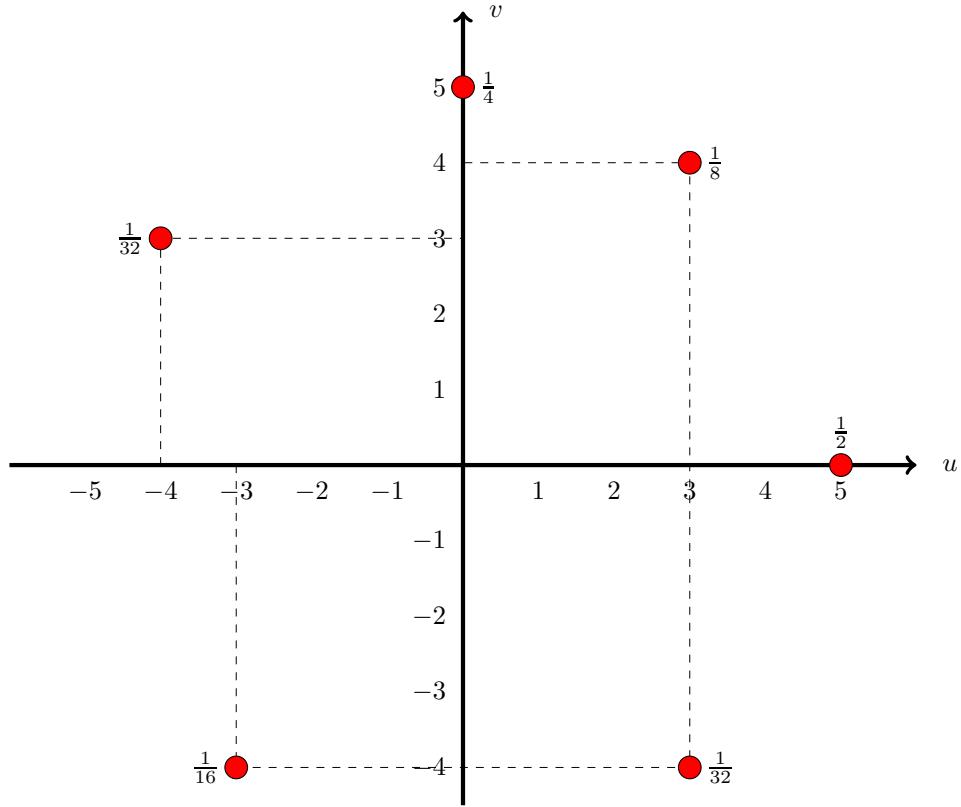
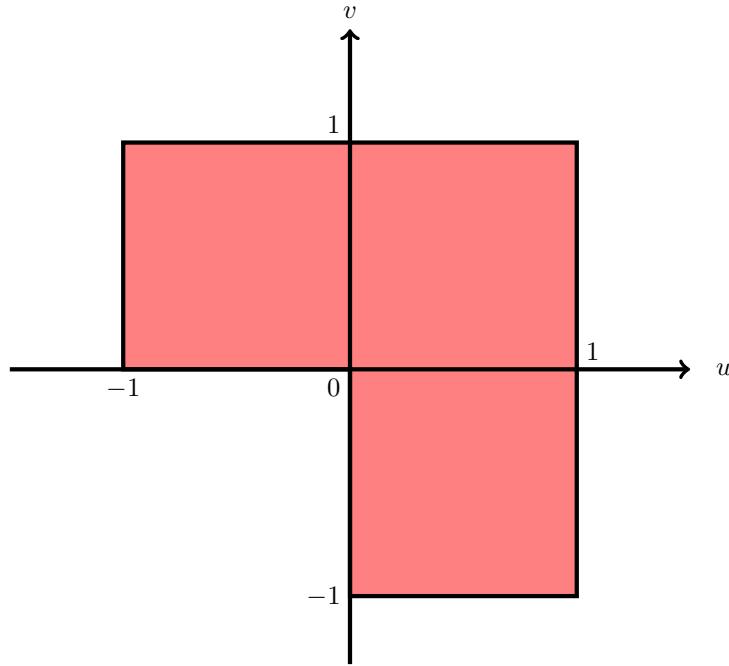


If random variables  $X$  and  $Y$  have joint probability mass function  $p_{X,Y}(u, v)$  shown below (each red dot has integer coordinates), then what is the variance of  $3(X^2 + Y^2) - 1$ ?



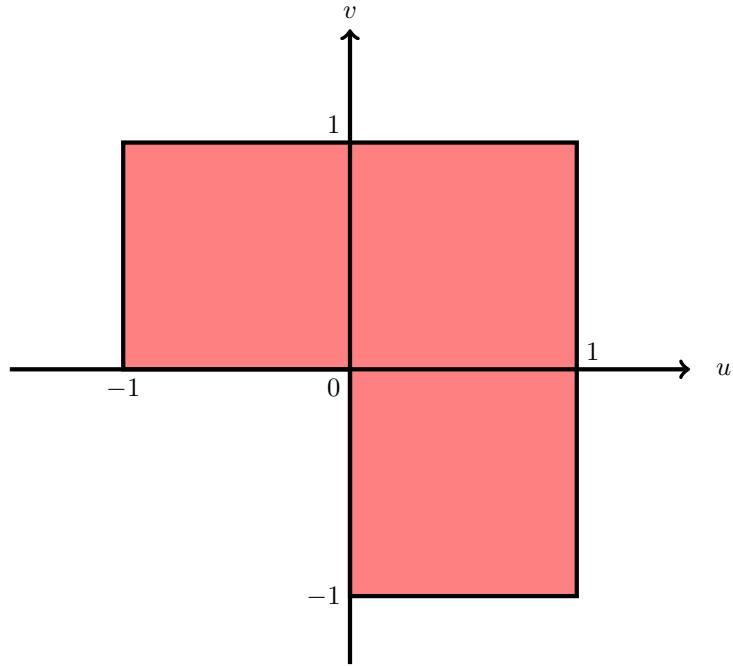
- (a) 0
- (b) 3
- (c) 4
- (d) 5
- (e) 9
- (f) 16
- (g) 25
- (h)  $5/2$
- (i)  $3/2$
- (j)  $9/4$
- (k)  $4/9$
- (l) 50
- (m) None of these

Suppose  $X$  and  $Y$  are random variables whose joint probability density function is uniform in the red region shown below, and zero elsewhere. What is the expected value of  $XY$ ?



- (a)  $-1/12$
- (b)  $1/12$
- (c)  $1/6$
- (d)  $-1/6$
- (e)  $1/3$
- (f)  $-1/3$
- (g)  $1/2$
- (h)  $-1/2$
- (i)  $2/3$
- (j)  $-2/3$
- (k)  $0$
- (l) None of these

Suppose  $X$  and  $Y$  are random variables whose joint probability density function is uniform in the red region shown below, and zero elsewhere. What is the variance of  $X$  ?



- (a)  $11/36$
- (b)  $11/18$
- (c)  $1/9$
- (d)  $1/3$
- (e)  $2/3$
- (f)  $5/36$
- (g)  $5/18$
- (h)  $5/9$
- (i)  $1/36$
- (j)  $1/6$
- (k)  $1/4$
- (l) None of these