), 119–135.
- 12647 Ritter, A., C. Cherry, and W. B. Dolan (2011). Data-driven response generation in social  
12648 media. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp.  
12649 583–593.
- 12650 Ritter, A., S. Clark, Mausam, and O. Etzioni (2011). Named entity recognition in tweets:  
12651 an experimental study. In *Proceedings of EMNLP*.
- 12652 Roark, B., M. Saracclar, and M. Collins (2007). Discriminative  $i_1 n_i / i_2$ -gram language  
12653 modeling. *Computer Speech & Language* 21(2), 373–392.

- 12654 Robert, C. and G. Casella (2013). *Monte Carlo statistical methods*. Springer Science & Busi-  
12655 ness Media.
- 12656 Rosenfeld, R. (1996). A maximum entropy approach to adaptive statistical language mod-  
12657 elling. *Computer Speech & Language* 10(3), 187–228.
- 12658 Ross, S., G. Gordon, and D. Bagnell (2011). A reduction of imitation learning and struc-  
12659 tured prediction to no-regret online learning. In *Proceedings of Artificial Intelligence and*  
12660 *Statistics (AISTATS)*, pp. 627–635.
- 12661 Roy, N., J. Pineau, and S. Thrun (2000). Spoken dialogue management using probabilistic  
12662 reasoning. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 93–  
12663 100.
- 12664 Rudnicky, A. and W. Xu (1999). An agenda-based dialog management architecture for  
12665 spoken language systems. In *IEEE Automatic Speech Recognition and Understanding Work-  
12666 shop*, Volume 13.
- 12667 Rush, A. M., S. Chopra, and J. Weston (2015). A neural attention model for abstractive sen-  
12668 tence summarization. In *Proceedings of Empirical Methods for Natural Language Processing  
(EMNLP)*, pp. 379–389.
- 12670 Rush, A. M., D. Sontag, M. Collins, and T. Jaakkola (2010). On dual decomposition and  
12671 linear programming relaxations for natural language processing. In *Proceedings of Em-  
12672 pirical Methods for Natural Language Processing (EMNLP)*, pp. 1–11.
- 12673 Russell, S. J. and P. Norvig (2009). *Artificial intelligence: a modern approach* (3rd ed.). Prentice  
12674 Hall.
- 12675 Rutherford, A., V. Demberg, and N. Xue (2017). A systematic study of neural discourse  
12676 models for implicit discourse relation. In *Proceedings of the European Chapter of the Asso-  
12677 ciation for Computational Linguistics (EACL)*, pp. 281–291.
- 12678 Rutherford, A. T. and N. Xue (2014). Discovering implicit discourse relations through  
12679 brown cluster pair representation and coreference patterns. In *Proceedings of the Euro-  
12680 pean Chapter of the Association for Computational Linguistics (EACL)*.
- 12681 Sag, I. A., T. Baldwin, F. Bond, A. Copestate, and D. Flickinger (2002). Multiword expres-  
12682 sions: A pain in the neck for nlp. In *International Conference on Intelligent Text Processing  
and Computational Linguistics*, pp. 1–15. Springer.
- 12684 Sagae, K. (2009). Analysis of discourse structure with syntactic dependencies and data-  
12685 driven shift-reduce parsing. In *Proceedings of the 11th International Conference on Parsing  
Technologies*, pp. 81–84.

- 12687 Santos, C. D. and B. Zadrozny (2014). Learning character-level representations for part-of-  
 12688 speech tagging. In *Proceedings of the International Conference on Machine Learning (ICML)*,  
 12689 pp. 1818–1826.
- 12690 Sato, M.-A. and S. Ishii (2000). On-line em algorithm for the normalized gaussian network.  
 12691 *Neural computation* 12(2), 407–432.
- 12692 Saurí, R. and J. Pustejovsky (2009). Factbank: a corpus annotated with event factuality.  
 12693 *Language resources and evaluation* 43(3), 227.
- 12694 Saxe, A. M., J. L. McClelland, and S. Ganguli (2014). Exact solutions to the nonlinear  
 12695 dynamics of learning in deep linear neural networks. In *Proceedings of the International  
 12696 Conference on Learning Representations (ICLR)*.
- 12697 Schank, R. C. and R. Abelson (1977). *Scripts, goals, plans, and understanding*. Hillsdale, NJ:  
 12698 Erlbaum.
- 12699 Schapire, R. E. and Y. Singer (2000). Boostexter: A boosting-based system for text catego-  
 12700 rization. *Machine learning* 39(2-3), 135–168.
- 12701 Schaul, T., S. Zhang, and Y. LeCun (2013). No more pesky learning rates. In *Proceedings of  
 12702 the International Conference on Machine Learning (ICML)*, pp. 343–351.
- 12703 Schnabel, T., I. Labutov, D. Mimno, and T. Joachims (2015). Evaluation methods for un-  
 12704 supervised word embeddings. In *Proceedings of Empirical Methods for Natural Language  
 12705 Processing (EMNLP)*, pp. 298–307.
- 12706 Schneider, N., J. Flanigan, and T. O’Gorman (2015). The logic of amr: Practical, unified,  
 12707 graph-based sentence semantics for nlp. In *Proceedings of the North American Chapter of  
 12708 the Association for Computational Linguistics (NAACL)*, pp. 4–5.
- 12709 Schütze, H. (1998). Automatic word sense discrimination. *Computational linguistics* 24(1),  
 12710 97–123.
- 12711 Schwarm, S. E. and M. Ostendorf (2005). Reading level assessment using support vector  
 12712 machines and statistical language models. In *Proceedings of the Association for Compu-  
 12713 tational Linguistics (ACL)*, pp. 523–530.
- 12714 See, A., P. J. Liu, and C. D. Manning (2017). Get to the point: Summarization with pointer-  
 12715 generator networks. In *Proceedings of the Association for Computational Linguistics (ACL)*,  
 12716 pp. 1073–1083.
- 12717 Sennrich, R., B. Haddow, and A. Birch (2016). Neural machine translation of rare words  
 12718 with subword units. In *Proceedings of the Association for Computational Linguistics (ACL)*,  
 12719 pp. 1715–1725.

- 12720 Serban, I. V., A. Sordoni, Y. Bengio, A. C. Courville, and J. Pineau (2016). Building end-to-end dialogue systems using generative hierarchical neural network models. In *Proceedings of the National Conference on Artificial Intelligence (AAAI)*, pp. 3776–3784.
- 12723 Settles, B. (2012). Active learning. *Synthesis Lectures on Artificial Intelligence and Machine Learning* 6(1), 1–114.
- 12725 Shang, L., Z. Lu, and H. Li (2015). Neural responding machine for short-text conversation. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 1577–1586.
- 12727 Shen, D. and M. Lapata (2007). Using semantic roles to improve question answering. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 12–21.
- 12729 Shen, S., Y. Cheng, Z. He, W. He, H. Wu, M. Sun, and Y. Liu (2016). Minimum risk training for neural machine translation. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 1683–1692.
- 12732 Shen, W., J. Wang, and J. Han (2015). Entity linking with a knowledge base: Issues, techniques, and solutions. *IEEE Transactions on Knowledge and Data Engineering* 27(2), 443–460.
- 12735 Shieber, S. M. (1985). Evidence against the context-freeness of natural language. *Linguistics and Philosophy* 8(3), 333–343.
- 12737 Siegelmann, H. T. and E. D. Sontag (1995). On the computational power of neural nets. *Journal of computer and system sciences* 50(1), 132–150.
- 12739 Singh, S., A. Subramanya, F. Pereira, and A. McCallum (2011). Large-scale cross-document coreference using distributed inference and hierarchical models. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 793–803.
- 12742 Sipser, M. (2012). *Introduction to the Theory of Computation*. Cengage Learning.
- 12743 Smith, D. A. and J. Eisner (2006). Minimum risk annealing for training log-linear models. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 787–794.
- 12745 Smith, D. A. and J. Eisner (2008). Dependency parsing by belief propagation. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 145–156.
- 12747 Smith, D. A. and N. A. Smith (2007). Probabilistic models of nonprojective dependency trees. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 132–140.
- 12750 Smith, N. A. (2011). Linguistic structure prediction. *Synthesis Lectures on Human Language Technologies* 4(2), 1–274.

- 12752 Snover, M., B. Dorr, R. Schwartz, L. Micciulla, and J. Makhoul (2006). A study of transla-  
 12753 tion edit rate with targeted human annotation. In *Proceedings of association for machine*  
 12754 *translation in the Americas*, Volume 200.
- 12755 Snow, R., B. O'Connor, D. Jurafsky, and A. Y. Ng (2008). Cheap and fast—but is it good?:  
 12756 evaluating non-expert annotations for natural language tasks. In *Proceedings of Empirical*  
 12757 *Methods for Natural Language Processing (EMNLP)*, pp. 254–263.
- 12758 Snyder, B. and R. Barzilay (2007). Database-text alignment via structured multilabel classi-  
 12759 fication. In *Proceedings of the International Joint Conference on Artificial Intelligence (IJCAI)*,  
 12760 pp. 1713–1718.
- 12761 Socher, R., J. Bauer, C. D. Manning, and A. Y. Ng (2013). Parsing with compositional vector  
 12762 grammars. In *Proceedings of the Association for Computational Linguistics (ACL)*.
- 12763 Socher, R., B. Huval, C. D. Manning, and A. Y. Ng (2012). Semantic compositionality  
 12764 through recursive matrix-vector spaces. In *Proceedings of the 2012 Joint Conference on Em-  
 12765 pirical Methods in Natural Language Processing and Computational Natural Language Learn-  
 12766 ing*, pp. 1201–1211. Association for Computational Linguistics.
- 12767 Socher, R., A. Perelygin, J. Y. Wu, J. Chuang, C. D. Manning, A. Y. Ng, and C. Potts (2013).  
 12768 Recursive deep models for semantic compositionality over a sentiment treebank. In  
 12769 *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*.
- 12770 Søgaard, A. (2013). Semi-supervised learning and domain adaptation in natural language  
 12771 processing. *Synthesis Lectures on Human Language Technologies* 6(2), 1–103.
- 12772 Solorio, T. and Y. Liu (2008). Learning to predict code-switching points. In *Proceedings*  
 12773 *of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 973–981. Association  
 12774 for Computational Linguistics.
- 12775 Somasundaran, S., G. Namata, J. Wiebe, and L. Getoor (2009). Supervised and unsuper-  
 12776 vised methods in employing discourse relations for improving opinion polarity classi-  
 12777 fication. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*.
- 12778 Somasundaran, S. and J. Wiebe (2009). Recognizing stances in online debates. In *Proceed-  
 12779 ings of the Association for Computational Linguistics (ACL)*, pp. 226–234.
- 12780 Song, L., B. Boots, S. M. Siddiqi, G. J. Gordon, and A. J. Smola (2010). Hilbert space  
 12781 embeddings of hidden markov models. In *Proceedings of the International Conference on*  
 12782 *Machine Learning (ICML)*, pp. 991–998.
- 12783 Song, L., Y. Zhang, X. Peng, Z. Wang, and D. Gildea (2016). Amr-to-text generation as  
 12784 a traveling salesman problem. In *Proceedings of Empirical Methods for Natural Language*  
 12785 *Processing (EMNLP)*, pp. 2084–2089.

- 12786 Soon, W. M., H. T. Ng, and D. C. Y. Lim (2001). A machine learning approach to coreference resolution of noun phrases. *Computational linguistics* 27(4), 521–544.
- 12787
- 12788 Sordoni, A., M. Galley, M. Auli, C. Brockett, Y. Ji, M. Mitchell, J.-Y. Nie, J. Gao, and B. Dolan (2015). A neural network approach to context-sensitive generation of conversational responses. In *Proceedings of the North American Chapter of the Association for Computational Linguistics (NAACL)*.
- 12789
- 12790
- 12791
- 12792 Soriceut, R. and D. Marcu (2003). Sentence level discourse parsing using syntactic and lexical information. In *Proceedings of the North American Chapter of the Association for Computational Linguistics (NAACL)*, pp. 149–156.
- 12793
- 12794
- 12795 Sowa, J. F. (2000). *Knowledge representation: logical, philosophical, and computational foundations*. Pacific Grove, CA: Brooks/Cole.
- 12796
- 12797 Spärck Jones, K. (1972). A statistical interpretation of term specificity and its application in retrieval. *Journal of documentation* 28(1), 11–21.
- 12798
- 12799 Spitskovsky, V. I., H. Alshawi, D. Jurafsky, and C. D. Manning (2010). Viterbi training improves unsupervised dependency parsing. In *CONLL*, pp. 9–17.
- 12800
- 12801 Sporleder, C. and M. Lapata (2005). Discourse chunking and its application to sentence compression. In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 257–264.
- 12802
- 12803
- 12804 Sproat, R., A. Black, S. Chen, S. Kumar, M. Ostendorf, and C. Richards (2001). Normalization of non-standard words. *Computer Speech & Language* 15(3), 287–333.
- 12805
- 12806 Sproat, R., W. Gale, C. Shih, and N. Chang (1996). A stochastic finite-state word-segmentation algorithm for chinese. *Computational linguistics* 22(3), 377–404.
- 12807
- 12808 Sra, S., S. Nowozin, and S. J. Wright (2012). *Optimization for machine learning*. MIT Press.
- 12809
- 12810 Srivastava, N., G. Hinton, A. Krizhevsky, I. Sutskever, and R. Salakhutdinov (2014). Dropout: A simple way to prevent neural networks from overfitting. *The Journal of Machine Learning Research* 15(1), 1929–1958.
- 12811
- 12812 Srivastava, R. K., K. Greff, and J. Schmidhuber (2015). Training very deep networks. In *Neural Information Processing Systems (NIPS)*, pp. 2377–2385.
- 12813
- 12814 Stab, C. and I. Gurevych (2014a). Annotating argument components and relations in persuasive essays. In *Proceedings of the International Conference on Computational Linguistics (COLING)*, pp. 1501–1510.
- 12815
- 12816

- 12817 Stab, C. and I. Gurevych (2014b). Identifying argumentative discourse structures in per-  
 12818 suasive essays. In *Proceedings of the 2014 Conference on Empirical Methods in Natural Lan-*  
 12819 *guage Processing (EMNLP)*, pp. 46–56.
- 12820 Stede, M. (2011, nov). *Discourse Processing*, Volume 4 of *Synthesis Lectures on Human Lan-*  
 12821 *guage Technologies*. Morgan & Claypool Publishers.
- 12822 Steedman, M. and J. Baldridge (2011). Combinatory categorial grammar. In *Non-*  
 12823 *Transformational Syntax: Formal and Explicit Models of Grammar*. Wiley-Blackwell.
- 12824 Stenetorp, P., S. Pyysalo, G. Topić, T. Ohta, S. Ananiadou, and J. Tsujii (2012). Brat: a web-  
 12825 based tool for nlp-assisted text annotation. In *Proceedings of the European Chapter of the*  
 12826 *Association for Computational Linguistics (EACL)*, pp. 102–107.
- 12827 Stern, M., J. Andreas, and D. Klein (2017). A minimal span-based neural constituency  
 12828 parser. In *Proceedings of the Association for Computational Linguistics (ACL)*.
- 12829 Stolcke, A., K. Ries, N. Coccaro, E. Shriberg, R. Bates, D. Jurafsky, P. Taylor, R. Martin,  
 12830 C. Van Ess-Dykema, and M. Meteer (2000). Dialogue act modeling for automatic tag-  
 12831 ging and recognition of conversational speech. *Computational linguistics* 26(3), 339–373.
- 12832 Stone, P. J. (1966). *The General Inquirer: A Computer Approach to Content Analysis*. The MIT  
 12833 Press.
- 12834 Stoyanov, V., N. Gilbert, C. Cardie, and E. Riloff (2009). Conundrums in noun phrase  
 12835 coreference resolution: Making sense of the state-of-the-art. In *Proceedings of the Associa-*  
 12836 *tion for Computational Linguistics (ACL)*, pp. 656–664.
- 12837 Strang, G. (2016). *Introduction to linear algebra* (Fifth ed.). Wellesley, MA: Wellesley-  
 12838 Cambridge Press.
- 12839 Strubell, E., P. Verga, D. Belanger, and A. McCallum (2017). Fast and accurate entity recog-  
 12840 nition with iterated dilated convolutions. In *Proceedings of Empirical Methods for Natural*  
 12841 *Language Processing (EMNLP)*.
- 12842 Suchanek, F. M., G. Kasneci, and G. Weikum (2007). Yago: a core of semantic knowledge.  
 12843 In *Proceedings of the Conference on World-Wide Web (WWW)*, pp. 697–706.
- 12844 Sun, X., T. Matsuzaki, D. Okanohara, and J. Tsujii (2009). Latent variable perceptron algo-  
 12845 rithm for structured classification. In *Proceedings of the International Joint Conference on*  
 12846 *Artificial Intelligence (IJCAI)*, Volume 9, pp. 1236–1242.
- 12847 Sun, Y., L. Lin, D. Tang, N. Yang, Z. Ji, and X. Wang (2015). Modeling mention, context  
 12848 and entity with neural networks for entity disambiguation. In *IJCAI*, pp. 1333–1339.

- 12849 Sundermeyer, M., R. Schlüter, and H. Ney (2012). Lstm neural networks for language  
12850 modeling. In *INTERSPEECH*.
- 12851 Surdeanu, M., J. Tibshirani, R. Nallapati, and C. D. Manning (2012). Multi-instance multi-  
12852 label learning for relation extraction. In *Proceedings of Empirical Methods for Natural Lan-*  
12853 *guage Processing (EMNLP)*, pp. 455–465.
- 12854 Sutskever, I., O. Vinyals, and Q. V. Le (2014). Sequence to sequence learning with neural  
12855 networks. In *Neural Information Processing Systems (NIPS)*, pp. 3104–3112.
- 12856 Sutton, R. S. and A. G. Barto (1998). *Reinforcement learning: An introduction*, Volume 1. MIT  
12857 press Cambridge.
- 12858 Sutton, R. S., D. A. McAllester, S. P. Singh, and Y. Mansour (2000). Policy gradient methods  
12859 for reinforcement learning with function approximation. In *Neural Information Process-*  
12860 *ing Systems (NIPS)*, pp. 1057–1063.
- 12861 Taboada, M., J. Brooke, M. Tofiloski, K. Voll, and M. Stede (2011). Lexicon-based methods  
12862 for sentiment analysis. *Computational linguistics* 37(2), 267–307.
- 12863 Taboada, M. and W. C. Mann (2006). Rhetorical structure theory: Looking back and mov-  
12864 ing ahead. *Discourse studies* 8(3), 423–459.
- 12865 Täckström, O., K. Ganchev, and D. Das (2015). Efficient inference and structured learning  
12866 for semantic role labeling. *Transactions of the Association for Computational Linguistics* 3,  
12867 29–41.
- 12868 Täckström, O., R. McDonald, and J. Uszkoreit (2012). Cross-lingual word clusters for  
12869 direct transfer of linguistic structure. In *Proceedings of the North American Chapter of the*  
12870 *Association for Computational Linguistics (NAACL)*, pp. 477–487.
- 12871 Tang, D., B. Qin, and T. Liu (2015). Document modeling with gated recurrent neural net-  
12872 work for sentiment classification. In *Proceedings of Empirical Methods for Natural Language*  
12873 *Processing (EMNLP)*, pp. 1422–1432.
- 12874 Taskar, B., C. Guestrin, and D. Koller (2003). Max-margin markov networks. In *Neural*  
12875 *Information Processing Systems (NIPS)*.
- 12876 Tausczik, Y. R. and J. W. Pennebaker (2010). The psychological meaning of words: LIWC  
12877 and computerized text analysis methods. *Journal of Language and Social Psychology* 29(1),  
12878 24–54.
- 12879 Teh, Y. W. (2006). A hierarchical bayesian language model based on pitman-yor processes.  
12880 In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 985–992.
- 12881 Tesnière, L. (1966). *Éléments de syntaxe structurale* (second ed.). Paris: Klincksieck.

- 12882 Teufel, S., J. Carletta, and M. Moens (1999). An annotation scheme for discourse-level  
12883 argumentation in research articles. In *Proceedings of the European Chapter of the Association*  
12884 *for Computational Linguistics (EACL)*, pp. 110–117.
- 12885 Teufel, S. and M. Moens (2002). Summarizing scientific articles: experiments with relevance  
12886 and rhetorical status. *Computational linguistics* 28(4), 409–445.
- 12887 Thomas, M., B. Pang, and L. Lee (2006). Get out the vote: Determining support or opposition  
12888 from Congressional floor-debate transcripts. In *Proceedings of Empirical Methods for*  
12889 *Natural Language Processing (EMNLP)*, pp. 327–335.
- 12890 Tibshirani, R. (1996). Regression shrinkage and selection via the lasso. *Journal of the Royal*  
12891 *Statistical Society. Series B (Methodological)*, 267–288.
- 12892 Titov, I. and J. Henderson (2007). Constituent parsing with incremental sigmoid belief  
12893 networks. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 632–  
12894 639.
- 12895 Toutanova, K., D. Klein, C. D. Manning, and Y. Singer (2003). Feature-rich part-of-speech  
12896 tagging with a cyclic dependency network. In *Proceedings of the North American Chapter*  
12897 *of the Association for Computational Linguistics (NAACL)*.
- 12898 Trivedi, R. and J. Eisenstein (2013). Discourse connectors for latent subjectivity in senti-  
12899 ment analysis. In *Proceedings of the North American Chapter of the Association for Compu-*  
12900 *tational Linguistics (NAACL)*, pp. 808–813.
- 12901 Tromble, R. W. and J. Eisner (2006). A fast finite-state relaxation method for enforcing  
12902 global constraints on sequence decoding. In *Proceedings of the North American Chapter of*  
12903 *the Association for Computational Linguistics (NAACL)*, pp. 423.
- 12904 Tsochantaridis, I., T. Hofmann, T. Joachims, and Y. Altun (2004). Support vector machine  
12905 learning for interdependent and structured output spaces. In *Proceedings of the twenty-*  
12906 *first international conference on Machine learning*, pp. 104. ACM.
- 12907 Tsvetkov, Y., M. Faruqui, W. Ling, G. Lample, and C. Dyer (2015). Evaluation of word  
12908 vector representations by subspace alignment. In *Proceedings of Empirical Methods for*  
12909 *Natural Language Processing (EMNLP)*, pp. 2049–2054.
- 12910 Tu, Z., Z. Lu, Y. Liu, X. Liu, and H. Li (2016). Modeling coverage for neural machine  
12911 translation. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 76–  
12912 85.
- 12913 Turian, J., L. Ratinov, and Y. Bengio (2010). Word representations: a simple and general  
12914 method for semi-supervised learning. In *Proceedings of the Association for Computational*  
12915 *Linguistics (ACL)*, pp. 384–394.

- 12916 Turing, A. M. (2009). Computing machinery and intelligence. In *Parsing the Turing Test*,  
12917 pp. 23–65. Springer.
- 12918 Turney, P. D. and P. Pantel (2010). From frequency to meaning: Vector space models of  
12919 semantics. *Journal of Artificial Intelligence Research* 37, 141–188.
- 12920 Tutin, A. and R. Kittredge (1992). Lexical choice in context: generating procedural texts.  
12921 In *Proceedings of the International Conference on Computational Linguistics (COLING)*, pp.  
12922 763–769.
- 12923 Twain, M. (1997). *A Tramp Abroad*. New York: Penguin.
- 12924 Tzeng, E., J. Hoffman, T. Darrell, and K. Saenko (2015). Simultaneous deep transfer across  
12925 domains and tasks. In *Proceedings of the IEEE International Conference on Computer Vision*,  
12926 pp. 4068–4076.
- 12927 Usunier, N., D. Buffoni, and P. Gallinari (2009). Ranking with ordered weighted pairwise  
12928 classification. In *Proceedings of the International Conference on Machine Learning (ICML)*,  
12929 pp. 1057–1064.
- 12930 Uthus, D. C. and D. W. Aha (2013). The ubuntu chat corpus for multiparicipant chat  
12931 analysis. In *AAAI Spring Symposium: Analyzing Microtext*, Volume 13, pp. 01.
- 12932 Utiyama, M. and H. Isahara (2001). A statistical model for domain-independent text seg-  
12933 mentation. In *Proceedings of the 39th Annual Meeting on Association for Computational  
12934 Linguistics*, pp. 499–506. Association for Computational Linguistics.
- 12935 Utiyama, M. and H. Isahara (2007). A comparison of pivot methods for phrase-based  
12936 statistical machine translation. In *Human Language Technologies 2007: The Conference of  
12937 the North American Chapter of the Association for Computational Linguistics; Proceedings of  
12938 the Main Conference*, pp. 484–491.
- 12939 Uzuner, Ö., X. Zhang, and T. Sibanda (2009). Machine learning and rule-based approaches  
12940 to assertion classification. *Journal of the American Medical Informatics Association* 16(1),  
12941 109–115.
- 12942 Vadas, D. and J. R. Curran (2011). Parsing noun phrases in the penn treebank. *Compu-  
12943 tational Linguistics* 37(4), 753–809.
- 12944 Van Eynde, F. (2006). NP-internal agreement and the structure of the noun phrase. *Journal  
12945 of Linguistics* 42(1), 139–186.
- 12946 Van Gael, J., A. Vlachos, and Z. Ghahramani (2009). The infinite hmm for unsuper-  
12947 vised pos tagging. In *Proceedings of Empirical Methods for Natural Language Processing  
12948 (EMNLP)*, pp. 678–687.

- 12949 Vaswani, A., S. Bengio, E. Brevdo, F. Chollet, A. N. Gomez, S. Gouws, L. Jones, L. Kaiser,  
 12950 N. Kalchbrenner, N. Parmar, R. Sepassi, N. Shazeer, and J. Uszkoreit (2018). Tensor2tensor  
 12951 for neural machine translation. *CoRR abs/1803.07416*.
- 12952 Vaswani, A., N. Shazeer, N. Parmar, J. Uszkoreit, L. Jones, A. N. Gomez, Ł. Kaiser, and  
 12953 I. Polosukhin (2017). Attention is all you need. In *Neural Information Processing Systems*  
 12954 (*NIPS*), pp. 6000–6010.
- 12955 Velldal, E., L. Øvreliid, J. Read, and S. Oopen (2012). Speculation and negation: Rules,  
 12956 rankers, and the role of syntax. *Computational linguistics* 38(2), 369–410.
- 12957 Versley, Y. (2011). Towards finer-grained tagging of discourse connectives. In *Proceedings*  
 12958 *of the Workshop Beyond Semantics: Corpus-based Investigations of Pragmatic and Discourse*  
 12959 *Phenomena*, pp. 2–63.
- 12960 Vilain, M., J. Burger, J. Aberdeen, D. Connolly, and L. Hirschman (1995). A model-  
 12961 theoretic coreference scoring scheme. In *Proceedings of the 6th conference on Message*  
 12962 *understanding*, pp. 45–52. Association for Computational Linguistics.
- 12963 Vincent, P., H. Larochelle, I. Lajoie, Y. Bengio, and P.-A. Manzagol (2010). Stacked de-  
 12964 noising autoencoders: Learning useful representations in a deep network with a local  
 12965 denoising criterion. *Journal of Machine Learning Research* 11(Dec), 3371–3408.
- 12966 Vincze, V., G. Szarvas, R. Farkas, G. Móra, and J. Csirik (2008). The bioscope corpus:  
 12967 biomedical texts annotated for uncertainty, negation and their scopes. *BMC bioinformatics*  
 12968 9(11), S9.
- 12969 Vinyals, O., A. Toshev, S. Bengio, and D. Erhan (2015). Show and tell: A neural image cap-  
 12970 tion generator. In *Computer Vision and Pattern Recognition (CVPR), 2015 IEEE Conference*  
 12971 *on*, pp. 3156–3164. IEEE.
- 12972 Viterbi, A. (1967). Error bounds for convolutional codes and an asymptotically optimum  
 12973 decoding algorithm. *IEEE transactions on Information Theory* 13(2), 260–269.
- 12974 Voll, K. and M. Taboada (2007). Not all words are created equal: Extracting semantic  
 12975 orientation as a function of adjective relevance. In *Proceedings of Australian Conference*  
 12976 *on Artificial Intelligence*.
- 12977 Wager, S., S. Wang, and P. S. Liang (2013). Dropout training as adaptive regularization. In  
 12978 *Neural Information Processing Systems (NIPS)*, pp. 351–359.
- 12979 Wainwright, M. J. and M. I. Jordan (2008). Graphical models, exponential families, and  
 12980 variational inference. *Foundations and Trends® in Machine Learning* 1(1-2), 1–305.

- 12981 Walker, M. A. (2000). An application of reinforcement learning to dialogue strategy selec-  
12982 tion in a spoken dialogue system for email. *Journal of Artificial Intelligence Research* 12,  
12983 387–416.
- 12984 Walker, M. A., J. E. Cahn, and S. J. Whittaker (1997). Improvising linguistic style: Social  
12985 and affective bases for agent personality. In *Proceedings of the first international conference*  
12986 on *Autonomous agents*, pp. 96–105. ACM.
- 12987 Wang, C., N. Xue, and S. Pradhan (2015). A Transition-based Algorithm for AMR Parsing.  
12988 In *Proceedings of the North American Chapter of the Association for Computational Linguistics*  
12989 (NAACL), pp. 366–375.
- 12990 Wang, H., T. Onishi, K. Gimpel, and D. McAllester (2017). Emergent predication structure  
12991 in hidden state vectors of neural readers. In *Proceedings of the 2nd Workshop on Repre-  
12992 sentation Learning for NLP*, pp. 26–36.
- 12993 Weaver, W. (1955). Translation. *Machine translation of languages* 14, 15–23.
- 12994 Webber, B. (2004, sep). D-LTAG: extending lexicalized TAG to discourse. *Cognitive Sci-  
12995 ence* 28(5), 751–779.
- 12996 Webber, B., M. Egg, and V. Kordoni (2012). Discourse structure and language technology.  
12997 *Journal of Natural Language Engineering* 1.
- 12998 Webber, B. and A. Joshi (2012). Discourse structure and computation: past, present and  
12999 future. In *Proceedings of the ACL-2012 Special Workshop on Rediscovering 50 Years of Dis-  
13000 coveries*, pp. 42–54. Association for Computational Linguistics.
- 13001 Wei, G. C. and M. A. Tanner (1990). A monte carlo implementation of the em algorithm  
13002 and the poor man’s data augmentation algorithms. *Journal of the American Statistical  
13003 Association* 85(411), 699–704.
- 13004 Weinberger, K., A. Dasgupta, J. Langford, A. Smola, and J. Attenberg (2009). Feature  
13005 hashing for large scale multitask learning. In *Proceedings of the International Conference  
13006 on Machine Learning (ICML)*, pp. 1113–1120.
- 13007 Weizenbaum, J. (1966). Eliza—a computer program for the study of natural language  
13008 communication between man and machine. *Communications of the ACM* 9(1), 36–45.
- 13009 Wellner, B. and J. Pustejovsky (2007). Automatically identifying the arguments of dis-  
13010 course connectives. In *Proceedings of Empirical Methods for Natural Language Processing  
13011 (EMNLP)*, pp. 92–101.
- 13012 Wen, T.-H., M. Gasic, N. Mrkšić, P.-H. Su, D. Vandyke, and S. Young (2015). Semantically  
13013 conditioned lstm-based natural language generation for spoken dialogue systems. In  
13014 *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 1711–1721.

- 13015 Weston, J., S. Bengio, and N. Usunier (2011). Wsabie: Scaling up to large vocabulary image  
13016 annotation. In *IJCAI*, Volume 11, pp. 2764–2770.
- 13017 Wiebe, J., T. Wilson, and C. Cardie (2005). Annotating expressions of opinions and emo-  
13018 tions in language. *Language resources and evaluation* 39(2), 165–210.
- 13019 Wieting, J., M. Bansal, K. Gimpel, and K. Livescu (2015). Towards universal paraphrastic  
13020 sentence embeddings. *arXiv preprint arXiv:1511.08198*.
- 13021 Wieting, J., M. Bansal, K. Gimpel, and K. Livescu (2016). CHARAGRAM: Embedding  
13022 words and sentences via character n-grams. In *Proceedings of Empirical Methods for Nat-*  
13023 *ural Language Processing (EMNLP)*, pp. 1504–1515.
- 13024 Williams, J. D. and S. Young (2007). Partially observable markov decision processes for  
13025 spoken dialog systems. *Computer Speech & Language* 21(2), 393–422.
- 13026 Williams, P., R. Sennrich, M. Post, and P. Koehn (2016). Syntax-based statistical machine  
13027 translation. *Synthesis Lectures on Human Language Technologies* 9(4), 1–208.
- 13028 Wilson, T., J. Wiebe, and P. Hoffmann (2005). Recognizing contextual polarity in phrase-  
13029 level sentiment analysis. In *Proceedings of Empirical Methods for Natural Language Pro-*  
13030 *cessing (EMNLP)*, pp. 347–354.
- 13031 Winograd, T. (1972). Understanding natural language. *Cognitive psychology* 3(1), 1–191.
- 13032 Wiseman, S., A. M. Rush, and S. M. Shieber (2016). Learning global features for corefer-  
13033 ence resolution. In *Proceedings of the North American Chapter of the Association for Compu-*  
13034 *tational Linguistics (NAACL)*, pp. 994–1004.
- 13035 Wiseman, S., S. Shieber, and A. Rush (2017). Challenges in data-to-document generation.  
13036 In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*, pp. 2253–  
13037 2263.
- 13038 Wiseman, S. J., A. M. Rush, S. M. Shieber, and J. Weston (2015). Learning anaphoricity and  
13039 antecedent ranking features for coreference resolution. In *Proceedings of the Association*  
13040 *for Computational Linguistics (ACL)*.
- 13041 Wolf, F. and E. Gibson (2005). Representing discourse coherence: A corpus-based study.  
13042 *Computational Linguistics* 31(2), 249–287.
- 13043 Wolfe, T., M. Dredze, and B. Van Durme (2017). Pocket knowledge base population. In  
13044 *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 305–310.
- 13045 Wong, Y. W. and R. Mooney (2007). Generation by inverting a semantic parser that uses  
13046 statistical machine translation. In *Proceedings of the North American Chapter of the Associa-*  
13047 *tion for Computational Linguistics (NAACL)*, pp. 172–179.

- 13048 Wong, Y. W. and R. J. Mooney (2006). Learning for semantic parsing with statistical ma-  
13049 chine translation. In *Proceedings of the North American Chapter of the Association for Com-*  
13050 *putational Linguistics (NAACL)*, pp. 439–446.
- 13051 Wu, B. Y. and K.-M. Chao (2004). *Spanning trees and optimization problems*. CRC Press.
- 13052 Wu, D. (1997). Stochastic inversion transduction grammars and bilingual parsing of par-  
13053 allel corpora. *Computational linguistics* 23(3), 377–403.
- 13054 Wu, F. and D. S. Weld (2010). Open information extraction using wikipedia. In *Proceedings*  
13055 *of the Association for Computational Linguistics (ACL)*, pp. 118–127.
- 13056 Wu, X., R. Ward, and L. Bottou (2018). Wngrad: Learn the learning rate in gradient de-  
13057 scent. *arXiv preprint arXiv:1803.02865*.
- 13058 Wu, Y., M. Schuster, Z. Chen, Q. V. Le, M. Norouzi, W. Macherey, M. Krikun, Y. Cao,  
13059 Q. Gao, K. Macherey, J. Klingner, A. Shah, M. Johnson, X. Liu, Łukasz Kaiser, S. Gouws,  
13060 Y. Kato, T. Kudo, H. Kazawa, K. Stevens, G. Kurian, N. Patil, W. Wang, C. Young,  
13061 J. Smith, J. Riesa, A. Rudnick, O. Vinyals, G. Corrado, M. Hughes, and J. Dean (2016).  
13062 Google’s neural machine translation system: Bridging the gap between human and ma-  
13063 chine translation. *CoRR abs/1609.08144*.
- 13064 Xia, F. (2000). The part-of-speech tagging guidelines for the penn chinese treebank (3.0).  
13065 Technical report, University of Pennsylvania Institute for Research in Cognitive Science.
- 13066 Xu, K., J. Ba, R. Kiros, K. Cho, A. Courville, R. Salakhudinov, R. Zemel, and Y. Bengio  
13067 (2015). Show, attend and tell: Neural image caption generation with visual attention.  
13068 In *Proceedings of the International Conference on Machine Learning (ICML)*, pp. 2048–2057.
- 13069 Xu, W., X. Liu, and Y. Gong (2003). Document clustering based on non-negative matrix  
13070 factorization. In *SIGIR*, pp. 267–273. ACM.
- 13071 Xu, Y., L. Mou, G. Li, Y. Chen, H. Peng, and Z. Jin (2015). Classifying relations via long  
13072 short term memory networks along shortest dependency paths. In *Proceedings of Empir-*  
13073 *ical Methods for Natural Language Processing (EMNLP)*, pp. 1785–1794.
- 13074 Xuan Bach, N., N. L. Minh, and A. Shimazu (2012). A reranking model for discourse seg-  
13075 mentation using subtree features. In *Proceedings of the Special Interest Group on Discourse*  
13076 *and Dialogue (SIGDIAL)*.
- 13077 Xue, N. et al. (2003). Chinese word segmentation as character tagging. *Computational*  
13078 *Linguistics and Chinese Language Processing* 8(1), 29–48.
- 13079 Xue, N., H. T. Ng, S. Pradhan, R. Prasad, C. Bryant, and A. T. Rutherford (2015). The  
13080 CoNLL-2015 shared task on shallow discourse parsing. In *Proceedings of the Conference*  
13081 *on Natural Language Learning (CoNLL)*.

- 13082 Xue, N., H. T. Ng, S. Pradhan, A. Rutherford, B. L. Webber, C. Wang, and H. Wang (2016).  
 13083 Conll 2016 shared task on multilingual shallow discourse parsing. In *CoNLL Shared  
 13084 Task*, pp. 1–19.
- 13085 Yamada, H. and Y. Matsumoto (2003). Statistical dependency analysis with support vector  
 13086 machines. In *Proceedings of IWPT*, Volume 3, pp. 195–206.
- 13087 Yamada, K. and K. Knight (2001). A syntax-based statistical translation model. In *Proceed-  
 13088 ings of the 39th Annual Meeting on Association for Computational Linguistics*, pp. 523–530.  
 13089 Association for Computational Linguistics.
- 13090 Yang, B. and C. Cardie (2014). Context-aware learning for sentence-level sentiment anal-  
 13091 ysis with posterior regularization. In *Proceedings of the Association for Computational Lin-  
 13092 guistics (ACL)*.
- 13093 Yang, Y., M.-W. Chang, and J. Eisenstein (2016). Toward socially-infused information ex-  
 13094 traction: Embedding authors, mentions, and entities. In *Proceedings of Empirical Methods  
 13095 for Natural Language Processing (EMNLP)*.
- 13096 Yang, Y. and J. Eisenstein (2013). A log-linear model for unsupervised text normalization.  
 13097 In *Proceedings of Empirical Methods for Natural Language Processing (EMNLP)*.
- 13098 Yang, Y. and J. Eisenstein (2015). Unsupervised multi-domain adaptation with feature em-  
 13099 beddings. In *Proceedings of the North American Chapter of the Association for Computational  
 13100 Linguistics (NAACL)*.
- 13101 Yang, Y., W.-t. Yih, and C. Meek (2015). WikiQA: A challenge dataset for open-domain  
 13102 question answering. In *Proceedings of Empirical Methods for Natural Language Processing  
 13103 (EMNLP)*, pp. 2013–2018.
- 13104 Yannakoudakis, H., T. Briscoe, and B. Medlock (2011). A new dataset and method for  
 13105 automatically grading esol texts. In *Proceedings of the 49th Annual Meeting of the Associa-  
 13106 tion for Computational Linguistics: Human Language Technologies-Volume 1*, pp. 180–189.  
 13107 Association for Computational Linguistics.
- 13108 Yarowsky, D. (1995). Unsupervised word sense disambiguation rivaling supervised meth-  
 13109 ods. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 189–196.  
 13110 Association for Computational Linguistics.
- 13111 Yee, L. C. and T. Y. Jones (2012, March). Apple ceo in china mission to clear up problems.  
 13112 *Reuters*. retrieved on March 26, 2017.
- 13113 Yi, Y., C.-Y. Lai, S. Petrov, and K. Keutzer (2011, October). Efficient parallel cky parsing on  
 13114 gpus. In *Proceedings of the 12th International Conference on Parsing Technologies*, Dublin,  
 13115 Ireland, pp. 175–185. Association for Computational Linguistics.

- 13116 Yu, C.-N. J. and T. Joachims (2009). Learning structural svms with latent variables. In  
13117 *Proceedings of the International Conference on Machine Learning (ICML)*, pp. 1169–1176.
- 13118 Yu, F. and V. Koltun (2016). Multi-scale context aggregation by dilated convolutions. In  
13119 *Proceedings of the International Conference on Learning Representations (ICLR)*.
- 13120 Zaidan, O. F. and C. Callison-Burch (2011). Crowdsourcing translation: Professional qual-  
13121 ity from non-professionals. In *Proceedings of the Association for Computational Linguistics*  
13122 (*ACL*), pp. 1220–1229.
- 13123 Zaremba, W., I. Sutskever, and O. Vinyals. Recurrent neural network regularization. *arXiv*  
13124 *preprint arXiv:1409.2329*.
- 13125 Zeiler, M. D. (2012). Adadelta: an adaptive learning rate method. *arXiv preprint*  
13126 *arXiv:1212.5701*.
- 13127 Zelenko, D., C. Aone, and A. Richardella (2003). Kernel methods for relation extraction.  
13128 *The Journal of Machine Learning Research* 3, 1083–1106.
- 13129 Zelle, J. M. and R. J. Mooney (1996). Learning to parse database queries using induc-  
13130 tive logic programming. In *Proceedings of the National Conference on Artificial Intelligence*  
13131 (*AAAI*), pp. 1050–1055.
- 13132 Zeng, D., K. Liu, S. Lai, G. Zhou, and J. Zhao (2014). Relation classification via convolu-  
13133 tional deep neural network. In *Proceedings of the International Conference on Computational*  
13134 *Linguistics (COLING)*, pp. 2335–2344.
- 13135 Zettlemoyer, L. S. and M. Collins (2005). Learning to map sentences to logical form: Struc-  
13136 tured classification with probabilistic categorial grammars. In *Proceedings of UAI*.
- 13137 Zhang, X., J. Zhao, and Y. LeCun (2015). Character-level convolutional networks for text  
13138 classification. In *Neural Information Processing Systems (NIPS)*, pp. 649–657.
- 13139 Zhang, Y. and S. Clark (2008). A tale of two parsers: investigating and combining graph-  
13140 based and transition-based dependency parsing using beam-search. In *Proceedings of*  
13141 *Empirical Methods for Natural Language Processing (EMNLP)*, pp. 562–571.
- 13142 Zhang, Y., T. Lei, R. Barzilay, T. Jaakkola, and A. Globerson (2014). Steps to excellence:  
13143 Simple inference with refined scoring of dependency trees. In *Proceedings of the Associa-*  
13144 *tion for Computational Linguistics (ACL)*, pp. 197–207.
- 13145 Zhang, Y. and J. Nivre (2011). Transition-based dependency parsing with rich non-local  
13146 features. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp. 188–193.
- 13147 Zhang, Z. (2017). A note on counting dependency trees. *arXiv preprint arXiv:1708.08789*.

- 13148 Zhou, J. and W. Xu (2015). End-to-end learning of semantic role labeling using recurrent  
13149 neural networks. In *Proceedings of the Association for Computational Linguistics (ACL)*, pp.  
13150 1127–1137.
- 13151 Zhu, J., Z. Nie, X. Liu, B. Zhang, and J.-R. Wen (2009). Statsnowball: a statistical approach  
13152 to extracting entity relationships. In *Proceedings of the Conference on World-Wide Web*  
13153 (WWW), pp. 101–110.
- 13154 Zhu, X., Z. Ghahramani, and J. D. Lafferty (2003). Semi-supervised learning using gaus-  
13155 sian fields and harmonic functions. In *Proceedings of the International Conference on Ma-*  
13156 *chine Learning (ICML)*, pp. 912–919.
- 13157 Zhu, X. and A. B. Goldberg (2009). Introduction to semi-supervised learning. *Synthesis*  
13158 *lectures on artificial intelligence and machine learning* 3(1), 1–130.
- 13159 Zipf, G. K. (1949). Human behavior and the principle of least effort.
- 13160 Zirn, C., M. Niepert, H. Stuckenschmidt, and M. Strube (2011). Fine-grained sentiment  
13161 analysis with structural features. In *IJCNLP*, Chiang Mai, Thailand, pp. 336–344.
- 13162 Zou, W. Y., R. Socher, D. Cer, and C. D. Manning (2013). Bilingual word embeddings  
13163 for phrase-based machine translation. In *Proceedings of Empirical Methods for Natural*  
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