

Suppose the possible outcomes of an experiment are  $\frac{1}{15}, \frac{2}{15}, \frac{1}{5}, \frac{4}{15}, \frac{1}{3}$ , whose probabilities are  $\frac{1}{16}, \frac{1}{16}, \frac{1}{8}, \frac{1}{4}, \frac{1}{2}$ , respectively. How many different events have a probability less than  $1/2$  ?

- (a) 15
- (b) 0
- (c) 1
- (d) 2
- (e) 3
- (f) 4
- (g) 8
- (h) 16
- (i) 32
- (j) 7
- (k) 31
- (l) None of these

Suppose an experiment has sample space  $S = \{a, b, c\}$ . Define the three events  $E = \{a, b\}$ ,  $F = \{b, c\}$ , and  $G = \{a, c\}$ . If the probability that event  $G$  and event  $E \cup F$  both occur is  $3/4$ , and the probability that  $EF$  occurs is twice the probability that  $FE^cG$  occurs, then what is the probability the experiment's outcome is  $c$ ?

- (a)  $1/8$
- (b)  $3/8$
- (c)  $3/4$
- (d)  $1/4$
- (e)  $1/2$
- (f)  $0$
- (g)  $5/8$
- (h)  $1/3$
- (i)  $2/3$
- (j)  $7/8$
- (k)  $3/16$
- (l) None of these

Suppose  $E$ ,  $F$ , and  $G$  are events in a sample space  $S$ . If  $E - F$  and  $G - F$  both occur, but  $(E \cup F \cup G)^c$  does not occur, then which of the following events also must occur?

- (a)  $E(F \cup G)$
- (b)  $EFG$
- (c)  $FG$
- (d)  $FG^c$
- (e)  $F - E$
- (f)  $E^cFG$
- (g)  $E^cF^cG$
- (h)  $E^cG$
- (i)  $E^c \cup G^c$
- (j)  $S^c$
- (k) None of these