

440 Case Study I

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Set Up, Load, Clean Data

```
## load packages
library(dplyr)

##
## Attaching package: 'dplyr'
##
## The following objects are masked from 'package:stats':
##
##   filter, lag
##
## The following objects are masked from 'package:base':
##
##   intersect, setdiff, setequal, union
library(ggplot2)
library(MASS)

##
## Attaching package: 'MASS'
##
## The following object is masked from 'package:dplyr':
##
##   select

## read in data
births = read.csv("data/Yr1116Birth.csv", na.strings = "9999")
deaths = read.csv("data/Yr1116Death.csv")

## rewrite NAs
births$SEX[which(births$SEX == 9)] = NA
births$CIGPN[which(births$CIGPN == 99)] = NA
births$CIGFN[which(births$CIGFN == 99)] = NA
births$CIGSN[which(births$CIGSN == 99)] = NA
births$CIGLN[which(births$CIGLN == 99)] = NA
births$PARITY[which(births$PARITY == 99)] = NA
births$PLUR[which(births$PLUR == 99)] = NA
births$GEST[which(births$GEST == 99)] = NA
births$MAGE[which(births$MAGE == 99)] = NA

select = dplyr::select
```

Exploratory Data Analysis

Birthweight

```
summary(births$BWTG)
```

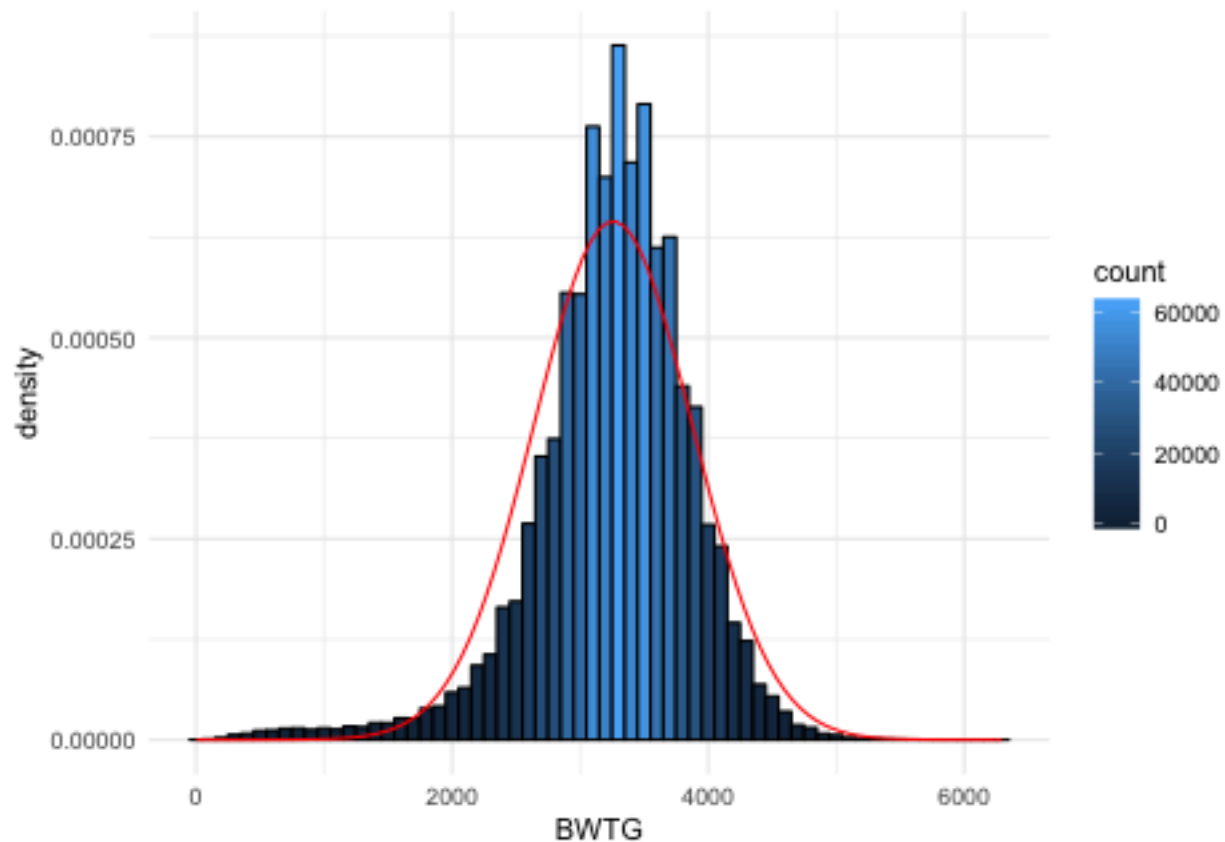
```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.     NA's  
##         4    2948    3310    3258    3640    6294      430
```

```
sd(births$BWTG, na.rm = TRUE)
```

```
## [1] 618.8703
```

```
ggplot(births, aes(x= BWTG))+  
  geom_histogram(binwidth=100, colour="black",  
                 aes(y=..density.., fill=..count..), position = "stack") +  
  stat_function(fun = dnorm, color = "red", args = list(mean = mean(births$BWTG, na.rm = TRUE), sd = sd  
  theme_minimal()
```

```
## Warning: Removed 430 rows containing non-finite values (stat_bin).
```



Birthweight is close to normally distributed, with a slight left skew, centered around ~3300g with a standard deviation of 600g. There appear to be no large outliers in terms of birthweight. 430 birth weights are missing. We see that the left tail is much larger than we would expect in a normal distribution

Smoking

```
births = births %>% mutate(
  CIGPN_binary = CIGPN>0,
  CIGFN_binary = CIGFN>0,
  CIGSN_binary = CIGSN>0,
  CIGLN_binary = CIGLN>0
)

births = births %>%
  mutate(total_smoked = CIGFN+CIGSN+CIGLN) %>%
  mutate(smoked_during = total_smoked >0)

mean(births$smoked_during,na.rm=TRUE)

## [1] 0.100175

mean(births$CIGPN_binary, na.rm = TRUE)

## [1] 0.1340957

mean(births$CIGFN_binar, na.rm = TRUE)

## [1] 0.09676666

mean(births$CIGSN_binary,na.rm = TRUE)

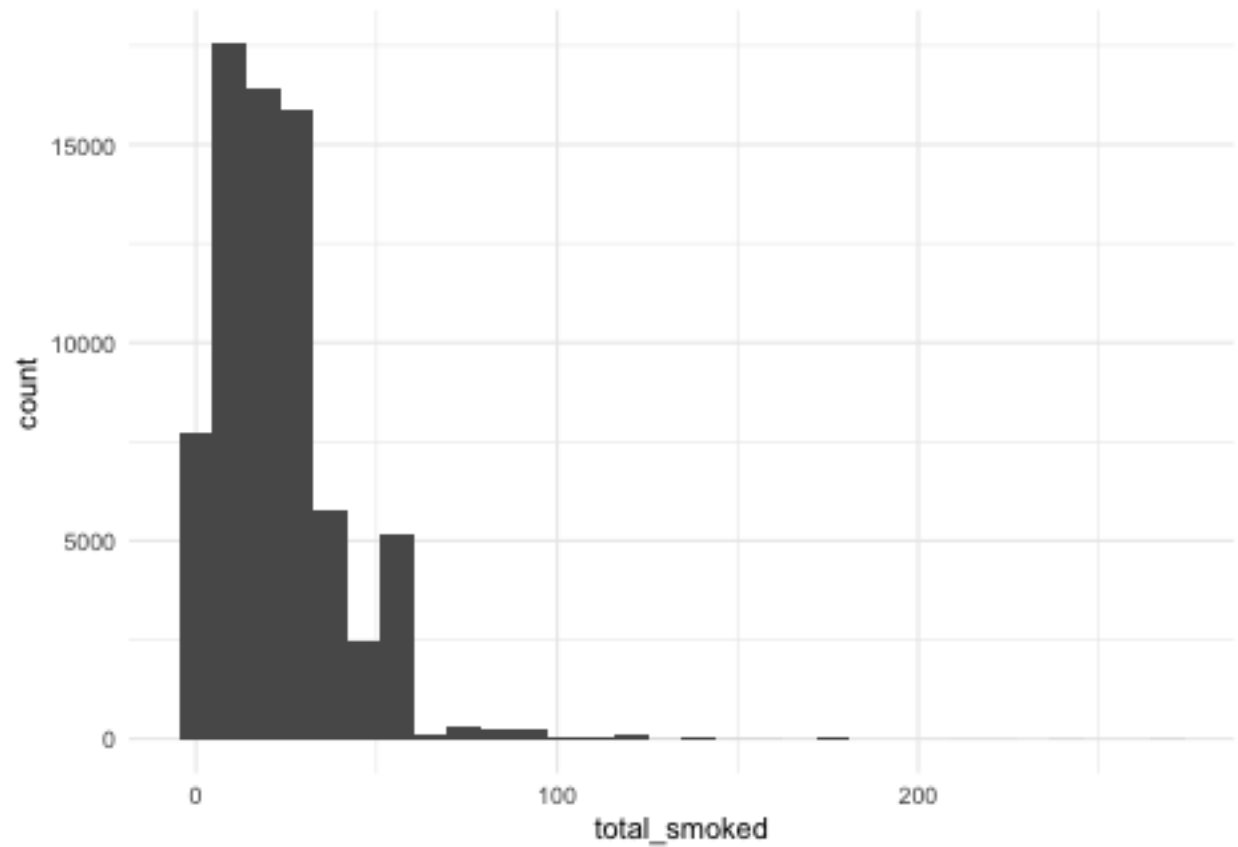
## [1] 0.08199303

mean(births$CIGLN_binary, na.rm = TRUE)

## [1] 0.07788803

ggplot(births %>% filter(smoked_during), aes(x = total_smoked))+
  geom_histogram() +
  theme_minimal()

## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```

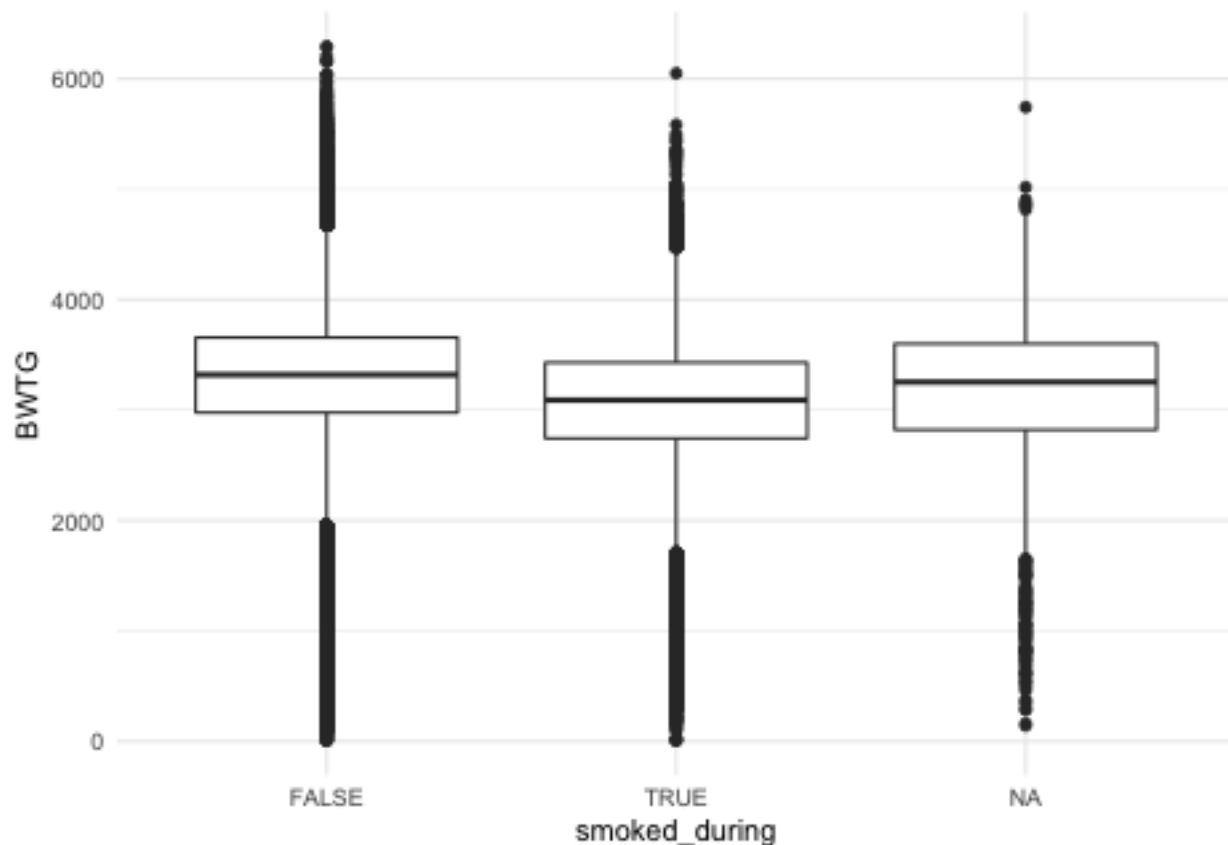


```
mean(births %>% filter(smoked_during) %>% select(total_smoked) %>% unlist())
```

```
## [1] 23.06795
```

```
ggplot(births, aes(x= smoked_during, y = BWTG)) +  
  geom_boxplot()+  
  theme_minimal()
```

```
## Warning: Removed 430 rows containing non-finite values (stat_boxplot).
```



```
lm_smoking_v_non = lm(data=births, BWG~smoked_during)
summary(lm_smoking_v_non)
```

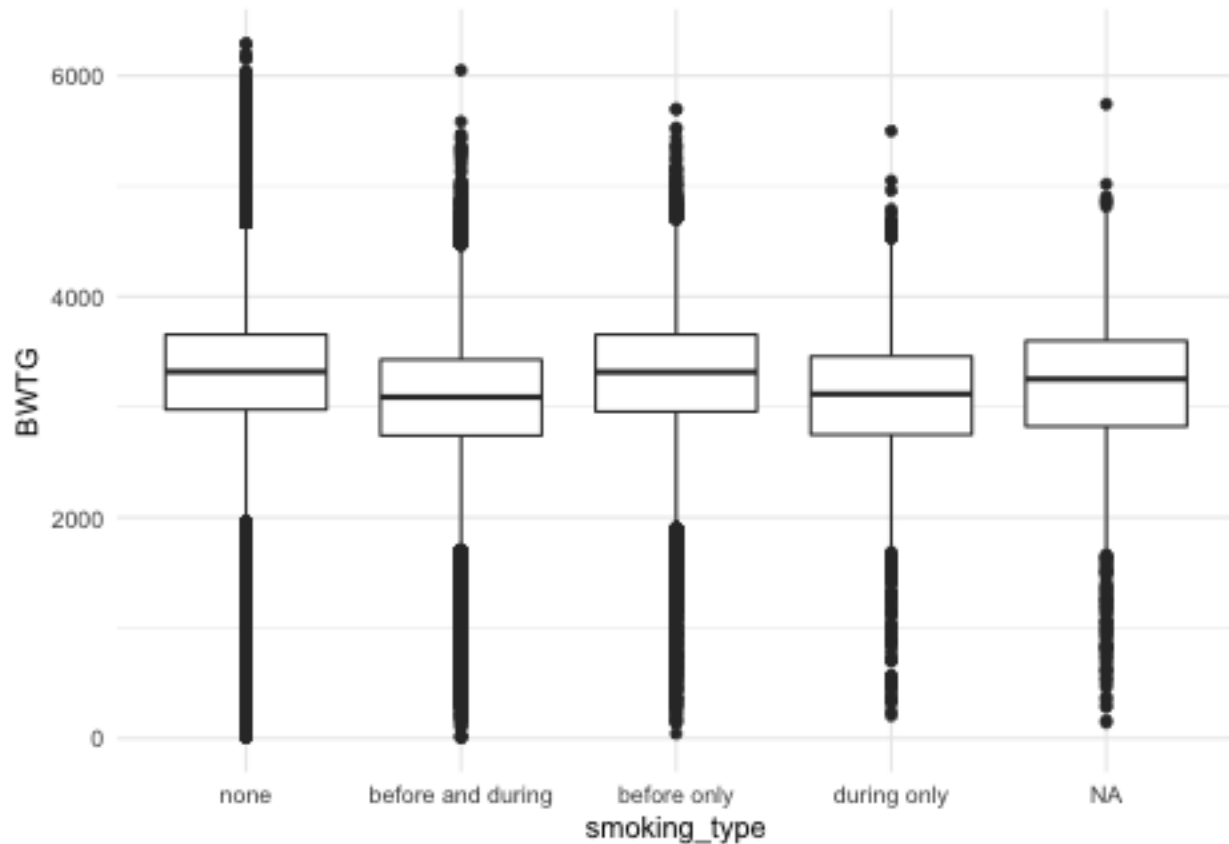
```
##
## Call:
## lm(formula = BWG ~ smoked_during, data = births)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3276.1  -304.1    40.2   375.9  3012.9
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    3281.064     0.764  4294.52  <2e-16 ***
## smoked_duringTRUE -231.237     2.414   -95.79  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 614.5 on 718931 degrees of freedom
## (2759 observations deleted due to missingness)
## Multiple R-squared:  0.0126, Adjusted R-squared:  0.0126
## F-statistic: 9175 on 1 and 718931 DF, p-value: < 2.2e-16
```

```
births = births %>%
  mutate(smoking_type = ifelse(smoked_during,
    ifelse(CIGPN_binary, "before and during", "during only"),
    ifelse(CIGPN_binary, "before only", "none"))) %>%
```

```
mutate(smoking_type = relevel(as.factor(smoking_type), ref = 4))

ggplot(births, aes(x= smoking_type, y = BWTG)) +
  geom_boxplot() +
  theme_minimal()
```

```
## Warning: Removed 430 rows containing non-finite values (stat_boxplot).
```



```
lm_smoking = lm(data=births, BWTG~smoking_type)
summary(lm_smoking)
```

```
##
## Call:
## lm(formula = BWTG ~ smoking_type, data = births)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3276.6  -304.6    40.5   375.4  3012.4
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    3281.6171     0.7802  4205.990 < 2e-16 ***
## smoking_typebefore and during  -232.0954     2.4538  -94.586 < 2e-16 ***
## smoking_typebefore only       -13.4168     3.8483   -3.486 0.00049 ***
## smoking_typeduring only      -223.2977    13.0480  -17.114 < 2e-16 ***
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 614.5 on 718904 degrees of freedom
## (2784 observations deleted due to missingness)
## Multiple R-squared:  0.01262,    Adjusted R-squared:  0.01262
## F-statistic: 3063 on 3 and 718904 DF,  p-value: < 2.2e-16
```

Around 13% of women smoked in the three months leading up to pregnancy and around 10% of women at any point during their pregnancy. Among those who did smoke during pregnancy, the average number of cigarettes smoked during pregnancy was 23. The birthweight of children of smokers was significantly lower than that of the children of nonsmokers, with an average difference of 231 grams. There is also a significant relationship between birthweight and smoking before pregnancy, even for those who did not smoke during pregnancy.

Parity

```
# Check the parity frequencies
```

```
summary(births$PARITY)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.     NA's
##    1.000   1.000   2.000   2.465   3.000   25.000     860
```

```
births$PARITY = as.numeric(births$PARITY)
```

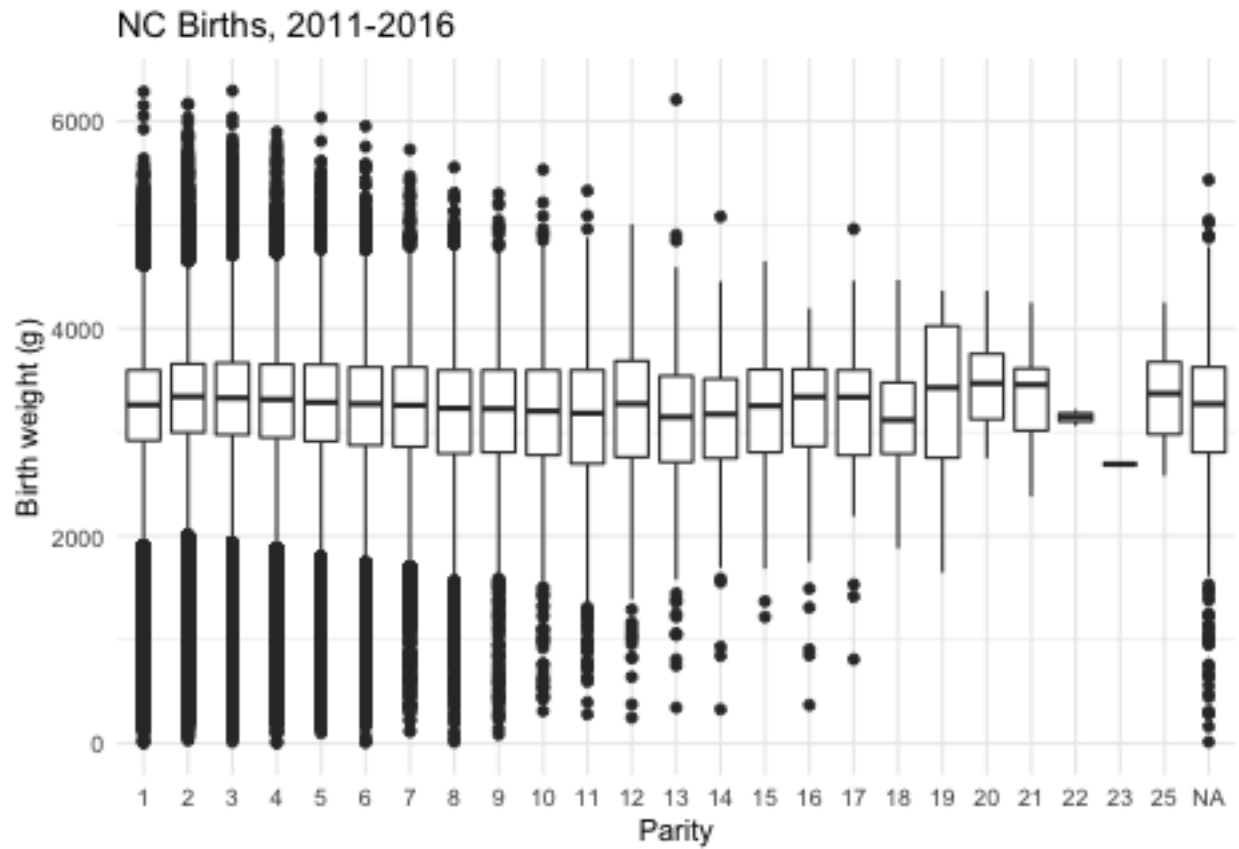
```
births = births %>%
```

```
  mutate(PARITY_truncated = ifelse(
    PARITY > 4, "5+", PARITY)
  )
```

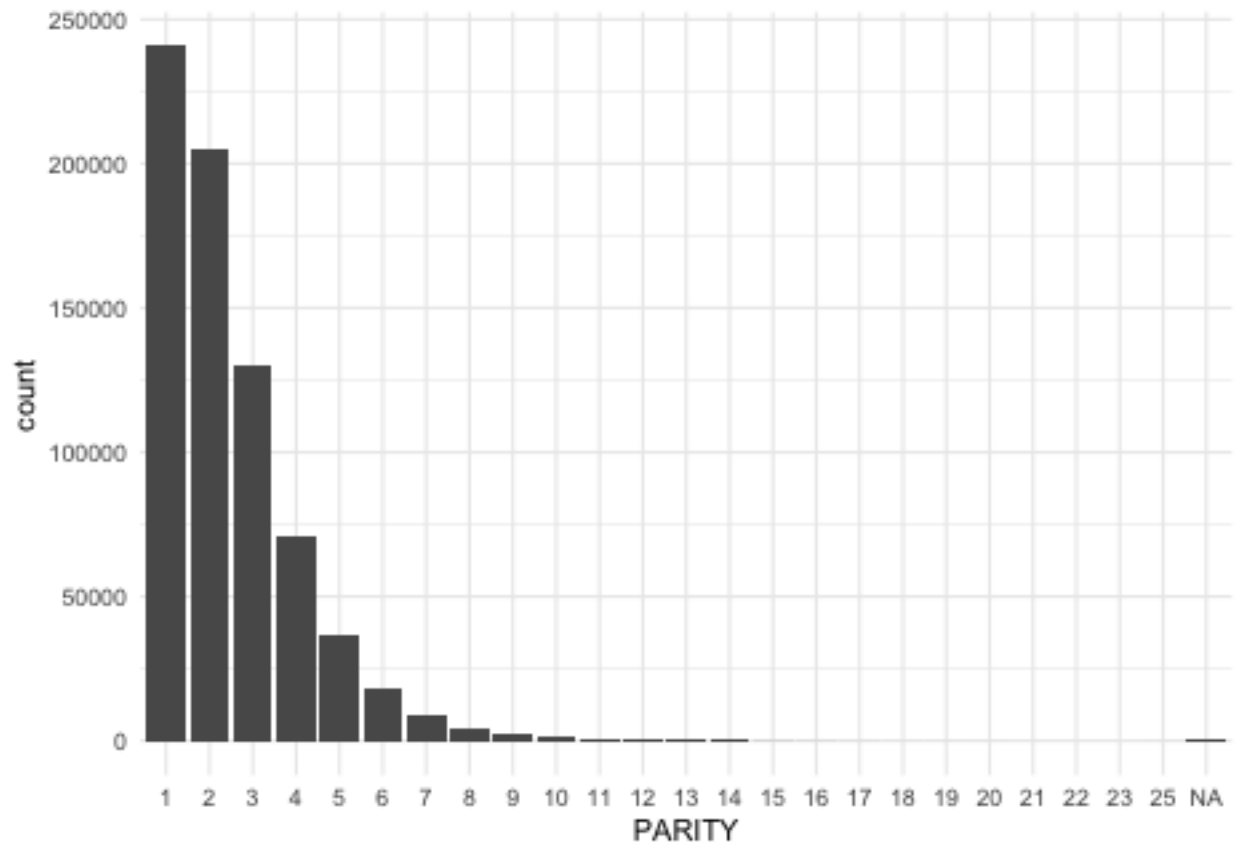
```
births$PARITY = as.factor(births$PARITY)
```

```
ggplot(data = births, mapping = aes(x = PARITY, y = BWTG)) +
  geom_boxplot() + xlab("Parity") + ylab("Birth weight (g)") +
  ggtitle("NC Births, 2011-2016") + theme_minimal()
```

```
## Warning: Removed 430 rows containing non-finite values (stat_boxplot).
```



```
ggplot(births, aes(x = PARITY)) +  
  stat_count() +  
  theme_minimal()
```

```
# Model without any change, significant up to the low teens
parity_reg = lm(BWTG ~ PARITY, births)
summary(parity_reg)
```

```
##
## Call:
## lm(formula = BWTG ~ PARITY, data = births)
##
## Residuals:
```

	Min	1Q	Median	3Q	Max
	-3272.9	-303.2	50.9	382.5	3126.8

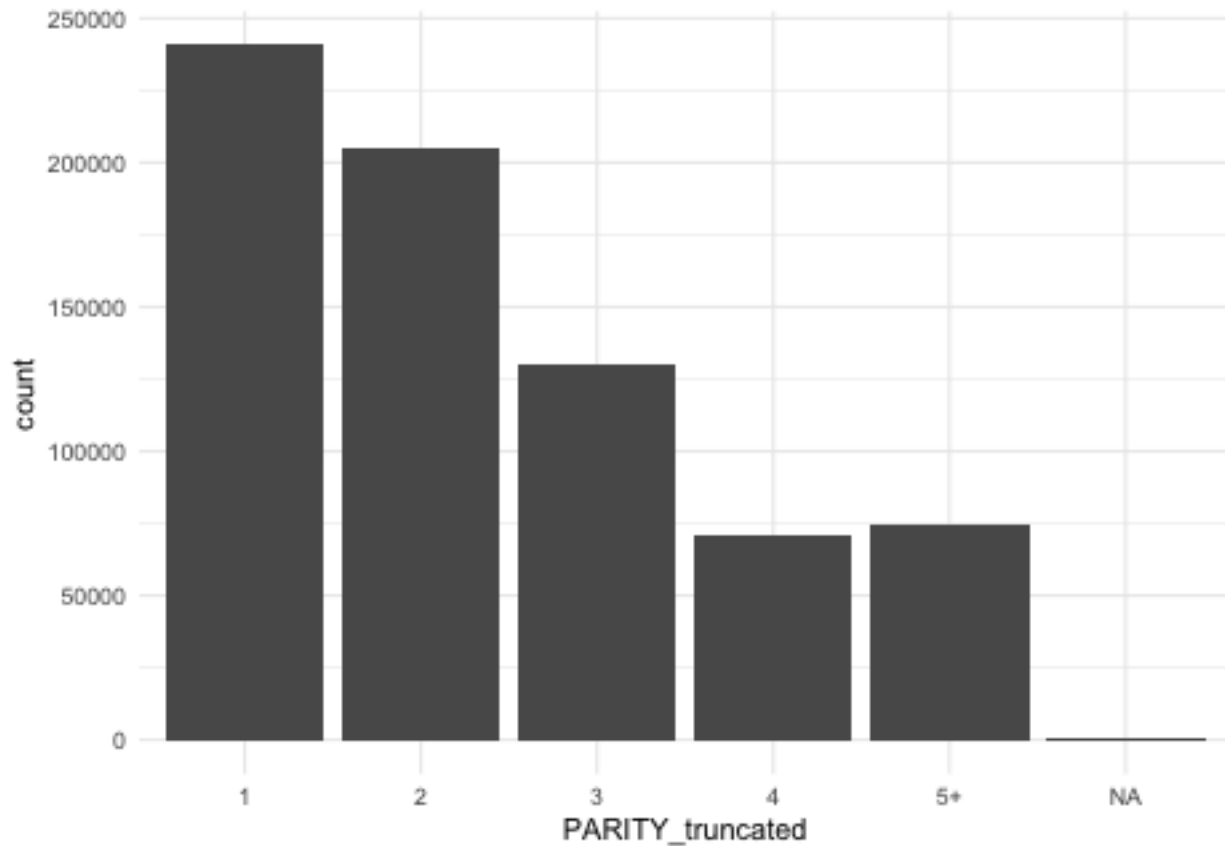
```
##
## Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	3223.242	1.259	2559.590	< 2e-16 ***
PARITY2	70.877	1.858	38.155	< 2e-16 ***
PARITY3	63.680	2.124	29.976	< 2e-16 ***
PARITY4	40.306	2.645	15.241	< 2e-16 ***
PARITY5	11.815	3.451	3.424	0.000618 ***
PARITY6	-11.166	4.751	-2.350	0.018757 *
PARITY7	-32.906	6.538	-5.033	4.84e-07 ***
PARITY8	-76.858	9.209	-8.345	< 2e-16 ***
PARITY9	-70.364	12.447	-5.653	1.58e-08 ***
PARITY10	-85.904	17.290	-4.968	6.75e-07 ***
PARITY11	-126.567	22.324	-5.670	1.43e-08 ***
PARITY12	-41.074	30.094	-1.365	0.172306

```
## PARITY13    -140.997    37.611    -3.749 0.000178 ***
## PARITY14    -157.146    55.261    -2.844 0.004459 **
## PARITY15     -20.675    62.728    -0.330 0.741706
## PARITY16   -158.545    82.550    -1.921 0.054782 .
## PARITY17    -64.515   107.530    -0.600 0.548530
## PARITY18    -61.242   145.592    -0.421 0.674019
## PARITY19     62.758   165.085     0.380 0.703829
## PARITY20    250.258   195.329     1.281 0.200120
## PARITY21    112.901   233.462     0.484 0.628673
## PARITY22    -80.242   356.616    -0.225 0.821972
## PARITY23   -530.242   617.674    -0.858 0.390645
## PARITY25    162.758   218.384     0.745 0.456100
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 617.7 on 720622 degrees of freedom
## (1046 observations deleted due to missingness)
## Multiple R-squared:  0.003304, Adjusted R-squared:  0.003272
## F-statistic: 103.9 on 23 and 720622 DF, p-value: < 2.2e-16
```

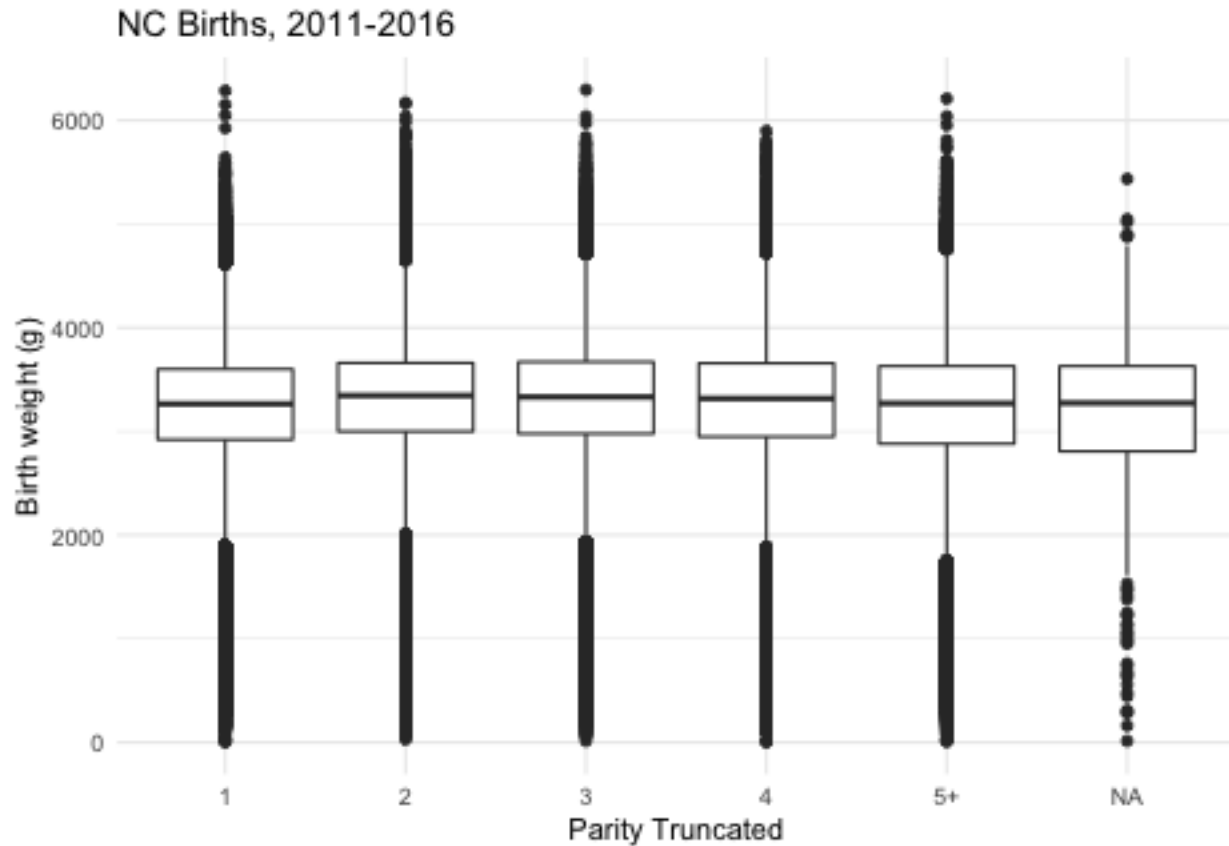
```
# Rerun EDA with truncated data
```

```
births$PARITY_truncated = as.factor(births$PARITY_truncated)
ggplot(births, aes(x = PARITY_truncated)) +
  stat_count() +
  theme_minimal()
```



```
ggplot(data = births, mapping = aes(x = PARITY_truncated, y = BWTG)) +
  geom_boxplot() + xlab("Parity Truncated") + ylab("Birth weight (g)") +
  ggtitle("NC Births, 2011-2016") +
  theme_minimal()
```

```
## Warning: Removed 430 rows containing non-finite values (stat_boxplot).
```



```
parity_truncated_reg = lm(BWTG ~ PARITY_truncated, births)
summary(parity_truncated_reg)
```

```
##
## Call:
## lm(formula = BWTG ~ PARITY_truncated, data = births)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3272.9  -303.2    48.7   383.1  3061.8
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   3223.242     1.259  2559.251 < 2e-16 ***
## PARITY_truncated2    70.877     1.858   38.150 < 2e-16 ***
## PARITY_truncated3    63.680     2.125   29.972 < 2e-16 ***
## PARITY_truncated4    40.306     2.645   15.239 < 2e-16 ***
## PARITY_truncated5+  -11.939     2.589   -4.612 3.99e-06 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 617.8 on 720641 degrees of freedom
## (1046 observations deleted due to missingness)
## Multiple R-squared: 0.003014, Adjusted R-squared: 0.003008
## F-statistic: 544.6 on 4 and 720641 DF, p-value: < 2.2e-16
```

Independent of other variables, we see a negative relationship between parity and birth weight past the first child. The frequency of parity decreases in an exponential fashion. A second variable was created that truncates parities of at least five to improve interpretability and prevent overfitting. The quantity of missing data is relatively small.

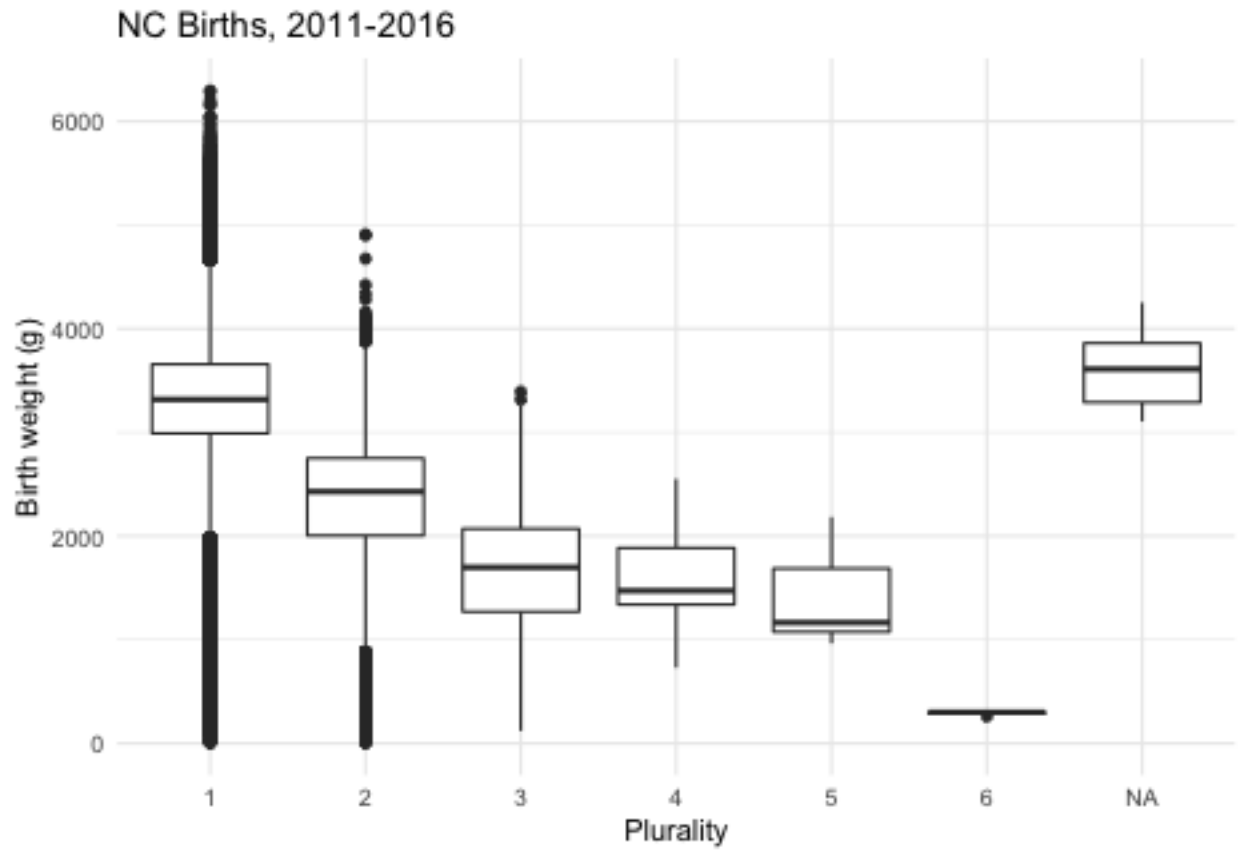
Plurality

```
# Check the plurality frequencies
births$PLUR = as.numeric(births$PLUR)

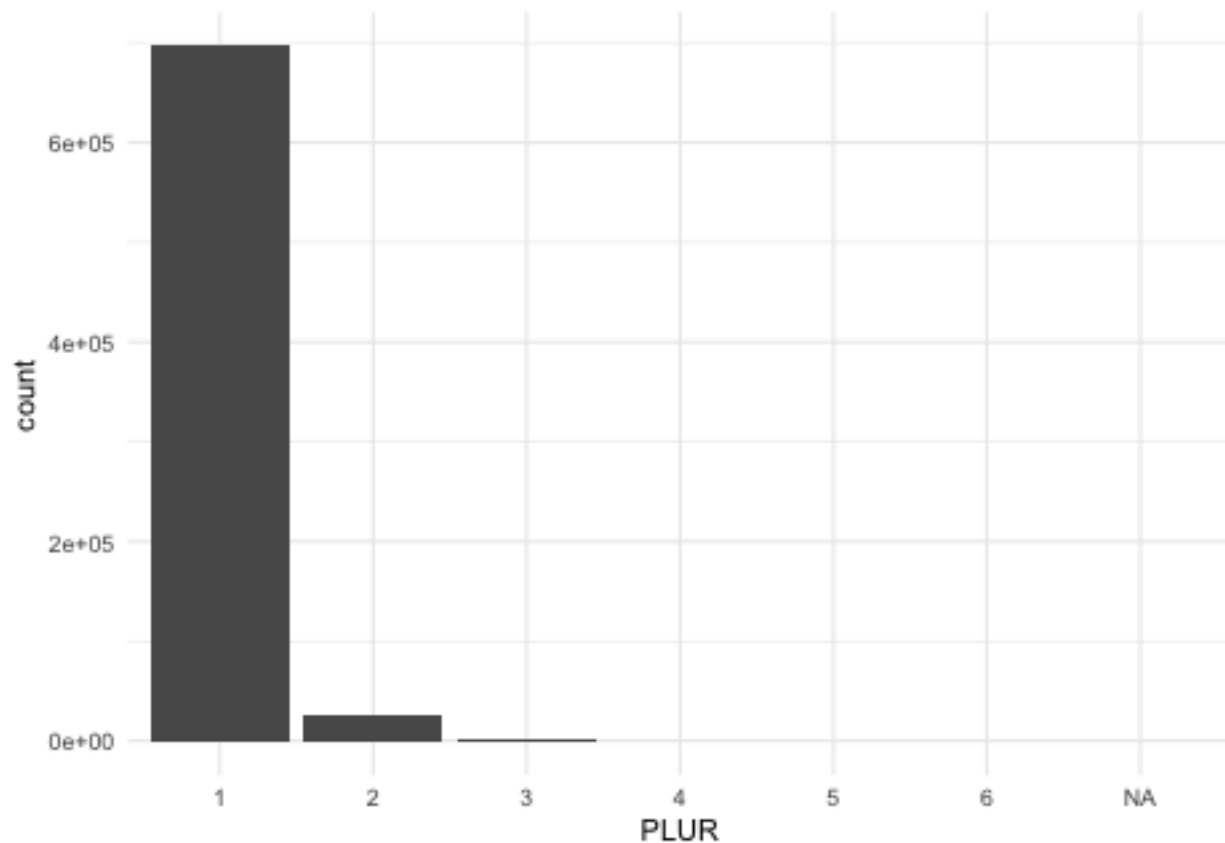
births = births %>%
  mutate(PLUR_truncated = ifelse(PLUR > 2, "3+", PLUR))

births$PLUR = as.factor(births$PLUR)
ggplot(data = births, mapping = aes(x = PLUR, y = BWTG)) +
  geom_boxplot() +
  xlab("Plurality") +
  ylab("Birth weight (g)") +
  ggtitle("NC Births, 2011-2016") +
  theme_minimal()
```

```
## Warning: Removed 430 rows containing non-finite values (stat_boxplot).
```



```
ggplot(births, aes(x = PLUR)) +  
  stat_count() +  
  theme_minimal()
```



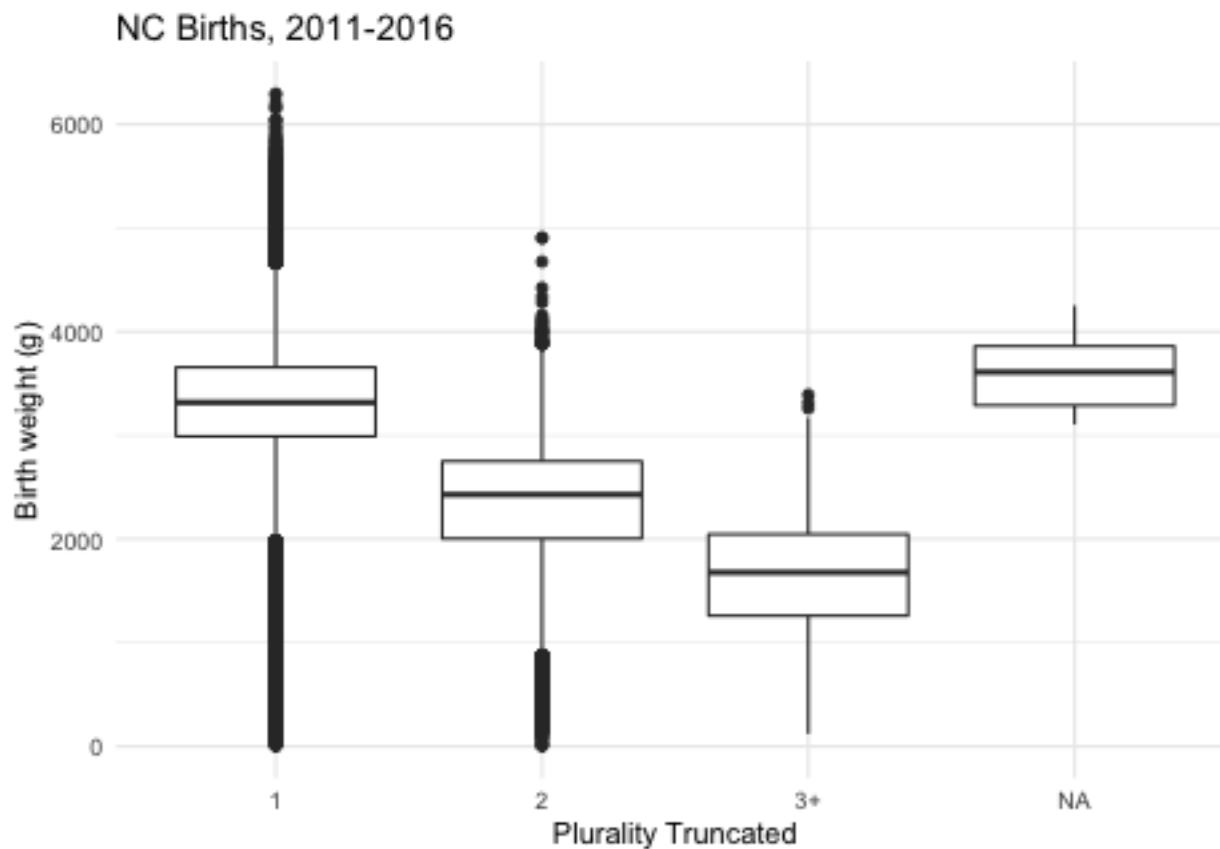
```
plurality_reg = lm(BWTG ~ PLUR, births)
summary(plurality_reg)
```

```
##
## Call:
## lm(formula = BWTG ~ PLUR, data = births)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3287.1  -302.1    28.9   364.9  3001.9
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  3292.1374     0.7085  4646.93 <2e-16 ***
## PLUR2        -969.8739     3.8495  -251.95 <2e-16 ***
## PLUR3       -1632.6058    21.4519   -76.11 <2e-16 ***
## PLUR4       -1767.3874    132.1681   -13.37 <2e-16 ***
## PLUR5       -1899.7374    186.9125   -10.16 <2e-16 ***
## PLUR6       -2999.9707    241.3023   -12.43 <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 591.1 on 721251 degrees of freedom
## (435 observations deleted due to missingness)
## Multiple R-squared:  0.08785,    Adjusted R-squared:  0.08784
## F-statistic: 1.389e+04 on 5 and 721251 DF,  p-value: < 2.2e-16
```

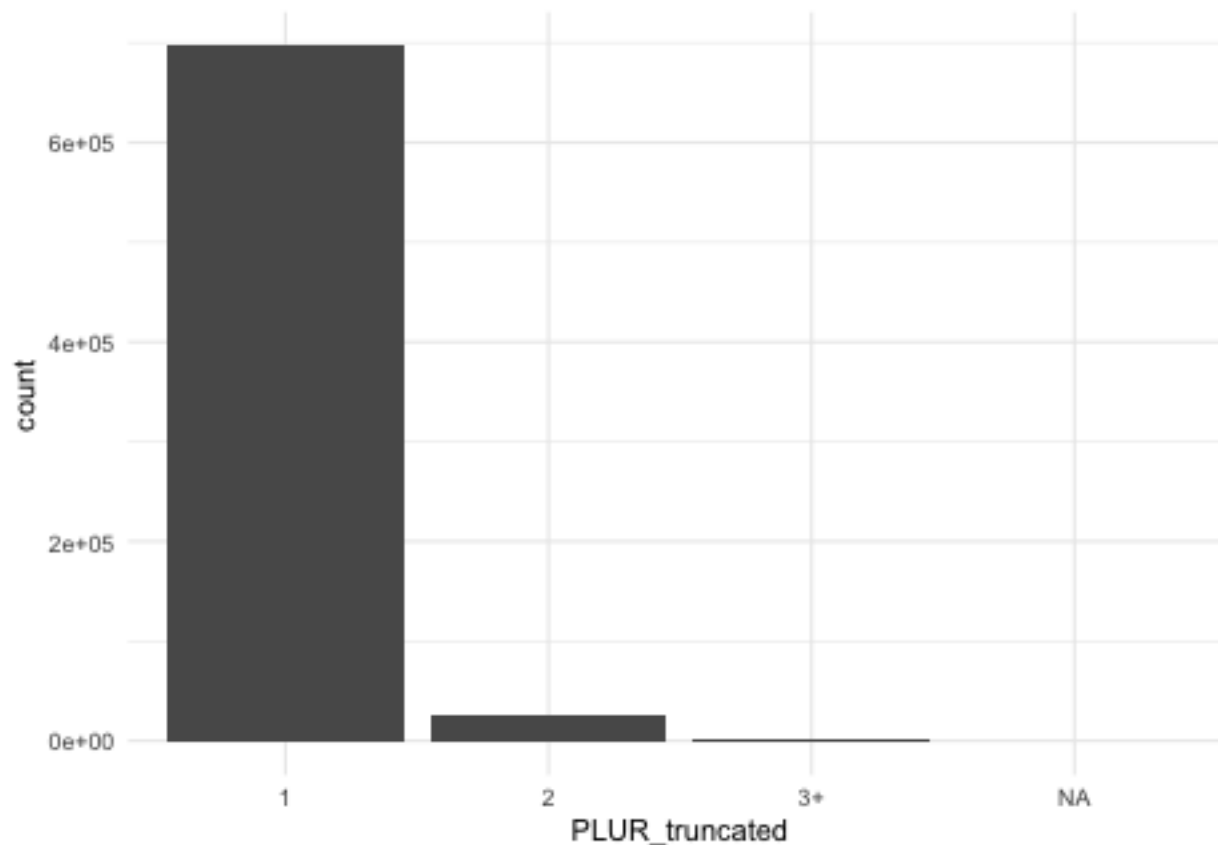
```
births$PLUR_truncated = as.factor(births$PLUR_truncated)
```

```
ggplot(data = births, mapping = aes(x = PLUR_truncated, y = BWTG)) +  
  geom_boxplot() +  
  xlab("Plurality Truncated") +  
  ylab("Birth weight (g)") +  
  ggtitle("NC Births, 2011-2016") +  
  theme_minimal()
```

```
## Warning: Removed 430 rows containing non-finite values (stat_boxplot).
```



```
ggplot(births, aes(x = PLUR_truncated)) +  
  stat_count() +  
  theme_minimal()
```



```
plurality_reg_truncated = lm(BWTG ~ PLUR_truncated, births)
summary(plurality_reg_truncated)
```

```
##
## Call:
## lm(formula = BWTG ~ PLUR_truncated, data = births)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3287.1  -302.1    28.9   364.9  3001.9
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   3292.1374     0.7085  4646.8  <2e-16 ***
## PLUR_truncated2 -969.8739     3.8496  -251.9  <2e-16 ***
## PLUR_truncated3+ -1649.6550    20.9622   -78.7  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 591.1 on 721254 degrees of freedom
## (435 observations deleted due to missingness)
## Multiple R-squared:  0.0878, Adjusted R-squared:  0.0878
## F-statistic: 3.471e+04 on 2 and 721254 DF, p-value: < 2.2e-16
```

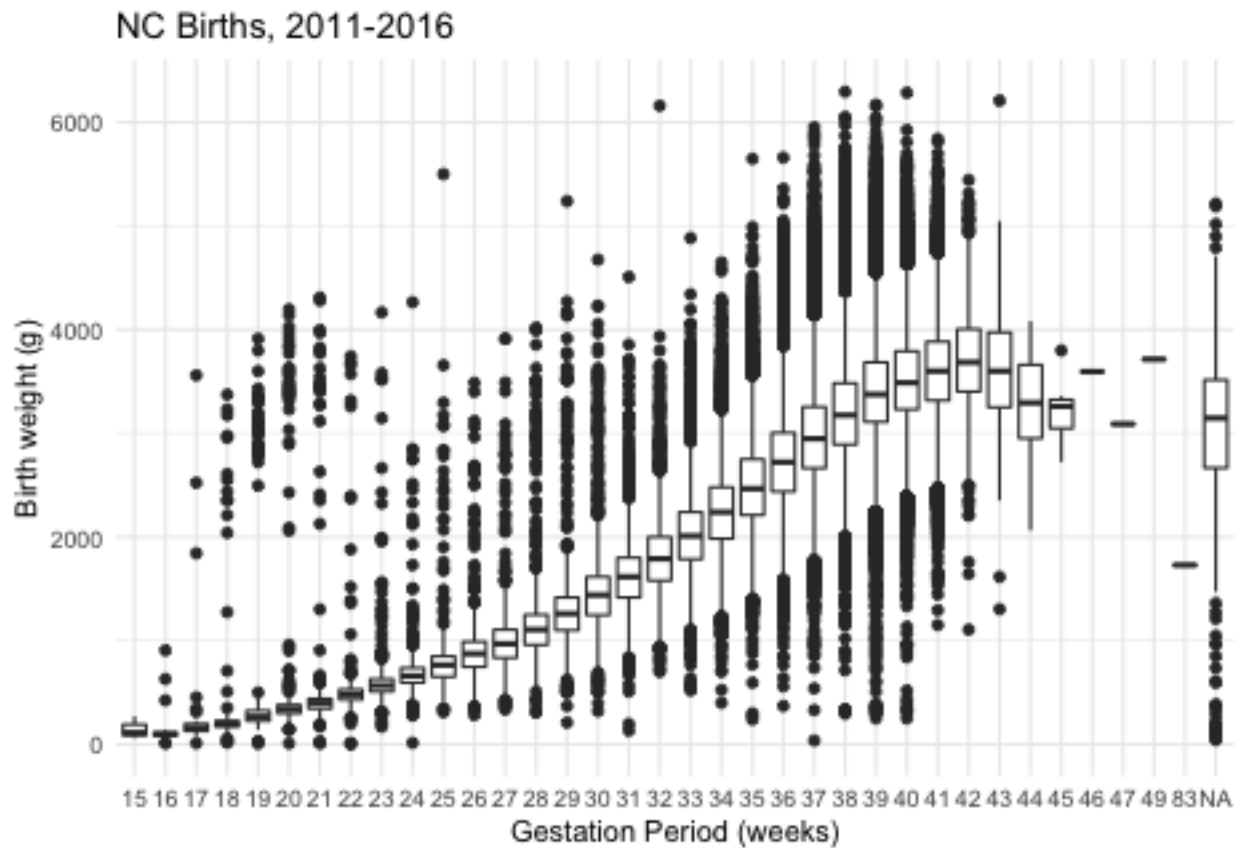
We see a strong non linear negative relationship between plurality and birth weight. The frequency of pluralities above two is extremely small, and we again see a proportionally small amount of missing data. A second variable was created that truncates pluralities of at least three to improve interpretability and prevent

overfitting

Gestation

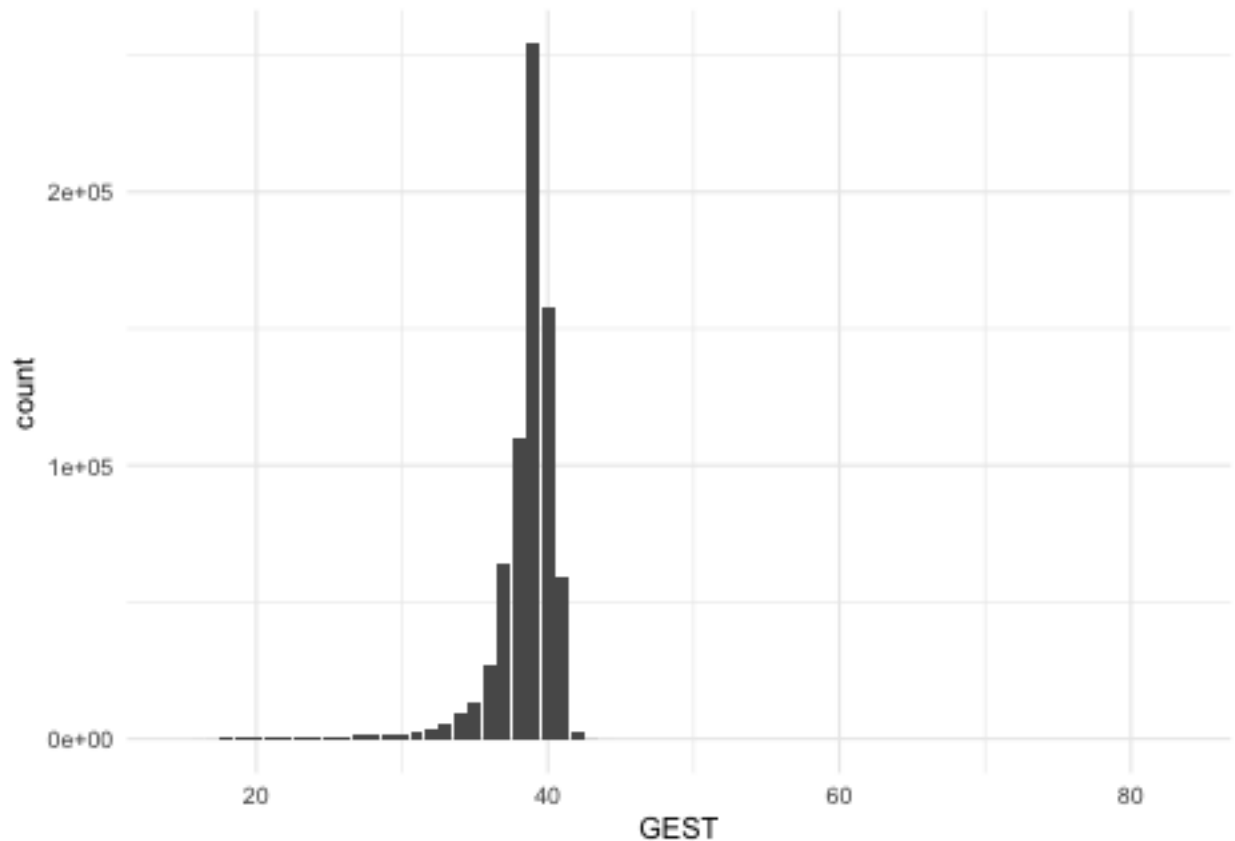
```
ggplot(data = births, mapping = aes(x = as.factor(GEST), y = BWTG)) +  
  xlab("Gestation Period (weeks)") +  
  ylab("Birth weight (g)") +  
  geom_boxplot() +  
  ggtitle("NC Births, 2011-2016") +  
  theme_minimal()
```

Warning: Removed 430 rows containing non-finite values (stat_boxplot).



```
ggplot(births, aes(x = GEST)) +  
  stat_count() +  
  theme_minimal()
```

Warning: Removed 539 rows containing non-finite values (stat_count).



```
gest_reg = lm(BWTG ~ GEST, births)
summary(gest_reg)
```

```
##
## Call:
## lm(formula = BWTG ~ GEST, data = births)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9797.7  -299.6   -20.5    276.2   4752.2
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -3898.2669     8.8696  -439.5  <2e-16 ***
## GEST         185.8433     0.2299   808.2  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 448.1 on 720801 degrees of freedom
## (889 observations deleted due to missingness)
## Multiple R-squared:  0.4754, Adjusted R-squared:  0.4754
## F-statistic: 6.532e+05 on 1 and 720801 DF, p-value: < 2.2e-16
```

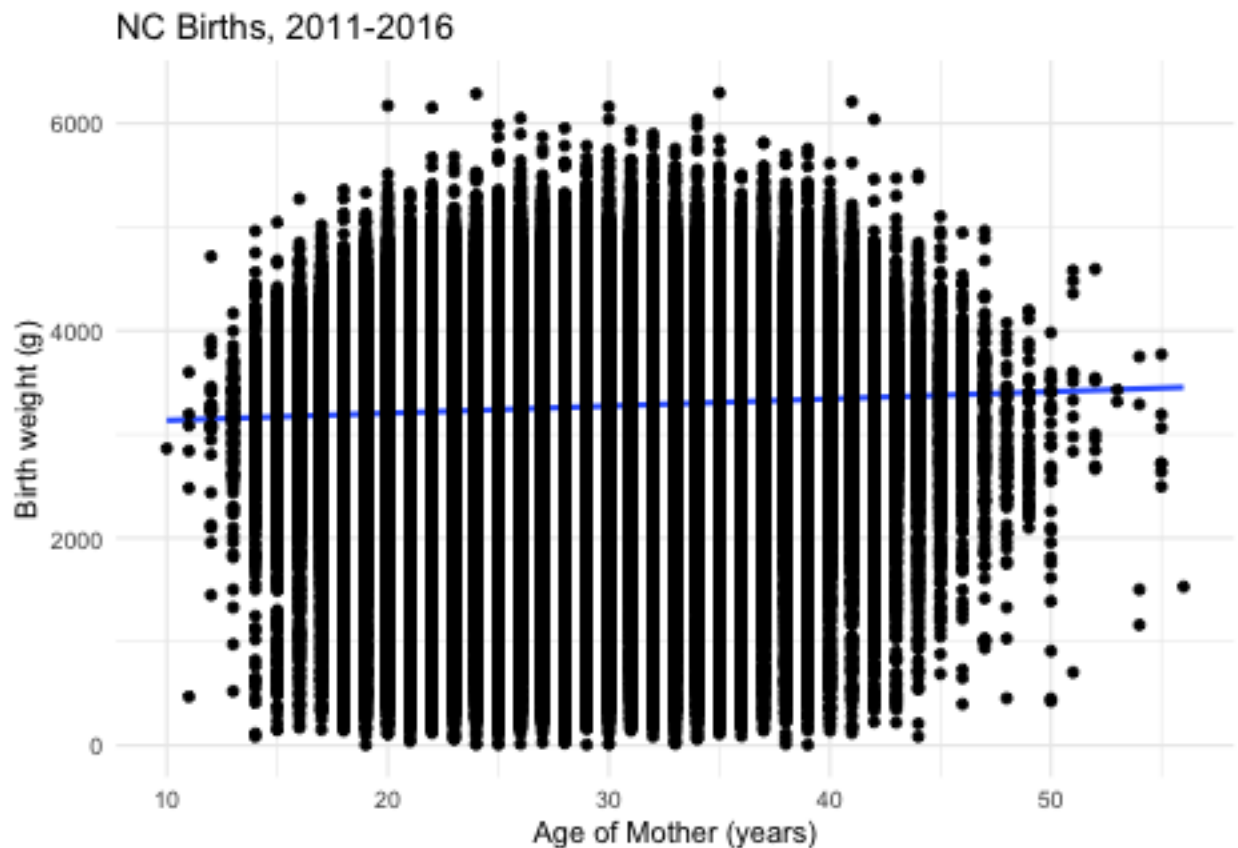
There appears to be a non linear positive relationship between gestation period and birth weight. The mean gestational period is approximately 38.5 weeks and the period with the highest median weight is 42 weeks. The frequency distribution is left skewed with the majority of babies having a gestational period between 38 and 40 weeks. There is some concern that more extreme gestational periods may lead to higher variance, and

it should be noted that there is a chunk of data points with gestational periods of 17 to 21 weeks that have much higher than expected birth weights. There is an extreme outlier with gestational age of 83 weeks. Given that this data point was probably incorrectly recorded, we will exclude it from our analysis when building the model.

Age of Mother

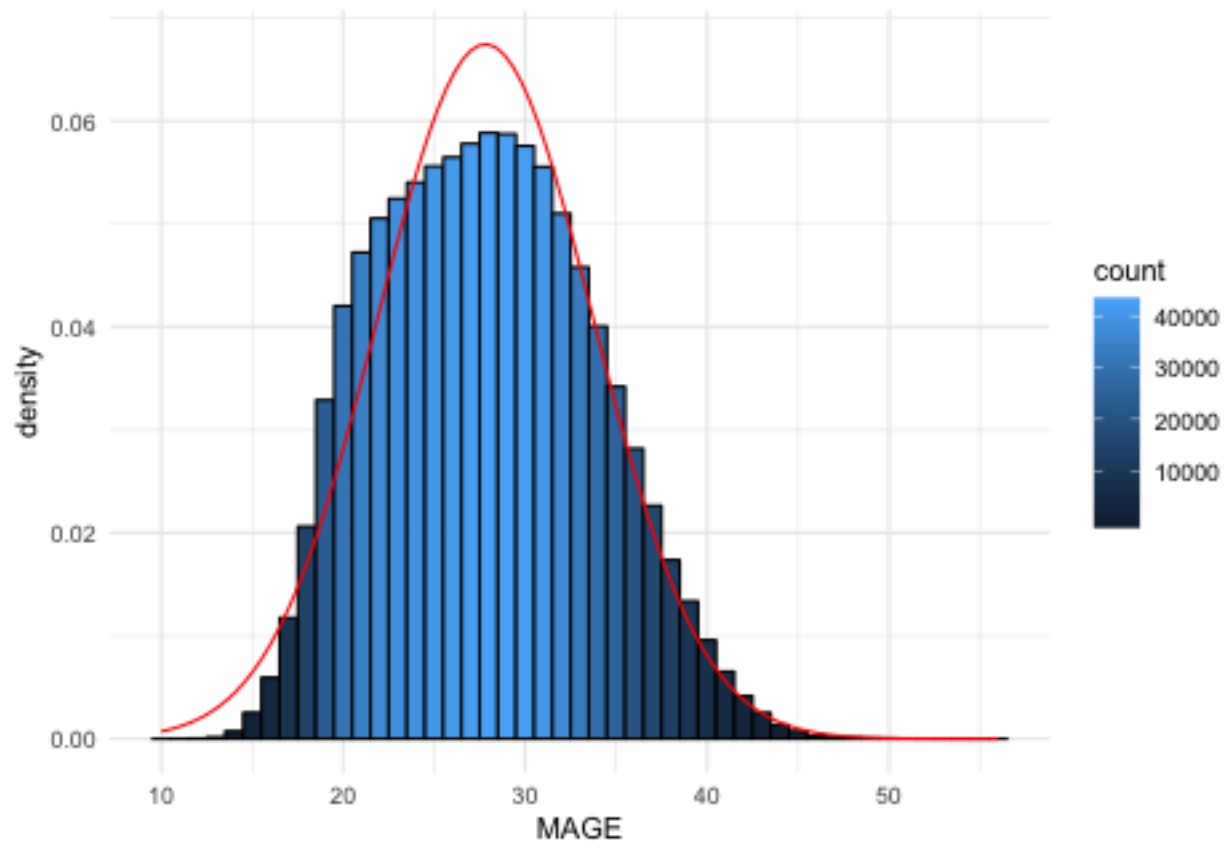
```
ggplot(data = births, mapping = aes(x = MAGE, y = BWTG)) +
  xlab("Age of Mother (years)") +
  ylab("Birth weight (g)") +
  geom_smooth(method='lm', na.rm = TRUE) +
  geom_point() +
  ggtitle("NC Births, 2011-2016") +
  theme_minimal()
```

Warning: Removed 457 rows containing missing values (geom_point).



```
ggplot(births, aes(x = MAGE)) +
  geom_histogram(binwidth=1, colour="black",
    aes(y=..density.., fill=..count..), position = "stack") +
  stat_function(fun = dnorm, color = "red", args = list(mean = mean(births$MAGE, na.rm = TRUE), sd = sd
  theme_minimal()
```

Warning: Removed 27 rows containing non-finite values (stat_bin).



```
mage_reg = lm(BWTG ~ MAGE, births)
summary(mage_reg)
```

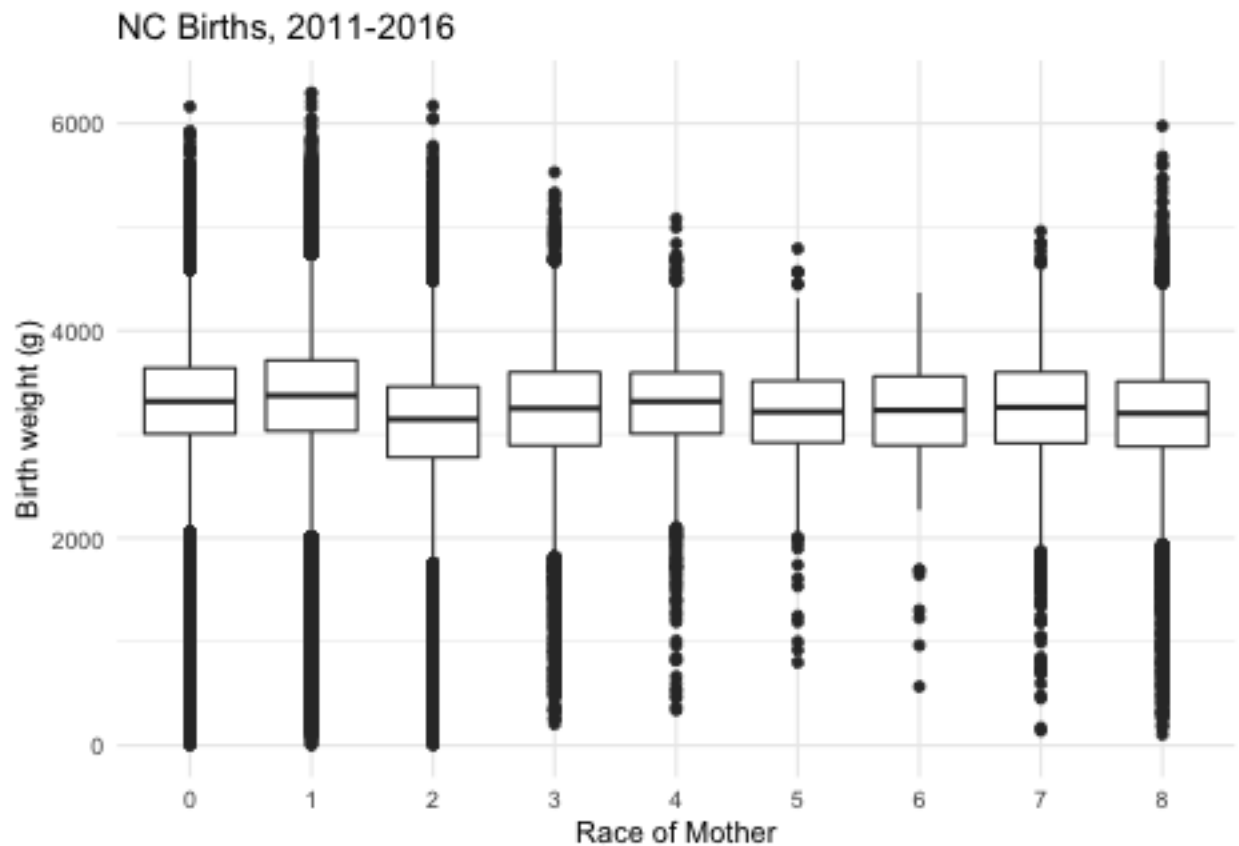
```
##
## Call:
## lm(formula = BWTG ~ MAGE, data = births)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3330.1  -302.3    49.7   383.5  3053.9
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3064.715      3.496   876.58 <2e-16 ***
## MAGE         6.932       0.123   56.38 <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 617.5 on 721233 degrees of freedom
## (457 observations deleted due to missingness)
## Multiple R-squared:  0.004388, Adjusted R-squared:  0.004386
## F-statistic: 3178 on 1 and 721233 DF, p-value: < 2.2e-16
```

Mother's age seems to be fairly normally distributed with a mean of 27.8. There appears to be a positive relationship between the age of the mother and the birth weight. There is no evidence to suggest that the birth weight variance is not constant across the mother's age.

Race of Mother

```
births$MRACER = as.factor(births$MRACER)
ggplot(data = births, mapping = aes(x = MRACER, y = BWTG)) +
  xlab("Race of Mother") +
  ylab("Birth weight (g)") +
  geom_boxplot() +
  ggtitle("NC Births, 2011-2016") +
  theme_minimal()
```

```
## Warning: Removed 430 rows containing non-finite values (stat_boxplot).
```

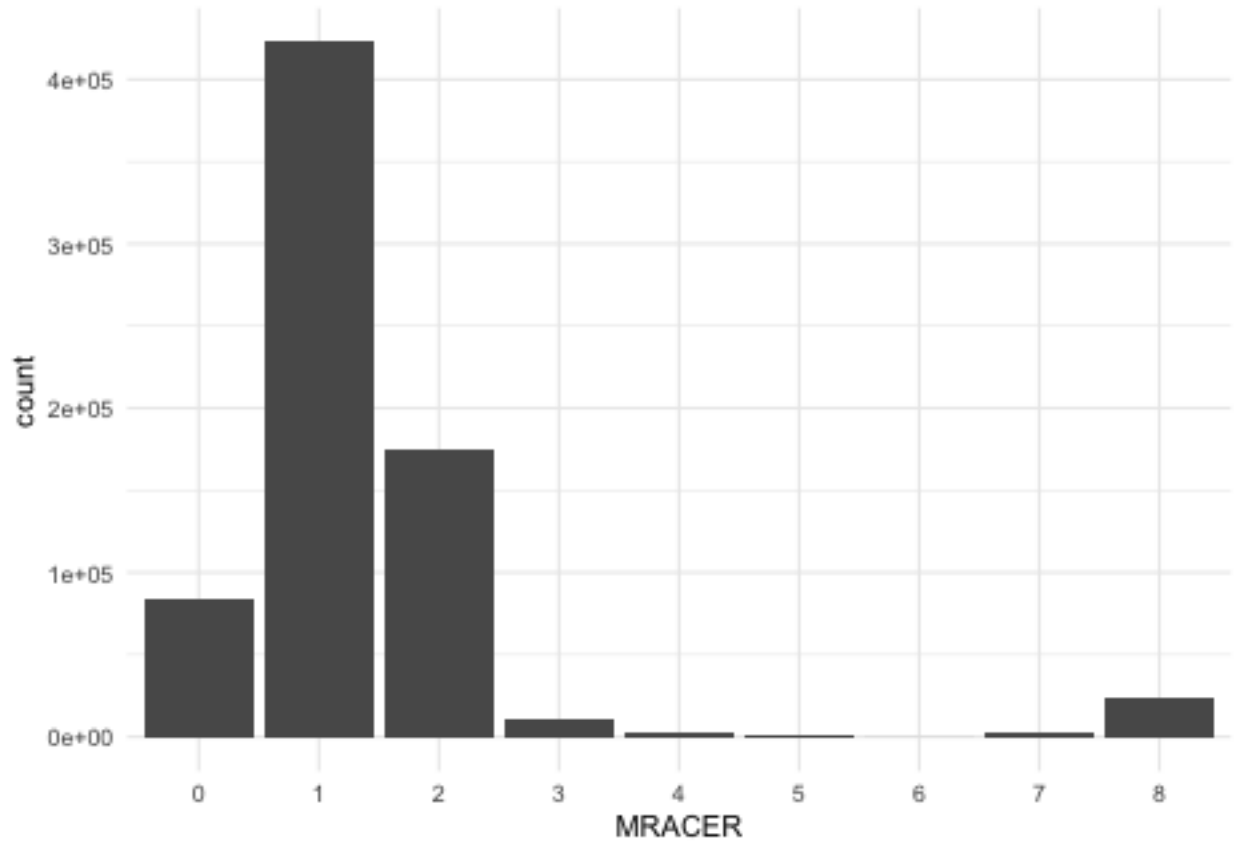


```
bw_race_avgs = births %>%
  group_by(MRACER) %>%
  summarize(mweight = mean(BWTG, na.rm = TRUE), freq_percent = n()/nrow(births))
bw_race_avgs
```

```
## # A tibble: 9 x 3
##   MRACER mweight freq_percent
##   <fct>   <dbl>     <dbl>
## 1 0      3292.     0.117
## 2 1      3335.     0.586
## 3 2      3069.     0.243
## 4 3      3196.     0.0141
## 5 4      3285.     0.00463
## 6 5      3193.     0.000806
```

```
## 7 6      3148      0.000132
## 8 7      3218.      0.00294
## 9 8      3169.      0.0322
```

```
ggplot(births, aes(x = MRACER)) +
  stat_count() +
  theme_minimal()
```



```
mage_reg = lm(BWTG ~ MRACER, births)
summary(mage_reg)
```

```
##
## Call:
## lm(formula = BWTG ~ MRACER, data = births)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3331.1  -301.3    48.7   378.9  3100.7
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  3291.649     2.095  1571.411 < 2e-16 ***
## MRACER1       43.495     2.295   18.956 < 2e-16 ***
## MRACER2    -222.359     2.550  -87.191 < 2e-16 ***
## MRACER3     -95.772     6.394  -14.978 < 2e-16 ***
## MRACER4      -7.146    10.741   -0.665  0.505820
## MRACER5     -98.199    25.315   -3.879  0.000105 ***
```

```
## MRACER6      -143.649      62.479    -2.299 0.021496 *
## MRACER7      -73.792      13.377    -5.516 3.46e-08 ***
## MRACER8     -122.502       4.511   -27.159 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 608.6 on 721253 degrees of freedom
## (430 observations deleted due to missingness)
## Multiple R-squared:  0.03285,    Adjusted R-squared:  0.03284
## F-statistic: 3062 on 8 and 721253 DF,  p-value: < 2.2e-16
```

0 - non-white,, 1 = white, 2 black, 3 indian, 8 other asian

There are significant differences between the average birth weights of mother's of different races. We see that mother's that self identified as white have the largest mean baby weight at 3.33 kg, while black mother's have the lowest mean baby weight at only 3.07 kg. 58 percent of mother's identify as white, 24 percent identify as black, 12 percent identify as non-white, and 3 percent identify as other asian.

County / Socioeconomic Status

```
#calculate infant mortality by county, to use as a proxy for socioeconomic status
deaths_by_county = deaths %>%
  group_by(county) %>%
  summarize(n_deaths = n()) %>%
  rename(CORES=county)

births_by_county = births %>%
  group_by(CORES) %>%
  summarize(n_births = n())

infant_mortality = merge(deaths_by_county, births_by_county, by = "CORES") %>%
  mutate(mortality = n_deaths/n_births*100) %>% #note: mortality rate is as percentage
  select(-n_births, -n_deaths)

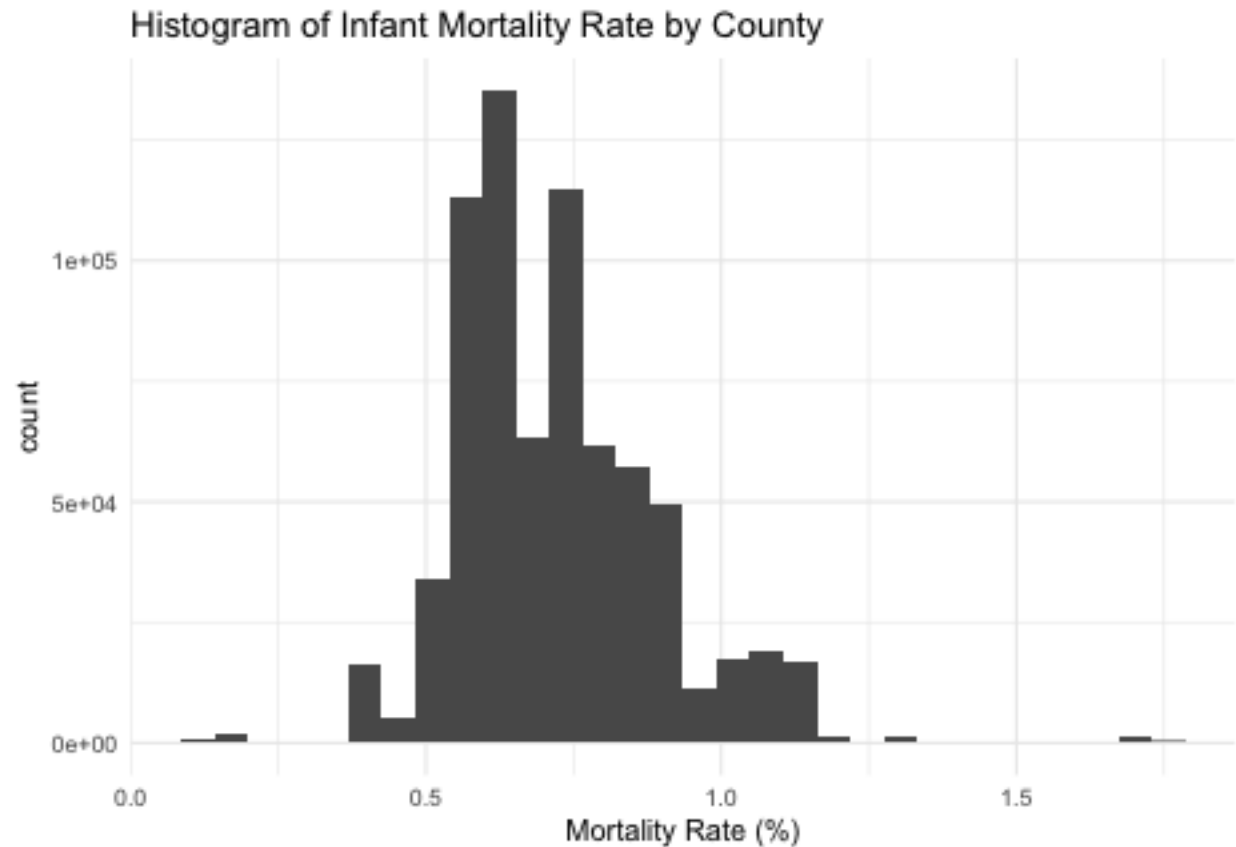
births = merge(births, infant_mortality, by = "CORES")

summary(births$mortality)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
## 0.1166 0.6149 0.7009 0.7203 0.7958 1.7606
```

```
ggplot(births, aes(x= mortality))+
  geom_histogram() +
  xlab("Mortality Rate (%)")+
  theme_minimal() +
  ggtitle("Histogram of Infant Mortality Rate by County")
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



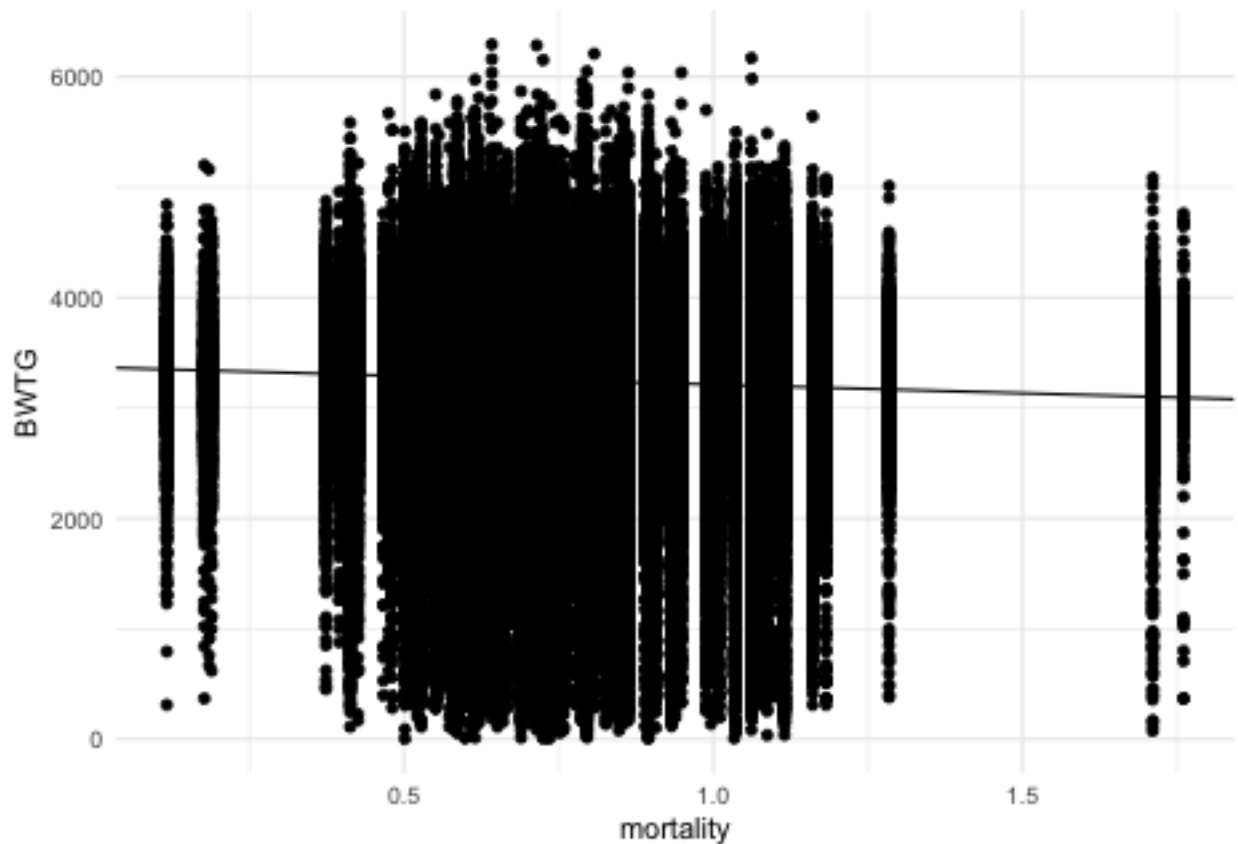
```
bwtg_vs_mortality = lm(data = births, BWTG~mortality)
summary(bwtg_vs_mortality)
```

```
##
## Call:
## lm(formula = BWTG ~ mortality, data = births)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3286.9  -303.6    45.3   382.9  3026.6
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  3370.843      3.187 1057.66  <2e-16 ***
## mortality    -157.360      4.308  -36.53  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 618.3 on 721260 degrees of freedom
## (430 observations deleted due to missingness)
## Multiple R-squared:  0.001846,    Adjusted R-squared:  0.001845
## F-statistic: 1334 on 1 and 721260 DF,  p-value: < 2.2e-16
```

```
ggplot(births, aes(x = mortality, y = BWTG))+
  geom_point() +
  geom_abline(slope = bwtg_vs_mortality$coefficients[[2]], intercept = bwtg_vs_mortality$coefficients[[1]])
  theme_minimal()
```



```
## Warning: Removed 430 rows containing missing values (geom_point).
```



We chose to use infant mortality rate of birth county as a proxy for socioeconomic status, calculated as number of deaths before the age of 1 divided by total number of births in a county. The median county in the data had a infant mortality rate of 0.7%, with the range of infant mortality rates in our dataset ranging from 0.12% to 1.76%. Infant mortality rate of birth county and birth weight appear to have a weak negative linear relationship, and in isolation, a 1 percentage point increase in infant mortality rate is associated with a 157g decrease in expected birth weight.

Build Model

```
births_excl = na.omit(births)
births_excl = births_excl[which(births_excl$GEST < 80), ]
births_excl = births_excl %>%
  mutate(GEST2 = GEST^2, GEST3 = GEST ^ 3, GEST4 = GEST^4)
model1 = lm(data = births_excl, BWTG ~ GEST + PARITY_truncated + PLUR_truncated + smoking_type + MAGE +
  summary(model1))
```

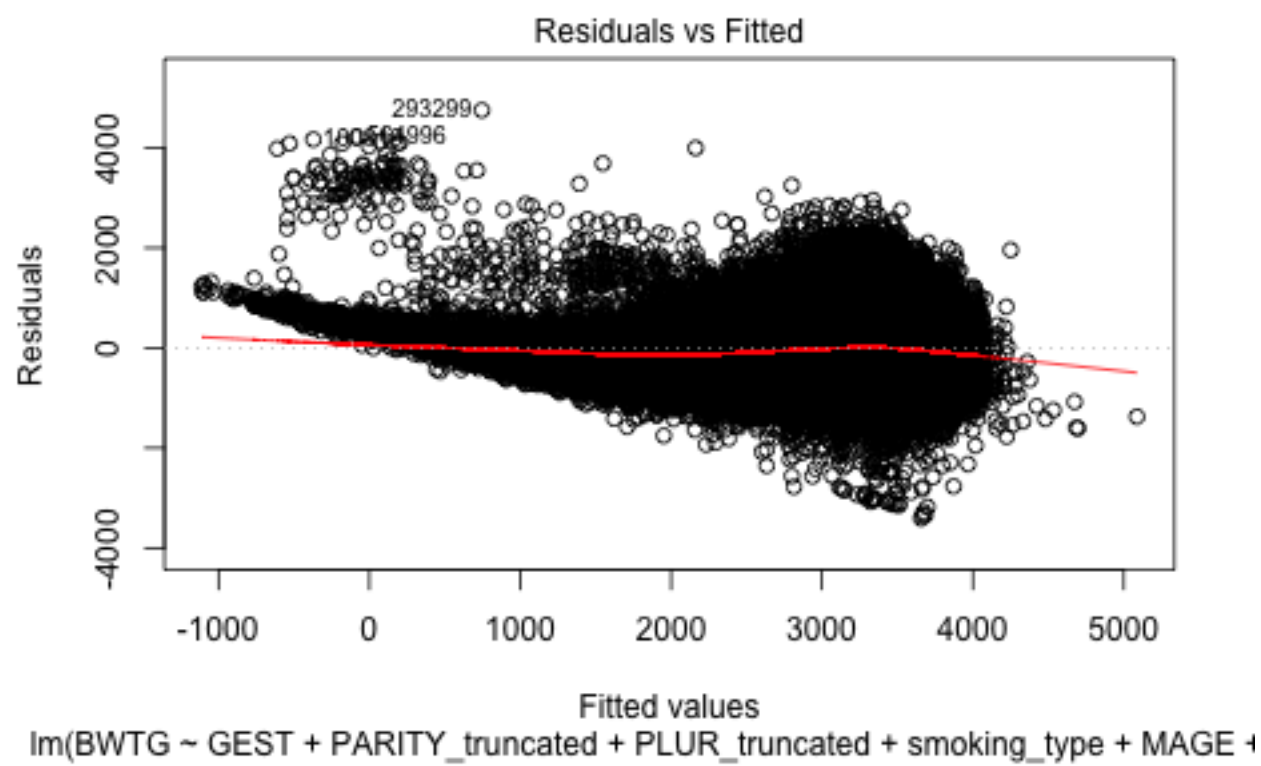
```
##
## Call:
## lm(formula = BWTG ~ GEST + PARITY_truncated + PLUR_truncated +
##       smoking_type + MAGE + MRACER + mortality, data = births_excl,
##       na.action = "na.exclude")
##
## Residuals:
```

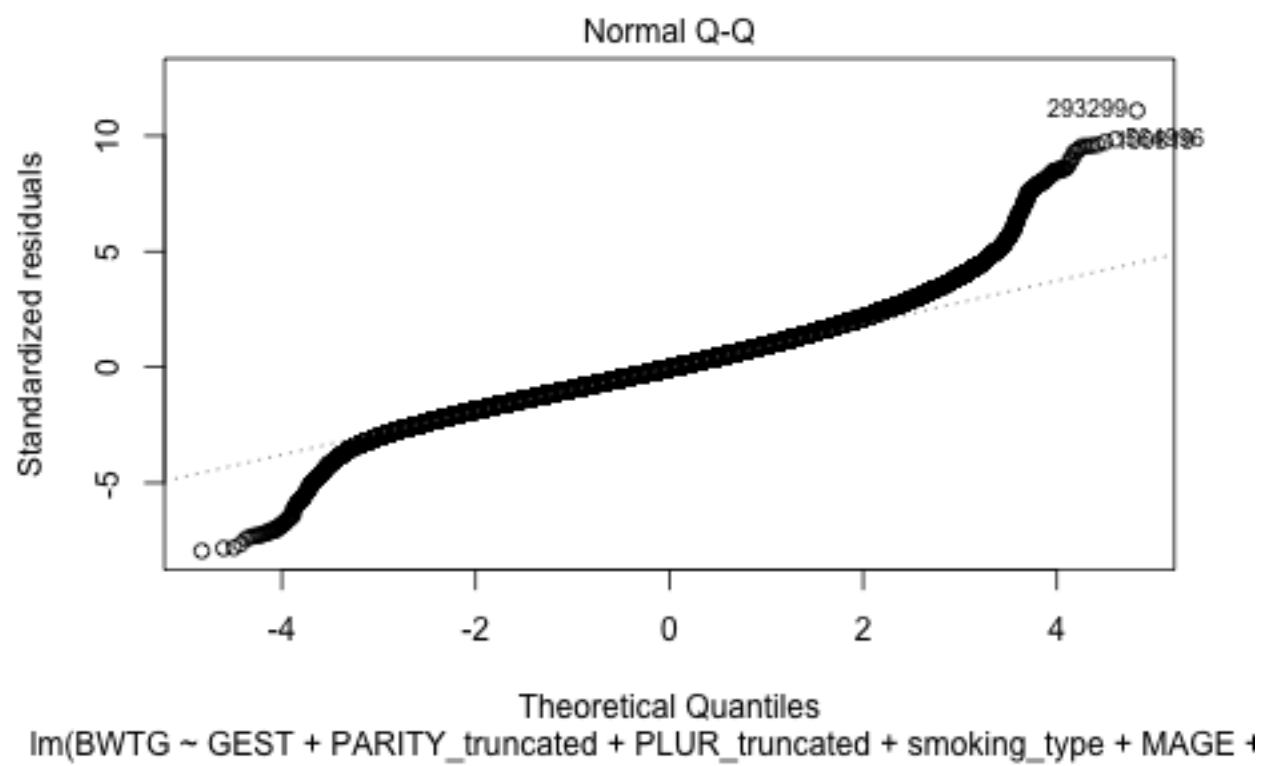
```

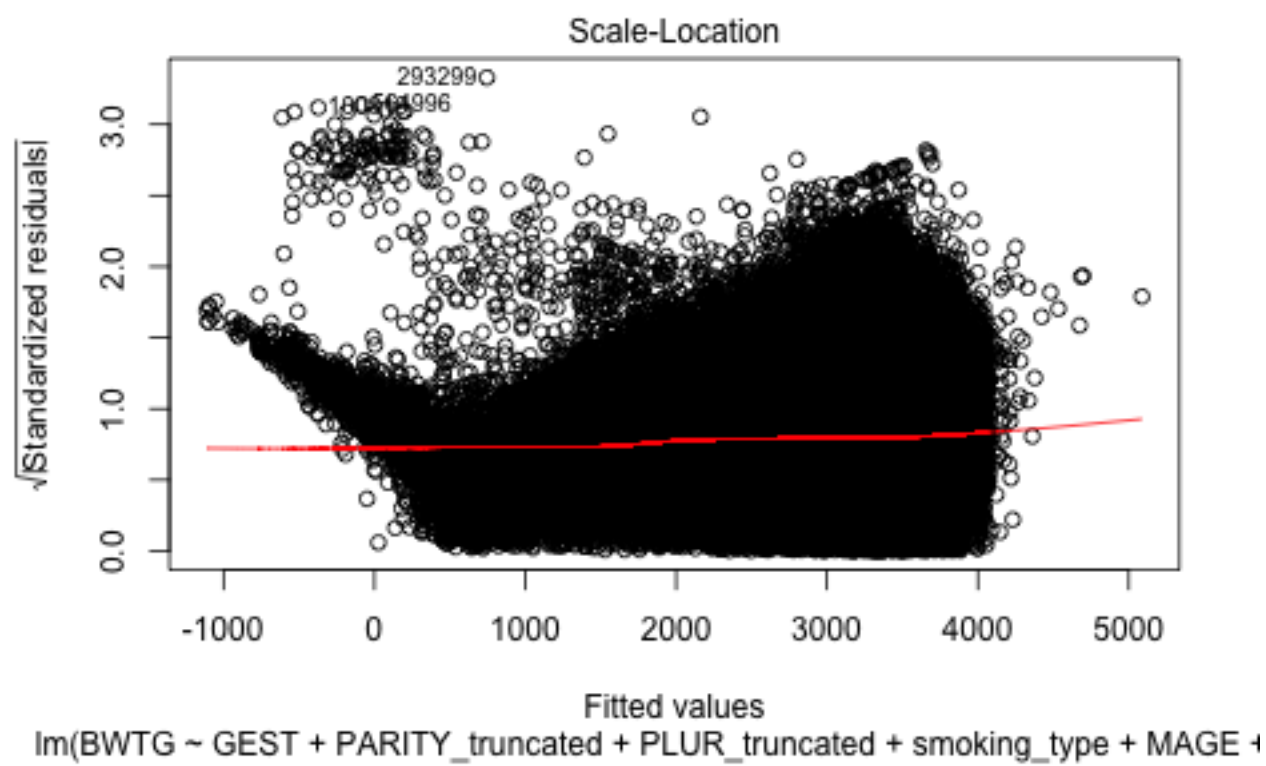
##      Min      1Q  Median      3Q      Max
## -3406.6 -282.9   -19.5   260.9  4754.8
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    -3691.4357      9.9287 -371.794 < 2e-16 ***
## GEST           175.2014      0.2336  749.962 < 2e-16 ***
## PARITY_truncated2    94.7007      1.3162   71.951 < 2e-16 ***
## PARITY_truncated3   113.4321      1.5379   73.756 < 2e-16 ***
## PARITY_truncated4   117.1821      1.9259   60.845 < 2e-16 ***
## PARITY_truncated5+  117.7775      1.9533   60.298 < 2e-16 ***
## PLUR_truncated2    -360.9193      2.9312 -123.128 < 2e-16 ***
## PLUR_truncated3+   -454.9182     15.3979  -29.544 < 2e-16 ***
## smoking_typebefore and during -204.8236      1.7697 -115.737 < 2e-16 ***
## smoking_typebefore only    -11.4791      2.7026   -4.247 2.16e-05 ***
## smoking_typeduring only   -165.3562      9.1294  -18.113 < 2e-16 ***
## MAGE              4.5889      0.0964   47.602 < 2e-16 ***
## MRACER1           83.5128      1.6596   50.323 < 2e-16 ***
## MRACER2          -99.3238      1.8206  -54.555 < 2e-16 ***
## MRACER3           -4.8456      4.5757   -1.059 0.290
## MRACER4          -33.5469      7.6017   -4.413 1.02e-05 ***
## MRACER5         -114.3371     17.9406   -6.373 1.85e-10 ***
## MRACER6           24.2023     44.0275    0.550 0.583
## MRACER7          -14.8664      9.4582   -1.572 0.116
## MRACER8         -102.9048      3.2079  -32.078 < 2e-16 ***
## mortality          23.1876      3.1019    7.475 7.72e-14 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 428.9 on 717848 degrees of freedom
## Multiple R-squared:  0.5184, Adjusted R-squared:  0.5184
## F-statistic: 3.864e+04 on 20 and 717848 DF,  p-value: < 2.2e-16

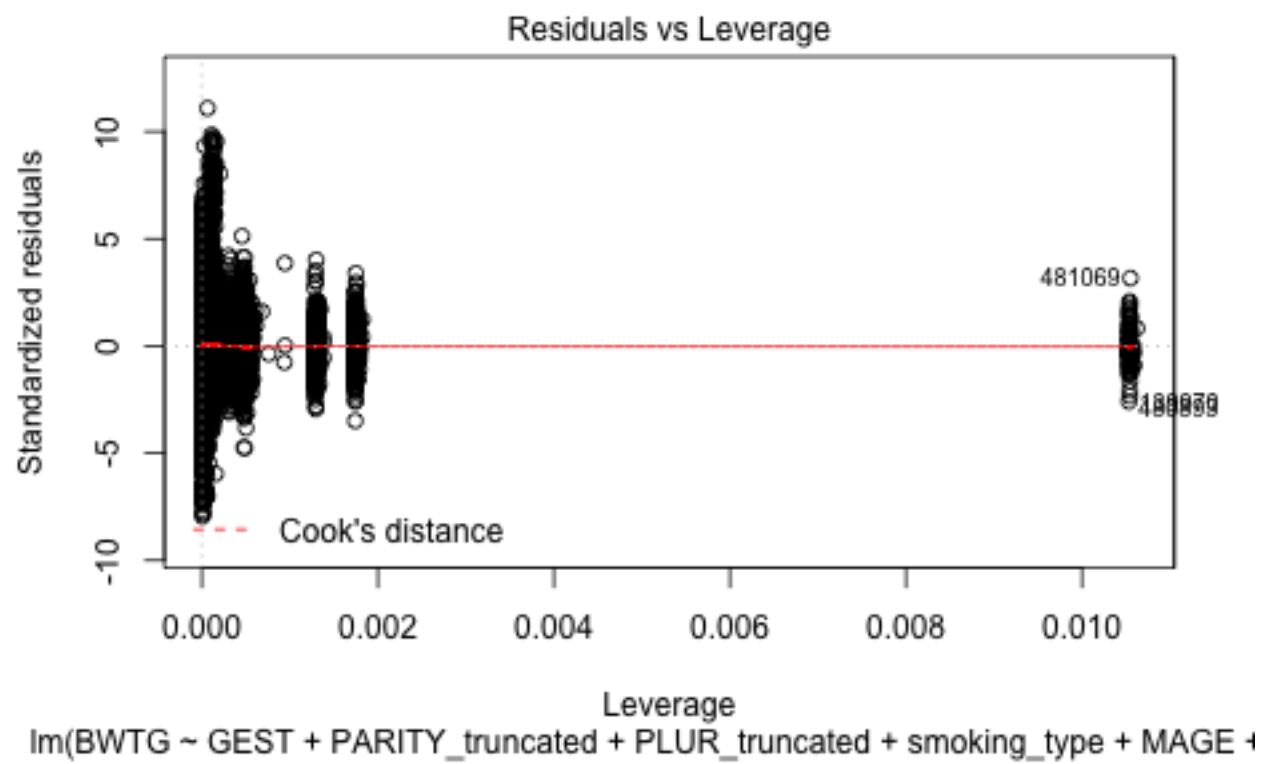
```

```
plot(model1)
```

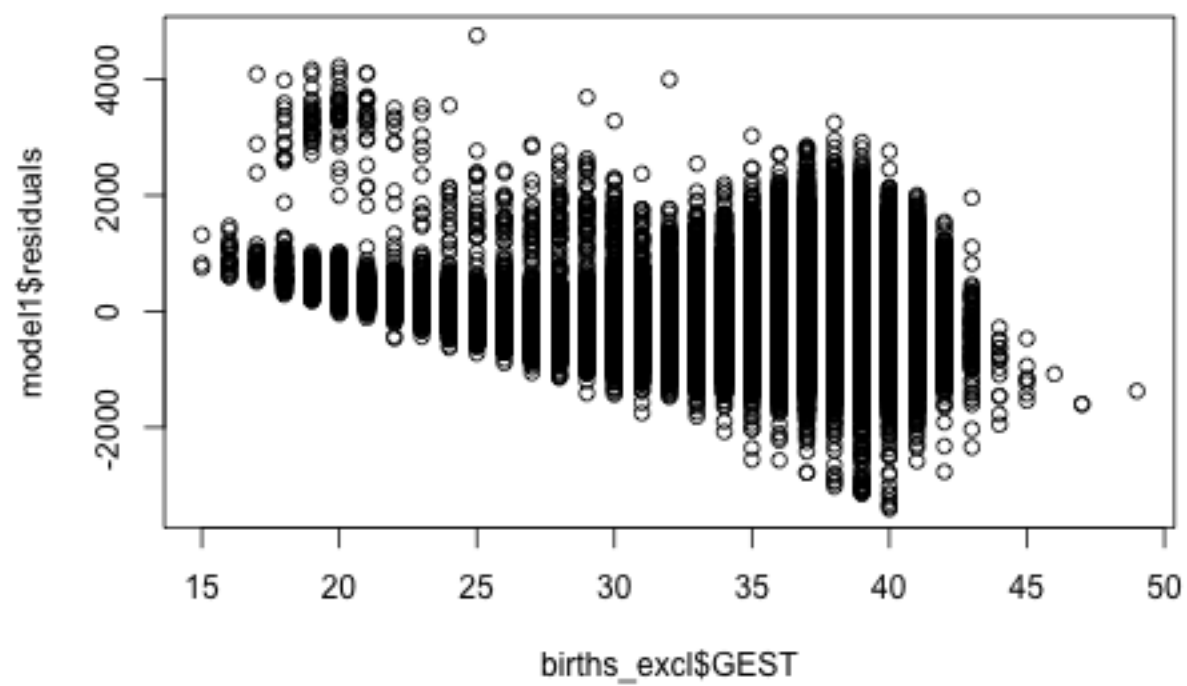




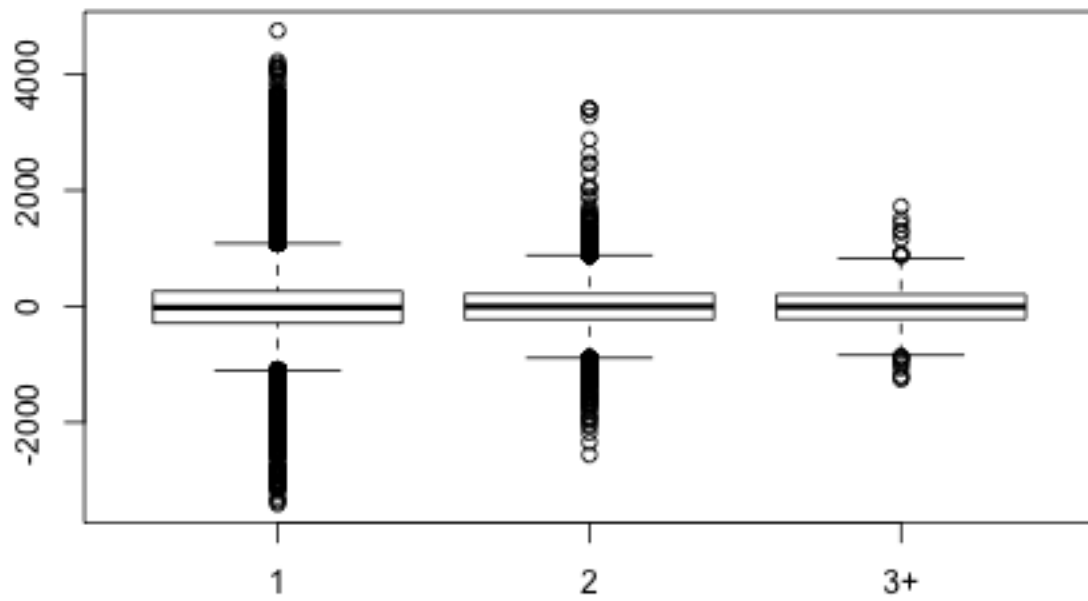




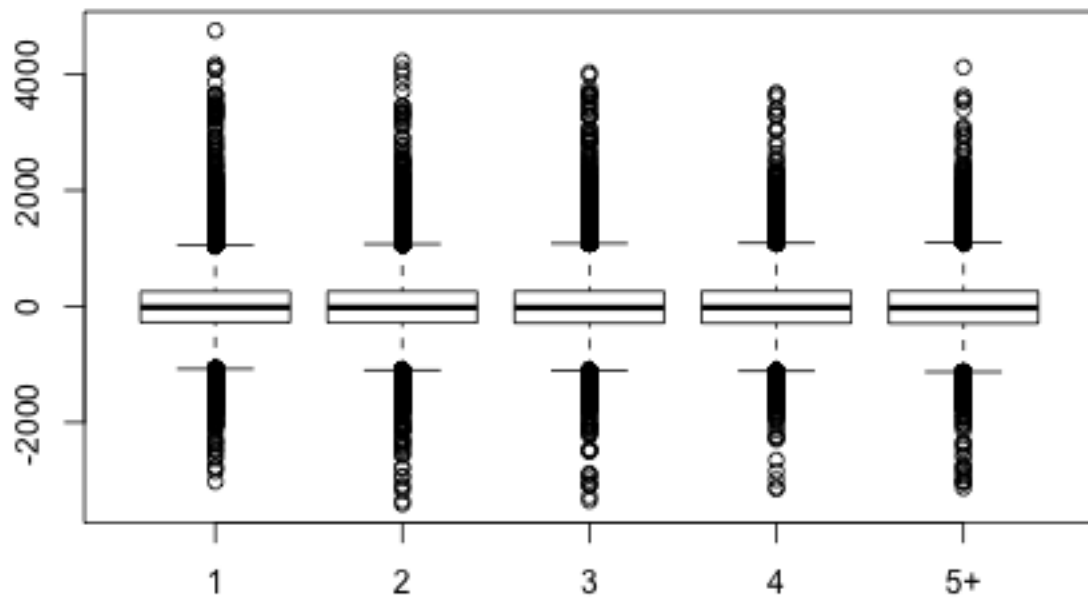
```
# plot(model1$fitted.values, model1$residuals)
plot(births_excl$GEST, model1$residuals)
```



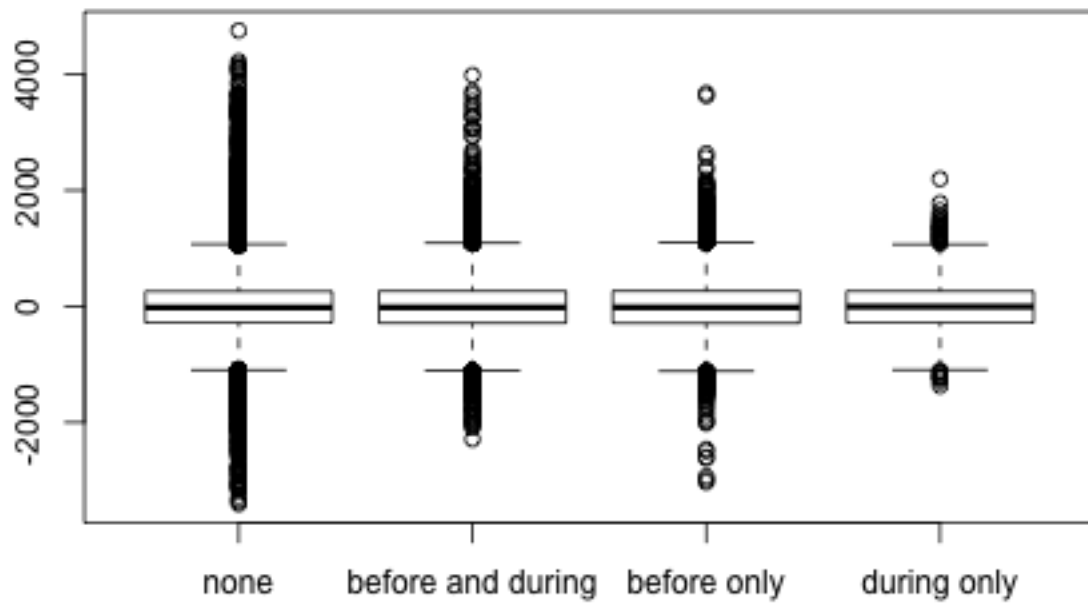
```
plot(births_excl$PLUR_truncated, model1$residuals)
```



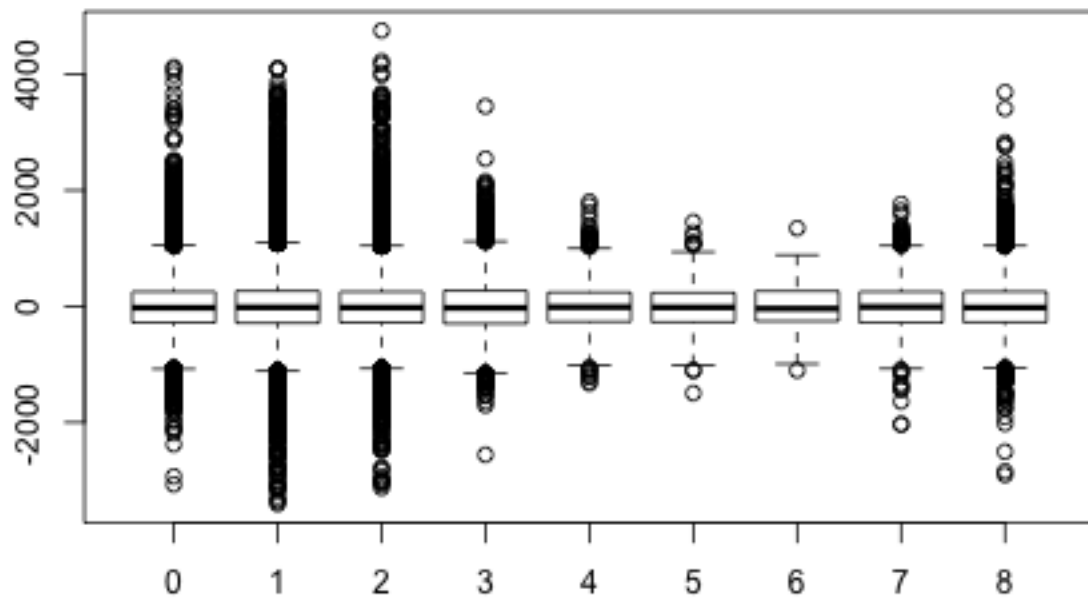
```
plot(births_excl$PARITY_truncated, model1$residuals)
```

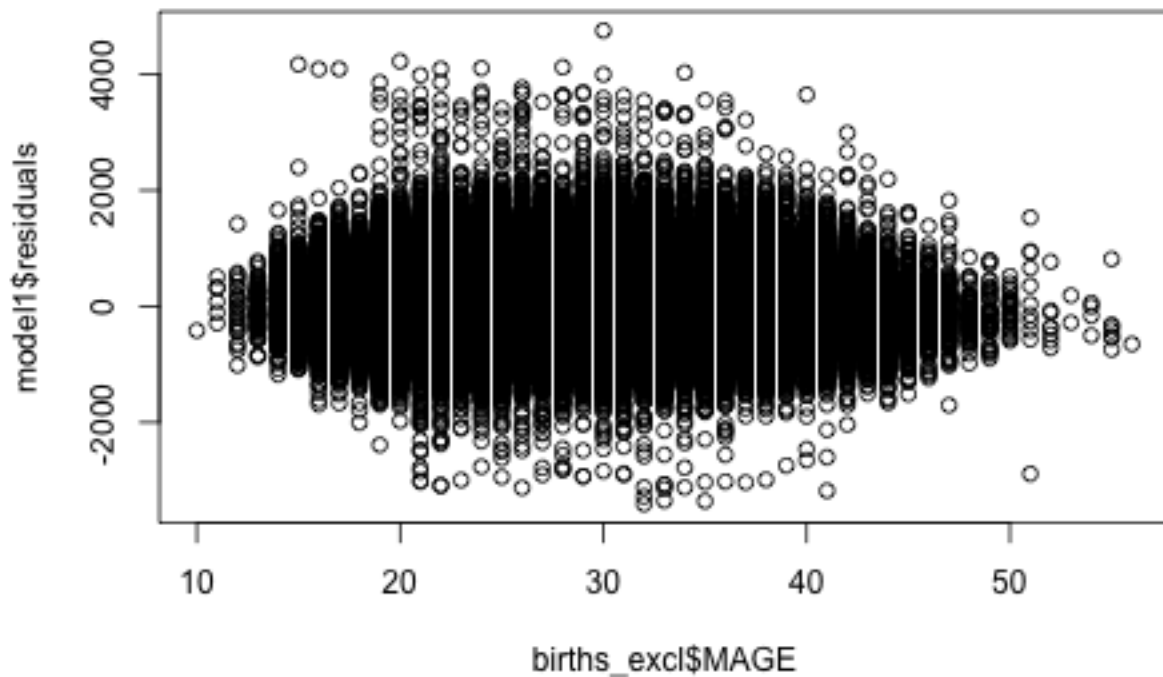
```
plot(births_excl$smoking_type, model1$residuals)
```



```
plot(births_excl$MRACER, model1$residuals)
```



```
plot(births_excl$MAGE, model1$residuals)
```



The residuals vs fitted values and residuals vs gestational period plot slope downwards, indicating that there is a departure from linearity. More precisely, the linear model underpredicts when gestational period is below ~30 and overpredicts when gestational period is above ~30. A transformation may be helpful. The model may improve if a square term is added. There is a particularly high residual (in terms of absolute value) around 80 weeks of gestation, which is likely an outlier that has no reason to be there, as no humans can possibly gestate for 80 weeks (~1.54 years).

The residual graph for Plurality (truncated) has decreasing residuals (in terms of absolute value) as plurality increases. This makes sense, as birth weight should get smaller (and as a result range of birth weights should get tighter, leading to smaller absolute value residuals) as more babies share a womb and share nutrients – More sharing will biologically cause them to come out smaller.

The residual graph for Parity (truncated) has pretty random residuals that are all around the same size for each group.

The residual graph for Smoking has higher residuals for no smoking than for smoking of any kind. This makes sense, as birth weight could biologically get smaller in the presence of smoking, as smoking can be damaging to the fetus and be detrimental to its growth and weight. This would lead to the range of birth weights of smoking mothers getting tighter, leading to smaller absolute value residuals.

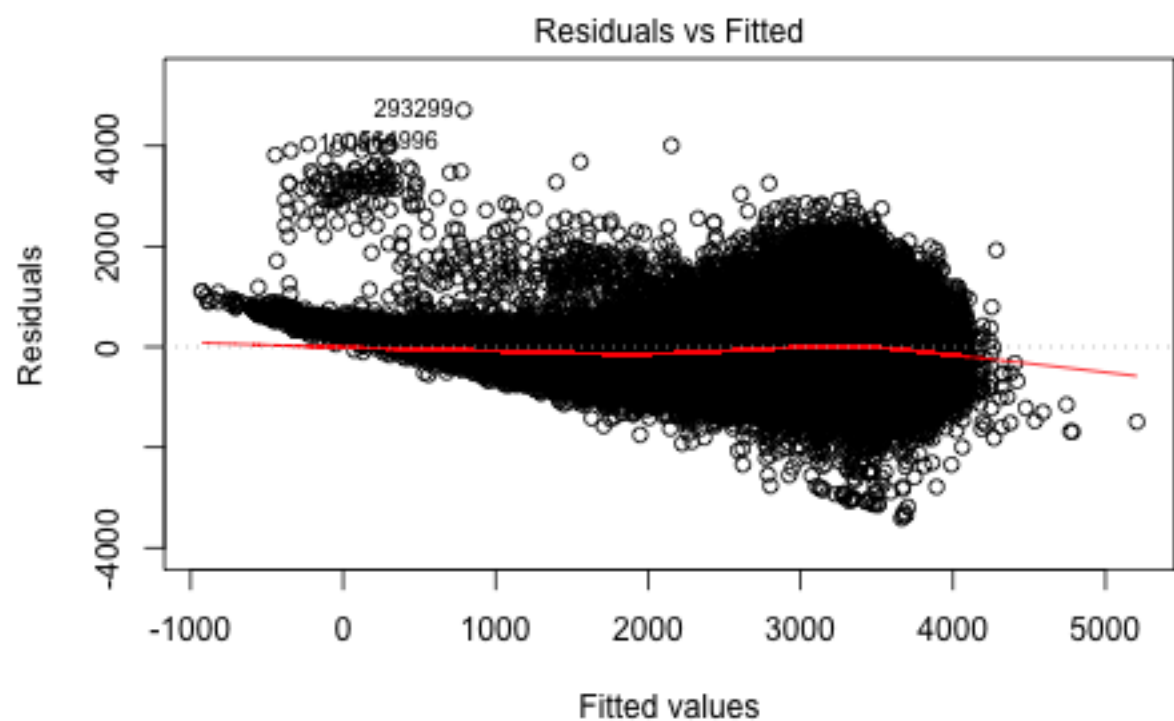
The residual graph for Mother's race indicates that residuals are lower for for races 3, 4, 5, 6, and 7 and higher for the other races. This could be something to explore.

The residual graph for Mother's age is fairly random, with residuals getting a bit smaller near the beginning and end (<20 years old and >45 years old).

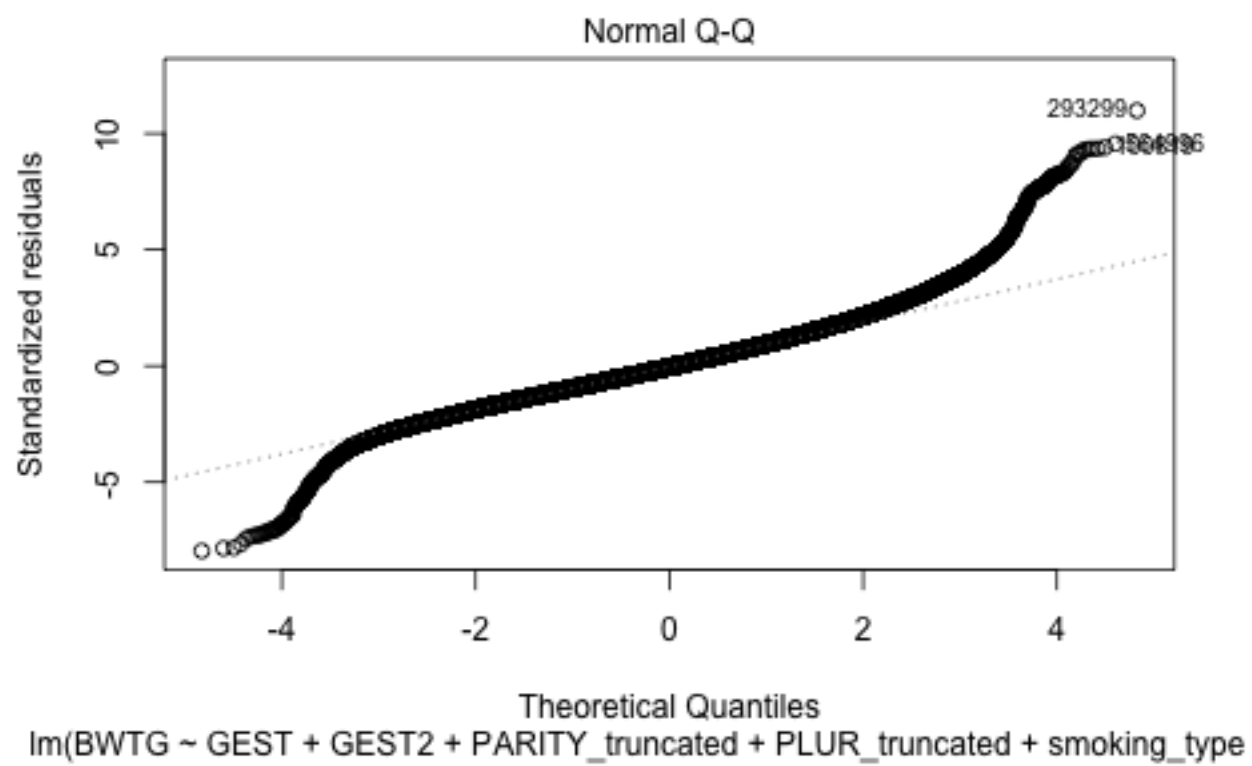
```
model2 = lm(data = births_excl, BWG ~ GEST + GEST2 + PARITY_truncated + PLUR_truncated + smoking_type +
summary(model2)
```

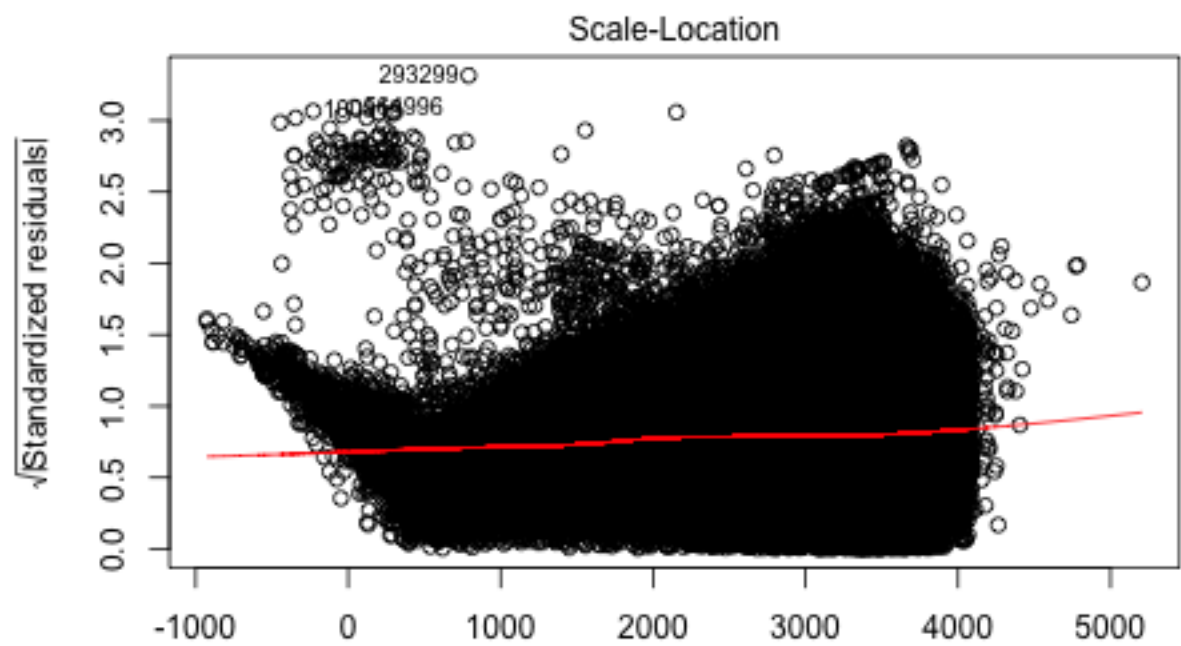
```
##
```

```
## Call:
## lm(formula = BWTG ~ GEST + GEST2 + PARITY_truncated + PLUR_truncated +
##      smoking_type + MAGE + MRACER + mortality, data = births_excl,
##      na.action = "na.exclude")
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3412.1  -282.9   -19.5   260.8  4709.9
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    -2.938e+03  4.046e+01  -72.608 < 2e-16 ***
## GEST           1.307e+02  2.327e+00   56.181 < 2e-16 ***
## GEST2          6.427e-01  3.346e-02   19.208 < 2e-16 ***
## PARITY_truncated2  9.593e+01  1.317e+00   72.817 < 2e-16 ***
## PARITY_truncated3  1.149e+02  1.540e+00   74.659 < 2e-16 ***
## PARITY_truncated4  1.190e+02  1.928e+00   61.738 < 2e-16 ***
## PARITY_truncated5+ 1.198e+02  1.956e+00   61.256 < 2e-16 ***
## PLUR_truncated2   -3.558e+02  2.943e+00 -120.901 < 2e-16 ***
## PLUR_truncated3+  -4.566e+02  1.539e+01  -29.658 < 2e-16 ***
## smoking_typebefore and during -2.041e+02  1.770e+00 -115.320 < 2e-16 ***
## smoking_typebefore only    -1.152e+01  2.702e+00   -4.264 2.00e-05 ***
## smoking_typeduring only    -1.651e+02  9.127e+00  -18.087 < 2e-16 ***
## MAGE             4.611e+00  9.638e-02   47.841 < 2e-16 ***
## MRACER1           8.373e+01  1.659e+00   50.463 < 2e-16 ***
## MRACER2          -9.902e+01  1.820e+00  -54.402 < 2e-16 ***
## MRACER3          -5.140e+00  4.575e+00   -1.124    0.261
## MRACER4          -3.340e+01  7.600e+00   -4.395 1.11e-05 ***
## MRACER5          -1.135e+02  1.794e+01   -6.329 2.47e-10 ***
## MRACER6           2.394e+01  4.402e+01    0.544    0.586
## MRACER7          -1.327e+01  9.456e+00   -1.403    0.161
## MRACER8          -1.020e+02  3.207e+00  -31.797 < 2e-16 ***
## mortality        2.390e+01  3.101e+00    7.707 1.29e-14 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 428.8 on 717847 degrees of freedom
## Multiple R-squared:  0.5187, Adjusted R-squared:  0.5186
## F-statistic: 3.683e+04 on 21 and 717847 DF,  p-value: < 2.2e-16
plot(model2)
```

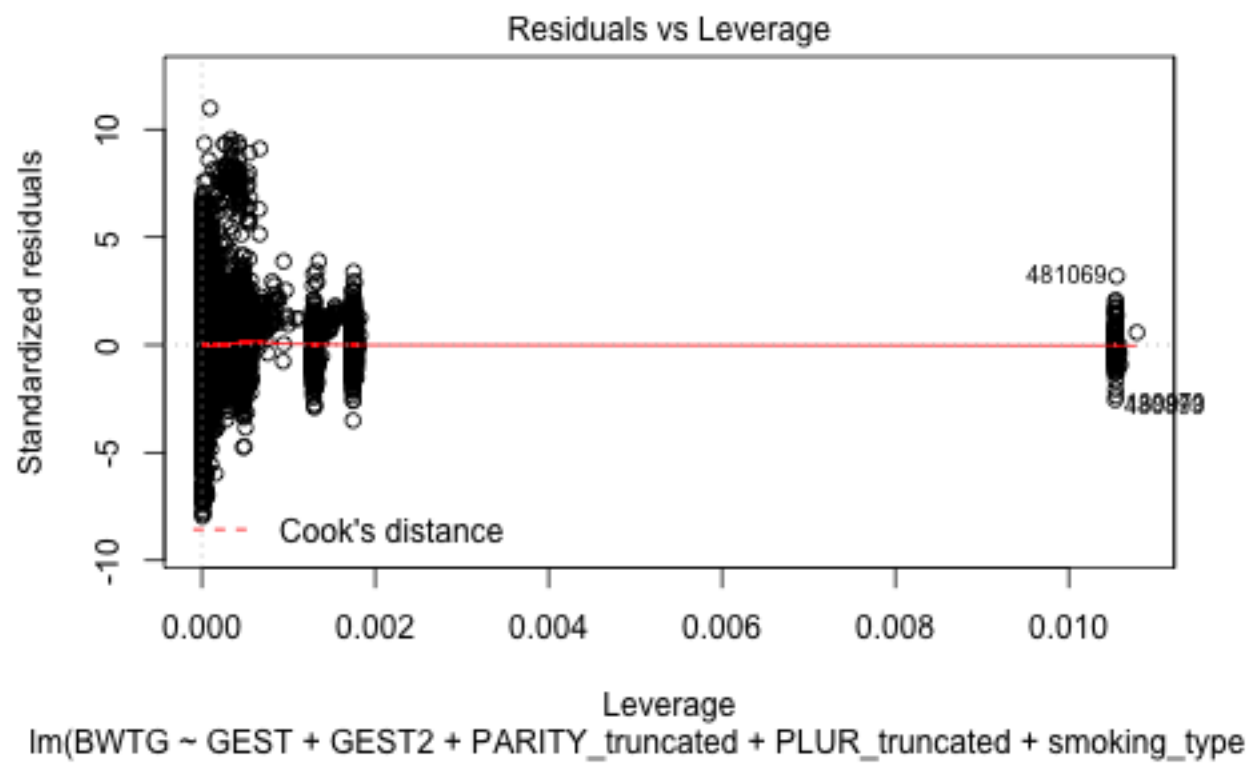


$\text{lm}(\text{BWTG} \sim \text{GEST} + \text{GEST2} + \text{PARITY_truncated} + \text{PLUR_truncated} + \text{smoking_type})$

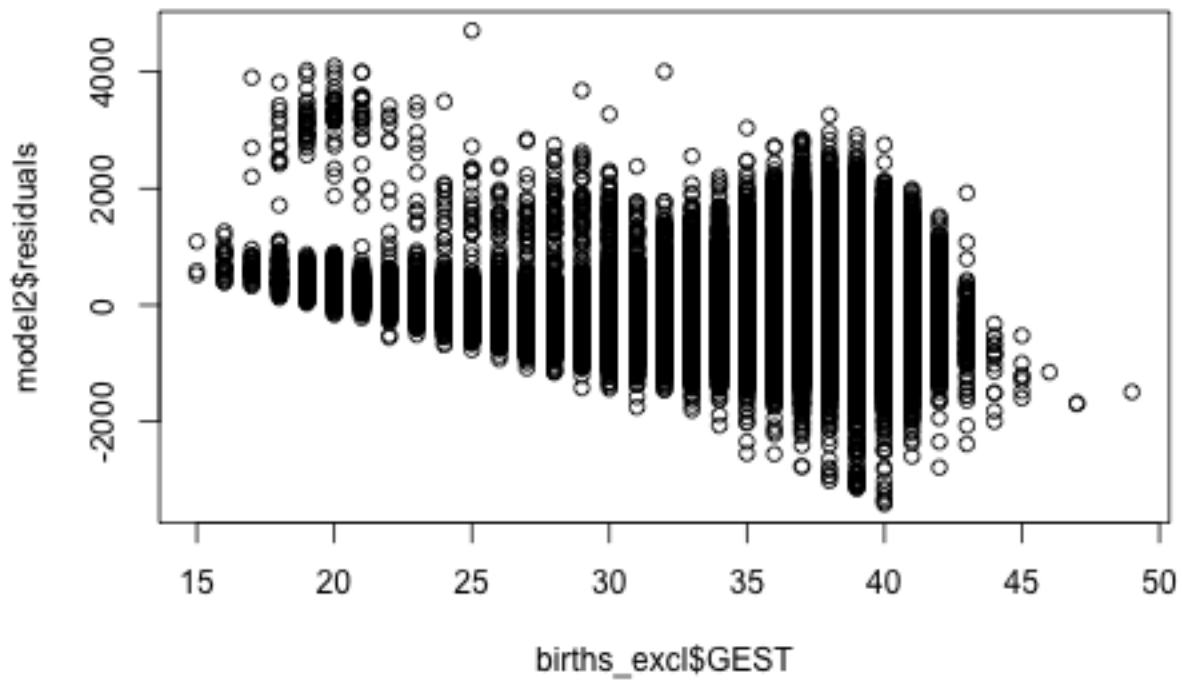




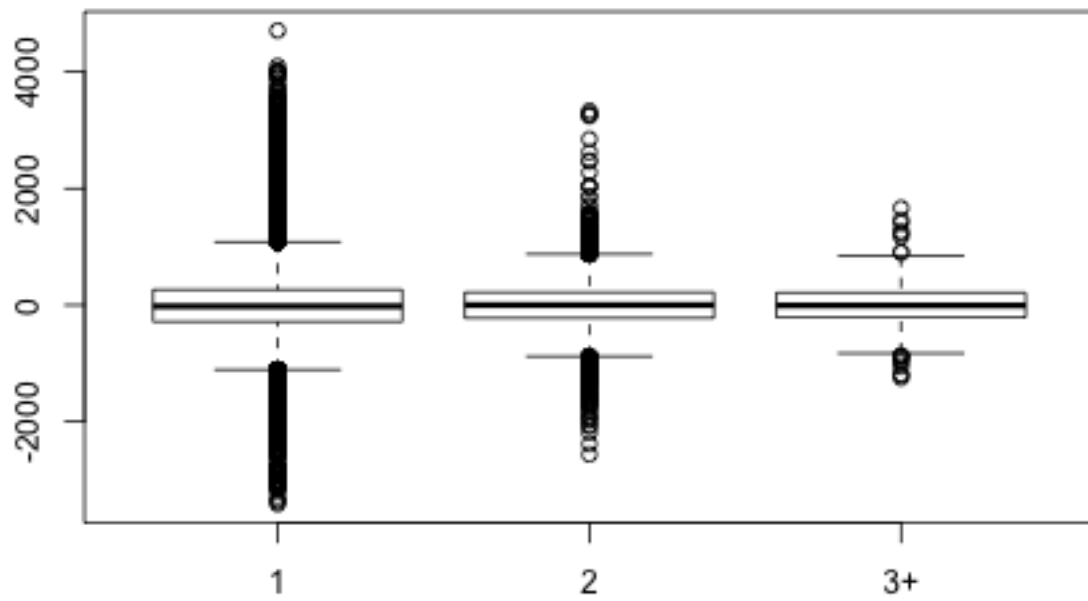
Fitted values
 $\text{lm}(\text{BWTG} \sim \text{GEST} + \text{GEST2} + \text{PARITY_truncated} + \text{PLUR_truncated} + \text{smoking_type})$



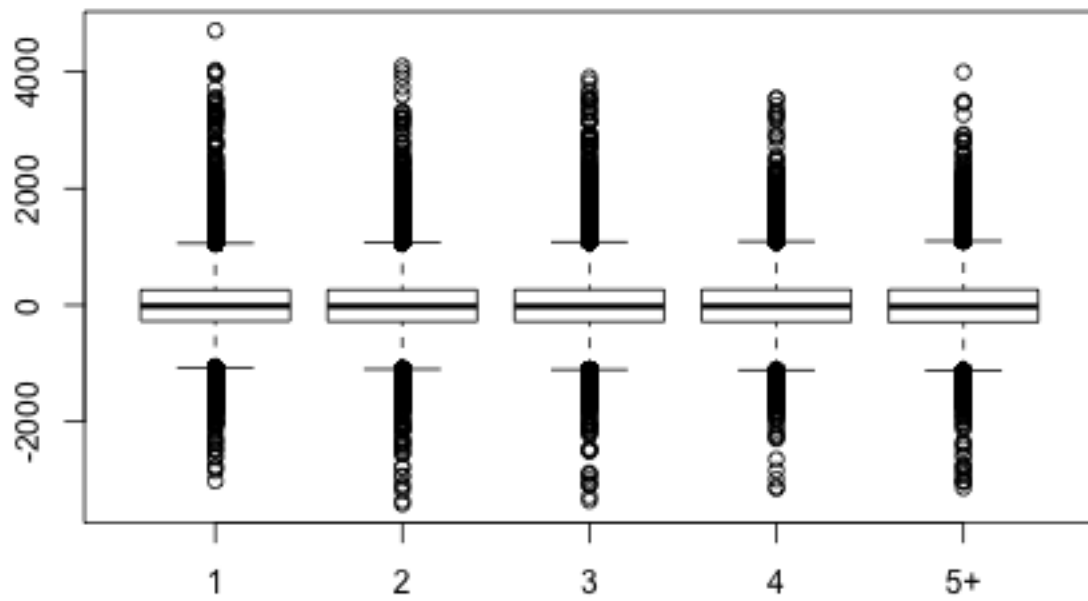
```
# plot(model2$fitted.values, model2$residuals)  
plot(births_excl$GEST, model2$residuals)
```



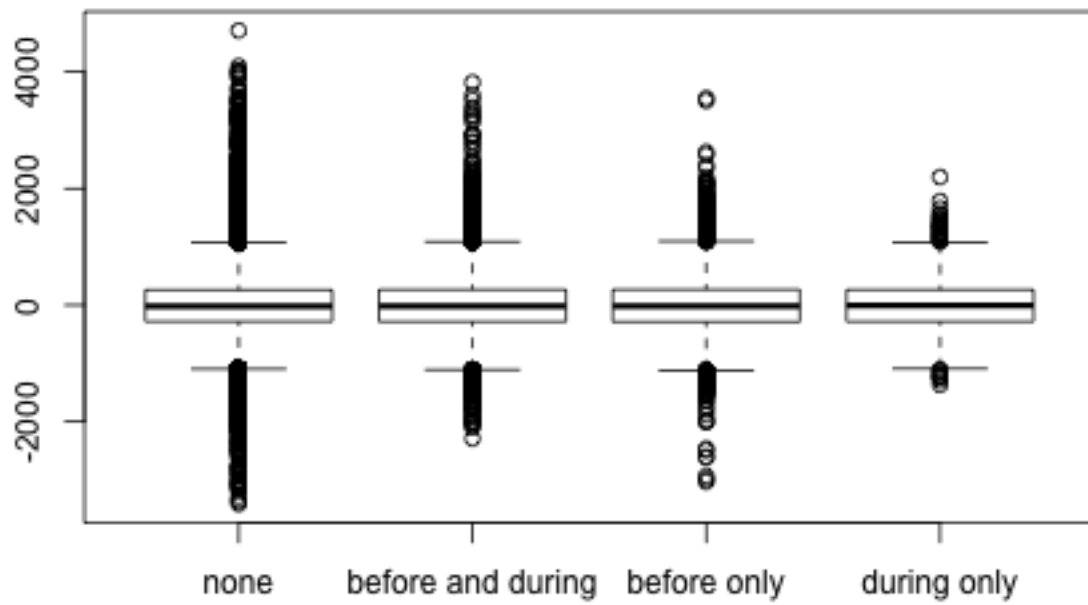
```
plot(births_excl$PLUR_truncated, model2$residuals)
```



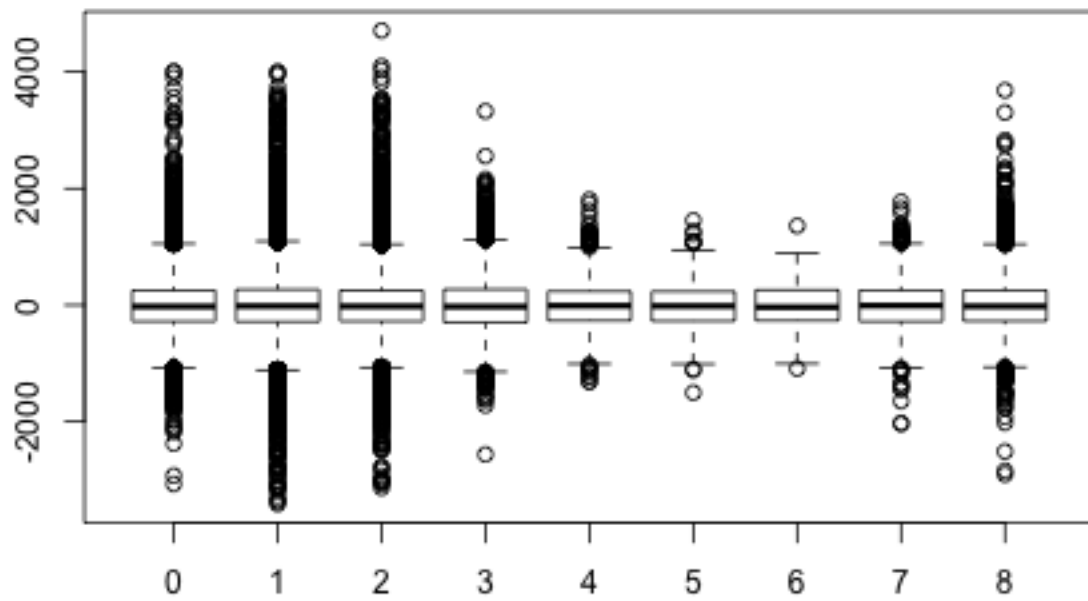
```
plot(births_excl$PARITY_truncated, model2$residuals)
```



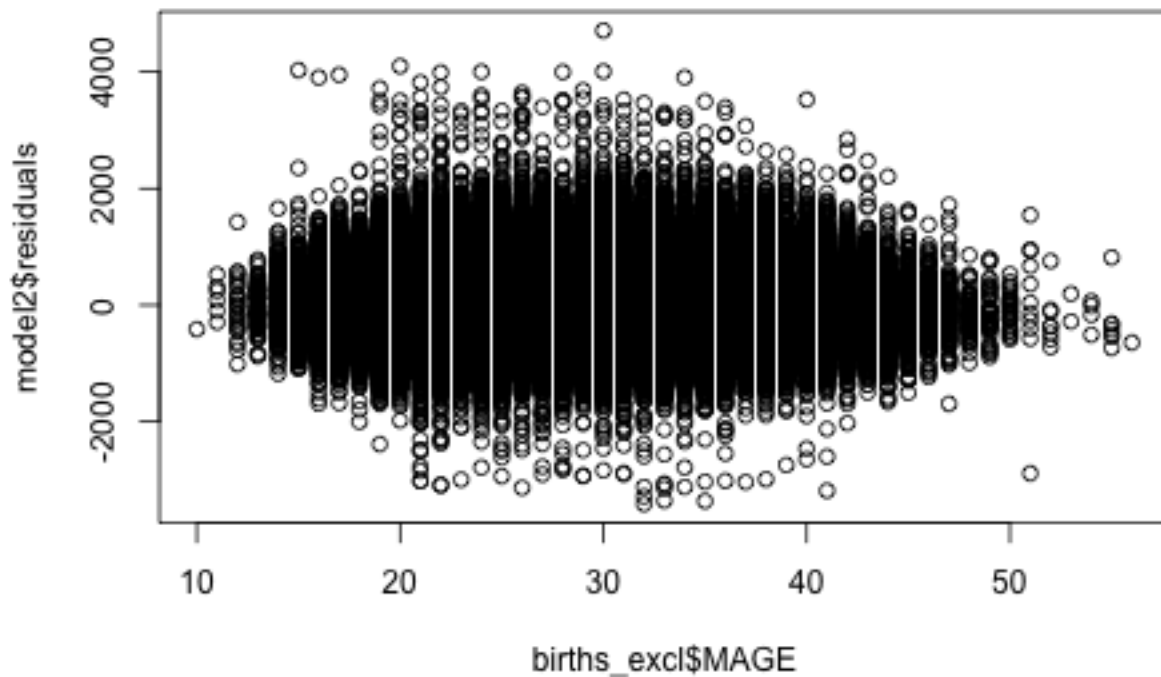
```
plot(births_excl$smoking_type, model2$residuals)
```



```
plot(births_excl$MRACER, model2$residuals)
```



```
plot(births_excl$MAGE, model2$residuals)
```



The new model still displays the original downwards trend in the residual vs gestational period graph. Perhaps another transformation on GEST would be helpful – a cubic term can be added. The other residuals plots also retain their trends from model 1.

```
model3 = lm(data = births_excl, BWG ~ GEST + GEST2 + GEST3 + PARITY_truncated + PLUR_truncated + smoking_type + MAGE + MRACER + mortality, data = births_excl, na.action = "na.exclude")
summary(model3)
```

```
##
## Call:
## lm(formula = BWG ~ GEST + GEST2 + GEST3 + PARITY_truncated +
##     PLUR_truncated + smoking_type + MAGE + MRACER + mortality,
##     data = births_excl, na.action = "na.exclude")
##
## Residuals:
```

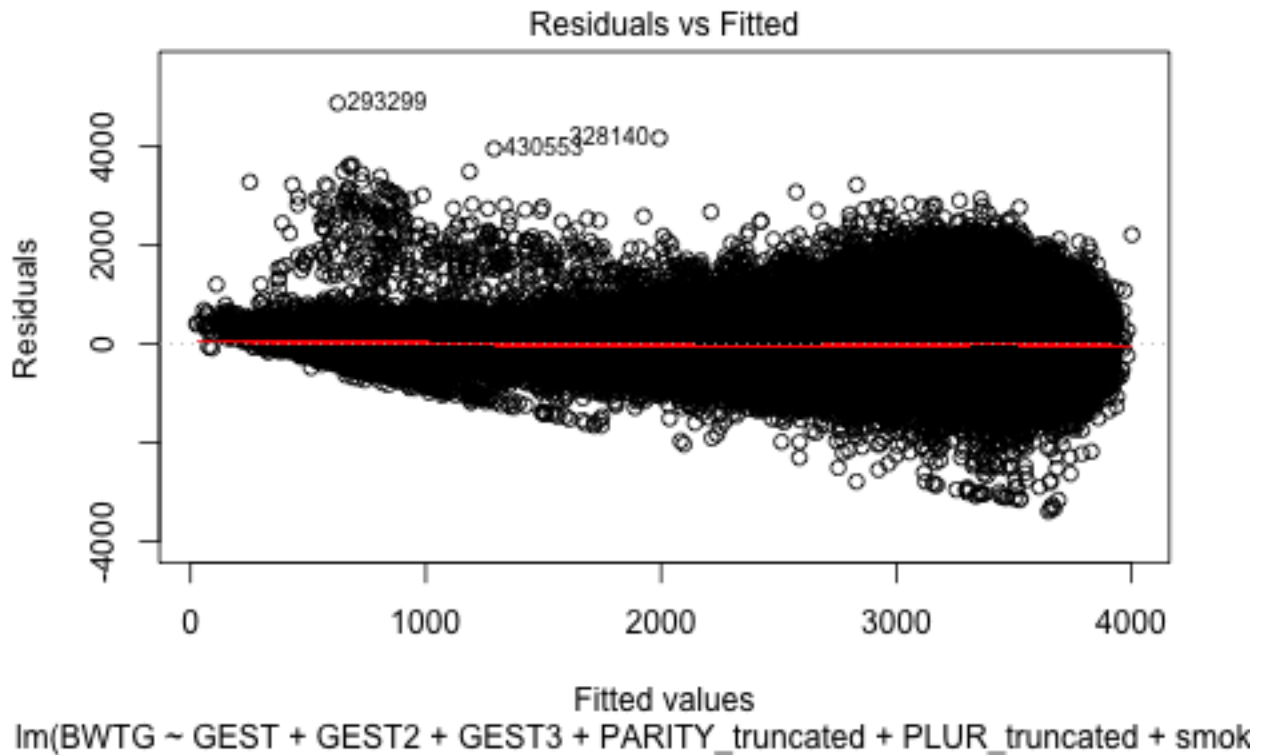
	Min	1Q	Median	3Q	Max
	-3396.9	-280.5	-18.7	258.0	4875.2

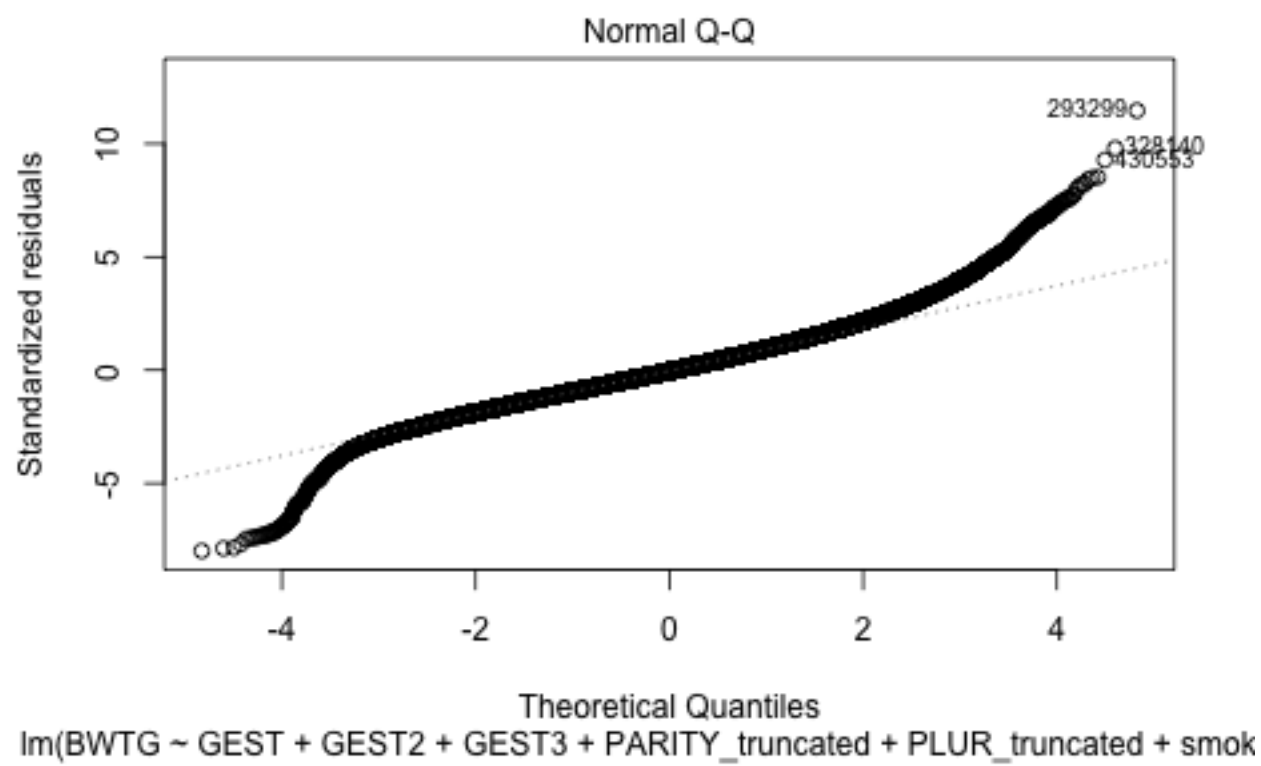
```
##
## Coefficients:
```

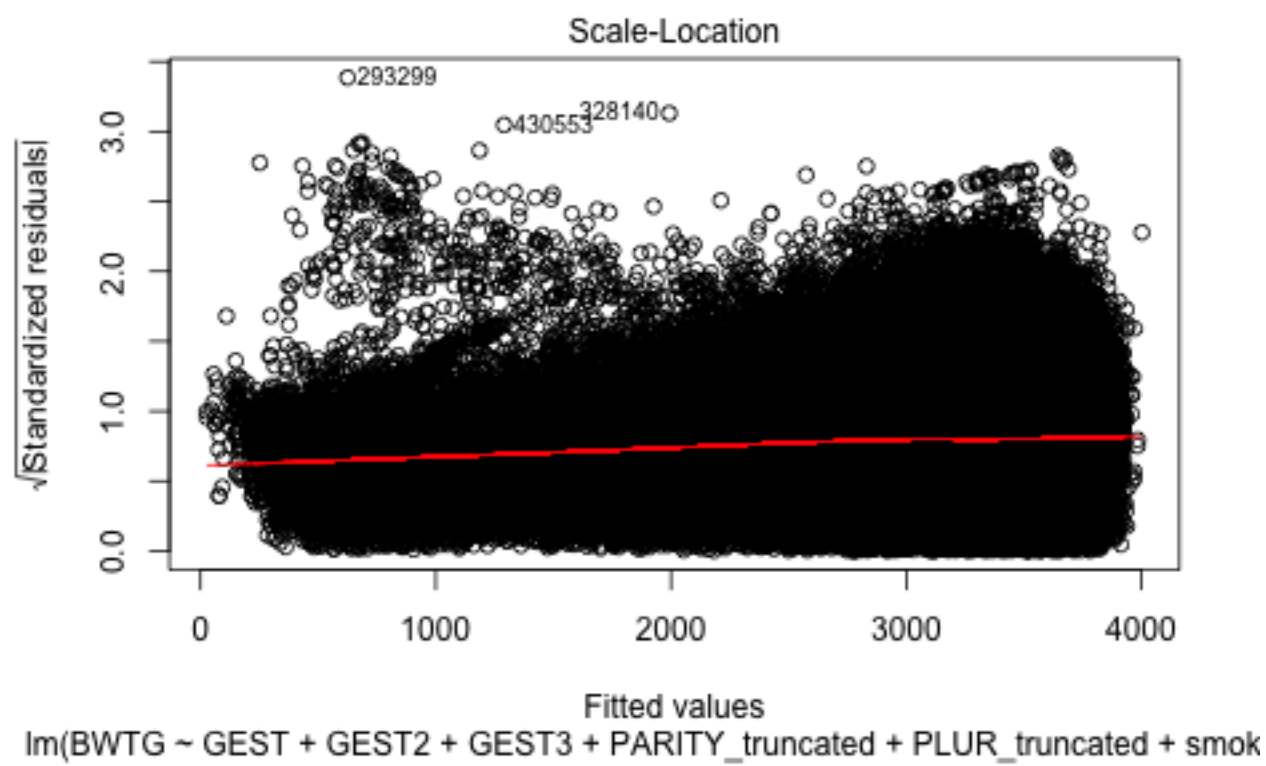
	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	1.701e+04	1.866e+02	91.157	< 2e-16 ***
GEST	-1.785e+03	1.765e+01	-101.116	< 2e-16 ***
GEST2	6.013e+01	5.445e-01	110.439	< 2e-16 ***
GEST3	-6.018e-01	5.498e-03	-109.462	< 2e-16 ***
PARITY_truncated2	8.815e+01	1.308e+00	67.366	< 2e-16 ***
PARITY_truncated3	1.055e+02	1.529e+00	68.985	< 2e-16 ***
PARITY_truncated4	1.100e+02	1.914e+00	57.459	< 2e-16 ***
PARITY_truncated5+	1.118e+02	1.941e+00	57.630	< 2e-16 ***

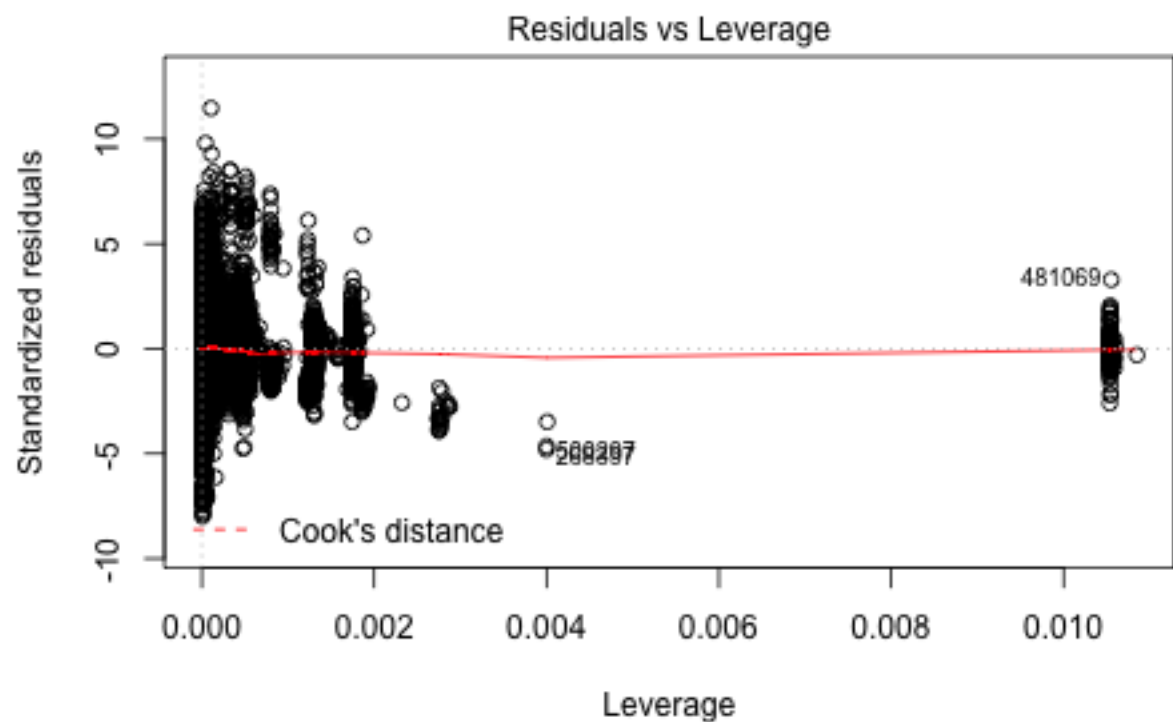
```
## PLUR_truncated2          -3.303e+02  2.928e+00 -112.810 < 2e-16 ***
## PLUR_truncated3+        -3.485e+02  1.530e+01 -22.780 < 2e-16 ***
## smoking_typebefore and during -2.033e+02  1.755e+00 -115.846 < 2e-16 ***
## smoking_typebefore only    -1.130e+01  2.680e+00  -4.218 2.46e-05 ***
## smoking_typeduring only    -1.651e+02  9.052e+00 -18.240 < 2e-16 ***
## MAGE                      4.592e+00  9.559e-02  48.040 < 2e-16 ***
## MRACER1                   8.254e+01  1.646e+00  50.158 < 2e-16 ***
## MRACER2                   -9.966e+01  1.805e+00 -55.206 < 2e-16 ***
## MRACER3                   -2.102e+00  4.537e+00  -0.463  0.6431
## MRACER4                   -3.828e+01  7.537e+00  -5.079 3.80e-07 ***
## MRACER5                   -1.184e+02  1.779e+01  -6.658 2.78e-11 ***
## MRACER6                    2.413e+01  4.365e+01   0.553  0.5805
## MRACER7                   -1.951e+01  9.378e+00  -2.080  0.0375 *
## MRACER8                   -1.070e+02  3.181e+00 -33.621 < 2e-16 ***
## mortality                  1.952e+01  3.076e+00   6.345 2.22e-10 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 425.2 on 717846 degrees of freedom
## Multiple R-squared:  0.5266, Adjusted R-squared:  0.5265
## F-statistic: 3.629e+04 on 22 and 717846 DF,  p-value: < 2.2e-16
```

```
plot(model3)
```



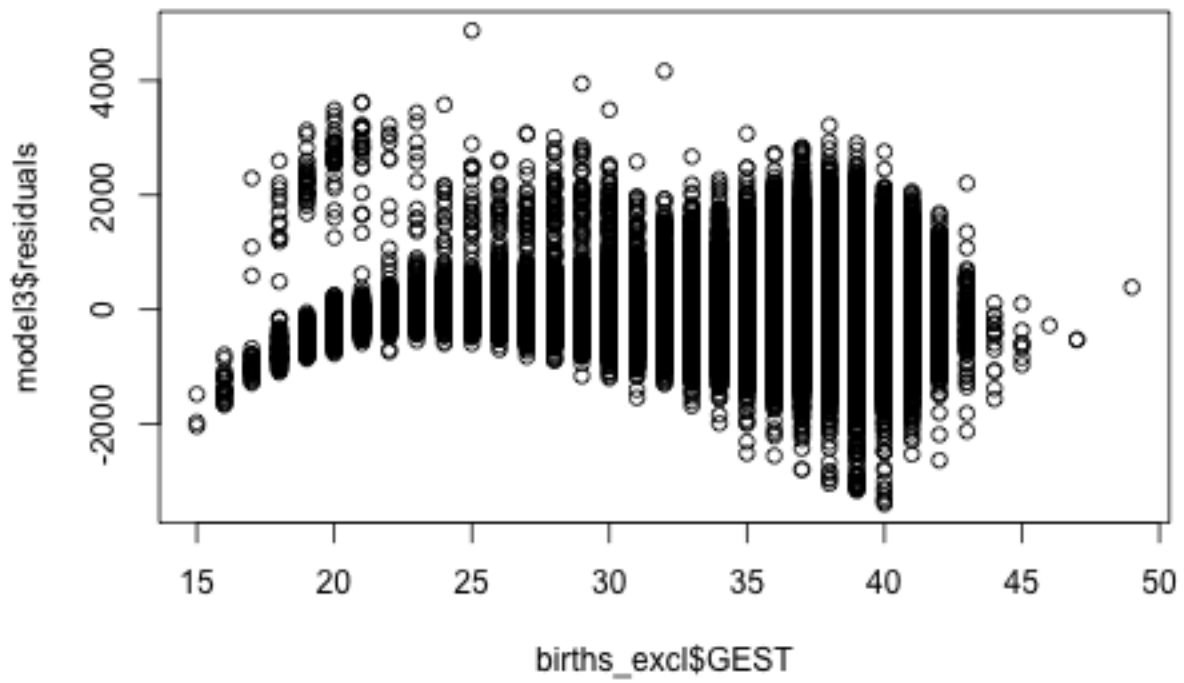




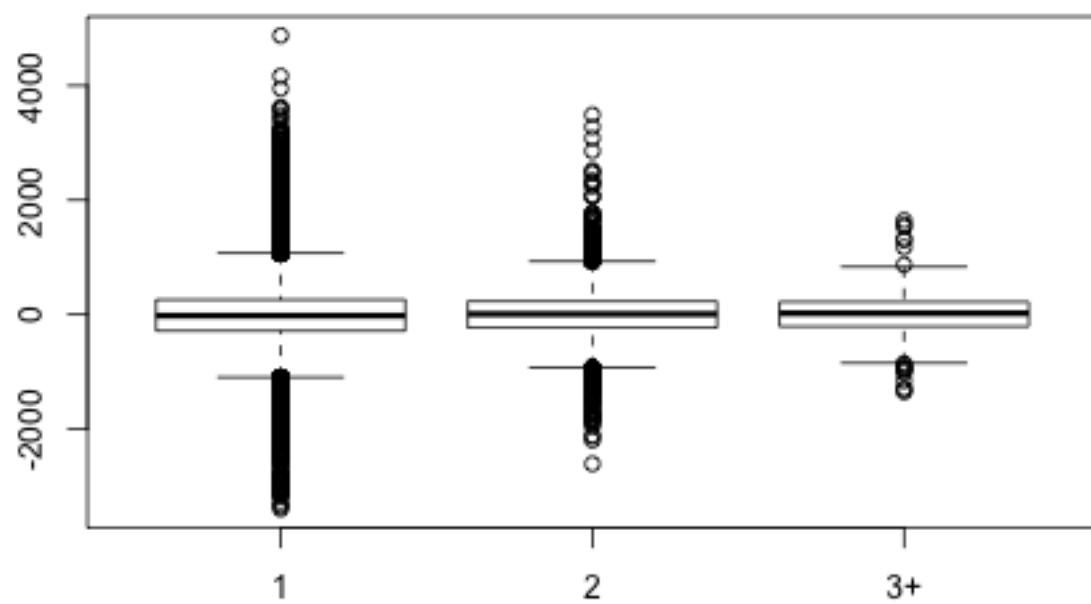


lm(BWTG ~ GEST + GEST2 + GEST3 + PARITY_truncated + PLUR_truncated + smok

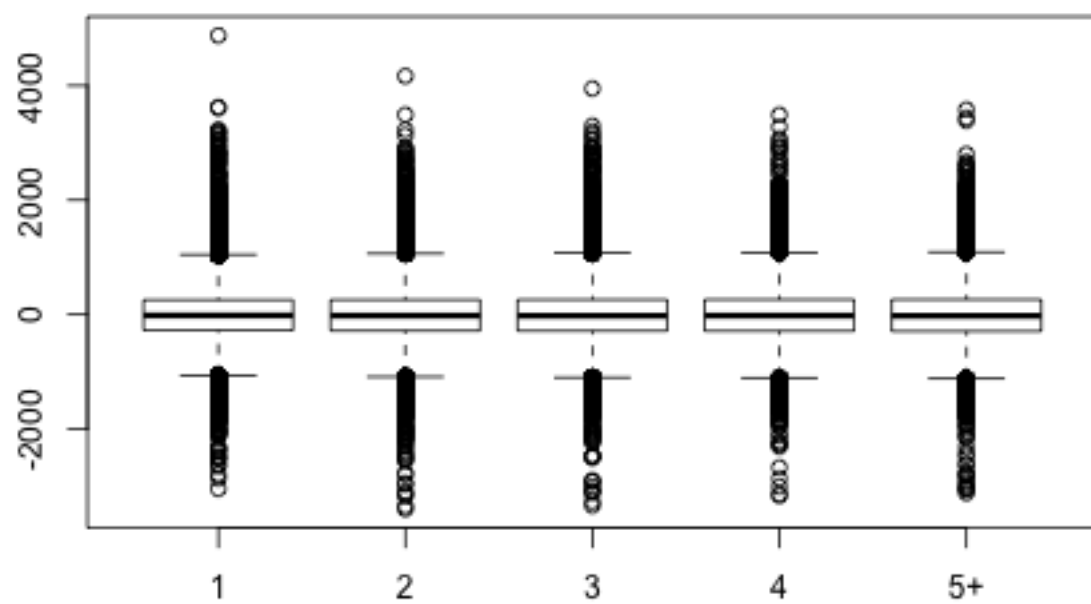
```
# plot(model3$fitted.values, model3$residuals)
plot(births_excl$GEST, model3$residuals)
```



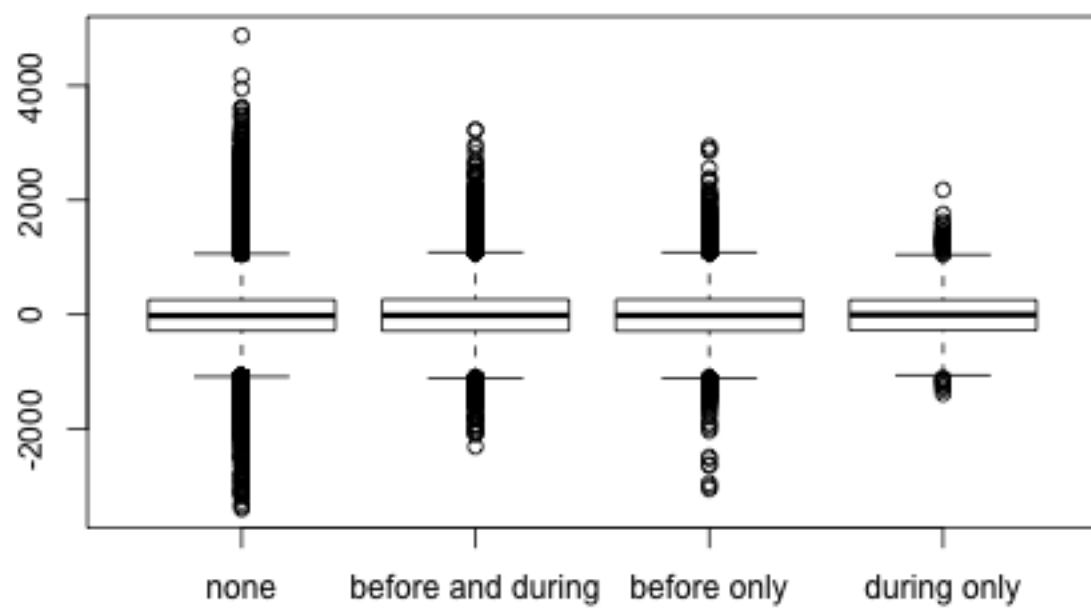
```
plot(births_excl$PLUR_truncated, model3$residuals)
```



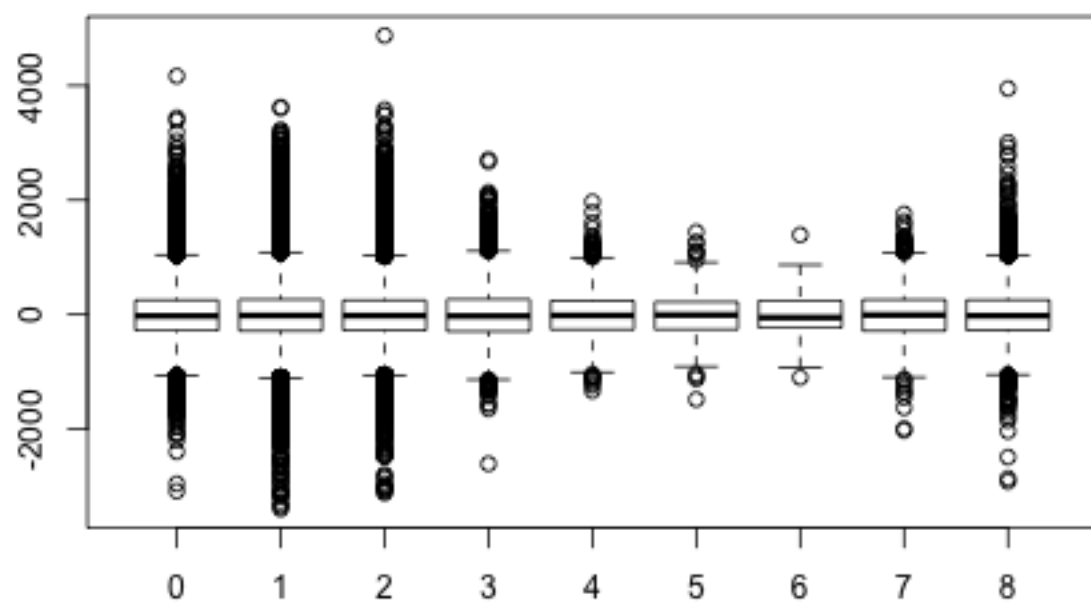
```
plot(births_excl$PARITY_truncated, model3$residuals)
```



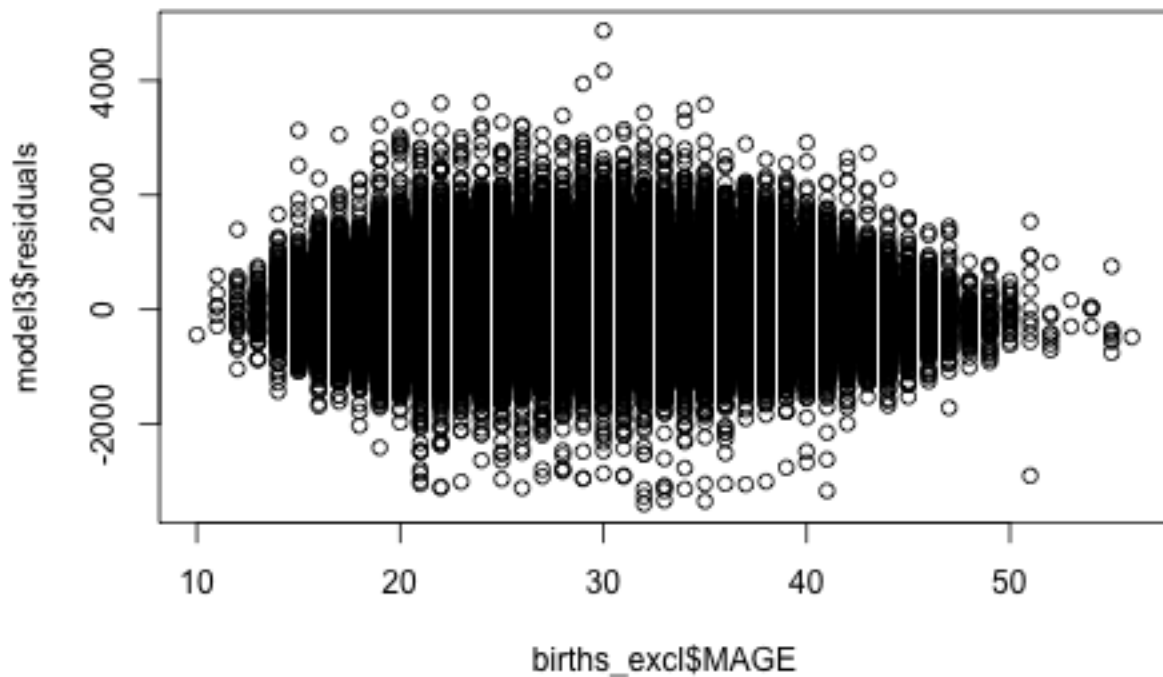
```
plot(births_excl$smoking_type, model3$residuals)
```



```
plot(births_excl$MRACER, model3$residuals)
```



```
plot(births_excl$MAGE, model3$residuals)
```

The residual vs gestational period shows a much more random pattern than before. It is worth investigating if adding a quartic term would help. The other residuals plots also retain their trends from model 1.

```
model4 = lm(data = births_excl, BWTG ~ GEST + GEST2 + GEST3 + GEST4 + PARITY_truncated + PLUR_truncated
summary(model4)
```

```
##
## Call:
## lm(formula = BWTG ~ GEST + GEST2 + GEST3 + GEST4 + PARITY_truncated +
##       PLUR_truncated + smoking_type + MAGE + MRACER + mortality,
##     data = births_excl, na.action = "na.exclude")
##
## Residuals:
```

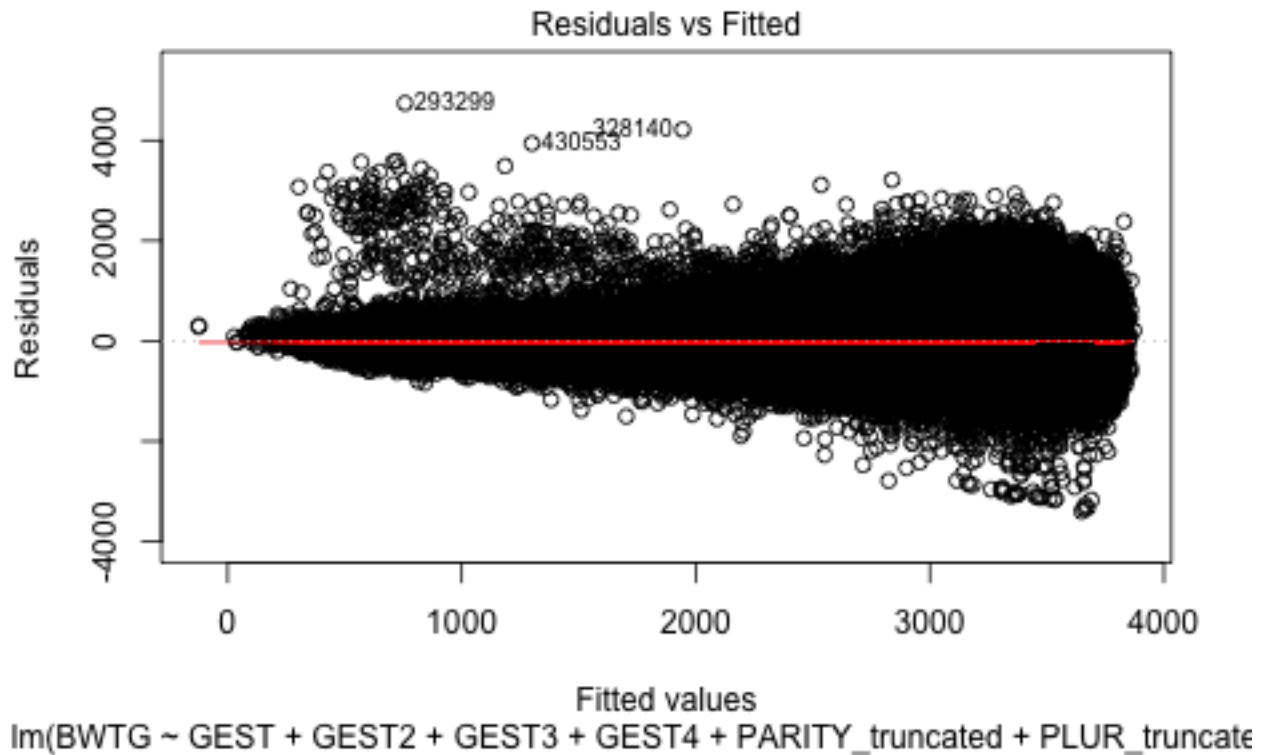
	Min	1Q	Median	3Q	Max
	-3398.1	-280.3	-19.4	257.3	4742.4

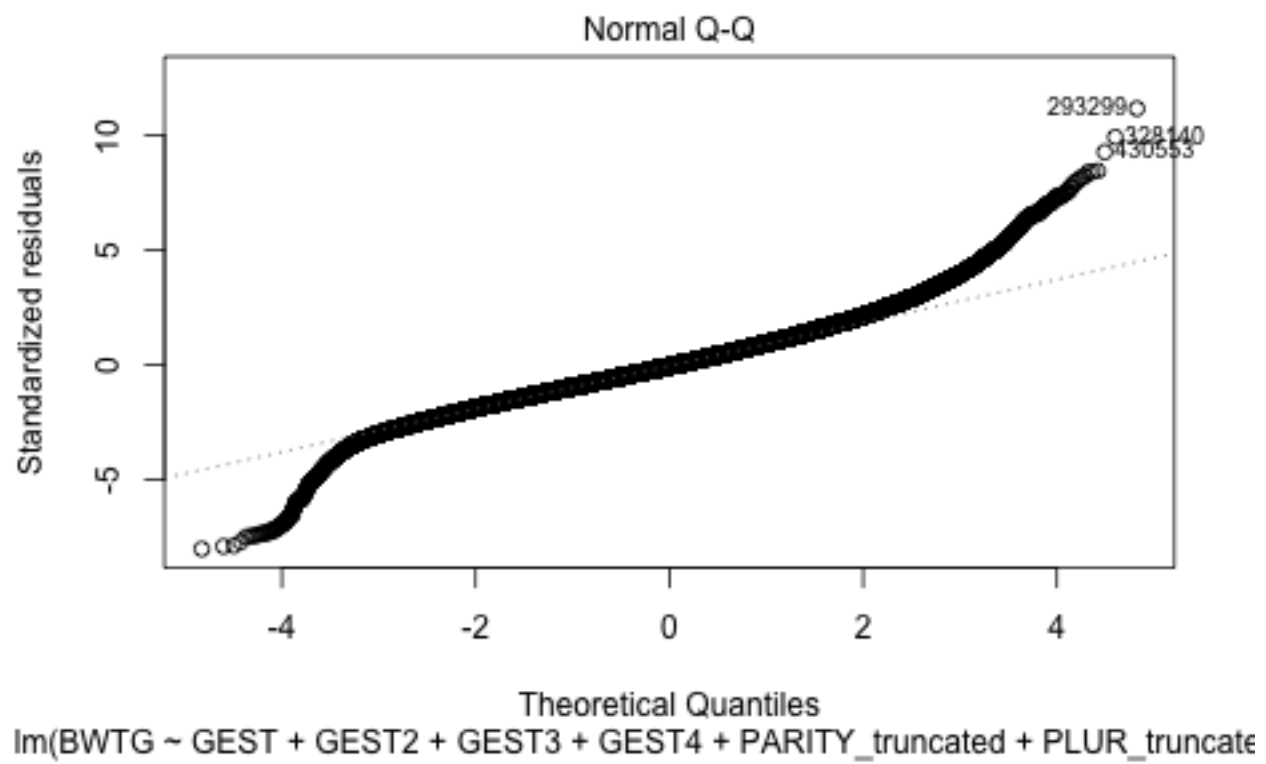
```
##
## Coefficients:
```

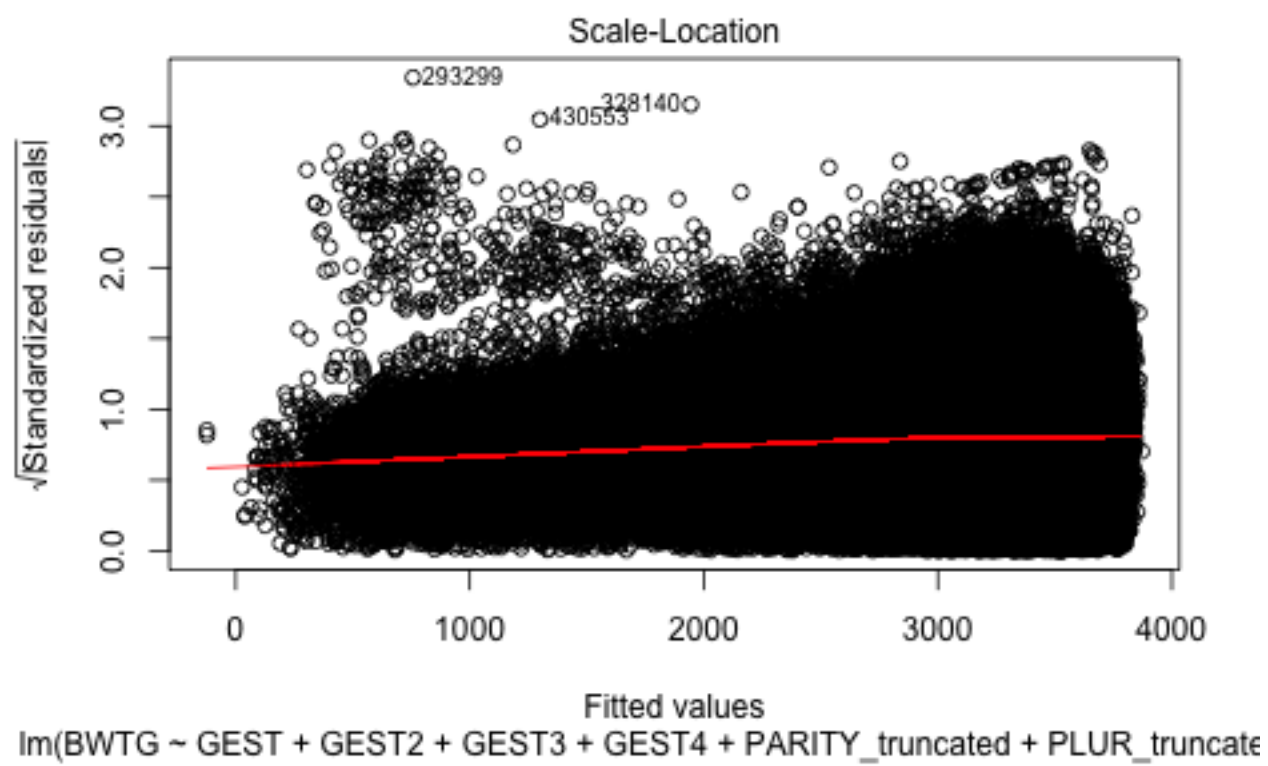
	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	-1.601e+04	7.646e+02	-20.934	< 2e-16 ***
GEST	2.640e+03	1.009e+02	26.157	< 2e-16 ***
GEST2	-1.565e+02	4.896e+00	-31.968	< 2e-16 ***
GEST3	4.009e+00	1.037e-01	38.660	< 2e-16 ***
GEST4	-3.610e-02	8.109e-04	-44.525	< 2e-16 ***
PARITY_truncated2	8.561e+01	1.308e+00	65.458	< 2e-16 ***
PARITY_truncated3	1.028e+02	1.528e+00	67.270	< 2e-16 ***
PARITY_truncated4	1.076e+02	1.912e+00	56.277	< 2e-16 ***
PARITY_truncated5+	1.104e+02	1.938e+00	56.945	< 2e-16 ***

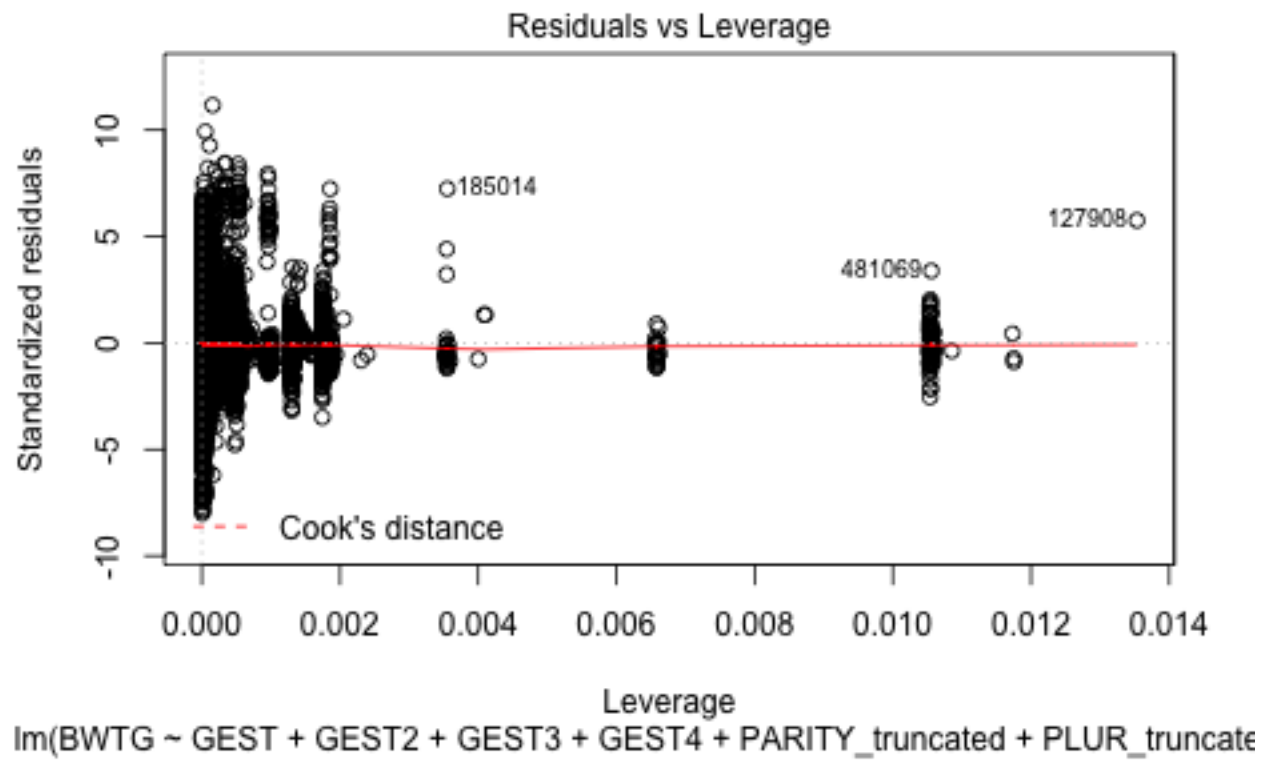
```
## PLUR_truncated2      -3.153e+02  2.943e+00 -107.137 < 2e-16 ***
## PLUR_truncated3+    -3.296e+02  1.528e+01  -21.565 < 2e-16 ***
## smoking_typebefore and during -2.024e+02  1.753e+00 -115.467 < 2e-16 ***
## smoking_typebefore only    -1.113e+01  2.676e+00  -4.161 3.17e-05 ***
## smoking_typeduring only    -1.647e+02  9.039e+00  -18.225 < 2e-16 ***
## MAGE                  4.592e+00  9.546e-02   48.105 < 2e-16 ***
## MRACER1              8.213e+01  1.643e+00   49.981 < 2e-16 ***
## MRACER2             -9.986e+01  1.803e+00  -55.396 < 2e-16 ***
## MRACER3             -1.772e+00  4.531e+00   -0.391  0.6958
## MRACER4             -4.031e+01  7.527e+00   -5.355 8.56e-08 ***
## MRACER5             -1.203e+02  1.776e+01   -6.775 1.25e-11 ***
## MRACER6              2.233e+01  4.359e+01    0.512  0.6086
## MRACER7             -2.029e+01  9.365e+00   -2.167  0.0302 *
## MRACER8            -1.081e+02  3.177e+00  -34.041 < 2e-16 ***
## mortality            1.814e+01  3.072e+00    5.905 3.53e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 424.6 on 717845 degrees of freedom
## Multiple R-squared:  0.5279, Adjusted R-squared:  0.5278
## F-statistic: 3.489e+04 on 23 and 717845 DF,  p-value: < 2.2e-16
```

```
plot(model4)
```

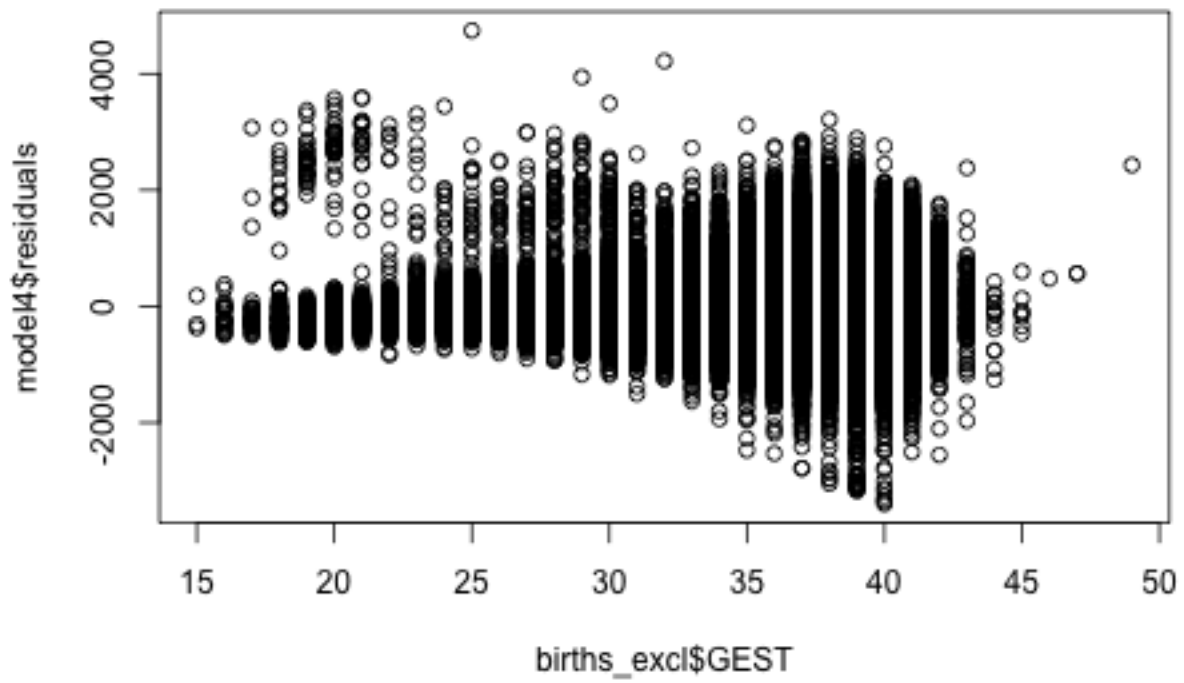




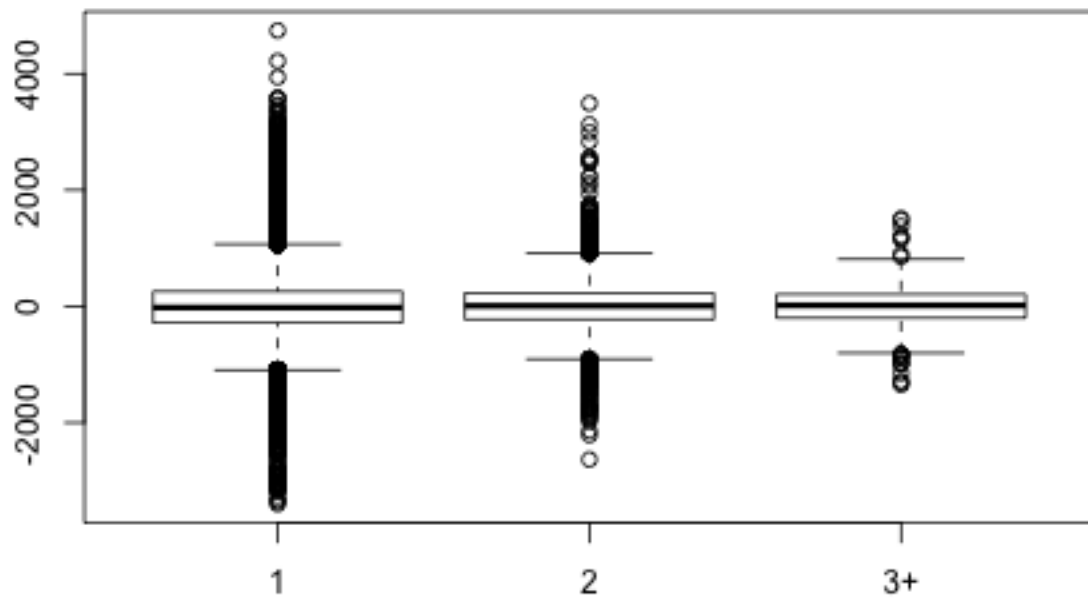




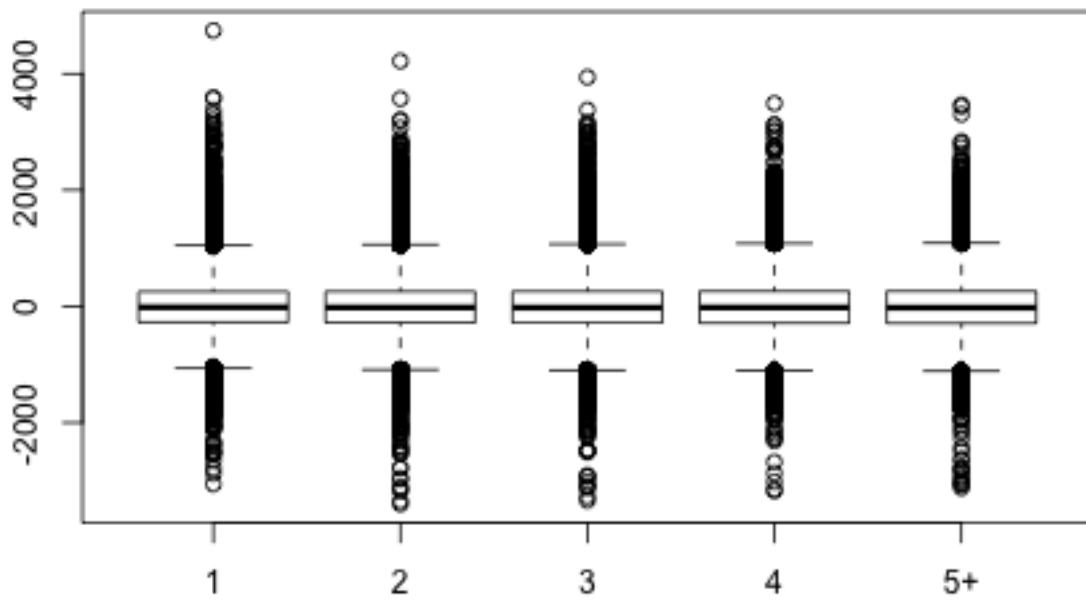
```
# plot(model4$fitted.values, model4$residuals)
plot(births_excl$GEST, model4$residuals)
```



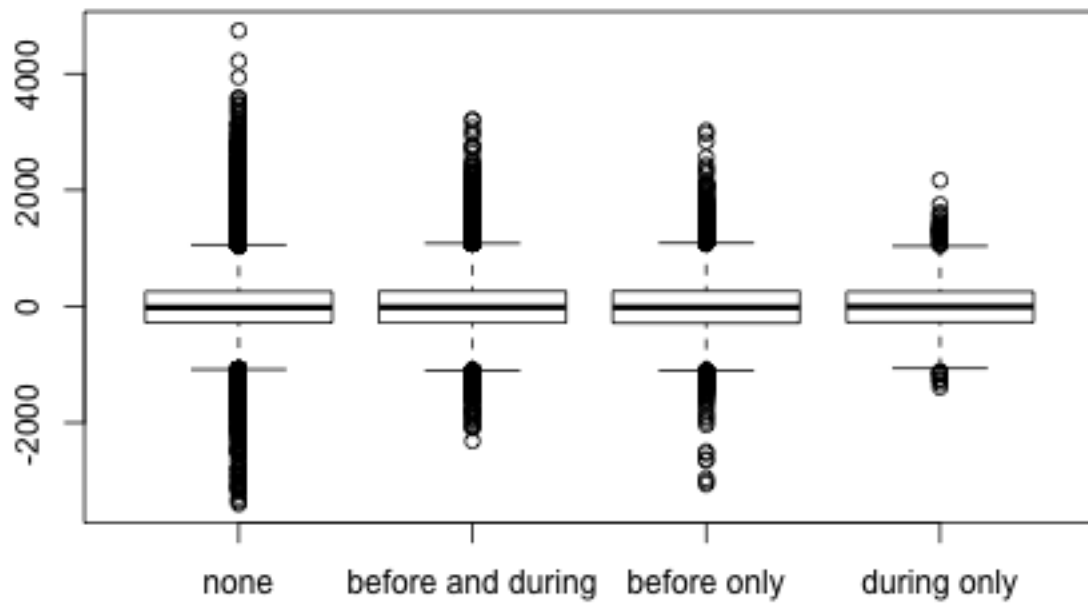
```
plot(births_excl$PLUR_truncated, model4$residuals)
```



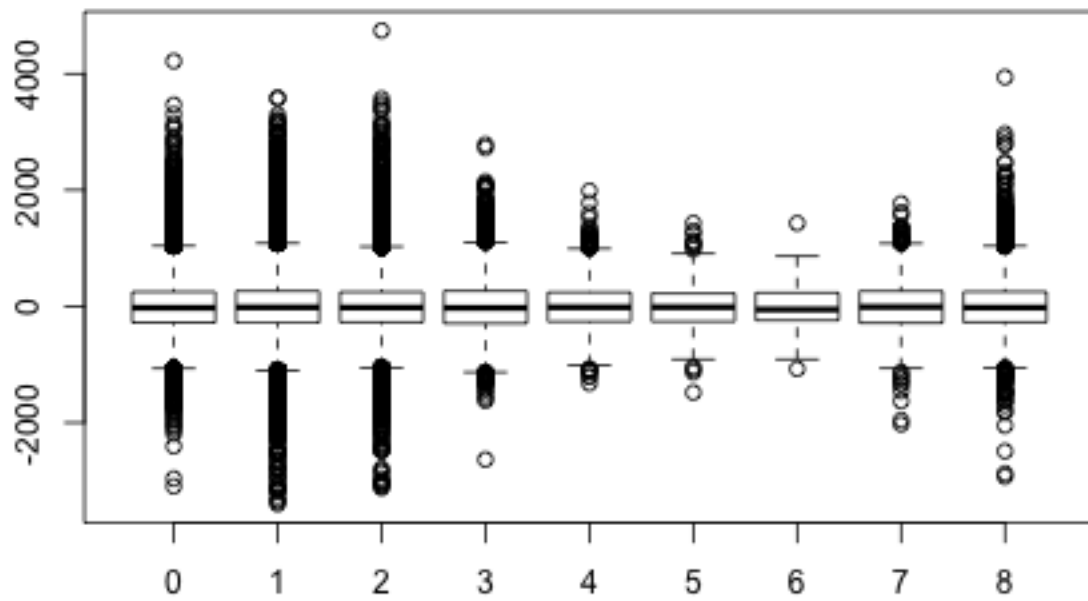
```
plot(births_excl$PARITY_truncated, model4$residuals)
```



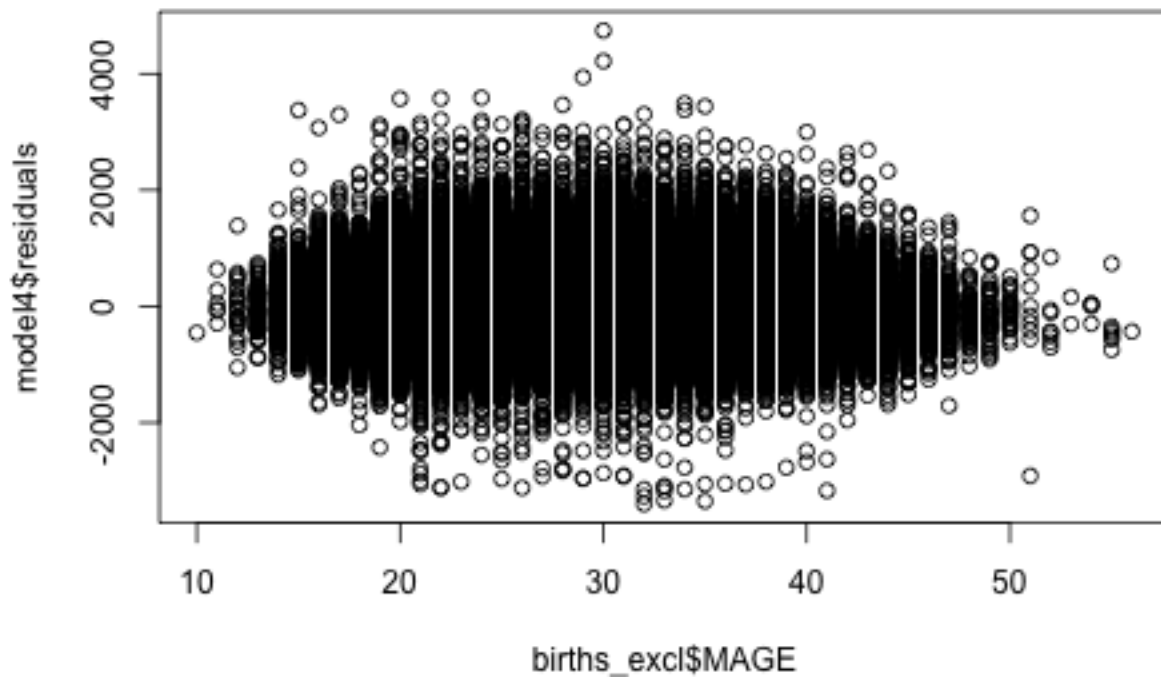
```
plot(births_excl$smoking_type, model4$residuals)
```

```
plot(births_excl$MRACER, model4$residuals)
```



```
plot(births_excl$MAGE, model4$residuals)
```



The addition of the quartic term does not seem to help. The residual vs gestational period graph shows that residuals increase in absolute value as gestational period increases from 20 to 40 weeks. These residuals are much less random than that of model 3.

Model 3 looks like the best, but perhaps we can use robust regression to improve upon this the massive residual of the outlier point near 80 weeks of gestational age.

Robust on Model 3

```
robust1 <- rlm(data = births_excl, BWTG ~ GEST + GEST2 + GEST3 + PARITY_truncated + PLUR_truncated + sm
summary(robust1)
```

```
##
## Call: rlm(formula = BWTG ~ GEST + GEST2 + GEST3 + PARITY_truncated +
##   PLUR_truncated + smoking_type + MAGE + MRACER + mortality,
##   data = births_excl, na.action = "na.exclude")
## Residuals:
```

	Min	1Q	Median	3Q	Max
	-3387.363	-269.680	-7.516	268.801	4917.081

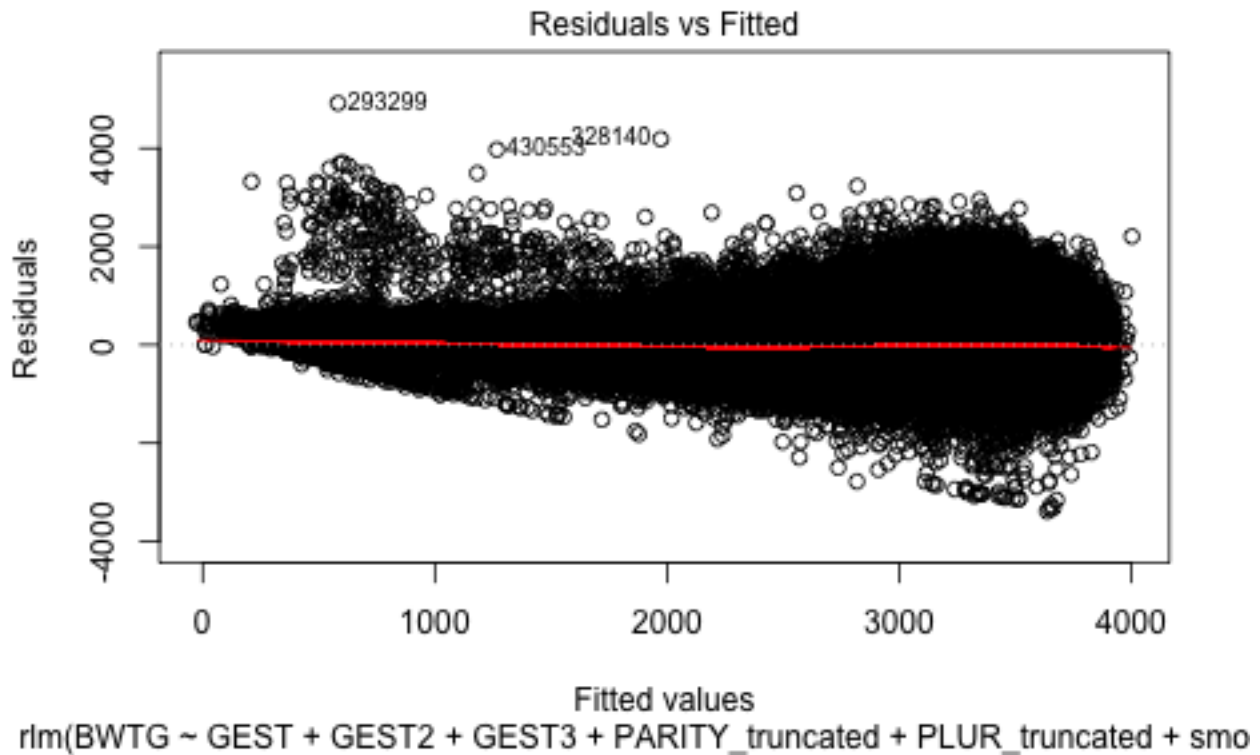
```
##
## Coefficients:
```

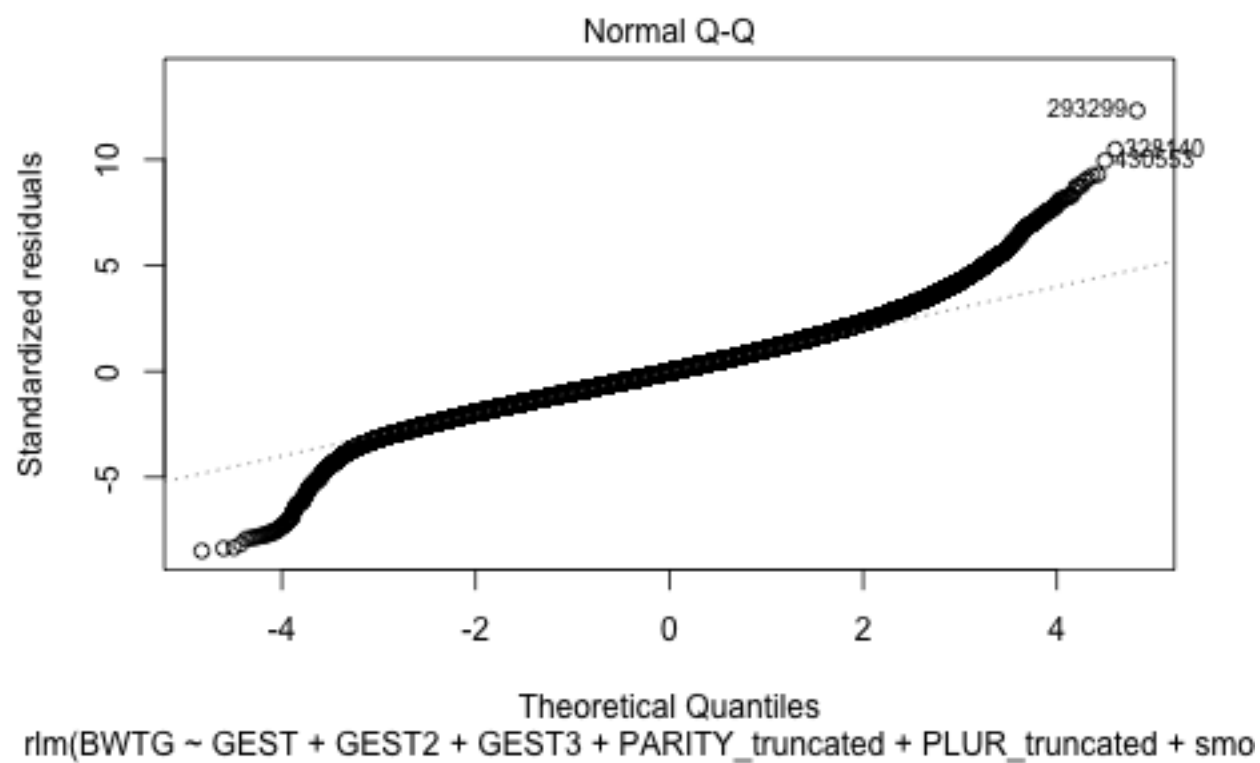
	Value	Std. Error	t value
(Intercept)	15903.5669	182.4842	87.1504
GEST	-1690.4719	17.2605	-97.9388
GEST2	57.4173	0.5325	107.8355
GEST3	-0.5757	0.0054	-107.0707

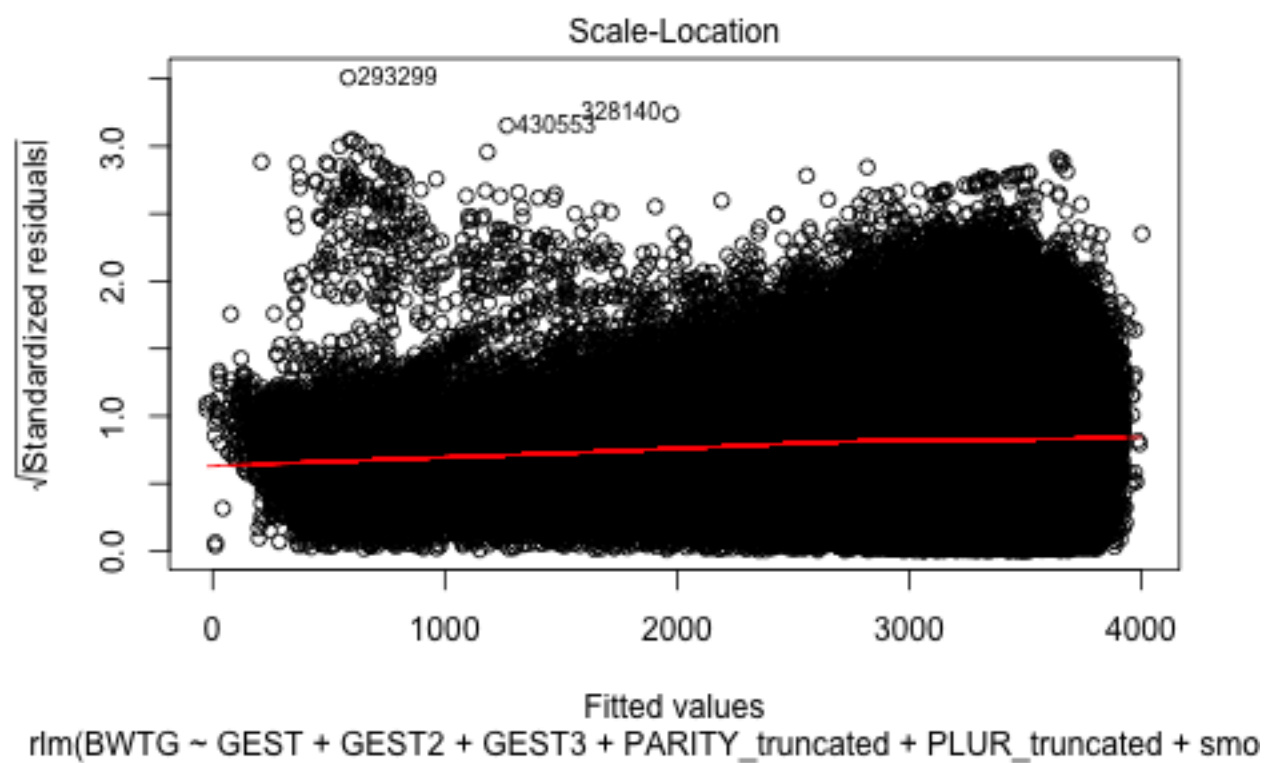
```
## PARITY_truncated2      86.8751      1.2796      67.8930
## PARITY_truncated3     104.1254      1.4955      69.6238
## PARITY_truncated4     109.3099      1.8715      58.4092
## PARITY_truncated5+    109.9214      1.8980      57.9151
## PLUR_truncated2      -312.0635      2.8631    -108.9943
## PLUR_truncated3+     -322.9106     14.9615     -21.5828
## smoking_typebefore and during -202.1493      1.7164    -117.7759
## smoking_typebefore only   -11.6944      2.6205     -4.4627
## smoking_typeduring only  -162.4023      8.8520    -18.3463
## MAGE                   4.4206      0.0935      47.2894
## MRACER1                85.4898      1.6092      53.1254
## MRACER2               -98.5591      1.7654     -55.8286
## MRACER3               -4.5143      4.4368     -1.0175
## MRACER4              -35.0959      7.3709     -4.7614
## MRACER5             -112.9427     17.3957     -6.4926
## MRACER6               27.0106     42.6900      0.6327
## MRACER7              -15.0170      9.1714     -1.6374
## MRACER8             -105.6237      3.1111    -33.9504
## mortality              20.0766      3.0082      6.6740
##
```

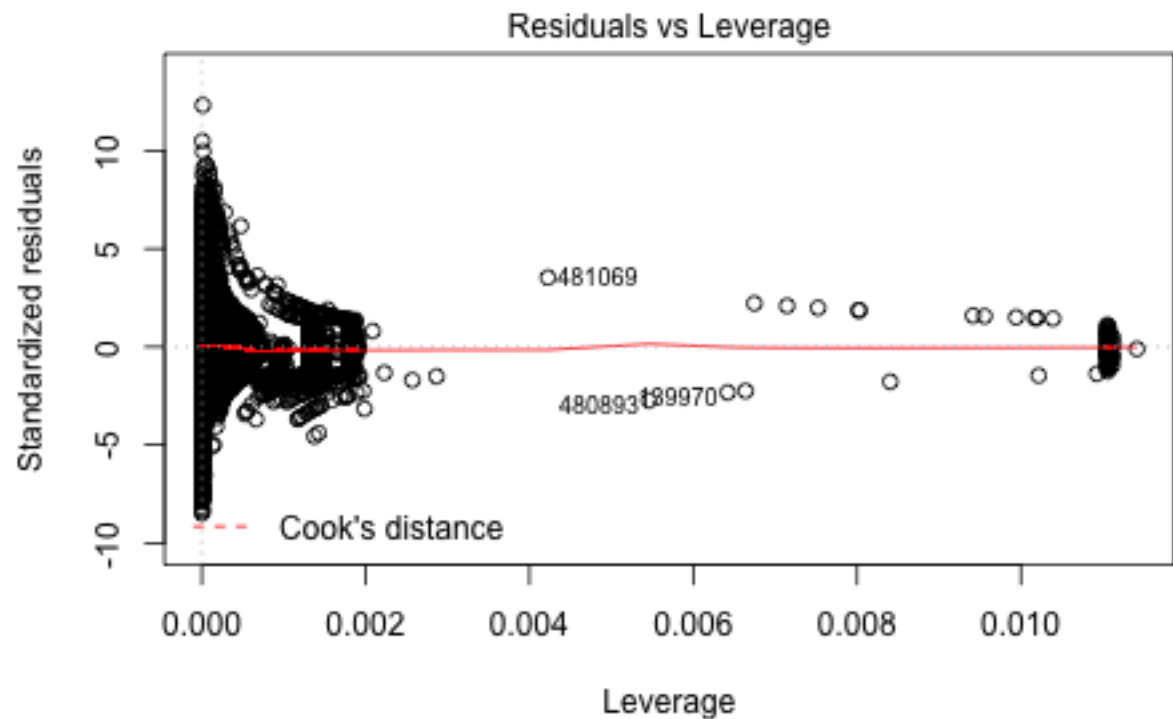
```
## Residual standard error: 399.2 on 717846 degrees of freedom
```

```
plot(robust1)
```



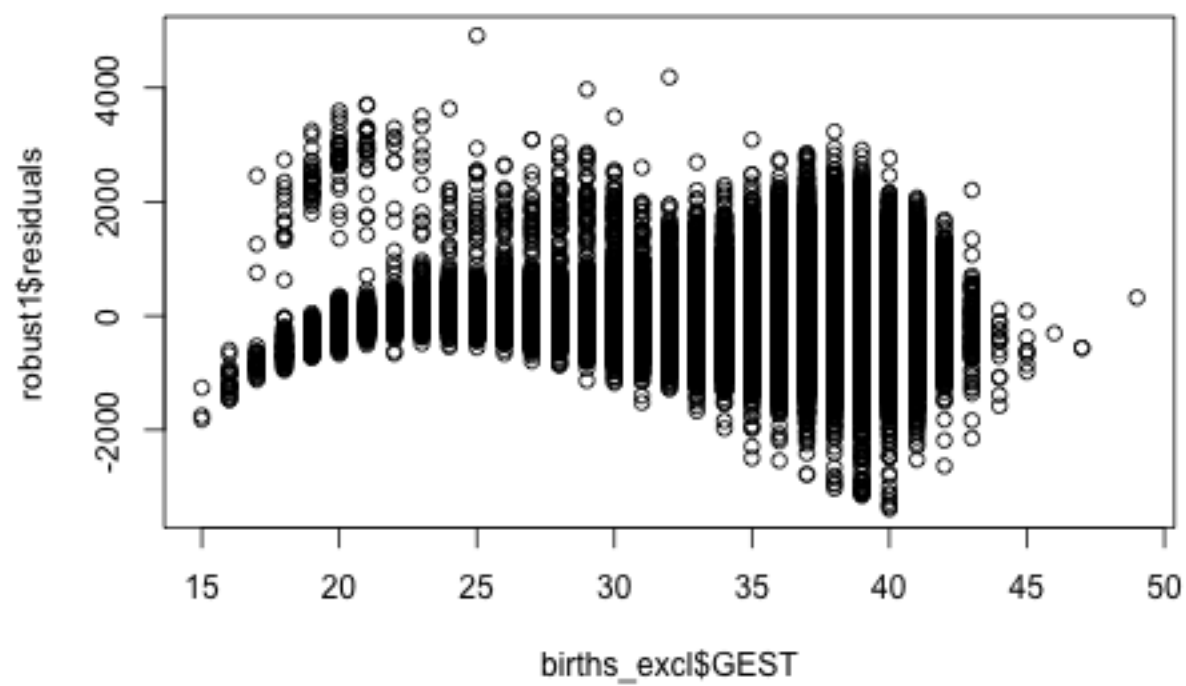




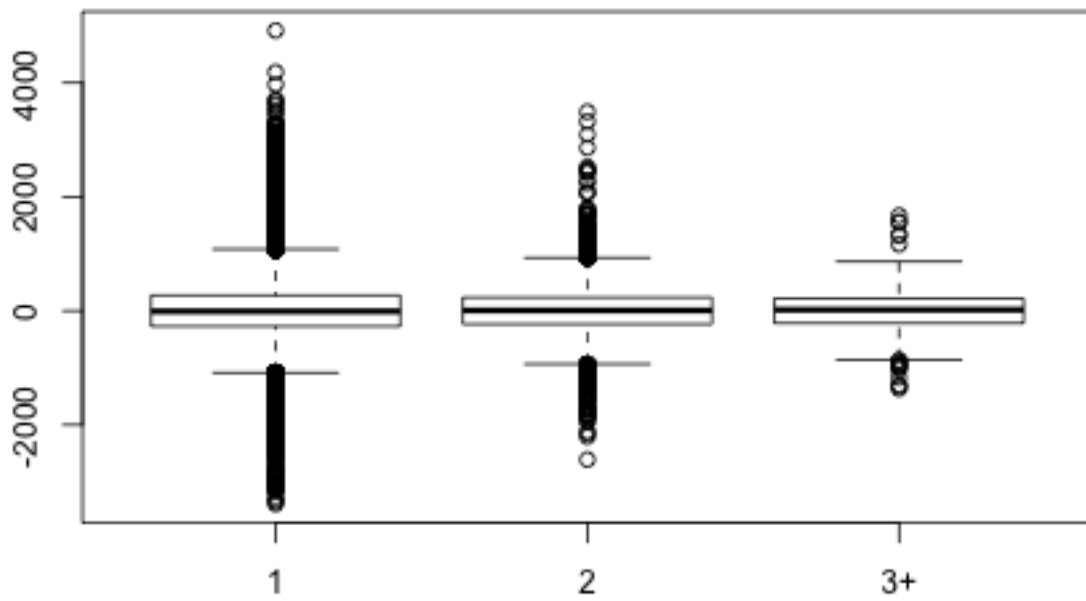


```
rlm(BWTG ~ GEST + GEST2 + GEST3 + PARITY_truncated + PLUR_truncated + smo
```

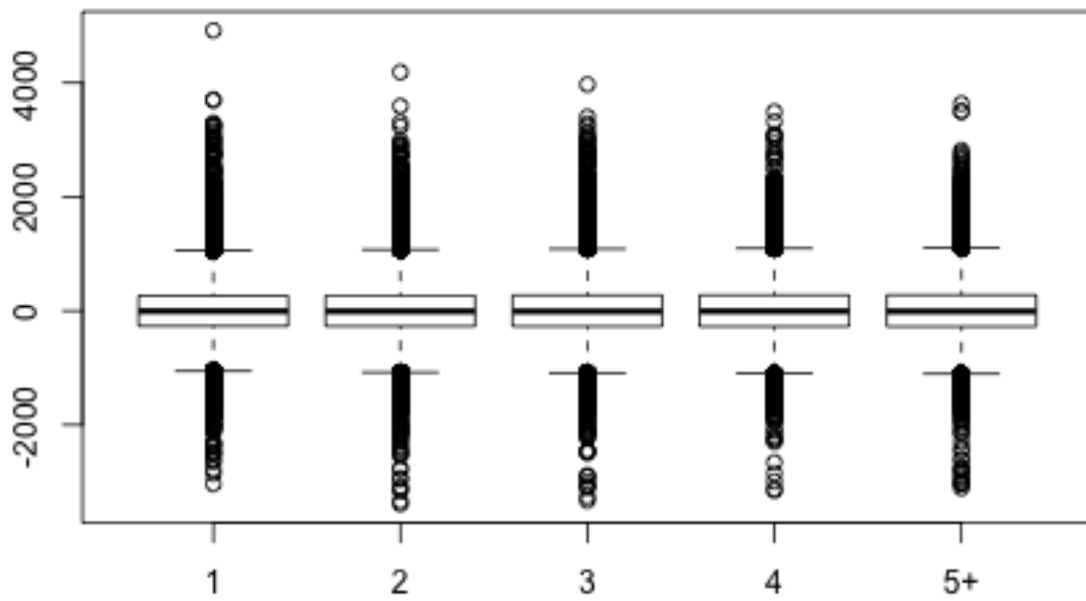
```
# plot(robust1$fitted.values, robust1$residuals)
plot(births_excl$GEST, robust1$residuals)
```



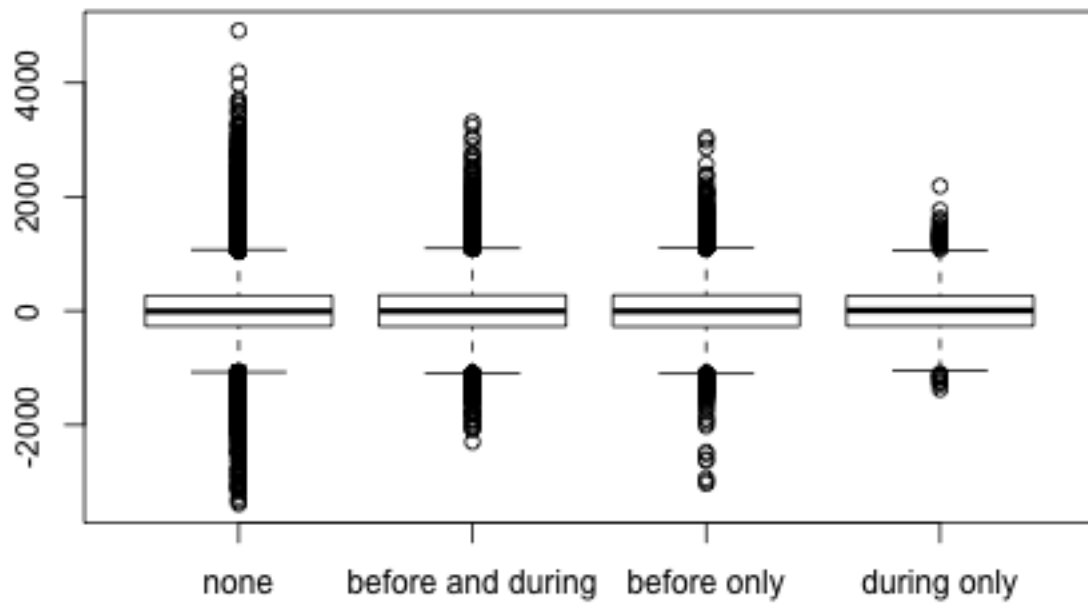
```
plot(births_excl$PLUR_truncated, robust1$residuals)
```

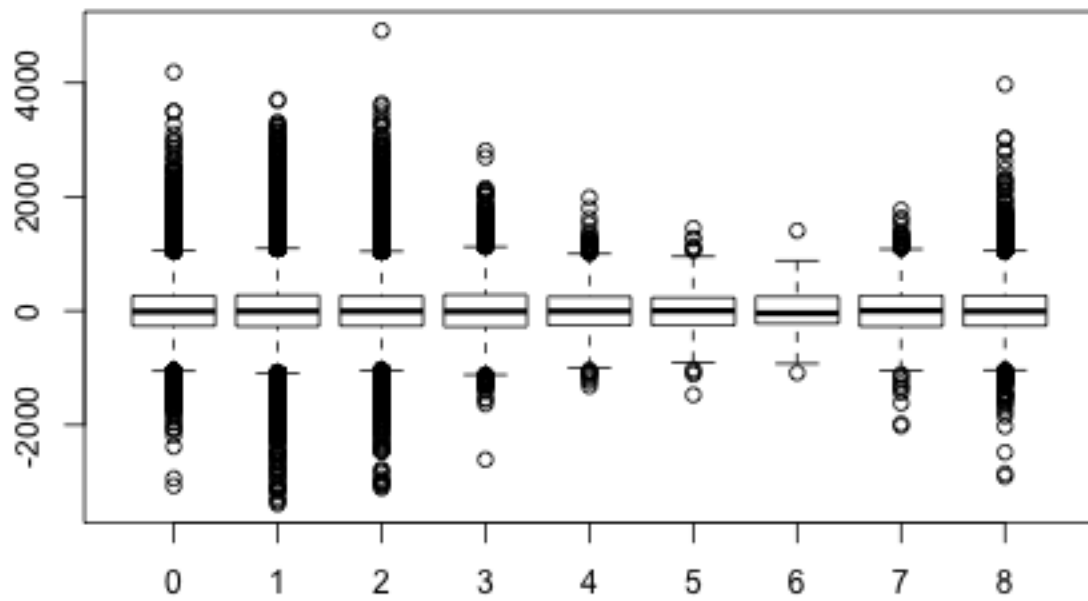
```
plot(births_excl$PARITY_truncated, robust1$residuals)
```



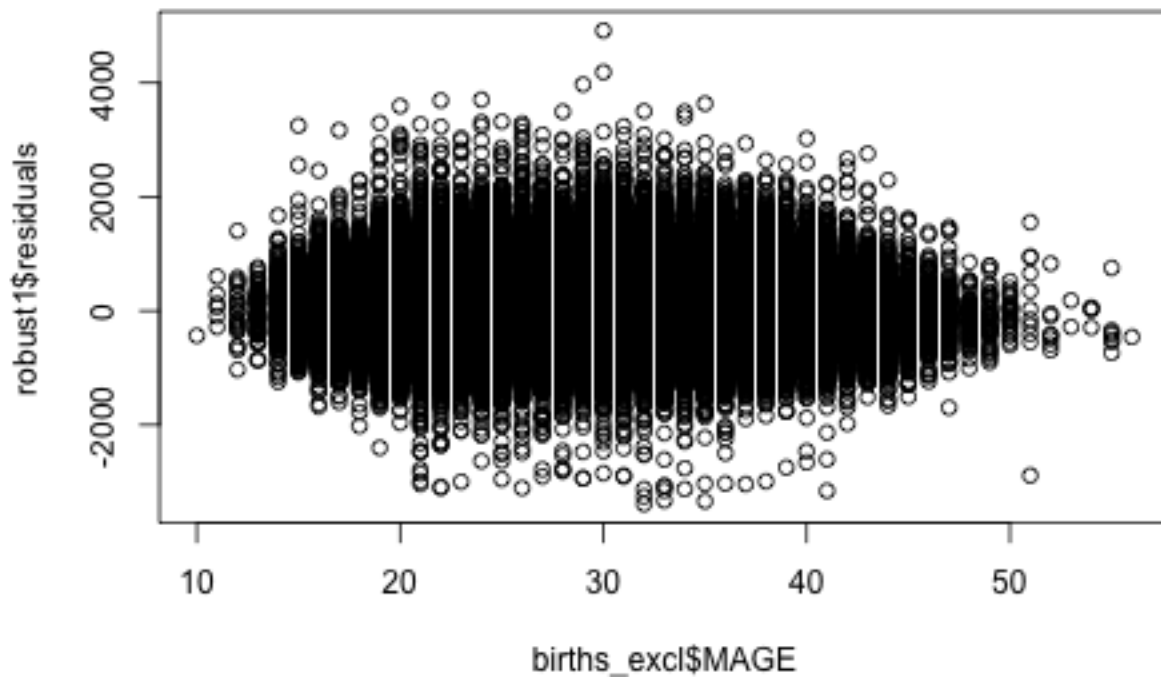
```
plot(births_excl$smoking_type, robust1$residuals)
```



```
plot(births_excl$MRACER, robust1$residuals)
```



```
plot(births_excl$MAGE, robust1$residuals)
```



```
#Check weights
robust1_weights = data.frame(bwt = births_excl$BWTG, gest = births_excl$GEST,
  resid=robust1$resid, weight=robust1$w)
robust1_weights[order(robust1$w)[c(1:5, (length(robust1$w)-5):length(robust1$w))],]
```

```
##      bwt gest      resid      weight
## 293299 5500   25 4917.08114 0.1091945
## 328140 6160   32 4186.78682 0.1282402
## 430553 5239   29 3971.68803 0.1351850
## 98978  4309   21 3704.98342 0.1449236
## 48677  4281   21 3691.28387 0.1454614
## 717861 3289   39  45.42608 1.0000000
## 717862 3770   41  106.21740 1.0000000
## 717863 2872   39 -371.57392 1.0000000
## 717864 3360   38  54.06698 1.0000000
## 717866 3713   40  194.44419 1.0000000
## 717867 3180   39 -283.40570 1.0000000
```

Note: change below to indicate taking out outlier

Checking the weights, the outlier point at gest = 83 with the residual of 57619 has indeed been weighted down (with a weight of 0.0093). The weights of four other points with high residuals are also weighted down.

Looking at the residual plot for gestational period, the residuals look mostly random (ignoring the outlier point at gest = 83).