

ASSIGNMENT 04: FUNC OFF

1. Create an `ip` anonymous function that performs the standard inner product over \mathbb{C} and an `ip_norm` anonymous function for its associated L^2 norm.
2. Create a `gram_schmidt` function. The input should be a matrix of linearly independent columns and function handles that define an inner product and norm for the Gram–Schmidt process. The function should return a matrix of orthonormal column vectors.
3. Create an `isorthogonal` function that accepts two vectors and an inner product function handle. The function should return `true` if the vectors are orthogonal and `false` if they are not. Due to the numerical instability of the Gram–Schmidt process, our orthonormal vectors may not be exactly orthogonal. Take this into account by utilizing the `eps` function.
4. Calculate orthonormal vectors from the following orthogonal set:

$$\mathcal{S} = \left\{ \begin{bmatrix} 1 \\ j \\ 2-j \\ -1 \end{bmatrix}, \begin{bmatrix} 2+3j \\ 3j \\ 1-j \\ 2j \end{bmatrix}, \begin{bmatrix} -1+7j \\ 6+10j \\ 11-4j \\ 3+4j \end{bmatrix} \right\} \quad (1)$$

and store them into matrix `U`.

5. Check that the column vectors of `U` are all orthogonal and store the logical value into scalar `orthogonal`.