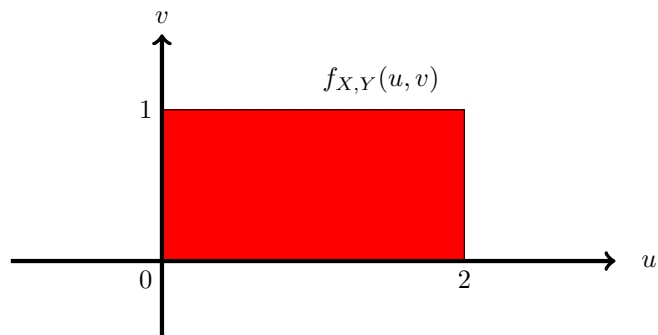


Suppose the joint probability mass function of random variables  $X$  and  $Y$  is  $p_{X,Y}(u,v) = 2^{-(u+v)}$  whenever  $u$  and  $v$  are both positive integers, and is zero otherwise. What is the probability that  $Y + (X - 2)^2$  is greater than or equal to two?

- (a)  $7/8$
- (b)  $1/2$
- (c)  $1/4$
- (d)  $1/8$
- (e)  $1/16$
- (f)  $3/4$
- (g)  $15/16$
- (h)  $3/8$
- (i)  $3/16$
- (j)  $5/16$
- (k)  $7/16$
- (l) None of these

If random variables  $X$  and  $Y$  have a joint pdf equal to  $f_{X,Y}(u,v) = uv$  in the red rectangle in the figure below and which is zero elsewhere, then what is the probability that  $X$  is less than one?



- (a)  $1/4$
- (b)  $1/2$
- (c)  $1/8$
- (d)  $1/16$
- (e)  $1/3$
- (f)  $2/3$
- (g)  $3/4$
- (h)  $3/8$
- (i)  $3/16$
- (j)  $5/16$
- (k)  $5/8$
- (l) None of these

If  $X$  is a random variable that is uniform on  $[0, 3]$  and  $Y = e^X$ , then what is the pdf value  $f_Y(8)$ ?

- (a)  $1/24$
- (b)  $1/8$
- (c)  $1/3$
- (d)  $1/4$
- (e)  $1/12$
- (f)  $(\ln 8)/8$
- (g)  $(3 \ln 8)/8$
- (h)  $(\ln 8)/24$
- (i)  $e^8$
- (j)  $\ln 8$
- (k)  $e^3$
- (l) None of these