

# MATH512 - Project 4

Wasif Ahmed, Haoxiang Deng, Jacob Fein-Ashley, Kanav Malhotra, Longzhe Yang

April 2024

## Question 1

Refer to Figure 1

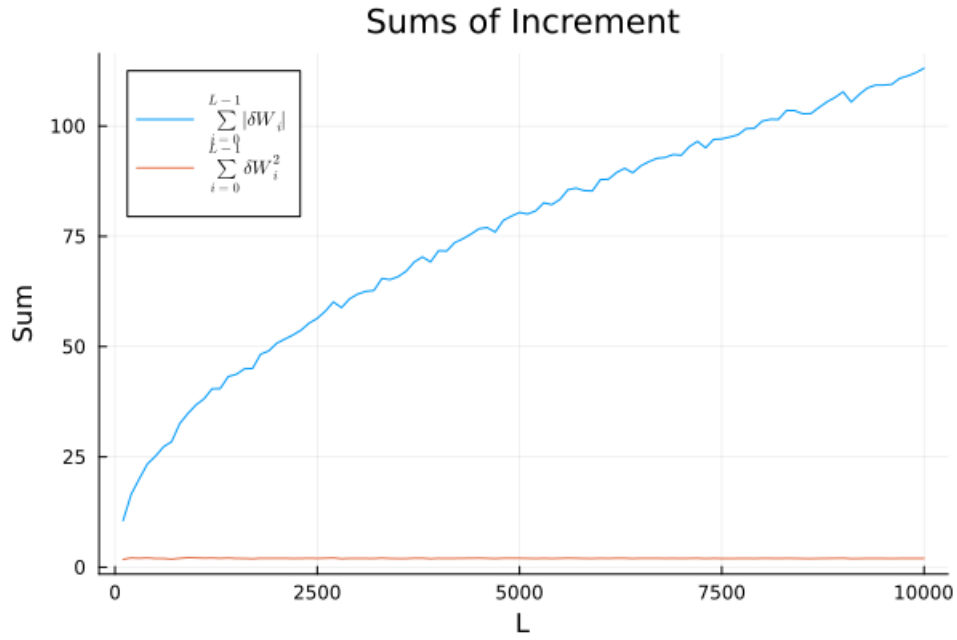


Figure 1: Stochastic Plots

Notice that as the  $L$  parameter increases, the  $|\delta W_i|$  term is unbounded while  $\delta W_i^2$  converges to 2 in probability.

## Question 2

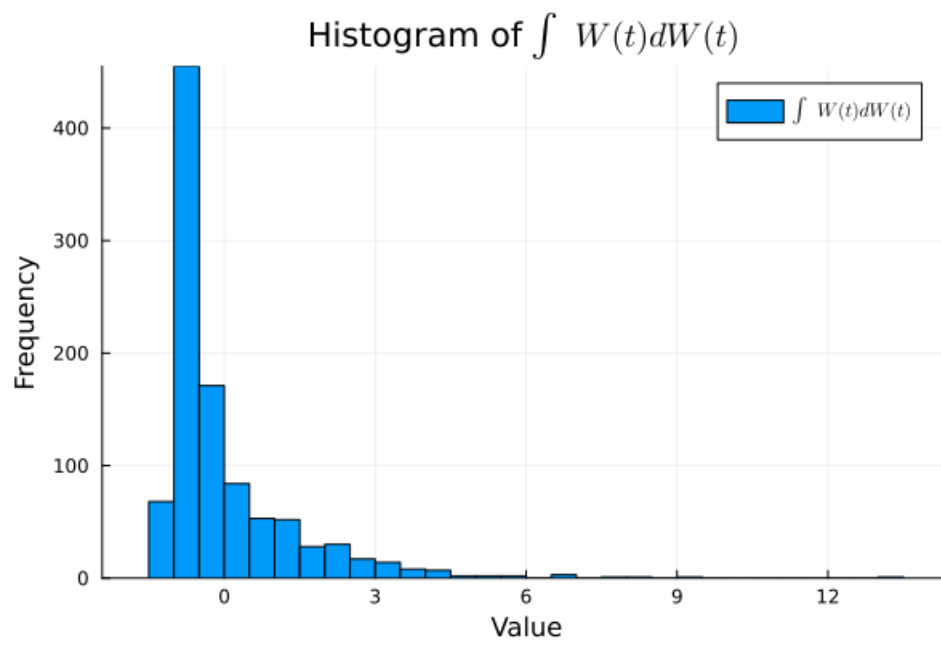


Figure 2: 2a

1.

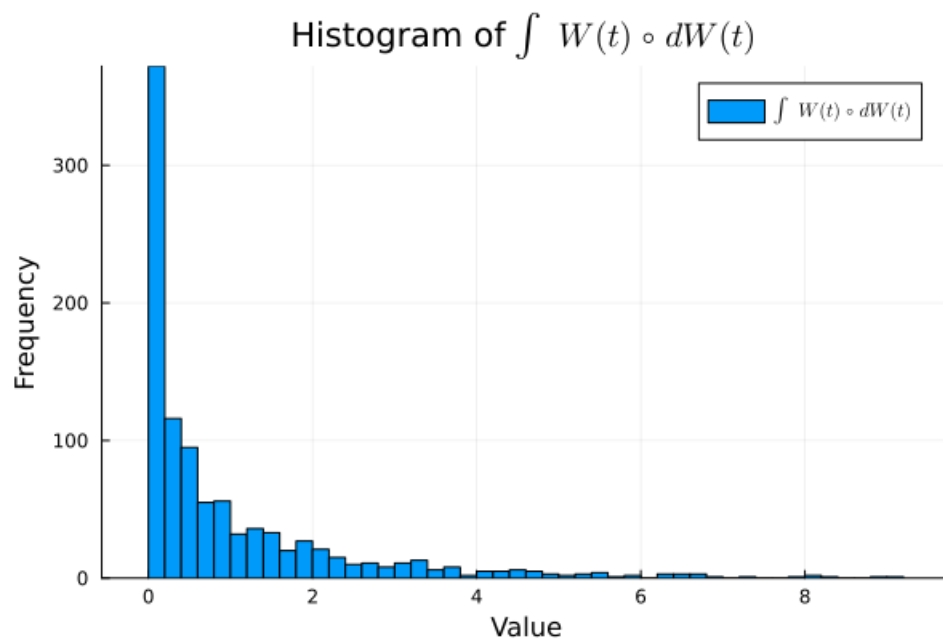


Figure 3: 2b

2.

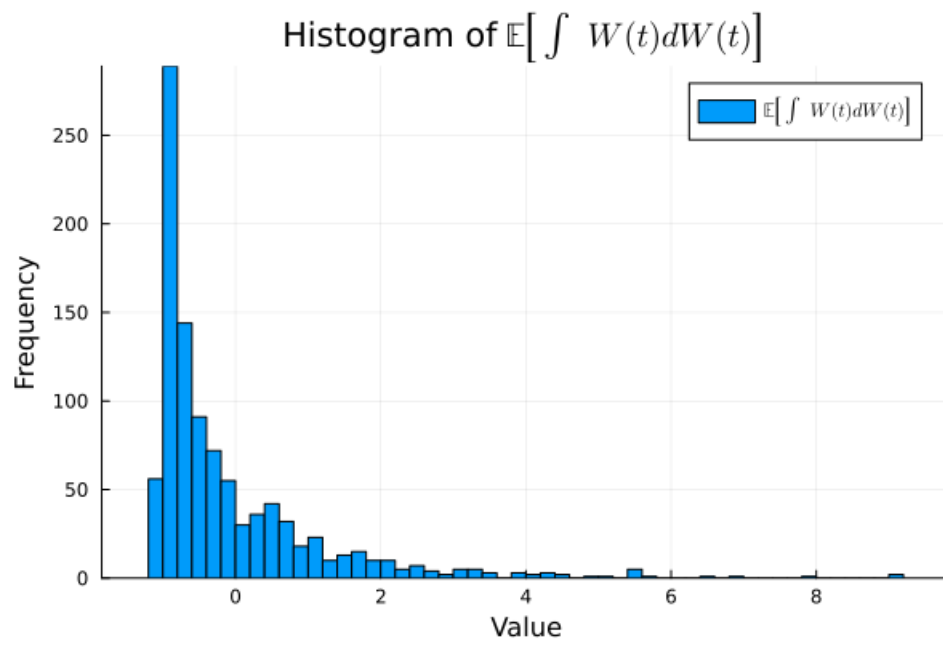


Figure 4: 2c

3.

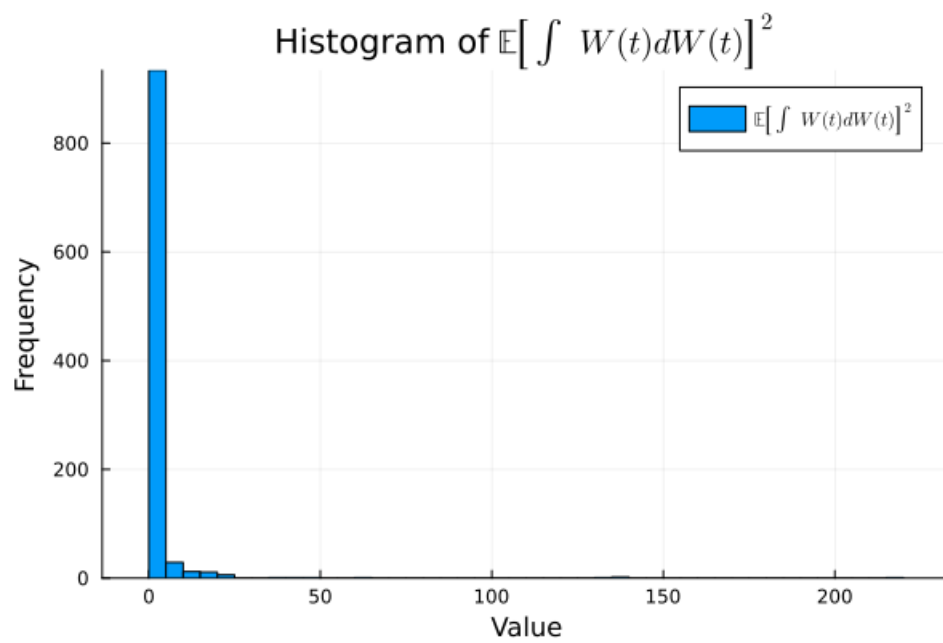


Figure 5: 2d

4.

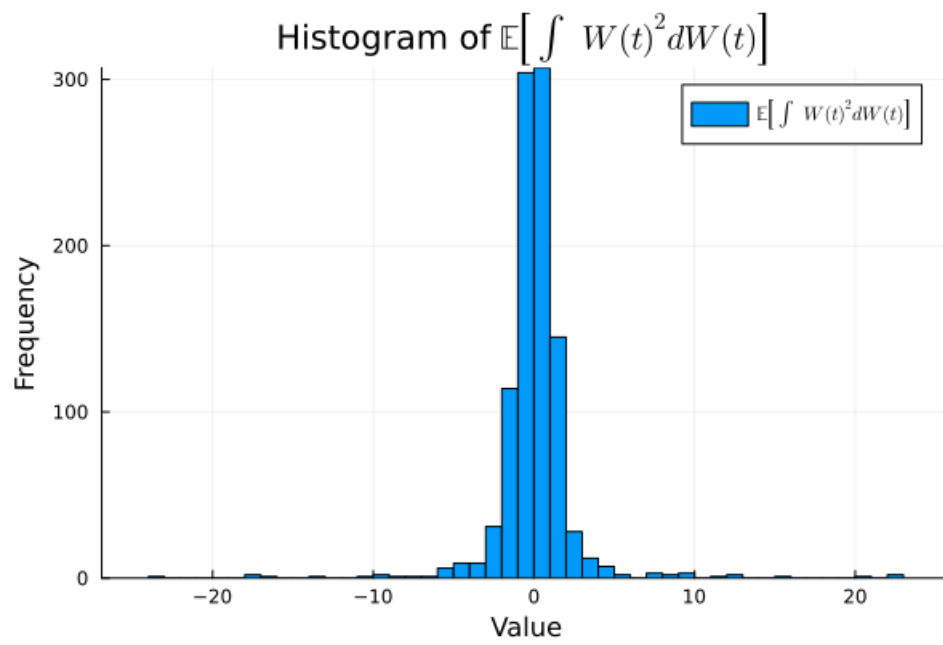


Figure 6: 2e

5.

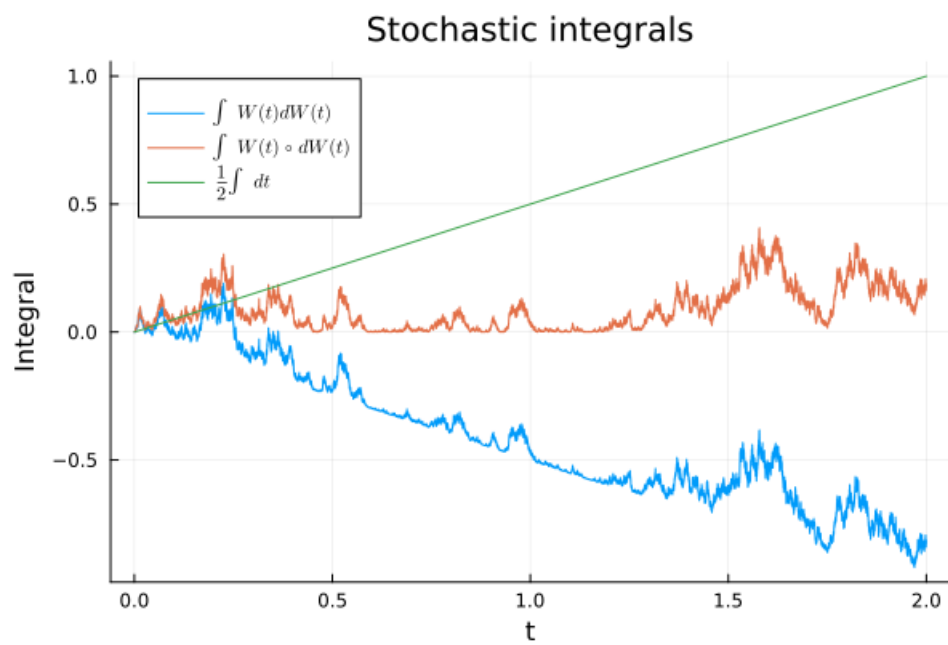


Figure 7: 2f

6.

Question 3

Question 4

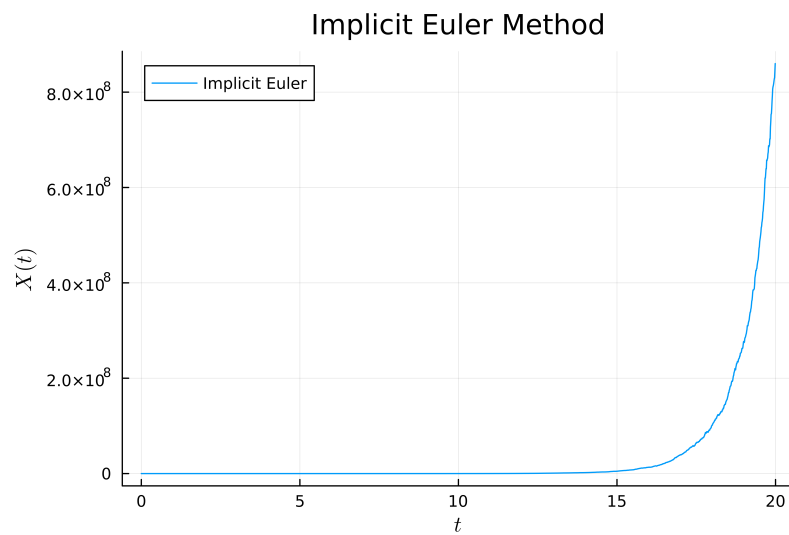


Figure 8: Implicit Euler

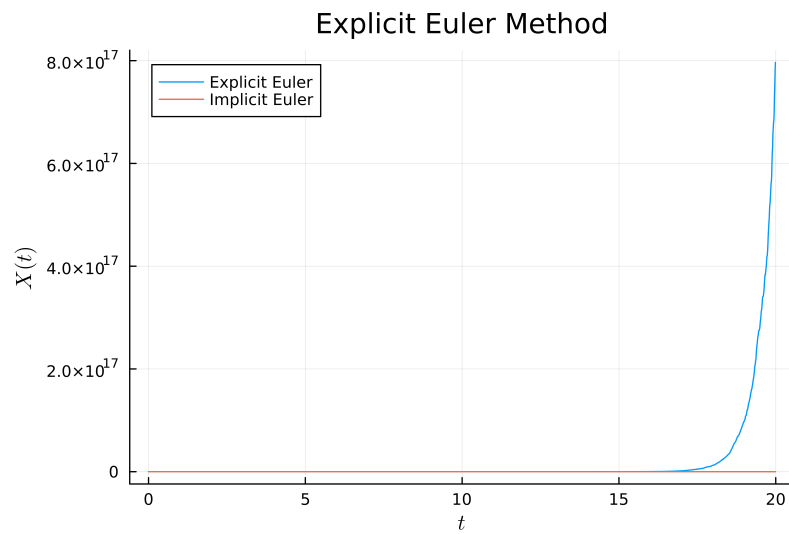


Figure 9: Explicit Euler



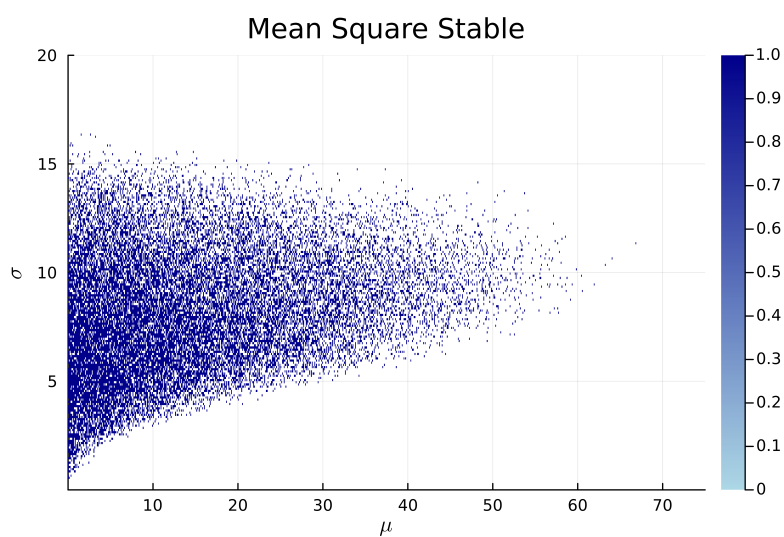


Figure 10: Mean Square Stable Values

## Question 5

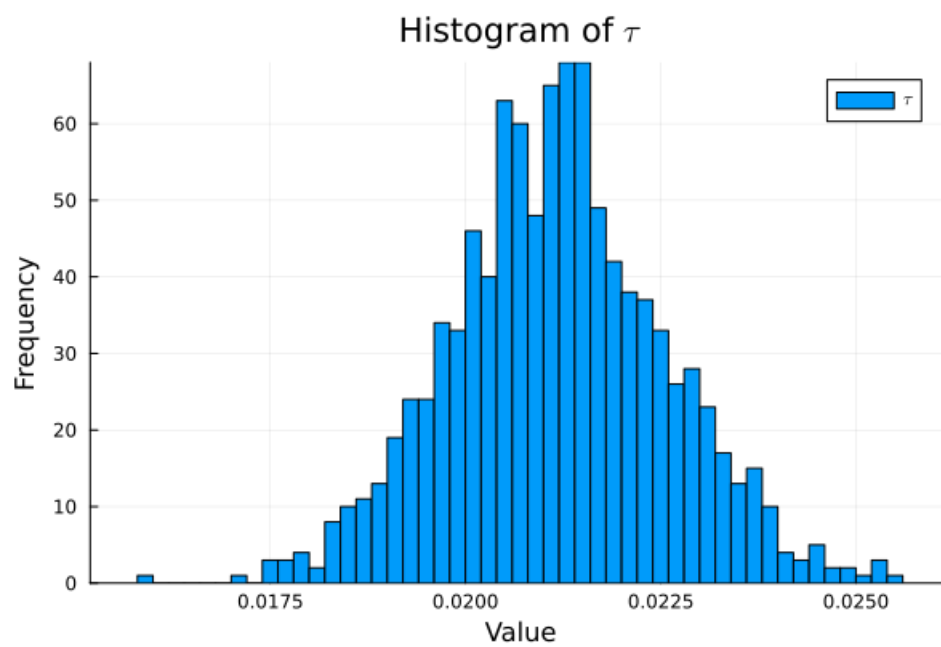


Figure 11: 5