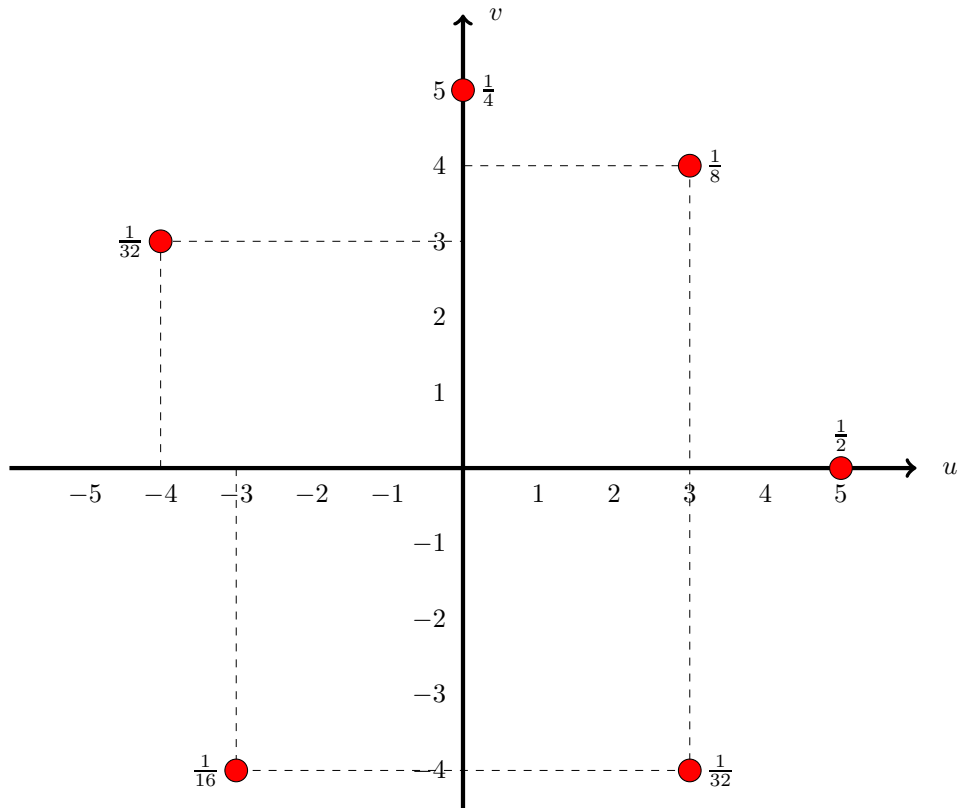
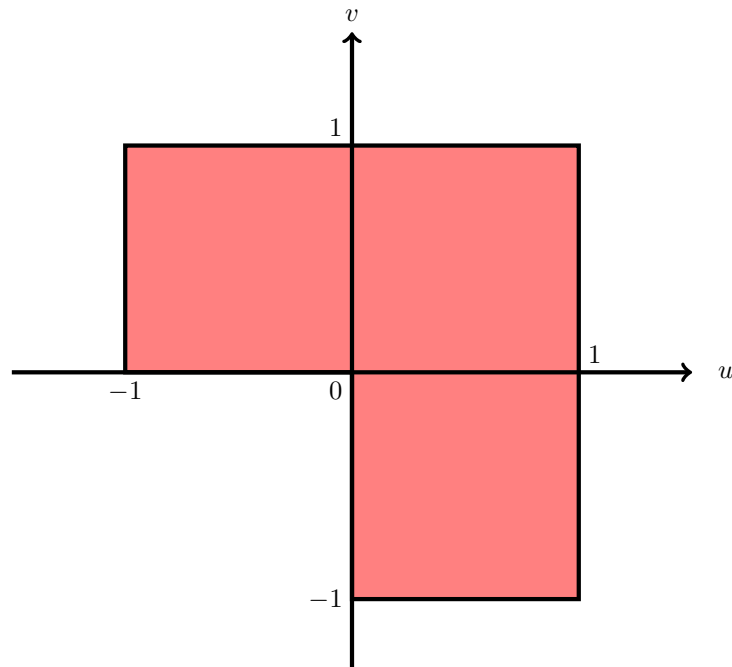


If random variables X and Y have joint probability mass function $p_{X,Y}(u, v)$ shown below (each red dot has integer coordinates), then what is the variance of $3(X^2 + Y^2) - 1$?



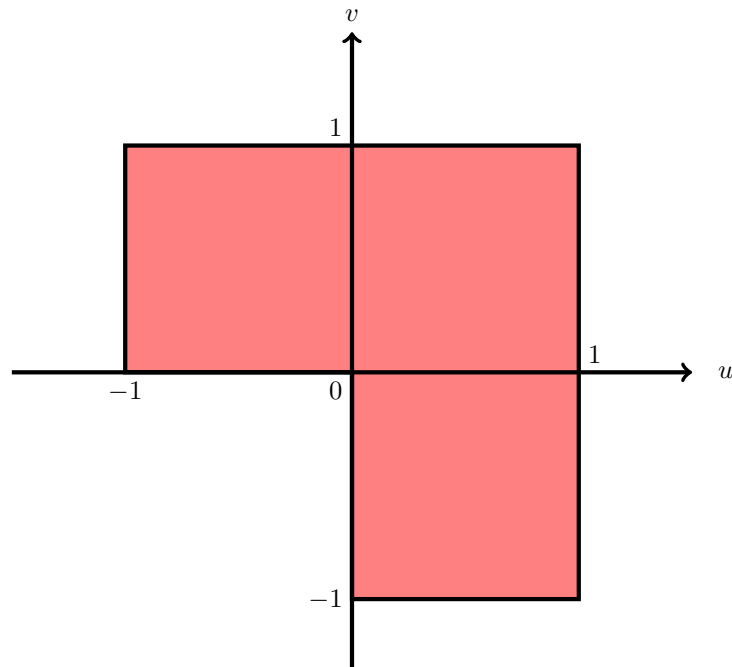
- (a) 0
- (b) 3
- (c) 4
- (d) 5
- (e) 9
- (f) 16
- (g) 25
- (h) $5/2$
- (i) $3/2$
- (j) $9/4$
- (k) $4/9$
- (l) 50
- (m) None of these

Suppose X and Y are random variables whose joint probability density function is uniform in the red region shown below, and zero elsewhere. What is the expected value of XY ?



- (a) $-1/12$
- (b) $1/12$
- (c) $1/6$
- (d) $-1/6$
- (e) $1/3$
- (f) $-1/3$
- (g) $1/2$
- (h) $-1/2$
- (i) $2/3$
- (j) $-2/3$
- (k) 0
- (l) None of these

Suppose X and Y are random variables whose joint probability density function is uniform in the red region shown below, and zero elsewhere. What is the variance of X ?



- (a) $11/36$
- (b) $11/18$
- (c) $1/9$
- (d) $1/3$
- (e) $2/3$
- (f) $5/36$
- (g) $5/18$
- (h) $5/9$
- (i) $1/36$
- (j) $1/6$
- (k) $1/4$
- (l) None of these