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Program: DfsSort.java

Theoretical worst-case running time is $\Theta(n^2)$. The reason for this is the algorithm would need to scan each edge for every vertex in the worst case, so it would perform n^2 checks.

The following are average run times and count for 5,6,7, and 10 nodes.

Nodes	ns	ns	ns	ns	ns	avg(ns)
5	24803	24804	23948	24804	24804	24632.6
6	28653	26086	42338	26514	26942	30106.6
7	46614	30791	29508	28653	28225	32758.2
10	42337	41482	64148	41055	41482	46100.8

Table 1: Run time for DFS sort

Nodes	Count
5	35
6	47
7	70
10	130

Table 2: Count for DFS

Looking at figure 1, which is the count results, it proves that the class of efficiency is $\Theta(n^2)$, using the line of best fit.

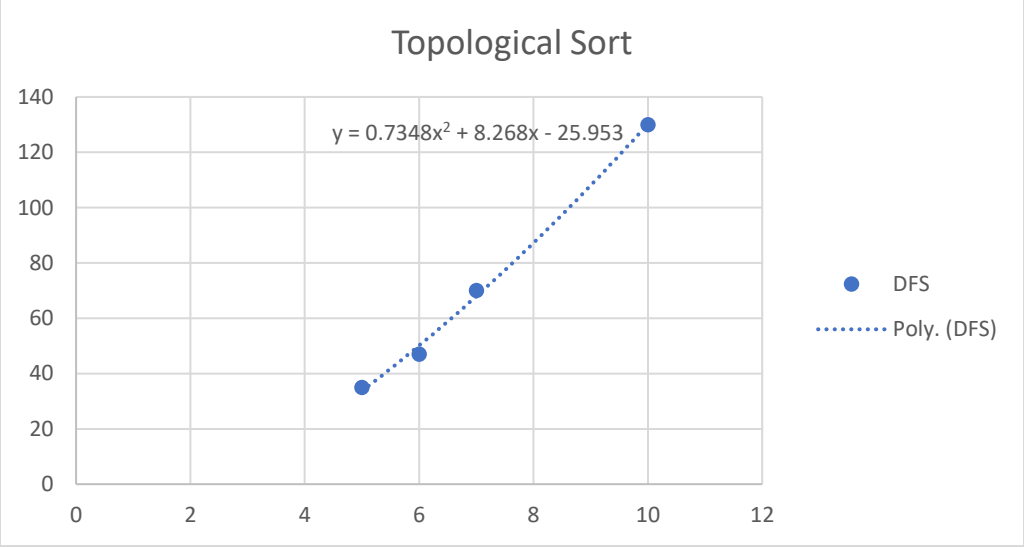

Figure 1: DFS (counts)

Program: SourceRemoval.java

Theoretical worst-case running time is $\Theta(n^3)$. The reason for this is in the worst case the algorithm finds the source at the end of the matrix. This requires n^2 checks. Once this row and column are removed you are left with $(n-1)^2$ and then $(n-2)^2$ checks and so on. This leads to $1^2+2^2+3^2+...+n^2 = n(n+1)(2n+1)/6$. From that it is found this algorithm runs in $\Theta(n^3)$.

The following are average run times and count for 5,6,7, and 10 nodes.

Nodes	ns	ns	ns	ns	ns	avg(ns)
5	13258	20527	16679	15823	12830	15823.4
6	11974	19672	20954	16679	11974	16250.6
7	17106	17106	20099	19244	16251	17961.2
10	26087	28226	32074	41482	47042	34982.2

Table 1: Run time for Source removal sort

Nodes	Count
5	25
6	36
7	55
10	132

Table 2: Count for source removal

Looking at the figure 2, which the graph of the count results it proves that the class of efficiency is $\Theta(n^3)$, using the line of best fit.

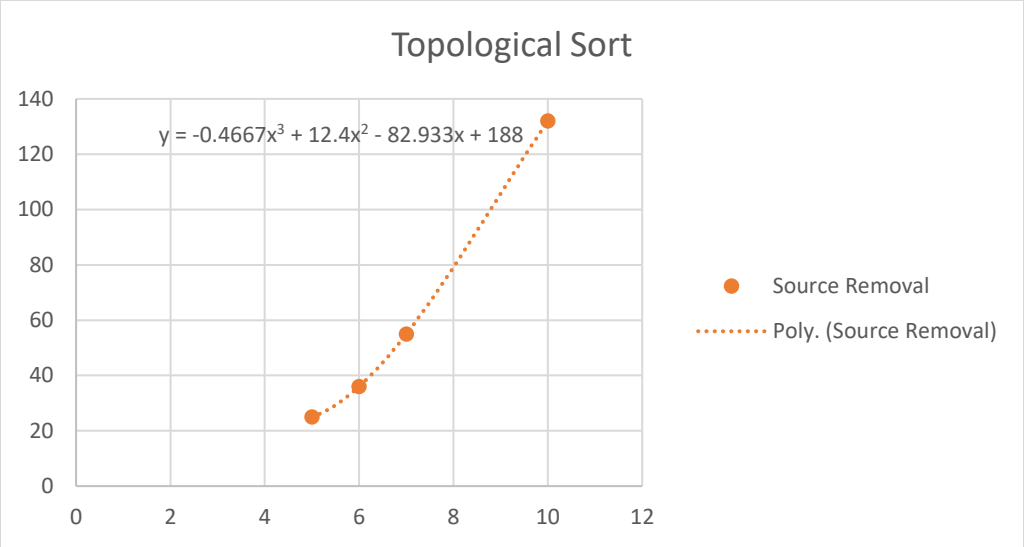

Figure 2: Source Removal (counts)

The faster algorithm is source removal when number of nodes is less than 10. If you look at figure 3 of the counts for these two algorithms you can see that source removal starts off with a smaller count and takes less time, if you compare run times from table 1 and table 3. However, as number of nodes increases the difference becomes less and less until number of nodes hits 10. Then the count becomes greater for source removal. So, dfs sort becomes the faster algorithm. This is backed up by the theoretical worst-case because dfs has a better class of efficiency than source removal.

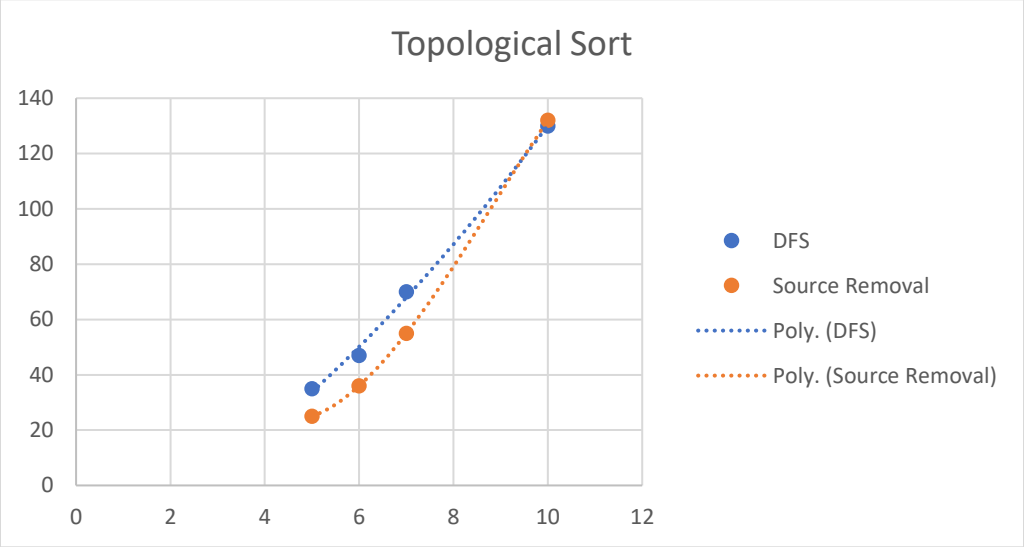

Figure 3: DFS vs Source Removal (counts)